

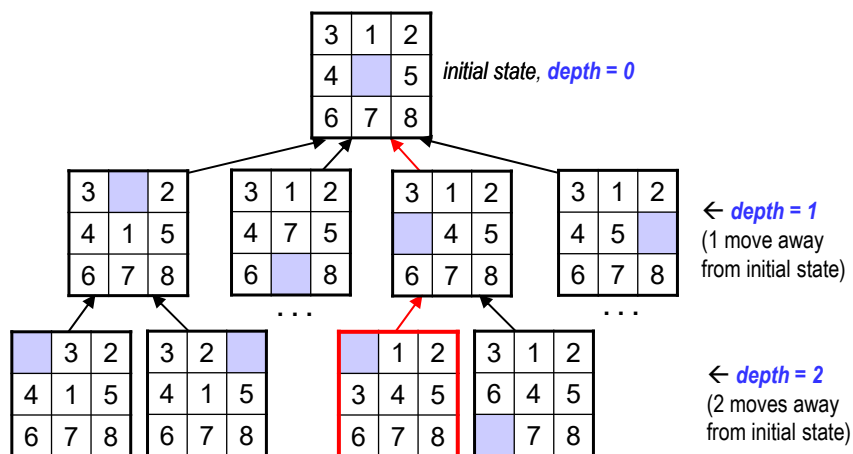
Final Project Revisited; Informed State-Space Search

Computer Science 111
Boston University

David G. Sullivan, Ph.D.

Recall: State-Space Search Tree

- The predecessor references connect the State objects, creating a structure known as a *tree*.



- When we reach a goal, we trace up the tree to get the solution – i.e., the sequence of moves from the initial state to the goal.

Part III: Initial Searcher Class

- The searcher object maintains a list of yet-to-be-tested states:

[<table><tr><td>3</td><td>1</td><td>2</td></tr><tr><td>4</td><td>5</td><td></td></tr><tr><td>6</td><td>7</td><td>8</td></tr></table>	3	1	2	4	5		6	7	8	,	<table><tr><td>3</td><td>1</td><td>2</td></tr><tr><td>4</td><td></td><td>5</td></tr><tr><td>6</td><td>7</td><td>8</td></tr></table>	3	1	2	4		5	6	7	8	,	<table><tr><td></td><td>3</td><td>2</td></tr><tr><td>4</td><td>1</td><td>5</td></tr><tr><td>6</td><td>7</td><td>8</td></tr></table>		3	2	4	1	5	6	7	8]
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- Searcher methods include:
 - `next_state()` – get and return the next state that should be considered (removing it from the searcher's list of states)
 - in Part III – pick a state at random!
 - `find_solution(init_state)` – search from `init_state` until you find a goal state, and return it when it's found
 - ***see pseudocode from last week!***

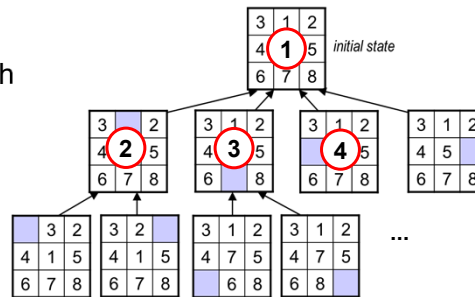
Part IV: Subclasses for Other Search Algorithms

- Each algorithm will have its own type of searcher object.
 - with its own version of at least one of the key methods
 - ***take advantage of inheritance!***

Recall: Breadth-First Search (BFS)

- When choosing from the list of yet-to-be-tested states, choose one of the states with the **smallest depth**.

- Thus, BFS considers:
 - all states at depth 0
 - all states at depth 1
 - all states at depth 2
 - ...



- The breadth-first searcher should follow FIFO ("first in, first out").
 - its `next_state()` should remove the state that has been in the list the longest

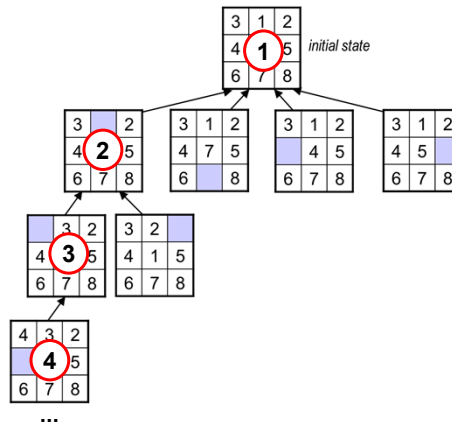
Recall: Features of Breadth-First Search

- It is *complete*: if there is a solution, BFS will find it.
- If each move has the same cost, BFS is *optimal*—it will find a minimal-cost solution.
- Key problems:
 - It can require too much *time*.
 - It can require too much *memory*.
 - all* previously tested states must be kept in memory

Depth-First Search (DFS)

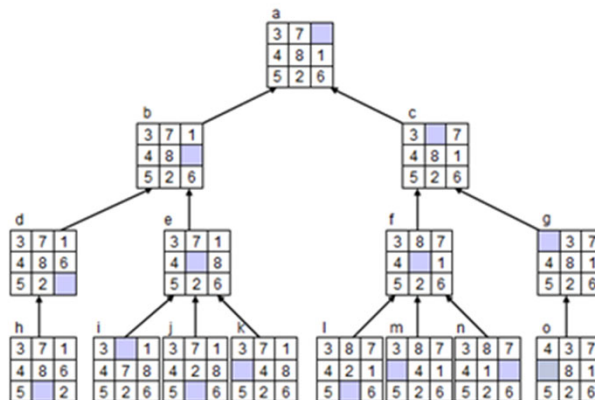
- When choosing from the list of yet-to-be-tested states, choose one of the states with the **largest depth**.

- Thus, DFS keeps going down a given path in the tree until it can't go any further.



- The depth-first searcher should follow LIFO ("last in, first out").
 - its `next_state()` should remove the state that was most recently added to the list

What are the first 4 states DFS would consider?
(break ties alphabetically)



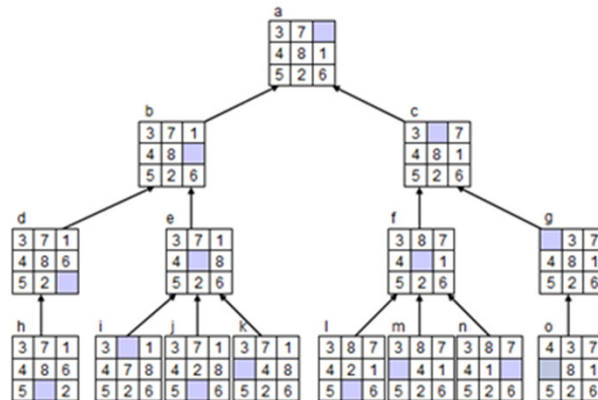
A. a, b, c, d

C. a, b, d, h

B. a, b, d, e

D. none of these

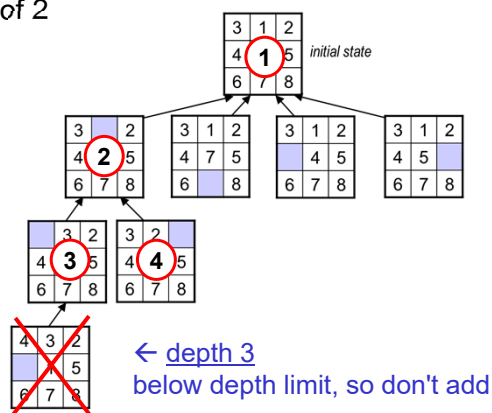
What are the first 4 states DFS would consider?
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- A. a, b, c, d C. **a, b, d, h**
B. a, b, d, e D. none of these

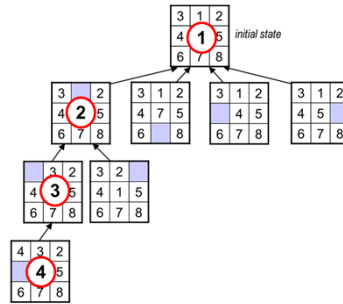
Imposing a Depth Limit

- DFS can end up going down very long paths.
 - can lead to solutions with too many steps
- To prevent this, we can use a *depth limit*.
 - the searcher won't add states whose depth > depth limit
 - example: depth limit of 2



Features of Depth-First Search

- Much better memory usage than BFS
 - DFS only stores a single path down the tree at a given time – along with the untested successors of states on that path
- What about time?
 - if there are many solutions, DFS can often find one quickly
 - if not, it can still be slow
- Key problem: it can get stuck going down long/"bad" paths.
 - ➔ thus, it is neither complete nor optimal.



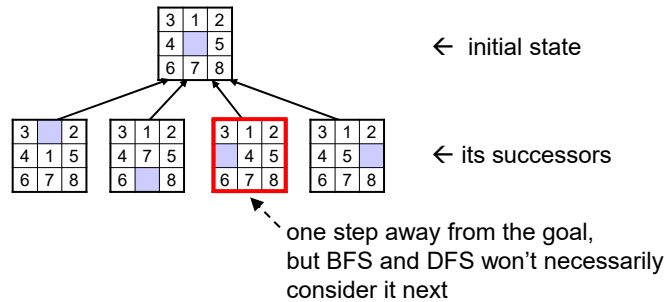
Comparing BFS and DFS

- BFS:
 - is *complete* – if there is a solution, it will eventually find it
 - is *optimal* – will find the solution with the fewest moves
 - can end up requiring too much time and memory
- DFS:
 - uses less memory than BFS
 - can also require too much time
 - is neither complete nor optimal!
- Examples: use CTRL-C as needed to terminate a search


```
>>> eight_puzzle('142635708', 'BFS', -1)
>>> eight_puzzle('142635708', 'DFS', -1)
>>> eight_puzzle('312065748', 'BFS', -1)
>>> eight_puzzle('312065748', 'DFS', -1) # -1 -> 31
>>> eight_puzzle('603872541', 'BFS', -1)
>>> eight_puzzle('603872541', 'DFS', -1) # -1 -> 31
```

Uninformed State-Space Search

- BFS and DFS are *uninformed* search algorithms.
 - always consider the states in a certain order
 - do not consider how close a given state is to the goal
- Example:



Part V: Informed State-Space Search

- *Informed* search algorithms attempt to consider more promising states first.
- They associate a *priority* with each successor state.
 - give a higher priority to states that seem closer to the goal
- When choosing the next state to consider, they select one with the highest priority.

Estimating the Remaining Cost

- We need some *heuristic function* $h(x)$ that takes a state x and computes an estimate of the remaining cost.
 - heuristic = rule of thumb
- To find optimal solutions, we need an *admissible* heuristic – one that never overestimates the remaining cost.
 - it's okay to underestimate!

One Heuristic Function for the Eight Puzzle

- $h_1(x)$ = # of misplaced tiles in the board for state x
 - i.e., # of tiles that aren't where they belong in the goal state
 - example:

1	4	2
3	5	8
6		7

state s

	1	2
3	4	5
6	7	8

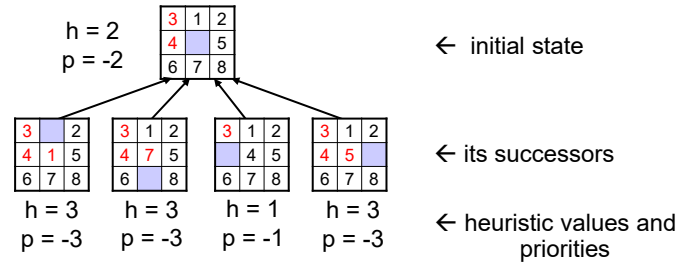
goal state

$h_1(s) = 5$, because the 1, 4, 5, 7, and 8 tiles are misplaced

- note that we do *not* include the blank in the count
- This heuristic is admissible (doesn't overestimate). Why?
every misplaced tile requires at least one move
to get to where it belongs
- In the final project, you will experiment with other heuristics!

Greedy Search

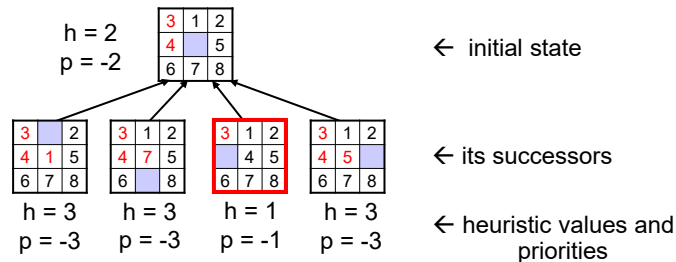
- Priority of state x , $p(x) = -1 * h(x)$
 - mult. by -1 so states closer to the goal have higher priorities



- Which successor would greedy test first?

Greedy Search

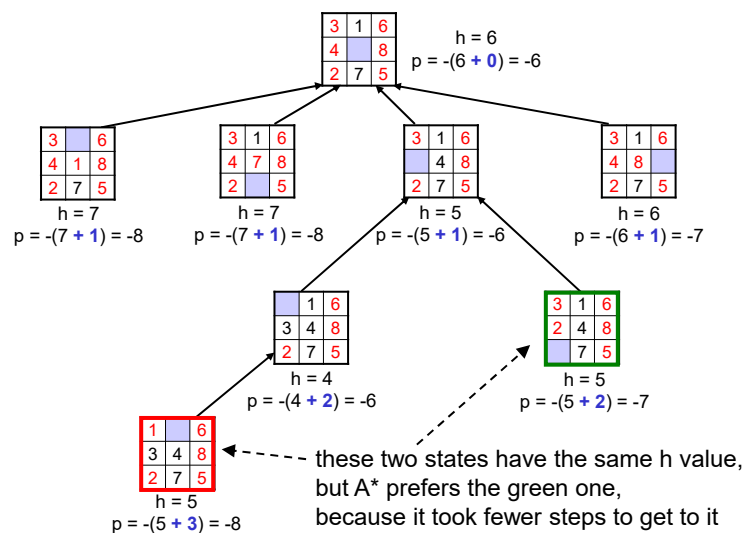
- Priority of state x , $p(x) = -1 * h(x)$
 - mult. by -1 so states closer to the goal have higher priorities



- Greedy search would test the red successor before the other ones, because it has the highest priority.
- However, greedy search is neither complete nor optimal!
 - key problem: fails to consider the cost that was already spent to get to the current state

A* Search

- Priority of state x , $p(x) = -1 * (h(x) + g(x))$
 where $g(x)$ = the cost of getting from the initial state to x



Characteristics of A*

- Incorporating $g(x)$ allows A* to find an optimal solution – one with the minimal *total* cost.
- Time and memory usage can still be problematic, but much less so than in uninformed search!

Implementing Informed Search

- In *uninformed* search, the searcher object maintains a list of untested states.

$\left[\begin{array}{|c|c|c|} \hline 3 & 1 & 2 \\ \hline 4 & 5 & \\ \hline 6 & 7 & 8 \\ \hline \end{array} , \begin{array}{|c|c|c|} \hline 3 & 1 & 2 \\ \hline 4 & & 5 \\ \hline 6 & 7 & 8 \\ \hline \end{array} , \begin{array}{|c|c|c|} \hline & 3 & 2 \\ \hline 4 & 1 & 5 \\ \hline 6 & 7 & 8 \\ \hline \end{array} \right]$

- In *informed* search, the searcher will maintain of a *list of lists*!

$\left[[-3, \begin{array}{|c|c|c|} \hline 3 & 1 & 2 \\ \hline 4 & 5 & \\ \hline 6 & 7 & 8 \\ \hline \end{array}], [-2, \begin{array}{|c|c|c|} \hline 3 & 1 & 2 \\ \hline 4 & & 5 \\ \hline 6 & 7 & 8 \\ \hline \end{array}], [-3, \begin{array}{|c|c|c|} \hline & 3 & 2 \\ \hline 4 & 1 & 5 \\ \hline 6 & 7 & 8 \\ \hline \end{array}] \right]$

- How could it find the next state to be tested?

Implementing Informed Search

- In *uninformed* search, the searcher object maintains a list of untested states.

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- How could it find the next state to be tested?
using `max()`!

Part VI: Make Things Faster!

- With our simple heuristic, even A* can be slow.
 - for puzzles that require many moves to solve
- You will devise your own heuristics.
 - try to get better estimates of the remaining cost
 - be careful not to overestimate!
- You will also perform experiments comparing approaches.

What's Left in CS 111

S	M	T	W	T	F	S
28	29	30	1	2	3	4
5	6	7	8	9	10	11
12	13	14	15	16	17	18

Problem Set 10

- FSM problems
- 50 points
- due **Sun (12/5)**

Final Project

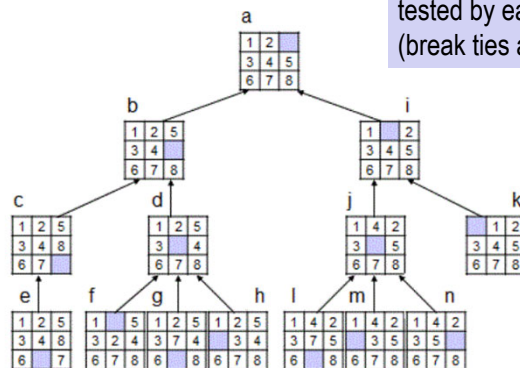
- late submissions of parts I & II through tonight
- full project due **12/9**

Final exam:

- **12/14**, 9-11 am
- email me with exam conflicts

Extra Practice

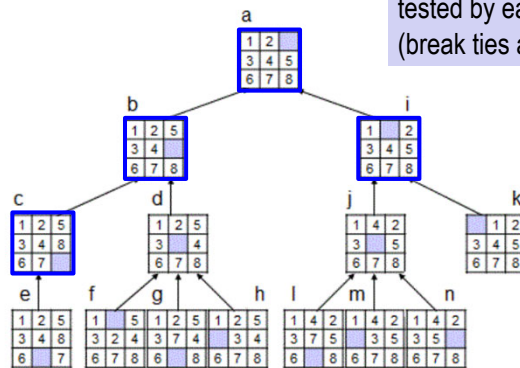
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(break ties alphabetically)



- BFS
- DFS (no depth limit)
- DFS (depth limit of 2)
- DFS (depth limit of 3)

Extra Practice

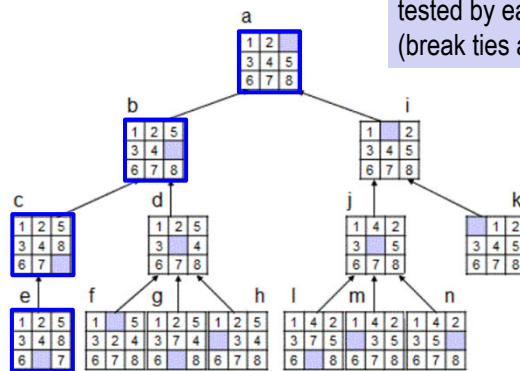
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- *BFS* – a, b, i, c
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Extra Practice

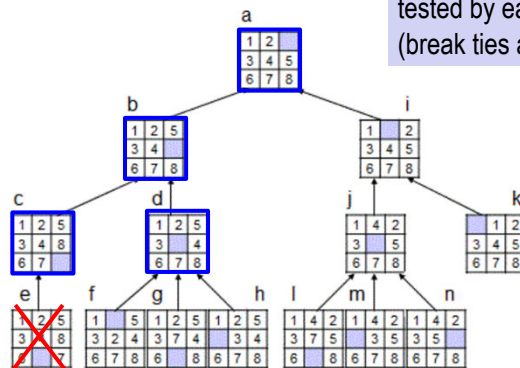
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- *BFS* – a, b, i, c
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Extra Practice

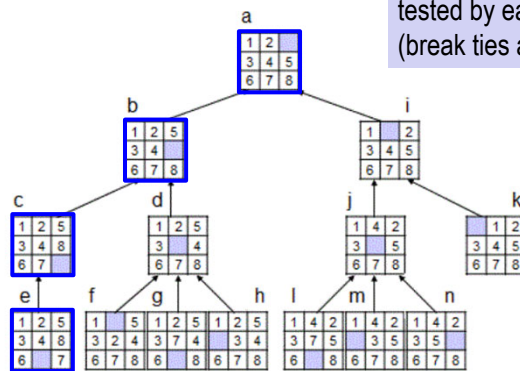
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- BFS – a, b, i, c
- DFS (no depth limit) – a, b, c, e
- *DFS (depth limit of 2)* – a, b, c, d
- DFS (depth limit of 3)

Extra Practice

What are the first four states tested by each algorithm?
(break ties alphabetically)



- BFS – a, b, i, c
- DFS (no depth limit) – a, b, c, e
- DFS (depth limit of 2) – a, b, c, d
- *DFS (depth limit of 3)* – a, b, c, e (would test d next)