

	1	2	3	4	5	6	
1	(1,1)	1,2	1,3	1,4	1,5	1,6	
2	2,1	2,2	2,3	2,4	2,5	2,6	
3	3,1	3,2	3,3	3,4	3,5	3,6	
4	4,1	4,2	4,3	4,4	4,5	4,6	
5	5,1	5,2	5,3	5,4	5,5	5,6	
6	6,1	6,2	6,3	6,4	6,5	6,6	

$$P(2) = \frac{1}{36}$$

$$P(12) = \frac{1}{36}$$

$$P(7) = \frac{6}{36} = \frac{1}{6}$$

$$P(6) = \frac{5}{36}$$

$$P(8) = \frac{5}{36}$$

Value of $E[X]$

$$E[X] = \sum_i x_i p(x_i)$$

UNIFORM DISTRIB

$$\begin{array}{cccccc} 1, 2, 3, 4, 5, 6 \\ | \quad | \quad | \\ \frac{1}{6} \quad \frac{1}{6} \quad \frac{1}{6} \quad \cdot \quad \cdot \quad \cdot \end{array}$$

$$E[X] \leq 1 \cdot \frac{1}{6} + 2 \cdot \frac{1}{6} + 3 \cdot \frac{1}{6} + 4 \cdot \frac{1}{6} + 5 \cdot \frac{1}{6} + 6 \cdot \frac{1}{6}$$

$$= \frac{1}{6} [1 + \underbrace{2 + 3 + 4 + 5 + 6}]$$

$$< \frac{21}{6}$$

$$\begin{array}{cc} T & C \\ \frac{1}{2} & 0 \\ | & \downarrow \end{array}$$

$$\begin{aligned} E[X] &\leq \frac{1}{2} \cdot 0 + \frac{1}{2} \cdot 1 \\ &= \frac{1}{2} \end{aligned}$$

$$\frac{1}{2} \quad \frac{1}{2}$$

$$Var(X) = E[(X - E(X))^2]$$

$$E(X) = \mu = m$$

$$Var(X) = \sum_i (x_i - m)^2 p(x_i)$$

$x_1 \quad x_2 \quad x_3$

$$= (x_1 - m)^2 \cdot p(x_1) + (x_2 - m)^2 p(x_2) + \\ (x_3 - m)^2 p(x_3)$$

$$\sigma = \sqrt{Var(X)}$$

\downarrow

sigma

DEVIAZIONE
STANDAR

$M=5$

$$P(X=0) = \binom{5}{0} \left(\frac{1}{2}\right)^0 \cdot \left(\frac{1}{2}\right)^{5-0} \quad P = \frac{1}{2} \quad (1-P) = \frac{1}{2}$$

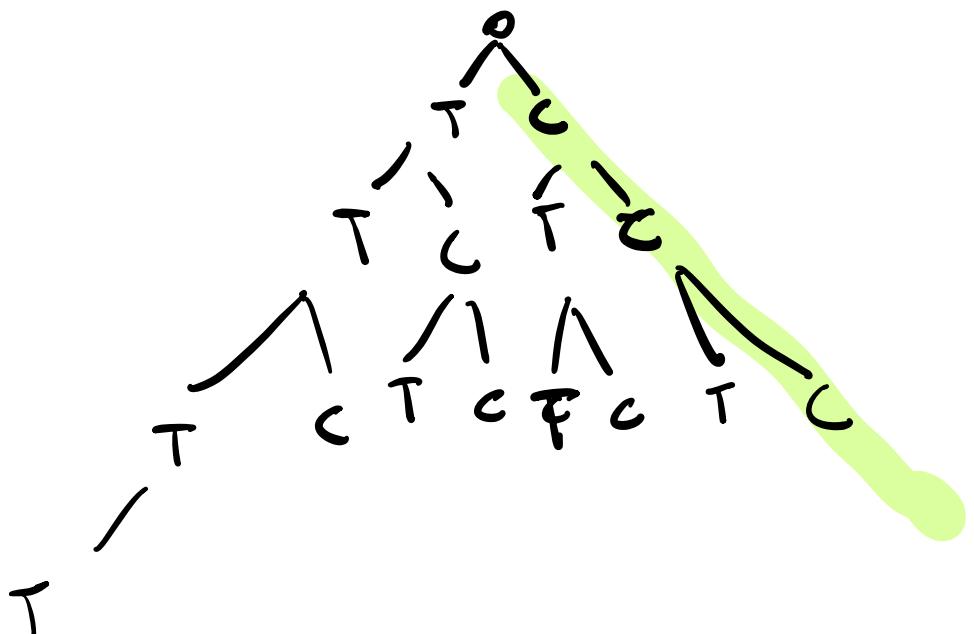
$k=0$

$$P(X=k) = \binom{n}{k} P^k (1-P)^{n-k} \quad \binom{n}{k} = \frac{n!}{k!(n-k)!}$$

$$P(X \geq 0) = \frac{s!}{0!(s-0)!} \cdot \left(\frac{1}{2}\right)^0 \cdot \left(\frac{1}{2}\right)^s$$

$$P(X \geq 5) = \sum_{s=5}^{10} 1 \cdot \left(\frac{1}{2}\right)^5 = \frac{1}{32}$$

$$\frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} = \frac{1}{32}$$



$$k=3$$

$$5$$

$$\left(\frac{1}{2}\right)^{5-3} = \left(\frac{1}{2}\right)^2$$

$$P(X \leq 3) \leq \binom{5}{3} \left(\frac{1}{2}\right)^3 \cdot \left(\frac{1}{2}\right)^{5-3}$$

$$P(X \leq 3) \leq \frac{5!}{3!(5-3)!} \cdot \frac{1}{8} \cdot \frac{1}{4}$$

$$P(X \leq 3) = \frac{5!}{3! 2!} \cdot \frac{1}{8} \cdot \frac{1}{4}$$

$$P(X \leq 3) \leq \frac{5 \cdot 4 \cdot 3!}{3! 2!} \cdot \frac{1}{8} \cdot \frac{1}{4}$$

$$P(X \leq 3) = \frac{20}{2} \cdot \frac{1}{6} \cdot \frac{1}{6} = \frac{10}{32} = \frac{5}{16}$$

DDDD

6

Würfel würfel

$$P(X \leq 3) = \binom{6}{3} \left(\frac{1}{6}\right)^3 \left(\frac{5}{6}\right)^3 \quad m=6 \\ \quad k=3$$

$$P(X=3) = \frac{6!}{3! (6-3)!} \cdot \left(\frac{1}{6}\right)^3 \left(\frac{5}{6}\right)^3 \quad P(6) = \frac{1}{6} \\ \quad Q = 1 - P = 1 - \frac{1}{6} = \frac{5}{6}$$

$$P(X=3) = \frac{6 \cdot 5 \cdot 4 \cdot 3!}{3! \cdot 3 \cdot 2 \cdot 1} \left(\frac{1}{6}\right)^3 \left(\frac{5}{6}\right)^3$$

$$P(X=3) = 20 \cdot \frac{1}{6^3} \cdot \frac{5^3}{6^3} = \frac{20 \cdot 5^3}{6^6}$$

$$P(X = k) = \frac{\lambda^k e^{-\lambda}}{k!}, \quad k = 0, 1, 2, \dots$$

$$\lambda = 5$$

$$k = 3$$

$$P(X = 3) = \frac{5^3 e^{-5}}{3!}$$