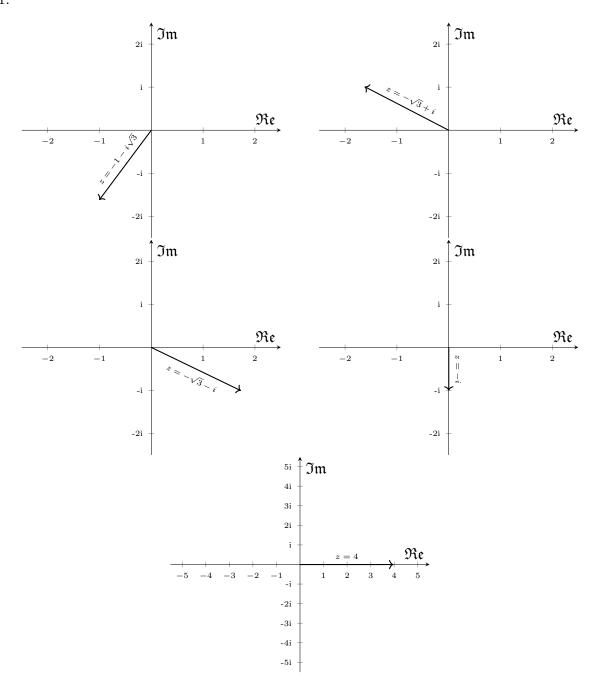


1.



(a)
$$\Re \epsilon z = -1$$
, $\Im m z = -\sqrt{3}$, $|z| = 2$, $\arg z = \arctan \frac{-\sqrt{3}}{-1} - \pi = -\frac{2\pi}{3}$, $z = 2\left(\cos -\frac{2\pi}{3} + i\sin -\frac{2\pi}{3}\right)$, $z = 2e^{-\frac{2\pi}{3}i}$

(b)
$$\Re e z = -\sqrt{3}$$
, $\Im m z = 1$, $|z| = 2$, $\arg z = \arctan \frac{1}{-\sqrt{3}} + \pi = \frac{5\pi}{6}$, $z = 2\left(\cos \frac{5\pi}{6} + i\sin \frac{5\pi}{6}\right)$, $z = 2e^{\frac{5\pi}{6}i}$

(c)
$$\Re \varepsilon z = \sqrt{3}$$
, $\Im m z = -1$, $|z| = 2$, $\arg z = \arctan \frac{-1}{\sqrt{3}} = -\frac{\pi}{6}$, $z = 2\left(\cos -\frac{\pi}{6} + i\sin -\frac{\pi}{6}\right)$, $z = 2e^{-\frac{\pi}{6}i}$

(d)
$$\Re \varepsilon z = 0$$
, $\Im m z = -1$, $|z| = 1$, $\arg z = \arctan -\frac{1}{0} = -\frac{\pi}{2}$, $z = \left(\cos -\frac{\pi}{2} + i\sin -\frac{\pi}{2}\right)$, $z = e^{-\frac{\pi}{2}i}$

(e)
$$\Re \varepsilon z = 4$$
, $\Im m z = 0$, $|z| = 4$, $\arg z = \arctan \frac{0}{4} = 0$, $z = 4(\cos 0 + i \sin 0)$, $z = 4e^{0 \cdot i}$

2. (a)
$$z = 2 \pm 5i$$
, $|z| = \sqrt{29}$, $\arg z = \arctan \pm \frac{5}{2}$

(b)
$$z = -2 \pm 5i$$
, $|z| = \sqrt{29}$, $\arg z = \arctan \mp \frac{5}{2} \pm \pi$

(c)
$$z = ib, b \in \mathbb{R}, b \neq 0, \quad |z| = |b|, \quad \arg z = \arctan \frac{b}{0} = \pm \frac{\pi}{2}$$

(d)
$$z = e^{-5i}$$
, $|z| = 1$, $\arg z = -5 + 2\pi$

3.
$$z = \frac{5+i}{1+2i} = \frac{7-9i}{5} = \frac{7}{5} - \frac{9}{5}i$$
, $\Re \epsilon z = \frac{7}{5}$, $\Im mz = -\frac{9}{5}$

4.
$$x(1-2i)+y(2i-3) = 4-8i$$
, $x-2ix+2iy-3y = 4-8i$, $(x-3y)+i(-2x+2y) = 4-8i$, $\begin{cases} x-3y=4\\ -8=-2x+2y \end{cases}$, $\begin{cases} y=0\\ x=4 \end{cases}$

5.
$$z_1 = 1 - 2i, z_2 = -2 + i$$

$$z_1 + z_2 = (1-2) + i(-2+1) = -1 - i$$

$$z_1 - z_2 = (1+2) + i(-2-1) = 3 - 3i$$

$$z_1 \cdot z_2 = -2 + 2 + i(1+4) = 5i$$

$$\frac{z_1}{z_2} = \frac{1-2i}{-2+i} \cdot \frac{-2-i}{-2-i} = \frac{-4+3i}{5} = -\frac{4}{5} + \frac{3}{5}i$$

6.
$$z_1 = 3 + 3i$$
, $z_2 = -\frac{1}{2} - i\frac{\sqrt{3}}{2}$, $z_3 = 2\sqrt{3} - 2i$, $|z_1| = \sqrt{3^2 + 3^2} = 3\sqrt{2}, |z_2| = \sqrt{\frac{1}{4} + \frac{3}{4}} = 1, |z_3| = \sqrt{4 \cdot 3 + 4} = 4$, $\arg z_1 = \arctan \frac{3}{3} = \frac{\pi}{4}, \arg z_2 = \arctan \frac{\sqrt{3}}{2} \cdot 2 - \pi = -\frac{2\pi}{3}, \arg z_3 = -\frac{2}{2\sqrt{3}} = -\frac{\pi}{6}$

$$z_1 = 3\sqrt{2} \left(\cos \frac{\pi}{4} + i \sin \frac{\pi}{4}\right), \quad z_2 = \cos -\frac{2\pi}{3} + i \sin -\frac{2\pi}{3}, \quad z_3 = 4 \left(\cos -\frac{\pi}{6} + i \sin -\frac{\pi}{6}\right)$$

$$z_1 \cdot z_2 = 3\sqrt{2} \left(\cos -\frac{5\pi}{12} + i \sin -\frac{5\pi}{12}\right), \frac{z_1 \cdot z_2}{z_3} = \frac{3\sqrt{2}}{4} \left(\cos -\frac{\pi}{4} + i \sin -\frac{\pi}{4}\right) = \frac{3\sqrt{2}}{4} \cdot \frac{\sqrt{2}}{2} - \frac{3\sqrt{2}}{4} \cdot \frac{\sqrt{2}}{2}i = \frac{3}{4} - \frac{3}{4}i$$

7. z = iy, y < 0

