Classification Tree: Carseats dataset

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```
library(ISLR)
library(tree)
library(caret)
Load packages and dataset
## Loading required package: ggplot2
## Loading required package: lattice
data(package="ISLR")
dtree <- Carseats
class(dtree)
dtree$Sales
View(dtree)
Investigate the data
names(dtree)
                                                   "Advertising" "Population"
  [1] "Sales"
                       "CompPrice"
                                     "Income"
## [6] "Price"
                       "ShelveLoc"
                                     "Age"
                                                   "Education"
                                                                  "Urban"
## [11] "US"
head(dtree)
##
     Sales CompPrice Income Advertising Population Price ShelveLoc Age Education
```

```
## 1 9.50
                138
                         73
                                     11
                                               276
                                                     120
                                                               Bad 42
                                                                               17
## 2 11.22
                                     16
                 111
                         48
                                               260
                                                      83
                                                              Good 65
                                                                               10
## 3 10.06
                 113
                         35
                                     10
                                               269
                                                      80
                                                            Medium
                                                                    59
                                                                               12
## 4 7.40
                 117
                        100
                                      4
                                               466
                                                      97
                                                            Medium
                                                                    55
                                                                              14
                                      3
                                                                              13
## 5 4.15
                 141
                         64
                                               340
                                                     128
                                                               Bad 38
## 6 10.81
                                     13
                 124
                        113
                                               501
                                                      72
                                                               Bad 78
                                                                              16
   Urban US
##
## 1
      Yes Yes
## 2
     Yes Yes
## 3
      Yes Yes
## 4
      Yes Yes
## 5
      Yes No
## 6
       No Yes
```

Sales CompPrice Income Advertising Population Price ShelveLoc Age Education
395 5.35 130 58 19 366 139 Bad 33 16

tail(dtree)

```
## 396 12.57
                    138
                           108
                                        17
                                                   203
                                                         128
                                                                   Good
                                                                         33
                                                                                    14
## 397
       6.14
                    139
                            23
                                         3
                                                    37
                                                         120
                                                                 Medium 55
                                                                                    11
## 398
       7.41
                    162
                            26
                                        12
                                                   368
                                                         159
                                                                 Medium 40
                                                                                    18
## 399 5.94
                    100
                            79
                                         7
                                                   284
                                                                                    12
                                                          95
                                                                    Bad 50
## 400
       9.71
                    134
                            37
                                         0
                                                    27
                                                         120
                                                                   Good 49
                                                                                    16
##
       Urban US
## 395
         Yes Yes
## 396
         Yes Yes
## 397
          No Yes
## 398
         Yes Yes
## 399
         Yes Yes
## 400
         Yes Yes
summary(dtree)
        Sales
                        CompPrice
##
                                        Income
                                                       Advertising
    Min.
           : 0.000
                     Min.
                             : 77
                                    Min.
                                            : 21.00
                                                      Min.
                                                             : 0.000
##
    1st Qu.: 5.390
                      1st Qu.:115
                                    1st Qu.: 42.75
                                                      1st Qu.: 0.000
    Median : 7.490
                     Median:125
                                    Median : 69.00
                                                      Median : 5.000
##
    Mean
          : 7.496
                     Mean
                            :125
                                    Mean
                                           : 68.66
                                                      Mean
                                                             : 6.635
    3rd Qu.: 9.320
                      3rd Qu.:135
                                    3rd Qu.: 91.00
                                                      3rd Qu.:12.000
##
##
    Max.
          :16.270
                     Max.
                             :175
                                    Max.
                                           :120.00
                                                      Max.
                                                             :29.000
##
      Population
                         Price
                                      ShelveLoc
                                                        Age
                                                                      Education
##
   Min.
          : 10.0
                           : 24.0
                                     Bad
                                          : 96
                                                          :25.00
                                                                    Min.
                                                                          :10.0
                    Min.
                                                   Min.
   1st Qu.:139.0
                    1st Qu.:100.0
                                     Good : 85
                                                   1st Qu.:39.75
                                                                    1st Qu.:12.0
   Median :272.0
                    Median :117.0
                                     Medium:219
                                                   Median :54.50
                                                                    Median:14.0
##
##
   Mean
           :264.8
                    Mean
                            :115.8
                                                   Mean
                                                          :53.32
                                                                    Mean
                                                                          :13.9
##
    3rd Qu.:398.5
                    3rd Qu.:131.0
                                                   3rd Qu.:66.00
                                                                    3rd Qu.:16.0
## Max.
           :509.0
                    Max.
                            :191.0
                                                   Max.
                                                          :80.00
                                                                    Max.
                                                                           :18.0
##
    Urban
                US
    No :118
##
              No :142
##
   Yes:282 Yes:258
##
##
##
##
Preprocessing - discretization
High <- ifelse(dtree$Sales<=8, "NO", "YES")</pre>
class(High)
## [1] "character"
High <- as.factor(High)</pre>
class(High)
## [1] "factor"
dtree <- data.frame(dtree,High)</pre>
dtree <- subset(dtree, select=-Sales)</pre>
```

Training

```
dtree.carseats <- tree(High~., dtree)
summary(dtree.carseats)</pre>
```

```
##
## Classification tree:
## tree(formula = High ~ ., data = dtree)
## Variables actually used in tree construction:
## [1] "ShelveLoc"
                    "Price"
                                 "Income"
                                               "CompPrice"
                                                            "Population"
## [6] "Advertising" "Age"
                                  "US"
## Number of terminal nodes:
                            27
## Residual mean deviance: 0.4575 = 170.7 / 373
## Misclassification error rate: 0.09 = 36 / 400
plot(dtree.carseats)
text(dtree.carseats, pretty = 0)
                                    ShelveLoc: Bad, Medium
                     Price k 92.5
                                                               Price < 135
                                                              USIntome < 46
                                                          Price < 109 d
                                 Advertising < 13.5
                                                                IYE$IØES
                                                 CompPride < 124.5
                                                        YESIO
                NØES
                                      YE8IQNO
print(dtree.carseats)
## node), split, n, deviance, yval, (yprob)
##
        * denotes terminal node
##
##
    1) root 400 541.500 NO ( 0.59000 0.41000 )
##
      2) ShelveLoc: Bad, Medium 315 390.600 NO (0.68889 0.31111)
        4) Price < 92.5 46 56.530 YES ( 0.30435 0.69565 )
##
##
          8) Income < 57 10 12.220 NO ( 0.70000 0.30000 )
##
           16) CompPrice < 110.5 5
                                   0.000 NO ( 1.00000 0.00000 ) *
##
           17) CompPrice > 110.5 5
                                   6.730 YES ( 0.40000 0.60000 ) *
          9) Income > 57 36 35.470 YES ( 0.19444 0.80556 )
##
           18) Population < 207.5 16 21.170 YES ( 0.37500 0.62500 ) *
##
##
           19) Population > 207.5 20
                                      7.941 YES ( 0.05000 0.95000 ) *
##
        5) Price > 92.5 269 299.800 NO ( 0.75465 0.24535 )
         10) Advertising < 13.5 224 213.200 NO ( 0.81696 0.18304 )
##
##
           20) CompPrice < 124.5 96 44.890 NO ( 0.93750 0.06250 )
             40) Price < 106.5 38 33.150 NO ( 0.84211 0.15789 )
##
##
               80) Population < 177 12 16.300 NO ( 0.58333 0.41667 )
##
                160) Income < 60.5 6 0.000 NO (1.00000 0.00000) *
##
                161) Income > 60.5 6
                                      5.407 YES ( 0.16667 0.83333 ) *
               81) Population > 177 26 8.477 NO ( 0.96154 0.03846 ) *
##
##
```

```
##
            21) CompPrice > 124.5 128 150.200 NO ( 0.72656 0.27344 )
              42) Price < 122.5 51 70.680 YES ( 0.49020 0.50980 )
##
                84) ShelveLoc: Bad 11
##
                                        6.702 NO ( 0.90909 0.09091 ) *
##
                85) ShelveLoc: Medium 40 52.930 YES ( 0.37500 0.62500 )
##
                 170) Price < 109.5 16
                                        7.481 YES ( 0.06250 0.93750 ) *
##
                 171) Price > 109.5 24 32.600 NO ( 0.58333 0.41667 )
##
                   342) Age < 49.5 13 16.050 YES ( 0.30769 0.69231 ) *
##
                   343) Age > 49.5 11
                                        6.702 NO ( 0.90909 0.09091 ) *
##
              43) Price > 122.5 77 55.540 NO ( 0.88312 0.11688 )
##
                86) CompPrice < 147.5 58 17.400 NO ( 0.96552 0.03448 ) *
##
                87) CompPrice > 147.5 19 25.010 NO ( 0.63158 0.36842 )
                 174) Price < 147 12 16.300 YES ( 0.41667 0.58333 )
##
##
                   348) CompPrice < 152.5 7
                                              5.742 YES ( 0.14286 0.85714 ) *
                   349) CompPrice > 152.5 5
##
                                              5.004 NO ( 0.80000 0.20000 ) *
##
                 175) Price > 147 7
                                    0.000 NO ( 1.00000 0.00000 ) *
##
          11) Advertising > 13.5 45 61.830 YES ( 0.44444 0.55556 )
            22) Age < 54.5 25 25.020 YES ( 0.20000 0.80000 )
##
##
              44) CompPrice < 130.5 14 18.250 YES ( 0.35714 0.64286 )
                88) Income < 100 9 12.370 NO ( 0.55556 0.44444 ) *
##
##
                89) Income > 100 5
                                    0.000 YES ( 0.00000 1.00000 ) *
##
              45) CompPrice > 130.5 11
                                        0.000 YES ( 0.00000 1.00000 ) *
            23) Age > 54.5 20 22.490 NO ( 0.75000 0.25000 )
##
              46) CompPrice < 122.5 10
##
                                        0.000 NO ( 1.00000 0.00000 ) *
              47) CompPrice > 122.5 10  13.860 NO ( 0.50000 0.50000 )
##
                                    0.000 YES ( 0.00000 1.00000 ) *
##
                94) Price < 125 5
##
                95) Price > 125 5
                                    0.000 NO ( 1.00000 0.00000 ) *
##
       3) ShelveLoc: Good 85 90.330 YES ( 0.22353 0.77647 )
##
         6) Price < 135 68 49.260 YES ( 0.11765 0.88235 )
##
         12) US: No 17 22.070 YES ( 0.35294 0.64706 )
##
            24) Price < 109 8 0.000 YES (0.00000 1.00000) *
##
            25) Price > 109 9 11.460 NO ( 0.66667 0.33333 ) *
##
         13) US: Yes 51 16.880 YES ( 0.03922 0.96078 ) *
##
         7) Price > 135 17 22.070 NO ( 0.64706 0.35294 )
##
                             0.000 NO ( 1.00000 0.00000 ) *
          14) Income < 46 6
##
          15) Income > 46 11 15.160 YES ( 0.45455 0.54545 ) *
```

Splitting the data

Splitting the original data set to create training and testing data sets

```
set.seed(123)
train.index <- sample(1:nrow(dtree), 200)
nrow(dtree)
## [1] 400</pre>
```

Splitting

```
train.set <- dtree[train.index,]
class(train.set)</pre>
```

```
## [1] "data.frame"
```

Training

```
dtree.tree <- tree(High~., train.set)
plot(dtree.tree)
text(dtree.tree, pretty = 0)</pre>
```

```
ShelveLoc: Bad, Medium
                 Price ₹ 101.5
                                                  Price < 111
                                                      US: No
                                                  YESducation < 14.5
                             Advertising < 13.5
  ShelveLoc: Bad
                                                      NO TOYES
Incom@engoPride < 118.5
                                         Income < 100
                   ShelveLoc: Bad
      |Price| < 84|
                         CompPrice < 123
             YES
                 NO
                        Age 44965pulation < 1249€S
                    Price < P3ic. € < 107.5
                Education < 14.5 YESNO
                    YESNONONO
```

```
summary(dtree.tree)
```

```
##
## Classification tree:
## tree(formula = High ~ ., data = train.set)
## Variables actually used in tree construction:
## [1] "ShelveLoc" "Price" "Income" "CompPrice" "Advertising"
## [6] "Age" "Education" "Population" "US"
## Number of terminal nodes: 20
## Residual mean deviance: 0.5056 = 91.02 / 180
## Misclassification error rate: 0.115 = 23 / 200
```

Testing

```
test.set <- dtree[-train.index,]
High.test <- High[-train.index]

tree.pred <- predict(dtree.tree, test.set, type="class")</pre>
```

Accuracy

```
table(tree.pred, High.test)

## High.test

## tree.pred NO YES

## NO 87 13

## YES 35 65

accuracy = (87+65)/200
accuracy
```

```
## [1] 0.76
```

Testing continued

Predict the class of the test set using the trained decision tree

```
tree.pred <- predict(dtree.tree, test.set, type="class")
#If type = "class": for a classification tree, a factor of the predicted
#classes (that with highest posterior probability, with ties split randomly).</pre>
```

Confusion matrix

Compare the predicted classes with the actual classes to evaluate the performance of the decision tree table(tree.pred, High.test)

```
## High.test
## tree.pred NO YES
## NO 87 13
## YES 35 65
#calculate the accuracy of the decision tree on the test set
accuracy = (87+65)/200
accuracy
## [1] 0.76
```

```
#calculating the misclassification rate (1-accuracy)
misclassification_rate <- 1-accuracy
misclassification_rate</pre>
```

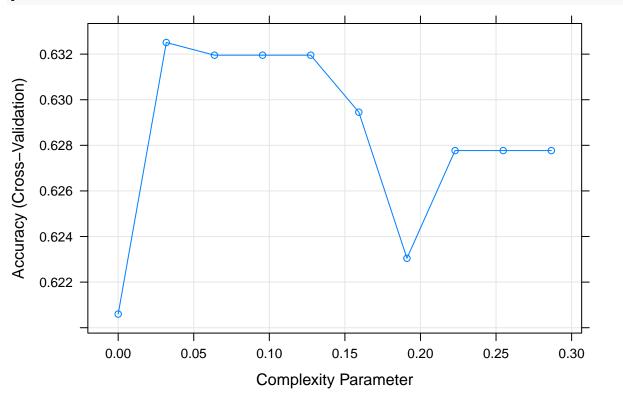
[1] 0.24

K-fold cross-validation

```
set.seed(123)
folds <- createFolds(dtree$High, k=10, list=TRUE, returnTrain=FALSE)</pre>
ctrl <- trainControl(method="cv", index=folds, savePredictions="final", classProbs=TRUE)
set.seed(123)
dtree.tree.cv <- train(High~., data=dtree, method="rpart", trControl=ctrl, tuneLength=10)
dtree.tree.cv
## CART
##
## 400 samples
## 10 predictor
##
    2 classes: 'NO', 'YES'
##
## No pre-processing
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 40, 40, 40, 39, 40, 41, ...
## Resampling results across tuning parameters:
##
##
                 Accuracy
                            Kappa
     ср
    0.00000000 0.6205982 0.2172401
##
    0.03184282 0.6325095 0.2316952
##
    0.06368564 0.6319540 0.2143365
```

```
0.09552846 0.6319540 0.2143365
##
    ##
##
    0.15921409 0.6294540 0.2041994
##
    0.19105691 0.6230473
                      0.1845560
##
    0.22289973
              0.6277695
                       0.1835560
##
    0.25474255   0.6277695   0.1835560
##
    ##
## Accuracy was used to select the optimal model using the largest value.
## The final value used for the model was cp = 0.03184282.
```

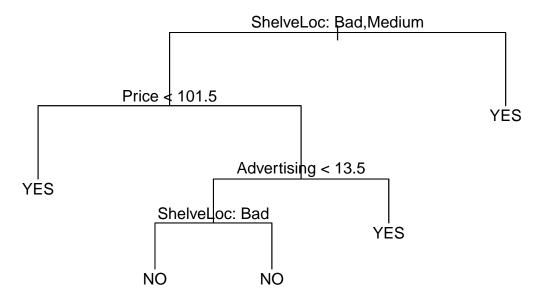
plot(dtree.tree.cv)



Fine-tuning the decision tree

Pruning the decision tree to avoid overfitting

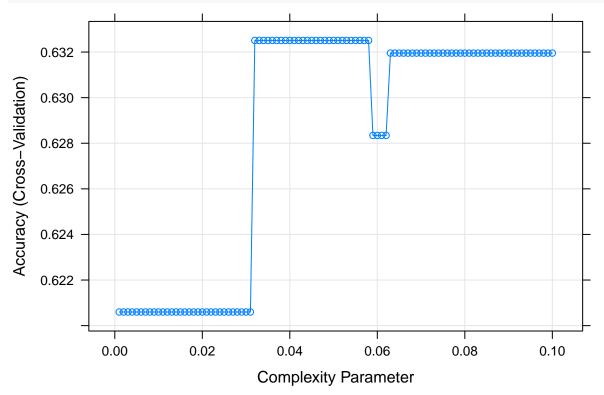
```
dtree.tree.prune <- prune.tree(dtree.tree, best=4)
plot(dtree.tree.prune)
text(dtree.tree.prune, pretty = 0)</pre>
```



Cross-validation

Using cross-validation to determine the optimal complexity parameter for pruning

dtree.tree.cv.prune <- train(High~., data=dtree, method="rpart", trControl=ctrl, tuneLength=10, tuneGri
plot(dtree.tree.cv.prune)</pre>



Predicting class of test set

Using the pruned decision tree to predict the class of the test set

tree.pred.prune <- predict(dtree.tree.prune, test.set, type="class")
table(tree.pred.prune, High.test)</pre>

```
## High.test
## tree.pred.prune NO YES
## NO 77 12
## YES 45 66
```

Accuracy and misclassification rate

```
accuracy.prune <- sum(tree.pred.prune == High.test)/length(High.test)
misclassification_rate.prune <- 1-accuracy.prune
accuracy.prune
## [1] 0.715
misclassification_rate.prune</pre>
```

[1] 0.285