

# Randomized Trials

## (SOC 412)

Week 1 Lecture 2

Sherred Hall 306



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CITP mit media lab

# What we will cover today

Discuss reading

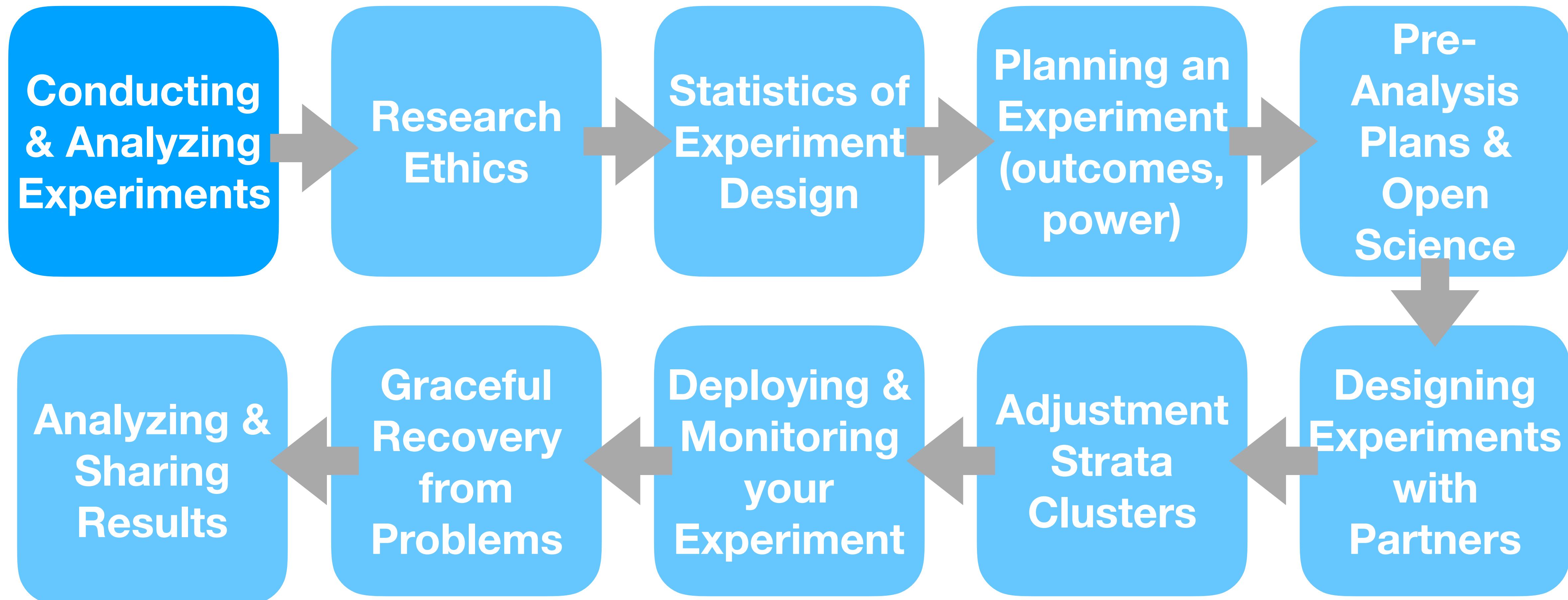
Introduction to randomized trials

Discuss assignment

# Questions about Assignments

- Project Assignments: Due Tuesday 9pm





# Lilly Heir Makes \$100 Million Bequest to Poetry Magazine

By STEPHEN KINZER NOV. 19, 2002

An ailing heir who tried but failed to have her poems published in a small literary journal has given that journal an astonishing bequest that is likely to be worth more than \$100 million.

Ruth Lilly, 87, an heir to the Eli Lilly pharmaceutical fortune, submitted several poems to Poetry magazine in the 1970's and was rewarded only with handwritten rejection notes from the editor, Joseph Parisi. Evidently she did not take the rejections to heart. Mr. Parisi announced her gift at the magazine's 90th-anniversary dinner on Friday.

"It's a real mind-blower," said the United States' poet laureate, Billy Collins, who was at the dinner. "Poetry has always had the reputation as being the poor little match girl of the arts. Well, the poor little match girl just hit the lottery."





Week 1: Introducing Randomized Trials (SOC412)



**POEM OF THE DAY**

## And Day Brought Back My Night

BY GEOFFREY BROCK

**COLLECTION**

## Celebrating Black History Month

**COLLECTION**

## An Introduction to the Harlem Renaissance

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POEMS POETS PROSE COLLECTIONS LISTEN LEARN VISIT **POETRY MAGAZINE**

PROSE FROM POETRY MAGAZINE

## From "Fiends Fell"

BY TOM PICKARD

A diary of a secluded place.



# How should the Poetry Foundation Share Poetry On Facebook?



# Reviewing Historical Data (Simulated)

```
1 head(all.poems[c("author", "title", "sim.interactions", "length", "name.sex", "color")], 15)
```

author	title	sim.interactions	length	name.sex	color
Aaron Shurin	The Bride of Frank	100	12	male	TRUE
Aaron Shurin	Plume	32	856	male	TRUE
Aaron Poochigian	The Vigil	34	147	male	TRUE
Aaron Shurin	Cool Dust	12	1082	male	FALSE
Aaron Shurin	Then	39	1552	male	FALSE
Abid B Al-Abras	Last Simile	13	554	male	TRUE
Abigail Deutsch	Twenty-Two	60	803	female	TRUE
Abigail Deutsch	After the Disaster	25	814	female	TRUE
Abraham Cowley	Platonic Love	17	1077	male	FALSE
Abraham Lincoln	To Rosa	50	277	male	TRUE

# Reviewing Historical Data (Simulated)

```
1 ## SHOW THE DIFFERENCE IN MEANS
2 aggregate(sim.interactions ~ color,
3             data=all.poems, mean)
```

color	sim.interactions
FALSE	25.75
TRUE	33.76

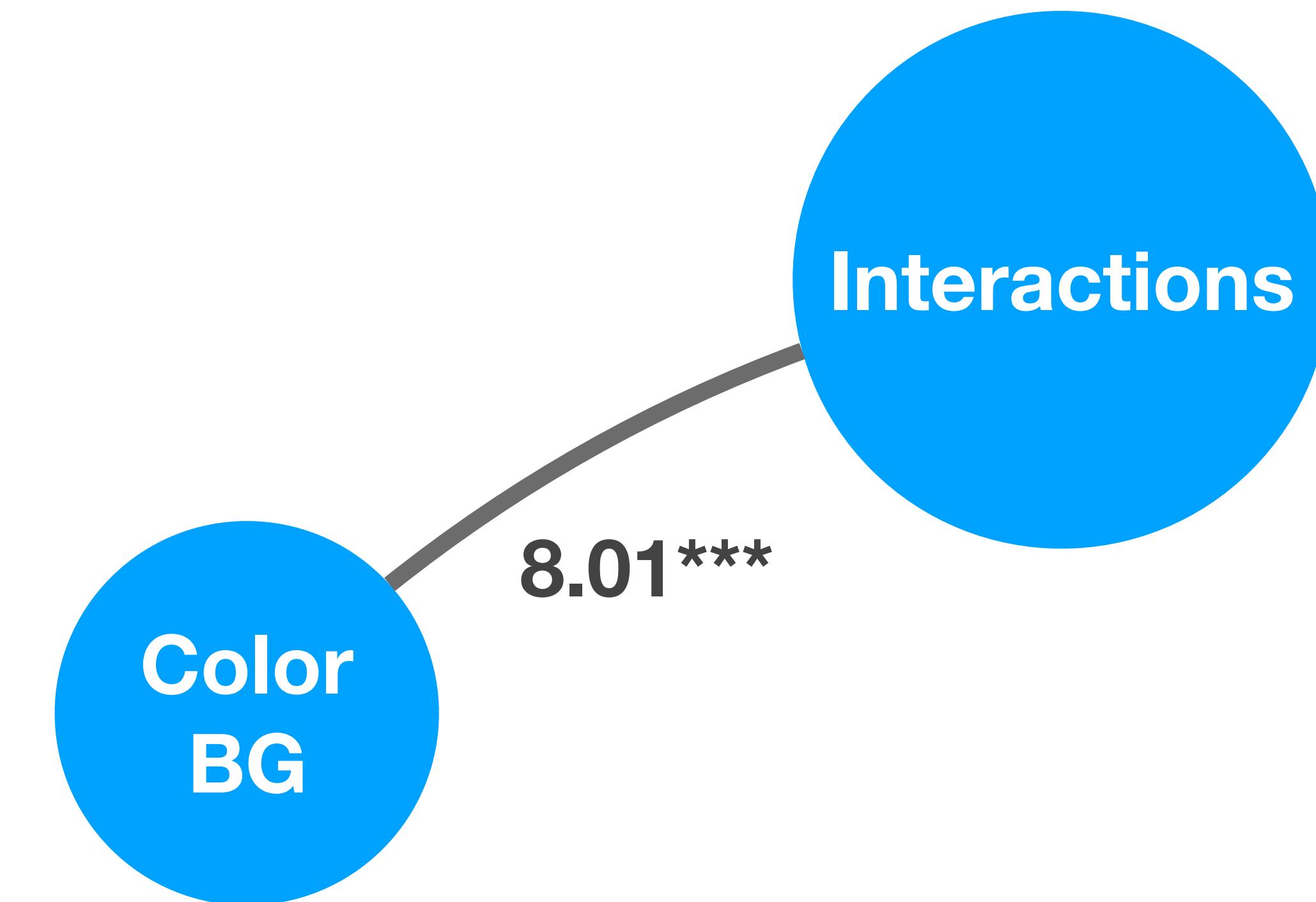
# Reviewing Historical Data (Simulated)

```
1 ## CONDUCT A T-TEST BETWEEN COLOR AND PLAIN  
2 print(t.test(all.poems$sim.interactions ~ all.poems$color))
```

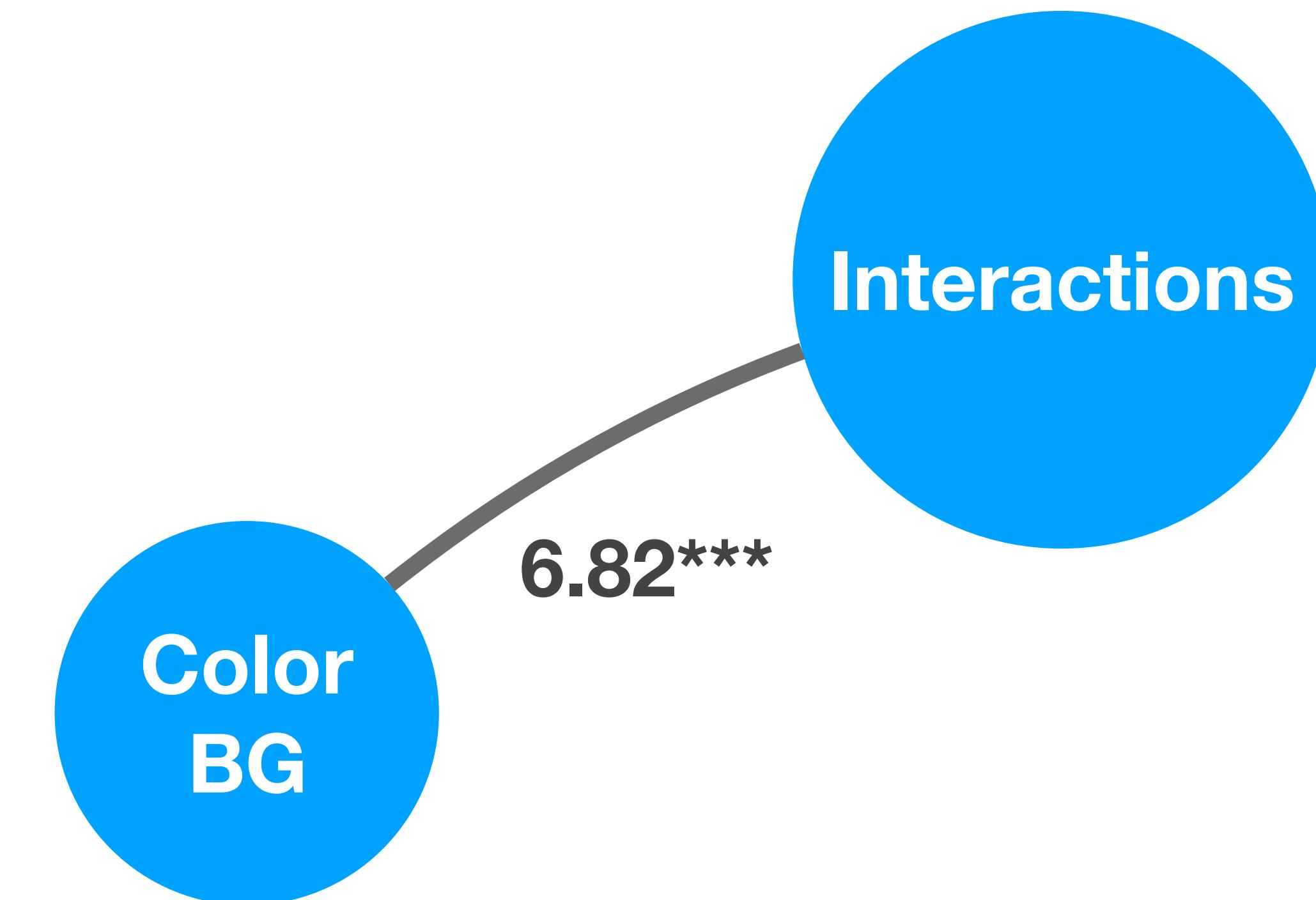
Welch Two Sample t-test

```
data: all.poems$sim.interactions by all.poems$color  
t = -26, df = 11000, p-value <2e-16  
alternative hypothesis: true difference in means is not equal to 0  
95 percent confidence interval:  
-8.621 -7.393  
sample estimates:  
mean in group FALSE mean in group TRUE  
25.75 33.76
```

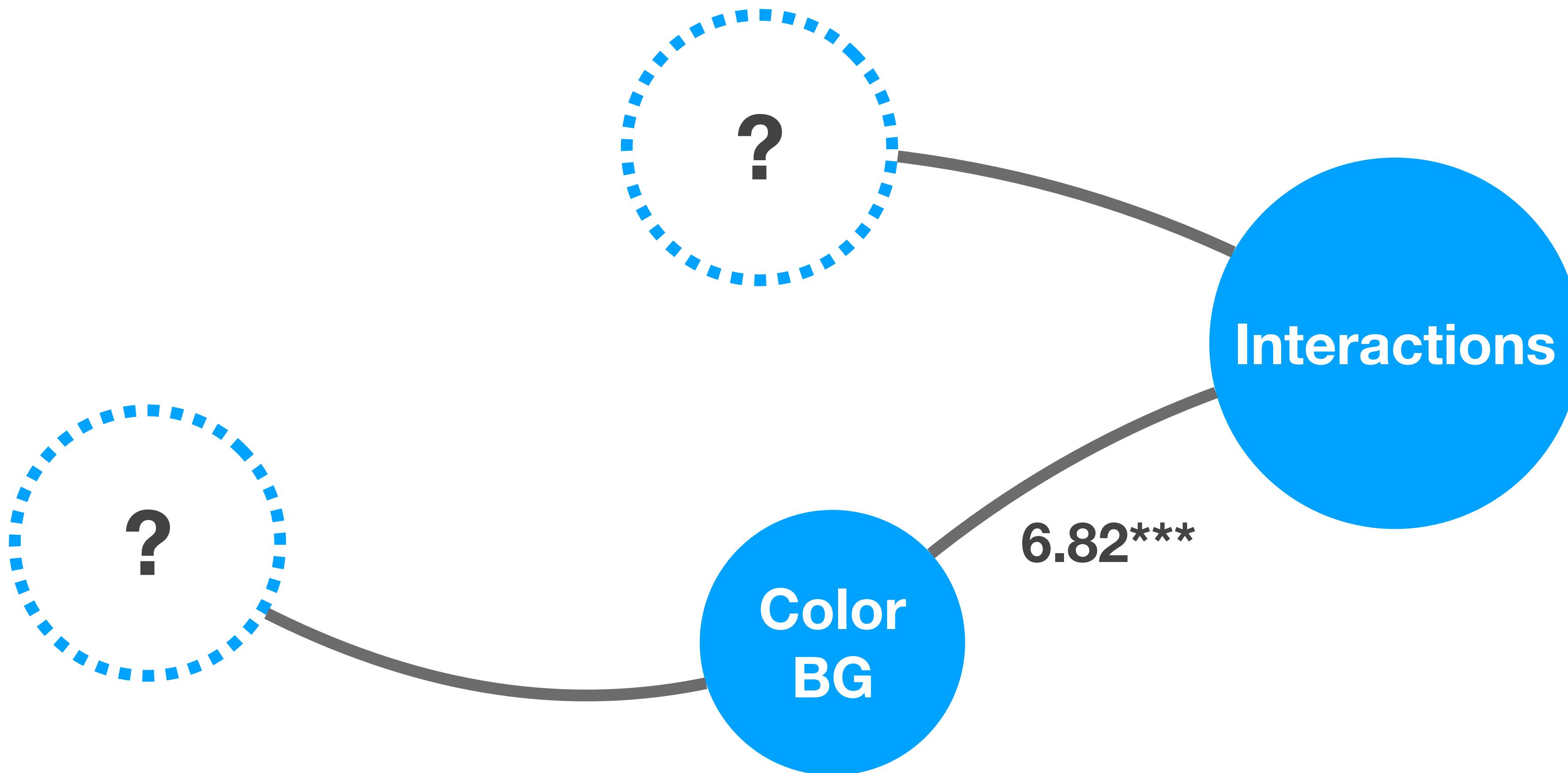
# Path Diagram



# What Do We Mean by Correlation != Causation?



# Unobserved Confounders

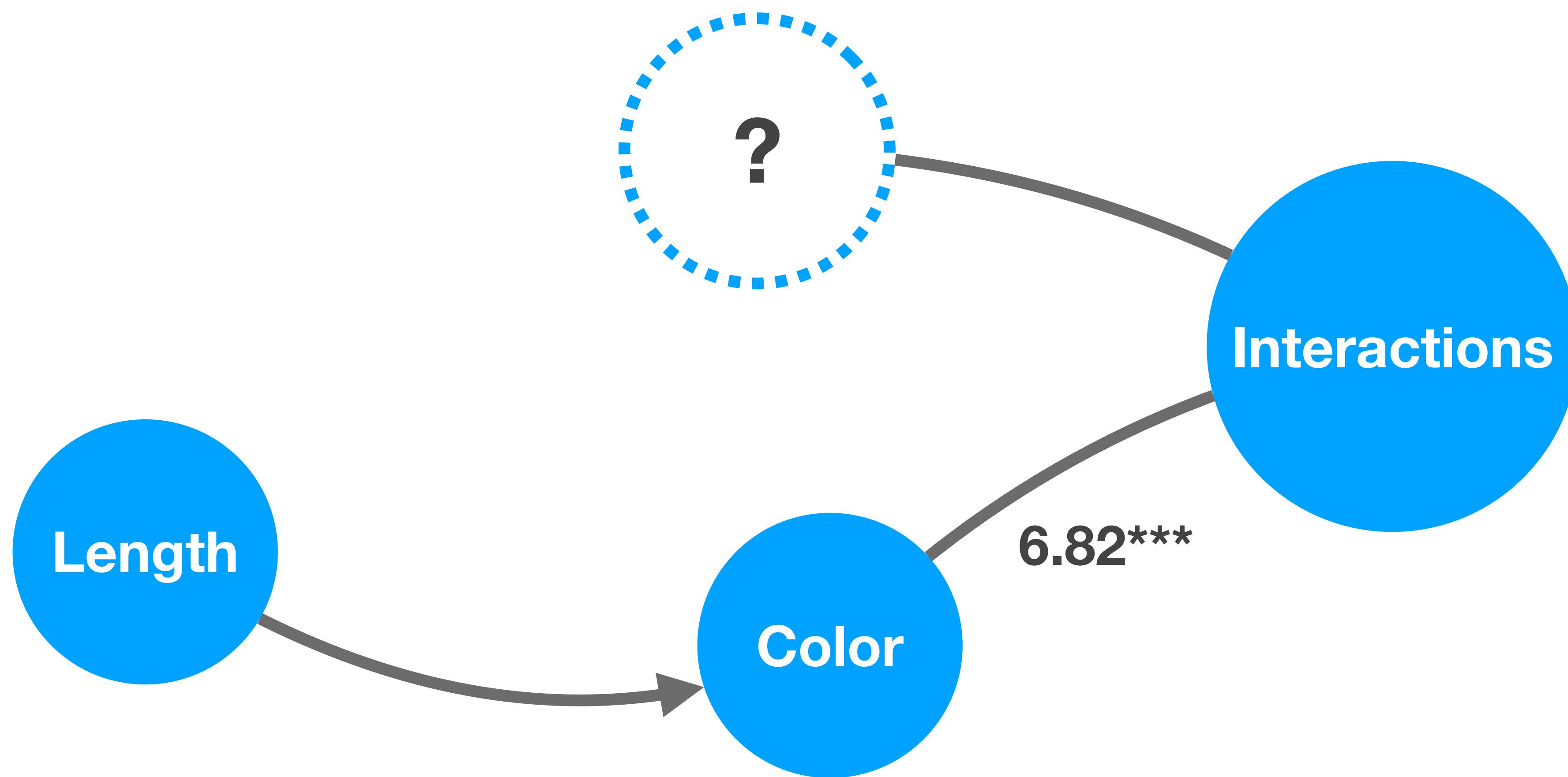


Twenge, J. M., Joiner, T. E., Rogers, M. L., & Martin, G. N. (2018). Increases in depressive symptoms, suicide-related outcomes, and suicide rates among US adolescents after 2010 and links to increased new media screen time. *Clinical Psychological Science*, 6(1), 3-17.

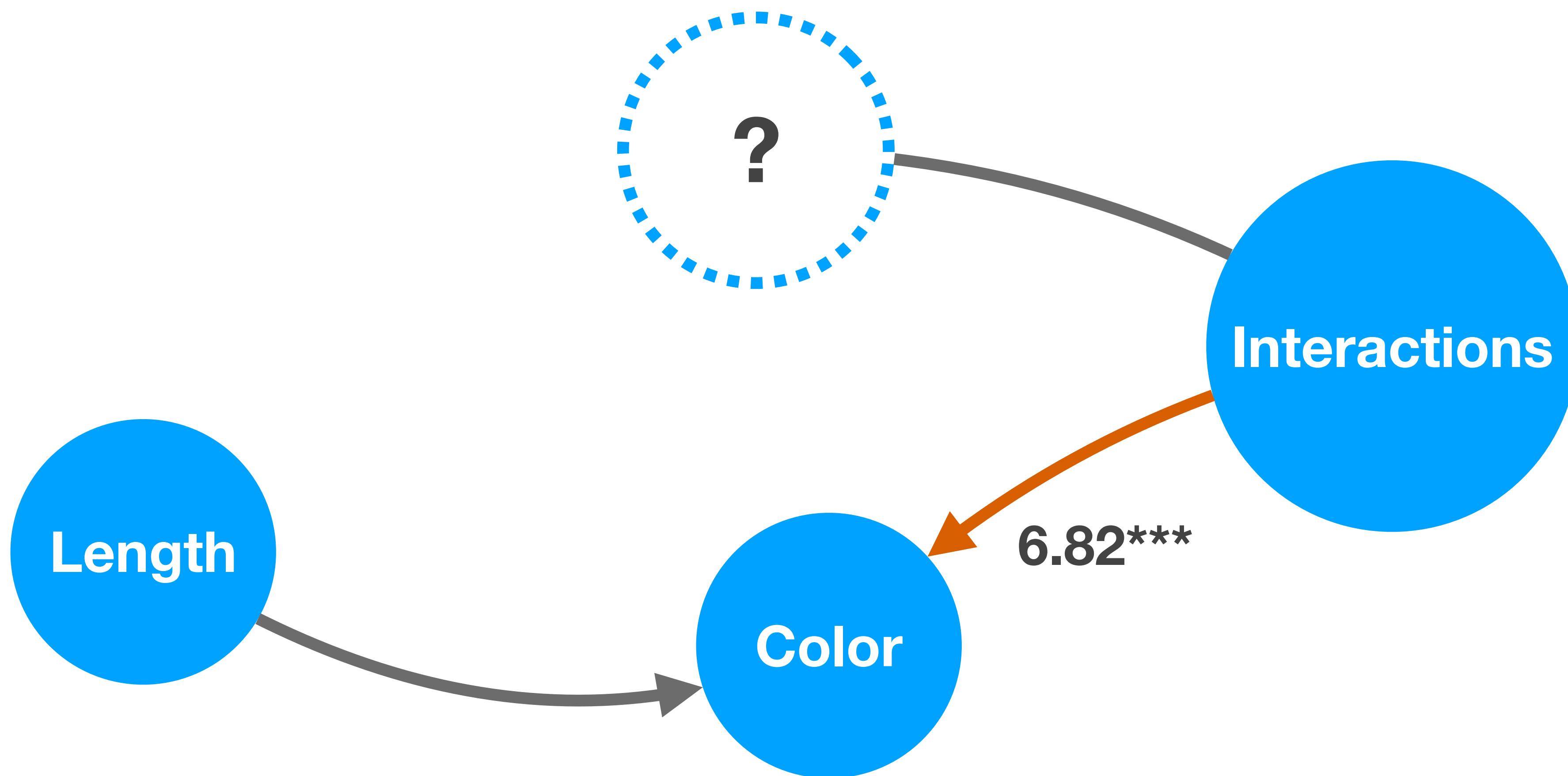
# Problem: Facebook Has a Character Limit for Color Backgrounds



# Confounder: Longer Poems are Less Popular, and Longer Poems Can't Have Color BGs



# Direction of Causality



# Why Experiment? (methodology)

- Causal explanation vs description
- Addresses unobserved confounders
- Unbiased inference (e.g. if the experiment were replicated an infinite number of times, our model would generate the right answer on average)
- Up-front design (“ex ante”) in principle limits the analyst’s discretion

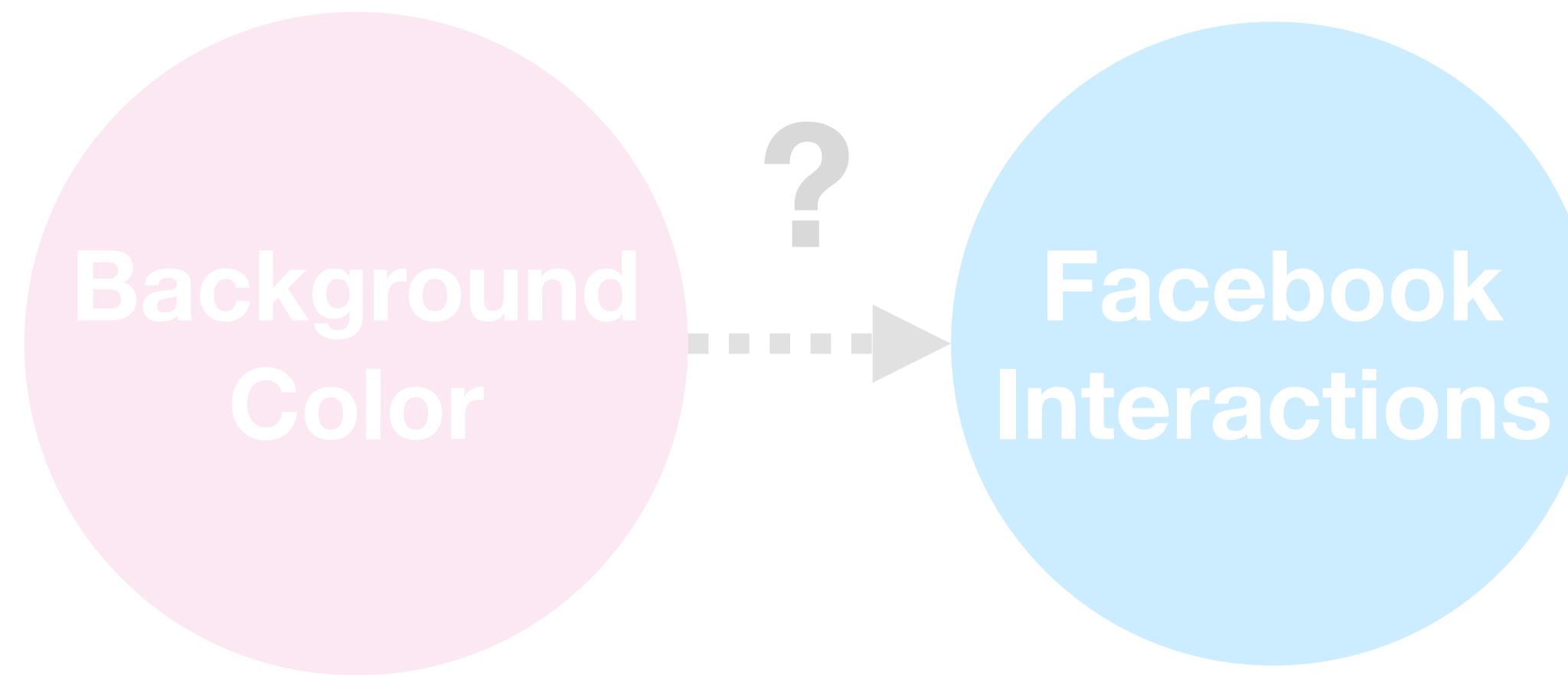
# Parts of an Experiment (example)

When the skies opened and **dumped \$185 million on an obscure Chicago poetry journal** in 2002, it was as much a burden as a gift...

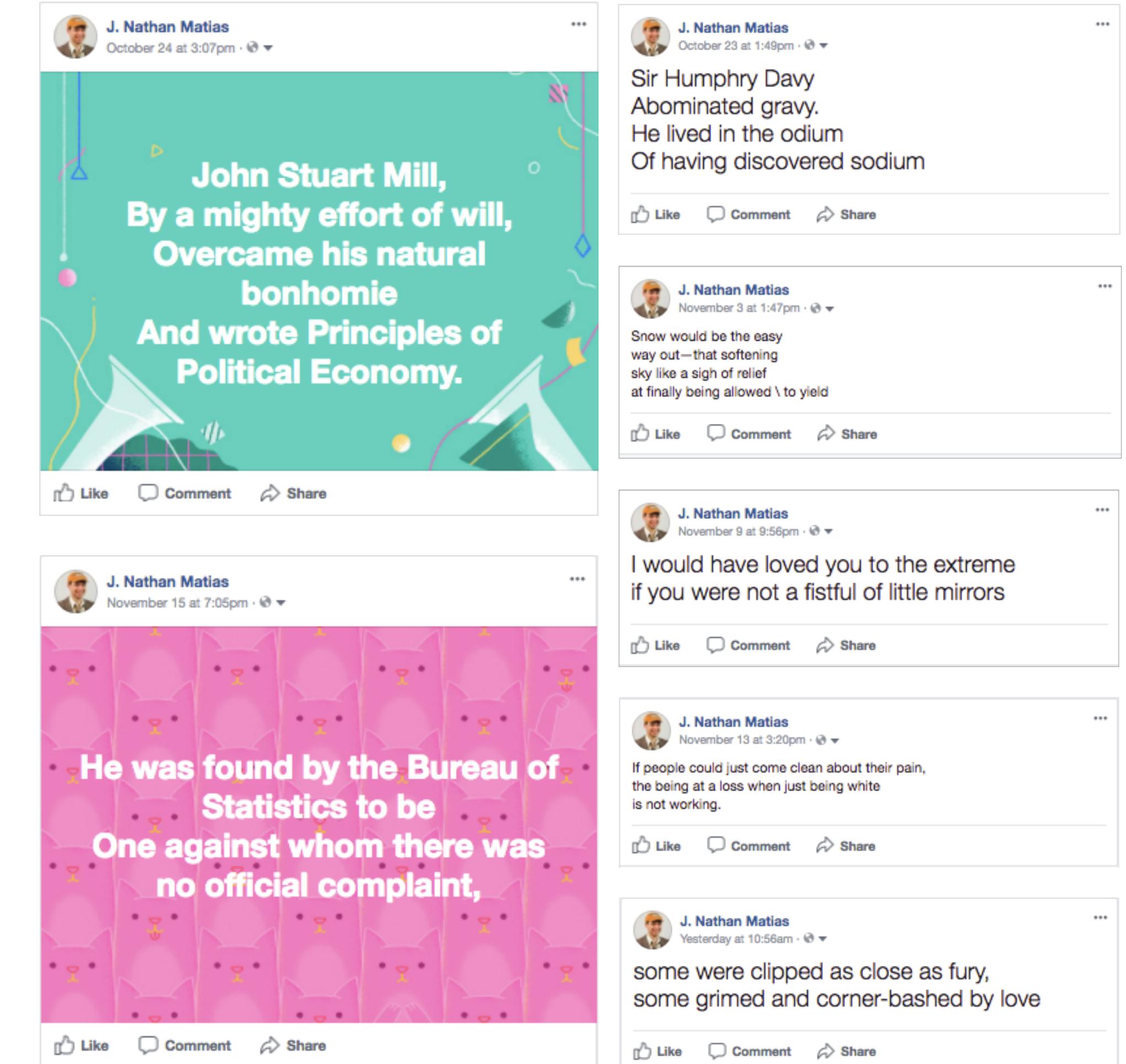
Barr still speaks in unpoetic terms like "cost per impact"

Fisher, Daniel. ***No Rhyme or Reason***. Forbes, Jan 7, 2011.

# Parts of an Experiment



1. Does A **Colored Background Increase Facebook Interactions** on average?
2. If so, **by how much** on average?



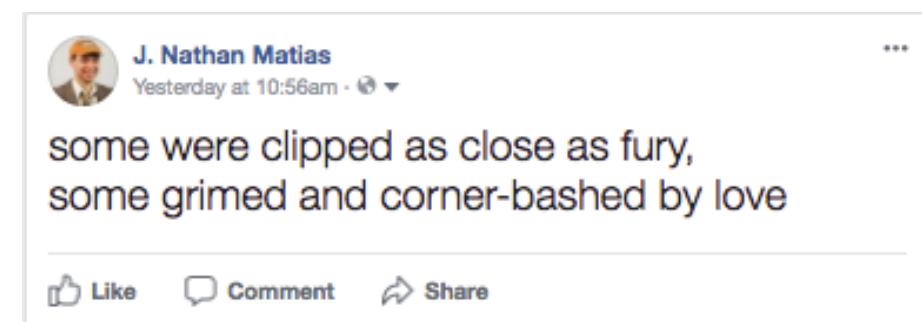
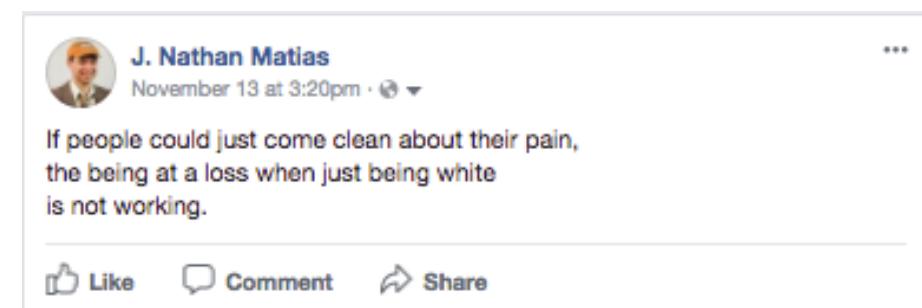
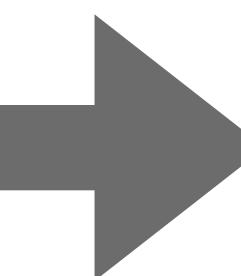
# Parts of an Experiment



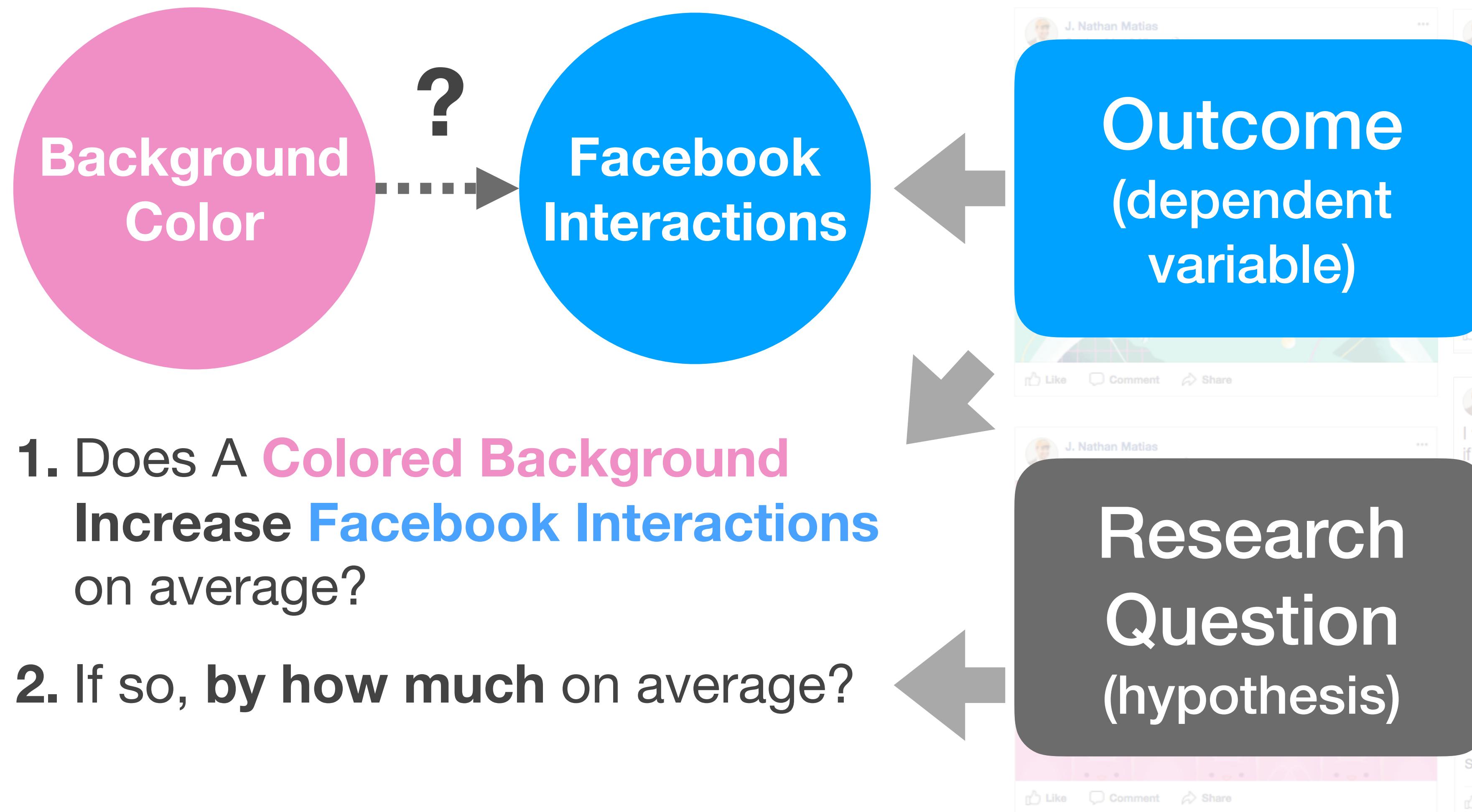
?



1. Does A **Colored Background Increase Facebook Interactions** on average?
2. If so, by how much?

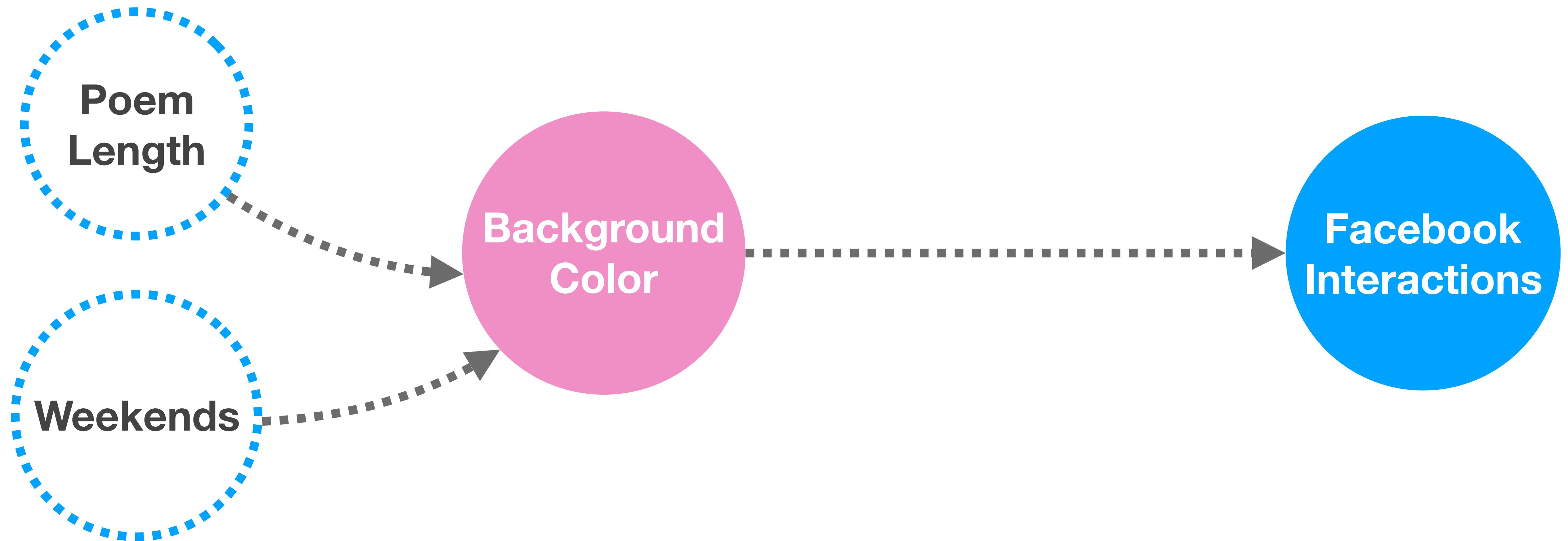


# Parts of an Experiment

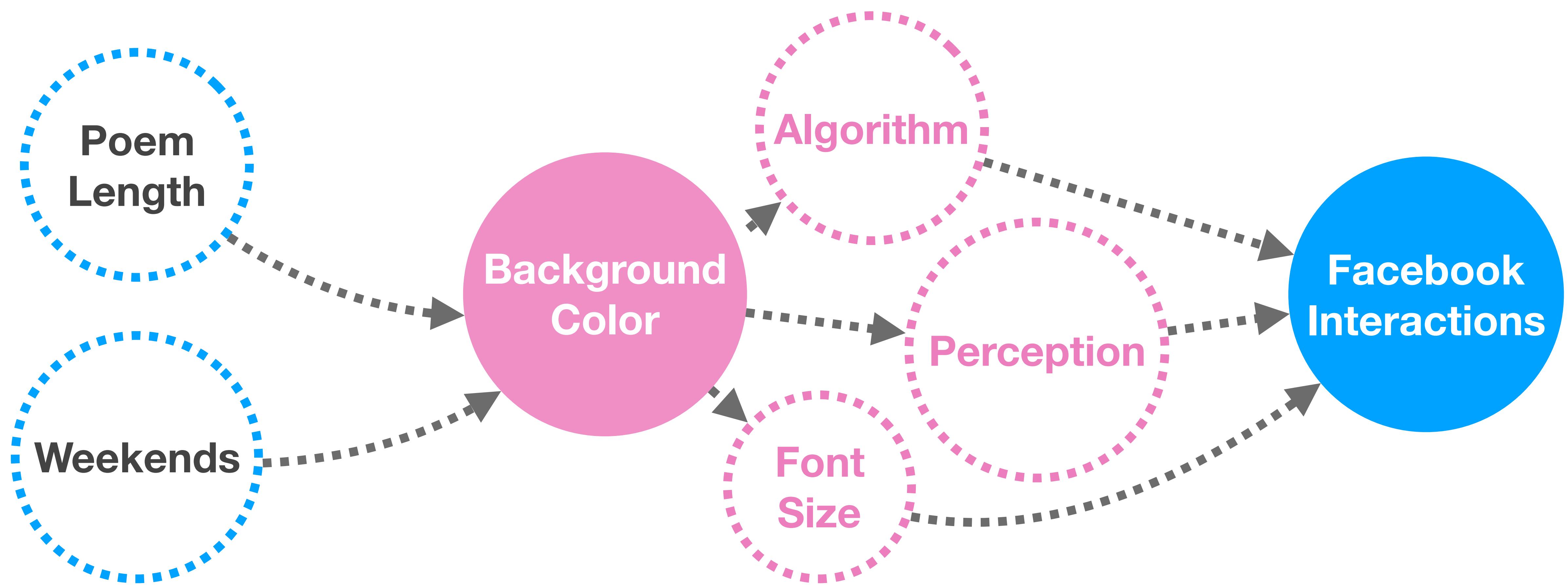


# Unobserved Confounders

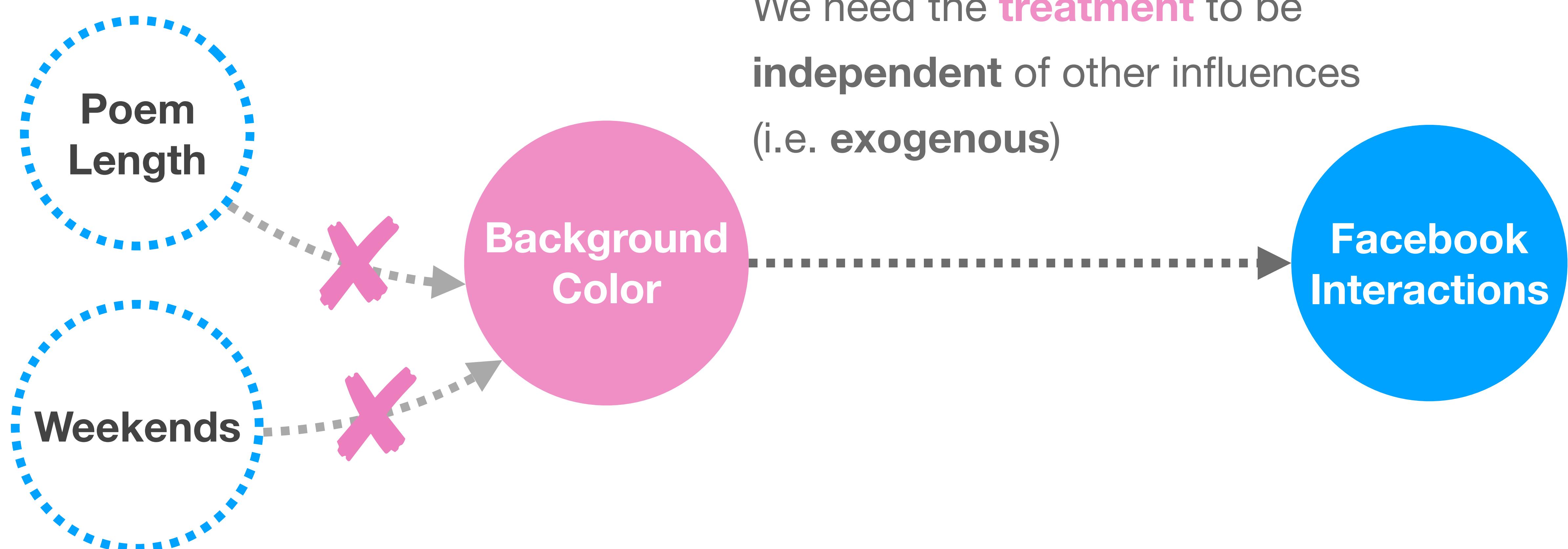
(by the way, this graph is called a path diagram)



# Unobserved Confounders



# Independence of the Treatment



# Random Assignment

By using random assignment to choose between the **treatment** and **control** (conditions)

we ensure that the treatment is **independent** (exogenous) of outside influence, and that any **difference in outcomes** is due to **the effect of the intervention**

# Understanding Randomization via Sampling

Imagine each poem has a basic potential “interactability” and that the poem-poster unconsciously allocates colors based on that factor

0 6 3 0 1 1 3 6 9 9 0 0



# Understanding Randomization via Sampling

Now imagine that we allocate poems into groups based on a random sample

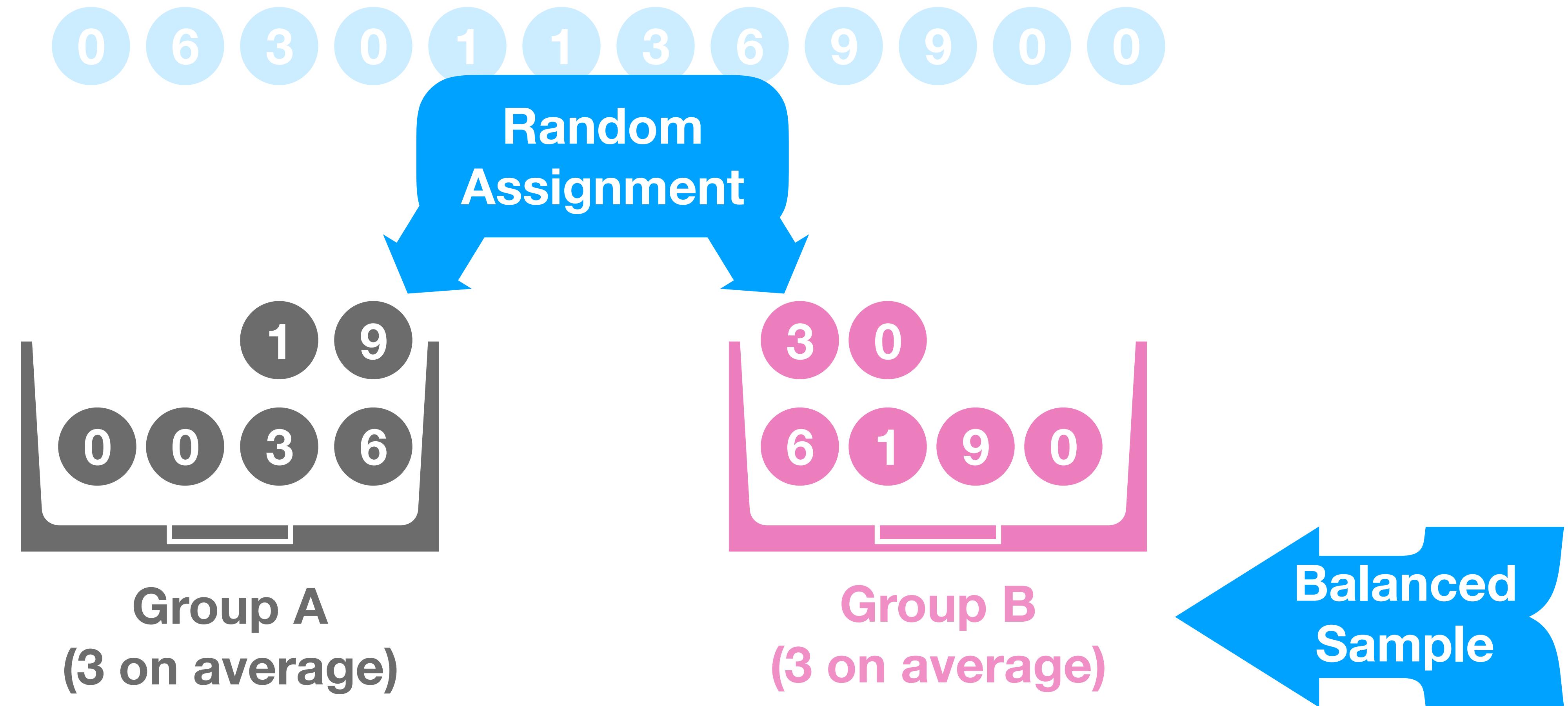


3 interactions  
on average



# Understanding Randomization via Sampling

Now imagine that we allocate poems into groups based on a random sample



# Understanding Randomization via Sampling

Now imagine that posting the colored background has an effect

0 6 3 0 1 1 3 6 9 9 0 0

⚡ +2 interactions  
on average



Plain Text



# Potential Outcomes (ATE = 2)

ID (Units)	CONTROL	TREATMENT	Effect
1	0	2	2
2	6	8	2
3	3	5	2
4	0	2	2
5	1	3	2
6	1	3	2
7	3	5	2
8	6	8	2
9	9	11	2
10	9	11	2
11	0	2	2
12	0	2	2

# Potential Outcomes (ATE = 2.15)

ID (Units)	CONTROL	TREATMENT	Effect
1	0	1	1.592
2	6	8	2.486
3	3	4	1.599
4	0	2	2.179
5	1	2	1.531
6	1	3	2.507
7	3	5	2.282
8	6	8	2.283
9	9	11	2.992
10	9	11	2.088
11	0	1	1.041
12	0	3	3.261

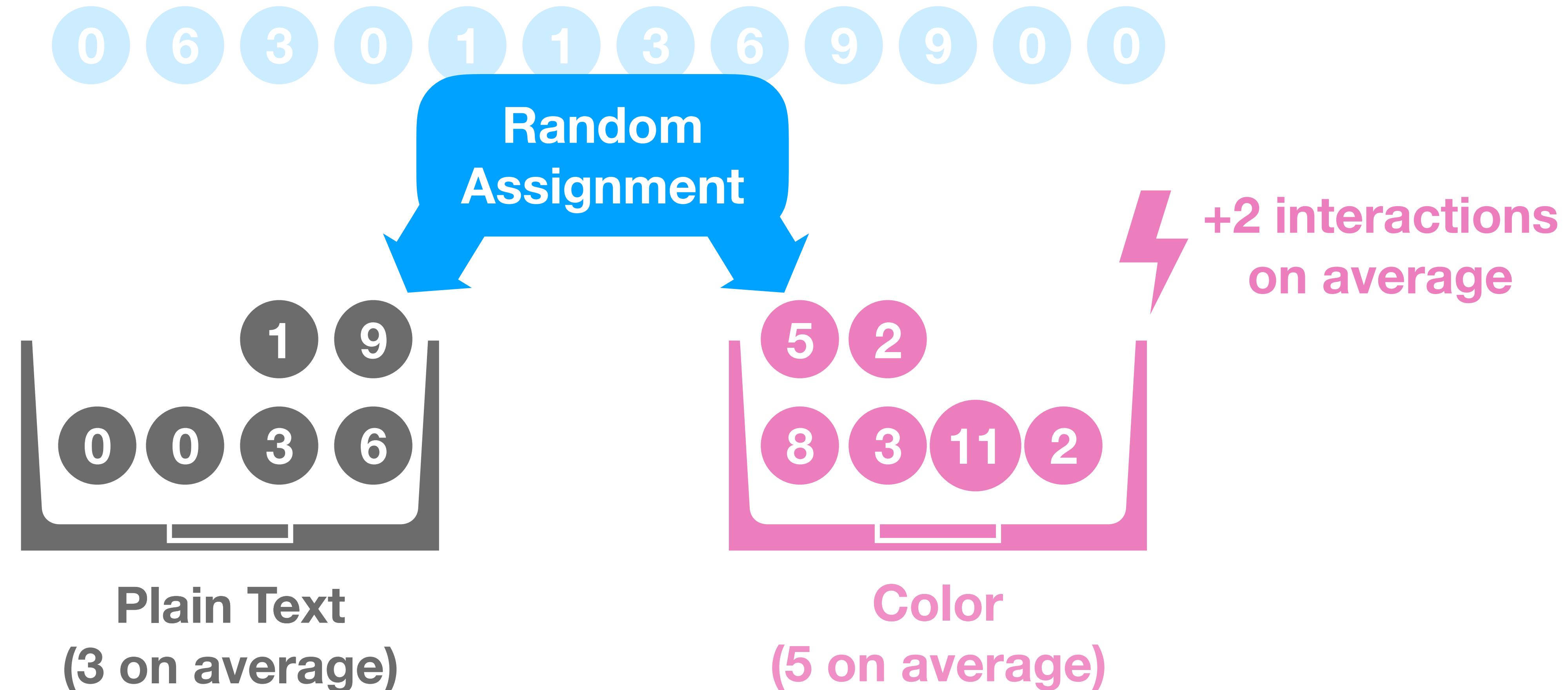
# Problem of Causal Inference:

we can observe, at most,  
one of the potential outcomes  
for each unit

Rubin, D. B. (2003). **Basic concepts of statistical inference for causal effects in experiments and observational studies.** Cambridge, MA: Harvard University, Department of Statistics.

# Understanding Randomization via Sampling

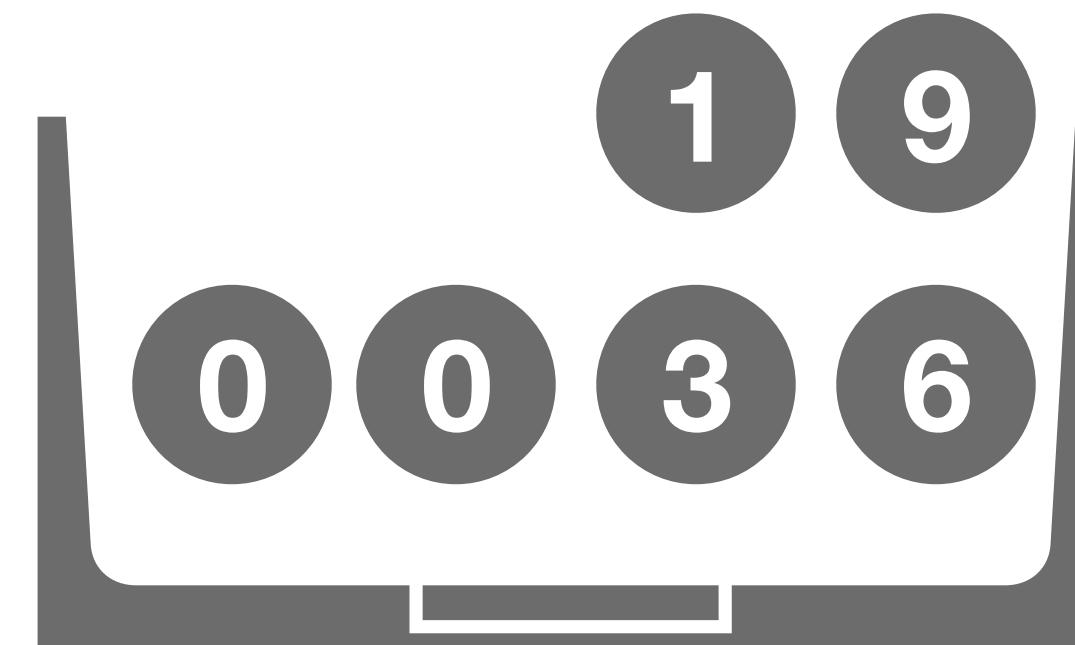
Now imagine that posting the colored background has an effect



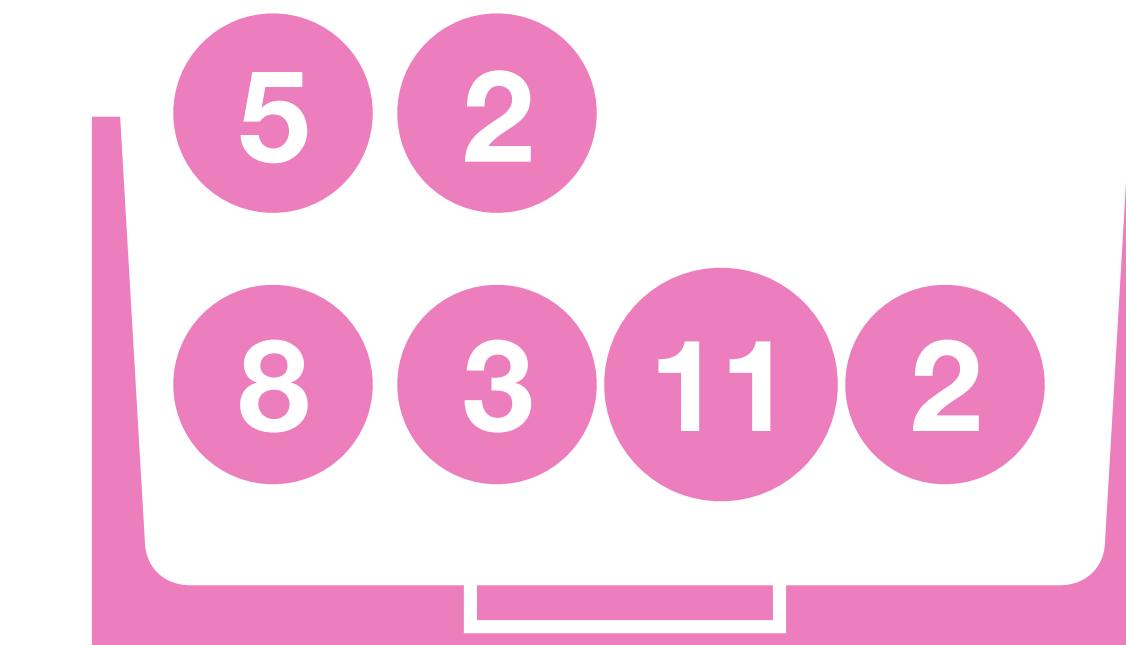
# Average Treatment Effect (ATE)



+2 interactions  
on average



Plain Text  
(3 on average)

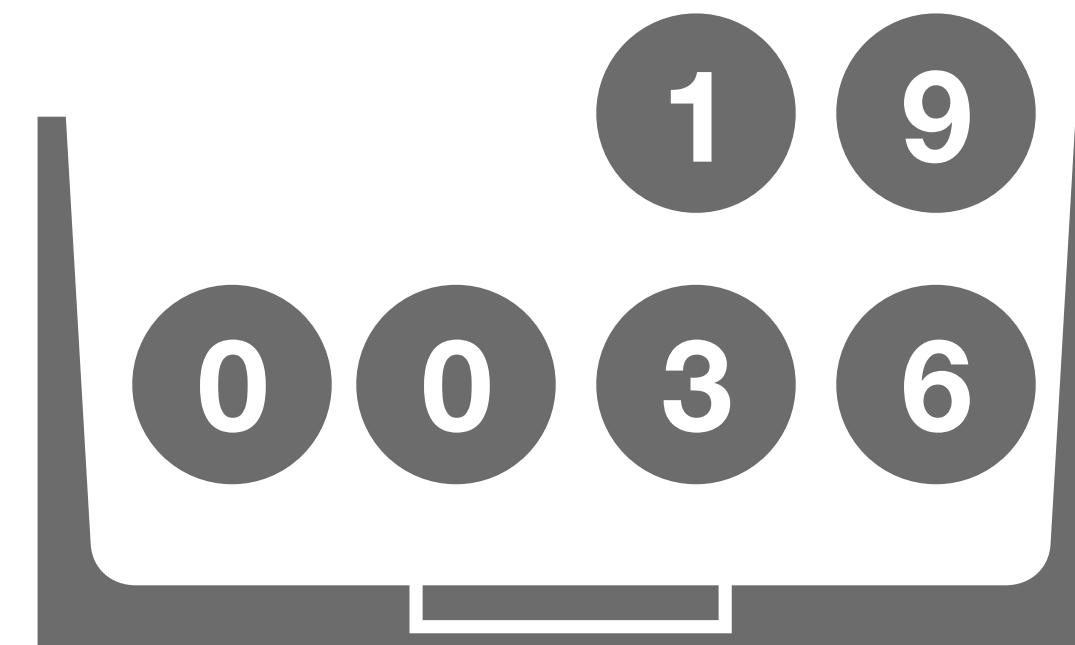


Color  
(5 on average)

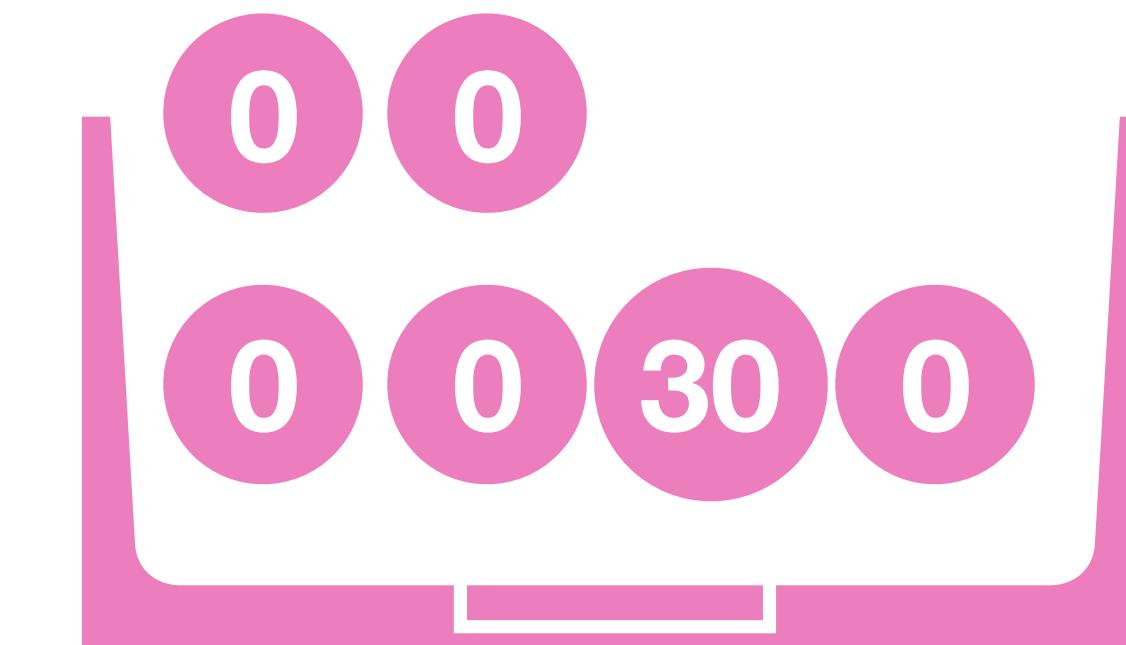
# Average Treatment Effect (ATE)

APPLIES TO POPULATIONS **NOT TO INDIVIDUALS**

 +2 interactions  
on average



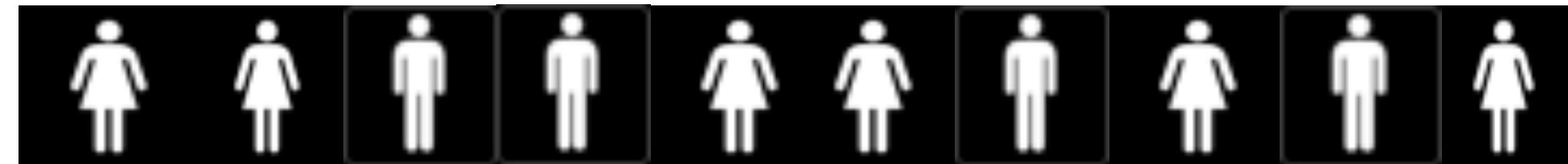
Plain Text  
(3 on average)



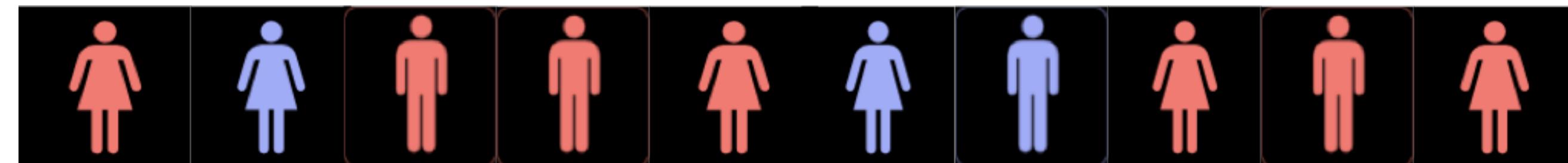
Color  
(5 on average)

# Simple Randomization

**Sample:**



**Iteration  
1:**



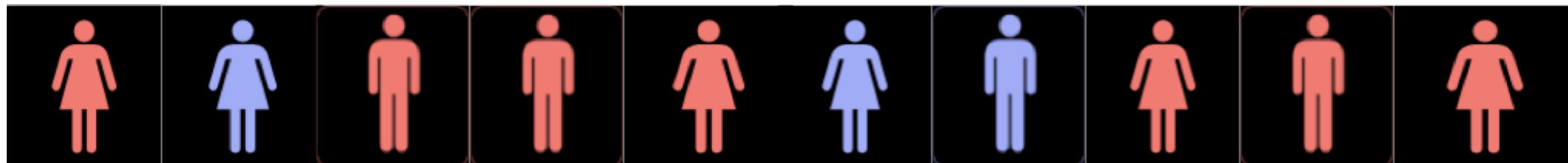
# Simple Randomization

May not allocate the expected number of participants  
to treatment and control

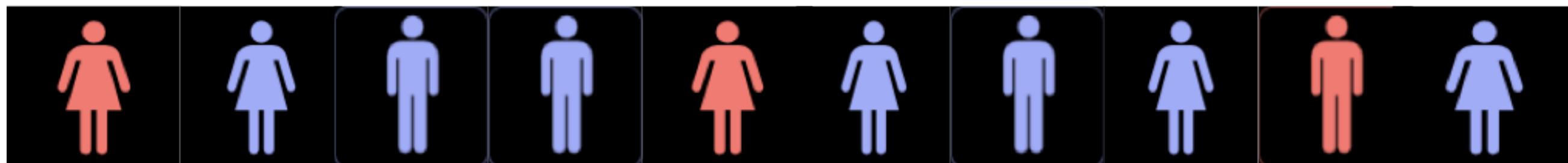
**Sample:**



**Iteration**

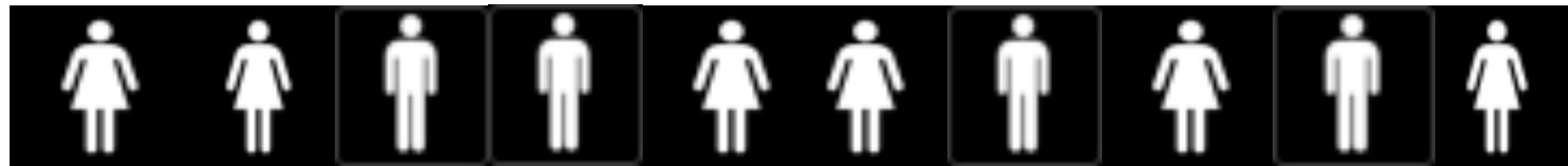


**Iteration**

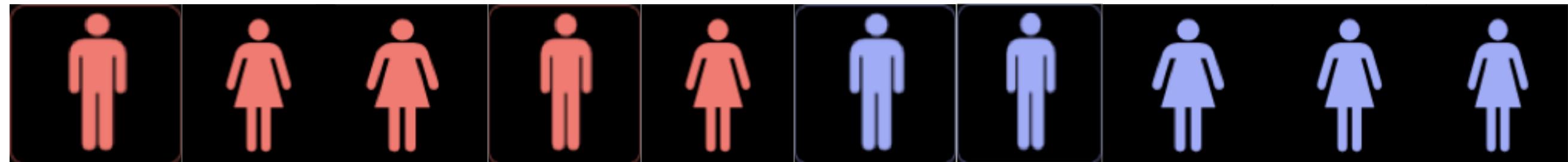


# Complete Randomization

**Sample:**



**Iteration**



# Average Treatment Effect (ATE)

(log-transformed dependent variable)

$$\ln(Interactions + 1) = \alpha + \beta_1 Background + \epsilon$$

```
lm( log1p(interactions) ~ condition, data=poems )
```

Example at [github.com/natematias/SOC412/tree/master/1-facebook-poem](https://github.com/natematias/SOC412/tree/master/1-facebook-poem)

# Average Treatment Effect (ATE)

(log-transformed dependent variable)

```
Call:
lm(formula = log1p(interactions) ~ condition, data = poems)

Residuals:
    Min      1Q  Median      3Q     Max 
-1.6856 -0.5869 -0.1596  0.7456  3.0329 

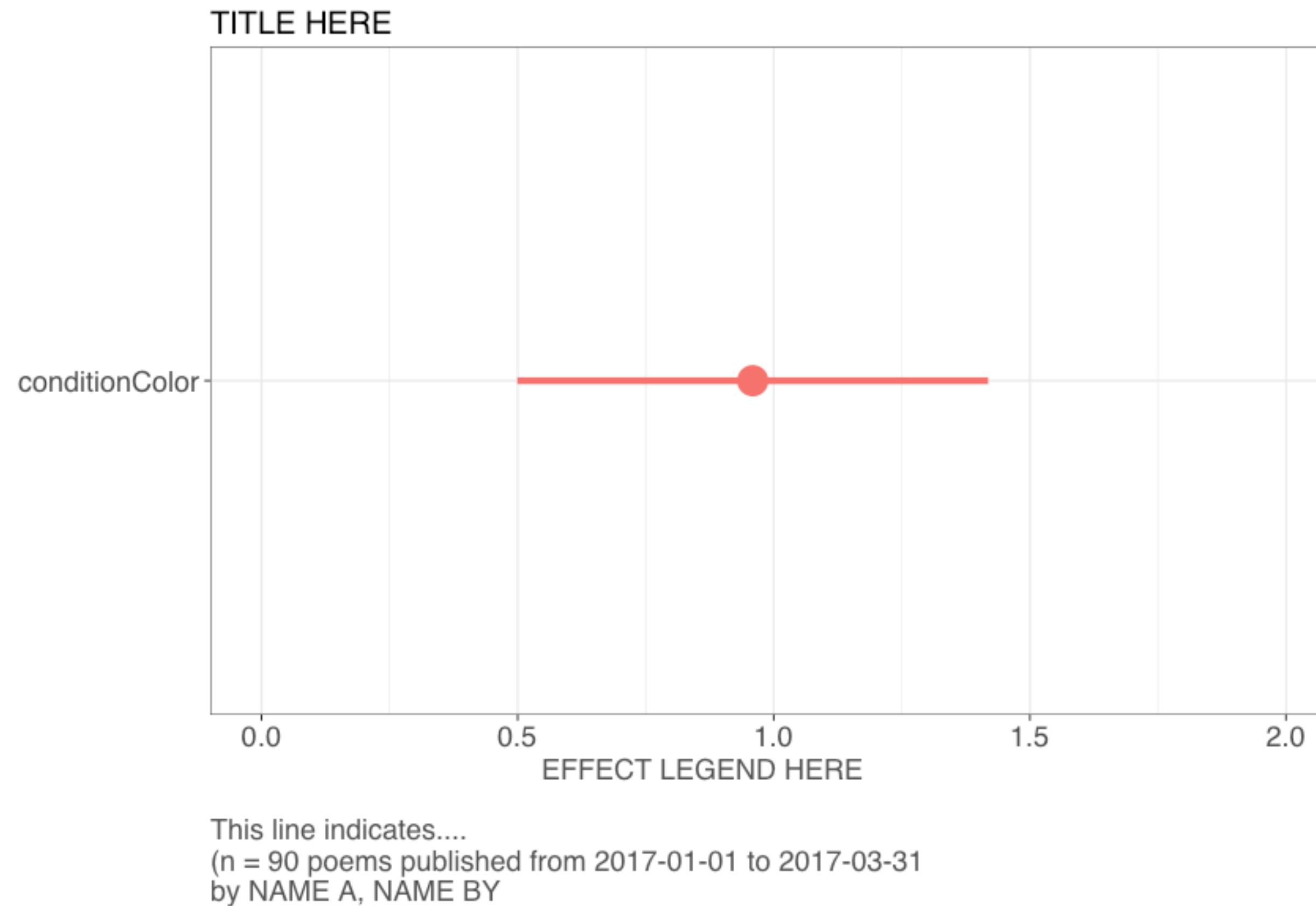
Coefficients:
            Estimate Std. Error t value Pr(>|t|)    
(Intercept)  1.6856     0.1635 10.309 < 2e-16 ***
conditionColor 0.9589     0.2312  4.147 7.74e-05 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 1.097 on 88 degrees of freedom
Multiple R-squared:  0.1635, Adjusted R-squared:  0.154 
F-statistic: 17.2 on 1 and 88 DF,  p-value: 7.737e-05
```

Example at [github.com/natematias/SOC412/tree/master/1-facebook-poem](https://github.com/natematias/SOC412/tree/master/1-facebook-poem)

# Average Treatment Effect (ATE)

(log-transformed dependent variable)



Example at [github.com/natematias/SOC412/tree/master/1-facebook-poem](https://github.com/natematias/SOC412/tree/master/1-facebook-poem)

# Assumptions of ATE

- **Random assignment** of participants to treatment
  - implies that receiving the treatment is statistically independent of participants' potential outcomes
- **Non-interference**: a participant's potential outcomes reflect only whether they receive the treatment themselves (not by others receiving it)

# Assumptions of ATE

- **Excludability** a participant's potential outcomes respond only to the defined treatment, not other extraneous factors that may be correlated with treatment
  - importance of defining the treatment precisely and maintaining symmetry between treatment and control groups (e.g. through blinding)

# Conspicuously Absent Assumptions

- Random sampling of subjects from a larger population is not a core assumption
- The issue of “external validity” is a separate question that relates to the issue of whether the results obtained from a given experiment apply to other subjects, treatments, contexts, and outcomes
- For now, we aim only to estimate the ATE in our subject pool