Домашня робота 7

$$5.15 \int \frac{dx}{x^{3}\sqrt{x^{2}+1}} = \int x^{-3}(1+x^{2})^{-\frac{1}{2}} dx = \begin{vmatrix} m = -3, & n = 2, & p = -\frac{1}{2} \\ t^{2} = 1+x^{2}, & x = \sqrt{t^{2}-1} \end{vmatrix} = \int \frac{dt}{\sqrt{t^{2}-1^{4}}} = \\ = \int (t^{2}-1)^{2} dt = \int (t^{4}-2t^{2}+1) dt = \frac{t^{5}}{5} - \frac{2t^{3}}{3} + t = \frac{\sqrt{x^{2}+1}^{5}}{5} - \frac{2\sqrt{x^{2}+1^{3}}}{3} + \sqrt{x^{2}+1} + c \\ = \int (t^{2}-1)^{2} dt = \int (t^{4}-2t^{2}+1) dt = \frac{t^{5}}{5} - \frac{2t^{3}}{3} + t = \frac{\sqrt{x^{2}+1}^{5}}{5} - \frac{2\sqrt{x^{2}+1^{3}}}{3} + \sqrt{x^{2}+1} + c \\ = \int x^{2} - \frac{t^{2}-2}{2+2t} dt = \int x^{2} - \frac{2t^{6}+6t^{5}+8t^{4}-16t^{2}-24t-16}{(2+2t)^{4}} dt = \int -\frac{2t^{6}+6t^{5}+8t^{4}-16t^{2}-24t-16}{(2+2t)^{4}} dt = \int x^{5} dx =$$

 $= -\sqrt{1-x^2} + \frac{2\sqrt{1-x^2}^3}{2} - \frac{\sqrt{1-x^2}^5}{5} + c$