# Program Structures and Algorithms Spring 2023(SEC – 8)

NAME: Natarajan Lekshmi Narayana Pillai

NUID: 002766033

## **Assignment 6**

#### Task:

In this assignment, your task is to determine--for sorting algorithms--what is the best predictor of total execution time: comparisons, swaps/copies, hits (array accesses), or something else.

You will run the benchmarks for merge sort, (dual-pivot) quick sort, and heap sort. You will sort randomly generated arrays of between 10,000 and 256,000 elements (doubling the size each time). If you use the *SortBenchmark*, as I expect, the number of runs is chosen for you. So, you can ignore the instructions about setting the number of runs.

For each experiment (a sort method of a given size), you will run it twice: once for the instrumentation, once (without instrumentation) for the timing.

Of course, you will be using the *Benchmark* and/or *Timer* classes, as you did in a previous assignment.

You must support your (clearly stated) conclusions with evidence from the benchmarks (you should provide log/log charts and spreadsheets typically).

All of the code to count comparisons, swaps/copies, and hits, is already implemented in the *InstrumentedHelper* class. You can see examples of the usage of this kind of analysis in:

- src/main/java/edu/neu/coe/info6205/util/SorterBenchmark.java
- src/test/java/edu/neu/coe/info6205/sort/linearithmic/MergeSortTest.java
- src/test/java/edu/neu/coe/info6205/sort/linearithmic/QuickSortDualPivotTest.java
- src/test/java/edu/neu/coe/info6205/sort/elementary/HeapSortTest.java (you will have to refresh your repository for HeapSort).

The configuration for these benchmarks is determined by the *config.ini* file. It should be reasonably easy to figure out how it all works. The config.ini file should look something like this:

```
[sortbenchmark]
version = 1.0.0 (sortbenchmark)
[helper]
instrument = true
seed = 0
cutoff =
[instrumenting]
# The options in this section apply only if instrument (in [helper]) is set to true.
swaps = true
compares = true
copies = true
fixes = false
hits = true
# This slows everything down a lot so keep this small (or zero)
inversions = 0
[benchmarkstringsorters]
words = 1000 # currently ignored
runs = 20 # currently ignored
mergesort = true
timsort = false
quicksort = false
introsort = false
insertionsort = false
bubblesort = false
quicksort3way = false
quicksortDualPivot = true
randomsort = false
[benchmarkdatesorters]
timsort = false
n = 100000
[mergesort]
insurance = false
nocopy = true
[shellsort]
n = 100000
[operationsbenchmark]
nlargest = 10000000
repetitions = 10
```

There is no config.ini entry for heapsort. You will have to work that one out for yourself.

The number of runs is actually determined by the problem sizes using a fixed formula.

One more thing: the sizes of the experiments are actually defined in the command line (if you are running in IntelliJ/IDEA then, under *Edit Configurations* for the *SortBenchmark*, enter 10000 20000 etc. in the box just above *CLI arguments to your application*).

You will also need to edit the SortBenchmark class. Insert the following lines before the introsort section:

```
if (isConfigBenchmarkStringSorter("heapsort")) {
    Helper<String> helper = HelperFactory.create("Heapsort", nWords, config);
    runStringSortBenchmark(words, nWords, nRuns, new HeapSort<>(helper), timeLoggersLinearithmic);
}
```

Then you can add the following extra line into the config.ini file (again, before the introsort line (which is 25 for me):

```
heapsort = true
```

Remember that your job is to determine the best predictor: that will mean the graph of the appropriate observation will match the graph of the timings most closely.

# **Relationship Conclusion using evidence:**

# **Heap Sort**

N	•	Time (Without Instrumentation)	Time	e (With Instrumentation)	<b>7</b>	Hits 🔻	Swaps	•	Copies	-	Compares 🕶
100	00	3.4340	4	337.1946	5	967590.2	124206	5.9		0	235381.3
200	00	6.1577	5	1445.33575	5	2094863	268364	1.8		0	510701.7
400	00	12.6593	8	6540.14478	8	4509677	576721	L.5		0	1101395.6
800	00	29.3191	8	15120.32783	1	9660326	12336	11		0	2362941.6
1600	00	64.3457	9	54840.79588	8	2.06E+07	26271	01		0	5045953.4

## **Quick Sort**

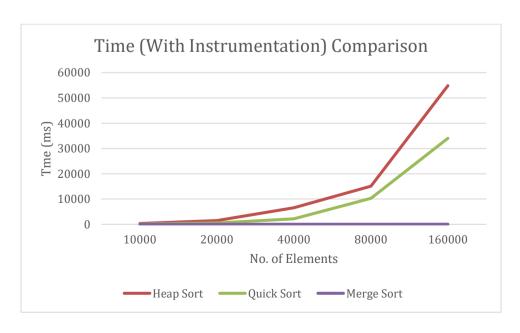
N	~	Time (Without Instrumentation) -	Time (With Instrumentation)	Hits <b>▼</b>	Swaps -	Copies 🔻	<b>Compares ▼</b>
1	.0000	11.62793	136.85341	410545.5	63211.4	0	161418.3
2	0000	6.43024	537.66496	881510.2	137246.1	0	339838.7
4	0000	10.71557	2167.36082	1940987	301192.9	0	751057.1
8	0000	21.2767	10268.29565	4150295	643995.9	0	1603625.5
16	0000	49.8276	34026.81186	8730320	1351509	0	3382965.3

# Merge Sort

N	▼ Time (Without Instrumentation) ▼	Time (With Instrumentation)	Hits 🔻	Swaps 🔻	Copies 🔻	Compares 🔻
100	00 6.41066	3.1032098	259158	0	9789.5	121494.3
200	00 6.72007	3.9345603	558088.8	0	19522.2	263023.2
400	00 13.09208	7.7190107	1196788	0	39197.1	566170.9
800	23.98621	17.8479802	2552392	0	78097.9	1212049
1600	00 51.9062	37.9105399	5425243	0	156310.7	2584173.5

1. If we look at the **times** with instrumentation for the different sorting algorithms:

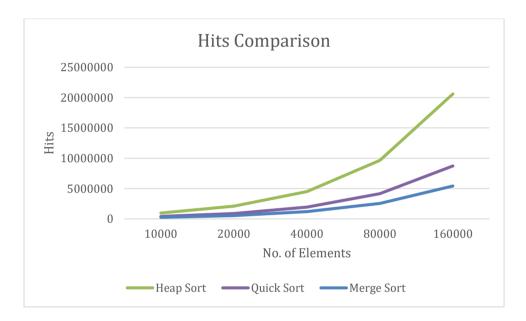
Ν		•	<b>Heap Sort</b>	•	<b>Quick Sort</b>	•	Merge Sort	•
	100	00	337.1946	55	136.853	41	3.10320	98
	200	00	1445.3357	75	537.664	96	3.93456	03
	400	00	6540.1447	78	2167.360	82	7.71901	07
	800	00	15120.327	78	10268.29	57	17.84798	02
	1600	00	54840.795	9	34026.81	19	37.91053	99



We can see that as the number of elements increase, the run time of the algorithm also increases. As seen on the graph, the run time for heap sort is the highest and the run time for merge sort is the lowest.

## 2. If we look at the number of **hits** for the different sorting algorithms:

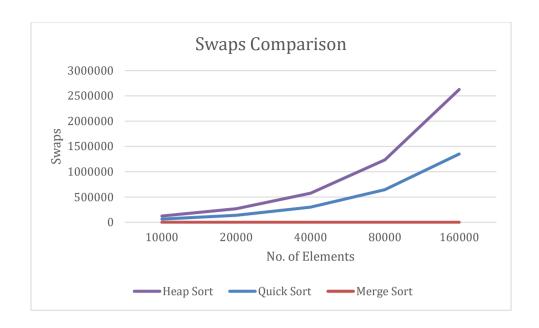
N	Heap Sort	Quick Sort	Merge Sort
10000	967590.2	410545.5	259158
20000	2094862.6	881510.2	558088.8
40000	4509677.2	1940986.8	1196788.4
80000	9660326.4	4150295.2	2552391.6
160000	2.06E+07	8730320.2	5425242.8



We can see that as the as the number of elements increase, the number of hits for each algorithm increases. As seen on the graph, the number of hits for heap sort is the highest and the number of hits for merge sort is the lowest. We can also see that the number of hits for quick sort is just less than half of heap sort.

## 3. If we look at the number of **swaps** for the different sorting algorithms:

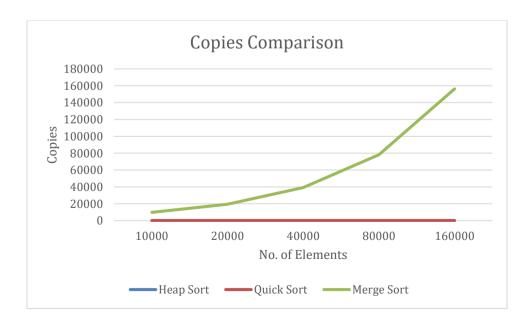
N	Heap Sort	Quick Sort	Merge Sort
10000	124206.9	63211.4	0
20000	268364.8	137246.1	0
40000	576721.5	301192.9	0
80000	1233610.8	643995.9	0
160000	2627100.5	1351508.5	0



We can see that as the number of elements increase, the number of swaps also increases. As seen on the graph, the number of swaps for heap sort is the highest and the number of swaps for quick sort is the lowest. This is not the case for merge sort which does not do any swaps. Therefore, the values of merge sort for number of swaps is 0.

# 4. If we look at the number of **copies** for the different sorting algorithms:

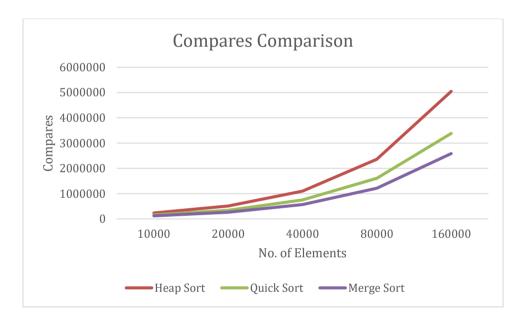
N	Heap Sort	Quick Sort	Merge Sort
10000	0	0	9789.5
20000	0	0	19522.2
40000	0	0	39197.1
80000	0	0	78097.9
160000	0	0	156310.7



We can see that as the number of elements increase, the number of copies increase for merge sort. Heap sort and quick sort do not have any copies. Therefore, the values of heap sort and quick sort for number of copies is 0.

## 5. If we look at the number of **compares** for the different sorting algorithms:

N	<b>Heap Sort</b>	Quick Sort	Merge Sort
10000	235381.3	161418.3	121494.3
20000	510701.7	339838.7	263023.2
40000	1101395.6	751057.1	566170.9
80000	2362941.6	1603625.5	1212049
160000	5045953.4	3382965.3	2584173.5



We can see that as the number of elements increase, the number of compares for each algorithm increases. As seen on the graph, the number of compares for heap sort is the highest, and the number of compares for merge sort is the lowest.

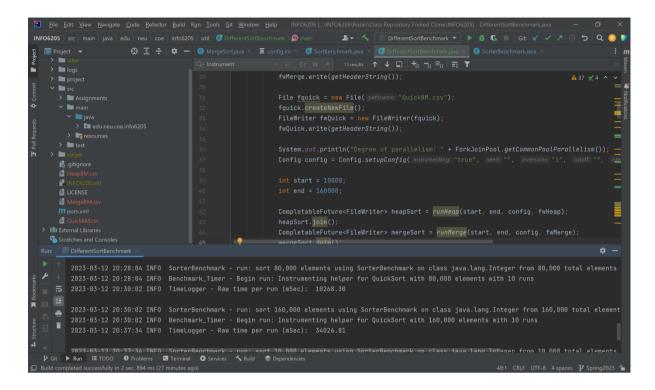
#### **Conclusion:**

The best predictor of total execution time among heap sort, quick sort, and merge sort would depend on several factors such as the size of the input, the distribution of the data, and the implementation of the algorithm. In general, an algorithm's total execution time can be significantly impacted by the quantity of comparisons, swaps/copies, and hits (array accesses). Certain algorithms, might be more susceptible to one factor than others.

- 1. Due to the low number of swaps and copies in heap sort, the number of comparisons and array accesses can serve as reliable indicators of the execution time.
- 2. Since quick sort can have a large number of swaps, the number of swaps may be a better predictor of total execution time than the number of comparisons or array accesses.
- 3. Since merge sort has a relatively small number of swaps/copies, the number of comparisons and array accesses can be good predictors of the total execution time.

In conclusion, the best predictor of total execution time among heap sort, quick sort, and merge sort would depend on various factors. While the amount of swaps may be a stronger predictor for quick sort, the number of comparisons and hits (array accesses) may be effective predictors for heap sort and merge sort.

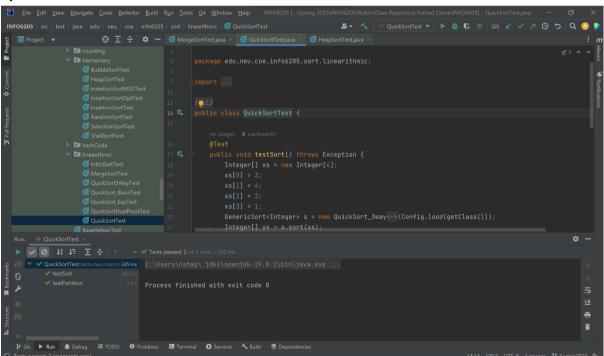
## **Output Screenshot:**



#### **Unit Test Screenshot:**

#### **Heap Sort**

## **Quick Sort**



## **Merge Sort**

