

La definició de connex: un viatge del contínu de Cantor a la definició moderna de Kelly

Natàlia Castellana

- “The point of this examination is to establish a precise criterion - but one that is simultaneously as generally applicable as possible - for designating P as a continuum.”

“A closed and bounded point set T is connected if for every two of its points t and t' , and arbitrary given positive number ϵ , there always exists a finite number of points t_1, t_2, \dots, t_n of T such that the distances $tt_1, t_1t_2, \dots, t_nt'$ are smaller than ϵ .”

Georg Cantor, Über die Ausdehnung eines Satzes aus der Theorie der trigonometrischen Reihen, Math. Ann., 5(1):123-132, **1872**.

- “Let E, E' be two closed sets with no point in common. The distance between the various points p in E to the various points p' in E' form a set of nonnegative numbers. It is therefore bounded below, and it admits a minimum Δ , positive or 0, we call the distance between the sets E, E' . If the distance is greater than 0, we say that the sets E, E' are separated.”

“We say that a closed and bounded set E is a component if it cannot decompose into several separated sets.”

Camille Jordan, Cours d'analyse (Course on Analysis). vol. 1, **1893**.

- “A perfect set T is called connected if it can not be decomposed into subsets, each of which is perfect.”

Arthur Moritz Schoenflies, Beitrage zur Theorie der Punktmengen I. Math. Ann., 58:195-238, **1904**.

- “A set of points is a connected set if at least one of any two complementary subsets contains a limit point of points in the other set.”

Nels Johann Lennes, Curves in Non-Metrical Analysis Situs with an Application in the Calculus of Variations. Amer. J. Math., 33(1-4):287-326, **1911**.

- “A topological space is connected iff X is not the union of two non-void separated open subsets.”

John L. Kelley, General topology. Springer-Verlag, New York, 1975. Reprint of the **1955** edition [Van Nostrand, Toronto, Ont.], Graduate Texts in Mathematics, No. 27.