Table 1: Additional swap gates and circuit depth,  $n\,=\,5$ 

benchmark	g	d	layout	s basic	s sabre	s look	swap (%)	d basic	d swap	d look	d (%)
ghz	7	7	full_10_2	0	0	0	nan	7	7	7	0
ghz	7	7	$full_7_3$	0	0	0	nan	7	7	7	0
ghz	7	7	$ring_10_2$	0	3	9	200	7	10	8	-20
ghz	7	7	$ring_{-}7_{-}3$	0	0	9	nan	7	7	8	14.29
ghz	7	7	grid_9_3	6	3	6	100	13	10	8	-20
ghz	7	7	grid_4_5	3	0	9	nan	10	7	8	14.29
ghz	7	7	line_5_4 t_horizontal_5_4	0	9	18	100	7	13	9	-30.77 -10
ghz ghz	7 7	7 7	t_norizontal_5_4 t_vertical_5_4	9 9	3 0	6 6	100	16 16	10 7	9	28.57
ghz	7	7	ring_5_4	0	6	9	nan 50	7	8	8	0
dj	36	11	full_10_2	0	0	0	nan	11	11	11	0
dj	36	11	full_7_3	0	0	0	nan	11	11	11	0
dj	36	11	ring_10_2	36	3	3	0	40	17	12	-29.41
dj	36	11	ring_7_3	24	3	3	0	30	14	12	-14.29
dj	36	11	$grid_{-}9_{-}3$	9	3	0	-100	21	17	11	-35.29
dj	36	11	$grid_4_5$	21	3	3	0	37	14	12	-14.29
dj	36	11	$line_5_4$	36	6	6	0	40	17	14	-17.65
dj	36	11	$t_{\text{horizontal}}_{5_4}$	24	3	3	0	37	16	12	-25
dj	36	11	$t_{vertical_5_4}$	24	3	3	0	37	17	12	-29.41
dj	36	11	$ring_5_4$	9	3	3	0	24	14	12	-14.29
graphstate	50	22	$full_10_2$	0	3	0	-100	22	22	22	0
graphstate	50	22	$full_7_3$	0	6	0	-100	22	25	22	-12
graphstate	50	22	$\operatorname{ring}_{-}10_{-}2$	12	6	9	50	32	25	20	-20
graphstate	50	22	$ring_{-7}_{-3}$	18	6	12	100	38	25	21	-16
graphstate	50	22	grid_9_3	15	3	6	100	37	32	20	-37.5
graphstate	50	22	grid_4_5	18	3	9	200	41	25	20	-20
graphstate	50	22	line_5_4	12	9	12	33.33	32	25 25	21	-16
graphstate	50	22	t_horizontal_5_4	12 12	6	9	50 50	35	$\frac{25}{22}$	20	-20 -9.09
graphstate graphstate	50 50	$\frac{22}{22}$	t_vertical_5_4 ring_5_4	12 12	6 6	9 12	50 100	$\frac{35}{33}$	$\frac{22}{25}$	20 25	-9.09 0
qft	50 71	38	full_10_2	0	0	0	nan	38	$\frac{25}{38}$	$\frac{25}{38}$	0
qft	71	38	full_7_3	0	0	0	nan	$\frac{38}{38}$	$\frac{38}{38}$	38	0
qft	71	38	ring_10_2	72	15	$\frac{3}{24}$	60	92	60	42	-30
qft	71	38	ring_7_3	51	18	24	33.33	77	59	42	-28.81
qft	71	38	grid_9_3	39	12	21	75	74	53	41	-22.64
qft	71	38	$grid_4_5$	36	15	27	80	82	54	52	-3.7
qft	71	38	$line_5_4$	72	24	24	0	92	57	42	-26.32
qft	71	38	$t_{borizontal_5_4}$	48	15	24	60	82	60	42	-30
qft	71	38	$t_{vertical_5_4}$	48	15	24	60	82	60	42	-30
qft	71	38	$ring_5_4$	27	18	18	0	65	57	43	-24.56
wstate	73	45	$full_10_2$	0	0	0	nan	45	45	45	0
wstate	73	45	$full_7_3$	0	0	0	nan	45	45	45	0
wstate	73	45	$ring_{-10}^{-2}$	0	0	9	nan	45	45	40	-11.11
wstate	73	45	ring_7_3	0	0	9	nan	45	45	40	-11.11
wstate	73 73	45	grid_9_3	18 12	0	12	nan	54 51	45	41	-8.89
wstate	73	45 $45$	$grid_4_5$ $line_5_4$	0	0	9 15	nan	51 45	45 $45$	40 33	-11.11 -26.67
wstate wstate	73	$\frac{45}{45}$	t_horizontal_5_4	18	0	6	nan nan	45 58	$45 \\ 45$	39	-20.07
wstate	73	45	t_vertical_5_4	18	0	6	nan	58	45	39	-13.33
wstate	73	45	ring_5_4	nan	nan	9	nan	nan	nan	39	nan
qftentangled	78	42	full_10_2	0	0	0	nan	42	42	42	0
qftentangled	78	42	full_7_3	0	6	0	-100	$\frac{-}{42}$	63	$\frac{-}{42}$	-33.33
qftentangled	78	42	ring_10_2	72	21	30	42.86	96	75	49	-34.67
qftentangled	78	42	$ring_7_3$	51	21	30	42.86	81	75	49	-34.67
qftentangled	78	42	$grid_9_3$	45	21	27	28.57	87	76	45	-40.79
qftentangled	78	42	$grid_4_5$	36	18	15	-16.67	78	57	45	-21.05
qftentangled	78	42	$line_5_4$	72	24	36	50	96	73	50	-31.51
qftentangled	78	42	$t_{horizontal_5_4}$	60	24	33	37.5	90	73	48	-34.25
qftentangled	78	42	$t_{vertical_5_4}$	60	21	33	57.14	90	75	48	-36
qftentangled	78	42	$ring_5_4$	27	21	30	42.86	69	76	49	-35.53
vqe	83	21	$full_10_2$	0	0	0	nan	21	21	21	0

Table 1: Additional swap gates and circuit depth,  $n\,=\,5$ 

						s look	swap (%)	d basic	d swap	d look	d (%)
vqe	83	21	full_7_3	0	0	0	nan	21	21	21	0
vqe	83	21	$ring_10_2$	0	0	15	nan	21	21	29	38.1
vqe	83	21	$ring_{-}7_{-}3$	0	0	15	nan	21	21	29	38.1
vqe	83	21	$grid_9_3$	15	0	12	nan	35	21	27	28.57
vqe	83	21	$grid_4_5$	18	0	15	nan	39	21	29	38.1
vqe	83	21	line_5_4	0	0	15	nan	21	21	24	14.29
vqe	83	$\frac{21}{21}$	t_horizontal_5_4	12 12	0	12	nan	33	21 21	25 25	19.05
vqe	83 83	21	$t_{vertical_5_4}$ ring_5_4	0	0	12 15	nan	33 21	21	25 29	$19.05 \\ 38.1$
vqe	95	31	full_10_2	0	3	0	nan -100	31	42	31	-26.19
qaoa qaoa	95	31	full_7_3	0	0	0	nan	31	31	31	0
qaoa	95	31	ring_10_2	48	12	27	125	106	47	45	-4.26
qaoa	95	31	ring_7_3	24	9	27	200	54	58	45	-22.41
qaoa	95	31	$grid_9_3$	9	9	21	133.33	37	48	48	0
qaoa	95	31	$grid_4_5$	18	6	27	350	59	50	45	-10
qaoa	95	31	$line_5_4$	48	12	18	50	106	42	39	-7.14
qaoa	95	31	$t_{horizontal_5_4}$	33	9	24	166.67	100	48	45	-6.25
qaoa	95	31	$t_{vertical_5_4}$	33	9	24	166.67	100	48	45	-6.25
qaoa	95	31	$ring_5_4$	18	9	27	200	53	39	48	23.08
${\rm real amprandom}$	130	37	$full_10_2$	0	0	0	nan	37	37	37	0
realamprandom	130	37	$full_7_3$	0	0	0	nan	37	37	37	0
realamprandom	130	37	$ring_10_2$	180	51	60	17.65	206	109	66	-39.45
realamprandom	130	37	$ring_{-}7_{-}3$	120	51	60	17.65	129	109	66	-39.45
realamprandom	130	37	$grid_9_3$	96	24	42	75	145	89	64	-28.09
realamprandom	130	37	$grid_4_5$	81	42	48	14.29	160	97	59	-39.18
realamprandom	130	37	line_5_4	180	72	93	29.17	206	128	59	-53.91
realamprandom	130	37	t_horizontal_5_4	117	51	60	17.65	185	106	66	-37.74
realamprandom	130	37	t_vertical_5_4	117	51	60	17.65	185	106	66	-37.74
twolocalrandom	130	37	full_10_2	0	0	0	nan	37	37	37	0
twolocalrandom twolocalrandom	130 130	$\frac{37}{37}$	full_7_3 ring_10_2	0 180	18 51	0 60	-100 17.65	37 206	81 109	37 66	-54.32 -39.45
twolocalrandom	130	$\frac{37}{37}$	ring_7_3	120	51 51	60	17.65	129	112	66	-39.43 -41.07
twolocalrandom	130	37	grid_9_3	96	36	42	16.67	145	93	64	-31.18
twolocalrandom	130	37	grid_4_5	81	42	48	14.29	160	101	59	-41.58
twolocalrandom	130	37	line_5_4	180	72	93	29.17	206	113	59	-47.79
twolocalrandom	130	37	t_horizontal_5_4	117	72	60	-16.67	185	126	66	-47.62
twolocalrandom	130	37	$t_{vertical_5_4}$	117	48	60	25	185	107	66	-38.32
su2random	150	41	$full_10_2$	0	15	0	-100	41	64	41	-35.94
su2random	150	41	$full_7_3$	0	0	0	nan	41	41	41	0
su2random	150	41	$ring_10_2$	180	48	60	25	219	110	70	-36.36
su2random	150	41	$ring_7_3$	120	48	60	25	138	115	70	-39.13
su2random	150	41	$grid_9_3$	96	24	42	75	155	96	68	-29.17
su2random	150	41	$grid_4_5$	81	42	48	14.29	174	106	63	-40.57
su2random	150	41	$line_5_4$	180	69	93	34.78	219	123	63	-48.78
su2random	150	41	$t_{horizontal_5_4}$	117	48	60	25	198	115	70	-39.13
su2random	150	41	t_vertical_5_4	117	48	60	25	198	110	70	-36.36
qnn	154	58	full_10_2	0	39	0	-100	58	133	58	-56.39
qnn	154	58	full_7_3	0	0	0	nan	58	58	58	0
qnn	154	58	ring_10_2	120	39	66	69.23	172	122	84	-31.15
qnn	154	58	ring_7_3	93	36	66	83.33	122	122	84	-31.15
qnn	154	58	grid_9_3	63	30	48	60	132	97	78	-19.59
qnn	154 154	58 58	$grid_4_5$ $line_5_4$	54 120	30 48	54 84	80 75	$151 \\ 172$	$103 \\ 127$	80 80	-22.33 -37.01
qnn	$154 \\ 154$	58	t_horizontal_5_4	81	48 48	84 66	75 37.5	$172 \\ 172$	$\frac{127}{127}$	80 84	-37.01
qnn	154	58	t_norizontar_5_4 t_vertical_5_4	81	46 45	66	37.5 46.67	$172 \\ 172$	133	84	-36.84
qnn qnn	154	58	ring_5_4	48	36	66	83.33	95	133 $122$	84	-31.15
portfolioqaoa	195	72	full_10_2	0	0	0	nan	72	72	72	0
portfolioqaoa	195	72	full_7_3	0	21	0	-100	72	135	72	-46.67
portfolioqaoa	195	72	ring_10_2	180	66	87	31.82	255	166	110	-33.73
portfolioqaoa	195	72	ring_7_3	120	51	87	70.59	157	164	110	-32.93
			0		~ -	٠.		•			3=.00

Table 1: Additional swap gates and circuit depth,  $n\,=\,5$ 

111-			14	_ 1 : _		- 11-	(07)	11:-	1	1 11-	1 (07)
benchmark	g	d	layout	s basic	s sabre	s look	swap (%)	d basic	d swap	d look	d (%)
portfolioqaoa	195	72	$grid_4_5$	81	42	69	64.29	220	138	104	-24.64
portfolioqaoa	195	72	$line_5_4$	180	66	93	40.91	255	166	90	-45.78
portfolioqaoa	195	72	$t_{horizontal_5_4}$	117	60	87	45	252	179	110	-38.55
portfolioqaoa	195	72	$t_{\text{vertical}}_{5}_{4}$	117	66	87	31.82	252	166	110	-33.73
random	223	97	$full_10_2$	0	12	0	-100	97	126	97	-23.02
$\operatorname{random}$	223	97	$full_7_3$	0	12	0	-100	97	123	97	-21.14
$\operatorname{random}$	223	97	$ring_10_2$	63	12	66	450	160	106	121	14.15
random	223	97	$ring_7_3$	60	12	66	450	157	106	121	14.15
$\operatorname{random}$	223	97	$grid_9_3$	30	12	27	125	114	106	111	4.72
$\operatorname{random}$	223	97	$grid_4_5$	39	12	27	125	169	106	111	4.72
$\operatorname{random}$	223	97	$line_5_4$	63	12	30	150	160	106	99	-6.6
$\operatorname{random}$	223	97	$t_{horizontal_5_4}$	36	12	66	450	151	106	121	14.15
random	223	97	$t_{\text{vertical}}_{5}_{4}$	36	12	66	450	151	106	121	14.15
random	223	97	$ring_5_4$	24	12	66	450	120	106	121	14.15
portfoliovqe	310	107	$full_10_2$	0	0	0	nan	107	107	107	0
portfoliovqe	310	107	$full_7_3$	0	21	0	-100	107	161	107	-33.54
portfoliovqe	310	107	$ring_10_2$	180	51	93	82.35	242	204	125	-38.73
portfoliovqe	310	107	$ring_7_3$	120	48	93	93.75	179	193	125	-35.23
portfoliovqe	310	107	$grid_9_3$	96	42	57	35.71	209	181	111	-38.67
portfoliovqe	310	107	$grid_4_5$	81	39	48	23.08	239	175	115	-34.29
portfoliovqe	310	107	$line_5_4$	180	69	90	30.43	242	187	126	-32.62
portfoliovqe	310	107	$t_{-}horizontal_{-}5_{-}4$	117	48	93	93.75	239	193	125	-35.23
portfoliovqe	310	107	$t_{\text{vertical}\_5\_4}$	117	57	93	63.16	239	205	125	-39.02

Table 2: Additional swap gates and circuit depth, n=10

benchmark	g	d	layout	s basic	s sabre	s look	swap (%)	d basic	d swap	d look	d (%)
ghz	12	12	$full_10_2$	0	6	0	-100	12	15	12	-20
ghz	12	12	$full_7_3$	0	9	0	-100	12	21	12	-42.86
ghz	12	12	$ring_10_2$	0	9	36	300	12	21	17	-19.05
ghz	12	12	$ring_{-}7_{-}3$	0	15	51	240	12	24	25	4.17
ghz	12	12	$grid_9_3$	12	9	24	166.67	24	21	16	-23.81
ghz	12	12	$grid_4_5$	6	6	24	300	18	18	16	-11.11
ghz	12	12	$line_5_4$	0	9	27	200	12	21	15	-28.57
ghz	12	12	t_horizontal_5_4	18	0	21	nan	30	12	17	41.67
ghz	12	12	$t_{vertical_5_4}$	27	9	30	233.33	39	18	19	5.56
$\operatorname{ghz}$	12	12	$ring_5_4$	nan	nan	45	nan	nan	nan	21	nan
$\mathrm{d}\mathrm{j}$	79	17	$full_10_2$	0	3	0	-100	17	20	17	-15
dj	79	17	$full_7_3$	48	9	9	0	70	26	22	-15.38
dj	79	17	$ring_10_2$	78	21	24	14.29	64	43	21	-51.16
dj	79	17	$ring_{-7}_{-3}$	126	15	24	60	79	35	19	-45.71
dj	79	17	$grid_{-}9_{-}3$	90	21	12	-42.86	82	46	22	-52.17
dj	79 <b>-</b> 2	17	grid_4_5	144	21	18	-14.29	88	44	24	-45.45
dj	79 70	17	line_5_4	216	21	21	0	94	54	30	-44.44
dj	79 70	17	t_horizontal_5_4	150	21	15	-28.57	88	51	26	-49.02
dj	79 70	17	t_vertical_5_4	135	30	15	-50	85	49	25	-48.98
dj	79	17	ring_5_4	nan	nan	12	nan	nan	nan	23	nan
graphstate	100	26	full_10_2	0	6	0	-100	23	30	23	-23.33
graphstate	100	26	full_7_3	18	3	12	300	53	24	23	-4.17
graphstate	100	26	ring_10_2	30	12	39	225	45	28	29	3.57
graphstate	100	26	ring_7_3	48	18	39	116.67	63	33	29	-12.12
graphstate	100	26 26	grid_9_3	42	15	48	220	57 70	33	26	-21.21
graphstate	100	26 26	grid_4_5	51	15	36	140	70	35	24	-31.43
graphstate	100	26 26	line_5_4	72 co	24	57 26	137.5	68 66	36	32	-11.11
graphstate	100	26 26	t_horizontal_5_4	60 63	21 21	$\frac{36}{39}$	71.43	66 76	38	23	-39.47
graphstate	100	$\frac{26}{26}$	t_vertical_5_4			39 39	85.71		34	24 30	-29.41
graphstate wstate	$\frac{100}{163}$	90	$ring_5_4$ $full_10_2$	$   \begin{array}{c}     \text{nan} \\     0   \end{array} $	$   \begin{array}{c}     \text{nan} \\     0   \end{array} $	0	nan nan	nan 90	nan 90	90	$ \begin{array}{c} \text{nan} \\ 0 \end{array} $
wstate	163	90	full_7_3	0	0	0	nan	90	90	90	0
wstate	163	90	ring_10_2	0	12	48	300	90	96	62	-35.42
wstate	163	90	grid_9_3	21	0	27	nan	102	90	46	-48.89
wstate	163	90	grid_4_5	$\frac{21}{24}$	15	42	180	96	99	65	-34.34
wstate	163	90	line_5_4	0	0	27	nan	90	90	76	-15.56
wstate	163	90	t_horizontal_5_4	45	0	27	nan	116	90	72	-20
wstate	163	90	t_vertical_5_4	72	0	45	nan	137	90	66	-26.67
wstate	163	90	ring_5_4	0	12	45	275	90	96	55	-42.71
wstate	163	90	ring_7_3	0	6	66	1000	90	96	62	-35.42
vqe	168	26	full_10_2	0	0	0	nan	26	26	26	0
vqe	168	26	full_7_3	0	0	0	nan	26	26	26	0
vqe	168	26	$ring_10_2$	0	9	66	633.33	26	40	$\frac{-3}{40}$	0
vqe	168	26	grid_9_3	9	6	54	800	31	35	43	22.86
vqe	168	26	$grid_4_5$	36	3	45	1400	61	35	33	-5.71
vqe	168	26	$line_5_4$	0	0	27	nan	26	26	33	26.92
vqe	168	26	$t_{horizontal_5_4}$	51	0	33	nan	71	26	37	42.31
vqe	168	26	$t_{vertical_5_4}$	66	3	51	1600	73	35	38	8.57
vqe	168	26	$ring_5_4$	0	15	57	280	26	38	35	-7.89
vqe	168	26	$ring_{-}7_{-}3$	0	0	84	nan	26	26	43	65.38
qaoa	190	34	$grid_9_3$	63	12	78	550	145	56	49	-12.5
qaoa	190	34	$grid_4_5$	105	21	33	57.14	174	59	38	-35.59
qaoa	190	34	$line_{-}5_{-}4$	168	30	75	150	228	53	44	-16.98
qaoa	190	34	$t_{\text{horizontal}\_5\_4}$	129	21	78	271.43	206	50	50	0
qaoa	190	34	$t_{vertical_5_4}$	114	27	81	200	196	82	56	-31.71
qaoa	190	34	$full_10_2$	0	6	0	-100	34	47	34	-27.66
qaoa	190	34	$full_7_3$	48	9	15	66.67	138	48	42	-12.5
qaoa	190	34	$ring_10_2$	120	24	60	150	154	42	48	14.29
qaoa	190	34	$ring_{-}7_{-}3$	81	18	75	316.67	158	64	52	-18.75
qaoa	190	34	$ring_{-}5_{-}4$	117	12	72	500	191	56	56	0
qft	270	78	$full_10_2$	0	18	0	-100	78	133	78	-41.35

Table 2: Additional swap gates and circuit depth, n=10

benchmark	g	d	layout	s basic	s sabre	s look	swap (%)	d basic	d swap	d look	d (%)
qft	270	78	$full_7_3$	168	75	150	100	236	181	140	-22.65
qft	270	78	$ring_10_2$	330	141	165	17.02	233	205	103	-49.76
qft	270	78 	ring_7_3	540	120	159	32.5	319	204	116	-43.14
qft	270	78 70	grid_9_3	279	96	180	87.5	288	211	120	-43.13
qft	270	78 70	grid_4_5	507	108	195	80.56	335	176	130	-26.14
qft	270	78 70	line_5_4	780	168	195	16.07	342	181	106	-41.44
qft	270	78	t_horizontal_5_4	486	162	195	20.37	331	198	106	-46.46
qft	$\frac{270}{282}$	78 82	t_vertical_5_4 full_10_2	$498 \\ 0$	144	195	35.42 -100	273 82	187	106 82	-43.32 -47.44
qftentangled qftentangled	282 282	82 82	full_7_3	168	18 45	$0 \\ 150$	233.33	82 240	$\frac{156}{176}$	62 144	-47.44
qftentangled	$\frac{282}{282}$	82	ring_10_2	330	$\frac{45}{147}$	165	233.33 12.24	$\frac{240}{237}$	239	$144 \\ 107$	-55.23
qftentangled	$\frac{282}{282}$	82	ring_7_3	540	129	150	16.28	323	$\frac{239}{244}$	115	-52.87
qftentangled	$\frac{282}{282}$	82	grid_9_3	282	99	198	100	288	177	135	-23.73
qftentangled	$\frac{282}{282}$	82	grid_4_5	414	108	180	66.67	285	213	122	-23.73 $-42.72$
qftentangled	$\frac{282}{282}$	82	line_5_4	780	195	195	0	346	217	110	-49.31
qftentangled	282	82	t_horizontal_5_4	510	156	195	25	313	$\frac{211}{225}$	110	-51.11
qftentangled	282	82	t_vertical_5_4	510	153	195	27.45	309	228	110	-51.75
qftentangled	282	82	ring_5_4	336	153	195	27.45	262	256	137	-46.48
realamprandom	335	57	full_10_2	0	105	0	-100	57	213	57	-73.24
realamprandom	335	57	$full_7_3$	471	99	141	42.42	632	223	130	-41.7
realamprandom	335	57	ring_10_2	885	399	516	29.32	522	351	215	-38.75
realamprandom	335	57	$grid_9_3$	690	231	321	38.96	591	248	151	-39.11
realamprandom	335	57	$grid_4_5$	1323	258	375	45.35	786	246	138	-43.9
realamprandom	335	57	$line_{-}5_{-}4$	2160	369	396	7.32	876	278	112	-59.71
realamprandom	335	57	$t_{\text{horizontal}}_{5_4}$	1614	363	414	14.05	840	263	143	-45.63
realamprandom	335	57	$t_{vertical_5_4}$	1515	378	447	18.25	835	243	154	-36.63
realamprandom	335	57	$ring_{-}7_{-}3$	1299	339	465	37.17	799	323	171	-47.06
two local random	335	57	$full_10_2$	0	81	0	-100	57	196	57	-70.92
two local random	335	57	$full_7_3$	471	162	141	-12.96	632	235	130	-44.68
two local random	335	57	$ring_10_2$	885	405	516	27.41	522	402	215	-46.52
two local random	335	57	$grid_9_3$	690	273	321	17.58	591	299	151	-49.5
two local random	335	57	$grid_4_5$	1323	258	375	45.35	786	254	138	-45.67
twolocalrandom	335	57	$line_{-}5_{-}4$	2160	360	396	10	876	268	112	-58.21
twolocalrandom	335	57	$t_{-}horizontal_{-}5_{-}4$	1614	366	414	13.11	840	265	143	-46.04
twolocalrandom	335	57	t_vertical_5_4	1515	423	447	5.67	835	304	154	-49.34
twolocalrandom	335	57	ring_7_3	1299	417	465	11.51	799	370	171	-53.78
su2random	375	61	full_10_2	0	99	0	-100	61	236	61	-74.15
su2random	375	61	full_7_3	471	174	141	-18.97	657	292	135	-53.77
su2random	375	61	ring_10_2	885	402	537	33.58	543	381	224	-41.21
su2random	375	61	grid_9_3	690	273	321	17.58	619	310	157	-49.35
su2random su2random	$\frac{375}{375}$	61 61	$grid_4_5$ $line_5_4$	1323 $2160$	261 360	$\frac{375}{396}$	43.68 10	815 904	$267 \\ 291$	142 116	-46.82 -60.14
su2random su2random	375	61	t_horizontal_5_4	1614	372	390 414	11.29	904 868	291	147	-49.66
su2random su2random	$\frac{375}{375}$	61	t_norizontar_5_4 t_vertical_5_4	1514 $1515$	384	447	16.41	863	310	160	-48.39
qnn	459	108	full_10_2	0	90	0	-100	108	310	108	-65.16
qnn	459	108	full_7_3	294	180	249	38.33	531	338	214	-36.69
qnn	459	108	ring_10_2	663	288	432	50.55	440	360	232	-35.56
qnn	459	108	grid_9_3	456	180	240	33.33	537	275	174	-36.73
qnn	459	108	grid_4_5	876	186	390	109.68	636	291	220	-24.4
qnn	459	108	line_5_4	1440	249	327	31.33	657	258	155	-39.92
qnn	459	108	t_horizontal_5_4	1056	249	402	61.45	662	258	194	-24.81
qnn	459	108	t_vertical_5_4	1002	258	423	63.95	662	304	204	-32.89
portfolioqaoa	615	132	full_10_2	0	111	0	-100	132	426	132	-69.01
portfolioqaoa	615	132	full_7_3	471	156	231	48.08	845	478	239	-50
portfolioqaoa	615	132	$ring_10_2$	885	387	594	53.49	606	496	292	-41.13
portfolioqaoa	615	132	$grid_{-}9_{-}3$	690	249	384	54.22	803	384	248	-35.42
portfolioqaoa	615	132	$grid_4_5$	1323	261	450	72.41	956	356	262	-26.4
portfolioqaoa	615	132	$line_5_4$	2160	360	408	13.33	985	380	176	-53.68
portfolioqaoa	615	132	$t_{borizontal_5_4}$	1614	366	489	33.61	979	367	238	-35.15
portfolioqaoa	615	132	$t_{vertical_5_4}$	1515	396	504	27.27	976	462	255	-44.81
random	646	155	$full_10_2$	0	93	0	-100	155	320	155	-51.56

Table 2: Additional swap gates and circuit depth,  $n\,=\,10$ 

benchmark	g	d	layout	s basic	s sabre	s look	swap (%)	d basic	d swap	d look	d (%)
random	646	155	full_7_3	159	111	132	18.92	419	348	179	-48.56
random	646	155	$ring_10_2$	402	237	381	60.76	493	375	244	-34.93
random	646	155	$grid_9_3$	285	171	225	31.58	455	312	185	-40.71
random	646	155	$grid_4_5$	477	186	375	101.61	643	325	222	-31.69
random	646	155	$line_5_4$	582	312	435	39.42	708	342	225	-34.21
random	646	155	$t_horizontal_5_4$	522	273	402	47.25	660	419	231	-44.87
random	646	155	$t_{vertical_5_4}$	525	246	381	54.88	710	351	228	-35.04
portfoliovqe	1145	217	$grid_9_3$	690	222	387	74.32	951	479	284	-40.71
portfoliovqe	1145	217	$grid_4_5$	1323	261	342	31.03	994	465	265	-43.01
portfoliovqe	1145	217	$line_5_4$	2160	360	408	13.33	1007	402	255	-36.57
portfoliovqe	1145	217	$t_{horizontal_5_4}$	1614	366	441	20.49	1001	444	276	-37.84
portfoliovqe	1145	217	$t_{vertical_5_4}$	1515	396	507	28.03	997	536	282	-47.39
portfoliovqe	1145	217	$full_10_2$	0	15	0	-100	217	288	217	-24.65
portfoliovqe	1145	217	$full_7_3$	471	105	255	142.86	878	450	308	-31.56
portfoliovqe	1145	217	$\rm ring\_10\_2$	885	411	636	54.74	636	588	298	-49.32

Table 3: Additional swap gates and circuit depth, n=15

benchmark	g	d	layout	s basic	s sabre	s look	swap (%)	d basic	d swap	d look	d (%)
ghz	17	17	full_10_2	0	6	0	-100	17	20	17	-15
ghz	17	17	$full_7_3$	0	6	0	-100	17	20	17	-15
ghz	17	17	ring_10_2	0	21	111	428.57	17	26	40	53.85
ghz	17	17	grid_9_3	18	9	42	366.67	35	20	25	25
ghz	17	17	grid_4_5	12	18	33	83.33	29	32	25	-21.88
ghz	17 17	17 17	line_5_4 t_horizontal_5_4	$0 \\ 27$	12 39	42 39	250 0	17 44	23 53	20 28	-13.04 -47.17
ghz ghz	$\frac{17}{17}$	17 17	t_norizontal_5_4 t_vertical_5_4	45	59 51	59 54	5.88	62	59	28 29	-47.17 -50.85
ghz	17 17	17 17	ring_5_4	0	$\frac{31}{27}$	54 51	5.00 88.89	02 17	41	30	-26.83
ghz	17	17	ring_7_3	0	18	84	366.67	17	32	28	-12.5
dj	118	22	full_10_2	66	9	9	0	95	33	29	-12.12
dj	118	$\frac{22}{22}$	full_7_3	96	9	15	66.67	116	36	30	-16.67
dj	118	22	ring_10_2	336	33	60	81.82	122	71	28	-60.56
dj	118	22	grid_9_3	234	48	24	-50	122	67	34	-49.25
d j	118	22	$grid_{-}4_{-}5$	324	45	27	-40	128	75	38	-49.33
dj	118	22	$line_5_4$	546	66	36	-45.45	146	102	45	-55.88
dj	118	22	$t_{\text{horizontal}\_5\_4}$	384	42	27	-35.71	137	65	40	-38.46
dj	118	22	$t_{vertical_5_4}$	318	48	27	-43.75	131	69	38	-44.93
dj	118	22	$ring_5_4$	153	36	27	-25	113	71	33	-53.52
dj	118	22	$ring_{-}7_{-}3$	168	39	42	7.69	116	66	29	-56.06
graphstate	150	29	full_10_2	30	6	24	300	51	40	34	-15
graphstate	150	29	$full_7_3$	36	9	27	200	67	35	32	-8.57
graphstate	150	29	$ring_10_2$	111	27	108	300	84	32	31	-3.12
graphstate	150	29	grid_9_3	108	30	87	190	86	38	33	-13.16
graphstate	150	29	grid_4_5	147	24	111	362.5	94	31	38	22.58
graphstate	150	29	line_5_4	186	36	138	283.33	95	33	49	48.48
graphstate	150	29	t_horizontal_5_4	147	42	147	250	96	37	45	21.62
graphstate	150	29	t_vertical_5_4	150	30	138	360 466.67	107	35	41	17.14
graphstate graphstate	$\frac{150}{150}$	29 29	ring_5_4 ring_7_3	78 84	18 24	102 96	400.07 300	72 85	38 43	$\frac{32}{35}$	-15.79 -18.6
vqe	$\frac{150}{253}$	31	full_10_2	0	6	0	-100	31	43 41	31	-16.0
vqe	$\frac{253}{253}$	31	ring_10_2	0	33	192	481.82	31	63	59	-24.59 $-6.35$
vqe	$\frac{253}{253}$	31	grid_9_3	48	9	66	633.33	60	45	47	4.44
vqe	253	31	grid_4_5	48	$\frac{3}{12}$	78	550	75	60	49	-18.33
vqe	253	31	line_5_4	0	69	42	-39.13	31	83	43	-48.19
vqe	253	31	t_horizontal_5_4	63	6	54	800	79	34	47	38.24
vqe	253	31	$t_{vertical_5_4}$	150	12	99	725	94	54	48	-11.11
vqe	253	31	$ring_7_3$	0	24	138	475	31	63	53	-15.87
vqe	253	31	$full_7_3$	0	12	0	-100	31	56	31	-44.64
vqe	253	31	$ring_5_4$	0	39	63	61.54	31	76	44	-42.11
wstate	253	135	$full_10_2$	0	12	0	-100	135	141	135	-4.26
wstate	253	135	$ring_{-}10_{-}2$	0	15	177	1080	135	138	78	-43.48
wstate	253	135	$grid_9_3$	57	18	72	300	156	147	107	-27.21
wstate	253	135	$grid_4_5$	39	3	57	1800	147	138	102	-26.09
wstate	253	135	line_5_4	0	0	42	nan	135	135	121	-10.37
wstate	253	135	t_horizontal_5_4	63	21	45	114.29	166	141	111	-21.28
wstate	253	135	t_vertical_5_4	126	45	84	86.67	200	153	97	-36.6
wstate	253	135	ring_7_3	0	15	108	620	135	144	81	-43.75
wstate	$253 \\ 253$	135	full_7_3	0	12 48	0 72	-100 50	135	141	135	-4.26
wstate	$\frac{255}{285}$	$\frac{135}{34}$	$ring_5_4$ full_ $10_2$	0 63	48 6	69	1050	$135 \\ 164$	150 50	79 65	-47.33 30
qaoa	$\frac{285}{285}$	34 34	ring_10_2	291	36	141	291.67	303	50	60	30 11.11
qaoa qaoa	$\frac{285}{285}$	34 34	grid_9_3	198	36	$\frac{141}{243}$	575	$\frac{303}{247}$	54 51	71	39.22
qaoa	$\frac{285}{285}$	34	grid_9_5 grid_4_5	357	39	141	261.54	369	58	70	20.69
qaoa	$\frac{285}{285}$	34	line_5_4	438	75	210	180	391	56	71	26.79
qaoa	$\frac{285}{285}$	34	t_horizontal_5_4	348	54	$\frac{210}{234}$	333.33	337	56	67	19.64
qaoa	285	34	t_vertical_5_4	336	63	234	271.43	351	62	89	43.55
qaoa	285	34	ring_5_4	171	51	93	82.35	250	83	43	-48.19
qaoa	285	34	ring_7_3	228	51	177	247.06	267	76	71	-6.58
qaoa	285	34	$full_{-7}$ _3	108	15	51	240	223	50	53	6
qft	591	118	$full_10_2$	378	48	321	568.75	485	307	241	-21.5

Table 3: Additional swap gates and circuit depth, n=15

benchmark	g	d	layout	s basic	s sabre	s look	swap (%)	d basic	d swap	d look	d (%)
qft	591	118	$ring_10_2$	2034	384	504	31.25	707	389	186	-52.19
qft	591	118	grid_9_3	1164	270	450	66.67	680	292	203	-30.48
qft	591	118	grid_4_5	1698	312	525	68.27	734	324	214	-33.95
qft	591	118	line_5_4	2877	426	519	21.83	742	316	170	-46.2
qft	591 591	118 118	t_horizontal_5_4 t_vertical_5_4	1842 1680	$\frac{381}{396}$	$519 \\ 615$	36.22 55.3	$729 \\ 642$	$\frac{309}{352}$	$\frac{170}{222}$	-44.98 -36.93
qft qft	591 591	118	full_7_3	501	390 117	300	55.5 156.41	588	$\frac{352}{295}$	213	-30.93 -27.8
qftentangled	608	122	full_10_2	378	72	$\frac{300}{321}$	345.83	489	$\frac{295}{329}$	$\frac{213}{245}$	-25.53
qftentangled	608	122	ring_10_2	2034	360	624	73.33	711	344	216	-25.95 -37.21
qftentangled	608	122	grid_9_3	1128	279	357	27.96	650	327	192	-41.28
qftentangled	608	122	grid_4_5	1575	300	561	87	687	315	$\frac{132}{223}$	-29.21
qftentangled	608	122	line_5_4	2877	414	543	31.16	746	311	177	-43.09
qftentangled	608	122	t_horizontal_5_4	1788	390	543	39.23	698	320	177	-44.69
qftentangled	608	122	$t_{vertical_5_4}$	1764	411	621	51.09	653	393	234	-40.46
qftentangled	608	122	$full_7_3$	501	150	300	100	592	399	217	-45.61
realamprandom	615	77	$full_10_2$	1146	177	315	77.97	1399	372	210	-43.55
realamprandom	615	77	$ring_10_2$	5427	1155	1332	15.32	1879	565	302	-46.55
realamprandom	615	77	$grid_9_3$	3018	666	834	25.23	1603	439	240	-45.33
realamprandom	615	77	$grid_4_5$	5277	645	759	17.67	1840	412	198	-51.94
realamprandom	615	77	$line_5_4$	8190	888	936	5.41	1996	418	162	-61.24
${\rm real amprandom}$	615	77	$t_{-}horizontal_{-}5_{-}4$	5859	885	1020	15.25	1927	446	234	-47.53
real amprandom	615	77	$t_{vertical_5_4}$	5304	1047	1098	4.87	1919	564	261	-53.72
realamprandom	615	77	$ring_{-}7_{-}3$	2679	999	1224	22.52	1444	740	319	-56.89
twolocalrandom	615	77	$full_10_2$	1146	138	315	128.26	1399	327	210	-35.78
twolocalrandom	615	77	$ring_10_2$	5427	1131	1332	17.77	1879	601	302	-49.75
twolocalrandom	615	77	grid_9_3	3018	672	834	24.11	1603	453	240	-47.02
twolocalrandom	615	77	$grid_4_5$	5277	696	759	9.05	1840	446	198	-55.61
twolocalrandom	615	77	line_5_4	8190	876	936	6.85	1996	416	162	-61.06
twolocalrandom	615	77	t_horizontal_5_4	5859	876	1020	16.44	1927	424	234	-44.81
twolocalrandom twolocalrandom	615	77	t_vertical_5_4	5304	1011	1098	8.61	1919	593	261	-55.99
twolocalrandom su2random	615	77 81	ring_7_3	2679	882 189	1224	38.78 66.67	$1444 \\ 1433$	$595 \\ 452$	$\frac{319}{215}$	-46.39
su2random su2random	$675 \\ 675$	81	full_10_2 ring_10_2	$1146 \\ 5427$	1155	$\frac{315}{1338}$	15.84	1433 $1922$	452 661	$\frac{215}{305}$	-52.43 -53.86
su2random su2random	675	81	grid_9_3	3018	672	831	23.66	1922 $1641$	489	$\frac{303}{242}$	-50.51
su2random su2random	675	81	grid_9_5 grid_4_5	5277	672	759	12.95	1881	422	202	-50.51 -52.13
su2random su2random	675	81	line_5_4	8190	897	936	4.35	2039	461	165	-64.21
su2random	675	81	t_horizontal_5_4	5859	993	1020	2.72	1970	538	237	-55.95
su2random	675	81	t_vertical_5_4	5304	1086	1098	1.1	1962	658	265	-59.73
qnn	914	158	full_10_2	720	90	369	310	1103	527	302	-42.69
qnn	914	158	ring_10_2	3576	708	1116	57.63	1356	558	349	-37.46
qnn	914	158	$grid_9_3$	2061	444	771	73.65	1277	456	343	-24.78
qnn	914	158	$grid_4_5$	3384	447	858	91.95	1386	414	355	-14.25
qnn	914	158	$line_{-}5_{-}4$	5460	591	732	23.86	1442	431	234	-45.71
qnn	914	158	$t_{range}$	4041	606	1065	75.74	1458	481	355	-26.2
qnn	914	158	$t_{vertical_5_4}$	3669	600	1077	79.5	1449	509	344	-32.42
portfolioqaoa	1260	192	$full_10_2$	1146	141	393	178.72	1766	777	351	-54.83
portfolioqaoa	1260	192	$ring_10_2$	5427	1065	1701	59.72	2060	793	534	-32.66
portfolioqaoa	1260	192	$grid_9_3$	3018	663	1074	61.99	1843	655	412	-37.1
portfolioqaoa	1260	192	$grid_4_5$	5277	663	1170	76.47	2077	585	418	-28.55
portfolioqaoa	1260	192	$line_5_4$	8190	888	948	6.76	2165	531	260	-51.04
portfolioqaoa	1260	192	t_horizontal_5_4	5859	822	1359	65.33	2156	636	420	-33.96
portfolioqaoa	1260	192	t_vertical_5_4	5304	879	1440	63.82	2150	641	430	-32.92
random	1992	412	full_10_2	534	246	597	142.68	1200	957	529	-44.72
random	1992	412	ring_10_2	2127	1050	1407	34	2042	1129	580 576	-48.63
random	1992	412	grid_9_3	1647	783	1140	45.59	1913	1177	576	-51.06
random	1992	412	grid_4_5	2250	1041	1533	47.26	2103	1056	629 656	-40.44
random	$1992 \\ 1992$	$412 \\ 412$	line_5_4	$3348 \\ 2613$	$1623 \\ 1407$	$1926 \\ 1815$	18.67 29	2915 $2408$	1128 1130	$656 \\ 644$	-41.84 -43.01
random random	1992 $1992$	$\frac{412}{412}$	t_horizontal_5_4 t_vertical_5_4	2613 $2475$	1407 $1203$	1815	49.63	2408 $2366$	1130 $1214$	$644 \\ 658$	-43.01 -45.8
portfoliovqe	$\frac{1992}{2505}$	$\frac{412}{327}$	t_vertical_5_4 full_10_2	$\frac{2475}{1146}$	1203 189	534	182.54	2300 1903	984	504	-45.8 -48.78
portfoliovqe	2505	$\frac{327}{327}$	ring_10_2	5427	1098	1590	44.81	2195	1030	520	-40.70 -49.51
bormonovde	2000	941	11115-10-4	0441	1090	1990	44.01	4130	1000	920	-43.01

Table 3: Additional swap gates and circuit depth,  $n\,=\,15$ 

benchmark	g	d	layout	s basic	s sabre	s look	swap (%)	d basic	d swap	d look	d (%)
portfoliovqe	2505	327	$grid_9_3$	3018	636	1107	74.06	2112	835	471	-43.59
portfoliovqe	2505	327	$grid_4_5$	5277	648	768	18.52	2244	756	412	-45.5
portfoliovqe	2505	327	$line_5_4$	8190	891	948	6.4	2297	695	378	-45.61
portfoliovqe	2505	327	$t_{-}horizontal_{-}5_{-}4$	5859	975	1047	7.38	2288	893	431	-51.74
portfoliovqe	2505	327	$t_{\text{vertical}}_{-5}_{-4}$	5304	942	1251	32.8	2280	834	456	-45.32