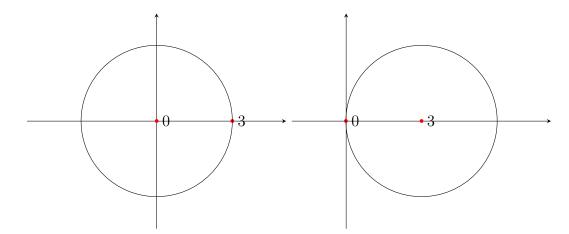


2.
$$f(z) = \frac{1}{z(z-3)}, z = 0, z = 3$$



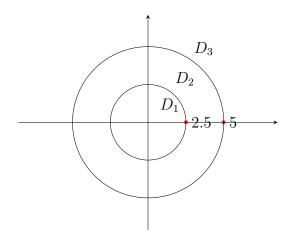
$$z_{0} = 0, \quad |z| < 3, \quad \frac{1}{z - 3} = -\frac{1}{3} \cdot \frac{1}{1 - \frac{z}{3}} = \left\langle \left| \frac{z}{3} \right| < 1 \right\rangle = -\frac{1}{3} \sum_{n=0}^{\infty} \left(\frac{z}{3} \right)^{n} = -\sum_{n=0}^{\infty} \frac{z^{n}}{3^{n+1}}$$

$$f(z) = -\frac{1}{z} \sum_{n=0}^{\infty} \frac{z^{n}}{3^{n+1}} = -\sum_{n=0}^{\infty} \frac{z^{n-1}}{3^{n+1}}$$

$$z_{0} = 3, \quad |z - 3| < 3, \quad \frac{1}{z} = -\frac{1}{-3 - (z - 3)} = \frac{1}{3} \cdot \frac{1}{1 - \left(-\frac{z - 3}{3} \right)} = \frac{1}{3} \sum_{n=0}^{\infty} \left(-\frac{z - 3}{3} \right)^{n} = \sum_{n=0}^{\infty} \frac{(-1)^{n} (z - 3)^{n}}{3^{n+1}}$$

$$f(z) = \frac{1}{z - 3} \sum_{n=0}^{\infty} \frac{(-1)^{n} (z - 3)^{n}}{3^{n+1}} = \sum_{n=0}^{\infty} \frac{(-1)^{n} (z - 3)^{n-1}}{3^{n+1}}$$

3.
$$f(z) = \frac{5z - 50}{2z^3 + 5z^2 - 25z}, \quad z_0 = 0$$



$$\begin{bmatrix} z_1 = 0, & D_1 : & 0 < |z| < 2.5 \\ z_2 = 2.5 & D_2 : & 2.5 < |z| < 5 \\ z_3 = -5 & D_3 : & |z| > 5 \end{bmatrix}$$

$$f(z) = \frac{5}{z} \cdot \frac{z - 10}{(z + 5)(2z - 5)} = \frac{5}{z} \cdot \left(\frac{A}{z + 5} + \frac{B}{2z - 5}\right) = \frac{5}{z} \cdot \left(\frac{1}{z + 5} + \frac{1}{2z - 5}\right)$$

$$\frac{1}{z + 5} = \frac{1}{5} \cdot \frac{1}{1 - \left(-\frac{z}{5}\right)} = \frac{1}{5} \sum_{n=0}^{\infty} \left(-\frac{z}{5}\right) = \sum_{n=0}^{\infty} \frac{(-1)^n z^n}{5^{n+1}} \in D_1, D_2$$

$$\frac{1}{z + 5} = \frac{1}{z} \cdot \frac{1}{1 - \left(-\frac{5}{z}\right)} = \frac{1}{z} \sum_{n=0}^{\infty} \left(-\frac{5}{z}\right) = \sum_{n=0}^{\infty} \frac{(-1)^n 5^n}{z^{n+1}} \in D_3$$

$$\frac{1}{2z-5} = -\frac{1}{5} \cdot \frac{1}{1-\frac{2z}{5}} = -\frac{1}{5} \sum_{n=0}^{\infty} \left(\frac{2z}{5}\right) = \sum_{n=0}^{\infty} \frac{(-1)^n 2^n z^n}{5^{n+1}} \in D_1$$

$$\frac{1}{2z-5} = \frac{1}{2z} \cdot \frac{1}{1-\frac{5}{2z}} = \frac{1}{2z} \sum_{n=0}^{\infty} \left(\frac{5}{2z}\right) = \sum_{n=0}^{\infty} \frac{5^n}{2^{n+1}z^{n+1}} \in D_1, D_3$$

$$D_1: \quad 0 < |z| < 2.5: \quad f(z) = \frac{5}{z} \left(\sum_{n=0}^{\infty} \frac{(-1)^n z^n}{5^{n+1}} + \sum_{n=0}^{\infty} \frac{2^n z^n}{5^{n+1}}\right) = \sum_{n=0}^{\infty} \frac{((-1)^n + 2^n)z^{n-1}}{5^n}$$

$$D_2: \quad 2.5 < |z| < 5: \quad f(z) = \sum_{n=0}^{\infty} \frac{(-1)^n z^{n-1}}{5^n} - \sum_{n=0}^{\infty} \frac{5^{n+1}}{2^{n+1}z^{n+2}}$$

$$D_3: \quad |z| > 5: \quad f(z) = \sum_{n=0}^{\infty} \frac{(-1)^n - 2^{-n-1}5^{n+2}}{z^{n+2}}$$