

	1	2	3	4	5	6
1	(1,1)	1,2	1,3	1,4	1,5	1,6
2	2,1	2,2	2,3	2,4	2,5	2,6
3	3,1	3,2	3,3	3,4	3,5	3,6
4	4,1	4,2	4,3	4,4	4,5	4,6
5	5,1	5,2	5,3	5,4	5,5	5,6
6	6,1	6,2	6,3	6,4	6,5	6,6

$$P(2) = \frac{1}{36}$$

$$P(12) = \frac{1}{36}$$

$$P(7) = \frac{6}{36} = \frac{1}{6}$$

$$P(6) = \frac{5}{36}$$

$$P(8) = \frac{5}{36}$$

Value of $E[X]$

$$E[X] = \sum_i x_i P(x_i)$$

UNCO OR DDD

1, 2, 3, 4, 5, 6

↓

↓

↓

$\frac{1}{6}$ $\frac{1}{6}$ $\frac{1}{6}$...

$$E[X] = 1 \cdot \frac{1}{6} + 2 \cdot \frac{1}{6} + 3 \cdot \frac{1}{6} + 4 \cdot \frac{1}{6} + 5 \cdot \frac{1}{6} + 6 \cdot \frac{1}{6}$$

$$= \frac{1}{6} [1 + 2 + 3 + 4 + 5 + 6]$$

$$= \frac{21}{6}$$

T

C

1

0

1

0

1

↓

$$E[X] = \frac{1}{2} \cdot 0 + \frac{1}{2} \cdot 1$$

$$= \left(\frac{1}{2} \right)$$

$$\frac{1}{2} \quad \frac{1}{2}$$

$$\text{Var}(X) = \mathbb{E}[(X - \mathbb{E}(X))^2]$$

$$\mathbb{E}(X) = \mu = m$$

$$\text{Var}(X) = \left(\sum_i (x_i - m)^2 P(x_i) \right)$$

$x_1 \quad x_2 \quad x_3$

$$= (x_1 - m)^2 \cdot P(x_1) + (x_2 - m)^2 P(x_2) + (x_3 - m)^2 P(x_3)$$

$$\sigma = \sqrt{\text{Var}(X)}$$

↓
sigma

DEVIAZIONE
STANDARD

$$n=5$$

$$P(X=0) = \binom{5}{0} \left(\frac{1}{2}\right)^0 \cdot \left(\frac{1}{2}\right)^{5-0} \quad p = \frac{1}{2} \quad (1-p) = q = \frac{1}{2}$$

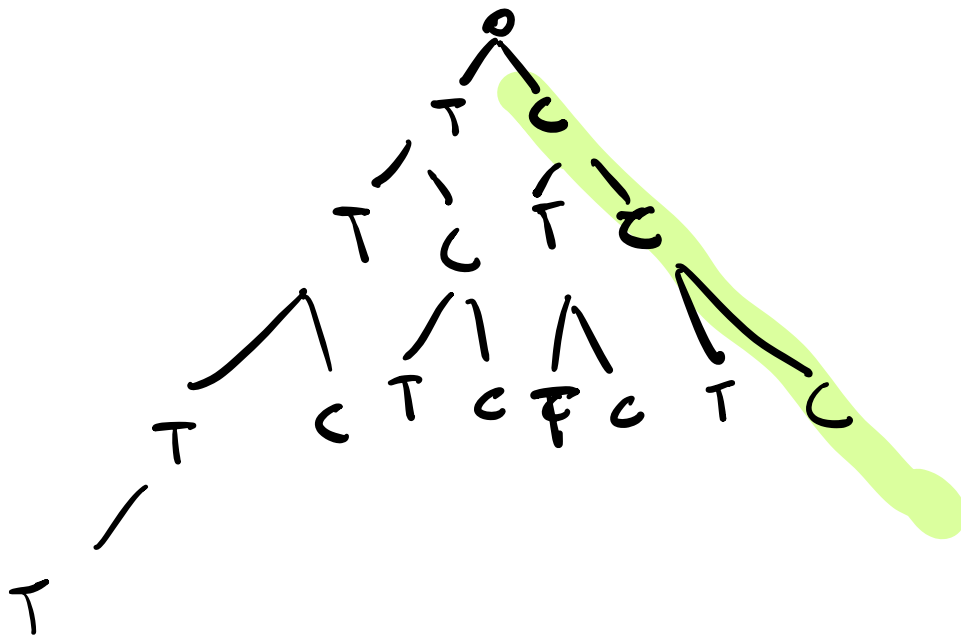
$$k=0$$

$$P(X=k) = \binom{n}{k} p^k (1-p)^{n-k} \quad \binom{n}{k} = \frac{n!}{k!(n-k)!}$$

$$P(X=0) = \frac{5!}{0!(5-0)!} \cdot \left(\frac{1}{2}\right)^0 \cdot \left(\frac{1}{2}\right)^5$$

$$P(X=0) = \frac{5!}{5!} 1 \cdot \left(\frac{1}{2}\right)^5 = \frac{1}{32}$$

$$\frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} = \frac{1}{32}$$



$$k=3 \quad 5 \quad \left(\frac{1}{2}\right)^{5-3} = \left(\frac{1}{2}\right)^2$$

$$P(X=3) = \binom{5}{3} \left(\frac{1}{2}\right)^3 \cdot \left(\frac{1}{2}\right)^{5-3}$$

$$P(X=3) = \frac{5!}{3!(5-3)!} \cdot \frac{1}{8} \cdot \frac{1}{4}$$

$$P(X=3) = \frac{(5!)}{3! \cdot 2!} \cdot \frac{1}{8} \cdot \frac{1}{4}$$

$$P(X=3) = \frac{5 \cdot 4 \cdot \cancel{3!}}{\cancel{3!} \cdot 2!} \cdot \frac{1}{8} \cdot \frac{1}{4}$$

$$P(X=3) = \frac{20}{2} \cdot \frac{1}{8} \cdot \frac{1}{4} = \frac{10}{32} = \frac{5}{16}$$

DSDB (6)

with 6 dice

$$P(X=3) = \binom{6}{3} \left(\frac{1}{6}\right)^3 \cdot \left(\frac{5}{6}\right)^3$$

$$n=6$$

$$k=3$$

$$P(X=3) = \frac{6!}{3!(6-3)!} \cdot \left(\frac{1}{6}\right)^3 \cdot \left(\frac{5}{6}\right)^3$$

$$P(6) = \frac{1}{6}$$

$$Q = 1 - P = 1 - \frac{1}{6} = \frac{5}{6}$$

$$P(X=3) = \frac{\cancel{6} \cdot \cancel{5} \cdot \cancel{4} \cdot \cancel{3}!}{\cancel{3}! \cdot \cancel{3} \cdot \cancel{2} \cdot \cancel{1}} \left(\frac{1}{6}\right)^3 \cdot \left(\frac{5}{6}\right)^3$$

$$P(X=3) = 20 \cdot \frac{1}{6^3} \cdot \frac{5^3}{6^3} = \frac{20 \cdot 5^3}{6^6}$$

$$P(X=k) = \frac{\lambda^k e^{-\lambda}}{k!}, \quad k = 0, 1, 2, \dots$$

$$\lambda = 5$$

$$k = 3$$

$$P(X=3) = \frac{5^3 e^{-5}}{3!}$$