

**Info:** Computed up to  $N^4$ , max anticommutator value  $N^2$

**Term symbol:**  $^2\Sigma$ :  $S = 1/2$ ,  $\Lambda = 0$

**Basis states**  $|\Lambda, \Sigma, \Omega\rangle$ :

- $|\pm 0, -1/2, -1/2\rangle$
- $|\pm 0, +1/2, +1/2\rangle$

**Hamiltonian matrix:**

$$\begin{bmatrix} Bx + \frac{B}{4} - Dx^2 - \frac{3Dx}{2} - \frac{5D}{16} - \frac{\gamma}{2} - \gamma_D x - \frac{\gamma_D}{4} & \frac{\sqrt{4x+1}(-8B+4D(4x+1)+4\gamma+\gamma_D(4x+5))}{16} \\ \frac{\sqrt{4x+1}(-8B+4D(4x+1)+4\gamma+\gamma_D(4x+5))}{16} & Bx + \frac{B}{4} - Dx^2 - \frac{3Dx}{2} - \frac{5D}{16} - \frac{\gamma}{2} - \gamma_D x - \frac{\gamma_D}{4} \end{bmatrix}$$

**Eigenvalues:**

$$F_1 = Bx + \frac{B}{4} - Dx^2 - \frac{3Dx}{2} - \frac{5D}{16} - \frac{\gamma}{2} - \gamma_D x - \frac{\gamma_D}{4} - \sqrt{4x+1} \left( -\frac{B}{2} + Dx + \frac{D}{4} + \frac{\gamma}{4} + \frac{\gamma_D x}{4} + \frac{5\gamma_D}{16} \right)$$

$$F_2 = Bx + \frac{B}{4} - Dx^2 - \frac{3Dx}{2} - \frac{5D}{16} - \frac{\gamma}{2} - \gamma_D x - \frac{\gamma_D}{4} + \sqrt{4x+1} \left( -\frac{B}{2} + Dx + \frac{D}{4} + \frac{\gamma}{4} + \frac{\gamma_D x}{4} + \frac{5\gamma_D}{16} \right)$$