

MAE 150 Problem 2

$$\begin{bmatrix} X(i) \\ Y(i) \\ 1 \end{bmatrix} = \begin{bmatrix} \cos(\theta_2) & -\sin(\theta_2) & t_x \\ \sin(\theta_2) & \cos(\theta_2) & t_y \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x(i) \\ y(i) \\ 1 \end{bmatrix} \rightarrow \begin{aligned} X(i) &= x(i)\cos\theta_2 - y(i)\sin\theta_2 + t_x \\ Y(i) &= x(i)\sin\theta_2 + y(i)\cos\theta_2 + t_y \\ 1 &= 1 \end{aligned}$$

these are the same!

vs

(rotation first)

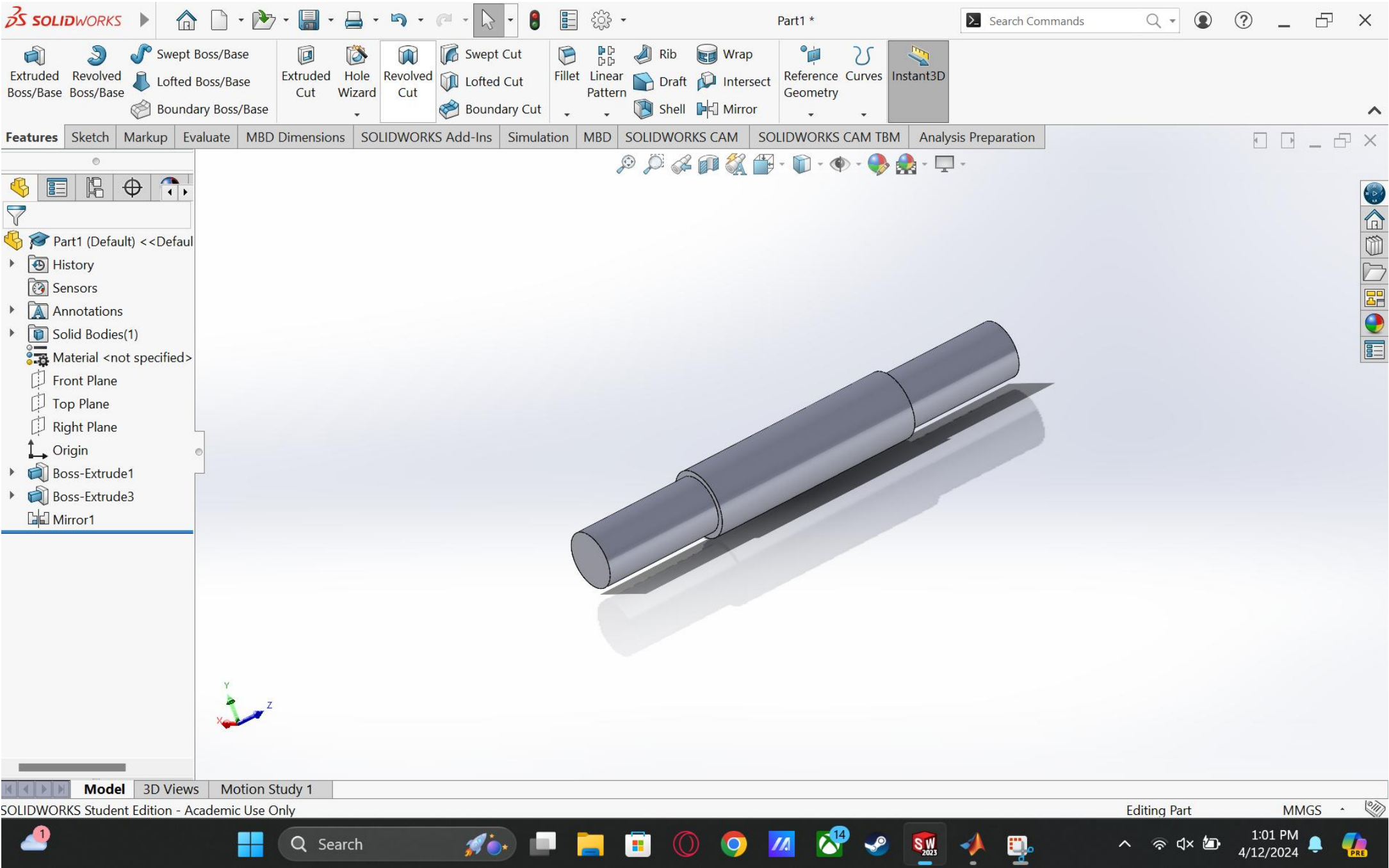
$$\begin{bmatrix} X(i) \\ Y(i) \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & t_x \\ 0 & 1 & t_y \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \cos\theta_2 & -\sin\theta_2 & 0 \\ \sin\theta_2 & \cos\theta_2 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x(i) \\ y(i) \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & t_x \\ 0 & 1 & t_y \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x(i)\cos\theta_2 - y(i)\sin\theta_2 \\ x(i)\sin\theta_2 + y(i)\cos\theta_2 \\ 1 \end{bmatrix} \rightarrow \begin{aligned} X(i) &= x(i)\cos\theta_2 - y(i)\sin\theta_2 + t_x \\ Y(i) &= x(i)\sin\theta_2 + y(i)\cos\theta_2 + t_y \\ 1 &= 1 \end{aligned}$$

vs

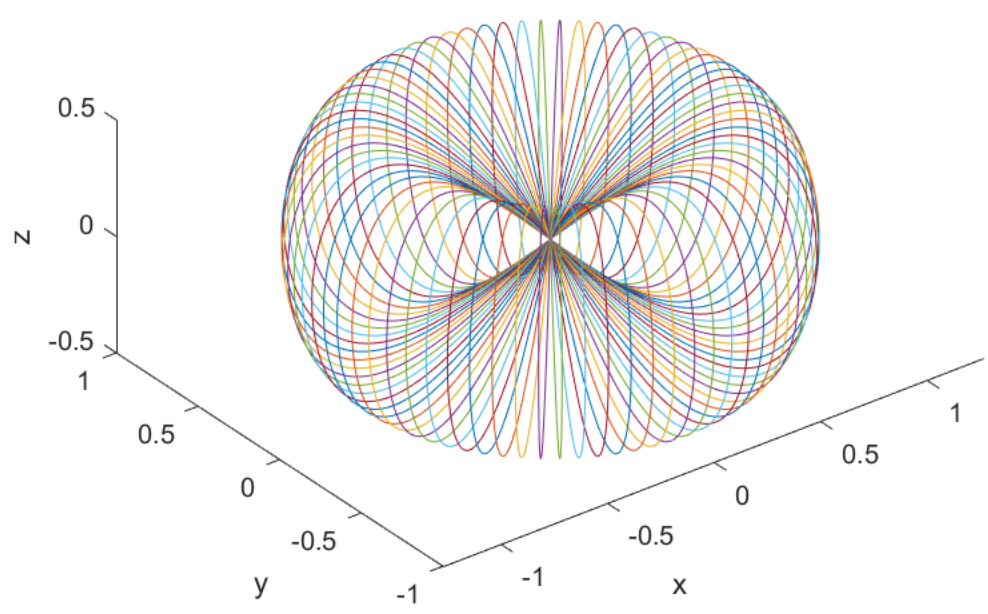
(translation first)

$$\begin{bmatrix} X(i) \\ Y(i) \\ 1 \end{bmatrix} = \begin{bmatrix} \cos\theta_2 & -\sin\theta_2 & 0 \\ \sin\theta_2 & \cos\theta_2 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & t_x \\ 0 & 1 & t_y \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x(i) \\ y(i) \\ 1 \end{bmatrix} = \begin{bmatrix} \cos\theta_2 & -\sin\theta_2 & 0 \\ \sin\theta_2 & \cos\theta_2 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x(i) + t_x \\ y(i) + t_y \\ 1 \end{bmatrix} \rightarrow \begin{aligned} X(i) &= [x(i) + t_x]\cos\theta_2 - [y(i) + t_y]\sin\theta_2 \\ Y(i) &= [x(i) + t_x]\sin\theta_2 + [y(i) + t_y]\cos\theta_2 \\ 1 &= 1 \end{aligned}$$

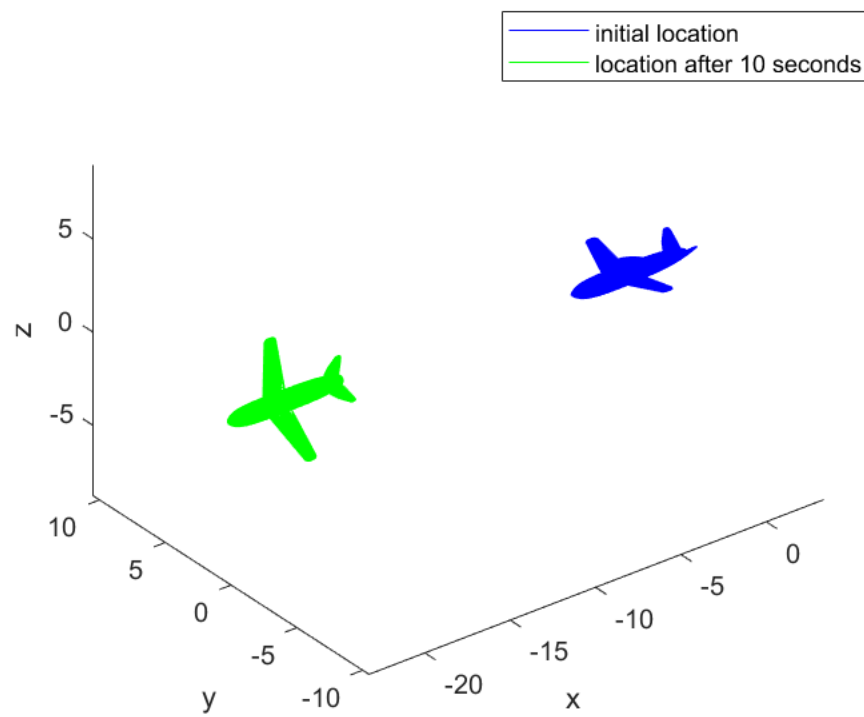
→ The suggestion is valid, and corresponds to performing the rotation prior to the translation.



Rotation of a curve about Z-axis



Translation and Rotation of a Plane



```

clear all;
close all;
clc;
format long;

name = 'Natalie Ratzlaff';
id = 'A170911327';
hw_num = 1;

data = readmatrix("US_COVID19.txt");
date = data(:,2);

p1a = data(find(date == 20200704),4)

p1b = data(find(date == 20201126),4)

for i = 8:1:319
    data(i,6) = 0;
    for j = -7:7
        data(i,6) = data(i,6) + data(i+j,4);
    end
    data(i,6) = data(i,6)/15;
end

data(1:7,6) = NaN;
data(320:326,6) = NaN;

hold on;
figure(1);
xlabel('Year Day');
ylabel('Number of Positive Cases');
bar(data(:,1),data(:,4));
plot(data(:,1),data(:,6), 'LineWidth',3);
plot(186,p1a,'cdiamond','MarkerFaceColor','c');
plot(331,p1b,'mo','MarkerFaceColor','m');
title('Daily COVID-19 Cases in 2020');
legend('Positive Tests per day','15-day running average','Positive Cases on July 4th','Positive Cases on Thanksgiving');

p1c = 'See figure 1'

t = 0:360;
x = cosd(t);
y = 0*t;
z = sind(t).*cosd(t);

m = [x;y;z;1+t*0];
R = @(theta) [cosd(theta) -sind(theta) 0 0; sind(theta) cosd(theta) 0 0; 0 0 1 0; 0 0 0 1];

figure(2);
hold on;
plot3(x,y,z);
for i = 5:5:175
    M = R(i)*m;
    plot3(M(1,:),M(2,:),M(3,:));
end
xlabel('x');
ylabel('y');
zlabel('z');
title('Rotation of a curve about Z-axis');
axis equal;
view(3);

```

```

p3 = 'See figure 2'

figure(3);
hold on;
plane = stlread("aircraft.stl");
trimesh(plane,'FaceColor','none','EdgeColor','b');

Rx = @(rad) [1 0 0; 0 cos(rad) -sin(rad); 0 sin(rad) cos(rad)];
pfinal = Rx(1)*((plane.Points).');
pfinal(1,:) = pfinal(1,:) - 20;
final = triangulation(plane.ConnectivityList,pfinal. ');
trimesh(final,'FaceColor','none','EdgeColor','g');
xlabel('x');
ylabel('y');
zlabel('z');
legend('initial location','location after 10 seconds');
title('Translation and Rotation of a Plane');
axis equal;
view(3);

p4a = pfinal(:,find(pfinal(3,:) == max(pfinal(3,:)))).'
p4b = 'See figure 3'

```

```

p1a =

    54144

```

```

p1b =

    128439

```

```

p1c =

    'See figure 1'

```

```

p3 =

    'See figure 2'

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p4a =

    -20.024535119533539    1.412572869860626    2.650511116873443

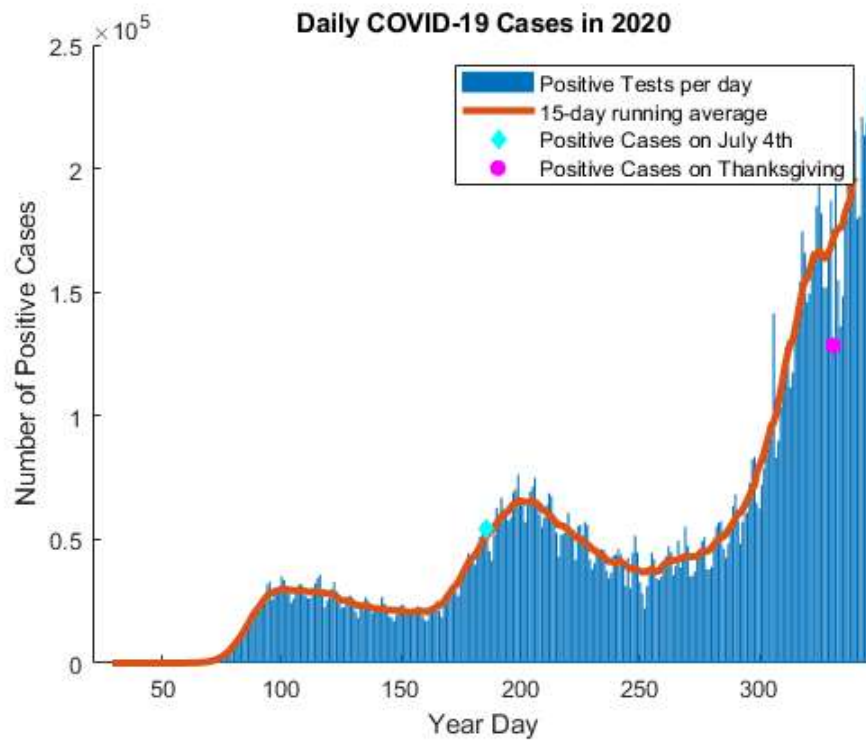
```

```

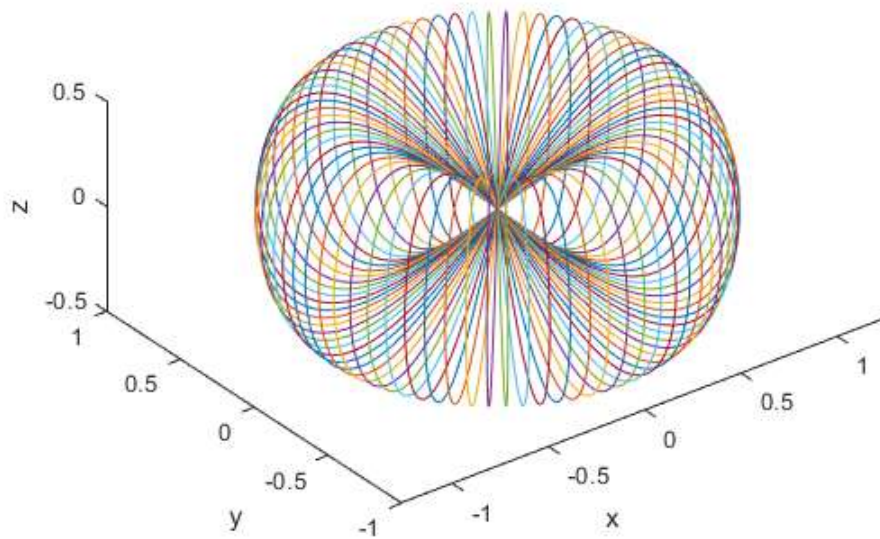
p4b =

    'See figure 3'

```



Rotation of a curve about Z-axis



Translation and Rotation of a Plane

