

I. Important Formulas in Analysis

algorithm

$$\sum_{i=1}^u 1 = u - 1 + 1$$

C++ code

```
int i = 0;
int n = 5;
while (i <= n) {
    cout << "hi" << endl;
    i++;
}
```

algorithm

$$\sum_{i=0}^n i = \sum_{i=1}^n i = 1 + 2 + \dots + n = \frac{n(n+1)}{2} \approx \frac{1}{2} n^2 \in \Theta(n^2)$$

C++ code

```
int i, j;
int n = 5;
for (i = 1; i <= n; i++) {
    for (j = 1; j <= i; j++) {
        cout << "hi" << endl;
    }
}
```

II. Practice Problems

[0, 1, 3, 2, 7, 3, 5] $O(n^2)$

Distinct
array elements
algorithm

i j - - - -
i - - - -
i - - - -
i - - - -
i - - - -
i - - - -
i - - - -

```
for (int i = 0; i < n - 2; i++) {
    for (int j = i + 1; j < n - 1; j++) {
        if A[i] == A[j] {
            return false;
        }
    }
}
```

Number of Binary digits

in Bin out

5 \rightarrow 101 \rightarrow 3

6 \rightarrow 1000 \rightarrow 4

11 \rightarrow 1011 \rightarrow 4

$5 \% 2 = 1 \rightarrow 101$

$5 / 2 = 2$

$2 \% 2 = 0$

$2 / 2 = 1$

$1 \% 2 = 1$

count = 1;

while (n > 1) {

count++;

n /= 2;

}

return count;

16 \rightarrow 8 \rightarrow 4 \rightarrow 2 \rightarrow 1

$O(\log n)$