

# Machine Learning Guidelines for Natural Resource Management Practitioners

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# Chapter 1

## Motivation

As machine learning (ML) has become a powerful tool, it is noted by some that ML has not been widely used in environmental studies. Some might prefer process based models, but they can be costly and ML provides a large variety of tools that should be explored. This booklet is meant to provide a concise guide for natural resource management practitioners. This book serves as a starting point rather than a comprehensive resource, so that practitioners can have a basic understanding of how ML works and how to utilize it to analyze data and answer research questions. When appropriate, we provide case studies and R code as well as other online resources to help the readers on the journey of gaining one powerful tool that seems to be omnipresent in the research world.



## Chapter 2

# Introduction

What is machine learning? Essentially, machine learning teaches computer models to look for patterns or make predictions. This might seem complicated, but you can think of machine learning models as finding underlying formulas that the data come from. To solve for such formula, many, many mathematical calculations are involved. As we human beings are prone to mistakes for such kind of task, a more effective way to work with data is for us to identify a framework and give the framework and data to a computer model. The computer is best at repeating meticulous calculations to find a best guess based on our believes of the system and the data we observed.

Even though ML models are commonly considered black boxes, they are not necessarily so. Many ML methods lend easily to interpretation. Random forests, for example, is a powerful method that can offer a glimpse into what the important variables are, even if the straightforward explanation that can come from a linear model is unavailable. Below we introduce the two large branch of machine learning.

The book *An Introduction to Statistical Learning* by James et al. (2013) is a great resource! This book provides a wealth of information about machine learning models; further, the authors do not assume that the readers are mainly interested in applying, rather than studying, ML models. The four premises offered by the authors, listed on pp 8-9 of the version about R, pointing to the practical focus of the book:

1. Many statistical learning methods are relevant and useful in a wide range of academic and non-academic disciplines, beyond just the statistical sciences.
2. Statistical learning should not be viewed as a series of black boxes.
3. While it is important to know what job is performed by each cog, it is not necessary to have the skills to construct the machine inside the box!

4. We presume that the reader is interested in applying statistical learning methods to real-world problems.

There are free PDF versions with applications in R and Python [here](#). Be sure to check it out if you are interested in learning more about machine learning models!

## 2.1 Supervised Learning

Simply put, supervised learning is when there is a true answer for the model. For example, if we want to use environmental traits (temperature, precipitation, chemical composition) to predict algal growth. In a dataset that record such activities, there are growths that are the right answers. The model can then use the predictors to make predictions, and the comparison between the predictions and the truth can show how well the model performs.

## 2.2 Unsupervised Learning

Unsupervised learning, on the other hand, performs tasks that do not have a correct/true answer. For example, for a group of chemicals, some might have more similar traits than the others. Unsupervised learning can perform clustering to find such groupings, but it is still unsupervised because the grouping depends on the context. One could imagine that clustering can be performed first, and the groupings are used as the predictors instead of the chemicals themselves. This way the dimension can be reduced, assuming that the number of groups is smaller than the number of chemicals.



## Chapter 3

# Data

When you have data, don't feel so rushed to jump into data analysis yet. Some steps can help you know your data better and, more than often, avoid problems down the road.

### 3.1 Data Exploratory Analysis

After you read in data, do some checks. Below we use the embedded `mtcars` as an example for illustration.

```
library(tidyverse)
```

```
## -- Attaching core tidyverse packages ----- tidyverse 2.0.0 --
## v dplyr      1.1.4      v readr      2.1.4
## v forcats    1.0.0      v stringr   1.5.1
## v ggplot2    3.4.4      v tibble    3.2.1
## v lubridate  1.9.3      v tidyr     1.3.0
## v purrr      1.0.2
## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()     masks stats::lag()
## i Use the conflicted package (<http://conflicted.r-lib.org/>) to force all conflicts to become
```

```
data("mtcars")
str(mtcars)
```

```
## 'data.frame':   32 obs. of  11 variables:
## $ mpg : num  21 21 22.8 21.4 18.7 18.1 14.3 24.4 22.8 19.2 ...
```

```
## $ cyl : num  6 6 4 6 8 6 8 4 4 6 ...
## $ disp: num 160 160 108 258 360 ...
## $ hp  : num 110 110 93 110 175 105 245 62 95 123 ...
## $ drat: num 3.9 3.9 3.85 3.08 3.15 2.76 3.21 3.69 3.92 3.92 ...
## $ wt  : num 2.62 2.88 2.32 3.21 3.44 ...
## $ qsec: num 16.5 17 18.6 19.4 17 ...
## $ vs  : num 0 0 1 1 0 1 0 1 1 1 ...
## $ am  : num 1 1 1 0 0 0 0 0 0 0 ...
## $ gear: num 4 4 4 3 3 3 3 4 4 4 ...
## $ carb: num 4 4 1 1 2 1 4 2 2 4 ...
```

As seen above, the command `str` allows you to see the variables and their types. For this dataset, all variables are numerical. If some are categorical but they should be numerical, make sure you transform them into the right type of data. (Sometimes numbers can be saved as characters, and the analysis would not be correct if the datatype remains as character.)

Next, try to make some plots—typically histograms for numerical variables and barplots for categorical variables.

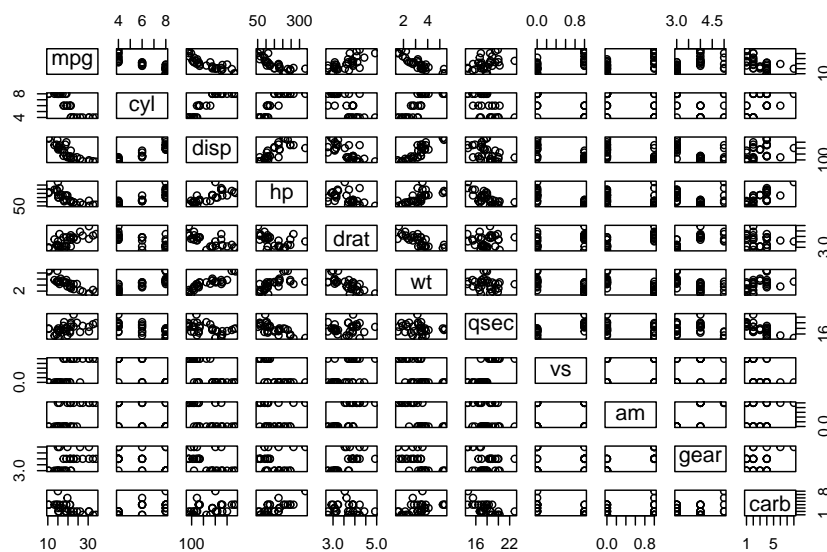
```
par(mfrow = c(3,3), mar = c(2,2,2,2))
for (i in 1:ncol(mtcars)){
  hist(mtcars[,i], main = paste0("Histogram of ", colnames(mtcars)[i]))
}
```





You can also look at the paired plots to see if two variables are too perfectly correlated, which could cause problems in regression models.

```
pairs(mtcars)
```



Next, take a look at the summary statistics.

```
for (i in 1:ncol(mtcars)){
  print(paste0("***** Summaries of ", colnames(mtcars)[i], " *****"))
  print(summary(mtcars[,i]))
}
```

```
## [1] "***** Summaries of mpg *****"
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##    10.40   15.43   19.20   20.09   22.80   33.90
## [1] "***** Summaries of cyl *****"
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##     4.000   4.000   6.000   6.188   8.000   8.000
## [1] "***** Summaries of disp *****"
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##     71.1   120.8   196.3   230.7   326.0   472.0
## [1] "***** Summaries of hp *****"
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##     52.0   96.5   123.0   146.7   180.0   335.0
## [1] "***** Summaries of drat *****"
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##     2.760   3.080   3.695   3.597   3.920   4.930
## [1] "***** Summaries of wt *****"
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##     1.513   2.581   3.325   3.217   3.610   5.424
## [1] "***** Summaries of qsec *****"
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##     14.50   16.89   17.71   17.85   18.90   22.90
## [1] "***** Summaries of vs *****"
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##     0.0000  0.0000  0.0000  0.4375  1.0000  1.0000
## [1] "***** Summaries of am *****"
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##     0.0000  0.0000  0.0000  0.4062  1.0000  1.0000
## [1] "***** Summaries of gear *****"
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##     3.000   3.000   4.000   3.688   4.000   5.000
## [1] "***** Summaries of carb *****"
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##     1.000   2.000   2.000   2.812   4.000   8.000
```

The summaries can show, for example, ranges and means of the variables. They can give you a better understanding of where the values are and whether there might be data entry errors.

## 3.2 Data Requirement

## 3.3 Strategies for Missing Data

### 3.3.1 Removing observations

If you have a large dataset and the percentage of missing data is small, you can simply ignore those observations. Note that you should check whether the pattern of missingness is “missing at random,” meaning that the reason why certain observations are missing is pure chance. If, for example, some observations are missing because the pollution level is too high or too low and the detection is not ideal, then ignoring these observations could result in biased conclusions.

### 3.3.2 Imputation

Imputation is a commonly used method for missing data. If linearity is plausible, you can use linear imputation. If some response variables are missing, some Bayesian method can fill in the values using posterior draws. (In other words, in the process of running the analysis, the algorithm can predict what the response variable should be and fill it in.) Imputation is a big tool set that, if needed, you should consult a more comprehensive resource. [provide suggestions]



## Chapter 4

# Evaluation

### 4.1 Training vs Testing

We should first address the concepts of training and testing. Instead of using the entire data, it is common to split the dataset into a training set and a test set. Typically people use percentages such as 70% vs 30% or 80% vs 20%. The idea is to use only, say, 80% of the data for training, which means to run the select model on this part of data. Then you have a model with some coefficients (you can think of them as slopes) and test such results on the test set to see how well the model performs. Since the part of the data for testing is not used in training, this way there is no double dipping. Sometimes people split the dataset into three sets: training, test, and validation. So the trained models are used on the test set for model selection. Then the validation set is used only once at the end to gauge how the model should perform if there's new data.

### 4.2 Metrics

#### 4.2.1 Numerical Responses

The most common metrics for numerical responses include mean squared errors (MSE), bias, and  $R^2$  (or adjusted  $R^2$ ). The way to calculate MSE is:

$$MSE = \frac{1}{n} \sum_{i=1}^n \left( \hat{y}_i - y_i \right)^2.$$

The metric shows, on average, the squared distance between predictions and true responses. Bias is calculated as

$$Bias = \frac{1}{n} \sum_{i=1}^n (\hat{y}_i - y).$$

The two metrics seem similar, but they reveal different aspects of model performance. In general, bias shows if the predictions are centered around the truth, while the MSE shows how far the predictions are from the truth. If the bias is zero, it means that the mean prediction goes towards the truth as the sample size increases to infinity. This is naturally a desired property, but you might be surprised that sometimes we are willing to accept some bias to reduce the variance.

One important formula,

$$MSE = Bias^2 + Variance,$$

where

$$Variance = \frac{1}{n} \sum_{i=1}^n \left( \hat{y}_i - E(\hat{y}) \right)^2$$

and

$$E(\hat{y}) = \frac{1}{n} \sum_{i=1}^n \hat{y}_i.$$

We skip the derivation here, but the interested readers can find the derivation readily online. The formula tells us that, if the MSE is large but the bias is small, this means the model has a large variance. This is to say, if you fit the model multiple times, it has quite different results every time. These formulas might seem too technical, but the message is important. There is a trade off between the bias and variance; in other words, there is no free lunch. A balance between bias and variance is where many methods strive to achieve.

### 4.2.2 Categorical Responses

When the responses are categorical, a common way to measure the performance is a confusion matrix, which shows the numbers of predictions that are correct or incorrect.

[provide an example]

Other metrics include sensitivity, specificity, precision, recall, and other metrics that try to combine these metrics to present a one-number summary.



## 4.3 Overfitting

Overfitting means that the model can make good predictions with the available data, but it cannot generalize well on new data. It is kind of like if a student memorizes all the past exam questions without really studying the materials, then, on the exam, the student can do really well on questions coming from past exams but might do poorly on questions never seen before. Splitting data into training and testing is one strategy to avoid overfitting. Certain ML methods are less likely to overfit, such as neural networks. And there are some more strategies, such as early stopping, that can be used. Our point here is to make you aware this potential pitfall of machine learning methods.

## 4.4 Cross Validation

One very standard way of evaluation is  $k$ -fold cross validation, commonly with  $k = 5$  or  $k = 10$ . The idea is simple. Divide the data into  $k$  groups. Each time, choose  $k - 1$  groups for training, fit the model on the last group, which is the test data, and calculate the desired metrics, such as MSE.

In this way, although less data is used for training, the metrics are more accurate, because now we are not using the same data points for training and testing. Using metrics from cross validation for model selection can ensure that your model does not overfit, which means the model does well with training data but does not generalize well on new data.



Figure 4.1: Image Source: [https://en.wikipedia.org/wiki/Cross-validation\\_\(statistics\)](https://en.wikipedia.org/wiki/Cross-validation_(statistics))



## Chapter 5

# Machine Learning Methods

Here we discuss some machine learning methods you might find useful. Although linear regression models are commonly used, we skip it because it is well understood and many online resources can be easily located.

### 5.1 Tree-based Methods

Tree-based methods are popular for their ease for interpretation. Essentially, the algorithm tries to split the data into subsets by finding the most significant (or consequential) variables in a way that reduces the prediction error the most. For example, in the graph below, the variable that helps reduce prediction error at the first level is gender. In other words, the object being male or female can greatly help the algorithm predict the survival of passengers on Titanic.

Decision trees are easy to use but not very accurate for complex data; however, we can go beyond one tree. If we use multiple trees and, for instance, take the average of the predictions of all the trees, we can improve the performance. This is the idea of ensemble methods. One of the ensemble methods, random forests, is commonly used, including in natural resources management, and quite accurate for many kinds of data. So next we'll dive into this one method.

#### 5.1.1 Random Forests

For random forests, the algorithm randomly selects a smaller number, say  $m$ , of predictors from the total number, say  $p$ , each time a tree is being fit. This process is repeated many times, for example, 500 times. The average (for continuous responses) or the majority votes (for discrete responses) of the predictions from the individual trees are used as final predictions. By randomly choosing

## Survival of passengers on the Titanic

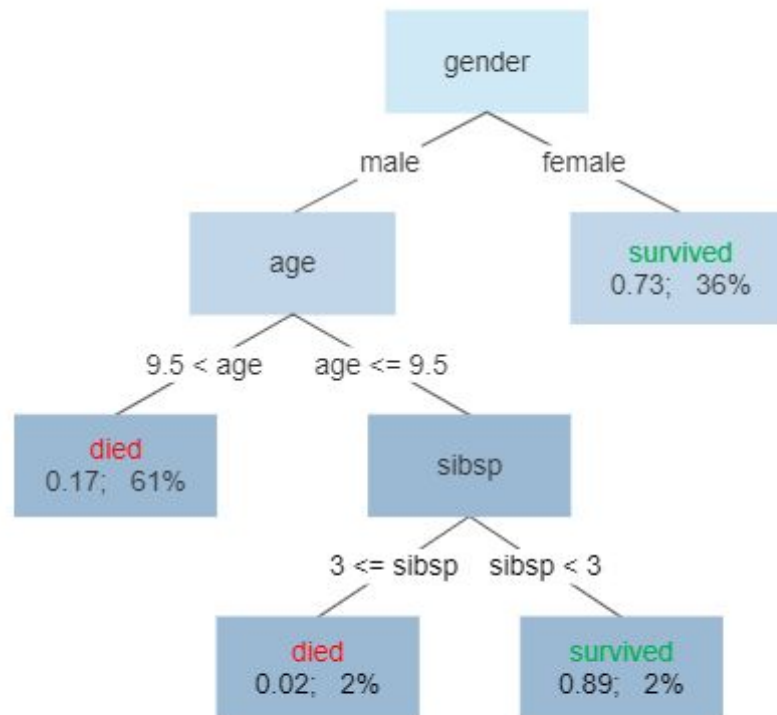


Figure 5.1: By Gilgoldm - Own work, CC BY-SA 4.0, <https://commons.wikimedia.org/w/index.php?curid=90405437>

a subset of predictors each time, random forests can avoid relying on the same variables every time and prevent overfitting.

Even though coefficients of each predictors are not available for random forests, you can easily get the important variables and at least know which variables are more important for predicting the response. You can also use random forests as a tool for variable selection and then use a different method to fit the model on a subset of predictors chosen by random forests.

[Need examples]

### 5.1.2 Other Ensemble Tree Methods

Other ensemble tree methods include boosting and bagging. If you are interested, take a look at [a source].

## 5.2 Neural Network

Neural network has been enjoying its popularity. A neural network model is composed of an input layer, some hidden layers, and an output layer, as seen below. There is only one hidden layer below. When there are enough hidden layers, the model is then called deep learning.

So the input layer is the observed predictors, and each of the hidden layers has nodes that contain coefficients. You can think of these coefficients similar to those for linear models, except they do not have linear relationships with the observed predictors. These values are derived from finding the best fit between data and some kind of cost function; essentially, these values are meant to minimize the differences between observed outcome and predictions. When the values from one hidden layer are passed onto the next layer, a nonlinear activation function called ReLU is commonly used. If the task is classification, the layer right before output is often some kind of algorithm to turn the values into predicted class. While neural network is a powerful ML model, the values in the nodes in the hidden layers are not interpretable. So this indeed is a black-box method. For interested readers, check out **Chapter 10 Deep Learning** in James et al. (2013) (*An Introduction to Statistical Learning*).

## 5.3 Gaussian Process (GP)

Another powerful ML method that could be useful for natural resource management type of research is Gaussian Process. This method, commonly called kriging in spatial statistics, is non-parametric, which sounds like there are no parameters in the model but in fact means there can be an infinite number of

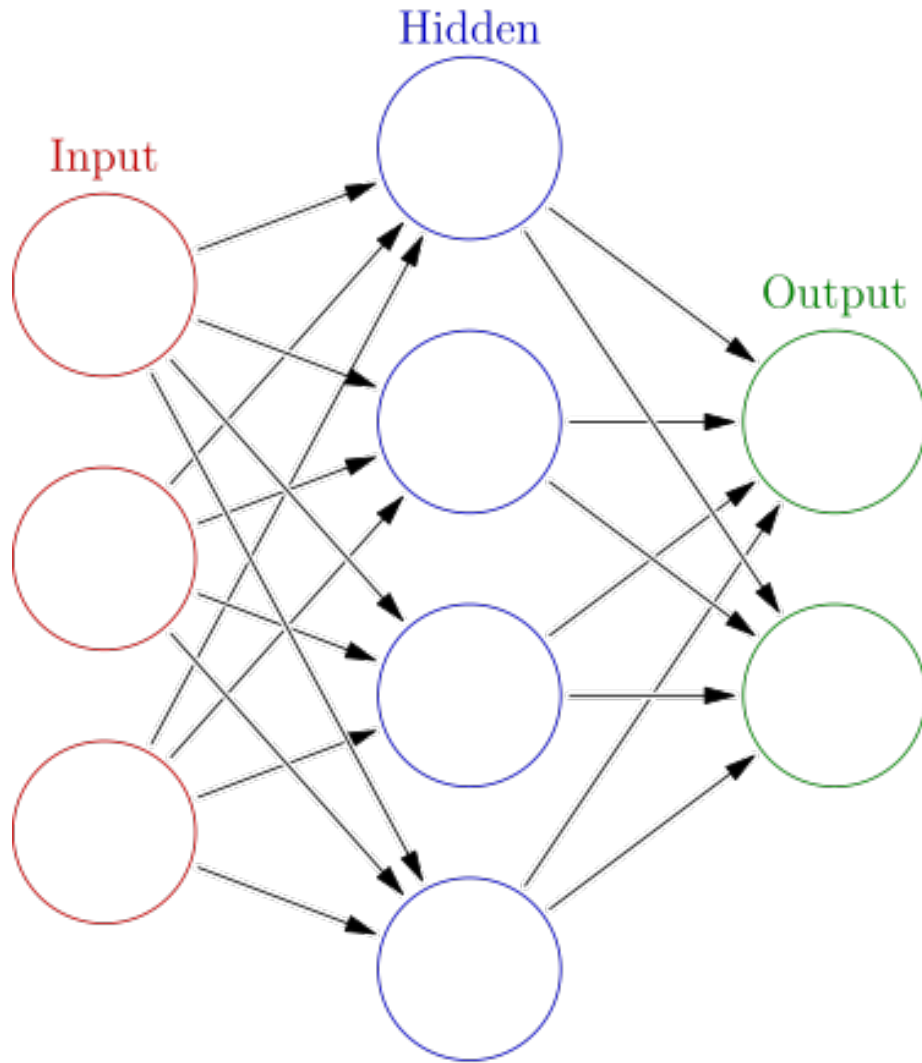


Figure 5.2: By Glosser.ca - Own work, Derivative of File: Artificial neural network.svg, CC BY-SA 3.0, <https://commons.wikimedia.org/w/index.php?curid=24913461>

parameters. (Of course in any real model we'll have finite parameters, but that's the idea.) The fact that the parameters can increase towards infinity tells us that this is a flexible model. Essentially, for a GP model, and here I quote from Chapter 5 of Gramacy's *Surrogates*, "any finite collection of realizations (i.e.  $n$  observations) is modeled as having a multivariate normal (MVN) distribution." In other words, the model tries to learn information from similar items, judging from some kind of distance from each other. MVN has some great properties. And, when there is a new data point, all the observed data points can be used to make prediction for it.

GP is widely used in the machine learning, computer experiments, and spatial statistics communities. There are ready-made R packages, such as **GpGp** and **deepgp**. It's also easy to use in Python. Chapter 5 ("Gaussian Process Regression") of the book *Surrogates* by Gramacy (2020) is a great resource if you are interested in learning more about Gaussian process!





## Chapter 6

# Workflow Demonstration

In this section, we use a wine dataset to exemplify a typical workflow for constructing ML models. R code is included and several ML models are constructed.



## Chapter 7

# Case Studies

Since ML models are easy to construct, they can at least be used to compare results or explore areas in which not much is known, so some basic hypothesis can be made and other process-based models can be used to confirm these results.

### 7.1 Case Study 1: Machine learning approach for modeling daily pluvial flood dynamics in agricultural landscapes

#### 7.1.1 Takeaway

With the remote sensed images as important data sources, the researchers had to do quite a lot of pre-processing. While pre-processing images might seem time consuming, once the workflow is established, studying flood in other areas becomes easier, as long as images are available. This is one of the strengths of ML models—the process can be at least partially automated, and data is more easily obtained than if measuring at each site is required.

#### 7.1.2 Summary

In this study, Fidan et al. (2023) build a random forest model using gridded rainfall data, derived from remotely sensed imagery, from the 2016 hurricane Matthew’s impact in Kinston, North Carolina. Besides the proprietary images, the researchers also included readily available geospatial landscape traits for the models. With the objectives of (1) develop a pluvial flood dataset using imagery, (2) test the performance of random forest models for the modeling

flood in “low-lying and flat agricultural terrain,” (3) find important predictors, and (4) “generate pluvial flood time series.”

The outcome variable is binary in terms of flooding. Each pixel is treated as one data point. Non-flooded areas were covered by 5,875,480 pixels, and flooded areas by 678,010 pixels. Since there were many more non-flooded pixels than flooded pixels, overall accuracy alone would not be a good performance metric, since, if the model just always predict that a pixel is not flooded, the accuracy rate would be high. The researchers chose other metrics such as precision, recall, specificity, and F1 scores to reflect model performance in different scenarios. The model achieved an overall accuracy of 0.97 and an F1 score of 0.69. Considering that the no information rate (if the model predicts non-flooded all the time) is around 88.5%, this performance seems satisfactory. They found the important variables to be population density, distance to the nearest river, height above nearest drainage, and distance to the nearest road.

The full paper can be accessed [here](#).

## 7.2 Case Study 2: Short-term forecasting of fecal coliforms in shellfish growing waters

### 7.2.1 Takeaway

This study serves as a nice case study because (1) it demonstrates that random forest does well with nonlinear relationships between the predictors and outcomes, (2) the performance is at least as good as other studies, (3) the findings are consistent with what researchers have knowns. These reasons tell us that we can trust random forest models. Furthermore, random forest models are easy and cheap to construct. The R package `caret` and function `rf`, used by Chazal et al. (2024), is easy to use and quick to run, if the number of trees are reasonably chosen. The important variables, readily provided by `caret::rf`, helps greatly with interpretation.

### 7.2.2 Summary

This study’s goal was to predict near-term (1-3 days) fecal contamination in coastal shellfish growing waters. For each of the five management areas, Chazal et al. (2024) constructed five random forest models to (1) use watershed characteristics as well as antecedent hydrologic and meteorologic observations to predict the level of fecal coliform (FC), (2) test whether forecasted rainfall can be useful for predictions, and (3) find important variables. Let’s focus on goals (1) and (3) for this case study.

For their first goal, depending on the management areas, the  $R^2$  value is between 0.40 and 0.74. According to Chazal et al. (2024), this performance is similar to

previous studies. The other settings are typical of ML studies. They split the data into 80% training and 20% testing and use the variance inflation factor (VIF) to remove variables that are collinear, which means some variables are correlated with each other. For their third goal, they found (1) antecedent rainfall, (2) river stage threshold, and (3) wind are high on the importance for prediction. These findings are consistent with the current understanding. In short, this study demonstrates the reliability and ease for construction and interpretation of random forest models.

The full paper can be accessed [here](#).

### 7.3 Case Study 3



## Chapter 8

# Ethical Considerations

Ethics might sound heavy, but this section is mainly about ensuring that the analysis is carried out in a responsible way. These concerns are not unique to ML models, but the complexity of ML methods makes it ever more important to think about these issues.

### 8.1 Reproducibility

To allow for others to reproduce your work, it is important to provide enough details in terms of methods, data processing, code implementation, etc. It is also encouraged to have all the code and data available online in a repository. If parts or all of the data should not be shared publicly, it helps to provide a simulated data set.

Another aspect of reproducibility might be surprising. Try to use programming scripts rather than drag-and-drop software. Starting from reading in the data, write a script to read, clean, and wrangle with the data. The scripts can preserve all the steps of data analysis. In the future, when you cannot remember how you changed the data or how you arrived at a p-value, the scripts can show all the details, but drag-and-drop software will not leave any trace.

Note that the best practice is to read in the data into the programming environment and make any data cleaning and merging in the script. You can save the cleaned version in a different file, but don't change the file with the raw data.

### 8.2 Decision making

Since research related to environmental sciences and natural resources could likely affect decision making, we will now address some topics.

### 8.2.1 Uncertain qualification

While all ML models can provide point estimates, not all can quantify uncertainty. It is, however, important to show how confident the model is about the estimates. If the conclusion of the study could affect an important policy change, it is crucial to present a full picture of the findings, which include uncertainty quantification. It is wildly different whether the model is 20% or 95% confident about its answer, for instance.

### 8.2.2 Interpretability

While some models, such as neural networks, are highly efficient, they are more like black boxes and do not lend easily to interpretability. In the case of neural networks, even if you are able to find all the weights in the hidden layers, there is really no way to interpret them. To ensure that the model arrives at a reasonable conclusion, you might consider using a model that is more interpretable, such as linear regression or tree-based methods. This way, experts with domain knowledge can examine whether the conclusion makes sense. In other words, the findings from ML models can add to researchers' understanding of the field rather than throwing out an answer that is not easily interpreted.



## Chapter 9

# Appendix

### 9.1 Do's and Don'ts

Below we provide some tips for what to do and what not to do when you build machine learning models.

#### 9.1.1 Do's

- Do data exploratory analysis before jumping into analysis. Look at summary statistics and make plots to familiarize yourself with the data.
- Document the process with reasonable details, so you or other researchers can reproduce the study if needed.
- Along the same line, if you write script for your code, add comments along the way.
- In the publication, explain what the result entails and the limitations of the model.
- When possible, use interpretable and/or parsimonious models. Think Occam's razor.
- Make data and code available to others if possible.
- 

#### 9.1.2 Don'ts

- Don't alter the raw data. Use a script to process data instead.
- Don't over interpret the result. For example, if the samples all come from one geographic area, you might not be able to generalize the result to other areas.

-

# Bibliography

- Chazal, N., Carr, M., Leight, A. K., Saia, S. M., and Nelson, N. G. (2024). Short-term forecasting of fecal coliforms in shellfish growing waters. *Marine Pollution Bulletin*, 200:116053.
- Fidan, E., Gray, J., Doll, B., and Nelson, N. G. (2023). Machine learning approach for modeling daily pluvial flood dynamics in agricultural landscapes. *Environmental Modelling and Software*, 167:105758.
- Gramacy, R. B. (2020). *Surrogates: Gaussian Process Modeling, Design and Optimization for the Applied Sciences*. Chapman Hall/CRC, Boca Raton, Florida. <http://bobby.gramacy.com/surrogates/>.
- James, G., Witten, D., Hastie, T., Tibshirani, R., et al. (2013). *An introduction to statistical learning*, volume 112. Springer.