

HW 2

Nathan Hawkins

1/26/2021

1

```
linmdl1 <- "
  model {

    for(i in 1:15){
      y[i] ~ dnorm(mu[i], prec)
      mu[i] <- b0 + b1*x[i]
    }

    #Priors
    b0 ~ dnorm(0, .001)
    b1 ~ dnorm(0, .002)
    prec <- 1/vr

    #Variance
    vr ~ dgamma(1.1, .1667)

  }
"

x <- hw2$x
y <- hw2$y

writeLines(linmdl1, 'linreg.txt')

data.jags <- c('x', 'y')
parms <- c('b0', 'b1', 'vr')

linreg.sim1 <- jags(data.jags,
  inits = NULL,
  parameters.to.save = parms,
  model.file = 'linreg.txt',
  n.iter = 35000,
  n.burnin = 10000,
  n.chains = 4,
  n.thin = 10)
```

Intermediary steps

```
sims <- as.mcmc(linreg.sim1)
chains <- as.matrix(sims)
```

```
b0 = chains[,1]
b1 = chains[,2]
vr = chains[,4]
```

#Make some data

```
xx <- seq(0,100,by = 5)
```

#Find Fitted values

#Fit each x value

#Make a matrix

```
fittedy <- matrix(0, 10000, 21)
```

*#For Loop that follows intercept + slope * data*

```
for(i in 1:10000){
  fittedy[i,] <- b0[i] + b1[i] * xx
}
```

#Find Predicted Values

#Make matrix to hold predicted values

```
predicted_y <- matrix(0, 10000, 21)
```

*#For Loop that follows intercept + slope * data + noise*

```
for(i in 1:10000){
  predicted_y[i,] <- b0[i] + b1[i] * xx + rnorm(1,0,sqrt(vr[i]))
}
```

#Plot Line of best fit

```
plot(x,y, main = "Data, Line of Best Fit, and Intervals for Y")
abline(mean(b0), mean(b1), col = 'green')
```

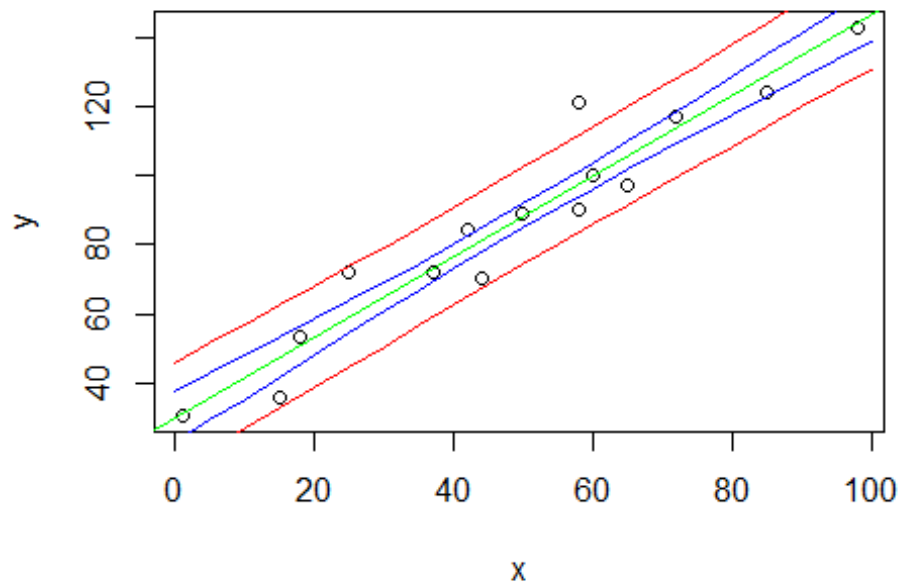
#Plot Posterior Interval

```
lines(xx,apply(fittedy, 2, quantile, 0.975), col = 'blue')
lines(xx,apply(fittedy, 2, quantile, 0.025), col = 'blue')
```

#Plot Posterior Predicted Interval

```
lines(xx,apply(predicted_y, 2, quantile, 0.975), col = 'red')
lines(xx,apply(predicted_y, 2, quantile, 0.025), col = 'red')
```

Data, Line of Best Fit, and Intervals for Y



2 Y1

```
linmdl1 <- "  
  model {  
  
    for(i in 1:15){  
      y[i] ~ dnorm(mu[i], prec)  
      mu[i] <- b0 + b1*x[i]  
    }  
  
    #Priors  
    b0 ~ dnorm(0, .001)  
    b1 ~ dnorm(0, .002)  
    prec <- 1/vr  
  
    #Variance  
    vr ~ dgamma(1.1, .1667)  
  
  }  
"  
  
x <- hw2$x  
y <- hw2$y1
```

```

writeLines(linmdl1, 'linreg.txt')

data.jags <- c('x', 'y')
parms <- c('b0', 'b1', 'vr')

linreg.sim1 <- jags(data.jags,
                    inits = NULL,
                    parameters.to.save = parms,
                    model.file = 'linreg.txt',
                    n.iter = 35000,
                    n.burnin = 10000,
                    n.chains = 4,
                    n.thin = 10)

# Intermediary steps

sims <- as.mcmc(linreg.sim1)
chains <- as.matrix(sims)

b0 = chains[,1]
b1 = chains[,2]
vr = chains[,4]

#Make some data
xx <- seq(0,100,by = 5)

#Find Fitted values
#Fit each x value

#Make a matrix
fittedy <- matrix(0, 10000, 21)

#For Loop that follows intercept + slope * data
for(i in 1:10000){
  fittedy[i,] <- b0[i] + b1[i] * xx
}

#Find Predicted Values
#Make matrix to hold predicted values
predicted_y <- matrix(0, 10000, 21)

#For Loop that follows intercept + slope * data + noise
for(i in 1:10000){
  predicted_y[i,] <- b0[i] + b1[i] * xx + rnorm(1,0,sqrt(vr[i]))
}

```

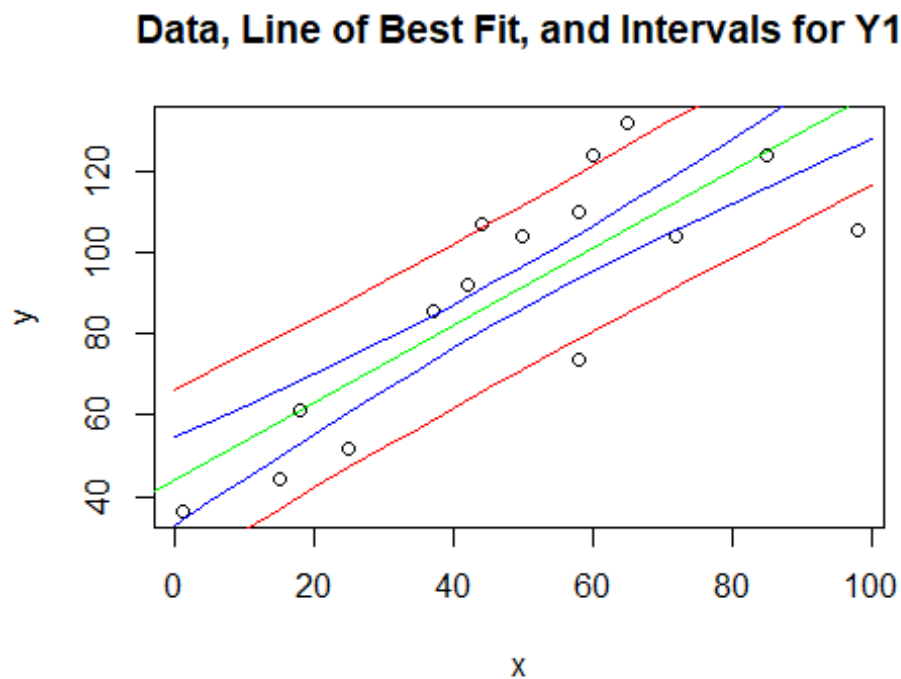
```

#Plot line of best fit
plot(x,y, main = "Data, Line of Best Fit, and Intervals for Y1")
abline(mean(b0), mean(b1), col = 'green')

#Plot Posterior Interval
lines(xx,apply(fittedy, 2, quantile, 0.975), col = 'blue')
lines(xx,apply(fittedy, 2, quantile, 0.025), col = 'blue')

#Plot Posterior Predicted Interval
lines(xx,apply(predicted_y, 2, quantile, 0.975), col = 'red')
lines(xx,apply(predicted_y, 2, quantile, 0.025), col = 'red')

```



3 Let Variances increase linearly with x

For hw make $\text{variance}[i] = a_0 + a_1 * x$ $\text{var}[i] <- a_0 + a_1 * x$ we need priors for a_0 and a_1 draw a_0 and a_1 from a uniform distribution from 0 to 1000 maybe

```

linmdl3 <- "
model {

  for(i in 1:15){
    y[i] ~ dnorm(mu[i], 1/s2[i])
    mu[i] <- b0 + b1*x[i]
    s2[i] = a1 * x[i]
  }
}

```

```

    #Priors
    b0 ~ dnorm(0, .001)
    b1 ~ dnorm(0, .002)
    a1 ~ dgamma(1, .5)

  }
"

x <- hw2$x
y <- hw2$y

writeLines(linmdl3, 'linreg.txt')

data.jags <- c('x', 'y')
parms <- c('b0', 'b1', 'a1', 's2')

linreg.sim3 <- jags(data.jags,
  inits = NULL,
  parameters.to.save = parms,
  model.file = 'linreg.txt',
  n.iter = 35000,
  n.burnin = 10000,
  n.chains = 4,

library(R2jags)
# Intermediary steps

sims <- as.mcmc(linreg.sim3)
chains <- as.matrix(sims)

b0 = chains[,2]
b1 = chains[,3]

s2 = chains[,c(5,12:19,6:11)]

#Make some data
xx <- seq(0,100,length.out = 15)

#Find Fitted values
#Fit each x value

#Make a matrix
fittedy <- matrix(0, 10000, 15)

```

```

#For loop that follows intercept + slope * data
for(i in 1:10000){
  for(j in 1:15){
    fittedy[i,] <- b0[i] + b1[i] * xx
  }
}

#Find Predicted Values
#Make matrix to hold predicted values
predicted_y <- matrix(0, 10000, 15)

#For loop that follows intercept + slope * data + noise
for(i in 1:10000){
  for(j in 1:15){
    predicted_y[i,] <- b0[i] + b1[i] * xx + rnorm(1,0,sqrt(s2[i,]))
  }
}

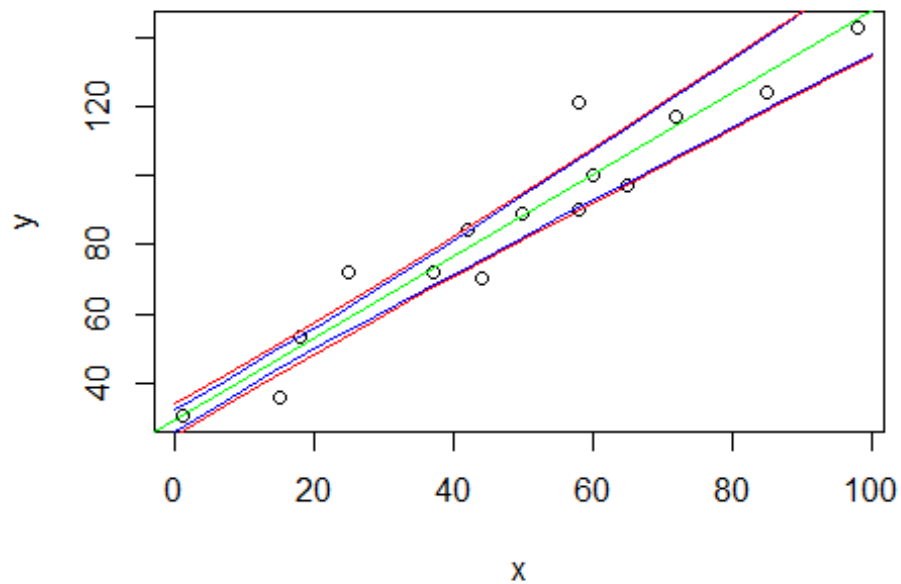
#Plot Line of best fit
plot(x,y, main = "Data, Line of Best Fit, and Intervals for Y1, variance
increasing with x")
abline(mean(b0), mean(b1), col = 'green')

#Plot Posterior Interval
lines(xx,apply(fittedy, 2, quantile, 0.975), col = 'blue')
lines(xx,apply(fittedy, 2, quantile, 0.025), col = 'blue')

#Plot Posterior Predicted Interval
lines(xx,apply(predicted_y, 2, quantile, 0.975), col = 'red')
lines(xx,apply(predicted_y, 2, quantile, 0.025), col = 'red')

```

Line of Best Fit, and Intervals for Y1, variance inceas



4 SD increase with x

```
linmdl4 <- "  
  model {  
  
    for(i in 1:15){  
      y[i] ~ dnorm(mu[i], 1/s2[i])  
      mu[i] <- b0 + b1*x[i]  
      s2[i] = sqrt(a1 * x[i])  
    }  
  
    #Priors  
    b0 ~ dnorm(0, .001)  
    b1 ~ dnorm(0, .002)  
    a1 ~ dgamma(1, .5)  
  
  }  
"  
  
x <- hw2$x  
y <- hw2$y  
  
writeLines(linmdl4, 'linreg.txt')
```



```

data.jags <- c('x', 'y')
parms <- c('b0', 'b1', 'a1', 's2')

linreg.sim4 <- jags(data.jags,
  inits = NULL,
  parameters.to.save = parms,
  model.file = 'linreg.txt',
  n.iter = 35000,
  n.burnin = 10000,
  n.chains = 4,
  n.thin = 10)

library(R2jags)
# Intermediary steps

sims <- as.mcmc(linreg.sim3)
chains <- as.matrix(sims)
colnames(chains)

## [1] "a1"          "b0"          "b1"          "deviance"    "s2[1]"       "s2[10]"
## [7] "s2[11]"      "s2[12]"      "s2[13]"      "s2[14]"      "s2[15]"      "s2[2]"
## [13] "s2[3]"       "s2[4]"       "s2[5]"       "s2[6]"       "s2[7]"       "s2[8]"
## [19] "s2[9]"

b0 = chains[,2]
b1 = chains[,3]

s2 = chains[,c(5,12:19,6:11)]

#Make some data
xx <- seq(0,100,length.out = 15)

#Find Fitted values
#Fit each x value

#Make a matrix
fittedy <- matrix(0, 10000, 15)

#For loop that follows intercept + slope * data
for(i in 1:10000){
  for(j in 1:15){
    fittedy[i,] <- b0[i] + b1[i] * xx
  }
}

#Find Predicted Values
#Make matrix to hold predicted values
predicted_y <- matrix(0, 10000, 15)

```

```

#For loop that follows intercept + slope * data + noise
for(i in 1:10000){
  for(j in 1:15){
    predicted_y[i,] <- b0[i] + b1[i] * xx + rnorm(1,0,(s2[i,]))
  }
}

#Plot line of best fit
plot(x,y, main = "Data, Line of Best Fit, and Intervals for Y1, Standard
Deviation inceasing with x")
abline(mean(b0), mean(b1), col = 'green')

#Plot Posterior Interval
lines(xx,apply(fittedy, 2, quantile, 0.975), col = 'blue')
lines(xx,apply(fittedy, 2, quantile, 0.025), col = 'blue')

#Plot Posterior Predicted Interval
lines(xx,apply(predicted_y, 2, quantile, 0.975), col = 'red')
lines(xx,apply(predicted_y, 2, quantile, 0.025), col = 'red')

```

of Best Fit, and Intervals for Y1, Standard Deviation in

