

Time Series Analysis

Basics of Time Series Analysis

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Trend Estimation: Data Example

About This Lesson



Data Example: Temperature in Atlanta, Georgia

Data: Average monthly temperature records starting in 1879 until 2016.

- Available from the iWearherNet.com
- The Weather Bureau (now the National Weather Service) began keeping weather records for Atlanta for 138 years since October 1, 1878.
- Provided in Fahrenheit degrees

Do we find an increasing trend in temperature in Atlanta?

Data Example in R

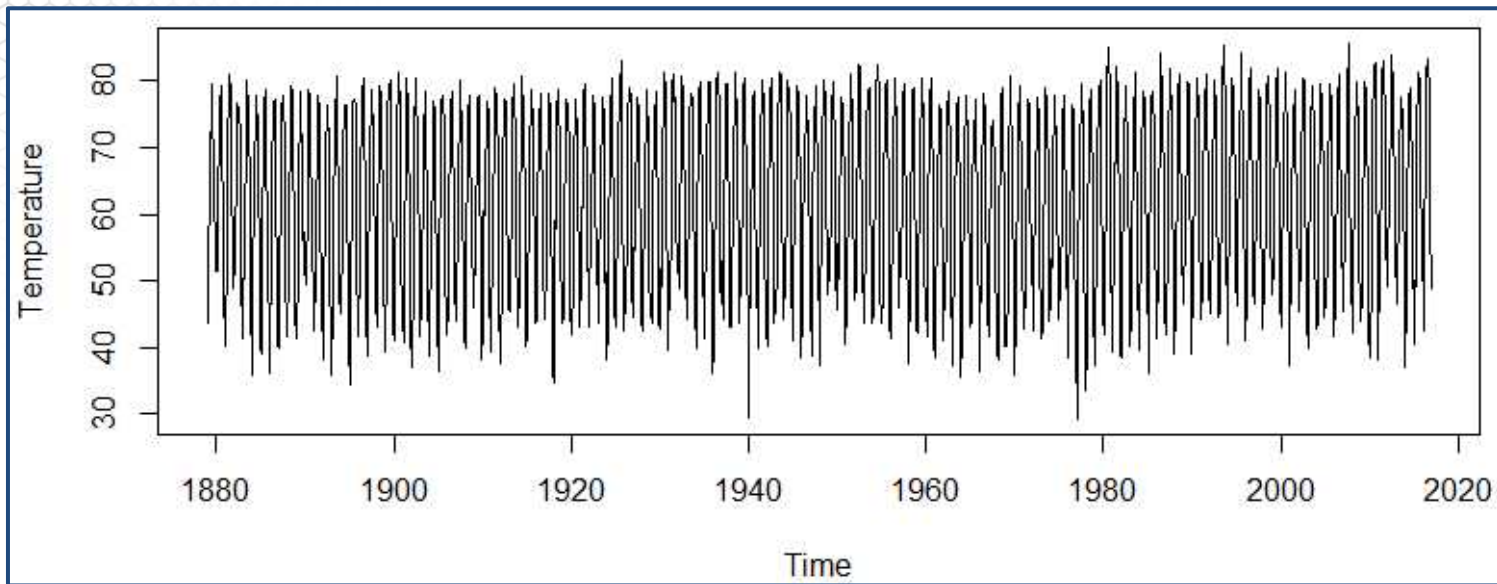
Time Series Plot

```
data = read.table("AvTempAtlanta.txt",header=T)  
names(data)
```

```
[1] "Year"  "Jan"   "Feb"   "Mar"   "Apr"   "May"   "Jun"   "Jul"   "Aug"   "Sep"  
[11] "Oct"   "Nov"   "Dec"   "Annual"
```

```
temp = as.vector(t(data[,-c(1,14)]))  
temp = ts(temp,start=1879,frequency=12)  
ts.plot(temp, ylab="Temperature")
```

Data Example in R



Trend: Moving Average

Create equally spaced time points for fitting trends

```
time.pts = c(1:length(temp))
```

```
time.pts = c(time.pts - min(time.pts))/max(time.pts)
```

Fit a moving average

```
mav.fit = ksmooth(time.pts, temp, kernel = "box")
```

```
temp.fit.mav = ts(mav.fit$y,start= 1879,frequency=12)
```

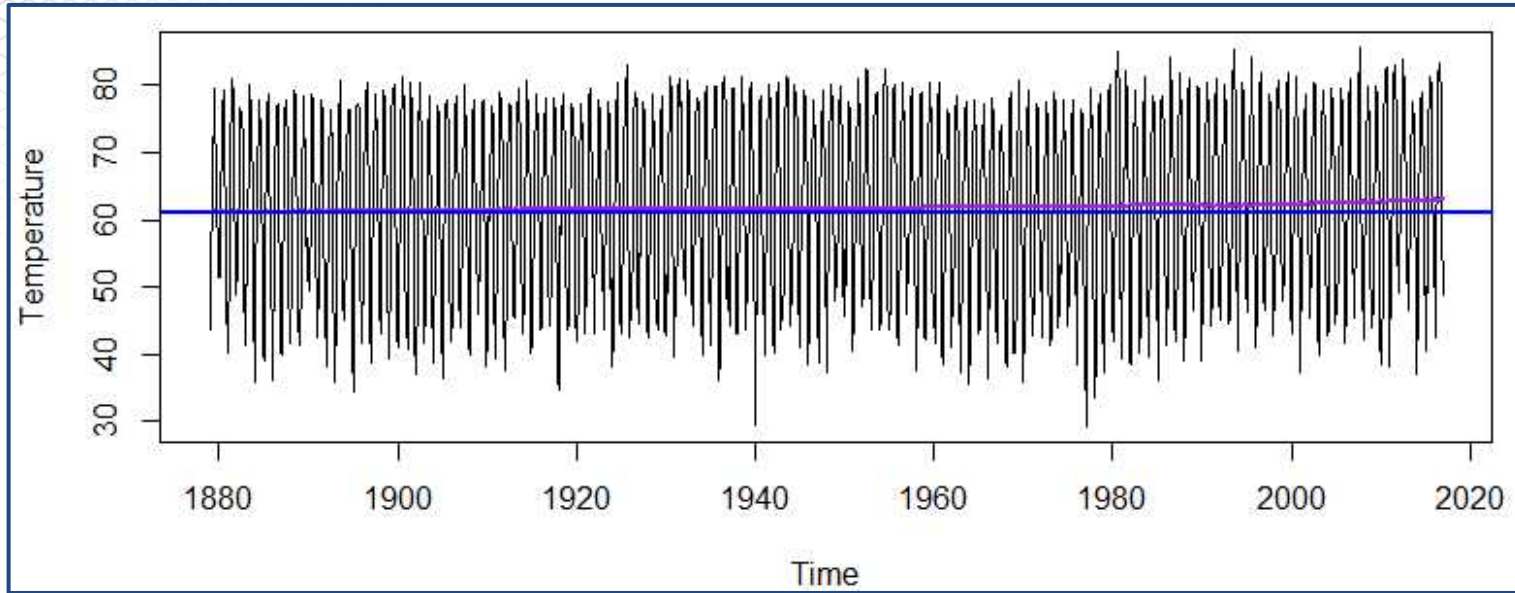
Is there a trend?

```
ts.plot(temp,ylab="Temperature")
```

```
lines(temp.fit.mav,lwd=2,col="purple")
```

```
abline(temp.fit.mav[1],0,lwd=2,col="blue")
```

Trend: Moving Average



Trend: Parametric Regression

Fit a parametric quadratic polynomial

```
x1 = time.pts
```

```
x2 = time.pts^2
```

```
lm.fit = lm(temp~x1+x2)
```

```
summary(lm.fit)
```

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	61.4247	0.9841	62.420	<2e-16 ***
x1	-1.5723	4.5481	-0.346	0.730
x2	3.4937	4.4062	0.793	0.428

Is there a trend?

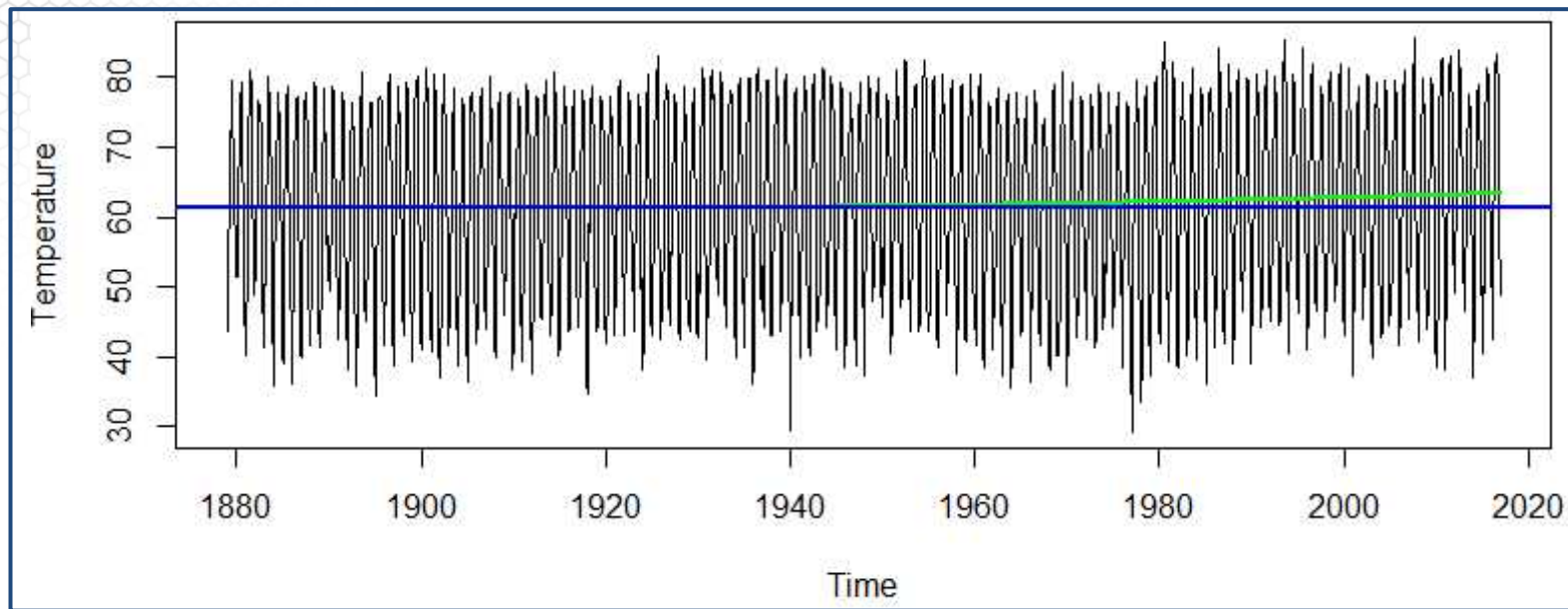
```
temp.fit.lm = ts(fitted(lm.fit),start=1879,frequency=12)
```

```
ts.plot(temp,ylab="Temperature")
```

```
lines(temp.fit.lm,lwd=2,col="green")
```

```
abline(temp.fit.mav[1],0,lwd=2,col="blue")
```


Trend: Parametric Regression



Trend: Non- Parametric Regression

Local Polynomial Trend Estimation

```
loc.fit = loess(temp~time.pts)
temp.fit.loc = ts(fitted(loc.fit),start=1879,frequency=12)
```

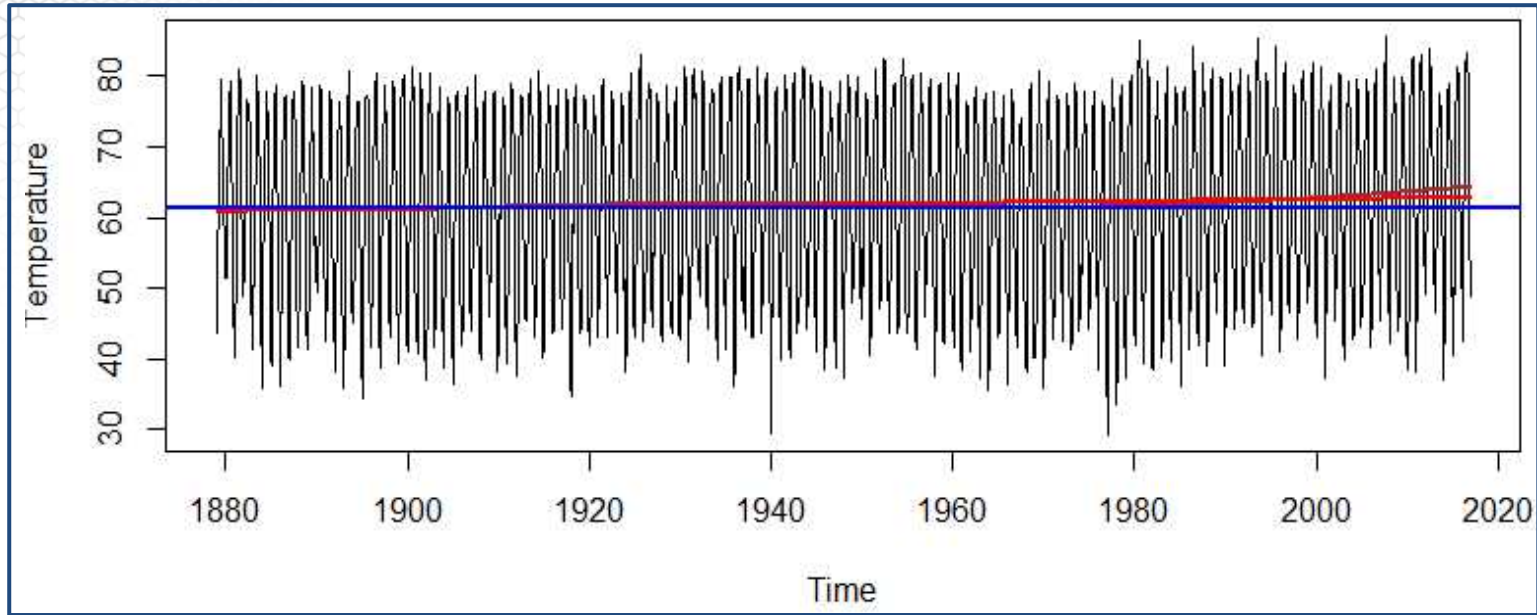
Splines Trend Estimation

```
library(mgcv)
gam.fit = gam(temp~s(time.pts))
temp.fit.gam = ts(fitted(gam.fit),start=1879,frequency=12)
```

Is there a trend?

```
ts.plot(temp,ylab="Temperature")
lines(temp.fit.loc,lwd=2,col="brown")
lines(temp.fit.gam,lwd=2,col="red")
abline(temp.fit.loc[1],0,lwd=2,col="blue")
```

Trend: Non- Parametric Regression

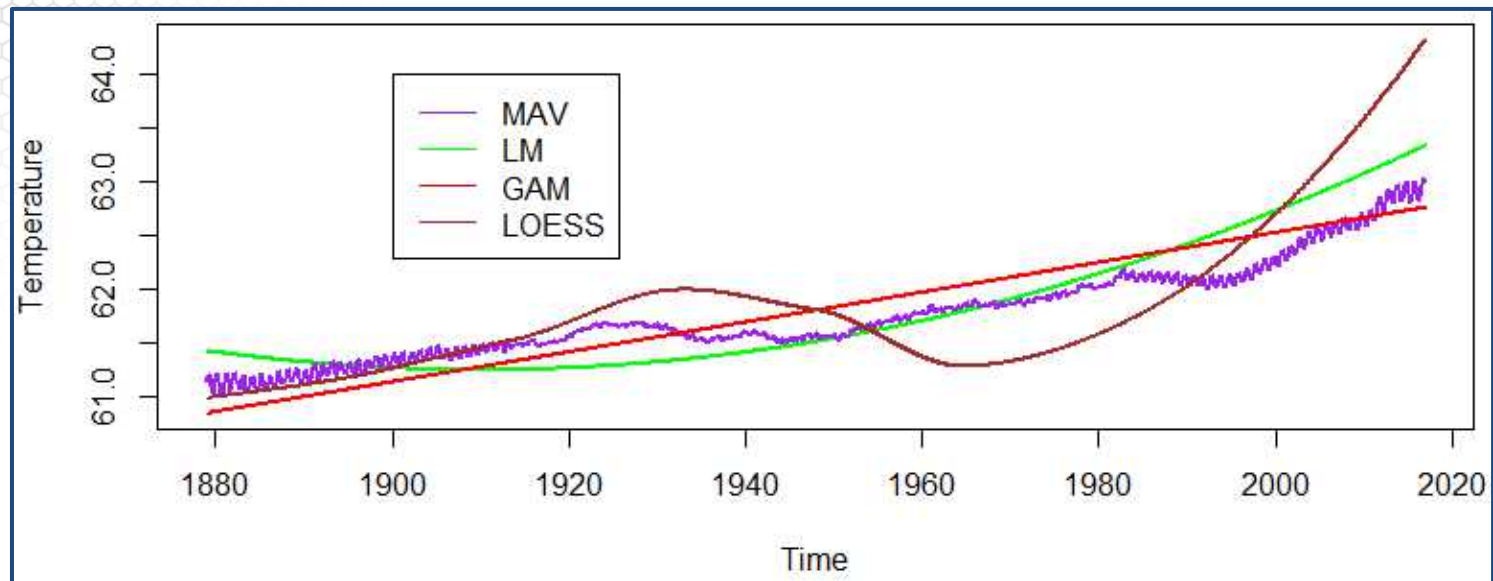


Trend: Comparison

Compare all estimated trends

```
all.val = c(temp.fit.mav,temp.fit.lm,temp.fit.gam,temp.fit.loc)
ylim= c(min(all.val),max(all.val))
ts.plot(temp.fit.lm,lwd=2,col="green",ylim=ylim,ylab="Temperature")
lines(temp.fit.mav,lwd=2,col="purple")
lines(temp.fit.gam,lwd=2,col="red")
lines(temp.fit.loc,lwd=2,col="brown")
legend(x=1900,y=64,legend=c("MAV", "LM", "GAM", "LOESS"),lty = 1,
col=c("purple", "green", "red", "brown"))
```

Trend: Comparison



Summary

