

Бекешева Анастасія ФІ-12

$$\begin{aligned}x &= A_0 e^{-\beta t} \cos(\omega t), & v &= \int A_0 e^{-\beta t} \cos(\omega t) dt = \\&= \frac{1}{\omega^2 + \beta^2} A_0 e^{-\beta t} (\omega \sin(\omega t) - \beta \cos(\omega t)), \\0 &= \frac{1}{\omega^2 + \beta^2} A_0 e^{-\beta t} (\omega \sin(\omega t) - \beta \cos(\omega t)) = \omega \sin(\omega t) - \beta \cos(\omega t), \\ \sin \omega t &= \frac{\beta}{\omega} \cos \omega t, & \tan \omega t &= \frac{\beta}{\omega}, & t &= \frac{1}{\omega} \arctan \frac{\beta}{\omega}, \\v = 0 : S &= x(t) = A_0 e^{-\beta t} \cos \left(\frac{1}{\omega} \arctan \frac{\beta}{\omega} \right)\end{aligned}$$