

Notebook - Maratona de Programação

Lenhadoras de Segtree

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1 Math 38 // How to use: $_{39}$ // vector<vector<ll>> v = {{1, 1}, {1, 0}}; 40 // Matriz transition = Matriz(v); 1.1 Ceil 41 // cout << fexp(transition, n)[0][1] << '\n'; 1 long long division_ceil(long long a, long long b) { 43 using 11 = long long; return 1 + ((a - 1) / b); // if a != 0 45 const int MOD = 1e9+7; 3 } 46 1.2 To Decimal 47 struct Matriz{ vector < vector < 11 >> mat; 48 int rows, columns; 1 long long to_decimal(const string& rep, long long 50 base) { vector<ll> operator[](int i){ 51 long long n = 0; 52 return mat[i]; 53 for (auto c : rep) { // if the number can't be represented in this Matriz(vector < vector < 11 >> & matriz) { 55 base mat = matriz; if (c > digits[base - 1]) return -1; rows = mat.size(); 57 n *= base;columns = mat[0].size(); 58 n += digits.find(c); 59 60 10 Matriz(int row, int column, bool identity=false){ 61 return n; rows = row; columns = column; 62 12 } 63 mat.assign(rows, vector<11>(columns, 0)); 64 if(identity) { 1.3 Matrix Exponentiation for(int i = 0; i < min(rows, columns); i</pre> 65 ++) { mat[i][i] = 1; 1 // Description: 66 } 67 $_{2}$ // Calculate the nth term of a linear recursion } 68 69 4 // Example Fibonacci: $_{5}$ // Given a linear recurrence, for example fibonacci Matriz operator * (Matriz a) { 6 // F(n) = n, x <= 171 assert(columns == a.rows); 7 // F(n) = F(n - 1) + F(n - 2), x > 1vector < vector < 11 >> resp(rows, vector < 11 > (a. 73 $_{\rm 9}$ // The recurrence has two terms, so we can build a columns, 0)); matrix 2 x 1 so that for(int i = 0; i < rows; i++){</pre> $_{10}$ // n + 1 = transition * n 75 76 for (int j = 0; j < a.columns; j++) { for(int k = 0; k < a.rows; k++){ $_{12}$ // (2 x 1) = (2 x 2) * (2 x 1) 77 resp[i][j] = (resp[i][j] + (mat[i $_{13}$ // F(n) = a b * F(n - 1) 78 $_{14}$ // F(n - 1) c d F(n - 2)][k] * 1LL * a[k][j]) % MOD) % MOD; 79 } 16 // Another Example: } $_{\rm 17}$ // Given a grid 3 x n, you want to color it using 3 81 return Matriz(resp); distinct colors so that $_{\rm 18}$ // no adjacent place has the same color. In how many $^{\rm 83}$ different ways can you do that? Matriz operator + (Matriz a) { 19 // There are 6 ways for the first column to be assert(rows == a.rows && columns == a.columns colored using 3 distinct colors 86 $_{20}$ // ans 6 ways using 2 equal colors and 1 distinct one vector < vector < ll >> resp(rows, vector < ll > (87 columns,0)); $_{22}$ // Adding another column, there are: for(int i = 0; i < rows; i++){</pre> 23 // 3 ways to go from 2 equal to 2 equal for(int j = 0; j < columns; j++){</pre> 89 24 // 2 ways to go from 2 equal to 3 distinct resp[i][j] = (resp[i][j] + mat[i][j] $_{25}$ // 2 ways to go from 3 distinct to 2 equal $_{26}$ // 2 ways to go from 3 distinct to 3 distinct + a[i][j]) % MOD; 91 $_{28}$ // So we star with matrix 6 6 and multiply it by the 92 return Matriz(resp); 93 transition 3 2 and get $18\ 12$ 6 6 2 2 95 }: 12 12 $_{ m 30}$ // the we can exponentiate this matrix to find the 97 Matriz fexp(Matriz base, 11 exponent){ nth column Matriz result = Matriz(base.rows, base.rows, 1); 98 while(exponent > 0){ 32 // Problem: 99 if(exponent & 1LL) result = result * base; 33 // https://cses.fi/problemset/task/1722/ 100

9

35 // Complexity:

36 // O(log n)

101

102

103 104 base = base * base;

return result;

exponent = exponent >> 1;

```
105
                                                           6 // }
                                                           7 // else if (a == 0) {
   1.4 Crt
                                                                if (c % b == 0 && y1 <= c / b && y2 >= c / b)
                                                           8 //
                                                                 ans = (x2 - x1 + 1);
                                                                   else ans = 0;
 1 ll crt(const vector < pair < ll, ll >> & vet) {
                                                          10 // }
       11 \text{ ans} = 0, 1cm = 1;
                                                          11 // else if (b == 0) {
       ll a, b, g, x, y;
                                                          12 //
                                                                if (c % a == 0 && x1 <= c / a && x2 >= c / a)
       for(const auto &p : vet) {
                                                               ans = (y2 - y1 + 1);
           tie(a, b) = p;
                                                          13 //
                                                                   else ans = 0;
           tie(g, x, y) = gcd(lcm, b);
                                                          14 // }
           if((a - ans) % g != 0) return -1; // no
       solution
                                                          16 // Careful when a or b are negative or zero
         ans = ans + x * ((a - ans) / g) % (b / g) *
                                                          _{18} // if (ans == -1) ans = find_all_solutions(a, b, c,
           lcm = lcm * (b / g);
 a
                                                                x1, x2, y1, y2);
           ans = (ans \% lcm + lcm) \% lcm;
10
                                                          19 // cout << ans << '\n';
11
       return ans:
12
                                                          21 // Problems:
13 }
                                                          22 // https://www.spoj.com/problems/CEQU/
                                                          23 // http://codeforces.com/problemsets/acmsguru/problem
         Binary To Decimal
                                                                /99999/106
                                                          _{25} // consider trivial case a or b is 0
 int binary_to_decimal(long long n) {
                                                          26 int gcd(int a, int b, int& x, int& y) {
    int dec = 0, i = 0, rem;
                                                          27
                                                                 if (b == 0) {
                                                                     x = 1;
     while (n!=0) {
                                                          28
                                                                     y = 0;
      rem = n \% 10;
                                                          29
       n /= 10;
                                                                     return a;
                                                          30
                                                                 }
      dec += rem * pow(2, i);
                                                          31
       ++i;
                                                          32
                                                                 int x1, y1;
                                                                int d = gcd(b, a % b, x1, y1);
                                                          33
                                                                 x = y1;
                                                          34
10
    return dec:
                                                          35
                                                                 y = x1 - y1 * (a / b);
                                                                 return d:
                                                          36
12 }
                                                          37 }
13
14 long long decimal_to_binary(int n) {
                                                          38
   long long bin = 0;
                                                          39 // x and y are one solution and g is the gcd, all
15
    int rem, i = 1;
                                                                passed as reference
                                                          _{40} // minx <= x <= maxx miny <= y <= maxy
17
    while (n!=0) {
                                                          41 bool find_any_solution(int a, int b, int c, int &x0,
18
      rem = n \% 2;
                                                                int &y0, int &g) {
19
      n /= 2;
                                                                 g = gcd(abs(a), abs(b), x0, y0);
20
      bin += rem * i;
                                                          43
                                                                 if (c % g) {
       i *= 10;
                                                                    return false;
                                                          44
22
                                                          45
                                                                 }
23
24
                                                          46
     return bin;
                                                          47
                                                                x0 *= c / g;
25
                                                                 y0 *= c / g;
26 }
                                                          48
                                                          49
                                                                 if (a < 0) x0 = -x0;
   1.6 Fast Exponentiation
                                                          50
                                                                 if (b < 0) y0 = -y0;
                                                                 return true;
                                                          51
                                                          52 }
 1 11 fexp(11 b, 11 e, 11 mod) {
                                                          53
      ll res = 1;
                                                          54 void shift_solution(int & x, int & y, int a, int b,
       b \% = mod;
 3
                                                                int cnt) {
       while(e){
                                                                x += cnt * b;
                                                          55
          if(e & 1LL)
                                                                 y -= cnt * a;
                                                          56
              res = (res * b) % mod;
                                                          57 }
           e = e >> 1LL;
           b = (b * b) \% mod;
                                                          59 // return number of solutions in the interval
       }
 9
                                                          60 int find_all_solutions(int a, int b, int c, int minx,
       return res;
10
                                                                 int maxx, int miny, int maxy) {
11 }
                                                                 int x, y, g;
                                                          61
                                                          62
                                                                 if (!find_any_solution(a, b, c, x, y, g))
   1.7 Linear Diophantine Equation
                                                                    return 0:
                                                          63
                                                                 a /= g;
 _1 // int a, b, c, x1, x2, y1, y2; cin >> a >> b >> c >> ^{65}
                                                                 b /= g;
                                                          66
        x1 >> x2 >> y1 >> y2;
                                                                 int sign_a = a > 0 ? +1 : -1;
 _2 // int ans = -1;
                                                          67
                                                                int sign_b = b > 0 ? +1 : -1;
 _3 // if (a == 0 && b == 0) {
                                                          68
 4 //
         if (c != 0) ans = 0;
          else ans = (x2 - x1 + 1) * (y2 - y1 + 1);
                                                          70
                                                                 shift_solution(x, y, a, b, (minx - x) / b);
```

```
if (x < minx)
                                                                 for (int i = 2; i < MAX; i++) {
71
                                                           6
72
           shift_solution(x, y, a, b, sign_b);
                                                           7
                                                                     if (is_prime[i]) {
       if (x > maxx)
73
                                                                         primes.push_back(i);
74
          return 0;
       int lx1 = x;
                                                                          for (int j = i + i; j < MAX; j += i)
                                                                              is_prime[j] = false;
76
                                                          11
       shift_solution(x, y, a, b, (maxx - x) / b);
                                                                     }
                                                          12
       if (x > maxx)
78
                                                          13
          shift_solution(x, y, a, b, -sign_b);
                                                          14 }
79
       int rx1 = x;
80
                                                                    Horner Algorithm
                                                             1.10
81
       shift_solution(x, y, a, b, -(miny - y) / a);
       if (y < miny)</pre>
83
                                                           1 // Description:
           shift_solution(x, y, a, b, -sign_a);
                                                           _2 // Evaluates y = f(x)
84
85
       if (y > maxy)
          return 0;
86
                                                           4 // Problem:
87
       int 1x2 = x;
                                                           5 // https://onlinejudge.org/index.php?option=
88
                                                                 com_onlinejudge&Itemid=8&page=show_problem&
       shift_solution(x, y, a, b, -(maxy - y) / a);
                                                                 problem=439
90
       if (y > maxy)
           shift_solution(x, y, a, b, sign_a);
                                                           7 // Complexity:
91
       int rx2 = x;
92
                                                           8 // O(n)
93
       if (1x2 > rx2)
                                                          10 using polynomial = std::vector<int>;
          swap(1x2, rx2);
95
                                                          11
       int 1x = max(1x1, 1x2);
96
                                                          12 polynomial p \{6, -5, 2\}; // p(x) = x^2 - 5x + 6;
       int rx = min(rx1, rx2);
97
                                                          13
98
                                                          14 int degree(const polynomial& p) {
       if (lx > rx)
99
                                                              return p.size() - 1;
                                                          15
          return 0:
100
                                                          16 }
       return (rx - lx) / abs(b) + 1;
101
                                                          17
102 }
                                                          18 int evaluate(const polynomial& p, int x) {
                                                              int y = 0, N = degree(p);
       Function Root
                                                               for (int i = N; i >= 0; --i) {
                                                              y *= x;
                                                          22
 const ld EPS1 = 1e-9; // iteration precision error
                                                                 y += p[i];
                                                          23
 2 const ld EPS2 = 1e-4; // output precision error
                                                          24
 4 ld f(ld x) {
                                                               return y;
    // \exp(-x) == e^{-x}
     return p * exp(-x) + q * sin(x) + r * cos(x) + s * 27 }
       tan(x) + t * x * x + u;
                                                             1.11 Multiplicative Inverse
                                                           1 ll extend_euclid(ll a, ll b, ll &x, ll &y) {
 9 ld root(ld a, ld b) {
                                                           2
                                                                 if (a == 0)
    while (b - a >= EPS1) {
                                                                 {
      1d c = (a + b) / 2.0;
                                                           3
11
                                                                     x = 0; y = 1;
                                                           4
       1d y = f(c);
                                                           5
                                                                     return b:
13
                                                           6
       if (y < 0) b = c;
14
                                                                 11 x1, y1;
                                                           7
      else a = c;
15
                                                                 11 d = extend_euclid(b%a, a, x1, y1);
                                                           8
16
                                                                 x = y1 - (b / a) * x1;
                                                           9
17
                                                                 y = x1;
                                                          10
     return (a + b) / 2;
18
                                                          11
                                                                 return d;
19 }
                                                          12 }
20
                                                          13
21 int main() {
                                                          14 // gcd(a, m) = 1 para existir solucao
   ld ans = root(0, 1);
                                                          _{15} // ax + my = 1, ou a*x = 1 (mod m)
    if (abs(f(ans)) <= EPS2) cout << fixed <<</pre>
                                                          16 ll inv_gcd(ll a, ll m) { // com gcd
      setprecision(4) << ans << '\n';</pre>
     else cout << "No solution\n";</pre>
                                                          17 11 x, y;
                                                               extend_euclid(a, m, x, y);
                                                          18
25
                                                               return (((x \% m) + m) \%m);
                                                          19
     return 0;
26
                                                          20 }
                                                          22 ll inv(ll a, ll phim) { // com phi(m), se m for primo
         Sieve Of Eratosthenes
                                                                  entao phi(m) = p-1
                                                              11 e = phim - 1;
 1 vector < bool > is_prime(MAX, true);
                                                               return fexp(a, e, MOD);
                                                          24
 vector < int > primes;
```

25 }

4 void sieve() {

is_prime[0] = is_prime[1] = false;

Representation Arbitrary Base

```
1 const string digits { "0123456789
                                                                     n /= p;
      ABCDEFGHIJKLMNOPQRSTUVWXYZ" };
                                                           8
                                                                     expoente++;
                                                           9
3 string representation(int n, int b) {
                                                                   ans.emplace_back(p, expoente);
                                                          10
   string rep;
                                                          11
                                                               }
                                                          12
                                                               if(n > 1) ans.emplace_back(n, 1);
                                                          13
     rep.push_back(digits[n % b]);
                                                          14
                                                               return ans:
      n /= b;
    } while (n);
10
                                                                  DP
    reverse(rep.begin(), rep.end());
                                                                  Knapsack With Index
    return rep;
13
14 }
                                                           void knapsack(int W, int wt[], int val[], int n) {
         Set Operations
                                                                 int i, w;
                                                                 int K[n + 1][W + 1];
1 // Complexity;
_{2} // O(n * m) being n and m the sizes of the two sets
                                                                 for (i = 0; i \le n; i++) {
_3 // 2*(count1+count2)-1 (where countX is the distance _6
                                                                     for (w = 0; w \le W; w++) {
                                                                          if (i == 0 || w == 0)
      between firstX and lastX):
                                                                             K[i][w] = 0;
5 vector<int> res;
                                                                          else if (wt[i - 1] <= w)
_{6} set_union(s1.begin(), s1.end(), s2.begin(), s2.end(), _{10}
                                                                             K[i][w] = max(val[i - 1] +
       inserter(res, res.begin()));
                                                                                  K[i - 1][w - wt[i - 1]], K[i -
7 set_intersection(s1.begin(), s1.end(), s2.begin(), s2
                                                                 1][w]);
      .end(), inserter(res, res.begin()));
                                                                          else
_{8} // present in the first set, but not in the second
                                                                              K[i][w] = K[i - 1][w];
9 set_difference(s1.begin(), s1.end(), s2.begin(), s2. 14
                                                                     }
      end(), inserter(res, res.begin()));
                                                          15
_{\rm 10} // present in one of the sets, but not in the other
set_symmetric_difference(s1.begin(), s1.end(), s2.
                                                                 int res = K[n][W];
                                                          17
      begin(), s2.end(), inserter(res, res.begin()));
                                                                 cout << res << endl;</pre>
                                                          19
  1.14 Divisors
                                                                 for (i = n; i > 0 && res > 0; i--) {
                                                          21
                                                                     if (res == K[i - 1][w])
                                                          22
1 vector < long long > all_divisors(long long n) {
                                                          23
                                                                         continue;
    vector <long long > ans;
                                                                     else {
                                                          24
    for(long long a = 1; a*a <= n; a++){
                                                                         cout << " " << wt[i - 1] ;</pre>
      if(n \% a == 0) {
                                                                         res = res - val[i - 1];
                                                          26
        long long b = n / a;
                                                                          w = w - wt[i - 1];
        ans.push_back(a);
                                                                     }
                                                          28
        if(a != b) ans.push_back(b);
                                                          29
                                                          30 }
    }
9
                                                          31
    sort(ans.begin(), ans.end());
10
                                                          32 int main()
    return ans;
                                                          33 {
12 }
                                                                 int val[] = { 60, 100, 120 };
                                                          34
                                                          35
                                                                 int wt[] = { 10, 20, 30 };
  1.15 Check If Bit Is On
                                                                 int W = 50;
                                                          36
                                                                 int n = sizeof(val) / sizeof(val[0]);
1 // msb de 0 é undefined
                                                          38
2 #define msb(n) (32 - __builtin_clz(n))
3 // #define msb(n) (64 - __builtin_clz11(n) )
                                                          39
                                                                 knapsack(W, wt, val, n);
                                                          40
4 // popcount
                                                                 return 0;
                                                          41
5 // turn bit off
                                                          42 }
                                                                   Substr Palindrome
7 bool bit_on(int n, int bit) {
      if(1 & (n >> bit)) return true;
      else return false;
                                                           1 // êvoc deve informar se a substring de S formada
10 }
                                                                 pelos elementos entre os indices i e j
                                                           _{2} // \acute{e} um palindromo ou \~{a}no.
  1.16 Prime Factors
                                                           4 char s[MAX];
1 vector < pair < long long, int >> fatora(long long n) {
                                                           5 int calculado[MAX][MAX]; // inciado com false, ou 0
    vector < pair < long long, int >> ans;
                                                           6 int tabela[MAX][MAX];
    for(long long p = 2; p*p <= n; p++) {
      if(n \% p == 0) {
                                                           8 int is_palin(int i, int j){
```

10

int expoente = 0;

while (n % p == 0) {

5

9 if(calculado[i][j]){

return tabela[i][j];

```
dp[i][j] = dp[i-1][j];
1.1
                                                           11
12
    if(i == j) return true;
                                                           12
                                                                    }
    if(i + 1 == j) return s[i] == s[j];
                                                                 }
13
                                                           13
                                                                 return dp[n][m];
14
                                                          14
    int ans = false;
                                                          15 }
    if(s[i] == s[j]){
16
                                                                  Digits
      if(is_palin(i+1, j-1)){
17
        ans = true;
18
19
                                                           _{\rm 1} // achar a quantidade de numeros menores que R que
20
                                                                 possuem no maximo 3 digitos nao nulos
    calculado[i][j] = true;
21
                                                           2 // a ideia eh utilizar da ordem lexicografica para
22
    tabela[i][j] = ans;
                                                                 checar isso pois se temos por exemplo
23
    return ans;
                                                           _{\rm 3} // o numero 8500, a gente sabe que se pegarmos o
                                                                 numero 7... qualquer digito depois do 7
                                                           _4 // sera necessariamente menor q 8500
       Edit Distance
  2.3
                                                           6 string r;
                                                           7 int tab[20][2][5];
1 // Description:
2 // Minimum number of operations required to transform
                                                           _{9} // i - digito de R
       a string into another
                                                           _{10} // menor - ja pegou um numero menor que um digito de
3 // Operations allowed: add character, remove
      character, replace character
                                                           _{11} // qt - quantidade de digitos nao nulos
                                                           12 int dp(int i, bool menor, int qt){
5 // Parameters:
                                                                 if(qt > 3) return 0;
_{6} // str1 - string to be transformed into str2
                                                                 if(i >= r.size()) return 1;
7 // str2 - string that str1 will be transformed into
                                                          14
                                                                 if(tab[i][menor][qt] != -1) return tab[i][menor][
8 // m - size of str1
                                                           15
9 // n - size of str2
                                                           16
11 // Problem:
                                                                 int dr = r[i] - '0';
                                                           17
                                                                 int res = 0;
12 // https://cses.fi/problemset/task/1639
                                                          18
                                                                 for(int d = 0; d <= 9; d++) {
14 // Complexity:
                                                          20
                                                                     int dnn = qt + (d > 0);
                                                           21
15 // 0(m \times n)
                                                                      if(menor == true) {
                                                           22
                                                                          res += dp(i+1, true, dnn);
17 // How to use:
                                                           23
                                                                      }
18 // memset(dp, -1, sizeof(dp));
                                                           25
                                                                      else if(d < dr) {
19 // string a, b;
                                                                          res += dp(i+1, true, dnn);
_{20} // edit_distance(a, b, (int)a.size(), (int)b.size()); ^{26}
                                                                      else if(d == dr) {
22 // Notes:
                                                           28
_{\rm 23} // Size of dp matriz is m x n
                                                                          res += dp(i+1, false, dnn);
                                                           30
25 int dp[MAX][MAX];
                                                           32
                                                                 return tab[i][menor][qt] = res;
27 int edit_distance(string &str1, string &str2, int m, 33
      int n) {
      if (m == 0) return n;
                                                             2.6 Coins
      if (n == 0) return m;
29
30
      if (dp[m][n] != -1) return dp[m][n];
31
                                                           1 int tb[1005];
32
      if (str1[m - 1] == str2[n - 1]) return dp[m][n] = 3 vector <int> moedas;
33
       edit_distance(str1, str2, m - 1, n - 1);
      return dp[m][n] = 1 + min({edit_distance(str1,
34
                                                           5 int dp(int i){
      str2, m, \hat{n} - 1), edit_distance(str1, str2, m - 1, \hat{i} if(\hat{i} >= n)
       n), edit_distance(str1, str2, m - 1, n - 1)}); 7
35 }
                                                               if(tb[i] != -1)
                                                                 return tb[i];
  2.4 Knapsack
                                                               tb[i] = max(dp(i+1), dp(i+2) + moedas[i]);
                                                           11
                                                           12
                                                               return tb[i];
int val[MAXN], peso[MAXN], dp[MAXN][MAXS];
                                                           13
                                                          14
3 int knapsack(int n, int m){ // n Objetos | Peso max
                                                           15 int main(){
      for(int i=0;i<=n;i++){
                                                              memset(tb,-1,sizeof(tb));
         for(int j=0; j \le m; j++){
                                                           16
               if(i==0 \text{ or } j==0)
                   dp[i][j] = 0;
                                                                   Minimum Coin Change
                                                             2.7
               else if(peso[i-1]<=j)</pre>
                  dp[i][j] = max(val[i-1]+dp[i-1][j-1]
      peso[i-1]], dp[i-1][j]);
                                                           1 int n;
              else
                                                           vector <int > valores;
```

```
4 int tabela[1005];
6 int dp(int k){
   if(k == 0) {
     return 0:
   if(tabela[k] != -1)
10
     return tabela[k];
11
   int melhor = 1e9;
    for(int i = 0; i < n; i++){
13
     if(valores[i] <= k)</pre>
15
        melhor = min(melhor,1 + dp(k - valores[i]));
16
   return tabela[k] = melhor;
```

2.8 Kadane

```
_{1} // achar uma subsequencia continua no array que a
      soma seja a maior possivel
2 // nesse caso vc precisa multiplicar exatamente 1
      elemento da subsequencia
3 // e achar a maior soma com isso
5 int n, x, arr[MAX], tab[MAX][2]; // tab[maior
      resposta no intervalo][foi multiplicado ou ano]
7 int dp(int i, bool mult) {
      if (i == n-1) {
          if (!mult) return arr[n-1]*x;
9
          return arr[n-1];
10
11
      if (tab[i][mult] != -1) return tab[i][mult];
12
      int res;
14
15
      if (mult) {
16
          res = max(arr[i], arr[i] + dp(i+1, 1));
19
      else {
          res = max({
              arr[i]*x,
21
              arr[i]*x + dp(i+1, 1),
22
              arr[i] + dp(i+1, 0)
          });
24
25
26
27
      return tab[i][mult] = res;
28 }
29
30 int main() {
31
      memset(tab, -1, sizeof(tab));
33
      int ans = -00;
34
      for (int i = 0; i < n; i++) {
35
          ans = max(ans, dp(i, 0));
36
38
      return 0;
39
40 }
41
44 int ans = a[0], ans_1 = 0, ans_r = 0;
45 int sum = 0, minus_pos = -1;
47 for (int r = 0; r < n; ++r) {
   sum += a[r];
48
      if (sum > ans) {
          ans = sum;
50
          ans_l = minus_pos + 1;
51
```

3 Template

3.1 Template

```
1 #include <bits/stdc++.h>
2 using namespace std;
 4 #define int long long
 5 #define optimize std::ios::sync_with_stdio(false);
       cin.tie(NULL);
6 #define vi vector<int>
7 #define ll long long
8 #define pb push_back
9 #define mp make_pair
10 #define ff first
11 #define ss second
12 #define pii pair <int, int>
13 #define MOD 100000007
_{14} #define sqr(x) ((x) * (x))
#define all(x) (x).begin(), (x).end()
16 #define FOR(i, j, n) for (int i = j; i < n; i++)
17 #define qle(i, n) (i == n ? "\n" : "
18 #define endl "\n"
19 const int 00 = 1e9;
20 const int MAX = 1e6;
22 int32_t main(){ optimize;
23
       return 0;
25 }
```

3.2 Template Clean

```
1 // Notes:
2 // Compile and execute
3 // g++ teste.cpp -o teste -std=c++17
4 // ./teste < teste.txt
6 // Print with precision
7 // cout << fixed << setprecision(12) << value << endl
9 // File as input and output
10 // freopen("input.txt", "r", stdin);
11 // freopen("output.txt", "w", stdout);
13 #include <bits/stdc++.h>
14 using namespace std;
15
16 int main() {
    ios::sync_with_stdio(false);
17
      cin.tie(NULL);
18
20
21
22
      return 0:
23 }
```

4 Strings

4.1 Kmp

```
vector <int > prefix_function(string s) {
                                                                     LCS_{table[i][j]} = LCS_{table[i - 1][j - 1]} +
                                                          18
      int n = (int)s.length();
                                                                 1;
      vector < int > pi(n);
                                                          19
                                                                   else
      for (int i = 1; i < n; i++) {
                                                                     LCS_table[i][j] = max(LCS_table[i - 1][j],
                                                          20
          int j = pi[i-1];
                                                                 LCS_table[i][j - 1]);
          while (j > 0 && s[i] != s[j])
                                                          21
              j = pi[j-1];
                                                          22
           if (s[i] == s[j])
                                                          23
               j++;
                                                               int index = LCS_table[m][n];
                                                          24
          pi[i] = j;
                                                               char lcsAlgo[index + 1];
10
                                                          25
      }
                                                               lcsAlgo[index] = '\0';
11
                                                          26
12
      return pi;
                                                          27
13 }
                                                               int i = m, j = n;
                                                          28
                                                               while (i > 0 \&\& j > 0) {
                                                          29
  4.2 Generate All Permutations
                                                                 if (s1[i - 1] == s2[j - 1]) {
                                                          30
                                                                   lcsAlgo[index - 1] = s1[i - 1];
                                                          31
vector < string > generate_permutations(string s) {
                                                                   j--;
                                                          33
      int n = s.size():
                                                                   index --;
      vector<string> ans;
3
                                                          35
                                                          36
      sort(s.begin(), s.end());
                                                                 else if (LCS_table[i - 1][j] > LCS_table[i][j -
                                                          37
                                                                 11)
                                                                   i - -;
          ans.push_back(s);
                                                                 else
                                                          39
      } while (next_permutation(s.begin(), s.end()));
                                                          40
10
                                                          41
      return ans;
11
                                                          42
12 }
                                                               return lcsAlgo;
                                                          43
                                                          44 }
  4.3 Generate All Sequences Length K
                                                                   Trie
1 // gera todas as ípossveis êsequncias usando as letras
       em set (de comprimento n) e que tenham tamanho k
                                                           1 const int K = 26;
2 // sequence = ""
3 vector < string > generate_sequences(char set[], string
                                                           3 struct Vertex {
      sequence, int n, int k) {
                                                                 int next[K];
     if (k == 0){
                                                                 bool output = false;
         return { sequence };
                                                                 int p = -1;
6
                                                                 char pch;
                                                                 int link = -1;
     vector<string> ans;
                                                                 int go[K];
9
     for (int i = 0; i < n; i++) {
       auto aux = generate_sequences(set, sequence + 11
set[i], n, k - 1);
                                                                 Vertex(int p=-1, char ch='$') : p(p), pch(ch) {
                                                                     fill(begin(next), end(next), -1);
          ans.insert(ans.end(), aux.begin(), aux.end())
                                                                     fill(begin(go), end(go), -1);
           // for (auto e : aux) ans.push_back(e);
12
                                                          15 };
     }
13
                                                          16
14
                                                          17 vector < Vertex > t(1):
     return ans;
                                                          18
16 }
                                                             void add_string(string const& s) {
                                                          19
                                                                 int v = 0:
                                                          20
  4.4 Lcs
                                                                 for (char ch : s) {
                                                          21
                                                                     int c = ch - 'a';
                                                          22
1 // Description:
                                                                     if (t[v].next[c] == -1) {
                                                          23
2 // Finds the longest common subsquence between two
                                                                         t[v].next[c] = t.size();
                                                                         t.emplace_back(v, ch);
      string
                                                          25
                                                                     }
4 // Problem:
                                                          27
                                                                     v = t[v].next[c];
5 // https://codeforces.com/gym/103134/problem/B
                                                          28
                                                          29
                                                                 t[v].output = true;
7 // Complexity:
                                                          30 }
_8 // _0(mn) where m and n are the length of the strings _{31}
                                                          32 int go(int v, char ch);
10 string lcsAlgo(string s1, string s2, int m, int n) { 33
    int LCS_table[m + 1][n + 1];
11
                                                          34 int get_link(int v) {
                                                                 if (t[v].link == -1) {
12
                                                          35
                                                                     if (v == 0 || t[v].p == 0)
    for (int i = 0; i \le m; i++) {
     for (int j = 0; j <= n; j++) {
                                                                         t[v].link = 0;
14
                                                          37
        if (i == 0 || i == 0)
                                                                     else
15
          LCS_table[i][j] = 0;
                                                                         t[v].link = go(get_link(t[v].p), t[v].pch
16
                                                          39
        else if (s1[i - 1] == s2[j - 1])
                                                                 );
17
```

```
}
                                                                     ch = getchar();
40
                                                          10
41
      return t[v].link;
                                                          11
                                                                 }
42 }
                                                          12
                                                                 return x * f;
                                                          13 }
43
44 int go(int v, char ch) {
                                                          14 void print(__int128 x) {
      int c = ch - 'a';
                                                                 if (x < 0) {
45
                                                          15
      if (t[v].go[c] == -1) {
                                                                     putchar('-');
46
                                                          16
          if (t[v].next[c] != -1)
                                                                     x = -x;
47
                                                          17
              t[v].go[c] = t[v].next[c];
48
                                                          18
           else
                                                                 if (x > 9) print(x / 10);
              t[v].go[c] = v == 0 ? 0 : go(get_link(v), 20
                                                                 putchar(x % 10 + '0');
50
       ch);
      }
51
      return t[v].go[c];
52
                                                                  Graphs
53 }
                                                             6.1 Centroid Find
  4.6 Z-function
                                                           1 // Description:
1 vector<int> z_function(string s) {
                                                           2 // Indexed at zero
      int n = (int) s.length();
                                                           _{\rm 3} // Find a centroid, that is a node such that when it
      vector < int > z(n);
                                                                is appointed the root of the tree,
      for (int i = 1, l = 0, r = 0; i < n; ++i) {
                                                           _4 // each subtree has at most floor(n/2) nodes.
          if (i \le r)
              z[i] = min (r - i + 1, z[i - 1]);
                                                           6 // Problem:
           while (i + z[i] < n && s[z[i]] == s[i + z[i]]
                                                           7 // https://cses.fi/problemset/task/2079/
      ]])
               ++z[i];
                                                           9 // Complexity:
           if (i + z[i] - 1 > r)
9
                                                          10 // O(n)
              1 = i, r = i + z[i] - 1;
10
                                                          11
11
                                                          _{12} // How to use:
12
      return z;
                                                          13 // get_subtree_size(0);
13 }
                                                          14 // cout << get_centroid(0) + 1 << endl;</pre>
       Misc
                                                          16 int n;
                                                          17 vector < int > adj [MAX];
  5.1 Split
                                                          18 int subtree_size[MAX];
                                                          20 int get_subtree_size(int node, int par = -1) {
vector<string> split(string txt, char key = ' '){
                                                             int &res = subtree_size[node];
      vector<string> ans;
                                                          22
                                                              res = 1:
                                                          23
                                                               for (int i : adj[node]) {
      string palTemp = "";
                                                                if (i == par) continue;
                                                          24
      for(int i = 0; i < txt.size(); i++){</pre>
                                                                 res += get_subtree_size(i, node);
                                                          25
                                                               }
           if(txt[i] == key){
                                                          27
                                                              return res;
               if(palTemp.size() > 0){
                                                          28 }
                   ans.push_back(palTemp);
                   palTemp = "";
10
                                                          30 int get_centroid(int node, int par = -1) {
              }
11
                                                              for (int i : adj[node]) {
                                                          31
          } else{
                                                                 if (i == par) continue;
                                                          32
               palTemp += txt[i];
13
                                                          33
14
           }
                                                                 if (subtree_size[i] * 2 > n) { return
                                                          34
                                                                 get_centroid(i, node); }
16
                                                               }
                                                          35
17
                                                          36
                                                               return node;
      if(palTemp.size() > 0)
18
                                                          37 }
           ans.push_back(palTemp);
                                                          38
20
                                                          39 int main() {
      return ans;
                                                          40
                                                               cin >> n;
22 }
                                                               for (int i = 0; i < n - 1; i++) {
                                                          41
                                                          42
                                                                 int u, v; cin >> u >> v;
  5.2 Int128
                                                                 u--: v--:
                                                          43
                                                                 adj[u].push_back(v);
                                                          44
1 __int128 read() {
                                                          45
                                                                 adj[v].push_back(u);
      _{-int128} x = 0, f = 1;
                                                          46
      char ch = getchar();
                                                          47
      while (ch < '0' || ch > '9') {
                                                               get_subtree_size(0);
                                                          48
          if (ch == '-') f = -1;
                                                               cout << get_centroid(0) + 1 << endl;</pre>
          ch = getchar();
                                                          50 }
      while (ch >= '0' && ch <= '9') {
                                                             6.2
                                                                   Bipartite
```

x = x * 10 + ch - '0';

```
1 const int NONE = 0, BLUE = 1, RED = 2;
                                                                           if (adj[v][to] < min_e[to].w)</pre>
                                                           33
vector < vector < int >> graph (100005);
                                                            34
                                                                               min_e[to] = {adj[v][to], v};
3 vector < bool > visited(100005);
                                                                       }
                                                            35
4 int color [100005];
                                                            36
                                                            37
6 bool bfs(int s = 1){
                                                                   cout << total_weight << endl;</pre>
                                                            38
                                                            39 }
       queue <int> q;
       q.push(s);
9
                                                                    Ford Fulkerson Edmonds Karp
       color[s] = BLUE;
10
11
                                                            1 // Description:
12
       while (not q.empty()){
                                                            _{2} // Obtains the maximum possible flow rate given a
13
          auto u = q.front(); q.pop();
                                                                  network. A network is a graph with a single
14
                                                                  source vertex and a single sink vertex in which
           for (auto v : graph[u]){
                                                                  each edge has a capacity
               if (color[v] == NONE){
16
                    color[v] = 3 - color[u];
                                                            4 // Complexity:
18
                   q.push(v);
                                                            _{5} // O(V * E^2) where V is the number of vertex and E
               }
                                                                  is the number of edges
               else if (color[v] == color[u]){
20
                   return false;
21
                                                            7 int n;
22
                                                            8 vector < vector < int >> capacity;
           }
23
                                                            9 vector < vector < int >> adj;
25
                                                            int bfs(int s, int t, vector<int>& parent) {
26
       return true;
                                                                   fill(parent.begin(), parent.end(), -1);
27 }
                                                           12
                                                            13
                                                                   parent[s] = -2;
                                                                  queue <pair <int, int >> q;
29 bool is_bipartite(int n){
                                                            14
                                                                  q.push({s, INF});
30
                                                            16
31
       for (int i = 1; i <= n; i++)
           if (color[i] == NONE and not bfs(i))
                                                           17
                                                                   while (!q.empty()) {
32
                                                                      int cur = q.front().first;
               return false;
                                                           18
33
                                                                       int flow = q.front().second;
                                                            19
                                                                       q.pop();
                                                            20
      return true:
35
36 }
                                                           21
                                                            22
                                                                       for (int next : adj[cur]) {
  6.3 Prim
                                                                           if (parent[next] == -1 && capacity[cur][
                                                            23
                                                                   nextl) {
                                                                                parent[next] = cur;
1 int n;
                                                                                int new_flow = min(flow, capacity[cur
2 vector < vector < int >> adj; // adjacency matrix of graph 25
                                                                  ][next]);
_{3} const int INF = 1000000000; // weight INF means there
                                                                                if (next == t)
       is no edge
                                                                                    return new_flow;
                                                            27
                                                                                q.push({next, new_flow});
                                                            28
5 struct Edge {
                                                                           }
                                                            29
      int w = INF, to = -1;
6
                                                                       }
7 };
                                                                  }
                                                           31
                                                           32
9 void prim() {
                                                                  return 0;
                                                           33
       int total_weight = 0;
10
                                                           34 }
       vector < bool > selected(n, false);
11
                                                           35
       vector < Edge > min_e(n);
12
                                                           36 int maxflow(int s, int t) {
       min_e[0].w = 0;
13
                                                           37
                                                                   int flow = 0;
14
                                                                   vector < int > parent(n);
       for (int i=0; i < n; ++i) {
                                                           38
1.5
                                                                   int new_flow;
           int v = -1;
16
           for (int j = 0; j < n; ++ j) {
17
             if (!selected[j] && (v == -1 || min_e[j]. 41
                                                                   while (new_flow = bfs(s, t, parent)) {
18
                                                                      flow += new_flow;
       w < min_e[v].w)
                                                                       int cur = t;
                                                            43
19
                   v = j;
                                                                       while (cur != s) {
20
                                                                           int prev = parent[cur];
                                                            45
21
                                                                           capacity[prev][cur] -= new_flow;
                                                            46
           if (min_e[v].w == INF) {
22
                                                                           capacity[cur][prev] += new_flow;
                                                            47
               cout << "No MST!" << endl;</pre>
                                                                           cur = prev;
               exit(0);
                                                            48
24
                                                                       }
           }
                                                                  }
                                                            50
26
                                                            51
           selected[v] = true;
                                                            52
                                                                   return flow;
           total_weight += min_e[v].w;
                                                            53 }
           if (min_e[v].to != -1)
29
               cout << v << " " << min_e[v].to << endl;</pre>
                                                                     Floyd Warshall
                                                              6.5
31
           for (int to = 0; to < n; ++to) {
```

```
#include <bits/stdc++.h>
                                                                  auto [v, depth] = q.front();
                                                           35
                                                           36
                                                                  q.pop();
                                                                  level[v] = depth;
3 using namespace std;
                                                           37
4 using 11 = long long;
                                                           38
                                                                  for (auto [u,d] : adj[v]) {
6 const int MAX = 507;
                                                                    if (!visited[u]) {
                                                           40
7 const long long INF = 0x3f3f3f3f3f3f3f3f3fLL;
                                                                       visited[u] = true;
                                                           41
                                                                       up[u][0] = v;
                                                           42
                                                                       q.push(mp(u, depth + 1));
9 11 dist[MAX][MAX];
                                                           43
                                                                    }
                                                           44
                                                                  }
11
                                                           45
12 void floyd_warshall() {
                                                           46
                                                                }
      for (int i = 0; i < n; i++) {
                                                           47 }
13
           for (int j = 0; j < n; j++) {
                                                           48
14
               if (i == j) dist[i][j] = 0;
15
                                                           49 void find_level_peso() {
               else if (!dist[i][j]) dist[i][j] = INF;
                                                                queue <pii > q;
16
                                                           50
17
           }
      }
                                                                q.push(mp(1, 0));
18
                                                           52
                                                                visited[1] = true;
       for (int k = 0; k < n; k++) {
20
                                                           54
           for (int i = 0; i < n; i++) {
                                                                while (!q.empty()) {
                                                           55
21
               for (int j = 0; j < n; j++) {
                                                                  auto [v, depth] = q.front();
22
                                                           56
                   // trata o caso no qual o grafo tem
                                                           57
                                                                  q.pop();
23
       arestas com peso negativo
                                                                  level_peso[v] = depth;
                   if (dist[i][k] < INF && dist[k][j] < 59</pre>
24
                                                                  for (auto [u,d] : adj[v]) {
                                                           60
                        dist[i][j] = min(dist[i][j], dist 61
25
                                                                    if (!visited[u]) {
       [i][k] + dist[k][j]);
                                                                      visited[u] = true;
                                                           62
                   }
                                                                      up[u][0] = v;
26
               }
                                                                      q.push(mp(u, depth + d));
27
                                                           64
           }
                                                           65
28
       }
                                                                  }
29
                                                           66
30 }
                                                           67
                                                                }
                                                           68 }
  6.6 Lca
                                                           69
                                                           70 int lca(int a, int b) {
                                                                 // get the nodes to the same level
                                                           71
1 // Description:
                                                                  int mn = min(level[a], level[b]);
_{
m 2} // Find the lowest common ancestor between two nodes _{
m 72}
      in a tree
                                                                  for (int j = 0; j \le BITS; j++) {
                                                           74
                                                                    if (a != -1 && ((level[a] - mn) & (1 << j))) a
4 // Problem:
                                                                  = up[a][j];
5 // https://cses.fi/problemset/task/1135
                                                                    if (b != -1 && ((level[b] - mn) & (1 << j))) b
                                                            76
                                                                  = up[b][j];
7 // Complexity:
                                                           77
8 // O(log n)
                                                            78
                                                                  // special case
10 // How to use:
                                                           79
                                                                  if (a == b) return a;
11 // preprocess();
12 // lca(a, b);
                                                           81
                                                                  // binary search
                                                           82
                                                                  for (int j = BITS; j >= 0; j--) {
_{14} // Notes
                                                            83
                                                                    if (up[a][j] != up[b][j]) {
_{15} // To calculate the distance between two nodes use
                                                           84
                                                                      a = up[a][j];
      the following formula
                                                                       b = up[b][j];
16 // level_peso[a] + level_peso[b] - 2*level_peso[lca(a 86
                                                           87
      , b)]
                                                           88
17
                                                           89
                                                                  return up[a][0];
18 const int MAX = 2e5+10;
                                                           90 }
19 const int BITS = 30;
                                                           91
                                                           92 void preprocess() {
21 vector < pii > adj [MAX];
                                                                visited = vector < bool > (MAX, false);
22 vector < bool > visited(MAX);
                                                           93
                                                                find_level();
                                                           94
                                                                visited = vector < bool > (MAX, false);
24 int up[MAX][BITS + 1];
                                                           95
                                                                find_level_peso();
25 int level[MAX];
                                                           96
26 int level_peso[MAX];
                                                                for (int j = 1; j \le BITS; j++) {
                                                           98
                                                                   for (int i = 1; i <= n; i++) {
                                                           99
28 void find_level() {
                                                                    if (up[i][j - 1] != -1) up[i][j] = up[up[i][j -
   queue <pii > q;
29
                                                                   1]][j - 1];
    q.push(mp(1, 0));
                                                           101
31
                                                                }
    visited[1] = true;
                                                           102
                                                           103 }
33
    while (!q.empty()) {
34
```

6.7 Bellman Ford 11 capacity; 39 40 11 flow; Edge* residual; 41 1 struct edge 42 43 Edge() {} int a, b, cost; 44 Edge(int from, int to, ll capacity) : from(from), to(to), capacity(capacity) { 6 int n, m, v; flow = 0;46 7 vector<edge> e; 47 8 const int INF = 1000000000; 48 49 11 get_capacity() { 10 void solve() return capacity - flow; 50 11 { 51 vector < int > d (n, INF); 12 52 13 d[v] = 0;11 get_flow() { 53 for (int i=0; i < n-1; ++i) return flow; for (int j=0; j < m; ++j) 15 55 if (d[e[j].a] < INF)d[e[j].b] = min (d[e[j].b], d[e[j].a] 56 -void augment(ll bottleneck) { + e[j].cost); flow += bottleneck; 58 18 } residual ->flow -= bottleneck; 59 60 6.8 Dinic void reverse(ll bottleneck) { 62 flow -= bottleneck; 1 // Description: 63 residual ->flow += bottleneck; $_{2}$ // Obtains the maximum possible flow rate given a 64 network. A network is a graph with a single 65 source vertex and a single sink vertex in which bool operator < (const Edge& e) const { each edge has a capacity 67 return true; 68 69 70 }; 5 // https://codeforces.com/gym/103708/problem/J 72 struct Dinic { 7 // Complexity: $_8$ // O(V^2 * E) where V is the number of vertex and E 73 int source; int sink: is the number of edges 74 75 int nodes; 10 // Unit network 11 flow; 76 vector < vector < Edge *>> adj; 77 11 // A unit network is a network in which for any vertex except source and sink either incoming or 78 vector < int > level; vector < int > next; outgoing edge is unique and has unit capacity (79 vector < int > reach; 80 matching problem). 81 vector < bool > visited; 12 // Complexity on unit networks: O(E * sqrt(V)) vector < vector < int >> path; 82 $_{14}$ // Unity capacity networks Dinic(int source, int sink, int nodes) : source($_{\rm 15}$ // A more generic settings when all edges have unit 84 capacities, but the number of incoming and source), sink(sink), nodes(nodes) { adj.resize(nodes + 1); outgoing edges is unbounded $_{16}$ // Complexity on unity capacity networks: O(E * sqrt(86 void add_edge(int from, int to, ll capacity) { 88 Edge* e1 = new Edge(from, to, capacity); 18 // How to use: Edge* e2 = new Edge(to, from, 0); 19 // Dinic dinic = Dinic(num_vertex, source, sink); 90 20 // dinic.add_edge(vertex1, vertex2, capacity); 91 // Edge* e2 = new Edge(to, from, capacity); e1->residual = e2; 92 21 // cout << dinic.max_flow() << '\n';</pre> e2->residual = e1; 93 adj[from].pb(e1); 23 #include <bits/stdc++.h> 94 95 adj[to].pb(e2); 96 25 #define pb push_back 97 26 #define mp make_pair 98 bool bfs() { 27 #define pii pair<int, int> level.assign(nodes + 1, -1); 28 #define ff first 99 queue <int > q; 29 #define ss second 100 q.push(source); 101 30 #define ll long long level[source] = 0; 102 103 32 using namespace std; while (!q.empty()) { 104 int node = q.front(); 105 34 const 11 INF = 1e18+10; q.pop(); 106 36 struct Edge { 107 for (auto e : adj[node]) { int from; 37 if (level[e->to] == -1 && e-> 109 int to;

```
get_capacity() > 0) {
                                                                               }
                                                               176
110
                          level[e->to] = level[e->from] +
                                                              177
                                                                           }
                                                                      }
        1:
                                                               178
                          q.push(e->to);
111
                                                               179
112
                     }
                                                               180
                                                                      ll build_path(int v, int id, ll flow) {
                }
                                                                           visited[v] = true;
113
                                                              181
            }
                                                                           if (v == sink) {
114
                                                               182
                                                                               return flow:
115
                                                               183
            return level[sink] != -1;
116
                                                               184
        }
117
                                                               185
                                                                           for (auto e : adj[v]) {
118
                                                               186
        11 dfs(int v, 11 flow) {
119
                                                               187
                                                                                if (!visited[e->to] && e->get_flow() > 0)
            if (v == sink)
                                                                        ₹
120
                                                                                    visited[e->to] = true;
                 return flow;
121
                                                                                    11 bottleneck = build_path(e->to, id,
122
                                                               189
            int sz = adj[v].size();
                                                                       min(flow, e->get_flow()));
123
                                                                                    if (bottleneck > 0) {
124
            for (int i = next[v]; i < sz; i++) {</pre>
                 Edge* e = adj[v][i];
                                                                                         path[id].pb(e->to);
125
                                                               191
                 if (level[e->to] == level[e->from] + 1 &&192
                                                                                         e->reverse(bottleneck);
126
         e->get_capacity() > 0) {
                                                                                         return bottleneck;
                     11 bottleneck = dfs(e->to, min(flow, 194
                                                                                    }
127
        e->get_capacity()));
                                                                               }
                     if (bottleneck > 0) {
                                                                           }
128
                                                               196
                          e->augment(bottleneck);
                                                               197
                          return bottleneck;
130
                                                              198
                                                                           return 0;
                     }
                                                               199
131
                }
132
                                                              200
                                                                       void print_flow_path() {
133
                                                              201
                 next[v] = i + 1;
                                                                           path.clear();
134
                                                               202
            }
                                                                           11 \text{ sent} = -1;
135
                                                              203
                                                                           int id = -1;
136
                                                               204
                                                                           while (sent != 0) {
            return 0:
137
                                                              205
        }
                                                                               visited.assign(nodes + 1, false);
                                                              206
138
139
                                                               207
                                                                               path.pb(vector<int>{});
                                                                               sent = build_path(source, ++id, INF);
        11 max_flow() {
140
                                                              208
            flow = 0;
                                                                               path[id].pb(source);
141
            while(bfs()) {
                                                                           }
142
                                                              210
                next.assign(nodes + 1, 0);
                                                              211
                                                                           path.pop_back();
143
                 11 sent = -1;
                                                              212
144
                 while (sent != 0) {
                                                                           for (int i = 0; i < id; i++) {
                                                              213
145
                                                                                cout << path[i].size() << '\n';</pre>
146
                     sent = dfs(source, INF);
                                                               214
                                                                               reverse(path[i].begin(), path[i].end());
                     flow += sent;
147
                                                              215
                 }
                                                              216
                                                                                for (auto e : path[i]) {
148
149
            }
                                                              217
                                                                                    cout << e << ' ';
            return flow;
                                                              218
150
        }
                                                               219
                                                                                cout << '\n';
151
                                                                           }
152
                                                              220
153
        void reachable(int v) {
                                                               221
                                                                      }
            visited[v] = true;
                                                              222 };
154
155
                                                              223
            for (auto e : adj[v]) {
                                                               224 int main() {
156
                 if (!visited[e->to] && e->get_capacity() 225
                                                                      ios::sync_with_stdio(false);
157
       > 0) {
                                                                      cin.tie(NULL);
                     reach.pb(e->to);
158
                                                              227
                     visited[e->to] = true;
                                                                       int n, m; cin >> n >> m;
159
                                                              228
                     reachable(e->to);
160
                                                              229
                }
                                                                      Dinic dinic = Dinic(1, n, n);
161
                                                              230
            }
                                                               231
162
                                                                       for (int i = 1; i <= m; i++) {
163
        }
                                                               232
                                                                           int v, u; cin >> v >> u;
164
                                                               233
165
        void print_min_cut() {
                                                              234
                                                                           dinic.add_edge(v, u, 1);
            reach.clear();
166
                                                              235
            visited.assign(nodes + 1, false);
167
                                                               236
                                                                      cout << dinic.max_flow() << '\n';</pre>
            reach.pb(source):
                                                              237
168
169
            reachable(source);
                                                               238
                                                                       // dinic.print_min_cut();
                                                                      // dinic.print_flow_path();
170
                                                              239
            for (auto v : reach) {
171
                                                              240
                 for (auto e : adj[v]) {
                                                              241
                                                                      return 0;
172
                     if (!visited[e->to] && e->
                                                              242 }
173
        get_capacity() == 0) {
                                                                  6.9
                                                                        2sat
                          cout << e->from << ' ' ' << e->to
174
        << '\n';
                     }
175
                                                                1 // Description:
```

```
_2 // Solves expression of the type (a v b) ^ (c v d) ^ _{73}
                                                                       add_or(get_not(a), get_not(b));
      (e v f)
                                                            75
4 // Problem:
                                                                   void add_xnor(int a, int b) {
                                                            76
5 // https://cses.fi/problemset/task/1684
                                                            77
                                                                       add_or(get_not(a), b);
                                                                       add_or(a, get_not(b));
                                                            78
                                                            79
_{8} // O(n + m) where n is the number of variables and m _{80}
      is the number of clauses
                                                                   void departure_time(int v) {
                                                            81
                                                                       visited[v] = true;
10 #include <bits/stdc++.h>
                                                            83
11 #define pb push_back
                                                                       for (auto u : adj[v]) {
12 #define mp make_pair
                                                                            if (!visited[u]) departure_time(u);
                                                            85
13 #define pii pair<int, int>
                                                            86
14 #define ff first
                                                            87
15 #define ss second
                                                                       departure.pb(mp(++curr, v));
                                                            88
                                                            89
17 using namespace std;
                                                            90
                                                                   void find_component(int v, int component) {
                                                            91
19 struct SAT {
                                                                       scc[v] = component;
                                                            92
                                                                       visited[v] = true;
      int nodes;
                                                            93
20
       int curr = 0:
21
                                                            94
      int component = 0;
                                                                       for (auto u : rev[v]) {
22
                                                            95
       vector < vector < int >> adj;
                                                                           if (!visited[u]) find_component(u,
      vector < vector < int >> rev;
                                                                   component);
24
       vector < vector < int >> condensed;
                                                                       }
25
                                                            97
      vector < pii > departure;
26
                                                            98
       vector < bool > visited;
27
                                                            99
       vector < int > scc;
                                                                   void topological_order(int v) {
                                                           100
      vector<int> order;
                                                                       visited[v] = true;
29
                                                           101
                                                           102
30
       // 1 to nodes
                                                                       for (auto u : condensed[v]) {
31
                                                           103
       // nodes + 1 to 2 * nodes
                                                                            if (!visited[u]) topological_order(u);
                                                           104
32
       SAT(int nodes) : nodes(nodes) {
                                                           105
           adj.resize(2 * nodes + 1);
34
                                                           106
           rev.resize(2 * nodes + 1);
                                                                       order.pb(v);
                                                           107
           visited.resize(2 * nodes + 1);
36
                                                           108
           scc.resize(2 * nodes + 1);
                                                           109
37
      }
                                                           110
                                                                   bool is_possible() {
38
                                                                       component = 0;
39
                                                           111
                                                                       for (int i = 1; i <= 2 * nodes; i++) {
40
       void add_imp(int a, int b) {
                                                           112
                                                                            if (!visited[i]) departure_time(i);
           adj[a].pb(b);
41
                                                           113
           rev[b].pb(a);
                                                           114
42
       7
                                                           115
43
                                                                       sort(departure.begin(), departure.end(),
44
                                                           116
       int get_not(int a) {
                                                                   greater < pii > ());
45
           if (a > nodes) return a - nodes;
46
                                                           117
           return a + nodes;
                                                                       visited.assign(2 * nodes + 1, false);
48
                                                           119
                                                                       for (auto [_, node] : departure) {
49
                                                            120
       void add_or(int a, int b) {
                                                                           if (!visited[node]) find_component(node,
50
                                                           121
           add_imp(get_not(a), b);
                                                                   ++component);
51
           add_imp(get_not(b), a);
                                                                       }
                                                           122
53
                                                           123
                                                                       for (int i = 1; i <= nodes; i++) {
54
                                                           124
                                                                            if (scc[i] == scc[i + nodes]) return
       void add_nor(int a, int b) {
55
                                                           125
           add_or(get_not(a), get_not(b));
                                                                   false;
56
                                                           126
57
58
                                                           127
       void add_and(int a, int b) {
                                                           128
                                                                       return true;
59
60
           add_or(get_not(a), b);
                                                           129
           add_or(a, get_not(b));
61
                                                           130
           add_or(a, b);
                                                                   int find_value(int e, vector<int> &ans) {
                                                           131
       }
                                                                       if (e > nodes && ans[e - nodes] != 2) return
63
                                                           132
                                                                   !ans[e - nodes];
                                                                       if (e <= nodes && ans[e + nodes] != 2) return
       void add_nand(int a, int b) {
65
                                                           133
           add_or(get_not(a), b);
                                                                    !ans[e + nodes];
66
           add_or(a, get_not(b));
                                                           134
                                                                       return 0;
67
           add_or(get_not(a), get_not(b));
                                                           135
68
69
                                                            136
                                                                   vector < int > find_ans() {
70
                                                           137
       void add_xor(int a, int b) {
                                                                       condensed.resize(component + 1);
71
                                                           138
           add_or(a, b);
                                                           139
72
```

```
for (int i = 1; i <= 2 * nodes; i++) {
                                                         3 vector < int > adj[MAX];
140
141
                for (auto u : adj[i]) {
                    if (scc[i] != scc[u]) condensed[scc[i 5 bool dfs(int u, int p){
142
       ]].pb(scc[u]);
                                                                    if (visited[u]) return false;
           }
144
                                                                    path.pb(u);
145
                                                                    visited[u] = true;
            visited.assign(component + 1, false);
146
                                                             10
147
                                                             11
            for (int i = 1; i <= component; i++) {</pre>
                                                                    for (auto v : adj[u]){
                if (!visited[i]) topological_order(i);
                                                                        if (visited[v] and u != v and p != v){
149
                                                             13
                                                                             path.pb(v); return true;
151
                                                             15
            reverse(order.begin(), order.end());
152
                                                             16
                                                                         if (dfs(v, u)) return true;
153
                                                             17
            // 0 - false
154
                                                             18
            // 1 - true
155
            // 2 - no value yet
                                                                    path.pop_back();
156
                                                             20
            vector < int > ans(2 * nodes + 1, 2);
                                                                    return false;
                                                             22 }
158
            vector < vector < int >> belong (component + 1);
159
                                                             23
                                                             24 bool has_cycle(int N){
160
            for (int i = 1; i <= 2 * nodes; i++) {
                                                             25
161
                belong[scc[i]].pb(i);
                                                                    visited.reset();
163
                                                             27
                                                                    for (int u = 1; u \le N; ++u){
                                                             28
164
165
            for (auto p : order) {
                                                             29
                                                                         path.clear();
                for (auto e : belong[p]) {
                                                                         if (not visited[u] and dfs(u,-1))
166
                                                             30
                    ans[e] = find_value(e, ans);
                                                                             return true;
                                                             31
168
                                                             32
            }
169
                                                             33
170
                                                             34
            return ans;
                                                                    return false;
171
                                                             35
                                                             36 }
173 }:
                                                                6.11
                                                                       Cycle Path Recovery
174
175 int main() {
176
       ios::sync_with_stdio(false);
                                                             1 int n;
       cin.tie(NULL);
177
                                                             vector < vector < int >> adj;
178
                                                              3 vector < char > color;
179
       int n, m; cin >> n >> m;
                                                              4 vector <int> parent;
180
                                                              5 int cycle_start, cycle_end;
       SAT sat = SAT(m);
181
182
                                                              7 bool dfs(int v) {
       for (int i = 0; i < n; i++) {
183
                                                                    color[v] = 1;
            char op1, op2; int a, b; cin >> op1 >> a >>
                                                                    for (int u : adj[v]) {
                                                             9
       op2 >> b;
                                                                         if (color[u] == 0) {
           if (op1 == '+' && op2 == '+') sat.add_or(a, b<sub>11</sub>
                                                                             parent[u] = v;
                                                                             if (dfs(u))
           if (op1 == '-' && op2 == '-') sat.add_or(sat.<sub>13</sub>
186
                                                                                 return true;
       get_not(a), sat.get_not(b));
                                                                         } else if (color[u] == 1) {
                                                             14
           if (op1 == '+' && op2 == '-') sat.add_or(a,
187
                                                                             cycle_end = v;
       sat.get_not(b));
                                                                             cycle_start = u;
           if (op1 == '-' && op2 == '+') sat.add_or(sat.<sub>17</sub>
188
                                                                             return true;
       get_not(a), b);
                                                             18
189
                                                             19
190
                                                                    color[v] = 2;
       if (!sat.is_possible()) cout << "IMPOSSIBLE\n";</pre>
191
                                                             21
                                                                    return false:
192
       else {
193
            vector < int > ans = sat.find_ans();
                                                             23
            for (int i = 1; i <= m; i++) {
194
                                                             24 void find_cycle() {
                cout << (ans[i] == 1 ? '+' : '-') << ' '; 25
195
                                                                    color.assign(n, 0);
            }
                                                                    parent.assign(n, -1);
                                                             26
            cout << '\n';</pre>
197
                                                                    cycle_start = -1;
198
       }
                                                             28
199
                                                                    for (int v = 0; v < n; v++) {
                                                             29
       return 0;
                                                                         if (color[v] == 0 && dfs(v))
200
                                                             30
201 }
                                                             31
                                                                             break;
                                                             32
   6.10
          Find Cycle
                                                             33
                                                                    if (cycle_start == -1) {
                                                             34
                                                                        cout << "Acyclic" << endl;</pre>
 1 bitset < MAX > visited;
                                                             35
 vector < int > path;
                                                                    } else {
                                                             36
```

```
vector <int > cycle;
                                                         57 int32_t main(){
37
          cycle.push_back(cycle_start);
                                                         ios::sync_with_stdio(false);
38
          for (int v = cycle_end; v != cycle_start; v = 59
                                                                cin.tie(NULL);
39
       parent[v])
                                                        60
              cycle.push_back(v);
                                                                cin >> n;
                                                                adj.resize(n + 1);
           cycle.push_back(cycle_start);
                                                         62
41
          reverse(cycle.begin(), cycle.end());
                                                                ans.resize(n + 1);
                                                         63
                                                                removed.resize(n + 1);
43
                                                         64
          cout << "Cycle found: ";</pre>
                                                                subtree_size.resize(n + 1);
                                                         65
          for (int v : cycle)
                                                         66
            cout << v << " ";
                                                                for (int i = 1; i \le n - 1; i++) {
46
                                                         67
                                                                    int u, v; cin >> u >> v;
47
           cout << endl;</pre>
                                                         68
      }
                                                                     adj[u].insert(v);
48
                                                         69
49 }
                                                                     adj[v].insert(u);
                                                         70
                                                         71
         Centroid Decomposition
  6.12
                                                         72
                                                                solve(1, 'A');
                                                         73
                                                         74
1 int n;
vector < set < int >> adj;
                                                         75
                                                                if (!flag) cout << "Impossible!\n";</pre>
3 vector < char > ans;
                                                         76
                                                                else {
                                                         77
                                                                    for (int i = 1; i <= n; i++) {
                                                                         cout << ans[i] << ' ';
                                                         78
5 vector < bool > removed;
                                                         79
                                                                     cout << '\n';</pre>
7 vector<int> subtree_size;
                                                         81
9 int dfs(int u, int p = 0) {
                                                         82
   subtree_size[u] = 1;
                                                         83
                                                                return 0;
10
                                                         84 }
   for(int v : adj[u]) {
12
                                                                   Tarjan Bridge
                                                            6.13
     if(v != p && !removed[v]) {
        subtree_size[u] += dfs(v, u);
                                                          1 // Description:
15
                                                          2 // Find a bridge in a connected unidirected graph
16
                                                          3 // A bridge is an edge so that if you remove that
17
    return subtree_size[u];
                                                               edge the graph is no longer connected
19 }
                                                          5 // Problem:
20
                                                          6 // https://cses.fi/problemset/task/2177/
21 int get_centroid(int u, int sz, int p = 0) {
22 for(int v : adj[u]) {
     if(v != p && !removed[v]) {
                                                          8 // Complexity:
       if(subtree_size[v]*2 > sz) {
                                                          _{9} // O(V + E) where V is the number of vertices and E
24
          return get_centroid(v, sz, u);
                                                                is the number of edges
26
              }
                                                         11 int n;
28
      }
                                                         12 vector < vector < int >> adj;
29
                                                         13
30
    return u;
                                                         14 vector < bool > visited;
31 }
                                                         15 vector <int> tin, low;
                                                         16 int timer;
33 char get_next(char c) {
                                                         17
34    if (c != 'Z') return c + 1;
                                                         18 void dfs(int v, int p) {
      return '$';
                                                               visited[v] = true;
36 }
                                                                tin[v] = low[v] = timer++;
                                                         20
                                                                for (int to : adj[v]) {
                                                         21
                                                                    if (to == p) continue;
38 bool flag = true;
                                                         22
                                                         23
                                                                    if (visited[to]) {
39
40 void solve(int node, char c) {
                                                                         low[v] = min(low[v], tin[to]);
   int center = get_centroid(node, dfs(node));
                                                                    } else {
41
                                                         25
     ans[center] = c;
                                                                         dfs(to, v);
      removed[center] = true;
                                                                         low[v] = min(low[v], low[to]);
43
                                                         27
                                                                         if (low[to] > tin[v]) {
                                                         28
44
      for (auto u : adj[center]) {
                                                                             IS_BRIDGE(v, to);
45
                                                         29
          if (!removed[u]) {
46
                                                         30
               char next = get_next(c);
                                                         31
                                                                    }
               if (next == '$') {
48
                                                         32
                   flag = false;
49
                                                         33 }
50
                   return;
                                                         34
                                                         35 void find_bridges() {
51
               solve(u, next);
                                                                timer = 0;
                                                         36
          }
                                                                visited.assign(n, false);
53
                                                         37
      }
                                                                tin.assign(n, -1);
                                                          38
55 }
                                                                low.assign(n, -1);
                                                         39
                                                                for (int i = 0; i < n; ++i) {
56
                                                          40
```

Tree Diameter 6.15 if (!visited[i]) 41 42 dfs(i, -1); } 43 1 #include <bits/stdc++.h> 44 } 3 using namespace std; 6.14Small To Large 5 const int MAX = 3e5+17; 1 // Problem: 7 vector < int > adj[MAX]; 2 // https://codeforces.com/contest/600/problem/E 8 bool visited[MAX]; 4 void process_colors(int curr, int parent) { 10 int max_depth = 0, max_node = 1; 11 for (int n : adj[curr]) { 12 void dfs (int v, int depth) { if (n != parent) { visited[v] = true; 13 process_colors(n, curr); if (depth > max_depth) { if (colors[curr].size() < colors[n].size 16 10 max_depth = depth; ()) { max_node = v; 17 sum_num[curr] = sum_num[n]; 11 18 vmax[curr] = vmax[n]; 12 19 swap(colors[curr], colors[n]); 13 for (auto u : adi[v]) { 20 14 if (!visited[u]) dfs(u, depth + 1); 15 22 for (auto [item, vzs] : colors[n]) { 16 23 } if(colors[curr][item]+vzs > vmax[curr 17 1){ vmax[curr] = colors[curr][item] + 25 int tree_diameter() { dfs(1, 0); 18 vzs: max_depth = 0; 27 sum_num[curr] = item; 19 for (int i = 0; i < MAX; i++) visited[i] = false;</pre> 28 } 20 29 dfs(max_node, 0); else if(colors[curr][item]+vzs == 21 return max_depth; 30 vmax[curr]){ 31 } 22 sum_num[curr] += item; } 23 6.16 Dijkstra colors[curr][item] += vzs; 25 1 const int MAX = 2e5+7; 26 } 2 const int INF = 1000000000; 27 } 28 3 vector < vector < pair < int , int >>> adj(MAX); 30 } 5 void dijkstra(int s, vector<int> & d, vector<int> & p 31) { 32 int n = adj.size(); 6 33 int32_t main() { 7 d.assign(n, INF); p.assign(n, -1); 8 int n; cin >> n; 35 d[s] = 0;10 for (int i = 1; i <= n; i++) { 37 11 set < pair < int , int >> q; int a; cin >> a; q.insert({0, s}); 38 12 colors[i][a] = 1; 39 while (!q.empty()) { 13 vmax[i] = 1; 40 int v = q.begin()->second; 14 sum_num[i] = a; q.erase(q.begin()); 15 } 42 16 43 for (auto edge : adj[v]) { 17 for (int i = 1; i < n; i++) { 44 int to = edge.first; 18 int a, b; cin >> a >> b; 45 int len = edge.second; 19 20 47 adj[a].push_back(b); if (d[v] + len < d[to]) {</pre> adj[b].push_back(a); 48 q.erase({d[to], to}); 22 49 d[to] = d[v] + len;23 50 24 p[to] = v;process_colors(1, 0); 25 q.insert({d[to], to}); 52 } 53 for (int i = 1; $i \le n$; i++) { } 27 cout << sum_num[i] << (i < n ? " " : "\n");</pre> 54 28 55 29 } 56 30 return 0; 57 31 vector<int> restore_path(int s, int t) { vector < int > path; 32 59 } 33 60 for (int v = t; v != s; v = p[v]) 34 path.push_back(v); 35

```
path.push_back(s);
                                                                           swap(a, b);
36
                                                            32
37
                                                            33
                                                                       sizes[a] += sizes[b];
       reverse(path.begin(), path.end());
38
                                                            34
                                                                       link[b] = a;
       return path;
                                                            35
39
40 }
                                                            37 }:
41
42 int adj[MAX][MAX];
43 int dist[MAX]:
                                                            39 struct Edge {
44 int minDistance(int dist[], bool sptSet[], int V) {
                                                                   int u, v;
                                                           40
       int min = INT_MAX, min_index;
                                                                   long long weight;
                                                            41
46
                                                            42
47
       for (int v = 0; v < V; v++)
                                                            43
                                                                   Edge() {}
           if (sptSet[v] == false && dist[v] <= min)</pre>
48
                                                            44
               min = dist[v], min_index = v;
                                                                   Edge(int u, int v, long long weight) : u(u), v(v)
49
                                                            45
50
                                                                   , weight(weight) {}
       return min_index;
51
                                                            46
52 }
                                                            47
                                                                   bool operator < (const Edge& other) const {</pre>
                                                                       return weight < other.weight;</pre>
53
                                                            48
54 void dijkstra(int src, int V) {
55
                                                            50
       bool sptSet[V];
                                                                   bool operator > (const Edge& other) const {
                                                            51
56
       for (int i = 0; i < V; i++)
                                                            52
                                                                      return weight > other.weight;
57
           dist[i] = INT_MAX, sptSet[i] = false;
58
                                                            53
                                                            54 };
       dist[src] = 0:
60
                                                            55
                                                            56 vector < Edge > kruskal (vector < Edge > edges, int n) {
61
       for (int count = 0; count < V - 1; count++) {</pre>
                                                                   vector < Edge > result; // arestas da MST
62
                                                            57
           int u = minDistance(dist, sptSet, V);
                                                                   long long cost = 0;
63
                                                            58
                                                            59
           sptSet[u] = true;
                                                                   sort(edges.begin(), edges.end());
65
                                                            60
                                                            61
66
                                                                   DSU dsu(n);
67
                                                            62
           for (int v = 0; v < V; v++)
                                                            63
68
               if (!sptSet[v] && adj[u][v]
                                                            64
                                                                   for (auto e : edges) {
                   && dist[u] != INT_MAX
                                                                       if (!dsu.same(e.u, e.v)) {
70
                                                            65
                   && dist[u] + adj[u][v] < dist[v])
                                                                            cost += e.weight;
                   dist[v] = dist[u] + adj[u][v];
                                                                           result.push_back(e);
72
                                                            67
73
                                                            68
                                                                           dsu.unite(e.u, e.v);
74 }
                                                            69
                                                                       }
                                                                   }
                                                            70
         Kruskall
  6.17
                                                            71
                                                                   return result;
                                                            72
1 struct DSU {
                                                            73 }
      int n;
       vector<int> link, sizes;
                                                                   Geometry
       DSU(int n) {
          this ->n = n;
                                                              7.1 2d
           link.assign(n+1, 0);
           sizes.assign(n+1, 1);
9
                                                            1 #define vp vector<point>
           for (int i = 0; i \le n; i++)
                                                            2 #define ld long double
                                                            3 const ld EPS = 1e-6;
               link[i] = i;
11
       }
                                                            4 const ld PI = acos(-1);
12
13
       int find(int x) {
                                                            6 // typedef ll cod;
14
           while (x != link[x])
                                                            7 // bool eq(cod a, cod b){ return (a==b); }
15
               x = link[x];
                                                            8 typedef ld cod;
16
                                                            9 bool eq(cod a, cod b){ return abs(a - b) <= EPS; }</pre>
18
           return x;
                                                            10
                                                            11 struct point{
19
20
                                                            12
                                                                  cod x, y;
       bool same(int a, int b) {
                                                                   int id;
21
                                                            13
```

14

15

16

17

18

19

point(cod x=0, cod y=0): x(x), y(y){}

o.x, y+o.y}; }

o.x, y-o.y}; }

point operator+(const point &o) const{ return {x+

point operator-(const point &o) const{ return {x-

point operator*(cod t) const{ return {x*t, y*t};

point operator/(cod t) const{ return {x/t, y/t};

22

23

25

26

28

30

31

return find(a) == find(b);

void unite(int a, int b) {

if (a == b) return;

if (sizes[a] < sizes[b])</pre>

a = find(a);

b = find(b);

```
cod operator*(const point &o) const{ return x * 087
                                                                 for(int i=0;i<len;i++)
20
      .x + y * o.y; }
                                                                    c=c+A[i];
      cod operator (const point &o) const{ return x * 089
                                                                  return c/len;
21
      .y - y * o.x; }
                                                          90 }
22
      bool operator < (const point &o) const{</pre>
          return (eq(x, o.x) ? y < o.y : x < o.x);
                                                           92 point forca_mod(point p, ld m){
23
                                                                  ld cm = norm(p);
24
                                                                  if(cm<EPS) return point();</pre>
      bool operator == (const point &o) const{
25
                                                           94
          return eq(x, o.x) and eq(y, o.y);
                                                                  return point(p.x*m/cm,p.y*m/cm);
26
                                                           95
27
    friend ostream& operator << (ostream& os, point p) { 97</pre>
28
      return os << "(" << p.x << "," << p.y << ")"; }
29
                                                           98 ld param(point a, point b, point v){
                                                                 // v = t*(b-a) + a // return t;
30 };
                                                           99
                                                                 // assert(line(a, b).inside_seg(v));
31
                                                           100
_{32} int ccw(point a, point b, point e){ // -1=dir; 0=
                                                                  return ((v-a) * (b-a)) / ((b-a) * (b-a));
                                                          101
      collinear; 1=esq;
cod tmp = (b-a) ^ (e-a); // vector from a to b
                                                          102 }
                                                          103
      return (tmp > EPS) - (tmp < -EPS);
                                                          104 bool simetric(vp &a){ //ordered
34
35 }
                                                                 int n = a.size();
                                                                  point c = center(a);
36
                                                          106
37 ld norm(point a){ // Modulo
                                                          107
                                                                  if(n&1) return false;
      return sqrt(a * a);
                                                                  for (int i=0; i < n/2; i++)
38
                                                          108
39 }
                                                                      if(ccw(a[i], a[i+n/2], c) != 0)
                                                          109
40 cod norm2(point a){
                                                                          return false;
                                                          110
      return a * a;
                                                                  return true;
41
                                                          111
42 }
                                                          112 }
43 bool nulo(point a){
                                                          113
      return (eq(a.x, 0) \text{ and } eq(a.y, 0));
                                                          114 point mirror(point m1, point m2, point p){
44
45 }
                                                                  // mirror point p around segment m1m2
                                                          115
46 point rotccw(point p, ld a){
                                                                  point seg = m2-m1;
                                                          116
      // a = PI*a/180; // graus
                                                                  1d \ t0 = ((p-m1)*seg) / (seg*seg);
                                                          117
      return point((p.x*cos(a)-p.y*sin(a)), (p.y*cos(a)118
                                                                  point ort = m1 + seg*t0;
48
      +p.x*sin(a)));
                                                                  point pm = ort-(p-ort);
                                                          119
49 }
                                                                  return pm;
50 point rot90cw(point a) { return point(a.y, -a.x); }; 121 }
51 point rot90ccw(point a) { return point(-a.y, a.x); };122
53 ld proj(point a, point b){ // a sobre b
                                                          124 ///////////
      return a*b/norm(b);
                                                          125 // Line //
54
55 }
                                                          126 //////////
56 ld angle(point a, point b){ // em radianos
                                                          127
      ld ang = a*b / norm(a) / norm(b);
                                                          128 struct line{
57
      return acos(max(min(ang, (ld)1), (ld)-1));
                                                          129
                                                                 point p1, p2;
58
                                                                  cod a, b, c; // ax+by+c = 0;
59 }
                                                          130
                                                                  // y-y1 = ((y2-y1)/(x2-x1))(x-x1)
60 ld angle_vec(point v){
                                                          131
      // return 180/PI*atan2(v.x, v.y); // graus
                                                          132
                                                                  line(point p1=0, point p2=0): p1(p1), p2(p2){
61
                                                                      a = p1.y - p2.y;
      return atan2(v.x, v.y);
62
                                                          133
63 }
                                                                      b = p2.x - p1.x;
64 ld order_angle(point a, point b){ // from a to b ccw 135
                                                                      c = p1 ^p2;
      (a in front of b)
                                                          136
                                                                  line(cod a=0, cod b=0, cod c=0): a(a), b(b), c(c)
      ld aux = angle(a,b)*180/PI;
                                                           137
      return ((a^b) \le 0 ? aux : 360 - aux);
66
67 }
                                                                      // Gera os pontos p1 p2 dados os coeficientes
                                                                      // isso aqui eh um lixo mas quebra um galho
68 bool angle_less(point a1, point b1, point a2, point 139
      b2){ // ang(a1,b1) <= ang(a2,b2)
                                                                  kkkkkk
      point p1((a1*b1), abs((a1^b1)));
                                                                      if(b==0){}
69
      point p2((a2*b2), abs((a2^b2)));
                                                                          p1 = point(1, -c/a);
70
                                                          141
                                                                          p2 = point(0, -c/a);
      return (p1^p2) <= 0;
71
                                                          142
72 }
                                                          143
                                                                      }else{
                                                                          p1 = point(1, (-c-a*1)/b);
73
                                                          144
                                                                          p2 = point(0, -c/b);
74 ld area(vp &p){ // (points sorted)
                                                          145
      ld ret = 0:
75
                                                          146
      for(int i=2;i<(int)p.size();i++)</pre>
                                                                  }
                                                          147
          ret += (p[i]-p[0])^(p[i-1]-p[0]);
77
                                                          148
      return abs(ret/2);
                                                          149
                                                                  cod eval(point p){
79 }
                                                                      return a*p.x+b*p.v+c:
                                                          150
80 ld areaT(point &a, point &b, point &c){
                                                          151
      return abs((b-a)^(c-a))/2.0;
                                                          152
                                                                  bool inside(point p){
81
82 }
                                                                      return eq(eval(p), 0);
                                                          153
                                                          154
84 point center(vp &A){
                                                                  point normal(){
                                                          155
     point c = point();
                                                          156
                                                                      return point(a, b);
      int len = A.size();
                                                          157
```

```
r = norm(a-c):
158
                                                           224
       bool inside_seg(point p){
                                                           225
                                                                   }
159
                                                                   bool inside(const point &a) const{
160
           return (
                                                           226
                ((p1-p) ^ (p2-p)) == 0 and
                                                           227
                                                                      return norm(a - c) <= r + EPS;
161
                ((p1-p) * (p2-p)) <= 0
                                                           228
           ):
                                                           229 }:
163
164
                                                           230
                                                           231 pair < point , point > tangent_points (circle cr, point p)
165
166 };
                                                                   1d d1 = norm(p-cr.c), theta = asin(cr.r/d1);
167
                                                           232
_{168} // be careful with precision error
                                                                   point p1 = rotccw(cr.c-p, -theta);
                                                           233
      inter_line(line 11, line 12){
                                                           234
                                                                   point p2 = rotccw(cr.c-p, theta);
                                                                   assert(d1 >= cr.r);
       ld det = l1.a*l2.b - l1.b*l2.a;
170
                                                           235
       if(det==0) return {};
                                                                   p1 = p1 * (sqrt(d1*d1-cr.r*cr.r) / d1) + p;
                                                           236
171
       1d x = (11.b*12.c - 11.c*12.b)/det;
                                                                   p2 = p2 * (sqrt(d1*d1-cr.r*cr.r) / d1) + p;
172
                                                           237
       1d y = (11.c*12.a - 11.a*12.c)/det;
                                                                   return {p1, p2};
173
                                                           238
174
       return {point(x, y)};
                                                           239 }
175
                                                           240
                                                           241
                                                           242 circle incircle(point p1, point p2, point p3){
177 // segments not collinear
178 vp inter_seg(line 11, line 12){
                                                                   1d m1 = norm(p2-p3);
                                                           243
                                                                   1d m2 = norm(p1-p3);
       vp ans = inter_line(l1, l2);
179
                                                           244
                                                                   1d m3 = norm(p1-p2);
       if(ans.empty() or !l1.inside_seg(ans[0]) or !l2. 245
180
       inside_seg(ans[0]))
                                                                   point c = (p1*m1 + p2*m2 + p3*m3)*(1/(m1+m2+m3));
                                                                   1d s = 0.5*(m1+m2+m3);
           return {};
181
                                                           247
       return ans;
                                                                   1d r = sqrt(s*(s-m1)*(s-m2)*(s-m3)) / s;
                                                           248
182
183 }
                                                           249
                                                                   return circle(c, r);
184 bool seg_has_inter(line 11, line 12){
                                                           250 }
       return ccw(l1.p1, l1.p2, l2.p1) * ccw(l1.p1, l1. 251
185
       p2, 12.p2) < 0 and
                                                           252 circle circumcircle(point a, point b, point c) {
              ccw(12.p1, 12.p2, 11.p1) * ccw(12.p1, 12.253
                                                                   circle ans;
186
       p2, 11.p2) < 0;
                                                                   point u = point((b-a).y, -(b-a).x);
                                                           254
187
                                                                   point v = point((c-a).y, -(c-a).x);
                                                           255
                                                           256
                                                                   point n = (c-b)*0.5;
189 ld dist_seg(point p, point a, point b){ // point -
                                                                   1d t = (u^n)/(v^u);
                                                           257
                                                                   ans.c = ((a+c)*0.5) + (v*t);
                                                           258
                                                                   ans.r = norm(ans.c-a);
       if((p-a)*(b-a) < EPS) return norm(p-a);
190
                                                           259
       if((p-b)*(a-b) < EPS) return norm(p-b);
                                                           260
                                                                   return ans;
191
       return abs((p-a)^(b-a)) / norm(b-a);
                                                           261 }
192
193
                                                           262
194
                                                           263 vp inter_circle_line(circle C, line L){
195 ld dist_line(point p, line l){ // point - line
                                                                   point ab = L.p2 - L.p1, p = L.p1 + ab * ((C.c-L.
                                                           264
                                                                   p1)*(ab) / (ab*ab));
       return abs(1.eval(p))/sqrt(1.a*1.a + 1.b*1.b);
196
197 }
                                                                   ld s = (L.p2-L.p1)^(C.c-L.p1), h2 = C.r*C.r - s*s
                                                           265
                                                                    / (ab*ab);
198
199 line bisector(point a, point b){
                                                                   if (h2 < -EPS) return {};
                                                           266
                                                                   if (eq(h2, 0)) return {p};
       point d = (b-a)*2:
200
                                                           267
201
       return line(d.x, d.y, a*a - b*b);
                                                                   point h = (ab/norm(ab)) * sqrt(h2);
202 }
                                                                   return \{p - h, p + h\};
                                                           269
                                                           270 }
203
204 line perpendicular(line 1, point p){ // passes
                                                           271
                                                           272 vp inter_circle(circle C1, circle C2){
       through p
       return line(1.b, -1.a, -1.b*p.x + 1.a*p.y);
                                                                   if(C1.c == C2.c) { assert(C1.r != C2.r); return
206 }
                                                                   {}; }
                                                                   point vec = C2.c - C1.c;
207
                                                           274
                                                           275
                                                                   1d d2 = vec*vec, sum = C1.r+C2.r, dif = C1.r-C2.r
208
209 ///////////
210 // Circle //
                                                                   1d p = (d2 + C1.r*C1.r - C2.r*C2.r)/(d2*2), h2 =
                                                           276
211 //////////
                                                                   C1.r*C1.r - p*p*d2;
                                                                   if (sum*sum < d2 or dif*dif > d2) return {};
212
                                                           277
                                                                   point mid = C1.c + vec*p, per = point(-vec.y, vec
213 struct circle{
                                                           278
       point c; cod r;
                                                                   .x) * sqrt(max((1d)0, h2) / d2);
214
       circle() : c(0, 0), r(0) {}
                                                                   if(eq(per.x, 0) and eq(per.y, 0)) return {mid};
                                                           279
       circle(const point o) : c(o), r(0){}
                                                                   return {mid + per, mid - per};
216
                                                           280
217
       circle(const point a, const point b){
                                                           281 }
           c = (a+b)/2;
218
                                                           282
           r = norm(a-c);
                                                           283 // minimum circle cover O(n) amortizado
219
       }
                                                           284 circle min_circle_cover(vp v){
220
       circle(const point a, const point b, const point 285
                                                                   random_shuffle(v.begin(), v.end());
221
                                                                   circle ans;
           assert(ccw(a, b, cc) != 0);
                                                                   int n = v.size();
222
                                                           287
            c = inter_line(bisector(a, b), bisector(b, cc288
                                                                   for(int i=0;i<n;i++) if(!ans.inside(v[i])){</pre>
223
       ))[0]:
                                                                       ans = circle(v[i]);
```

```
for(int j=0;j<i;j++) if(!ans.inside(v[j])){</pre>
                                                                 for(int j = 0; j < n; j++){
290
291
               ans = circle(v[i], v[j]);
                                                                  if((counter & (1LL << j)) != 0) {
                                                                      cout << nums[j] << '';</pre>
               for(int k=0; k < j; k++) if(!ans.inside(v[k]) 8
292
       ) {
                    ans = circle(v[i], v[j], v[k]);
                                                                  }
               }
                                                                  cout << '\n';</pre>
294
                                                           11
                                                                }
           }
                                                           12
       }
                                                           13 }
296
       return ans;
297
                                                                    Binary Search Last True
298 }
        Algorithms
                                                                 {
                                                                10--;
```

8.1 Lis

```
int lis(vector < int > const& a) {
      int n = a.size();
      vector < int > d(n, 1);
      for (int i = 0; i < n; i++) {
          for (int j = 0; j < i; j++) {
              if (a[j] < a[i])
                  d[i] = max(d[i], d[j] + 1);
9
      }
10
11
      int ans = d[0];
      for (int i = 1; i < n; i++) {
12
13
          ans = max(ans, d[i]);
14
      return ans;
15
16 }
```

Delta-encoding

```
1 #include <bits/stdc++.h>
2 using namespace std;
4 int main(){
      int n, q;
      cin >> n >> q;
       int [n];
      int delta[n+2];
9
       while(q--){
         int 1, r, x;
11
           cin >> 1 >> r >> x;
12
           delta[1] += x;
13
           delta[r+1] = x;
14
      }
16
17
       int curr = 0;
       for(int i=0; i < n; i++){
18
          curr += delta[i];
19
           v[i] = curr;
20
      }
21
22
       for(int i=0; i < n; i++){</pre>
23
         cout << v[i] << '';
25
       cout << '\n';
26
27
28
       return 0:
29 }
```

8.3 Subsets

```
void subsets(vector<int>& nums){
   int n = nums.size():
    int powSize = 1 << n;</pre>
```

```
int last_true(int lo, int hi, function < bool(int) > f)
   while (lo < hi) {
     int mid = lo + (hi - lo + 1) / 2;
4
      if (f(mid)) {
       lo = mid;
      } else {
        hi = mid - 1;
9
    }
10
    return lo:
11
12 }
```

Ternary Search

```
1 double ternary_search(double 1, double r) {
      double eps = 1e-9;
                                     //set the error
      limit here
      while (r - 1 > eps) {
3
          double m1 = 1 + (r - 1) / 3;
4
          double m2 = r - (r - 1) / 3;
5
          double f1 = f(m1);
                                 //evaluates the
      function at m1
          double f2 = f(m2); //evaluates the
      function at m2
         if (f1 < f2)
             1 = m1;
          else
10
             r = m2;
11
      }
12
      return f(1);
                                      //return the
13
      maximum of f(x) in [1, r]
```

Binary Search First True

```
int first_true(int lo, int hi, function < bool(int) > f)
      -{
    hi++;
2
   while (lo < hi) {
     int mid = lo + (hi - lo) / 2;
      if (f(mid)) {
       hi = mid;
6
      } else {
        lo = mid + 1;
      }
9
10
   }
   return lo;
11
```

Biggest K 8.7

```
_{\rm 1} // Description: Gets sum of k biggest or k smallest
                                                             elements in an array
                                                       3 // Problem: https://atcoder.jp/contests/abc306/tasks/
                                                             abc306_e
                                                       5 // Complexity: O(log n)
for(int counter = 0; counter < powSize; counter++){ 7 struct SetSum {</pre>
```

```
11 s = 0;
9
       multiset <11> mt;
      void add(ll x){
10
11
          mt.insert(x);
           s += x;
      }
13
      int pop(11 x){
14
          auto f = mt.find(x);
1.5
           if(f == mt.end()) return 0;
16
           mt.erase(f);
           s -= x;
18
19
           return 1;
      }
20
21 };
23 struct BigK {
24
      int k;
       SetSum gt, mt;
25
       BigK(int _k){
          k = _k;
27
28
       void balancear(){
29
         while((int)gt.mt.size() < k && (int)mt.mt.
30
       size()){
               auto p = (prev(mt.mt.end()));
31
               gt.add(*p);
32
33
               mt.pop(*p);
34
           while((int)mt.mt.size() && (int)gt.mt.size()
      &r. &r.
           *(gt.mt.begin()) < *(prev(mt.mt.end())) ){
36
               11 u = *(gt.mt.begin());
37
               11 v = *(prev(mt.mt.end()));
38
               gt.pop(u); mt.pop(v);
               gt.add(v); mt.add(u);
40
           }
41
      }
42
       void add(11 x){
43
           mt.add(x);
           balancear();
45
46
      void rem(ll x){
47
          //x = -x;
48
           if(mt.pop(x) == 0)
10
               gt.pop(x);
50
           balancear();
51
      }
52
53 };
54
55 int main() {
      ios::sync_with_stdio(false);
56
       cin.tie(NULL);
57
      int n, k, q; cin >> n >> k >> q;
59
60
      BigK big = BigK(k);
61
62
      int arr[n] = {};
64
       while (q--) {
65
66
         int pos, num; cin >> pos >> num;
           big.rem(arr[pos]);
           arr[pos] = num:
69
           big.add(arr[pos]);
           cout << big.gt.s << '\n';</pre>
      }
74
       return 0;
75
76 }
```

9 Data Structures

9.1 Ordered Set

```
1 // Description:
2 // insert(k) - add element k to the ordered set
3 // erase(k) - remove element k from the ordered set
4 // erase(it) - remove element it points to from the
       ordered set
5 // order_of_key(k) - returns number of elements
      strictly smaller than k
6 // find_by_order(n) - return an iterator pointing to
      the k-th element in the ordered set (counting
       from zero).
8 // Problem:
9 // https://cses.fi/problemset/task/2169/
10
11 // Complexity:
_{12} // O(log n) for all operations
_{14} // How to use:
15 // ordered_set <int> os;
16 // cout << os.order_of_key(1) << '\n;</pre>
17 // cout << os.find_by_order(1) << '\n;</pre>
_{19} // Notes
20 // The ordered set only contains different elements
21 // By using less_equal <T> instead of less <T> on using
       ordered_set declaration
22 // The ordered_set becomes an ordered_multiset
_{\rm 23} // So the set can contain elements that are equal
25 #include <ext/pb_ds/assoc_container.hpp>
26 #include <ext/pb_ds/tree_policy.hpp>
28 using namespace __gnu_pbds;
29 template <typename T>
30 using ordered_set = tree<T,null_type,less<T>,
       rb_tree_tag,tree_order_statistics_node_update>;
31
32 void Erase(ordered_set < int >& a, int x){
      int r = a.order_of_key(x);
       auto it = a.find_by_order(r);
34
       a.erase(it);
35
```

9.2 Priority Queue

```
1 // Description:
2 // Keeps the largest (by default) element at the top
      of the queue
4 // Problem:
5 // https://cses.fi/problemset/task/1164/
7 // Complexity:
8 // O(log n) for push and pop
_{9} // O (1) for looking at the element at the top
10
11 // How to use:
12 // prioriy_queue < int > pq;
13 // pq.push(1);
14 // pq.top();
15 // pq.pop()
17 // Notes
_{18} // To use the priority queue keeping the smallest
      element at the top
20 priority_queue <int, vector <int>, greater <int>> pq;
```

9.3 Dsu

```
#include <bits/stdc++.h>
3 using namespace std;
5 const int MAX = 1e6+17;
7 struct DSU {
      int n;
      vector <int > link, sizes;
10
11
      DSU(int n) {
         this ->n = n;
12
           link.assign(n+1, 0);
13
          sizes.assign(n+1, 1);
15
           for (int i = 0; i \le n; i++)
               link[i] = i;
17
      }
18
19
      int find(int x) {
20
           while (x != link[x])
21
             x = link[x];
22
23
24
           return x;
25
      bool same(int a, int b) {
27
          return find(a) == find(b);
29
30
      void unite(int a, int b) {
31
          a = find(a);
32
          b = find(b);
34
           if (a == b) return;
36
           if (sizes[a] < sizes[b])</pre>
               swap(a, b);
39
           sizes[a] += sizes[b];
           link[b] = a;
41
42
43
      int size(int x) {
44
45
           return sizes[x];
46
47 };
48
49 int main() {
       ios::sync_with_stdio(false);
       cin.tie(NULL);
51
      int cities, roads; cin >> cities >> roads;
53
       vector < int > final_roads;
54
       int ans = 0;
55
       DSU dsu = DSU(cities);
56
       for (int i = 0, a, b; i < roads; i++) {
           cin >> a >> b;
58
           dsu.unite(a, b);
59
60
61
       for (int i = 2; i <= cities; i++) {</pre>
           if (!dsu.same(1, i)) {
63
               ans++:
               final_roads.push_back(i);
65
               dsu.unite(1,i);
66
           }
      }
68
       cout << ans << '\n';</pre>
70
       for (auto e : final_roads) {
71
```

```
1 // Description
 _{2} // THe values are divided in two multisets so that
      one of them contain all values that are
 _{\mathrm{3}} // smaller than the median and the other one contains
       all values that are greater or equal to the
       median.
5 // Problem:
 6 // https://atcoder.jp/contests/abc306/tasks/abc306_e
7 // Problem I - Maratona Feminina de çãProgramao da
       Unicamp 2023
 8 // https://codeforces.com/group/WYIydkiPyE/contest
      /450037/attachments
9
10 // Complexity:
_{11} // Add and remove elements - O(log n)
12 // Return sum of biggest or smallest set or return
       the median - 0(1)
13
14 using ll = long long;
16 struct TwoSets {
17 multiset <int > small;
    multiset <int > big;
18
     11 \text{ sums} = 0:
19
     11 \text{ sumb} = 0;
20
21
    int n = 0;
22
     int size_small() {
23
      return small.size();
24
25
26
27
     int size_big() {
      return big.size();
28
29
30
     void balance() {
31
32
       while (size_small() > n / 2) {
         int v = *small.rbegin();
33
34
         small.erase(prev(small.end()));
        big.insert(v);
35
36
         sums -= v;
         sumb += v;
37
38
       while (size_big() > n - n / 2) {
39
        int v = *big.begin();
40
         big.erase(big.begin());
41
         small.insert(v);
42
43
         sumb -= v;
         sums += v;
44
45
     }
47
     void add(int x) {
48
49
      n++;
50
       small.insert(x);
51
       sums += x;
       while (!small.empty() && *small.rbegin() > *big.
52
       begin()) {
        int v = *small.rbegin();
53
         small.erase(prev(small.end()));
54
55
        big.insert(v);
56
        sums -= v;
         sumb += v;
57
       }
58
       balance();
59
```

```
}
                                                                      this -> n = n:
60
                                                           33
                                                           34
                                                                       create();
61
    bool rem(int x) {
                                                                       create();
62
                                                           35
      n - - ;
63
                                                           36
      auto it1 = small.find(x);
                                                           37
      auto it2 = big.find(x);
                                                                  ftype f(ftype a, ftype b) {
65
                                                           38
      bool flag = false;
66
                                                           39
                                                                      return a + b;
      if (it1 != small.end()) {
67
                                                           40
        sums -= *it1;
68
                                                           41
        small.erase(it1);
                                                                  ftype create() {
                                                           42
         flag = true;
                                                                      seg.push_back(0);
70
                                                           43
71
      } else if (it2 != big.end()) {
                                                           44
                                                                       e.push_back(0);
         sumb -= *it2;
72
                                                           45
                                                                      d.push_back(0);
         big.erase(it2);
                                                                      return seg.size() - 1;
73
                                                           46
                                                                  7
74
         flag = true;
                                                           47
75
                                                           48
76
      balance();
                                                            49
                                                                   ftype query(int pos, int ini, int fim, int p, int
77
      return flag;
                                                                      if (q < ini || p > fim) return NEUTRAL;
                                                                      if (pos == 0) return 0;
79
                                                           51
    11 sum_small() {
                                                                       if (p <= ini && fim <= q) return seg[pos];</pre>
                                                           52
80
                                                                       int m = (ini + fim) >> 1;
      return sums;
81
                                                           53
                                                                       return f(query(e[pos], ini, m, p, q), query(d
82
                                                           54
                                                                   [pos], m + 1, fim, p, q));
    11 sum_big() {
84
                                                           55
      return sumb;
85
                                                           56
                                                                  void update(int pos, int ini, int fim, int id,
86
                                                           57
                                                                  int val) {
87
    int median() {
                                                                      if (ini > id || fim < id) {</pre>
                                                           58
      return *big.begin();
                                                                           return:
89
                                                           59
90
                                                           60
91 };
                                                           61
                                                                       if (ini == fim) {
                                                           62
        Dynamic Implicit Sparse
                                                                           seg[pos] = val;
                                                           64
1 // Description:
                                                                           return;
                                                                      }
2 // Indexed at one
                                                           66
                                                           67
                                                                      int m = (ini + fim) >> 1;
_{4} // When the indexes of the nodes are too big to be
                                                           69
      stored in an array
_{5} // and the queries need to be answered online so we
                                                                       if (id <= m) {
                                                                           if (e[pos] == 0) e[pos] = create();
      can't sort the nodes and compress them
                                                           71
                                                                           update(e[pos], ini, m, id, val);
_{6} // we create nodes only when they are needed so there ^{72}
                                                           73
                                                                       } else {
      'll be (Q*log(MAX)) nodes
                                                                           if (d[pos] == 0) d[pos] = create();
_{7} // where Q is the number of queries and MAX is the
                                                           74
                                                                           update(d[pos], m + 1, fim, id, val);
      maximum index a node can assume
                                                           76
9 // Query - get sum of elements from range (1, r)
                                                                       seg[pos] = f(seg[e[pos]], seg[d[pos]]);
      inclusive
                                                            78
_{
m 10} // Update - update element at position id to a value ^{
m 79}
                                                                   ftype query(int p, int q) {
                                                           81
                                                                      return query(1, 1, n, p, q);
12 // Problem:
13 // https://cses.fi/problemset/task/1648
                                                           83
                                                           84
                                                                  void update(int id, int val) {
                                                           85
15 // Complexity:
                                                                      update(1, 1, n, id, val);
                                                           86
16 // O(log n) for both query and update
                                                           87
18 // How to use:
                                                           88 }:
_{\rm 19} // MAX is the maximum index a node can assume
                                                                   Segtree2d
21 // Segtree seg = Segtree(MAX);
                                                            1 // Description:
23 typedef long long ftype;
                                                            2 // Indexed at zero
                                                            _{\rm 3} // Given a N x M grid, where i represents the row and
24
25 const int MAX = 1e9+17;
                                                                   j the column, perform the following operations
                                                            _4 // update(j, i) - update the value of grid[i][j]
                                                            5 // query(j1, j2, i1, i2) - return the sum of values
27 struct Segtree {
      vector<ftype> seg, d, e;
                                                                  inside the rectangle
      const ftype NEUTRAL = 0;
                                                            6 // defined by grid[i1][j1] and grid[i2][j2] inclusive
29
      int n;
                                                            8 // Problem:
31
      Segtree(int n) {
                                                            9 // https://cses.fi/problemset/task/1739/
32
```

```
updateY(noX, lX, rX, 2*noY+1,lY, m, y
10
11 // Complexity:
                                                                   );
12 // Time complexity:
                                                                            else if(m < v)
_{13} // O(log N * log M) for both query and update
                                                                                updateY(noX, 1X, rX, 2*noY+2, m+1, rY
                                                            79
_{14} // O(N * M) for build
                                                                    , y);
15 // Memory complexity:
                                                            80
16 // 4 * M * N
                                                            81
                                                                            seg[noX][noY] = seg[noX][2*noY+1] + seg[
17
                                                            82
18 // How to use:
                                                                   noX][2*noY+2];
19 // Segtree2D seg = Segtree2D(n, n);
                                                            83
                                                                        }
20 // vector < vector < int >> v(n, vector < int >(n));
                                                                   }
                                                            84
21 // seg.build(v);
                                                                   void updateX(int noX, int lX, int rX, int x, int
22
                                                            86
23 // Notes
_{24} // Indexed at zero
                                                                        int m = (1X+rX)/2:
                                                            87
25
                                                            88
26 struct Segtree2D {
                                                                        if(1X != rX){
      const int MAXN = 1025;
                                                                            if(x \le m){
27
                                                            90
      int N. M:
                                                                                updateX(2*noX+1, 1X, m, x, y);
29
                                                            92
                                                                            else if(m < x)
      vector < vector < int >> seg;
                                                                                updateX(2*noX+2, m+1, rX, x, y);
                                                            93
30
31
                                                            94
       Segtree2D(int N, int M) {
                                                                        }
32
                                                            95
           this ->N = N;
           this ->M = M;
                                                                        updateY(noX, 1X, rX, 0, 0, M - 1, y);
34
                                                            97
           seg.resize(2*MAXN, vector<int>(2*MAXN));
35
                                                            98
36
                                                            99
                                                                   int queryY(int noX, int noY, int lY, int rY, int
37
                                                            100
       void buildY(int noX, int 1X, int rX, int noY, int
                                                                   aY, int bY){
38
                                                                        if(aY <= 1Y && rY <= bY) return seg[noX][noY</pre>
       1Y, int rY, vector < vector < int >> &v) {
                                                            101
           if(1Y == rY){
39
               if(1X == rX){
40
                                                            102
                    seg[noX][noY] = v[rX][rY];
                                                                        int m = (1Y+rY)/2;
                                                            103
41
42
                    seg[noX][noY] = seg[2*noX+1][noY] +
                                                                        if(bY <= m) return queryY(noX, 2*noY+1, 1Y, m</pre>
43
                                                           105
       seg[2*noX+2][noY];
                                                                    , aY, bY);
               }
                                                                        if (m < aY) return queryY(noX, 2*noY+2, m+1,
44
                                                            106
           }else{
                                                                   rY, aY, bY);
45
               int m = (1Y+rY)/2;
46
                                                            107
                                                                        return queryY(noX, 2*noY+1, 1Y, m, aY, bY) +
47
                                                            108
               buildY(noX, 1X, rX, 2*noY+1, 1Y, m, v);
                                                                   queryY(noX, 2*noY+2, m+1, rY, aY, bY);
               buildY(noX, 1X, rX, 2*noY+2, m+1, rY, v);109
49
50
               seg[noX][noY] = seg[noX][2*noY+1] + seg[_{111}
                                                                   int queryX(int noX, int 1X, int rX, int aX, int
51
      noX][2*noY+2];
                                                                   bX, int aY, int bY){
          }
                                                                        if(aX <= 1X && rX <= bX) return queryY(noX,
52
      }
                                                                   0, 0, M - 1, aY, bY);
53
       void buildX(int noX, int 1X, int rX, vector<</pre>
                                                                        int m = (1X+rX)/2;
55
                                                            114
       vector <int>> &v){
                                                            115
          if(1X != rX){
                                                                        if(bX <= m) return queryX(2*noX+1, 1X, m, aX,</pre>
56
                                                            116
               int m = (1X+rX)/2;
                                                                    bX, aY, bY);
57
                                                                        if (m < aX) return queryX(2*noX+2, m+1, rX, aX
               buildX(2*noX+1, 1X, m, v);
                                                                    , bX, aY, bY);
59
               buildX(2*noX+2, m+1, rX, v);
60
                                                            118
                                                                        return queryX(2*noX+1, lX, m, aX, bX, aY, bY)
61
                                                            119
                                                                    + queryX(2*noX+2, m+1, rX, aX, bX, aY, bY);
62
           buildY(noX, 1X, rX, 0, 0, M - 1, v);
63
                                                            120
64
      }
                                                            121
                                                                   void build(vector<vector<int>> &v) {
65
                                                            122
      void updateY(int noX, int lX, int rX, int noY,
                                                                       buildX(0, 0, N - 1, v);
66
                                                            123
      int lY, int rY, int y){
                                                            124
           if(1Y == rY){
67
                                                            125
                                                                   int query(int aX, int bX, int aY, int bY) {
               if(1X == rX){
68
                                                            126
                    seg[noX][noY] = !seg[noX][noY];
                                                            127
                                                                        return queryX(0, 0, N - 1, aX, bX, aY, bY);
70
                                                            128
                    seg[noX][noY] = seg[2*noX+1][noY] +
                                                           129
71
      seg[2*noX+2][noY];
                                                                   void update(int x, int y) {
                                                            130
               }
                                                                        updateX(0, 0, N - 1, x, y);
72
                                                            131
           }else{
                                                            132
               int m = (1Y+rY)/2;
                                                            133 };
74
75
               if(y <= m){
76
```

```
9.7 Minimum And Amount
                                                                     if (ini == id && fim == id) {
                                                                          seg[pos] = mp(val, 1);
1 // Description:
                                                          67
_{2} // Query - get minimum element in a range (1, r)
                                                          68
      inclusive
                                                                          return;
_3 // and also the number of times it appears in that
                                                          70
                                                                     int e = 2*pos + 1:
_4 // Update - update element at position id to a value
                                                                     int d = 2*pos + 2;
      val
                                                           73
                                                                     int m = ini + (fim - ini) / 2;
                                                          74
6 // Problem:
                                                          75
7 // https://codeforces.com/edu/course/2/lesson/4/1/
                                                                      update(e, ini, m, id, val);
                                                                      update(d, m + 1, fim, id, val);
      practice/contest/273169/problem/C
                                                          77
                                                          78
                                                                     seg[pos] = f(seg[e], seg[d]);
9 // Complexity:
                                                          79
                                                          80
_{10} // O(log n) for both query and update
                                                          81
11
                                                                 void build(int pos, int ini, int fim, vector<int>
_{12} // How to use:
                                                          82
13 // Segtree seg = Segtree(n);
                                                                  &v) {
                                                                     if (ini == fim) {
14 // seg.build(v);
                                                          83
                                                                          if (ini < (int)v.size()) {</pre>
                                                          84
                                                                              seg[pos] = mp(v[ini], 1);
16 #define pii pair<int, int>
                                                          85
17 #define mp make_pair
                                                          86
                                                                          return;
18 #define ff first
                                                          87
                                                                     }
                                                          88
19 #define ss second
                                                          89
                                                                     int e = 2*pos + 1;
21 const int INF = 1e9+17;
                                                          90
                                                                      int d = 2*pos + 2;
                                                          91
                                                                     int m = ini + (fim - ini) / 2;
23 typedef pii ftype;
                                                          92
                                                          93
                                                          94
                                                                      build(e, ini, m, v);
25 struct Segtree {
                                                                     build(d, m + 1, fim, v);
      vector<ftype> seg;
                                                          95
26
                                                          96
      int n;
27
      const ftype NEUTRAL = mp(INF, 0);
                                                          97
                                                                      seg[pos] = f(seg[e], seg[d]);
28
                                                          98
      Segtree(int n) {
30
                                                                 ftype query(int p, int q) {
          int sz = 1;
                                                          100
31
          while (sz < n) sz *= 2;
                                                          101
                                                                     return query (0, 0, n - 1, p, q);
32
                                                          102
          this ->n = sz;
33
                                                          103
                                                                 void update(int id, int val) {
                                                          104
          seg.assign(2*sz, NEUTRAL);
35
                                                                     update(0, 0, n - 1, id, val);
                                                          105
                                                          106
37
                                                          107
      ftype f(ftype a, ftype b) {
38
                                                                 void build(vector<int> &v) {
                                                          108
39
          if (a.ff < b.ff) return a;
                                                          109
                                                                     build(0, 0, n - 1, v);
          if (b.ff < a.ff) return b;
40
                                                          110
          return mp(a.ff, a.ss + b.ss);
42
                                                                 void debug() {
43
                                                          112
                                                                     for (auto e : seg) {
                                                          113
44
                                                                          cout << e.ff << ' ' << e.ss << '\n';</pre>
      ftype query(int pos, int ini, int fim, int p, int114
45
                                                         115
                                                                      cout << '\n';</pre>
          if (ini >= p && fim <= q) {
46
                                                          117
              return seg[pos];
                                                          118 };
          }
48
49
                                                                  Lazy Addition To Segment
           if (q < ini || p > fim) {
              return NEUTRAL;
51
          }
                                                           1 // Description:
53
                                                           2 // Query - get sum of elements from range (1, r)
           int e = 2*pos + 1;
                                                                 inclusive
54
           int d = 2*pos + 2;
                                                           _{\rm 3} // Update - add a value val to elementos from range (
          int m = ini + (fim - ini) / 2;
                                                                 l, r) inclusive
56
          return f(query(e, ini, m, p, q), query(d, m + 5 // Problem:
58
                                                           6 // https://codeforces.com/edu/course/2/lesson/5/1/
       1, fim, p, q));
59
                                                                 practice/contest/279634/problem/A
60
                                                           8 // Complexity:
      void update(int pos, int ini, int fim, int id,
      int val) {
                                                           9 // O(log n) for both query and update
          if (ini > id || fim < id) {
                                                           11 // How to use:
63
               return;
                                                           12 // Segtree seg = Segtree(n);
64
```

65

```
return f(query(e, ini, m, p, q), query(d, m +
13 // seg.build(v);
                                                            81
                                                                   1, fim, p, q));
15 // Notes
                                                            82
16 // Change neutral element and f function to perform a 83
       different operation
                                                                   void update(int pos, int ini, int fim, int p, int
                                                                   q, int val) {
17
                                                                       propagate(pos, ini, fim);
18 const long long INF = 1e18+10;
19
                                                            86
20 typedef long long ftype;
                                                                       if (ini > q || fim < p) {
                                                            87
                                                                           return;
                                                            88
22 struct Segtree {
                                                            89
      vector<ftype> seg;
                                                            90
       vector<ftype> lazy;
                                                                       if (ini >= p && fim <= q) {
24
                                                            91
                                                                           lazy[pos] = apply_lazy(lazy[pos], val, 1)
       int n;
25
       const ftype NEUTRAL = 0;
26
       const ftype NEUTRAL_LAZY = -1; // change to -INF 93
                                                                           seg[pos] = apply_lazy(seg[pos], val, fim
27
       if there are negative numbers
                                                                   - ini + 1);
28
       Segtree(int n) {
                                                                           return;
                                                                       }
           int sz = 1;
30
                                                            96
           while (sz < n) sz *= 2;
                                                            97
31
                                                                       int e = 2*pos + 1;
           this->n = sz;
32
                                                            98
                                                                       int d = 2*pos + 2;
33
                                                           99
           seg.assign(2*sz, NEUTRAL);
                                                                       int m = ini + (fim - ini) / 2;
           lazy.assign(2*sz, NEUTRAL_LAZY);
35
                                                           101
       }
                                                                       update(e, ini, m, p, q, val);
36
                                                           102
                                                                       update(d, m + 1, fim, p, q, val);
37
                                                           103
       ftype apply_lazy(ftype a, ftype b, int len) {
38
                                                           104
           if (b == NEUTRAL_LAZY) return a;
                                                                       seg[pos] = f(seg[e], seg[d]);
39
                                                           105
           if (a == NEUTRAL_LAZY) return b * len;
                                                                   }
40
                                                           106
           else return a + b * len;
41
                                                           107
                                                                   void build(int pos, int ini, int fim, vector<int>
42
                                                           108
                                                                    &v) {
43
44
       void propagate(int pos, int ini, int fim) {
                                                           109
                                                                       if (ini == fim) {
           if (ini == fim) {
                                                                           if (ini < (int)v.size()) {</pre>
45
                                                           110
               return;
                                                                                seg[pos] = v[ini];
                                                           111
           }
47
                                                           112
                                                           113
                                                                           return;
48
           int e = 2*pos + 1;
                                                                       }
49
                                                           114
           int d = 2*pos + 2;
50
                                                           115
                                                                       int e = 2*pos + 1;
51
           int m = ini + (fim - ini) / 2;
                                                           116
                                                                       int d = 2*pos + 2;
52
                                                           117
           lazy[e] = apply_lazy(lazy[e], lazy[pos], 1); 118
                                                                       int m = ini + (fim - ini) / 2;
53
54
           lazy[d] = apply_lazy(lazy[d], lazy[pos], 1); 119
                                                                       build(e, ini, m, v);
55
           seg[e] = apply_lazy(seg[e], lazy[pos], m -
                                                                       build(d, m + 1, fim, v);
56
                                                           121
       ini + 1):
           seg[d] = apply_lazy(seg[d], lazy[pos], fim - 123
                                                                       seg[pos] = f(seg[e], seg[d]);
                                                                   }
      m):
                                                           124
58
                                                           125
           lazy[pos] = NEUTRAL_LAZY;
                                                                   ftype query(int p, int q) {
59
                                                           126
                                                                       return query(0, 0, n - 1, p, q);
60
                                                           127
                                                           128
       ftype f(ftype a, ftype b) {
62
                                                           129
                                                                   void update(int p, int q, int val) {
           return a + b;
                                                           130
63
                                                                       update(0, 0, n - 1, p, q, val);
64
                                                           131
65
                                                           132
       ftype query(int pos, int ini, int fim, int p, int133
66
                                                                   void build(vector<int> &v) {
       a) {
                                                           134
           propagate(pos, ini, fim);
                                                                       build(0, 0, n - 1, v);
67
                                                           135
                                                           136
68
           if (ini >= p && fim <= q) {
                                                           137
69
               return seg[pos];
                                                                   void debug() {
70
                                                           138
           }
                                                                       for (auto e : seg) {
71
                                                           139
                                                                            cout << e << ' ';
           if (q < ini || p > fim) {
                                                                       }
73
                                                           141
                                                                       cout << '\n';
               return NEUTRAL;
74
                                                           142
           }
                                                                       for (auto e : lazy) {
75
                                                           143
                                                                           cout << e << ' ';
76
                                                           144
           int e = 2*pos + 1;
                                                                       }
                                                           145
           int d = 2*pos + 2;
                                                                       cout << '\n';
78
                                                           146
           int m = ini + (fim - ini) / 2;
                                                                       cout << '\n';
                                                           147
80
                                                           148
                                                                   }
```

149 }; 61 62 Segment With Maximum Sum 9.9ftype query(int pos, int ini, int fim, int p, int 63 1 // Description: if (ini >= p && fim <= q) { return seg[pos]; 2 // Query - get sum of segment that is maximum among 65 all segments 3 // E.g 67 if (q < ini || p > fim) { 4 // Array: 5 -4 4 3 -5 68 return NEUTRAL; $_{5}$ // Maximum segment sum: 8 because 5 + (-4) + 4 = 8 $_{\rm 6}$ // Update - update element at position id to a value $^{\rm 70}$ val int e = 2*pos + 1;72 8 // Problem: int d = 2*pos + 2;73 int m = ini + (fim - ini) / 2; 9 // https://codeforces.com/edu/course/2/lesson/4/2/ 74 75 practice/contest/273278/problem/A return f(query(e, ini, m, p, q), query(d, m + 10 1, fim, p, q)); 11 // Complexity: $_{12}$ // O(log n) for both query and update 77 78 void update(int pos, int ini, int fim, int id, 14 // How to use: 79 int val) { 15 // Segtree seg = Segtree(n); if (ini > id || fim < id) { 16 // seg.build(v); 80 return; 82 19 // The maximum segment sum can be a negative number 83 if (ini == id && fim == id) { 20 // In that case, taking zero elements is the best 84 seg[pos] = Node(val, val, val, val); choice 85 $_{ m 21}$ // So we need to take the maximum between 0 and the return: 87 } 88 22 // max(OLL, seg.query(0, n).max_seg) 89 int e = 2*pos + 1;90 24 using ll = long long; 91 int d = 2*pos + 2;int m = ini + (fim - ini) / 2; 26 typedef ll ftype_node; 92 27 update(e, ini, m, id, val); 28 struct Node { 94 update(d, m + 1, fim, id, val); 95 29 ftype_node max_seg; 96 ftype_node pref; 30 seg[pos] = f(seg[e], seg[d]); 97 ftype_node suf; 98 ftype_node sum; 32 99 void build(int pos, int ini, int fim, vector<int> 34 Node(ftype_node max_seg, ftype_node pref, ftype_node suf, ftype_node sum) : max_seg(max_seg &v) { if (ini == fim) {), pref(pref), suf(suf), sum(sum) {}; // se a çãposio existir no array original 35 }; // seg tamanho potencia de dois 103 if (ini < (int)v.size()) {</pre> 37 typedef Node ftype; seg[pos] = Node(v[ini], v[ini], v[ini 38], v[ini]); 39 struct Segtree { } vector<ftype> seg; 106 40 int n; 107 return: 41 } const ftype NEUTRAL = Node(0, 0, 0, 0); 42 109 43 int e = 2*pos + 1;Segtree(int n) { 110 44 int d = 2*pos + 2;111 int sz = 1; 45 int m = ini + (fim - ini) / 2; 112 // potencia de dois mais proxima 46 while (sz < n) sz *= 2;113 47 build(e, ini, m, v); this->n = sz; 114 build(d, m + 1, fim, v); 115 49 // numero de nos da seg 116 50 seg[pos] = f(seg[e], seg[d]); 117 seg.assign(2*sz, NEUTRAL); 51 } 118 52 53 119 ftype query(int p, int q) { ftype f(ftype a, ftype b) { 54 return query(0, 0, n - 1, p, q); ftype_node max_seg = max({a.max_seg, b. 121 max_seg, a.suf + b.pref}); 122 ftype_node pref = max(a.pref, a.sum + b.pref)123 56 void update(int id, int val) { 124 ftype_node suf = max(b.suf, b.sum + a.suf); update(0, 0, n - 1, id, val); 125 57 ftype_node sum = a.sum + b.sum; 126 59 128 void build(vector<int> &v) { return Node(max_seg, pref, suf, sum); 60

```
build(0, 0, n - 1, v);
                                                                       int d = 2*pos + 2;
129
                                                            53
130
                                                            54
                                                                       int m = ini + (fim - ini) / 2;
131
                                                            55
       void debug() {
                                                                       return f(query(e, ini, m, p, q), query(d, m +
132
                                                            56
           for (auto e : seg) {
                                                                    1, fim, p, q));
               cout << e.max_seg << ', ' << e.pref << ', '57</pre>
134
        << e.suf << ' ' << e.sum << '\n';
                                                            58
                                                                   void update(int pos, int ini, int fim, int id,
135
                                                            59
           cout << '\n';</pre>
                                                                   int val) {
136
                                                                       if (ini > id || fim < id) {</pre>
137
                                                            60
138 };
                                                                           return;
                                                            61
           Range Query Point Update
                                                            63
                                                                       if (ini == id && fim == id) {
 1 // Description:
                                                            65
                                                                            seg[pos] = val;
                                                            66
 _{2} // Indexed at zero
 3 // Query - get sum of elements from range (1, r)
                                                                            return;
       inclusive
 _4 // Update - update element at position id to a value ^{69}
                                                                       int e = 2*pos + 1;
                                                                       int d = 2*pos + 2;
                                                            71
 6 // Problem:
                                                                       int m = ini + (fim - ini) / 2;
                                                            72
 7 // https://codeforces.com/edu/course/2/lesson/4/1/
                                                            73
       practice/contest/273169/problem/B
                                                                       update(e, ini, m, id, val);
                                                                       update(d, m + 1, fim, id, val);
                                                            75
 9 // Complexity:
                                                            76
                                                                       seg[pos] = f(seg[e], seg[d]);
10 // O(\log n) for both query and update
                                                            77
                                                            78
12 // How to use:
                                                            79
                                                                   void build(int pos, int ini, int fim, vector<int>
13 // Segtree seg = Segtree(n);
                                                            80
                                                                    &v) {
14 // seg.build(v);
                                                                       if (ini == fim) {
                                                            81
                                                                           if (ini < (int)v.size()) {</pre>
16 // Notes
                                                            82
_{
m 17} // Change neutral element and f function to perform a ^{
m 83}
                                                                                seg[pos] = v[ini];
                                                                           }
       different operation
                                                                            return;
                                                                       }
19 // If you want to change the operations to point
                                                            86
       query and range update
                                                            87
                                                                       int e = 2*pos + 1;
20 // Use the same segtree, but perform the following
                                                                       int d = 2*pos + 2;
       operations
                                                            89
21 // Query - seg.query(0, id);
                                                                       int m = ini + (fim - ini) / 2;
22 // Update - seg.update(1, v); seg.update(r + 1, -v);
                                                            91
                                                                       build(e, ini, m, v);
24 typedef long long ftype;
                                                            93
                                                                       build(d, m + 1, fim, v);
                                                            94
25
                                                            95
                                                                       seg[pos] = f(seg[e], seg[d]);
26 struct Segtree {
       vector <ftype > seg;
27
                                                            96
       int n;
28
                                                                   ftype query(int p, int q) {
       const ftype NEUTRAL = 0;
                                                            98
                                                            99
                                                                       return query(0, 0, n - 1, p, q);
30
                                                           100
       Segtree(int n) {
31
           int sz = 1;
                                                           101
           while (sz < n) sz *= 2;
                                                                   void update(int id, int val) {
                                                           102
33
                                                                       update(0, 0, n - 1, id, val);
           this ->n = sz;
                                                           103
                                                           104
35
                                                           105
           seg.assign(2*sz, NEUTRAL);
36
                                                                   void build(vector<int> &v) {
       }
                                                           106
37
                                                                       build(0, 0, n - 1, v);
                                                           107
38
       ftype f(ftype a, ftype b) {
                                                           108
                                                                   }
                                                           109
40
           return a + b;
                                                                   void debug() {
                                                           110
41
                                                                       for (auto e : seg) {
                                                           111
42
                                                                            cout << e << ' ';
       ftype query(int pos, int ini, int fim, int p, int112
43
                                                                       cout << '\n';</pre>
           if (ini >= p && fim <= q) {
44
                                                                   }
                return seg[pos];
                                                           115
45
                                                           116 };
46
47
                                                                       Lazy Assignment To Segment
                                                               9.11
            if (q < ini || p > fim) {
                return NEUTRAL;
49
                                                             const long long INF = 1e18+10;
51
           int e = 2*pos + 1;
                                                             3 typedef long long ftype;
52
```

```
71
5 struct Segtree {
                                                           72
                                                                      if (ini > q || fim < p) {
      vector<ftype> seg;
                                                           73
                                                                          return;
      vector<ftype> lazy;
                                                           74
      int n;
      const ftype NEUTRAL = 0;
                                                                      if (ini >= p && fim <= q) {</pre>
9
                                                           76
      const ftype NEUTRAL_LAZY = -1; // Change to -INF
                                                                           lazy[pos] = apply_lazy(lazy[pos], val, 1)
10
      if there are negative numbers
                                                                          seg[pos] = apply_lazy(seg[pos], val, fim
11
      Segtree(int n) {
                                                                  - ini + 1);
12
          int sz = 1:
13
                                                           79
           // potencia de dois mais proxima
                                                                          return;
                                                                      }
15
           while (sz < n) sz *= 2;
                                                           81
          this ->n = sz;
16
                                                           82
                                                                      int e = 2*pos + 1;
17
                                                           83
                                                                      int d = 2*pos + 2;
           // numero de nos da seg
18
                                                           84
19
           seg.assign(2*sz, NEUTRAL);
                                                                      int m = ini + (fim - ini) / 2;
           lazy.assign(2*sz, NEUTRAL_LAZY);
20
                                                           86
                                                                      update(e, ini, m, p, q, val);
                                                                      update(d, m + 1, fim, p, q, val);
22
                                                           88
      ftype apply_lazy(ftype a, ftype b, int len) {
23
                                                           89
           if (b == NEUTRAL_LAZY) return a;
                                                                      seg[pos] = f(seg[e], seg[d]);
24
                                                           90
           if (a == NEUTRAL_LAZY) return b * len;
25
                                                           91
           else return b * len;
                                                           92
                                                                  void build(int pos, int ini, int fim, vector<int>
27
                                                           93
                                                                   &v) {
28
      void propagate(int pos, int ini, int fim) {
                                                                      if (ini == fim) {
29
          if (ini == fim) {
                                                                          // se a çãposio existir no array original
30
                                                           95
               return;
                                                                           // seg tamanho potencia de dois
31
                                                           96
          }
                                                                          if (ini < (int)v.size()) {</pre>
32
                                                           97
                                                           98
                                                                              seg[pos] = v[ini];
33
          int e = 2*pos + 1;
34
                                                           99
          int d = 2*pos + 2;
                                                                          return;
                                                          100
35
          int m = ini + (fim - ini) / 2;
                                                                      }
37
                                                          102
           lazy[e] = apply_lazy(lazy[e], lazy[pos], 1); 103
                                                                      int e = 2*pos + 1;
          lazy[d] = apply_lazy(lazy[d], lazy[pos], 1); 104
                                                                      int d = 2*pos + 2;
39
                                                                      int m = ini + (fim - ini) / 2;
40
          seg[e] = apply_lazy(seg[e], lazy[pos], m -
41
                                                                      build(e, ini, m, v);
      ini + 1);
                                                          107
                                                                      build(d, m + 1, fim, v);
42
           seg[d] = apply_lazy(seg[d], lazy[pos], fim - 108
      m):
                                                          109
                                                                      seg[pos] = f(seg[e], seg[d]);
43
                                                          110
44
           lazy[pos] = NEUTRAL_LAZY;
                                                          111
                                                                  7
                                                          112
45
                                                          113
                                                                  ftype query(int p, int q) {
46
      ftype f(ftype a, ftype b) {
                                                                      return query(0, 0, n - 1, p, q);
47
                                                          114
          return a + b;
49
                                                          116
                                                                  void update(int p, int q, int val) {
50
                                                          117
      ftype query(int pos, int ini, int fim, int p, int118
                                                                      update(0, 0, n - 1, p, q, val);
51
                                                          119
          propagate(pos, ini, fim);
52
                                                                  void build(vector<int> &v) {
53
                                                          121
           if (ini >= p && fim <= q) {
                                                          122
                                                                      build(0, 0, n - 1, v);
54
55
               return seg[pos];
                                                          123
                                                          124
56
                                                                  void debug() {
                                                          125
          if (q < ini || p > fim) {
58
                                                          126
                                                                      for (auto e : seg) {
               return NEUTRAL;
                                                                          cout << e << '';
                                                          127
59
          }
                                                                      }
60
                                                          128
                                                                      cout << '\n';
                                                          129
61
          int e = 2*pos + 1;
                                                                      for (auto e : lazy) {
                                                          130
          int d = 2*pos + 2;
                                                                          cout << e << ' ':
63
                                                          131
           int m = ini + (fim - ini) / 2;
                                                                      cout << '\n':
65
          return f(query(e, ini, m, p, q), query(d, m +134
                                                                      cout << '\n';
66
       1, fim, p, q));
                                                                  }
                                                          136 }:
67
                                                                     Lazy Dynamic Implicit Sparse
      void update(int pos, int ini, int fim, int p, int 9.12
69
       q, int val) {
70
          propagate(pos, ini, fim);
                                                            1 // Description:
```

```
2 // Indexed at one
                                                                  pos], fim - m);
                                                           64
_{\rm 4} // When the indexes of the nodes are too big to be
                                                                      lazy[pos] = NEUTRAL_LAZY;
                                                           65
      stored in an array
                                                           66
_{5} // and the queries need to be answered online so we
      can't sort the nodes and compress them
                                                                  ftype f(ftype a, ftype b) {
                                                           68
_{6} // we create nodes only when they are needed so there _{69}
                                                                      return a + b;
      'll be (Q*log(MAX)) nodes
                                                           70
_{7} // where Q is the number of queries and MAX is the
                                                           71
      maximum index a node can assume
                                                                  ftype create() {
                                                           72
                                                                      seg.push_back(0);
                                                           73
9 // Query - get sum of elements from range (1, r)
                                                           74
                                                                      e.push_back(0);
                                                                      d.push_back(0);
      inclusive
                                                           75
_{10} // Update - update element at position id to a value _{76}
                                                                      lazy.push_back(-1);
      val
                                                           77
                                                                      return seg.size() - 1;
11
                                                           78
12 // Problem:
13 // https://oj.uz/problem/view/IZhO12_apple
                                                                  ftype query(int pos, int ini, int fim, int p, int
                                                           80
                                                                   q) {
15 // Complexity:
                                                                      propagate(pos, ini, fim);
                                                           81
_{16} // O(log n) for both query and update
                                                                      if (q < ini || p > fim) return NEUTRAL;
                                                           82
                                                                      if (pos == 0) return 0;
18 // How to use:
                                                                      if (p <= ini && fim <= q) return seg[pos];</pre>
                                                           84
_{
m 19} // MAX is the maximum index a node can assume
                                                                      int m = (ini + fim) >> 1;
20 // Create a default null node
                                                                      return f(query(e[pos], ini, m, p, q), query(d
                                                           86
                                                                  [pos], m + 1, fim, p, q));
21 // Create a node to be the root of the segtree
                                                           87
23 // Segtree seg = Segtree(MAX);
                                                           88
                                                                  void update(int pos, int ini, int fim, int p, int
                                                           89
25 const int MAX = 1e9+10;
                                                                   q, int val) {
26 const long long INF = 1e18+10;
                                                                      propagate(pos, ini, fim);
                                                           90
                                                                      if (ini > q || fim < p) {
                                                           91
28 typedef long long ftype;
                                                                          return;
                                                           92
29
30 struct Segtree {
                                                           94
      vector<ftype> seg, d, e, lazy;
                                                                      if (ini >= p && fim <= q) {
31
      const ftype NEUTRAL = 0;
                                                                          lazy[pos] = apply_lazy(lazy[pos], val, 1)
32
      const ftype NEUTRAL_LAZY = -1; // change to -INF
33
      if the elements can be negative
                                                                          seg[pos] = apply_lazy(seg[pos], val, fim
                                                                  - ini + 1);
      int n:
34
35
      Segtree(int n) {
36
                                                           99
                                                                          return;
          this ->n = n;
37
                                                          100
           create();
                                                          101
38
           create();
                                                                      int m = (ini + fim) >> 1;
                                                          102
39
      }
40
                                                          103
                                                                      if (e[pos] == 0) e[pos] = create();
41
                                                          104
      ftype apply_lazy(ftype a, ftype b, int len) {
                                                                      update(e[pos], ini, m, p, q, val);
           if (b == NEUTRAL_LAZY) return a;
43
                                                          106
           else return b * len; // change to a + b * len107
                                                                      if (d[pos] == 0) d[pos] = create();
44
       to add to an element instead of updating it
                                                                      update(d[pos], m + 1, fim, p, q, val);
45
                                                          109
                                                                      seg[pos] = f(seg[e[pos]], seg[d[pos]]);
      void propagate(int pos, int ini, int fim) {
47
                                                          111
          if (seg[pos] == 0) return;
48
                                                          112
                                                                  ftype query(int p, int q) {
                                                          113
49
           if (ini == fim) {
                                                                      return query(1, 1, n, p, q);
                                                          114
50
               return;
                                                          115
52
          }
                                                          116
                                                                  void update(int p, int q, int val) {
                                                          117
53
          int m = (ini + fim) >> 1;
                                                          118
                                                                      update(1, 1, n, p, q, val);
54
                                                          119
55
           if (e[pos] == 0) e[pos] = create();
                                                          120 };
          if (d[pos] == 0) d[pos] = create();
57
                                                             9.13
                                                                     Persistent
          lazy[e[pos]] = apply_lazy(lazy[e[pos]], lazy[
59
      pos], 1);
                                                            _{1} // Description:
          lazy[d[pos]] = apply_lazy(lazy[d[pos]], lazy[ 2 // Persistent segtree allows for you to save the
60
      pos], 1);
                                                                  different versions of the segtree between each
                                                                  update
           seg[e[pos]] = apply_lazy(seg[e[pos]], lazy[
                                                            3 // Indexed at one
62
      pos], m - ini + 1);
                                                            _{\rm 4} // Query - get sum of elements from range (1, r)
63
           seg[d[pos]] = apply_lazy(seg[d[pos]], lazy[
                                                                  inclusive
```

```
5 // Update - update element at position id to a value 46
                                                                 ftype query(int pos, int ini, int fim, int p, int
                                                           48
7 // Problem:
8 // https://cses.fi/problemset/task/1737/
                                                           49
                                                                     if (q < ini || p > fim) return NEUTRAL;
                                                                     if (pos == 0) return 0;
                                                          50
                                                                      if (p <= ini && fim <= q) return seg[pos];</pre>
10 // Complexity:
                                                           51
                                                                     int m = (ini + fim) >> 1;
_{11} // O(log n) for both query and update
                                                          52
                                                                     return f(query(e[pos], ini, m, p, q), query(d
                                                          53
_{13} // How to use:
                                                                 [pos], m + 1, fim, p, q));
_{14} // vector<int> raiz(MAX); // vector to store the
                                                          54
      roots of each version
15 // Segtree seg = Segtree(INF);
                                                                 int update(int pos, int ini, int fim, int id, int
                                                          56
16 // raiz[0] = seg.create(); // null node
                                                                  val) {
_{17} // curr = 1; // keep track of the last version
                                                                     int novo = create();
                                                          57
                                                          58
19 // raiz[k] = seg.update(raiz[k], idx, val); //
                                                                      seg[novo] = seg[pos];
                                                                     e[novo] = e[pos];
      updating version k
                                                          60
20 // seg.query(raiz[k], l, r) // querying version k
                                                                     d[novo] = d[pos];
_{21} // raiz[++curr] = raiz[k]; // create a new version
                                                          62
      based on version k
                                                                      if (ini == fim) {
                                                          63
                                                                          seg[novo] = val;
                                                           64
23 const int MAX = 2e5+17;
                                                          65
                                                                          return novo;
                                                                      }
24 const int INF = 1e9+17;
                                                          66
25
                                                          67
26 typedef long long ftype;
                                                          68
                                                                      int m = (ini + fim) >> 1;
27
                                                          69
28 struct Segtree {
                                                                      if (id <= m) e[novo] = update(e[novo], ini, m</pre>
                                                           70
      vector<ftype> seg, d, e;
                                                                  , id, val);
      const ftype NEUTRAL = 0;
                                                                     else d[novo] = update(d[novo], m + 1, fim, id
30
                                                           71
                                                                  , val);
31
      int n;
32
                                                           72
      Segtree(int n) {
                                                                      seg[novo] = f(seg[e[novo]], seg[d[novo]]);
                                                           73
33
          this -> n = n;
                                                           74
                                                                      return novo:
                                                          75
35
                                                           76
      ftype f(ftype a, ftype b) {
37
                                                          77
                                                                 ftype query(int pos, int p, int q) {
          return a + b;
                                                          78
38
      7
39
                                                          79
                                                                      return query(pos, 1, n, p, q);
                                                          80
40
41
      ftype create() {
                                                           81
          seg.push_back(0);
                                                                 int update(int pos, int id, int val) {
42
                                                          82
          e.push_back(0);
                                                                      return update(pos, 1, n, id, val);
                                                          83
43
44
          d.push_back(0);
                                                          84
          return seg.size() - 1;
                                                          85 };
45
```