Table 1: Additional swap gates and circuit depth, $n\,=\,5$

benchmark	g	d	layout	s_B	s_S	s_L	Δs_B	Δs_S	d_B	d_S	d_L	Δd_B	Δd_S
ghz	7	7	full_20_1	0	0	0	nan	nan	7	7	7	0	0
ghz	7	7	$line_20_1$	0	0	18	nan	nan	7	7	9	-28.57	-28.57
ghz	7	7	full_10_2	0	0	0	nan	nan	7	7	7	0	0
ghz	7	7	full_7_3	0	0	0	nan	nan	7	7	7	0	0
ghz	7	7	$grid_{-9}_{-2}$	6	0	6	0	nan	13	7	8	38.46	-14.29
ghz	7	7	grid_8_3	6	3	3	50	0	13	10	8	38.46	20
ghz	7	7	ring_10_2	0	0	9	nan	nan	7	7	8	-14.29	-14.29
ghz	7	7	ring_7_3	0	3	9	nan	-200	7	10	8	-14.29	20
ghz	7	7	t_horizontal_5_4	9	3	6	33.33	-100	16	10	9	43.75	10
ghz	7	7	t_vertical_5_4	9	3	6	33.33	-100	16	10	9	43.75	10
ghz	7	7	ring_5_4	0	0	9	nan	nan	7	7 7	8 7	-14.29	-14.29
ghz	7 7	7 7	full_5_4 grid_6_4	0	0	$0 \\ 3$	nan 50	nan	7 13	7	8	$0 \\ 38.46$	0 -14.29
ghz	36	11	grid_0_4 full_20_1	6 0	$0 \\ 0$	o		nan	13 11	11	8 11	38.40 0	-14.29 0
dj	36	11	line_20_1	36	6	6	nan 83.33	$ \begin{array}{c} \text{nan} \\ 0 \end{array} $	40	$\frac{11}{24}$	$\frac{11}{14}$	65	41.67
dj dj	36	11	full_10_2	0	3	0	nan	100	11	$\frac{24}{17}$	11	0	35.29
dj	36	11	full_7_3	0	0	0	nan	nan	11	11	11	0	0
dj	36	11	grid_9_2	9	3	0	100	100	21	14	11	47.62	21.43
dj	36	11	grid_8_3	18	3	3	83.33	0	$\frac{21}{22}$	17	12	45.45	29.41
dj	36	11	ring_10_2	36	3	3	91.67	0	40	17	12	70	29.41
dj	36	11	ring_7_3	$\frac{33}{24}$	3	3	87.5	0	30	16	12	60	25
dj	36	11	t_horizontal_5_4	24	3	3	87.5	0	37	14	12	67.57	14.29
dj	36	11	$t_{vertical_5_4}$	24	3	3	87.5	0	37	18	12	67.57	33.33
dj	36	11	$ring_5_4$	9	3	3	66.67	0	24	17	12	50	29.41
d j	36	11	$full_5_4$	0	0	0	nan	nan	11	11	11	0	0
ďj	36	11	$grid_6_4$	18	3	3	83.33	0	22	14	12	45.45	14.29
graphstate	50	22	full_20_1	0	0	0	nan	nan	22	22	22	0	0
graphstate	50	22	$line_20_1$	12	9	12	0	-33.33	32	28	21	34.38	25
graphstate	50	22	$full_10_2$	0	0	0	nan	nan	22	22	22	0	0
graphstate	50	22	$full_7_3$	0	0	0	nan	nan	22	22	22	0	0
graphstate	50	22	$grid_9_2$	15	3	6	60	-100	37	25	20	45.95	20
graphstate	50	22	$grid_8_3$	15	9	9	40	0	34	32	21	38.24	34.38
$\operatorname{graphstate}$	50	22	$ring_10_2$	12	6	9	25	-50	32	25	20	37.5	20
graphstate	50	22	$ring_7_3$	6	6	9	-50	-50	24	28	20	16.67	28.57
graphstate	50	22	$t_{horizontal_5_4}$	12	9	9	25	0	35	28	20	42.86	28.57
graphstate	50	22	t_vertical_5_4	12	9	9	25	0	35	28	20	42.86	28.57
graphstate	50	22	$ring_5_4$	9	0	9	0	nan	31	22	18	41.94	18.18
graphstate	50	22	full_5_4	0	0	0	nan	nan	22	22	22	0	0
graphstate	50	22	grid_6_4	6	3	9	-50	-200	32	25	22	31.25	12
qft	71	38	full_20_1	0	0	0	nan	nan	38	38	38	0	0
qft	71	38	line_20_1	72	24	24	66.67	0	92	57	42	54.35	26.32
qft	71 71	$\frac{38}{38}$	full_10_2 full_7_3	0	$0\\12$	$0 \\ 0$	nan	nan 100	$\frac{38}{38}$	$\frac{38}{55}$	$\frac{38}{38}$	$0 \\ 0$	$0 \\ 30.91$
qft qft	71	38	grid_9_2	39	$\frac{12}{15}$	$\frac{0}{21}$	nan 46.15	-40	30 74	59	38 41	44.59	30.51
qft	71	$\frac{38}{38}$	grid_8_3	33	12	18	45.45	- 40 -50	70	47	34	51.43	27.66
qft	71	$\frac{38}{38}$	ring_10_2	72	15	$\frac{16}{24}$	66.67	-60	92	60	$\frac{34}{42}$	54.35	30
qft	71	$\frac{38}{38}$	ring_7_3	51	15	24	52.94	-60	77	60	$\frac{42}{42}$	45.45	30
qft	71	38	t_horizontal_5_4	48	15	$\frac{24}{24}$	50	-60	82	60	42	48.78	30
qft	71	38	t_vertical_5_4	48	18	24	50	-33.33	82	59	42	48.78	28.81
qft	71	38	ring_5_4	27	15	18	33.33	-20	65	53	43	33.85	18.87
qft	71	38	full_5_4	0	0	0	nan	nan	38	38	38	0	0
qft	71	38	grid_6_4	33	12	18	45.45	-50	70	51	34	51.43	33.33
wstate	73	45	full_20_1	0	0	0	nan	nan	45	45	45	0	0
wstate	73	45	$line_20_1$	0	0	15	nan	nan	45	45	33	26.67	26.67
wstate	73	45	$full_10_2$	0	0	0	nan	nan	45	45	45	0	0
wstate	73	45	$full_7_3$	0	0	0	nan	nan	45	45	45	0	0
wstate	73	45	$grid_9_2$	18	0	12	33.33	nan	54	45	41	24.07	8.89
wstate	73	45	$grid_8_3$	15	0	3	80	nan	51	45	46	9.8	-2.22
wstate	73	45	ring_10_2	0	0	9	nan	nan	45	45	40	11.11	11.11
wstate	73	45	$ring_{-}7_{-}3$	0	0	9	nan	nan	45	45	40	11.11	11.11
wstate	73	45	$t_{-horizontal_5_4}$	18	0	6	66.67	nan	58	45	39	32.76	13.33

benchmark	g	d	layout	s_B	s_S	s_L	Δs_B	Δs_S	d_B	d_S	d_L	Δd_B	Δd_S
wstate	73	45	$t_{vertical_5_4}$	18	0	6	66.67	nan	58	45	39	32.76	13.33
wstate	73	45	$ring_5_4$	0	0	9	nan	nan	45	45	40	11.11	11.11
wstate	73	45	$full_5_4$	0	0	0	nan	nan	45	45	45	0	0
wstate	73	45	$grid_6_4$	15	0	3	80	nan	51	45	46	9.8	-2.22
qftentangled	78	42	full_20_1	0	0	0	nan	nan	42	42	42	0	0
qftentangled	78	42	$line_20_1$	72	24	36	50	-50	96	73	50	47.92	31.51
qftentangled	78	42	full_10_2	0	0	0	nan	nan	42	42	42	0	0
qftentangled	78	42	full_7_3	0	6	0	nan	100	42	63	42	0	33.33
qftentangled	78	42	$grid_9_2$	45	18	27	40	-50	87	60	45	48.28	25
qftentangled	78 7 8	42	grid_8_3	33	15	27	18.18	-80	78	78 - 2	48	38.46	38.46
qftentangled	78	42	ring_10_2	72	24	30	58.33	-25	96	73	49	48.96	32.88
qftentangled	78 70	42	ring_7_3	51	24	30	41.18	-25	81	73 70	49	39.51	32.88
qftentangled	78 70	42	t_horizontal_5_4	60	21	33	45	-57.14	90	76	48	46.67	36.84
qftentangled	78 70	42	t_vertical_5_4	60	24	33	45	-37.5	90	73	48	46.67	34.25
qftentangled	78 70	42	ring_5_4	27	15	30	-11.11	-100	69	61	49	28.99	19.67
qftentangled	78 78	$\frac{42}{42}$	full_5_4 grid_6_4	0	0 21	$0 \\ 27$	nan 18.18	nan	42 78	42 76	42 48	$0 \\ 38.46$	$0 \\ 36.84$
qftentangled	83	21	grid_0_4 full_20_1	33		0		-28.57	21	21	48 21	38.40 0	0 0
vqe	83 83	$\frac{21}{21}$	line_20_1	$0 \\ 0$	0	0 15	nan	nan	21 21	$\frac{21}{21}$	$\frac{21}{24}$	0 -14.29	0 -14.29
vqe	83 83	21	full_10_2	0	0	0	nan nan	nan	21	$\frac{21}{21}$	$\frac{24}{21}$	-14.29 0	-14. <i>2</i> 9
vqe vqe	83	21	full_7_3	0	0	0	nan	nan nan	21	21	21	0	0
vqe vqe	83	21	grid_9_2	15	0	12	20	nan	$\frac{21}{35}$	21	$\frac{21}{27}$	$\frac{0}{22.86}$	-28.57
vqe	83	$\frac{21}{21}$	grid_8_3	6	0	12	-100	nan	26	21	$\frac{21}{25}$	3.85	-19.05
vqe	83	21	ring_10_2	0	0	15	nan	nan	21	21	29	-38.1	-38.1
vqe	83	21	ring_7_3	0	0	15	nan	nan	21	$\frac{21}{21}$	$\frac{25}{29}$	-38.1	-38.1
vqe	83	21	t_horizontal_5_4	12	0	12	0	nan	33	21	$\frac{25}{25}$	24.24	-19.05
vqe	83	21	t_vertical_5_4	12	0	12	0	nan	33	21	$\frac{25}{25}$	24.24	-19.05
vqe	83	21	$ring_5_4$	0	0	15	nan	nan	21	21	29	-38.1	-38.1
vqe	83	$\overline{21}$	full_5_4	0	0	0	nan	nan	21	21	21	0	0
vqe	83	21	$grid_6_4$	6	0	6	0	nan	26	21	21	19.23	0
qaoa	95	31	full_20_1	0	0	0	nan	nan	31	31	31	0	0
qaoa	95	31	$line_20_1$	48	12	18	62.5	-50	106	42	39	63.21	7.14
qaoa	95	31	$full_10_2$	0	0	0	nan	nan	31	31	31	0	0
qaoa	95	31	$full_{-}7_{-}3$	0	6	0	nan	100	31	47	31	0	34.04
qaoa	95	31	$grid_9_2$	9	9	21	-133.33	-133.33	37	58	48	-29.73	17.24
qaoa	95	31	$grid_8_3$	6	3	9	-50	-200	31	42	38	-22.58	9.52
qaoa	95	31	$ring_10_2$	48	15	27	43.75	-80	106	64	45	57.55	29.69
qaoa	95	31	$ring_7_3$	24	9	27	-12.5	-200	54	48	45	16.67	6.25
qaoa	95	31	$t_{horizontal_5_4}$	33	9	24	27.27	-166.67	100	48	45	55	6.25
qaoa	95	31	$t_{vertical_5_4}$	33	9	24	27.27	-166.67	100	48	45	55	6.25
qaoa	95	31	$ring_5_4$	18	0	27	-50	nan	53	31	45	15.09	-45.16
qaoa	95	31	full_5_4	0	0	0	nan	nan	31	31	31	0	0
qaoa	95	31	$grid_{-}6_{-}4$	6	3	12	-100	-300	31	42	36	-16.13	14.29
realamprandom	130	37	full_20_1	0	0	0	nan	nan	37	37	37	0	0
realamprandom	130	37	line_20_1	180	69	93	48.33	-34.78	206	113	59	71.36	47.79
realamprandom	130	37	full_10_2	0	0	0	nan	nan	37	37	37	0	0
realamprandom	130	37	full_7_3	0	42	0	nan	100	37	111	37	0	66.67
realamprandom	130	37	grid_9_2	96	42	42	56.25	0	145	97	66	54.48	31.96
realamprandom	130	37	grid_8_3	75	48	45	40	6.25	143	107	60	58.04	43.93
realamprandom	130	37 27	ring_10_2	180	48	60 60	66.67	-25 16.67	206	102	66 66	67.96	35.29
realamprandom	130	$\frac{37}{27}$	ring_7_3	$\frac{120}{117}$	72	60 60	50 48 72	16.67	129	128 107	66 66	48.84	48.44
realamprandom	130	$\frac{37}{27}$	t_horizontal_5_4	$\frac{117}{117}$	48 51	60 60	$48.72 \\ 48.72$	-25 17.65	185	107	66 66	64.32 64.32	38.32
realamprandom realamprandom	$\frac{130}{130}$	$\frac{37}{37}$	t_vertical_5_4	$\begin{array}{c} 117 \\ 57 \end{array}$	$\frac{51}{45}$	60	48.72 -5.26	-17.65 -33.33	185 86	109 94	66	$\frac{64.32}{23.26}$	39.45 29.79
realamprandom realamprandom	130 130	$\frac{37}{37}$	$ ring_5_4 $ $ full_5_4 $	0	45	0			80 37	$\frac{94}{37}$	37	23.20 0	29.79 0
realamprandom realamprandom	130 130	$\frac{37}{37}$	grid_6_4	75	$\frac{0}{42}$	$\frac{0}{45}$	$ \begin{array}{c} \text{nan} \\ 40 \end{array} $	nan -7.14	143	80	57 60	58.04	$\frac{0}{25}$
twolocalrandom	130	$\frac{37}{37}$	full_20_1	0	0	0 - 40	nan	nan	$\frac{145}{37}$	37	37	0 0	0
twolocalrandom	130	37 37	line_20_1	180	69	93	48.33	-34.78	206	113	59	71.36	47.79
twolocalrandom	130	37 37	full_10_2	0	09	95	nan	-34.76 nan	$\frac{200}{37}$	$\frac{113}{37}$	37	0	0
twolocalrandom	130	37 37	full_7_3	0	15	0	nan	100	37	74	37	0	50
twolocalrandom	130	37	grid_9_2	96	$\frac{13}{42}$	42	56.25	0	145	100	66	54.48	34
- worocarrandon	100	01	5114-9-2	50	14	14	55.25	•	140	100	50	01.10	O I

benchmark	g	d	layout	s_B	s_S	s_L	Δs_B	Δs_S	d_B	d_S	d_L	Δd_B	Δd_S
twolocalrandom	130	37	grid_8_3	75	45	45	40	0	143	95	60	58.04	36.84
two local random	130	37	ring_10_2	180	72	60	66.67	16.67	206	126	66	67.96	47.62
two local random	130	37	$ring_7_3$	120	48	60	50	-25	129	102	66	48.84	35.29
two local random	130	37	$t_{horizontal_5_4}$	117	72	60	48.72	16.67	185	113	66	64.32	41.59
two local random	130	37	$t_{\text{-}}vertical_{\text{-}}5_{\text{-}}4$	117	48	60	48.72	-25	185	107	66	64.32	38.32
two local random	130	37	$ring_5_4$	57	45	60	-5.26	-33.33	86	102	66	23.26	35.29
two local random	130	37	$full_5_4$	0	0	0	nan	nan	37	37	37	0	0
two local random	130	37	$grid_6_4$	75	39	45	40	-15.38	143	95	60	58.04	36.84
su2random	150	41	$full_20_1$	0	0	0	nan	nan	41	41	41	0	0
su2random	150	41	$line_20_1$	180	72	93	48.33	-29.17	219	135	63	71.23	53.33
su2random	150	41	full_10_2	0	15	0	nan	100	41	81	41	0	49.38
su2random	150	41	full_7_3	0	48	0	nan	100	41	108	41	0	62.04
su2random	150	41	$grid_9_2$	96	39	42	56.25	-7.69	155	102	70	54.84	31.37
su2random	150	41	$grid_8_3$	75	42	45	40	-7.14	155	108	64	58.71	40.74
su2random	150	41	ring_10_2	180	48	60	66.67	-25	219	115	70	68.04	39.13
su2random	150	41	ring_7_3	120	51	60	50	-17.65	138	120	70 70	49.28	41.67
su2random	150	41	t_horizontal_5_4	117	72	60	48.72	16.67	198	135	70 70	64.65	48.15
su2random	150	41	t_vertical_5_4	117	48	60 60	48.72	-25 25	198	110	70 70	64.65	36.36
su2random su2random	150 150	41 41	$ring_5_4$ $full_5_4$	57 0	48 0	60 0	-5.26	-25	$\frac{96}{41}$	115 41	70 41	$\frac{27.08}{0}$	39.13 0
su2random su2random					39	45	nan 40	nan 15.20	$\frac{41}{155}$	90	64	58.71	$\frac{0}{28.89}$
	150 154	41 58	$grid_6_4$ $full_20_1$	75 0	39 0	$\frac{45}{0}$	au nan	-15.38	155 58	90 58	64 58	58.71 0	28.89
qnn	154 154	58	line_20_1	120	48	84	30	nan -75	172	$\frac{38}{127}$	80	53.49	37.01
qnn	154	58	full_10_2	0	0	0	nan		58	58	58	0	0
qnn qnn	154	58	full_7_3	0	9	0	nan	nan 100	58	87	58	0	33.33
qnn	154	58	grid_9_2	63	30	66	-4.76	-120	132	103	84	36.36	18.45
qnn	154	58	grid_8_3	48	30	51	-6.25	-70	122	100	78	36.07	22
qnn	154	58	ring_10_2	120	39	66	45	-69.23	172	122	84	51.16	31.15
qnn	154	58	ring_7_3	93	36	66	29.03	-83.33	122	122	84	31.15	31.15
qnn	154	58	t_horizontal_5_4	81	39	66	18.52	-69.23	172	131	84	51.16	35.88
qnn	154	58	$t_{vertical_5_4}$	81	48	66	18.52	-37.5	172	127	84	51.16	33.86
qnn	154	58	$ring_5_4$	48	30	nan	nan	nan	95	98	nan	nan	nan
qnn	154	58	full_5_4	0	0	0	nan	nan	58	58	58	0	0
qnn	154	58	$grid_{-}6_{-}4$	48	30	51	-6.25	-70	122	103	78	36.07	24.27
portfolioqaoa	195	72	full_20_1	0	0	0	nan	nan	72	72	72	0	0
portfolioqaoa	195	72	$line_20_1$	180	66	93	48.33	-40.91	255	159	90	64.71	43.4
portfolioqaoa	195	72	$full_10_2$	0	0	0	nan	nan	72	72	72	0	0
portfolioqaoa	195	72	$full_7_3$	0	0	0	nan	nan	72	72	72	0	0
portfolioqaoa	195	72	$grid_9_2$	96	39	69	28.12	-76.92	199	132	121	39.2	8.33
portfolioqaoa	195	72	$grid_8_3$	75	39	57	24	-46.15	187	145	91	51.34	37.24
portfolioqaoa	195	72	$ring_10_2$	180	51	87	51.67	-70.59	255	174	110	56.86	36.78
portfolioqaoa	195	72	ring73	120	51	87	27.5	-70.59	157	161	110	29.94	31.68
portfolioqaoa	195	72	t_horizontal_5_4	117	48	87	25.64	-81.25	252	153	110	56.35	28.1
portfolioqaoa	195	72	t_vertical_5_4	117	51	87	25.64	-70.59	252	164	110	56.35	32.93
portfolioqaoa	195	72	ring_5_4	57	45	87	-52.63	-93.33	116	129	110	5.17	14.73
portfolioqaoa	195	72 70	full_5_4	0	0	0	nan	nan	72	72	72	0	0
portfolioqaoa	195	72	grid_6_4	75	39	57	24	-46.15	187	132	91	51.34	31.06
random	195	117	full_20_1	0	0	$0 \\ 30$	nan	nan	97	97	97	0	0
random	195	117	line_20_1	63	12		52.38	-150	160	106	99 07	38.12	6.6
random random	195 195	117 117	full_10_2 full_7_3	$0 \\ 0$	6 12	$0 \\ 0$	nan	100 100	97 97	141 126	97 97	0	$31.21 \\ 23.02$
random random	$\frac{195}{195}$	$\frac{117}{117}$	grid_9_2	30	12 12	$\frac{0}{27}$	nan 10	-125	$\frac{97}{114}$	$\frac{120}{117}$	97 111	$\frac{0}{2.63}$	$\frac{23.02}{5.13}$
random	195	117	grid_9_2 grid_8_3	36	$\frac{12}{12}$	21	41.67	-125 -75	162	106	106	$\frac{2.03}{34.57}$	0
random	195	117	ring_10_2	63	$\frac{12}{12}$	66	-4.76	-450	162	106	121	24.38	-14.15
random	195	117	$ring_{-7}_{-3}$	60	12	66	-10	-450	157	106	121	24.93	-14.15
random	195	117	t_horizontal_5_4	36	12	66	-83.33	-450	151	106	121	19.87	-14.15
random	195	117	t_vertical_5_4	36	12	66	-83.33	-450	151	106	121	19.87	-14.15
random	195	117	ring_5_4	75	42	81	-8	-92.86	180	158	132	26.67	16.46
random	195	117	full_5_4	0	0	0	nan	nan	117	117	117	0	0
random	195	117	$grid_{-}6_{-}4$	66	33	45	31.82	-36.36	165	149	116	29.7	$\frac{0}{22.15}$
portfoliovqe	310	107	full_20_1	0	0	0	nan	nan	107	107	107	0	0
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Table 1: Additional swap gates and circuit depth, $n\,=\,5$

benchmark	g	d	layout	s_B	s_S	s_L	Δs_B	Δs_S	d_B	d_S	d_L	Δd_B	Δd_S
portfoliovqe	310	107	line_20_1	180	69	90	50	-30.43	242	187	126	47.93	32.62
portfoliovqe	310	107	$full_10_2$	0	0	0	nan	nan	107	107	107	0	0
portfoliovqe	310	107	$full_7_3$	0	21	0	nan	100	107	158	107	0	32.28
portfoliovqe	310	107	$grid_9_2$	96	42	57	40.62	-35.71	209	154	111	46.89	27.92
portfoliovqe	310	107	$grid_8_3$	75	39	48	36	-23.08	192	164	117	39.06	28.66
portfoliovqe	310	107	$ring_10_2$	180	51	93	48.33	-82.35	242	204	125	48.35	38.73
portfoliovqe	310	107	$ring_7_3$	120	48	93	22.5	-93.75	179	193	125	30.17	35.23
portfoliovqe	310	107	$t_{horizontal_5_4}$	117	69	93	20.51	-34.78	239	187	125	47.7	33.16
portfoliovqe	310	107	$t_{vertical_5_4}$	117	48	93	20.51	-93.75	239	193	125	47.7	35.23
portfoliovqe	310	107	$ring_5_4$	57	45	93	-63.16	-106.67	146	158	125	14.38	20.89
portfoliovqe	310	107	$full_5_4$	0	0	0	nan	nan	107	107	107	0	0
portfoliovqe	310	107	$grid_6_4$	75	39	48	36	-23.08	192	162	117	39.06	27.78

Table 2: Additional swap gates and circuit depth, $n=10\,$

benchmark	g	d	layout	s_B	s_S	s_L	Δs_B	Δs_S	d_B	d_S	d_L	Δd_B	Δd_S
ghz	12	12	full_20_1	0	0	0	nan	nan	12	12	12	0	0
$_{ m ghz}$	12	12	$line_20_1$	0	30	27	nan	10	12	36	15	-25	58.33
ghz	12	12	$full_10_2$	0	6	0	nan	100	12	15	12	0	20
ghz	12	12	$full_7_3$	0	3	0	nan	100	12	15	12	0	20
ghz	12	12	$grid_9_2$	12	3	27	-125	-800	24	12	19	20.83	-58.33
ghz	12	12	$grid_8_3$	9	9	18	-100	-100	21	18	18	14.29	0
ghz	12	12	$ring_10_2$	0	15	51	nan	-240	12	24	21	-75	12.5
ghz	12	12	$ring_{-}7_{-}3$	0	6	51	nan	-750	12	18	25	-108.33	-38.89
ghz	12	12	t_horizontal_5_4	18	9	18	0	-100	30	18	17	43.33	5.56
ghz	12	12	t_vertical_5_4	27	6	30	-11.11	-400	39	18	19	51.28	-5.56
ghz	12	12	ring_5_4	0	3	45	nan	-1400	12	15	21	-75 0	-40
$_{ m ghz}$	12 12	12 12	full_5_4 grid_6_4	0 9	0	$0\\12$	nan -33.33	nan	$\begin{array}{c} 12 \\ 21 \end{array}$	12 12	12 14	$0 \\ 33.33$	0 -16.67
dj	79	$\frac{12}{17}$	full_20_1	0	0	0	-55.55 nan	nan nan	$\frac{21}{17}$	17	$\frac{14}{17}$	ээ.ээ 0	0
dj dj	79	17	line_20_1	216	27	$\frac{0}{21}$	90.28	22.22	94	51	30	68.09	41.18
dj	79	17	full_10_2	0	3	0	nan	100	17	20	17	00.03	15
dj	79	17	full_7_3	48	9	9	81.25	0	70	30	22	68.57	26.67
dj	79	17	$grid_9_2$	90	12	12	86.67	0	82	38	$\frac{-}{22}$	73.17	42.11
$ ext{dj}$	79	17	grid_8_3	108	15	12	88.89	20	79	41	25	68.35	39.02
$ ext{dj}$	79	17	ring_10_2	78	21	21	73.08	0	64	46	21	67.19	54.35
dj	79	17	ring_7_3	126	18	24	80.95	-33.33	79	41	19	75.95	53.66
$\mathrm{d}\mathrm{j}$	79	17	$t_{-}horizontal_{-}5_{-}4$	150	21	15	90	28.57	88	47	26	70.45	44.68
$\mathrm{d}\mathrm{j}$	79	17	$t_{\text{vertical}}_{5_{\text{-}}4}$	135	18	15	88.89	16.67	85	51	25	70.59	50.98
$\mathrm{d}\mathrm{j}$	79	17	$ring_5_4$	60	15	18	70	-20	69	35	23	66.67	34.29
$\mathrm{d}\mathrm{j}$	79	17	$full_5_4$	36	3	9	75	-200	56	24	24	57.14	0
dj	79	17	$grid_6_4$	108	12	12	88.89	0	79	43	26	67.09	39.53
graphstate	100	22	full_20_1	0	0	0	nan	nan	22	22	22	0	0
graphstate	100	22	line_20_1	66	18	42	36.36	-133.33	56	31	29	48.21	6.45
graphstate	100	$\frac{22}{22}$	full_10_2 full_7_3	0	3	0	nan	100	22	25	$\frac{22}{26}$	0	12
graphstate graphstate	100 100	$\frac{22}{22}$	grid_9_2	$\begin{array}{c} 21 \\ 24 \end{array}$	6 0	18 27	14.29 -12.5	-200	$\frac{43}{42}$	$\frac{22}{22}$	$\frac{20}{25}$	39.53 40.48	-18.18 -13.64
graphstate	100	$\frac{22}{22}$	grid_9_2 grid_8_3	$\frac{24}{42}$	6	$\frac{27}{24}$	42.86	nan -300	60	$\frac{22}{25}$	$\frac{25}{21}$	65	-13.04 16
graphstate	100	22	ring_10_2	27	18	51	-88.89	-183.33	42	28	33	21.43	-17.86
graphstate	100	22	ring_7_3	45	12	45	0	-275	56	28	31	44.64	-10.71
graphstate	100	22	t_horizontal_5_4	54	18	54	0	-200	53	29	32	39.62	-10.34
graphstate	100	22	$t_{vertical_5_4}$	57	15	48	15.79	-220	59	26	29	50.85	-11.54
graphstate	100	22	$ring_5_4$	24	6	42	-75	-600	50	29	28	44	3.45
graphstate	100	22	$full_5_4$	18	6	9	50	-50	44	32	25	43.18	21.88
graphstate	100	22	$grid_6_4$	27	6	30	-11.11	-400	49	25	27	44.9	-8
wstate	163	90	$full_20_1$	0	0	0	nan	nan	90	90	90	0	0
wstate	163	90	line_20_1	0	0	27	nan	nan	90	90	76	15.56	15.56
wstate	163	90	full_10_2	0	3	0	nan	100	90	93	90	0	3.23
wstate	163	90	full_7_3	0	0	0	nan	nan	90	90	90	0	0
wstate	163	90	grid_9_2	$\begin{array}{c} 21 \\ 12 \end{array}$	0	30	-42.86	nan -400	$\frac{102}{99}$	90 93	$\frac{57}{65}$	44.12	36.67
wstate wstate	163 163	90 90	grid_8_3 ring_10_2	0	$\begin{array}{c} 3 \\ 21 \end{array}$	15 57	-25 nan	-400 -171.43	99	$\frac{95}{102}$	57	$34.34 \\ 36.67$	30.11 44.12
wstate	163	90	ring_7_3	0	9	66	nan	-633.33	90	96	62	31.11	35.42
wstate	163	90	t_horizontal_5_4	45	0	$\frac{30}{24}$	46.67	nan	116	90	78	32.76	13.33
wstate	163	90	t_vertical_5_4	72	3	$\frac{24}{45}$	37.5	-1400	137	93	66	51.82	29.03
wstate	163	90	$ring_5_4$	0	3	42	nan	-1300	90	93	58	35.56	37.63
wstate	163	90	full_5_4	0	0	0	nan	nan	90	90	90	0	0
wstate	163	90	$grid_{-}6_{-}4$	12	0	12	0	nan	99	90	59	40.4	34.44
vqe	168	26	full_20_1	0	0	0	nan	nan	26	26	26	0	0
vqe	168	26	$line_20_1$	0	0	27	nan	nan	26	26	33	-26.92	-26.92
vqe	168	26	$full_10_2$	0	6	0	nan	100	26	38	26	0	31.58
vqe	168	26	$full_7_3$	0	0	0	nan	nan	26	26	26	0	0
vqe	168	26	$grid_9_2$	9	0	39	-333.33	nan	31	26	33	-6.45	-26.92
vqe	168	26	$grid_8_3$	54	3	21	61.11	-600	60	35	31	48.33	11.43
vqe	168	26	ring_10_2	0	3	90	nan	-2900	26	35	45	-73.08	-28.57
vqe	168	26 26	ring_7_3	0	6	66	nan	-1000	26	44	43	-65.38	2.27
vqe	168	26	t_horizontal_5_4	51	3	30	41.18	-900	71	35	37	47.89	-5.71

Table 2: Additional swap gates and circuit depth, $n=10\,$

benchmark	g	d	layout	s_B	s_S	s_L	Δs_B	Δs_S	d_B	d_S	d_L	Δd_B	Δd_S
vqe	168	26	$t_{vertical_5_4}$	66	0	51	22.73	nan	73	26	38	47.95	-46.15
vqe	168	26	$ring_5_4$	0	3	51	nan	-1600	26	35	38	-46.15	-8.57
vqe	168	26	full_5_4	0	0	0	nan	nan	26	26	26	0	0
vqe	168	26	grid_6_4	54	0	18	66.67	nan	60	26	31	48.33	-19.23
qaoa	190	34	full_20_1	0	0	0	nan	nan	34	34	34	0	0
qaoa	190	$\frac{34}{34}$	line_20_1 full_10_2	168	30	75 0	55.36	-150	$\frac{228}{34}$	53 34	$\frac{44}{34}$	80.7	16.98
qaoa	190 190	$\frac{34}{34}$	full_7_3	0 48	0 9	$0 \\ 15$	nan 68.75	nan -66.67	$\frac{34}{138}$	54 50	34 42	69.57	16
qaoa	190	$\frac{34}{34}$	grid_9_2	63	9	78	-23.81	-766.67	145	45	46	68.28	-2.22
qaoa qaoa	190	34	grid_8_3	96	21	33	65.62	-57.14	188	53	42	77.66	$\frac{-2.22}{20.75}$
qaoa	190	34	ring_10_2	120	24	66	45	-175	154	42	48	68.83	-14.29
qaoa	190	34	ring_7_3	81	6	75	7.41	-1150	158	42	56	64.56	-33.33
qaoa	190	34	t_horizontal_5_4	129	24	114	11.63	-375	206	53	64	68.93	-20.75
qaoa	190	34	$t_{\text{vertical}}_{5}_{4}$	114	21	111	2.63	-428.57	196	53	60	69.39	-13.21
qaoa	190	34	$ring_5_4$	117	15	69	41.03	-360	191	50	60	68.59	-20
qaoa	190	34	$full_5_4$	63	9	24	61.9	-166.67	150	48	46	69.33	4.17
qaoa	190	34	$grid_6_4$	96	12	24	75	-100	188	57	42	77.66	26.32
qft	270	78	$full_20_1$	0	0	0	nan	nan	78	78	78	0	0
qft	270	78	$line_20_1$	780	168	195	75	-16.07	342	184	106	69.01	42.39
qft	270	78	$full_10_2$	0	33	0	nan	100	78	151	78	0	48.34
qft	270	78	$full_7_3$	168	63	150	10.71	-138.1	236	170	140	40.68	17.65
qft	270	78	$grid_9_2$	279	96	180	35.48	-87.5	288	186	120	58.33	35.48
qft	270	78	$grid_8_3$	408	93	183	55.15	-96.77	318	183	119	62.58	34.97
qft	270	78	$ring_{-}10_{-}2$	330	147	165	50 50 50	-12.24	233	179	104	55.36	41.9
qft	270	78	ring_7_3	540	108	159	70.56	-47.22	319	191	116	63.64	39.27
qft	270	78 79	t_horizontal_5_4	486	162	195	59.88	-20.37	331	177	106	67.98	40.11
qft	$\frac{270}{270}$	78 78	t_vertical_5_4	$\frac{498}{336}$	138	195	60.84	-41.3	$\frac{273}{258}$	195 162	106	61.17	45.64
$rac{ ext{qft}}{ ext{qft}}$	$\frac{270}{270}$	78	$ring_5_4$ $full_5_4$	330 198	$105 \\ 42$	nan 78	$\begin{array}{c} \text{nan} \\ 60.61 \end{array}$	nan -85.71	$\frac{258}{280}$	162 164	nan 107	nan 61.79	$\begin{array}{c} \text{nan} \\ 34.76 \end{array}$
qft	$\frac{270}{270}$	78	grid_6_4	408	96	183	55.15	-90.62	318	197	119	62.58	39.59
qftentangled	282	82	full_20_1	0	0	0	nan	nan	82	82	82	02.50	0
qftentangled	$\frac{282}{282}$	82	line_20_1	780	195	195	75	0	346	214	110	68.21	48.6
qftentangled	282	82	full_10_2	0	36	0	nan	100	82	178	82	0	53.93
qftentangled	282	82	full_7_3	168	51	150	10.71	-194.12	240	191	144	40	24.61
qftentangled	282	82	$grid_9_2$	282	102	198	29.79	-94.12	288	167	135	53.12	19.16
qftentangled	282	82	$grid_8_3$	393	102	201	48.85	-97.06	314	175	138	56.05	21.14
qftentangled	282	82	$ring_10_2$	330	153	165	50	-7.84	237	219	107	54.85	51.14
qftentangled	282	82	$ring_7_3$	540	138	nan	nan	nan	323	239	nan	nan	nan
qftentangled	282	82	$t_horizontal_5_4$	510	150	195	61.76	-30	313	185	110	64.86	40.54
qftentangled	282	82	$t_{vertical_5_4}$	510	150	195	61.76	-30	309	198	110	64.4	44.44
qftentangled	282	82	$ring_5_4$	336	102	195	41.96	-91.18	262	163	137	47.71	15.95
qftentangled	282	82	full_5_4	198	48	78	60.61	-62.5	284	204	111	60.92	45.59
qftentangled	282	82	grid_6_4	393	108	201	48.85	-86.11	314	183	138	56.05	24.59
realamprandom	335	57	full_20_1	0	0	0	nan	nan	57	57	57	0	0
realamprandom	$\frac{335}{335}$	57 57	line_20_1 full_10_2	2160	$\frac{372}{99}$	$\frac{396}{0}$	81.67	-6.45 100	$876 \\ 57$	$272 \\ 223$	112 57	87.21	58.82 74.44
realamprandom realamprandom	ააა 335	57 57	full_7_3	$0 \\ 471$	219	141	nan 70.06	35.62	632	$\frac{223}{299}$	130	79.43	56.52
realamprandom	335	57 57	grid_9_2	690	$\frac{219}{222}$	$\frac{141}{321}$	53.48	-44.59	591	$\frac{299}{250}$	150 151	79.45 74.45	39.6
realamprandom	335	57	grid_8_3	828	$\frac{222}{225}$	$\frac{321}{249}$	69.93	-10.67	669	$\frac{230}{245}$	120	82.06	51.02
realamprandom	335	57	ring_10_2	885	$\frac{220}{390}$	516	41.69	-32.31	522	$\frac{240}{360}$	215	58.81	40.28
realamprandom	335	57	ring_7_3	1299	342	435	66.51	-27.19	799	338	167	79.1	50.59
realamprandom	335	57	t_horizontal_5_4	1614	366	414	74.35	-13.11	840	270	143	82.98	47.04
realamprandom	335	57	t_vertical_5_4	1515	378	447	70.5	-18.25	835	304	154	81.56	49.34
realamprandom	335	57	$ring_5_4$	852	231	nan	nan	nan	624	259	nan	nan	nan
realamprandom	335	57	$full_{-}5_{-}4$	531	99	183	65.54	-84.85	644	224	132	79.5	41.07
realamprandom	335	57	$grid_6_4$	828	228	264	68.12	-15.79	669	241	131	80.42	45.64
twolocalrandom	335	57	full_20_1	0	0	0	nan	nan	57	57	57	0	0
	000					000	01.05	1.0	070	000	110	0 - 04	58.21
two local random	335	57	$line_20_1$	2160	360	396	81.67	-10	876	268	112	87.21	36.21
twolocalrandom twolocalrandom	335 335	57	$full_10_2$	0	51	0	nan	100	57	142	57	0	59.86
two local random	335												

Table 2: Additional swap gates and circuit depth, n=10

benchmark	g	d	layout	s_B	s_S	s_L	Δs_B	Δs_S	d_B	d_S	d_L	Δd_B	Δd_S
twolocalrandom	335	57	grid_8_3	828	228	249	69.93	-9.21	669	234	120	82.06	48.72
two local random	335	57	ring_10_2	885	414	516	41.69	-24.64	522	406	215	58.81	47.04
two local random	335	57	$ring_7_3$	1299	330	435	66.51	-31.82	799	365	167	79.1	54.25
two local random	335	57	$t_{horizontal_5_4}$	1614	360	414	74.35	-15	840	268	143	82.98	46.64
two local random	335	57	$t_{\text{-}}vertical_{\text{-}}5_{\text{-}}4$	1515	384	447	70.5	-16.41	835	287	154	81.56	46.34
twolocalrandom	335	57	$ring_5_4$	852	231	nan	nan	nan	624	253	nan	nan	nan
twolocalrandom	335	57	full_5_4	531	138	183	65.54	-32.61	644	310	132	79.5	57.42
twolocalrandom	335	57	grid_6_4	828	228	264	68.12	-15.79	669	262	131	80.42	50
su2random	375	61	full_20_1	0	0	0	nan	nan	61	61	61	0	0
su2random	$\frac{375}{375}$	61 61	line_20_1 full_10_2	2160	360 96	$\frac{396}{0}$	81.67	-10 100	904 61	$\frac{291}{245}$	116 61	87.17	60.14 75.1
su2random $ su2random$	375	61	full_7_3	$0 \\ 471$	96 195	$\frac{0}{141}$	nan 70.06	27.69	657	$\frac{245}{262}$	135	79.45	48.47
su2random su2random	375	61	grid_9_2	690	288	321	53.48	-11.46	619	202	155 157	79.43 74.64	45.47
su2random su2random	375	61	grid_8_3	828	$\frac{234}{234}$	$\frac{321}{249}$	69.93	-6.41	690	$\frac{250}{260}$	123	82.17	52.69
su2random su2random	375	61	ring_10_2	885	$\frac{264}{366}$	537	39.32	-46.72	543	336	$\frac{120}{224}$	58.75	33.33
su2random su2random	375	61	ring_7_3	1299	345	435	66.51	-26.09	827	344	172	79.2	50
su2random	375	61	t_horizontal_5_4	1614	381	414	74.35	-8.66	868	271	147	83.06	45.76
su2random	375	61	$t_{vertical_5_4}$	1515	429	447	70.5	-4.2	863	374	160	81.46	57.22
su2random	375	61	$ring_5_4$	852	231	nan	nan	nan	646	274	nan	nan	nan
su2random	375	61	$full_5_4$	531	117	183	65.54	-56.41	663	258	136	79.49	47.29
su2random	375	61	$grid_6_4$	828	228	264	68.12	-15.79	690	254	135	80.43	46.85
qnn	459	108	$full_20_1$	0	0	0	nan	nan	108	108	108	0	0
qnn	459	108	$line_20_1$	1440	258	327	77.29	-26.74	657	296	155	76.41	47.64
qnn	459	108	$full_10_2$	0	78	0	nan	100	108	280	108	0	61.43
qnn	459	108	$full_7_3$	294	132	249	15.31	-88.64	531	366	214	59.7	41.53
qnn	459	108	grid_9_2	456	165	240	47.37	-45.45	537	251	174	67.6	30.68
qnn	459	108	grid_8_3	618	198	288	53.4	-45.45	594	315	181	69.53	42.54
qnn	459	108	ring_10_2	663	267	432	34.84	-61.8	440	390	232	47.27	40.51
qnn	$459 \\ 459$	108 108	ring_7_3 t_horizontal_5_4	$816 \\ 1056$	$\frac{240}{264}$	nan 402	$\begin{array}{c} \text{nan} \\ 61.93 \end{array}$	nan -52.27	$597 \\ 662$	343 288	nan 194	nan 70.69	$\begin{array}{c} \text{nan} \\ 32.64 \end{array}$
qnn qnn	459	108	t_norizontar_5_4 t_vertical_5_4	1000	249	402 423	57.78	-69.88	662	$\frac{258}{258}$	$\frac{194}{204}$	69.18	$\frac{32.04}{20.93}$
qnn	459	108	ring_5_4	603	180	nan	nan	nan	538	303	nan	nan	nan
qnn	459	108	full_5_4	345	123	135	60.87	-9.76	513	351	151	70.57	56.98
qnn	459	108	$grid_{-}6_{-}4$	618	171	297	51.94	-73.68	594	267	179	69.87	32.96
portfolioqaoa	615	132	full_20_1	0	0	0	nan	nan	132	132	132	0	0
portfolioqaoa	615	132	$line_20_1$	2160	360	408	81.11	-13.33	985	380	176	82.13	53.68
portfolioqaoa	615	132	$full_10_2$	0	81	0	nan	100	132	363	132	0	63.64
portfolioqaoa	615	132	$full_7_3$	471	180	231	50.96	-28.33	845	406	239	71.72	41.13
portfolioqaoa	615	132	$grid_9_2$	690	234	384	44.35	-64.1	803	347	248	69.12	28.53
portfolioqaoa	615	132	$grid_8_3$	828	249	450	45.65	-80.72	818	402	273	66.63	32.09
portfolioqaoa	615	132	$ring_10_2$	885	342	594	32.88	-73.68	606	443	292	51.82	34.09
portfolioqaoa	615	132	ring_7_3	1299	348	nan	nan	nan	925	482	nan	nan	nan
portfolioqaoa portfolioqaoa	$615 \\ 615$	$\frac{132}{132}$	t_horizontal_5_4	1614	$\frac{360}{354}$	489	69.7	-35.83	979	$\frac{380}{394}$	238	75.69	$37.37 \\ 35.28$
portionoqaoa portfolioqaoa	615	132 132	t_vertical_5_4 ring_5_4	$1515 \\ 852$	$\frac{354}{255}$	504 nan	66.73	-42.37 nan	976 798	$394 \\ 381$	$\begin{array}{c} 255 \\ \text{nan} \end{array}$	73.87 nan	
portfolioqaoa	615	132 132	full_5_4	532	$\frac{255}{156}$	300	$\begin{array}{c} \text{nan} \\ 43.5 \end{array}$	-92.31	781	481	240	69.27	$\begin{array}{c} \text{nan} \\ 50.1 \end{array}$
portfolioqaoa	615	132	grid_6_4	828	225	471	43.12	-109.33	818	349	$\frac{240}{281}$	65.65	19.48
random	1058	322	full_20_1	0	0	0	nan	nan	155	155	155	0	0
random	1058	322	line_20_1	582	312	435	25.26	-39.42	708	404	225	68.22	44.31
random	1058	322	full_10_2	0	78	0	nan	100	155	353	155	0	56.09
random	1058	322	$full_7_3$	159	102	132	16.98	-29.41	419	358	179	57.28	50
random	1058	322	$grid_9_2$	285	177	225	21.05	-27.12	455	309	185	59.34	40.13
random	1058	322	$grid_8_3$	327	165	306	6.42	-85.45	492	350	208	57.72	40.57
random	1058	322	$ring_10_2$	402	225	423	-5.22	-88	493	379	244	50.51	35.62
random	1058	322	$ring_{-}7_{-}3$	417	213	nan	nan	nan	555	369	nan	nan	nan
random	1058	322	t_horizontal_5_4	522	279	402	22.99	-44.09	660	345	231	65	33.04
random	1058	322	$t_{vertical_5_4}$	525	270	381	27.43	-41.11	710	344	228	67.89	33.72
random	1058	322	ring_5_4	801	468	nan	nan	nan	1130	716	nan	nan	nan
random	1058	322	full_5_4	423	225	504	-19.15	-124	923	712	430	53.41	39.61
random	1058	$\frac{322}{217}$	grid_6_4	801	420	699	12.73	-66.43	1085	666	438	59.63	34.23
portfoliovqe	1145	217	full_20_1	0	0	0	nan	nan	217	217	217	0	0

Table 2: Additional swap gates and circuit depth, $n=10\,$

benchmark	g	d	layout	s_B	s_S	s_L	Δs_B	Δs_S	d_B	d_S	d_L	Δd_B	Δd_S
portfoliovqe	1145	217	line_20_1	2160	360	408	81.11	-13.33	1007	402	255	74.68	36.57
portfoliovqe	1145	217	$full_10_2$	0	18	0	nan	100	217	261	217	0	16.86
portfoliovqe	1145	217	$full_7_3$	471	132	255	45.86	-93.18	878	499	308	64.92	38.28
portfoliovqe	1145	217	$grid_9_2$	690	276	387	43.91	-40.22	951	530	284	70.14	46.42
portfoliovqe	1145	217	$grid_8_3$	828	255	291	64.86	-14.12	890	477	251	71.8	47.38
portfoliovqe	1145	217	ring_10_2	885	405	636	28.14	-57.04	636	617	298	53.14	51.7
portfoliovqe	1145	217	$ring_7_3$	1299	360	nan	nan	nan	947	600	nan	nan	nan
portfoliovqe	1145	217	$t_{borizontal_5_4}$	1614	372	441	72.68	-18.55	1001	424	276	72.43	34.91
portfoliovqe	1145	217	$t_{vertical_5_4}$	1515	366	507	66.53	-38.52	997	508	282	71.72	44.49
portfoliovqe	1145	217	$ring_5_4$	852	231	nan	nan	nan	894	478	nan	nan	nan
portfoliovqe	1145	217	$full_5_4$	531	111	243	54.24	-118.92	818	550	288	64.79	47.64
portfoliovqe	1145	217	$grid_6_4$	828	222	297	64.13	-33.78	890	447	251	71.8	43.85

Table 3: Additional swap gates and circuit depth, $n=15\,$

benchmark	g	d	layout	s_B	s_S	s_L	Δs_B	Δs_S	d_B	d_S	d_L	Δd_B	Δd_S
ghz	17	17	full_20_1	0	0	0	nan	nan	17	17	17	0	0
ghz	17	17	$line_20_1$	0	27	42	nan	-55.56	17	29	20	-17.65	31.03
ghz	17	17	$full_10_2$	0	12	0	nan	100	17	23	17	0	26.09
ghz	17	17	$full_7_3$	0	18	0	nan	100	17	23	17	0	26.09
ghz	17	17	$grid_9_2$	18	9	30	-66.67	-233.33	35	23	25	28.57	-8.7
ghz	17	17	$grid_8_3$	15	12	39	-160	-225	32	26	29	9.38	-11.54
ghz	17	17	ring_10_2	0	21	114	nan	-442.86	17	32	37	-117.65	-15.62
ghz	17 17	17	ring_7_3	0	39	$\frac{84}{36}$	nan -33.33	-115.38	17	50	28 28	-64.71	$\frac{44}{12.5}$
$_{ m ghz}$	17 17	17 17	t_horizontal_5_4 t_vertical_5_4	$\begin{array}{c} 27 \\ 45 \end{array}$	18 15	50 54	-33.33 -20	-100 -260	$\frac{44}{62}$	$\frac{32}{32}$	28 29	$36.36 \\ 53.23$	9.38
ghz	17 17	17 17	ring_5_4	0	3	63	nan	-200	$\frac{62}{17}$	20	33	-94.12	9.30 -65
ghz	17	17	full_5_4	0	0	0	nan	nan	17	17	33 17	0	0
ghz	17	17	$grid_6_4$	15	0	27	-80	nan	32	17	23	28.12	-35.29
dj	118	22	full_20_1	0	0	0	nan	nan	22	22	22	0	0
dj	118	$\frac{-}{22}$	line_20_1	546	57	36	93.41	36.84	146	104	45	69.18	56.73
$ {dj}$	118	22	full_10_2	66	6	9	86.36	-50	95	27	29	69.47	-7.41
dj	118	22	$full_7_3$	96	15	15	84.38	0	116	41	30	74.14	26.83
dj	118	22	$grid_9_2$	234	27	24	89.74	11.11	122	50	32	73.77	36
dj	118	22	$grid_8_3$	261	27	21	91.95	22.22	125	57	40	68	29.82
dj	118	22	$ring_10_2$	336	45	63	81.25	-40	122	69	25	79.51	63.77
dj	118	22	$ring_7_3$	168	51	42	75	17.65	116	73	29	75	60.27
dj	118	22	$t_{norizontal_5_4}$	384	33	27	92.97	18.18	137	70	40	70.8	42.86
dj	118	22	$t_{\text{vertical}}_{-5}_{-4}$	318	36	27	91.51	25	131	73	38	70.99	47.95
dj	118	22	ring_5_4	153	24	27	82.35	-12.5	111	49	35	68.47	28.57
dj	118	22	full_5_4	114	9	21	81.58	-133.33	99	40	38	61.62	5
dj	118	22 31	$grid_6_4$ $full_20_1$	261	21	21	91.95	0	123	59 26	40	67.48	32.2
graphstate	150 150	31	line_20_1	0 99	$\begin{array}{c} 0 \\ 27 \end{array}$	0 90	nan 9.09	nan -233.33	$\frac{26}{72}$	$\frac{26}{35}$	$\frac{26}{38}$	$0 \\ 47.22$	0 -8.57
graphstate graphstate	$150 \\ 150$	31	full_10_2	99 18	3	90 15	$\frac{9.09}{16.67}$	-233.33 -400	57	26	30 29	49.12	-0.57 -11.54
graphstate	150	31	full_7_3	$\frac{10}{21}$	9	27	-28.57	-200	44	29	$\frac{23}{31}$	29.55	-6.9
graphstate	150	31	grid_9_2	75	15	60	20.51	-300	70	29	33	52.86	-13.79
graphstate	150	31	grid_8_3	63	9	51	$\frac{-5}{19.05}$	-466.67	81	26	34	58.02	-30.77
graphstate	150	31	ring_10_2	60	21	93	-55	-342.86	71	31	37	47.89	-19.35
graphstate	150	31	$ring_{-}7_{-}3$	54	24	90	-66.67	-275	61	35	36	40.98	-2.86
graphstate	150	31	$t_{horizontal_5_4}$	90	27	111	-23.33	-311.11	72	32	42	41.67	-31.25
$\operatorname{graphstate}$	150	31	$t_{vertical_5_4}$	78	24	120	-53.85	-400	68	39	49	27.94	-25.64
$\operatorname{graphstate}$	150	31	$ring_5_4$	75	24	69	8	-187.5	92	56	36	60.87	35.71
graphstate	150	31	$full_5_4$	48	12	36	25	-200	72	35	41	43.06	-17.14
graphstate	150	31	grid_6_4	72	21	69	4.17	-228.57	82	35	36	56.1	-2.86
vqe	253	31	full_20_1	0	0	0	nan	nan	31	31	31	0	0
vqe	253	31	line_20_1	0	0	42	nan	nan	31	31	43	-38.71	-38.71
vqe	$253 \\ 253$	31 31	full_10_2 full_7_3	$0 \\ 0$	$6 \\ 12$	$0 \\ 0$	nan	100 100	31 31	40 58	31 31	$0 \\ 0$	$22.5 \\ 46.55$
vqe vqe	$\frac{253}{253}$	31	grid_9_2	48	$\frac{12}{24}$	60	$ \begin{array}{r} \text{nan} \\ -25 \end{array} $	-150	60	45	50	16.67	-11.11
vqe	$\frac{253}{253}$	31	grid_8_3	66	9	54	18.18	-500	80	40	45	43.75	-11.11 -12.5
vqe	253	31	ring_10_2	0	15	144	nan	-860	31	48	51	-64.52	-6.25
vqe	253	31	$ring_{-7}$	0	30	nan	nan	nan	31	70	nan	nan	nan
vqe	253	31	t_horizontal_5_4	63	3	51	19.05	-1600	79	40	47	40.51	-17.5
vqe	253	31	$t_{vertical_5_4}$	150	36	99	34	-175	94	77	48	48.94	37.66
vqe	253	31	$ring_5_4$	0	3	nan	nan	nan	31	40	nan	nan	nan
vqe	253	31	$full_5_4$	0	0	0	nan	nan	31	31	31	0	0
vqe	253	31	grid64	66	0	33	50	nan	80	31	40	50	-29.03
wstate	253	135	$full_20_1$	0	0	0	nan	nan	135	135	135	0	0
wstate	253	135	line_20_1	0	0	42	nan	nan	135	135	121	10.37	10.37
wstate	253	135	full_10_2	0	6	0	nan	100	135	138	135	0	2.17
wstate	253	135	full_7_3	0	15	0	nan	100	135	141	135	0	4.26
wstate	253	135	grid_9_2	57	15	48	15.79	-220	156	144	96	38.46	33.33
wstate	253	135	grid_8_3	21	3	39	-85.71	-1200	147	138	99	32.65	28.26
wstate	253	135	ring_10_2	0	42	156	nan	-271.43	135	153	90	33.33	41.18
wstate	$253 \\ 253$	135 135	ring_7_3 t_horizontal_5_4	$0 \\ 63$	$\frac{27}{3}$	$\frac{108}{42}$	nan 33.33	-300 -1300	$\frac{135}{166}$	$\frac{150}{135}$	81 117	$40 \\ 29.52$	$46 \\ 13.33$
wstate	∠00	199	0_11011Z011ta1_0_4	0.0	9	42	აა.აა	-1900	100	199	111	∠g.0Z	10.00

Table 3: Additional swap gates and circuit depth, $n\,=\,15$

benchmark	g	d	layout	s_B	s_S	s_L	Δs_B	Δs_S	d_B	d_S	d_L	Δd_B	Δd_S
wstate	253	135	t_vertical_5_4	126	15	84	33.33	-460	200	147	97	51.5	34.01
wstate	253	135	$ring_5_4$	0	3	117	nan	-3800	135	138	102	24.44	26.09
wstate	253	135	$full_5_4$	0	0	0	nan	nan	135	135	135	0	0
wstate	253	135	$grid_{-}6_{-}4$	21	0	27	-28.57	nan	147	135	88	40.14	34.81
qaoa	285	34	full_20_1	0	0	0	nan	nan	34	34	34	0	0
qaoa	285	34	$line_20_1$	438	63	210	52.05	-233.33	391	53	71	81.84	-33.96
qaoa	285	34	$full_10_2$	63	6	69	-9.52	-1050	164	62	65	60.37	-4.84
qaoa	285	34	$full_7_3$	108	15	51	52.78	-240	223	56	53	76.23	5.36
qaoa	285	34	$grid_9_2$	198	18	141	28.79	-683.33	247	48	60	75.71	-25
qaoa	285	34	$grid_8_3$	300	33	135	55	-309.09	335	53	58	82.69	-9.43
qaoa	285	34	$ring_10_2$	291	51	141	51.55	-176.47	303	65	60	80.2	7.69
qaoa	285	34	$ring_{-}7_{-}3$	228	42	177	22.37	-321.43	267	65	71	73.41	-9.23
qaoa	285	34	t_horizontal_5_4	348	60	207	40.52	-245	337	65	66	80.42	-1.54
qaoa	285	34	$t_{\text{-}}\text{vertical}_{\text{-}}5_{\text{-}}4$	336	66	171	49.11	-159.09	351	57	68	80.63	-19.3
qaoa	285	34	ring_5_4	168	48	102	39.29	-112.5	234	78	48	79.49	38.46
qaoa	285	34	full_5_4	126	24	nan	nan	nan	213	65	nan	nan	nan
qaoa	285	34	grid_6_4	303	39	129	57.43	-230.77	293	70	67	77.13	4.29
qft	591	118	full_20_1	0	0	0	nan	nan	118	118	118	$0 \\ 77.09$	0
qft	591	118 118	line_20_1 full_10_2	$2877 \\ 378$	$450 \\ 48$	$\frac{519}{321}$	$81.96 \\ 15.08$	-15.33	$742 \\ 485$	$\frac{322}{307}$	$\frac{170}{241}$		47.2
qft	591 591	118	full_7_3	501	48 141	$\frac{321}{300}$	40.12	-568.75	485 588	313	$\frac{241}{213}$	$50.31 \\ 63.78$	21.5
$rac{ ext{qft}}{ ext{qft}}$	591 591	118	grid_9_2	1248	$\frac{141}{255}$	396	68.27	-112.77 -55.29	679	$\frac{313}{346}$	$\frac{215}{200}$	03.78 70.54	$31.95 \\ 42.2$
qft qft	591	118	grid_8_3	1413	$\frac{255}{270}$	405	71.34	-50.29 -50	697	254	195	70.94 72.02	$\frac{42.2}{23.23}$
qft	591	118	ring_10_2	2034	384	504	75.22	-31.25	707	358	186	73.69	48.04
qft	591	118	ring_7_3	1158	333	nan	nan	nan	633	380	nan	nan	nan
qft	591	118	t_horizontal_5_4	1842	420	519	71.82	-23.57	729	278	170	76.68	38.85
qft	591	118	t_vertical_5_4	1680	369	615	63.39	-66.67	642	327	222	65.42	32.11
qft	591	118	ring_5_4	636	294	nan	nan	nan	422	310	nan	nan	nan
qft	591	118	full_5_4	468	204	nan	nan	nan	466	389	nan	nan	nan
qft	591	118	$grid_6_4$	933	288	537	42.44	-86.46	550	335	239	56.55	28.66
qftentangled	608	122	full_20_1	0	0	0	nan	nan	122	122	122	0	0
qftentangled	608	122	$line_20_1$	2877	420	543	81.13	-29.29	746	308	177	76.27	42.53
qftentangled	608	122	$full_10_2$	378	72	321	15.08	-345.83	489	329	245	49.9	25.53
qftentangled	608	122	$full_7_3$	501	105	300	40.12	-185.71	592	361	217	63.34	39.89
qftentangled	608	122	$grid_9_2$	1113	255	357	67.92	-40	610	357	192	68.52	46.22
qftentangled	608	122	$grid_8_3$	1413	285	537	62	-88.42	709	294	234	67	20.41
qftentangled	608	122	$ring_10_2$	2034	387	627	69.17	-62.02	711	445	216	69.62	51.46
qftentangled	608	122	$ring_7_3$	1158	366	nan	nan	nan	637	407	nan	nan	nan
qftentangled	608	122	t_horizontal_5_4	1788	408	543	69.63	-33.09	698	375	177	74.64	52.8
qftentangled	608	122	$t_{vertical_5_4}$	1764	408	621	64.8	-52.21	653	382	234	64.17	38.74
qftentangled	608	122	ring_5_4	636	312	nan	nan	nan	426	319	nan	nan	nan
qftentangled	608	122	full_5_4	468	168	nan	nan	nan	470	436	nan	nan	nan
qftentangled realamprandom	$608 \\ 615$	$\frac{122}{77}$	$grid_{-}6_{-}4$ $full_{-}20_{-}1$	870	294	$\frac{597}{0}$	31.38	-103.06	$624 \\ 77$	$\frac{353}{77}$	233 77	62.66	33.99
realamprandom	615	77	line_20_1	0 8190	0 882	936	nan 88.57	nan -6.12	1996	418	162	$0 \\ 91.88$	61.24
realamprandom	615	77	full_10_2	1146	168	315	72.51	-0.12 -87.5	1399	401	210	84.99	47.63
realamprandom	615	77	full_7_3	1395	414	nan	nan	nan	1456	456	nan	nan	nan
realamprandom	615	77	grid_9_2	3033	624	834	72.5	-33.65	1625	453	240	85.23	47.02
realamprandom	615	77	grid_8_3	4404	645	711	83.86	-10.23	1828	446	$\frac{210}{224}$	87.75	49.78
realamprandom	615	77	ring_10_2	5427	1116	1332	75.46	-19.35	1879	568	302	83.93	46.83
realamprandom	615	77	t_horizontal_5_4	5859	1020	1020	82.59	0	1927	599	234	87.86	60.93
realamprandom	615	77	t_vertical_5_4	5304	1044	1098	79.3	-5.17	1919	565	261	86.4	53.81
realamprandom	615	77	ring_7_3	2679	963	1224	54.31	-27.1	1444	612	319	77.91	47.88
realamprandom	615	77	ring_5_4	2544	717	nan	nan	nan	1683	457	nan	nan	nan
realamprandom	615	77	$full_{-5}_{-4}$	1497	450	nan	nan	nan	1228	454	nan	nan	nan
realamprandom	615	77	$grid_6_4$	2646	639	714	73.02	-11.74	1371	453	224	83.66	50.55
twolocalrandom	615	77	full_20_1	0	0	0	nan	nan	77	77	77	0	0
two local random	615	77	$line_20_1$	8190	915	936	88.57	-2.3	1996	402	162	91.88	59.7
two local random	615	77	$full_10_2$	1146	168	315	72.51	-87.5	1399	395	210	84.99	46.84
two local random	615	77	$full_7_3$	1395	438	nan	nan	nan	1456	494	nan	nan	nan
twolocalrandom	615	77	grid_9_2	3033	609	834	72.5	-36.95	1625	431	240	85.23	44.32

Table 3: Additional swap gates and circuit depth, $n\,=\,15$

benchmark	g	d	layout	s_B	s_S	s_L	Δs_B	Δs_S	d_B	d_S	d_L	Δd_B	Δd_S
twolocalrandom	615	77	grid_8_3	4404	624	711	83.86	-13.94	1828	404	224	87.75	44.55
twolocalrandom	615	77	ring_10_2	5427	1056	1332	75.46	-26.14	1879	555	302	83.93	45.59
twolocalrandom	615	77	ring_7_3	2679	960	1224	54.31	-20.14 -27.5	1444	686	319	77.91	53.5
twolocalrandom	615	77	t_horizontal_5_4	5859	879	1020	82.59	-16.04	1927	430	234	87.86	45.58
twolocalrandom	615	77	t_vertical_5_4	5304	1059	1098	79.3	-3.68	1919	596	261	86.4	56.21
twolocalrandom	615	77	ring_5_4	2544	711	nan	nan	nan	1683	524	nan	nan	nan
twolocalrandom	615	77	full_5_4	1497	456	nan	nan	nan	1228	515	nan	nan	nan
twolocalrandom	615	77	$grid_6_4$	2646	672	714	73.02	-6.25	1371	393	224	83.66	43
su2random	675	81	full_20_1	0	0	0	nan	nan	81	81	81	0	0
su2random	675	81	$line_20_1$	8190	876	936	88.57	-6.85	2039	451	165	91.91	63.41
su2random	675	81	$full_10_2$	1146	186	315	72.51	-69.35	1433	429	215	85	49.88
su2random	675	81	$full_7_3$	1395	414	nan	nan	nan	1499	508	nan	nan	nan
su2random	675	81	$grid_9_2$	3033	657	855	71.81	-30.14	1659	508	249	84.99	50.98
su2random	675	81	$grid_8_3$	4404	606	711	83.86	-17.33	1869	429	230	87.69	46.39
su2random	675	81	$ring_{-}10_{-}2$	5427	1074	1338	75.35	-24.58	1922	596	305	84.13	48.83
su2random	675	81	$ring_7_3$	2679	1020	nan	nan	nan	1487	684	nan	nan	nan
su2random	675	81	$t_{-}horizontal_{-}5_{-}4$	5859	975	1020	82.59	-4.62	1970	514	237	87.97	53.89
su2random	675	81	$t_{vertical_5_4}$	5304	1041	1098	79.3	-5.48	1962	604	265	86.49	56.13
su2random	675	81	$ring_5_4$	2544	744	nan	nan	nan	1709	522	nan	nan	nan
su2random	675	81	$full_5_4$	1497	501	nan	nan	nan	1259	517	nan	nan	nan
su2random	675	81	$grid_6_4$	2646	627	714	73.02	-13.88	1400	434	228	83.71	47.47
qnn	914	158	full_20_1	0	0	0	nan	nan	158	158	158	0	0
qnn	914	158	line_20_1	5460	591	732	86.59	-23.86	1442	431	234	83.77	45.71
qnn	914	158	full_10_2	720	69	369	48.75	-434.78	1103	430	302	72.62	29.77
qnn	914	158	full_7_3	927	282	nan	nan	nan	1170	529	nan	nan	nan
qnn	914	158	grid_9_2	2064	438	726	64.83	-65.75	1266	486	328	74.09	32.51
qnn	914	158 158	grid_8_3	2721	426 684	813 1122	$70.12 \\ 68.62$	-90.85	1368	$\frac{393}{549}$	$\frac{338}{351}$	75.29	$13.99 \\ 36.07$
qnn	914 914	158	ring_10_2 t_horizontal_5_4	$3576 \\ 4041$	594	1065	73.65	-64.04 -79.29	$1356 \\ 1458$	$\frac{549}{427}$	355	$74.12 \\ 75.65$	36.07 16.86
qnn	914	158	t_norizontar_5_4 t_vertical_5_4	3669	618	1003 1077	70.65	-79.29 -74.27	1438 1449	547	344	76.26	37.11
qnn qnn	914	158	ring_7_3	1920	633	nan	nan	nan	1233	540	nan	nan	nan
qnn	914	158	ring_5_4	1767	447	nan	nan	nan	1319	492	nan	nan	nan
qnn	914	158	full_5_4	1134	276	nan	nan	nan	1077	498	nan	nan	nan
qnn	914	158	$grid_{-}6_{-}4$	1905	432	789	58.58	-82.64	1129	396	334	70.42	15.66
portfoliogaoa	1260	192	full_20_1	0	0	0	nan	nan	192	192	192	0	0
portfolioqaoa	1260	192	$line_20_1$	8190	876	948	88.42	-8.22	2165	591	260	87.99	56.01
portfolioqaoa	1260	192	$full_10_2$	1146	120	393	65.71	-227.5	1766	747	351	80.12	53.01
portfolioqaoa	1260	192	$full_7_3$	1395	318	nan	nan	nan	1787	897	nan	nan	nan
portfolioqaoa	1260	192	$grid_9_2$	3033	597	1077	64.49	-80.4	1849	633	416	77.5	34.28
portfolioqaoa	1260	192	$grid_8_3$	4404	684	1197	72.82	-75	2050	667	430	79.02	35.53
portfolioqaoa	1260	192	$ring_10_2$	5427	996	1701	68.66	-70.78	2060	678	534	74.08	21.24
portfolioqaoa	1260	192	$t_{-}horizontal_{-}5_{-}4$	5859	849	1359	76.8	-60.07	2156	650	420	80.52	35.38
portfolioqaoa	1260	192	$t_{\text{-}}vertical_{\text{-}}5_{\text{-}}4$	5304	822	1440	72.85	-75.18	2150	664	430	80	35.24
portfolioqaoa	1260	192	$ring_{-}7_{-}3$	2679	882	nan	nan	nan	1862	804	nan	nan	nan
portfolioqaoa	1260	192	ring_5_4	2550	684	nan	nan	nan	2020	656	nan	nan	nan
portfolioqaoa	1260	192	full_5_4	1497	450	nan	nan	nan	1557	883	nan	nan	nan
portfolioqaoa	1260	192	grid_6_4	2646	609	1179	55.44	-93.6	1613	578	424	73.71	26.64
portfoliovqe	2505	327	ring_7_3	2679	987	0	100	100	2156	1067	327	84.83	69.35
portfoliovqe	2505	$\frac{327}{227}$	full_7_3	1395	372	0	100	100	2112	837	$\frac{327}{227}$	84.52	60.93
portfoliovqe	2505	$\frac{327}{227}$	full_20_1	0	0 976	0	nan	nan	327	327	$\frac{327}{279}$	0	0 42.20
portfoliovge	2505	$\frac{327}{327}$	$line_20_1$ $full_10_2$	8190	$876 \\ 192$	$948 \\ 534$	$88.42 \\ 53.4$	-8.22 -178.12	$\frac{2297}{1003}$	655	$\frac{378}{504}$	83.54 73.52	$42.29 \\ 53.93$
portfoliovqe portfoliovqe	$2505 \\ 2505$	$\frac{327}{327}$	grid_9_2	$\frac{1146}{3033}$	651	$\frac{534}{1107}$	63.4	-178.12 -70.05	$\frac{1903}{2088}$	$1094 \\ 798$	$\frac{504}{471}$	73.52 77.44	53.93 40.98
portfoliovqe	2505 2505	$\frac{327}{327}$	grid_9_2 grid_8_3	3033 4404	720	744	63.5 83.11	-70.05 -3.33	2088 2212	198 829	$\frac{471}{429}$	80.61	40.98 48.25
portfoliovqe	2505	$\frac{327}{327}$	ring_10_2	5427	1125	1593	70.65	-3.33 -41.6	$\frac{2212}{2195}$	1049	536	75.58	48.23
portfoliovqe	2505	$\frac{327}{327}$	t_horizontal_5_4	5859	963	1047	82.13	-41.0 -8.72	$\frac{2195}{2288}$	809	431	81.16	46.72
portfoliovqe	2505	$\frac{327}{327}$	t_vertical_5_4	5304	1014	1251	76.41	-23.37	$\frac{2280}{2280}$	881	456	80	48.24
portfoliovqe	2505	327	ring_5_4	2544	783	nan	nan	nan	2033	916	nan	nan	nan
portfoliovqe	2505	327	full_5_4	1497	444	nan	nan	nan	1538	1013	nan	nan	nan
portfoliovqe	2505	327	grid_6_4	2646	627	837	68.37	-33.49	1756	734	425	75.8	42.1
random	2542	581	full_20_1	0	0	0	nan	nan	412	412	412	0	0

Table 3: Additional swap gates and circuit depth, $n\,=\,15$

benchmark	g	d	layout	s_B	s_S	s_L	Δs_B	Δs_S	d_B	d_S	d_L	Δd_B	Δd_S
random	2542	581	line_20_1	3348	1545	1926	42.47	-24.66	2915	1131	656	77.5	42
random	2542	581	$full_10_2$	534	252	597	-11.8	-136.9	1200	950	529	55.92	44.32
random	2542	581	$full_7_3$	705	492	nan	nan	nan	1490	1059	nan	nan	nan
random	2542	581	$grid_9_2$	1680	762	1125	33.04	-47.64	1845	1041	583	68.4	44
random	2542	581	$grid_8_3$	1962	915	1257	35.93	-37.38	1954	1054	577	70.47	45.26
random	2542	581	$ring_10_2$	2127	1050	1407	33.85	-34	2042	1105	580	71.6	47.51
random	2542	581	$t_{porizontal_5_4}$	2613	1422	1815	30.54	-27.64	2408	1155	644	73.26	44.24
random	2542	581	$t_{vertical_5_4}$	2475	1239	1800	27.27	-45.28	2366	1243	658	72.19	47.06
random	2542	581	$ring_7_3$	1737	924	nan	nan	nan	1888	1242	nan	nan	nan
random	2542	581	$ring_5_4$	2646	1515	nan	nan	nan	2874	1826	nan	nan	nan
random	2542	581	$full_{-}5_{-}4$	1689	918	nan	nan	nan	2380	1647	nan	nan	nan
random	2542	581	$grid_6_4$	3018	1548	2148	28.83	-38.76	2987	1668	853	71.44	48.86