

HW 4

Nathan Hawkins

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```
vo2 <- read.table("vo2.dat", header = TRUE)
head(vo2)
```

	ID	Gender	Age1	BMI	MPH	HR	RPE	MaxVO2ML
1	1	0	12	16.49	4.6	178	14	43.69
2	95	0	12	17.80	6.0	171	10	48.07
3	102	0	12	20.48	4.8	185	13	45.73
4	111	0	12	16.46	5.4	155	13	46.65
5	120	0	12	15.94	4.7	154	14	55.56
6	121	0	12	17.51	5.0	172	14	50.00

1

Running MLR with the 6 covariates, I get a DIC of 756.6.

```
mdl <- "
  model {

    for(i in 1:120){
      y[i] ~ dnorm(mu[i], prec)
      mu[i] <- b0 + bgen*gender[i] + bbmi*bmi[i] + brpe*rpe[i] + bhr*hr[i] +
      bmph*mph[i] + bage*age[i]
    }

    b0 ~ dnorm(0 , 0.001)
    bgen ~ dnorm(0, 0.001)
    bbmi ~ dnorm(0, 0.001)
    brpe ~ dnorm(0, 0.001)
    bhr ~ dnorm(0, 0.001)
    bmph ~ dnorm(0, 0.001)
    bage ~ dnorm(0, 0.001)

    prec <- 1/vv
    vv ~ dgamma(1.5, 0.2)

  }
"

mph <- vo2$MPH
```

```

bmi <- vo2$BMI
gender <- vo2$Gender
y <- vo2$MaxVO2ML
rpe <- vo2$RPE
hr <- vo2$HR
age <- vo2$Age1

# Standardize the covariates
mph <- (mph-mean(mph))/sd(mph)
bmi <- (bmi-mean(bmi))/sd(bmi)
gender <- (gender-mean(gender))/sd(gender)
rpe <- (rpe-mean(rpe))/sd(rpe)
age <- (age-mean(age))/sd(age)
hr <- (hr-mean(hr))/sd(hr)
mphhr <- mph*hr

writeLines(mdl, 'vo2.txt')

#What to use
data.jags <- c('y', 'gender', 'bmi', 'rpe', 'mph', 'hr', 'age')

#What to call it in the output
parms.jags <- c('b0', "brpe", 'bgen', 'bbmi', 'bmph', 'vv', 'bhr', 'bage')

vo2.sim <- jags(data= data.jags, parameters.to.save = parms.jags,
               model.file = 'vo2.txt', inits = NULL,
               n.iter = 6000, n.thin = 1, n.chains = 4,
               n.burnin = 1000)

module glm loaded

Compiling model graph
  Resolving undeclared variables
  Allocating nodes
Graph information:
  Observed stochastic nodes: 120
  Unobserved stochastic nodes: 8
  Total graph size: 1183

Initializing model

vo2.sim

Inference for Bugs model at "vo2.txt", fit using jags,
  4 chains, each with 6000 iterations (first 1000 discarded)

```

```

n.sims = 20000 iterations saved
      mu.vect sd.vect   2.5%    25%    50%    75%   97.5%  Rhat n.eff
b0      48.773   0.485  47.818  48.443  48.777  49.100  49.720 1.001 17000
bage     0.483   0.557  -0.604   0.109   0.483   0.864   1.561 1.001 13000
bbmi    -3.181   0.523  -4.198  -3.534  -3.186  -2.830  -2.154 1.001 20000
bgen     2.690   0.561   1.587   2.316   2.690   3.064   3.807 1.001 20000
bhr     -1.599   0.512  -2.612  -1.938  -1.599  -1.256  -0.590 1.001 20000
bmph     3.802   0.583   2.658   3.408   3.803   4.194   4.957 1.001 20000
brpe    -1.122   0.492  -2.082  -1.453  -1.124  -0.793  -0.140 1.001 20000
vv      28.195   3.561  22.038  25.725  27.893  30.389  36.048 1.001   9600
deviance 748.584   4.003 742.758 745.646 747.955 750.788 758.213 1.001   7900

```

For each parameter, n.eff is a crude measure of effective sample size, and Rhat is the potential scale reduction factor (at convergence, Rhat=1).

DIC info (using the rule, $pD = \text{var}(\text{deviance})/2$)

$pD = 8.0$ and $DIC = 756.6$

DIC is an estimate of expected predictive error (lower deviance is better).

2

Running the same model but without age, I get a DIC of 755.1.

```

library(R2jags)
mdl2 <- "
  model {

    for(i in 1:120){
      y[i] ~ dnorm(mu[i], prec)
      mu[i] <- b0 + bgen*gender[i] + bbmi*bmi[i] + brpe*rpe[i] + bhr*hr[i] +
bmph*mph[i]
    }

    b0 ~ dnorm(0 , 0.001)
    bgen ~ dnorm(0, 0.001)
    bbmi ~ dnorm(0, 0.001)
    brpe ~ dnorm(0, 0.001)
    bhr ~ dnorm(0, 0.001)
    bmph ~ dnorm(0, 0.001)

    prec <- 1/vv
    vv ~ dgamma(1.5, 0.2)

  }

"
# Assign simple names
mph <- vo2$MPH

```

```

bmi <- vo2$BMI
gender <- vo2$Gender
y <- vo2$MaxVO2ML
rpe <- vo2$RPE
hr <- vo2$HR
age <- vo2$Age1

# Standardize the covariates
mph <- (mph-mean(mph))/sd(mph)
bmi <- (bmi-mean(bmi))/sd(bmi)
gender <- (gender-mean(gender))/sd(gender)
rpe <- (rpe-mean(rpe))/sd(rpe)
age <- (age-mean(age))/sd(age)
hr <- (hr-mean(hr))/sd(hr)

writeLines(mdl12, 'vo2_v2.txt')

#What to use
data.jags <- c('y', 'gender', 'bmi', 'rpe', 'mph', 'hr')

#What to call it in the output
parms.jags <- c('b0', "brpe", 'bgen', 'bbmi', 'bmph', 'vv', 'bhr')

vo2_v2.sim <- jags(data= data.jags, parameters.to.save = parms.jags,
  model.file = 'vo2_v2.txt', inits = NULL,
  n.iter = 6000, n.thin = 1, n.chains = 4,
  n.burnin = 1000)

Compiling model graph
  Resolving undeclared variables
  Allocating nodes
Graph information:
  Observed stochastic nodes: 120
  Unobserved stochastic nodes: 7
  Total graph size: 1056

Initializing model

vo2_v2.sim

Inference for Bugs model at "vo2_v2.txt", fit using jags,
  4 chains, each with 6000 iterations (first 1000 discarded)
  n.sims = 20000 iterations saved

```

	mu.vect	sd.vect	2.5%	25%	50%	75%	97.5%	Rhat	n.eff
b0	48.773	0.483	47.830	48.445	48.770	49.099	49.715	1.001	20000
bbmi	-3.041	0.500	-4.025	-3.380	-3.042	-2.704	-2.062	1.001	13000
bgen	2.579	0.542	1.510	2.223	2.581	2.944	3.639	1.001	12000
bhr	-1.677	0.501	-2.661	-2.015	-1.674	-1.338	-0.690	1.001	5200
bmph	3.997	0.536	2.953	3.636	3.996	4.351	5.051	1.001	20000
brpe	-1.105	0.492	-2.064	-1.434	-1.108	-0.775	-0.134	1.001	20000
vv	28.070	3.462	22.049	25.589	27.801	30.288	35.516	1.001	4500
deviance	748.315	3.700	743.031	745.605	747.671	750.328	757.167	1.001	20000

For each parameter, n.eff is a crude measure of effective sample size, and Rhat is the potential scale reduction factor (at convergence, Rhat=1).

DIC info (using the rule, $pD = \text{var}(\text{deviance})/2$)

$pD = 6.8$ and $DIC = 755.2$

DIC is an estimate of expected predictive error (lower deviance is better).

3

I would choose the second model because it has a lower DIC so it is better at predicting with fewer covariates.

4

Same model but with mph*hr. This model has a DIC of 753.5.

```
library(R2jags)
mdl3 <- "
  model {

    for(i in 1:120){
      y[i] ~ dnorm(mu[i], prec)
      mu[i] <- b0 + bgen*gender[i] + bbmi*bmi[i] + brpe*rpe[i] + bhr*hr[i] +
        bmph*mph[i] + bmphhr*mphhr[i]
    }

    b0 ~ dnorm(0 , 0.001)
    bgen ~ dnorm(0, 0.001)
    bbmi ~ dnorm(0, 0.001)
    brpe ~ dnorm(0, 0.001)
    bhr ~ dnorm(0, 0.001)
    bmph ~ dnorm(0, 0.001)
    bmphhr ~ dnorm(0, .001)

    prec <- 1/vv
    vv ~ dgamma(1.5, 0.2)
```

```

}

"
#Assigning simple names for covariates
mph <- vo2$MPH
bmi <- vo2$BMI
gender <- vo2$Gender
y <- vo2$MaxVO2ML
rpe <- vo2$RPE
hr <- vo2$HR
age <- vo2$Age1

# Standardize the covariates
mph <- (mph-mean(mph))/sd(mph)
bmi <- (bmi-mean(bmi))/sd(bmi)
gender <- (gender-mean(gender))/sd(gender)
rpe <- (rpe-mean(rpe))/sd(rpe)
age <- (age-mean(age))/sd(age)
hr <- (hr-mean(hr))/sd(hr)
mphhr <- mph*hr
mphhr = (mphhr - mean(mphhr))/sd(mphhr)

writeLines(md13, 'vo2_v3.txt')

#What to use
data.jags <- c('y', 'gender', 'bmi', 'rpe', 'mph', 'hr', 'mphhr')

#What to call it in the output
parms.jags <- c('b0', "brpe", 'bgen', 'bbmi', 'bmph', 'vv', 'bhr', 'bmphhr')

vo2_v3.sim <- jags(data= data.jags, parameters.to.save = parms.jags,
  model.file = 'vo2_v3.txt', inits = NULL,
  n.iter = 6000, n.thin = 1, n.chains = 4,
  n.burnin = 1000)

Compiling model graph
  Resolving undeclared variables
  Allocating nodes
Graph information:
  Observed stochastic nodes: 120
  Unobserved stochastic nodes: 8
  Total graph size: 1293

Initializing model

```

```
vo2_v3.sim
```

```
Inference for Bugs model at "vo2_v3.txt", fit using jags,  
4 chains, each with 6000 iterations (first 1000 discarded)
```

```
n.sims = 20000 iterations saved
```

	mu.vect	sd.vect	2.5%	25%	50%	75%	97.5%	Rhat	n.eff
b0	48.780	0.476	47.854	48.460	48.776	49.100	49.709	1.001	9100
bbmi	-3.236	0.506	-4.229	-3.575	-3.239	-2.897	-2.251	1.001	8000
bgen	2.714	0.549	1.639	2.344	2.714	3.080	3.791	1.001	20000
bhr	-1.771	0.505	-2.750	-2.112	-1.771	-1.431	-0.783	1.001	5000
bmph	3.556	0.576	2.418	3.171	3.561	3.938	4.691	1.001	20000
bmphhr	-1.025	0.542	-2.075	-1.390	-1.026	-0.665	0.043	1.001	20000
brpe	-1.226	0.491	-2.182	-1.553	-1.231	-0.898	-0.258	1.001	20000
vv	27.554	3.422	21.576	25.158	27.296	29.681	34.910	1.001	20000
deviance	745.713	3.986	739.932	742.800	745.047	747.894	755.149	1.001	20000

For each parameter, n.eff is a crude measure of effective sample size,
and Rhat is the potential scale reduction factor (at convergence, Rhat=1).

DIC info (using the rule, $pD = \text{var}(\text{deviance})/2$)

$pD = 7.9$ and $DIC = 753.7$

DIC is an estimate of expected predictive error (lower deviance is better).

5

I prefer the last model because it has the lowest DIC. Adding the interaction term is worth it.

6 SAS code works, doesn't knit.

```
library(SASmarkdown)
```

```
saspath <- "C:/Program Files/SASHome/SASFoundation/9.4/sas.exe" sasopts <- "-nosplash  
-ls 75" knitr::opts_chunk$set(engine="sas", engine.path=saspath, engine.opts=sasopts,  
comment=NA)
```

```
knitr::opts_chunk$get()engine knitr::opts_chunk$get()engine.path  
knitr::opts_chunk$get()engine.opts
```

1 Sas

DIC is 756.5

```
data vo2; infile 'C:/Users/nateh/Documents/Stat 451/vo2.dat'; input ID Gender Age BMI  
MPH HR RPE MAXVO2ML; run;
```

```
proc standard data=vo2 out=vo2 mean=0 std=1; var ID Gender Age BMI MPH HR RPE;; run;
```

```
proc mcmc data = vo2 nbi = 30000 nmc = 300000 thin = 30 outpost =
'C:/Users/nateh/Documents/Stat 451/MLRHW4.sas7bdat' dic propcov=quanew
monitor=(parms) stats = all; parms b0 0; parms bmph 0; parms bage 0; parms bhr 0; parms
brpe 0; parms bgen 0; parms bbmi 0; parms vv 1.5; prior b0 ~ normal(0, var = 1000); prior
bmph: ~ normal(0, var = 1000); prior bage: ~ normal(0, var = 1000); prior bhr: ~
normal(0, var = 1000); prior brpe: ~ normal(0, var = 1000); prior bbmi: ~ normal(0, var =
1000); prior bgen: ~ normal(0, var = 1000); prior vv ~ gamma(1.5, scale = 5); mu = b0 +
bageGender + bbmiBMI + brpeRPE + bhrHR + bmphMPH + bageAge; model MAXVO2ML ~
normal(mu, var = vv); run;
```

2

Model without age, DIC is 755.1

```
data vo2; infile 'C:/Users/nateh/Documents/Stat 451/vo2.dat'; input ID Gender Age BMI
MPH HR RPE MAXVO2ML; run;
```

```
proc standard data=vo2 out=vo2 mean=0 std=1; var ID Gender Age BMI MPH HR RPE;; run;
```

```
proc mcmc data = vo2 nbi = 30000 nmc = 300000 thin = 30 outpost =
'C:/Users/nateh/Documents/Stat 451/MLRHW4_2.sas7bdat' dic propcov=quanew
monitor=(parms); parms b0 0; parms bmph 0; parms bhr 0; parms brpe 0; parms bgen 0;
parms bbmi 0; parms vv 1.5; prior b0 ~ normal(0, var = 1000); prior bmph: ~ normal(0,
var = 1000); prior bhr: ~ normal(0, var = 1000); prior brpe: ~ normal(0, var = 1000); prior
bbmi: ~ normal(0, var = 1000); prior bgen: ~ normal(0, var = 1000); prior vv ~
gamma(1.5, scale = 5); mu = b0 + bgenGender + bbmiBMI + brpeRPE + bhrHR + bmph*MPH;
model MAXVO2ML ~ normal(mu, var = vv); run;
```

3 Sas

2nd model is better, lower DIC

4 SAS

Model without age, with mphhr. DIC is 753.6

```
data vo2; infile 'C:/Users/nateh/Documents/Stat 451/vo2.dat'; input ID Gender Age BMI
MPH HR RPE MAXVO2ML; run;
```

```
# Standardize Variables
```

```
proc standard data=vo2 out=vo2 mean=0 std=1; var ID Gender Age BMI MPH HR RPE;; run;
```

```
proc mcmc data = vo2 nbi = 30000 nmc = 300000 thin = 30 outpost =
'C:/Users/nateh/Documents/Stat 451/MLRHW4_3.sas7bdat' dic propcov=quanew
monitor=(parms); parms b0 0; parms bmph 0; parms bhr 0; parms brpe 0; parms bgen 0;
```



```
parms bbmi 0; parms binteraction 0; parms vv 1.5; prior b0 ~ normal(0, var = 1000); prior  
bmph: ~ normal(0, var = 1000); prior bhr: ~ normal(0, var = 1000); prior brpe: ~  
normal(0, var = 1000); prior bbmi: ~ normal(0, var = 1000); prior bgen: ~ normal(0, var =  
1000); prior binteraction ~ normal(0, var = 1000); prior vv ~ gamma(1.5, scale = 5); mu =  
b0 + bgenGender + bbmiBMI + brpeRPE + bhrHR + bmphMPH + binteraction(MPH*HR);  
model MAXVO2ML ~ normal(mu, var = vv); run;
```

5 SAS

The results are the same, the third model is the best.