

Notebook - Maratona de Programação

Lenhadoras de Segtree

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1 DP

1.1 Substr Palindrome

```
1 // êvoc deve informar se a substring de S formada
      pelos elementos entre os indices i e j
2 // é um palindromo ou ãno.
4 char s[MAX];
5 int calculado [MAX] [MAX]; // inciado com false, ou 0
6 int tabela[MAX][MAX];
8 int is_palin(int i, int j){
   if(calculado[i][j]){
      return tabela[i][j];
10
11
    if(i == j) return true;
12
    if(i + 1 == j) return s[i] == s[j];
14
    int ans = false;
15
    if(s[i] == s[j]){
16
     if(is_palin(i+1, j-1)){
17
        ans = true;
19
20
    calculado[i][j] = true;
21
   tabela[i][j] = ans;
   return ans;
24 }
```

1.2 Coins

```
int tb[1005];
int n;
vector<int> moedas;

int dp(int i){
   if(i >= n)
      return 0;
   if(tb[i] != -1)
      return tb[i];

tb[i] = max(dp(i+1), dp(i+2) + moedas[i]);
   return tb[i];

int main(){
   memset(tb,-1,sizeof(tb));
}
```

1.3 Minimum Coin Change

```
1 int n;
vector < int > valores;
4 int tabela[1005];
6 int dp(int k){
    if(k == 0){
     return 0;
9
   if(tabela[k] != -1)
     return tabela[k];
1.1
    int melhor = 1e9;
    for(int i = 0; i < n; i++){
13
     if(valores[i] <= k)</pre>
14
        melhor = min(melhor,1 + dp(k - valores[i]));
16
    return tabela[k] = melhor;
18 }
```

1.4 Edit Distance

```
1 // Description:
 2 // Minimum number of operations required to transform
       a string into another
 3 // Operations allowed: add character, remove
      character, replace character
 5 // Parameters:
 6 // str1 - string to be transformed into str2
 7 // str2 - string that str1 will be transformed into
 _{8} // m - size of str1
 _{9} // n - size of str2
11 // Problem:
12 // https://cses.fi/problemset/task/1639
14 // Complexity:
15 // O(m x n)
17 // How to use:
18 // memset(dp, -1, sizeof(dp));
19 // string a, b;
20 // edit_distance(a, b, (int)a.size(), (int)b.size());
22 // Notes:
23 // Size of dp matriz is m x n
25 int dp[MAX][MAX];
26
27 int edit_distance(string &str1, string &str2, int m,
      int n) {
      if (m == 0) return n;
      if (n == 0) return m;
29
       if (dp[m][n] != -1) return dp[m][n];
3.1
32
       if (str1[m - 1] == str2[n - 1]) return dp[m][n] =
33
       edit_distance(str1, str2, m - 1, n - 1);
return dp[m][n] = 1 + min({edit_distance(str1,
       str2, m, n - 1), edit_distance(str1, str2, m - 1,
       n), edit_distance(str1, str2, m - 1, n - 1)});
35 }
  1.5 Digits
1 // achar a quantidade de numeros menores que R que
      possuem no maximo 3 digitos nao nulos
2 // a ideia eh utilizar da ordem lexicografica para
      checar isso pois se temos por exemplo
3 // o numero 8500, a gente sabe que se pegarmos o
      numero 7... qualquer digito depois do 7
4 // sera necessariamente menor q 8500
6 string r;
7 int tab [20] [2] [5];
9 // i - digito de R
_{\rm 10} // menor - ja pegou um numero menor que um digito de
_{\rm 11} // qt - quantidade de digitos nao nulos
12 int dp(int i, bool menor, int qt){
      if(qt > 3) return 0;
       if(i >= r.size()) return 1;
14
       if(tab[i][menor][qt] != -1) return tab[i][menor][
       qt];
      int dr = r[i]-'0';
17
      int res = 0;
18
```

for(int d = 0; d <= 9; d++) {

int dnn = qt + (d > 0);

20

```
if (i == n-1) {
          if(menor == true) {
22
                                                           8
23
              res += dp(i+1, true, dnn);
                                                           9
                                                                     if (!mult) return arr[n-1]*x;
                                                                     return arr[n-1];
24
                                                          10
          else if(d < dr) {</pre>
                                                          11
               res += dp(i+1, true, dnn);
                                                          12
                                                                 if (tab[i][mult] != -1) return tab[i][mult];
          }
27
                                                          13
           else if(d == dr) {
                                                          14
              res += dp(i+1, false, dnn);
29
                                                          1.5
                                                                 if (mult) {
30
                                                          16
      }
                                                          17
                                                                     res = max(arr[i], arr[i] + dp(i+1, 1));
31
32
                                                          18
33
      return tab[i][menor][qt] = res;
                                                          19
                                                                 else {
34 }
                                                                     res = max({
                                                          20
                                                                         arr[i]*x,
                                                          21
        Knapsack With Index
                                                                         arr[i]*x + dp(i+1, 1),
                                                          22
                                                                         arr[i] + dp(i+1, 0)
                                                          23
                                                                     });
void knapsack(int W, int wt[], int val[], int n) {
                                                          2.5
      int i, w;
      int K[n + 1][W + 1];
                                                                 return tab[i][mult] = res;
                                                          27
                                                          28 }
      for (i = 0; i <= n; i++) {
                                                          29
           for (w = 0; w \le W; w++) {
                                                          30 int main() {
               if (i == 0 | | w == 0)
                                                          31
                  K[i][w] = 0;
                                                                 memset(tab, -1, sizeof(tab));
                                                          32
               else if (wt[i - 1] <= w)
                                                          33
10
                  K[i][w] = max(val[i - 1] +
                                                          34
                                                                 int ans = -oo;
                       K[i - 1][w - wt[i - 1]], K[i -
11
                                                                 for (int i = 0; i < n; i++) {
                                                          35
      17[w]):
                                                          36
                                                                     ans = max(ans, dp(i, 0));
                                                          3.7
                   K[i][w] = K[i - 1][w];
13
                                                          38
          }
14
                                                                 return 0:
                                                          39
      }
15
                                                          40 }
16
                                                          41
      int res = K[n][W];
                                                          42
      cout << res << endl;</pre>
18
19
                                                          44 int ans = a[0], ans_1 = 0, ans_r = 0;
      w = W;
20
                                                          45 int sum = 0, minus_pos = -1;
      for (i = n; i > 0 && res > 0; i--) {
21
                                                          46
          if (res == K[i - 1][w])
                                                          47 for (int r = 0; r < n; ++r) {
               continue;
23
                                                          48
                                                                 sum += a[r];
           else {
                                                                 if (sum > ans) {
                                                          49
              cout << " " << wt[i - 1];
25
                                                                     ans = sum;
                                                          50
               res = res - val[i - 1];
                                                          5.1
                                                                     ans_l = minus_pos + 1;
               w = w - wt[i - 1];
27
                                                          52
                                                                     ans_r = r;
          }
28
                                                          53
                                                                 }
      }
29
                                                                 if (sum < 0) {
                                                          54
30 }
                                                          55
                                                                     sum = 0;
                                                          56
                                                                     minus_pos = r;
32 int main()
                                                          57
33 {
                                                          58 }
34
      int val[] = { 60, 100, 120 };
      int wt[] = { 10, 20, 30 };
35
      int W = 50;
                                                                   Knapsack
                                                             1.8
      int n = sizeof(val) / sizeof(val[0]);
37
      knapsack(W, wt, val, n);
39
                                                           int val[MAXN], peso[MAXN], dp[MAXN][MAXS];
40
      return 0;
                                                           3 int knapsack(int n, int m){ // n Objetos | Peso max
42 }
                                                                 for(int i=0;i<=n;i++){
                                                           4
                                                                    for(int j=0; j <= m; j++){
  1.7 Kadane
                                                                         if(i==0 \text{ or } j==0)
                                                                              dp[i][j] = 0;
                                                                          else if(peso[i-1] \le j)
1 // achar uma subsequencia continua no array que a
                                                                              dp[i][j] = max(val[i-1]+dp[i-1][j-1]
      soma seja a maior possivel
                                                                 peso[i-1]], dp[i-1][j]);
2 // nesse caso vc precisa multiplicar exatamente 1
                                                           1.0
                                                                         else
      elemento da subsequencia
                                                           11
                                                                              dp[i][j] = dp[i-1][j];
3 // e achar a maior soma com isso
                                                                    }
                                                          12
                                                          13
                                                                 }
5 int n, x, arr[MAX], tab[MAX][2]; // tab[maior
                                                                 return dp[n][m];
                                                          14
      resposta no intervalo][foi multiplicado ou ano]
```

7 int dp(int i, bool mult) {

Graphs 2

2.1 Kruskall

```
1 struct DSU {
      int n:
       vector < int > link , sizes;
      DSU(int n) {
          this -> n = n;
           link.assign(n+1, 0);
           sizes.assign(n+1, 1);
           for (int i = 0; i \le n; i++)
10
              link[i] = i;
12
      int find(int x) {
14
           while (x != link[x])
1.5
              x = link[x];
16
17
           return x;
19
20
      bool same(int a, int b) {
2.1
          return find(a) == find(b);
22
23
24
      void unite(int a, int b) {
          a = find(a);
26
           b = find(b);
          if (a == b) return;
           if (sizes[a] < sizes[b])</pre>
3.1
              swap(a, b);
33
           sizes[a] += sizes[b];
           link[b] = a;
      }
36
37 };
39 struct Edge {
40
      int u, v;
      long long weight;
41
42
       Edge() {}
43
44
      Edge(int u, int v, long long weight) : u(u), v(v) 38 }
45
       , weight(weight) {}
      bool operator < (const Edge & other) const {</pre>
47
          return weight < other.weight;
49
5.0
       bool operator > (const Edge & other) const {
51
          return weight > other weight;
52
54 }:
56 vector < Edge > kruskal (vector < Edge > edges, int n) {
      vector < Edge > result; // arestas da MST
      long long cost = 0;
59
                                                            1.0
       sort(edges.begin(), edges.end());
                                                            11
6.1
                                                            12
      DSU dsu(n);
62
                                                            13
                                                            14
      for (auto e : edges) {
64
                                                            1.5
           if (!dsu.same(e.u, e.v)) {
               cost += e.weight;
66
                                                            17
               result.push_back(e);
                                                            18
```

```
dsu unite(e.u, e.v);
68
            }
69
       }
7.0
7.1
72
       return result;
73 }
```

2.2 \mathbf{Prim}

```
1 int n;
vector < vector < int >> adj; // adjacency matrix of graph
3 const int INF = 1000000000; // weight INF means there
       is no edge
5 struct Edge {
     int w = INF, to = -1;
6
7 };
9 void prim() {
10
     int total_weight = 0;
       vector < bool > selected(n, false);
11
       vector < Edge > min_e(n);
12
       min_e[0].w = 0;
13
14
       for (int i=0; i<n; ++i) {
1.5
           int v = -1;
16
           for (int j = 0; j < n; ++j) {
17
              if (!selected[j] && (v == -1 || min_e[j].
18
       w < min_e[v].w))
                   v = j;
19
20
21
           if (min_e[v].w == INF) {
22
               cout << "No MST!" << endl;</pre>
               exit(0);
24
26
           selected[v] = true;
27
           total_weight += min_e[v].w;
28
           if (min_e[v].to != -1)
29
                cout << v << " " << min_e[v].to << endl;</pre>
30
3.1
           for (int to = 0; to < n; ++to) {
               if (adj[v][to] < min_e[to].w)</pre>
33
                    min_e[to] = {adj[v][to], v};
34
           }
35
36
       cout << total_weight << endl;</pre>
```

2.3 Dijkstra

```
1 const int MAX = 2e5+7;
2 const int INF = 1000000000;
3 vector < vector < pair < int , int >>> adj(MAX);
5 void dijkstra(int s, vector<int> & d, vector<int> & p
    ) {
      int n = adj.size();
      d.assign(n, INF);
     p.assign(n, -1);
     d[s] = 0;
      set < pair < int , int >> q;
      q.insert({0, s});
      while (!q.empty()) {
         int v = q.begin()->second;
         q.erase(q.begin());
          for (auto edge : adj[v]) {
              int to = edge.first;
```

```
int len = edge.second;
19
20
               if (d[v] + len < d[to]) {
2.1
                   q.erase({d[to], to});
                   d[to] = d[v] + len;
                   p[to] = v;
24
                   q.insert({d[to], to});
               }
26
          }
      }
29 }
31 vector < int > restore_path(int s, int t) {
      vector < int > path;
33
      for (int v = t; v != s; v = p[v])
34
35
           path.push_back(v);
       path.push_back(s);
36
      reverse(path.begin(), path.end());
38
39
      return path;
40 }
41
42 int adj[MAX][MAX];
43 int dist[MAX];
44 int minDistance(int dist[], bool sptSet[], int V) {
       int min = INT_MAX, min_index;
45
46
       for (int v = 0; v < V; v++)
47
           if (sptSet[v] == false && dist[v] <= min)</pre>
48
               min = dist[v], min_index = v;
49
5.0
5.1
       return min_index;
52 }
53
54 void dijkstra(int src, int V) {
5.5
56
       bool sptSet[V];
       for (int i = 0; i < V; i++)
           dist[i] = INT_MAX, sptSet[i] = false;
58
59
      dist[src] = 0;
60
61
      for (int count = 0; count < V - 1; count++) {</pre>
62
           int u = minDistance(dist, sptSet, V);
63
64
           sptSet[u] = true;
6.5
67
           for (int v = 0; v < V; v++)
68
               if (!sptSet[v] && adj[u][v]
69
                   && dist[u] != INT_MAX
70
                   && dist[u] + adj[u][v] < dist[v])
71
                   dist[v] = dist[u] + adj[u][v];
72
7.3
74 }
```

2.4 Bellman Ford

```
1 struct edge
2 {
3     int a, b, cost;
4 };
5
6 int n, m, v;
7 vector < edge > e;
8 const int INF = 1000000000;
9
10 void solve()
11 {
12     vector < int > d (n, INF);
13     d[v] = 0;
14     for (int i=0; i < n-1; ++i)</pre>
```

```
for (int j=0; j<m; ++j)
if (d[e[j].a] < INF)
d[e[j].b] = min (d[e[j].b], d[e[j].a]
+ e[j].cost);
</pre>
```

2.5 Bipartite

```
1 const int NONE = 0, BLUE = 1, RED = 2;
vector < vector < int >> graph (100005);
3 vector < bool > visited(100005);
4 int color [100005];
6 bool bfs(int s = 1){
       queue < int > q;
9
       q.push(s);
10
       color[s] = BLUE;
11
       while (not q.empty()){
           auto u = q.front(); q.pop();
13
14
           for (auto v : graph[u]){
1.5
                if (color[v] == NONE){
16
                    color[v] = 3 - color[u];
                    q.push(v);
1.8
                else if (color[v] == color[u]){
20
                    return false;
21
22
           }
23
24
       }
25
       return true:
27 }
28
29 bool is_bipartite(int n){
30
       for (int i = 1; i \le n; i++)
31
           if (color[i] == NONE and not bfs(i))
32
33
                return false;
34
       return true:
35
```

2.6 Floyd Warshall

```
1 #include <bits/stdc++.h>
3 using namespace std;
4 using ll = long long;
6 const int MAX = 507;
7 const long long INF = 0x3f3f3f3f3f3f3f3f3fLL;
9 ll dist[MAX][MAX];
10 int n;
11
12 void floyd_warshall() {
      for (int i = 0; i < n; i++) {
13
           for (int j = 0; j < n; j++) {
14
               if (i == j) dist[i][j] = 0;
15
               else if (!dist[i][j]) dist[i][j] = INF;
16
17
           }
18
19
20
      for (int k = 0; k < n; k++) {
           for (int i = 0; i < n; i++) {
21
               for (int j = 0; j < n; j++) {
22
                   // trata o caso no qual o grafo tem
23
      arestas com peso negativo
                   if (dist[i][k] < INF && dist[k][j] <
24
      INF) {
```

```
dist[i][j] = min(dist[i][j], dist 29
2.5
       [i][k] + dist[k][j]);
                                                           31 }
                   }
26
               }
                                                           32
           }
                                                           33 char get_next(char c) {
                                                           if (c != 'Z') return c + 1;
      }
29
30 }
                                                                  return '$';
                                                           36 }
       Tree Diameter
                                                           37
                                                           38 bool flag = true;
                                                           39
1 #include <bits/stdc++.h>
                                                           40 void solve(int node, char c) {
                                                               int center = get_centroid(node, dfs(node));
                                                           41
3 using namespace std;
                                                                 ans[center] = c;
                                                                  removed[center] = true;
                                                           43
5 const int MAX = 3e5 + 17;
                                                           44
                                                           45
                                                                  for (auto u : adj[center]) {
7 vector < int > adj [MAX];
                                                                       if (!removed[u]) {
                                                           46
8 bool visited[MAX];
                                                                           char next = get_next(c);
if (next == '$') {
                                                           48
int max_depth = 0, max_node = 1;
                                                                               flag = false;
                                                           49
11
                                                           50
                                                                               return;
12 void dfs (int v, int depth) {
                                                           5.1
      visited[v] = true;
13
                                                           52
                                                                           solve(u, next);
14
                                                                       }
                                                           5.3
      if (depth > max_depth) {
1.5
                                                           54
16
           max_depth = depth;
                                                           55 }
           max_node = v;
17
                                                           56
18
                                                           57 int32_t main(){
                                                               ios::sync_with_stdio(false);
                                                           5.8
      for (auto u : adj[v]) {
20
                                                                  cin.tie(NULL);
                                                           59
           if (!visited[u]) dfs(u, depth + 1);
21
                                                           60
22
                                                                  cin >> n;
                                                           61
23 }
                                                           62
                                                                  adj.resize(n + 1);
                                                                  ans.resize(n + 1);
                                                           63
25 int tree_diameter() {
                                                                  removed.resize(n + 1);
                                                           64
      dfs(1, 0);
                                                                  subtree_size.resize(n + 1);
                                                           6.5
      max_depth = 0;
27
      for (int i = 0; i < MAX; i++) visited[i] = false; 67
                                                                  for (int i = 1; i \le n - 1; i++) {
29
      dfs(max_node, 0);
                                                                       int u, v; cin >> u >> v;
                                                           68
      return max_depth;
3.0
                                                           69
                                                                       adj[u].insert(v);
31 }
                                                                       adj[v].insert(u);
                                                           7.0
                                                           71
  2.8 Centroid Decomposition
                                                           72
                                                                  solve(1, 'A');
                                                           73
                                                           74
1 int n:
                                                                  if (!flag) cout << "Impossible!\n";</pre>
                                                           7.5
vector < set < int >> adj;
                                                           76
3 vector < char > ans;
                                                                      for (int i = 1; i <= n; i++) {
                                                           7.7
                                                           78
                                                                           cout << ans[i] << ' ';</pre>
5 vector < bool > removed;
                                                           79
                                                                       cout << '\n';
7 vector < int > subtree_size;
                                                           80
                                                           81
9 int dfs(int u, int p = 0) {
                                                           82
   subtree_size[u] = 1;
                                                           83
                                                                  return 0;
                                                           84 }
11
    for(int v : adj[u]) {
12
                                                              2.9 Lca
      if(v != p && !removed[v]) {
13
         subtree_size[u] += dfs(v, u);
                                                            1 // Description:
1.5
                                                            _{2} // Find the lowest common ancestor between two nodes
16
17
                                                                  in a tree
    return subtree_size[u];
18
                                                            4 // Problem:
                                                            5 // https://cses.fi/problemset/task/1688/
21 int get_centroid(int u, int sz, int p = 0) {
    for(int v : adj[u]) {
                                                            7 // Complexity:
22
      if(v != p && !removed[v]) {
                                                            8 // O(log n)
23
         if(subtree_size[v]*2 > sz) {
          return get_centroid(v, sz, u);
                                                           10 // How to use:
25
               }
                                                           11 // preprocess(1);
                                                           12 // lca(a, b);
           }
27
      }
28
                                                           13
```

```
14 // Notes
                                                          4 // Problem:
15 // To calculate the distance between two nodes use
      the following formula
                                                          5 // https://cses.fi/problemset/task/1684
16 // dist[a] + dist[b] - 2*dist[lca(a, b)]
                                                          7 // Complexity:
18 const int MAX = 2e5 + 17;
                                                           _{8} // O(n + m) where n is the number of variables and m
                                                                 is the number of clauses
20 const int BITS = 32:
                                                          10 #include <bits/stdc++.h>
22 vector < int > adj [MAX];
                                                          11 #define pb push_back
                                                          12 #define mp make_pair
23 // vector<pair<int, int>> adj[MAX];
24 // int dist[MAX];
                                                          13 #define pii pair < int, int>
                                                          14 #define ff first
                                                          15 #define ss second
26 int timer:
27 vector < int > tin, tout;
                                                          16
28 vector < vector < int >> up;
                                                          17 using namespace std;
                                                          18
30 void dfs(int v, int p)
                                                          19 struct SAT {
31
                                                         20
                                                              int nodes;
      tin[v] = ++timer;
                                                               int curr = 0;
                                                         21
32
      up[v][0] = p;
                                                          22
                                                                int component = 0;
33
                                                                vector < vector < int >> adj;
                                                          23
34
      for (int i = 1; i <= BITS; ++i) {
                                                         24
                                                               vector < vector < int >> rev;
3.5
         up[v][i] = up[up[v][i-1]][i-1];
                                                               vector < vector < int >> condensed;
                                                        25
                                                               vector<pii> departure;
37
                                                         26
                                                          27
                                                                vector < bool > visited;
38
      for (auto u : adj[v]) {
                                                                vector < int > scc;
39
                                                          28
          if (u != p) {
                                                                vector < int > order;
                                                         29
40
              dfs(u, v);
                                                          30
41
                                                          3.1
                                                                // 1 to nodes
42
                                                                 // nodes + 1 to 2 * nodes
43
                                                          32
                                                                 SAT(int nodes) : nodes(nodes) {
44
                                                          33
      /*for (auto [u, peso] : adj[v]) {
                                                         34
                                                                   adj resize(2 * nodes + 1);
45
         if (u != p) {
                                                        35
                                                                     rev.resize(2 * nodes + 1);
              dist[u] = dist[v] + peso;
                                                         36
                                                                     visited.resize(2 * nodes + 1);
47
               dfs(u, v);
                                                                     scc.resize(2 * nodes + 1);
                                                          37
49
                                                          3.8
      } * /
50
                                                          39
                                                                 void add_imp(int a, int b) {
                                                          40
51
      tout[v] = ++timer;
                                                                   adj[a].pb(b);
52
                                                          41
53 }
                                                          42
                                                                     rev[b].pb(a);
54
                                                          43
55 bool is_ancestor(int u, int v)
                                                          44
56 {
                                                                 int get_not(int a) {
      return tin[u] <= tin[v] && tout[u] >= tout[v];
                                                                     if (a > nodes) return a - nodes;
57
                                                          46
58 }
                                                                     return a + nodes;
                                                          47
                                                          48
60 int lca(int u, int v)
                                                          49
                                                                 void add_or(int a, int b) {
61 {
                                                          5.0
62
      if (is_ancestor(u, v))
                                                          51
                                                                     add_imp(get_not(a), b);
63
          return u;
                                                          52
                                                                     add_imp(get_not(b), a);
      if (is_ancestor(v, u))
64
                                                         53
          return v;
                                                         54
      for (int i = BITS; i >= 0; --i) {
                                                                 void add_nor(int a, int b) {
                                                         5.5
66
          if (!is_ancestor(up[u][i], v))
                                                          5.6
                                                                     add_or(get_not(a), get_not(b));
              u = up[u][i];
68
                                                          5.7
6.9
                                                          58
      return up[u][0];
                                                          59
                                                                 void add_and(int a, int b) {
70
71 }
                                                                     add_or(get_not(a), b);
                                                          60
                                                                     add_or(a, get_not(b));
                                                          61
                                                                     add_or(a, b);
73 void preprocess(int root) {
                                                          62
   tin resize(MAX);
                                                         63
7.4
      tout resize(MAX);
                                                          64
      timer = 0;
                                                                 void add_nand(int a, int b) {
76
                                                          65
      up.assign(MAX, vector<int>(BITS + 1));
                                                          66
                                                                     add_or(get_not(a), b);
      dfs(root, root);
                                                                     add_or(a, get_not(b));
78
                                                          67
                                                          68
                                                                     add_or(get_not(a), get_not(b));
                                                          69
  2.10 2sat
                                                          70
                                                                 void add_xor(int a, int b) {
                                                                    add_or(a, b);
1 // Description:
                                                          72
                                                                     add_or(get_not(a), get_not(b));
_{2} // Solves expression of the type (a v b) ^ (c v d) ^ _{73}
      (e v f)
```

```
if (scc[i] != scc[u]) condensed[scc[i
7.5
                                                             142
76
       void add_xnor(int a, int b) {
                                                                    ]].pb(scc[u]);
            add_or(get_not(a), b);
                                                                             }
                                                             143
                                                                         }
78
            add_or(a, get_not(b));
                                                             144
79
                                                             145
                                                                         visited.assign(component + 1, false);
80
                                                             146
       void departure_time(int v) {
81
                                                             147
            visited[v] = true;
                                                                         for (int i = 1; i <= component; i++) {</pre>
82
                                                             148
                                                                             if (!visited[i]) topological_order(i);
83
                                                             149
            for (auto u : adj[v]) {
84
                if (!visited[u]) departure_time(u);
85
                                                             151
                                                                         reverse(order.begin(), order.end());
87
                                                             153
                                                                         // 0 - false
            departure.pb(mp(++curr, v));
                                                             154
88
       }
                                                                         // 1 - true
89
                                                             155
                                                                         // 2 - no value yet
90
91
       void find_component(int v, int component) {
                                                             157
                                                                         vector < int > ans(2 * nodes + 1, 2);
            scc[v] = component;
92
                                                             158
                                                                         vector < vector < int >> belong (component + 1);
            visited[v] = true;
94
                                                             160
            for (auto u : rev[v]) {
                                                                         for (int i = 1; i <= 2 * nodes; i++) {
                                                             161
95
                if (!visited[u]) find_component(u,
                                                                             belong[scc[i]].pb(i);
96
                                                             162
       component);
                                                             163
            }
97
                                                             164
       }
                                                                         for (auto p : order) {
98
                                                             165
                                                                              for (auto e : belong[p]) {
99
                                                                                  ans[e] = find_value(e, ans);
100
       void topological_order(int v) {
                                                             167
            visited[v] = true;
                                                             168
                                                                         }
102
            for (auto u : condensed[v]) {
103
                                                             170
                if (!visited[u]) topological_order(u);
104
                                                             171
                                                                         return ans;
                                                                    }
105
                                                             172
                                                             173 };
106
            order.pb(v);
                                                             174
       }
                                                             175 int main() {
108
                                                                     ios::sync_with_stdio(false);
109
                                                             176
                                                                     cin tie(NULL);
       bool is_possible() {
110
111
            component = 0;
                                                             178
            for (int i = 1; i <= 2 * nodes; i++) {
                                                                     int n, m; cin >> n >> m;
112
                                                             179
                if (!visited[i]) departure_time(i);
113
                                                             180
114
                                                             181
                                                                     SAT sat = SAT(m);
115
                                                             182
            sort(departure.begin(), departure.end(),
                                                                     for (int i = 0; i < n; i++) {
                                                             183
116
       greater < pii > ());
                                                                         char op1, op2; int a, b; cin >> op1 >> a >>
                                                             184
                                                                     op2 \gg b;
117
                                                                         if (op1 == '+' && op2 == '+') sat.add_or(a, b
            visited.assign(2 * nodes + 1, false);
118
119
            for (auto [_, node] : departure) {
                                                                         if (op1 == '-' && op2 == '-') sat.add_or(sat.
               if (!visited[node]) find_component(node,
                                                                     get_not(a), sat.get_not(b));
       ++component);
                                                                         if (op1 == '+' && op2 == '-') sat.add_or(a,
                                                             187
           }
                                                                     sat.get_not(b));
                                                                         if (op1 == '-' && op2 == '+') sat.add_or(sat.
123
                                                             188
            for (int i = 1; i <= nodes; i++) {
                                                                     get_not(a), b);
124
                if (scc[i] == scc[i + nodes]) return
125
                                                             189
       false;
                                                             190
                                                                     if (!sat.is_possible()) cout << "IMPOSSIBLE\n";</pre>
126
                                                             191
                                                                     else {
127
            return true;
                                                                         vector < int > ans = sat.find_ans();
128
                                                             193
                                                                         for (int i = 1; i <= m; i++) {
129
       }
                                                             194
                                                                             cout << (ans[i] == 1 ? '+' : '-') << ' ';</pre>
130
       int find_value(int e, vector<int> &ans) {
131
                                                             196
            if (e > nodes && ans[e - nodes] != 2) return 197
                                                                         cout << '\n';
132
       !ans[e - nodes];
            if (e <= nodes && ans[e + nodes] != 2) return199
133
        !ans[e + nodes];
                                                             200
                                                                     return 0;
                                                             201 }
134
            return 0:
135
136
                                                                        Ford Fulkerson Edmonds Karp
       vector < int > find_ans() {
137
            condensed.resize(component + 1);
138
139
                                                              1 // Description:
            for (int i = 1; i <= 2 * nodes; i++) {
140
                                                              _{2} // Obtains the maximum possible flow rate given a
141
                for (auto u : adj[i]) {
                                                                    network. A network is a graph with a single
```

```
source vertex and a single sink vertex in which 11 // A unit network is a network in which for any
      each edge has a capacity
                                                                  vertex except source and sink either incoming or
                                                                  outgoing edge is unique and has unit capacity (
4 // Complexity:
                                                                  matching problem).
                                                           12 // Complexity on unit networks: O(E * sqrt(V))
_{5} // O(V * E^{2}) where V is the number of vertex and E
      is the number of edges
                                                           14 // Unity capacity networks
7 int n:
                                                           _{15} // A more generic settings when all edges have unit
                                                                  capacities, but the number of incoming and
8 vector < vector < int >> capacity;
9 vector < vector < int >> adj;
                                                                  outgoing edges is unbounded
                                                           16 // Complexity on unity capacity networks: O(E * sqrt(
1.0
int bfs(int s, int t, vector<int>& parent) {
                                                                  E))
      fill(parent.begin(), parent.end(), -1);
12
      parent[s] = -2;
                                                           18 // How to use:
13
      queue <pair < int , int >> q;
                                                           19 // Dinic dinic = Dinic(num_vertex, source, sink);
14
                                                           20 // dinic.add_edge(vertex1, vertex2, capacity);
      q.push({s, INF});
15
                                                           21 // cout << dinic.max_flow() << '\n';</pre>
16
      while (!q.empty()) {
17
           int cur = q.front().first;
                                                           23 #include <bits/stdc++.h>
           int flow = q.front().second;
19
                                                           24
          q.pop();
                                                           25 #define pb push_back
20
                                                           26 #define mp make_pair
21
           for (int next : adj[cur]) {
                                                           27 #define pii pair < int, int>
22
              if (parent[next] == -1 && capacity[cur][ 28 #define ff first
      next]) {
                                                           29 #define ss second
                   parent[next] = cur;
                                                           30 #define ll long long
24
                   int new_flow = min(flow, capacity[cur 31
25
      ][next]);
                                                           32 using namespace std;
                   if (next == t)
26
                       return new_flow;
                                                           34 \text{ const.} 11 \text{ INF} = 1e18+10:
27
                   q.push({next, new_flow});
               }
                                                           36 struct Edge {
29
           }
                                                                 int from;
                                                           37
30
31
      }
                                                           38
                                                                  int to;
                                                                  11 capacity;
32
                                                           39
                                                                  11 flow;
33
      return 0;
                                                           40
34 }
                                                                  Edge* residual;
                                                           41
35
                                                           42
36 int maxflow(int s, int t) {
                                                           43
                                                                  Edge() {}
      int flow = 0;
37
                                                           44
      vector < int > parent(n);
                                                           45
                                                                  Edge(int from, int to, 11 capacity) : from(from),
      int new_flow;
                                                                   to(to), capacity(capacity) {
39
                                                                      flow = 0;
41
      while (new_flow = bfs(s, t, parent)) {
                                                           47
           flow += new_flow;
                                                           48
42
           int cur = t;
                                                           49
                                                                  11 get_capacity() {
43
           while (cur != s) {
                                                                      return capacity - flow;
44
                                                           5.0
               int prev = parent[cur];
                                                           51
               capacity[prev][cur] -= new_flow;
46
                                                           52
47
               capacity[cur][prev] += new_flow;
                                                           53
                                                                  11 get_flow() {
               cur = prev;
                                                           54
                                                                      return flow;
48
           }
49
                                                           55
      }
50
                                                           56
                                                                  void augment(ll bottleneck) {
                                                           5.7
5.1
      return flow;
                                                           58
                                                                      flow += bottleneck;
53
                                                                      residual -> flow -= bottleneck;
                                                           5.9
                                                           60
  2.12 Dinic
                                                           61
                                                                  void reverse(11 bottleneck) {
                                                           62
                                                                      flow -= bottleneck;
                                                           63
1 // Description:
                                                                      residual ->flow += bottleneck;
_{2} // Obtains the maximum possible flow rate given a
                                                           64
                                                           65
      network. A network is a graph with a single
      source vertex and a single sink vertex in which
                                                                  bool operator < (const Edge& e) const {
      each edge has a capacity
                                                           67
                                                                      return true;
4 // Problem:
                                                           69
                                                           70 }:
5 // https://codeforces.com/gym/103708/problem/J
                                                           72 struct Dinic {
7 // Complexity:
_{8} // O(V^2 * E) where V is the number of vertex and E
                                                                 int source;
                                                           73
                                                                  int sink:
      is the number of edges
                                                           74
                                                           75
                                                                  int nodes:
10 // Unit network
                                                           76
                                                                  11 flow;
```

```
vector < vector < Edge *>> adj;
                                                                              while (sent != 0) {
7.7
                                                              145
        vector < int > level;
                                                              146
                                                                                   sent = dfs(source, INF);
78
       vector < int > next;
                                                                                   flow += sent;
79
                                                              147
        vector < int > reach;
                                                              148
80
        vector < bool > visited;
81
                                                              149
                                                                          }
        vector < vector < int >> path;
                                                                          return flow;
82
83
                                                              151
       Dinic(int source, int sink, int nodes) : source( 152
84
        source), sink(sink), nodes(nodes) {
                                                                      void reachable(int v) {
                                                              153
            adj.resize(nodes + 1);
                                                                          visited[v] = true;
85
                                                              154
86
                                                                          for (auto e : adj[v]) {
        void add_edge(int from, int to, ll capacity) {
                                                                              if (!visited[e->to] && e->get_capacity()
88
                                                              157
            Edge* e1 = new Edge(from, to, capacity);
                                                                     > 0) {
89
            Edge* e2 = new Edge(to, from, 0);
90
                                                              158
                                                                                   reach.pb(e->to);
            // Edge* e2 = new Edge(to, from, capacity);
                                                                                   visited[e->to] = true;
91
                                                              159
            e1->residual = e2;
92
                                                              160
                                                                                   reachable(e->to);
            e2->residual = e1;
                                                                              }
93
                                                              161
            adj[from].pb(e1);
                                                                          }
                                                                     }
            adj[to].pb(e2);
95
                                                              163
       }
                                                              164
96
                                                              165
                                                                      void print_min_cut() {
97
       bool bfs() {
                                                                          reach clear();
98
            level.assign(nodes + 1, -1);
                                                                          visited assign(nodes + 1, false);
99
            queue < int > q;
                                                                          reach .pb(source);
100
                                                              168
            q.push(source);
                                                              169
                                                                          reachable (source);
            level[source] = 0;
102
                                                                          for (auto v : reach) {
            while (!q.empty()) {
                                                                              for (auto e : adj[v]) {
                                                              172
                int node = q.front();
                                                                                   if (!visited[e->to] && e->
                                                              173
                                                                     get_capacity() == 0) {
106
                q.pop();
                                                                                       cout << e->from << ' ' << e->to
                                                              174
                for (auto e : adj[node]) {
                                                                     << '\n';
108
                    if (level[e->to] == -1 && e->
                                                              175
                                                                                   }
        get_capacity() > 0) {
                                                                              }
                                                              176
                         level[e->to] = level[e->from] +
                                                                          }
                                                              177
       1:
                                                              178
111
                         q.push(e->to);
                                                              179
                     }
                                                                      11 build_path(int v, int id, ll flow) {
112
                                                              180
                }
                                                                          visited[v] = true;
113
                                                              181
            }
114
                                                              182
                                                                          if (v == sink) {
                                                                              return flow;
                                                              183
            return level[sink] != -1;
                                                              184
116
117
       }
                                                              185
                                                                          for (auto e : adj[v]) {
                                                              186
118
        11 dfs(int v, ll flow) {
                                                                               if (!visited[e->to] && e->get_flow() > 0)
119
                                                              187
            if (v == sink)
                return flow;
                                                                                   visited[e->to] = true;
                                                                                   11 bottleneck = build_path(e->to, id,
                                                              189
            int sz = adj[v].size();
                                                                      min(flow, e->get_flow());
123
                                                                                   if (bottleneck > 0) {
            for (int i = next[v]; i < sz; i++) {</pre>
124
                Edge* e = adj[v][i];
                                                                                       path[id].pb(e->to);
                if (level[e->to] == level[e->from] + 1 &&192
                                                                                       e->reverse(bottleneck);
        e->get_capacity() > 0) {
                                                                                       return bottleneck;
                     11 bottleneck = dfs(e->to, min(flow, 194
                                                                                   }
127
                                                                              }
       e->get_capacity()));
                     if (bottleneck > 0) {
                                                                          }
                                                              196
128
                         e->augment(bottleneck);
129
                                                              197
130
                         return bottleneck;
                                                              198
                                                                          return 0:
                     }
131
                                                              199
                }
132
                                                              200
                                                                      void print_flow_path() {
133
                                                              201
                next[v] = i + 1;
                                                                          path.clear();
134
                                                              202
            }
                                                                          11 sent = -1;
                                                             203
135
                                                                          int id = -1;
                                                              204
                                                                          while (sent != 0) {
137
            return 0:
                                                             205
                                                                              visited assign(nodes + 1, false);
138
                                                              206
                                                                              path.pb(vector<int>{});
                                                              207
139
       11 max_flow() {
                                                                               sent = build_path(source, ++id, INF);
                                                             208
140
            flow = 0;
                                                                              path[id].pb(source);
141
                                                              209
            while(bfs()) {
142
                                                             210
                next.assign(nodes + 1, 0);
143
                                                             211
                                                                          path.pop_back();
                11 sent = -1;
                                                             212
144
```

```
for (int i = 0; i < id; i++) {
                                                            1 // Description:
213
214
                cout << path[i].size() << '\n';</pre>
                                                            2 // Find a bridge in a connected unidirected graph
                reverse(path[i].begin(), path[i].end()); 3 // A bridge is an edge so that if you remove that
215
                                                                  edge the graph is no longer connected
216
                for (auto e : path[i]) {
                    cout << e << ' ';
                                                            5 // Problem:
218
                                                            6 // https://cses.fi/problemset/task/2177/
                cout << '\n';
219
           }
220
                                                            8 // Complexity:
221
                                                            _{\rm 9} // O(V + E) where V is the number of vertices and E
222 };
                                                                  is the number of edges
223
224 int main() {
       ios::sync_with_stdio(false);
225
                                                            11 int n;
       cin.tie(NULL);
                                                           12 vector < vector < int >> adj;
227
                                                           13
       int n, m; cin >> n >> m;
                                                            14 vector < bool > visited;
228
                                                            15 vector <int> tin, low;
       Dinic dinic = Dinic(1, n, n);
                                                           16 int timer;
230
       for (int i = 1; i <= m; i++) {
                                                           18 void dfs(int v, int p) {
232
                                                                 visited[v] = true;
233
           int v, u; cin >> v >> u;
                                                           19
                                                                  tin[v] = low[v] = timer++;
234
           dinic.add_edge(v, u, 1);
                                                            20
235
                                                                  for (int to : adj[v]) {
                                                           2.1
                                                                      if (to == p) continue;
                                                           22
                                                                       if (visited[to]) {
       cout << dinic.max_flow() << '\n';</pre>
237
                                                           23
       // dinic.print_min_cut();
                                                                           low[v] = min(low[v], tin[to]);
238
                                                           24
       // dinic.print_flow_path();
                                                                       } else {
239
                                                           25
                                                                           dfs(to, v);
240
                                                            26
241
       return 0;
                                                            27
                                                                           low[v] = min(low[v], low[to]);
242
                                                                           if (low[to] > tin[v]) {
                                                            28
                                                                               IS_BRIDGE(v, to);
                                                            29
   2.13 Find Cycle
                                                            3.0
                                                            31
                                                                       }
                                                            32
                                                                  }
 1 bitset < MAX > visited;
                                                           33 }
 2 vector < int > path;
 3 vector < int > adj[MAX];
                                                           35 void find_bridges() {
                                                           36
                                                                  timer = 0;
 5 bool dfs(int u, int p){
                                                           37
                                                                  visited.assign(n, false);
                                                                  tin.assign(n, -1);
                                                            38
       if (visited[u]) return false;
                                                            39
                                                                  low.assign(n, -1);
                                                                  for (int i = 0; i < n; ++i) {
                                                            40
       path.pb(u);
 9
                                                                       if (!visited[i])
                                                            41
       visited[u] = true;
 10
                                                            42
                                                                           dfs(i, -1);
 1.1
                                                            43
       for (auto v : adj[u]){
12
                                                            44 }
           if (visited[v] and u != v and p != v){
                                                                     Cycle Path Recovery
                                                              2.15
                path.pb(v); return true;
14
16
                                                            1 int n;
           if (dfs(v, u)) return true;
17
                                                            vector < vector < int >> adj;
                                                            3 vector < char > color;
19
                                                            4 vector <int> parent;
20
       path.pop_back();
                                                            5 int cycle_start, cycle_end;
       return false:
21
                                                            7 bool dfs(int v) {
                                                                  color[v] = 1;
24 bool has_cycle(int N){
                                                                  for (int u : adj[v]) {
                                                            9
                                                                       if (color[u] == 0) {
       visited reset();
26
                                                                           parent[u] = v;
                                                            11
                                                                           if (dfs(u))
                                                            12
       for (int u = 1; u \le N; ++u){
                                                            13
                                                                               return true;
           path.clear();
                                                                       } else if (color[u] == 1) {
                                                            14
            if (not visited[u] and dfs(u,-1))
30
                                                            15
                                                                           cycle_end = v;
               return true:
3.1
                                                                           cycle_start = u;
                                                            16
                                                                           return true;
                                                            17
       }
33
                                                                       }
                                                            18
3.4
                                                            19
35
       return false;
                                                            20
                                                                  color[v] = 2;
36 }
                                                                  return false;
                                                            2.1
                                                            22 }
   2.14 Tarjan Bridge
```

24 void find_cycle() {

```
color.assign(n, 0);
                                                                  u --; v --;
2.5
                                                           43
26
      parent assign(n, -1);
                                                           44
                                                                  adj[u].push_back(v);
      cycle_start = -1;
                                                                  adj[v].push_back(u);
27
                                                           45
28
                                                           46
      for (int v = 0; v < n; v++) {
                                                           47
           if (color[v] == 0 && dfs(v))
                                                                get_subtree_size(0);
                                                           48
30
               break;
                                                                cout << get_centroid(0) + 1 << endl;</pre>
                                                           49
                                                           50 }
32
33
                                                              2.17 Small To Large
      if (cycle_start == -1) {
34
          cout << "Acyclic" << endl;</pre>
3.5
36
      } else {
                                                            1 // Problem:
37
          vector<int> cycle;
                                                            2 // https://codeforces.com/contest/600/problem/E
           cycle push_back(cycle_start);
          for (int v = cycle_end; v != cycle_start; v = 4 void process_colors(int curr, int parent) {
39
        parent[v])
40
               cycle.push_back(v);
                                                                for (int n : adj[curr]) {
           cycle.push_back(cycle_start);
                                                                  if (n != parent) {
41
           reverse(cycle begin(), cycle end());
                                                                    process_colors(n, curr);
43
           cout << "Cycle found: ";</pre>
                                                                           if (colors[curr].size() < colors[n].size</pre>
44
                                                           1.0
           for (int v : cycle)
                                                                  ()) {
45
               cout << v << " ";
                                                                               sum_num[curr] = sum_num[n];
46
                                                           11
           cout << endl;</pre>
                                                                               vmax[curr] = vmax[n];
                                                           12
48
                                                                      swap(colors[curr], colors[n]);
                                                           13
49 }
                                                                    }
                                                           1.4
                                                           1.5
  2.16 Centroid Find
                                                                    for (auto [item, vzs] : colors[n]) {
                                                           16
                                                                               if(colors[curr][item]+vzs > vmax[curr
                                                           17
1 // Description:
                                                                  ]){
2 // Indexed at zero
                                                                                   vmax[curr] = colors[curr][item] +
_{\rm 3} // Find a centroid, that is a node such that when it
                                                                   VZS:
      is appointed the root of the tree,
                                                                                   sum_num[curr] = item;
_4 // each subtree has at most floor(n/2) nodes.
                                                                               else if(colors[curr][item]+vzs ==
6 // Problem:
                                                                  vmax[curr]){
7 // https://cses.fi/problemset/task/2079/
                                                                                   sum_num[curr] += item;
                                                           23
9 // Complexity:
                                                           24
                                                                               colors[curr][item] += vzs;
10 // O(n)
                                                           25
                                                           26
                                                                    }
12 // How to use:
                                                                  }
                                                           27
                                                                }
13 // get_subtree_size(0);
                                                           28
14 // cout << get_centroid(0) + 1 << endl;</pre>
                                                           29
1.5
                                                           30 }
16 int n;
                                                           31
17 vector < int > adj [MAX];
                                                           32
18 int subtree_size[MAX];
                                                           33 int32_t main() {
                                                           3.4
20 int get_subtree_size(int node, int par = -1) {
                                                           35
                                                                int n; cin >> n;
   int &res = subtree_size[node];
21
                                                           36
    res = 1;
                                                                for (int i = 1; i <= n; i++) {
                                                           37
    for (int i : adj[node]) {
                                                                 int a; cin >> a;
23
                                                           38
      if (i == par) continue;
                                                                  colors[i][a] = 1;
                                                           39
      res += get_subtree_size(i, node);
                                                                      vmax[i] = 1;
2.5
                                                           40
26
                                                           41
                                                                      sum_num[i] = a;
                                                                }
27
    return res;
                                                           42
28 }
                                                           43
                                                                for (int i = 1; i < n; i++) {
30 int get_centroid(int node, int par = -1) {
                                                                  int a, b; cin >> a >> b;
                                                           45
   for (int i : adj[node]) {
31
                                                           46
      if (i == par) continue;
                                                                  adj[a].push_back(b);
32
                                                           47
                                                                  adj[b].push_back(a);
33
                                                           48
      if (subtree_size[i] * 2 > n) { return
                                                           49
      get_centroid(i, node); }
                                                           5.0
                                                                process_colors(1, 0);
                                                           51
36
    return node:
                                                           52
37 }
                                                                for (int i = 1; i <= n; i++) {
                                                           53
                                                                  cout << sum_num[i] << (i < n ? " " : "\n");
                                                           54
39 int main() {
                                                           5.5
    cin >> n;
                                                           56
    for (int i = 0; i < n - 1; i++) {
                                                                  return 0;
41
                                                           5.7
     int u, v; cin >> u >> v;
                                                           58
42
```

Data Structures

Ordered Set

59 }

```
1 // Description:
2 // insert(k) - add element k to the ordered set
                                                           11
_{3} // erase(k) - remove element k from the ordered set
4 // erase(it) - remove element it points to from the
                                                           13
      ordered set
5 // order_of_key(k) - returns number of elements
      strictly smaller than k
6 // find_by_order(n) - return an iterator pointing to
                                                           17
      the k-th element in the ordered set (counting
                                                           18
      from zero).
                                                           20
8 // Problem:
                                                           21
9 // https://cses.fi/problemset/task/2169/
                                                           22
                                                          23
11 // Complexity:
                                                          24
12 // O(log n) for all operations
                                                          2.5
                                                           26
14 // How to use:
                                                           27
15 // ordered_set < int > os;
                                                           28
16 // cout << os.order_of_key(1) << '\n;</pre>
                                                           29
17 // cout << os.find_by_order(1) << '\n;</pre>
                                                           3.0
                                                           31
                                                           32
20 // The ordered set only contains different elements
                                                           33
_{21} // By using less_equal <T> instead of less<T> on using _{34}^{-}
       ordered_set declaration
                                                          35
22 // The ordered_set becomes an ordered_multiset
23 // So the set can contain elements that are equal
                                                          3.7
25 #include <ext/pb_ds/assoc_container.hpp>
                                                           39
26 #include <ext/pb_ds/tree_policy.hpp>
                                                           40
                                                           41
28 using namespace __gnu_pbds;
                                                           42
29 template <typename T>
                                                           43
30 using ordered_set = tree<T,null_type,less<T>,
                                                           44
      rb_tree_tag,tree_order_statistics_node_update>;
                                                           45
```

3.2 Priority Queue

3.3 Dsu

```
1 // Description:
_{2} // Keeps the largest (by default) element at the top ^{50}
      of the queue
4 // Problem:
5 // https://cses.fi/problemset/task/1164/
7 // Complexity:
8 // O(log n) for push and pop
_{9} // _{0} (1) for looking at the element at the top
11 // How to use:
12 // prioriy_queue < int > pq;
13 // pq.push(1);
14 // pq.top();
15 // pq.pop()
17 // Notes
_{18} // To use the priority queue keeping the smallest
      element at the top
20 priority_queue <int, vector <int>, greater <int>> pq;
```

```
1 #include <bits/stdc++.h>
3 using namespace std;
5 const int MAX = 1e6+17;
7 struct DSU {
     int n;
      vector < int > link, sizes;
      DSU(int n) {
          this -> n = n;
          link.assign(n+1, 0);
          sizes.assign(n+1, 1);
          for (int i = 0; i \le n; i++)
               link[i] = i;
      int find(int x) {
          while (x != link[x])
             x = link[x];
           return x;
      bool same(int a, int b) {
          return find(a) == find(b);
      void unite(int a, int b) {
         a = find(a);
          b = find(b);
          if (a == b) return;
          if (sizes[a] < sizes[b])</pre>
              swap(a, b);
           sizes[a] += sizes[b];
           link[b] = a;
      int size(int x) {
           return sizes[x];
47 ]:
49 int main() {
      ios::sync_with_stdio(false);
      cin tie(NULL);
      int cities, roads; cin >> cities >> roads;
      vector < int > final_roads;
      int ans = 0;
      DSU dsu = DSU(cities);
      for (int i = 0, a, b; i < roads; i++) {
          cin >> a >> b;
          dsu.unite(a, b);
      for (int i = 2; i <= cities; i++) {
          if (!dsu same(1, i)) {
               ans++:
               final_roads.push_back(i);
               dsu unite(1,i);
      cout << ans << '\n';
      for (auto e : final_roads) {
           cout << "1 " << e << '\n';
```

46

51

52

54 5.5

56

5.7

58

59

60

6.1 62

63

64

66

67

68

69

7.1

72

7.3

```
seg[novo] = seg[pos];
7.4
                                                          5.9
75 }
                                                          60
                                                                     e[novo] = e[pos];
                                                                     d[novo] = d[pos];
                                                          6.1
  3.4 Persistent
                                                          62
                                                                     if (ini == fim) {
                                                                         seg[novo] = val;
1 // Description:
                                                          64
                                                                         return novo;
2 // Persistent segtree allows for you to save the
       different versions of the segtree between each
                                                          66
      update
                                                          67
                                                                     int m = (ini + fim) >> 1;
3 // Indexed at one
4 // Query - get sum of elements from range (1, r)
                                                          69
                                                                     if (id <= m) e[novo] = update(e[novo], ini, m</pre>
      inclusive
                                                                 , id, val);
5 // Update - update element at position id to a value
                                                                     else d[novo] = update(d[novo], m + 1, fim, id
      val
                                                                 , val);
7 // Problem:
                                                          72
                                                                     seg[novo] = f(seg[e[novo]], seg[d[novo]]);
8 // https://cses.fi/problemset/task/1737/
                                                          73
                                                          7.4
10 // Complexity:
                                                                     return novo;
                                                                 }
11 // O(log n) for both query and update
                                                          76
                                                          7.7
                                                                 ftype query(int pos, int p, int q) {
13 // How to use:
                                                          78
                                                                     return query(pos, 1, n, p, q);
                                                          7.9
14 // vector <int > raiz(MAX); // vector to store the
      roots of each version
15 // Segtree seg = Segtree(INF);
                                                          8.1
                                                                 int update(int pos, int id, int val) {
16 // raiz[0] = seg.create(); // null node
                                                          82
                                                                     return update(pos, 1, n, id, val);
17 // curr = 1; // keep track of the last version
                                                          83
                                                          84
                                                          85 };
19 // raiz[k] = seg.update(raiz[k], idx, val); //
      updating version k
                                                                  Minimum And Amount
                                                             3.5
20 // seg.query(raiz[k], l, r) // querying version k
21 // raiz[++curr] = raiz[k]; // create a new version
                                                           1 // Description:
      based on version k
                                                           2 // Query - get minimum element in a range (1, r)
23 const int MAX = 2e5+17;
                                                                 inclusive
_{24} const int INF = 1e9+17;
                                                           _{\rm 3} // and also the number of times it appears in that
26 typedef long long ftype;
                                                           4 // Update - update element at position id to a value
28 struct Segtree {
      vector<ftype> seg, d, e;
                                                           6 // Problem:
29
      const ftype NEUTRAL = 0;
                                                           7 // https://codeforces.com/edu/course/2/lesson/4/1/
                                                                practice/contest/273169/problem/C
3.1
      int n:
32
                                                          9 // Complexity:
33
      Segtree(int n) {
          this -> n = n;
                                                          10 // O(log n) for both query and update
34
35
                                                          12 // How to use:
36
37
      ftype f(ftype a, ftype b) {
                                                          13 // Segtree seg = Segtree(n);
                                                          14 // seg.build(v);
38
          return a + b;
39
                                                          15
                                                          16 #define pii pair<int, int>
40
      ftype create() {
                                                          17 #define mp make_pair
41
          seg.push_back(0);
                                                          18 #define ff first
42
          e.push_back(0);
                                                          19 #define ss second
43
          d.push_back(0);
44
           return seg.size() - 1;
                                                          21 const int INF = 1e9+17;
45
46
                                                          23 typedef pii ftype;
      ftype query(int pos, int ini, int fim, int p, int 24
48
       q) {
                                                          25 struct Segtree {
          if (q < ini || p > fim) return NEUTRAL;
                                                                vector < ftype > seg;
49
                                                          26
          if (pos == 0) return 0;
                                                          27
                                                                 int n;
5.0
                                                                 const ftype NEUTRAL = mp(INF, 0);
51
          if (p <= ini && fim <= q) return seg[pos];
                                                          28
          int m = (ini + fim) >> 1;
52
           return f(query(e[pos], ini, m, p, q), query(d30
                                                                 Segtree(int n) {
       [pos], m + 1, fim, p, q));
                                                          3.1
                                                                     int sz = 1;
                                                                     while (sz < n) sz *= 2;
54
                                                                     this -> n = sz;
      int update(int pos, int ini, int fim, int id, int 34
56
       val) {
                                                                     seg.assign(2*sz, NEUTRAL);
          int novo = create();
                                                                 }
57
                                                          36
                                                          37
58
```

```
ftype f(ftype a, ftype b) {
38
                                                          107
39
           if (a.ff < b.ff) return a;
                                                          108
                                                                  void build(vector<int> &v) {
           if (b ff < a ff) return b;
                                                                     build(0, 0, n - 1, v);
40
                                                          109
                                                          110
41
           return mp(a ff, a ss + b ss);
                                                          111
                                                                  void debug() {
43
                                                          112
                                                                      for (auto e : seg) {
44
                                                          113
                                                                          cout << e ff << ' ' << e ss << '\n';
       ftype query(int pos, int ini, int fim, int p, int114
45
        q) {
                                                          115
           if (ini >= p && fim <= q) {
                                                                      cout << '\n';
46
                                                          116
               return seg[pos];
47
                                                          117
                                                          118 };
49
                                                                   Range Query Point Update
                                                              3.6
           if (q < ini || p > fim) {
50
               return NEUTRAL;
5.1
52
                                                           1 // Description:
                                                            2 // Indexed at zero
           int e = 2*pos + 1;
54
                                                            _3 // Query - get sum of elements from range (1, r)
           int d = 2*pos + 2;
                                                                  inclusive
           int m = ini + (fim - ini) / 2;
                                                            _{4} // Update - update element at position id to a value
56
57
                                                                  val
           return f(query(e, ini, m, p, q), query(d, m + 5
        1, fim, p, q));
                                                            6 // Problem:
59
                                                            7 // https://codeforces.com/edu/course/2/lesson/4/1/
6.0
                                                                 practice/contest/273169/problem/B
       void update(int pos, int ini, int fim, int id,
61
       int val) {
                                                            9 // Complexity:
           if (ini > id || fim < id) {
62
                                                           10 // O(log n) for both query and update
               return;
           }
64
                                                           12 // How to use:
                                                           13 // Segtree seg = Segtree(n);
65
           if (ini == id && fim == id) {
66
                                                           14 // seg.build(v);
               seg[pos] = mp(val, 1);
                                                           15
                                                           16 // Notes
               return:
69
                                                           17 // Change neutral element and f function to perform a
           }
                                                                  different operation
7.1
                                                           18
           int e = 2*pos + 1;
72
                                                           _{\rm 19} // If you want to change the operations to point
           int d = 2*pos + 2;
                                                                  query and range update
           int m = ini + (fim - ini) / 2;
74
                                                           _{
m 20} // Use the same segtree, but perform the following
75
                                                                 operations
           update(e, ini, m, id, val);
                                                           21 // Query - seg.query(0, id);
7.6
           update(d, m + 1, fim, id, val);
                                                           22 // Update - seg.update(1, v); seg.update(r + 1, -v);
                                                           23
           seg[pos] = f(seg[e], seg[d]);
79
                                                           24 typedef long long ftype;
       }
80
                                                           25
8.1
                                                           26 struct Segtree {
       void build(int pos, int ini, int fim, vector < int > 27
                                                                vector<ftype> seg;
        & v ) {
                                                           28
                                                                  int n;
83
           if (ini == fim) {
                                                                  const ftype NEUTRAL = 0;
                                                           29
               if (ini < (int)v.size()) {</pre>
84
                                                           30
                    seg[pos] = mp(v[ini], 1);
85
                                                                  Segtree(int n) {
                                                           31
               }
                                                                     int sz = 1;
                                                           32
               return:
87
                                                                      while (sz < n) sz *= 2;
                                                           33
           }
88
                                                                      this -> n = sz;
                                                           3.4
89
                                                           35
           int e = 2*pos + 1;
90
                                                                      seg.assign(2*sz, NEUTRAL);
                                                           36
           int d = 2*pos + 2;
                                                           37
           int m = ini + (fim - ini) / 2;
92
                                                           38
93
                                                                  ftype f(ftype a, ftype b) {
                                                           39
94
           build(e, ini, m, v);
                                                           40
                                                                      return a + b;
           build(d, m + 1, fim, v);
95
                                                           41
                                                           42
           seg[pos] = f(seg[e], seg[d]);
97
                                                           43
                                                                  ftype query(int pos, int ini, int fim, int p, int
99
                                                                      if (ini >= p && fim <= q) {
       ftype query(int p, int q) {
100
                                                           45
                                                                          return seg[pos];
101
          return query(0, 0, n - 1, p, q);
                                                           46
102
                                                           47
103
                                                                      if (q < ini || p > fim) {
                                                           48
       void update(int id, int val) {
104
                                                                          return NEUTRAL;
           update(0, 0, n - 1, id, val);
105
                                                           5.0
106
                                                           51
```

```
int e = 2*pos + 1;
                                                           2 // Query - get sum of segment that is maximum among
52
53
           int d = 2*pos + 2;
                                                                  all segments
           int m = ini + (fim - ini) / 2;
                                                            з // Е.g
54
                                                            4 // Array: 5 -4 4 3 -5
           return f(query(e, ini, m, p, q), query(d, m + 5 // Maximum segment sum: 8 because 5 + (-4) + 4 = 8
                                                            6 // Update - update element at position id to a value
        1, fim, p, q));
58
                                                            8 // Problem:
       void update(int pos, int ini, int fim, int id,
59
                                                            9 // https://codeforces.com/edu/course/2/lesson/4/2/
       int val) {
          if (ini > id || fim < id) {
                                                                  practice/contest/273278/problem/A
60
61
               return;
                                                           11 // Complexity:
62
                                                           _{12} // O(log n) for both query and update
63
           if (ini == id && fim == id) {
64
                                                           13
                                                           _{14} // How to use:
               seg[pos] = val;
65
                                                           15 // Segtree seg = Segtree(n);
66
                                                           16 // seg.build(v);
               return:
67
           }
                                                           18 // Notes
69
           int e = 2*pos + 1;
                                                           19 // The maximum segment sum can be a negative number
70
           int d = 2*pos + 2;
                                                           20 // In that case, taking zero elements is the best
71
           int m = ini + (fim - ini) / 2;
                                                                  choice
72
                                                           21 // So we need to take the maximum between 0 and the
           update(e, ini, m, id, val);
7.4
                                                                 query
7.5
           update(d, m + 1, fim, id, val);
                                                           22 // max(OLL, seg.query(0, n).max_seg)
76
                                                           23
           seg[pos] = f(seg[e], seg[d]);
                                                           24 using ll = long long;
7.7
       }
78
                                                           26 typedef ll ftype node:
7.9
       void build(int pos, int ini, int fim, vector < int > 27
80
        & v ) {
                                                           28 struct Node {
           if (ini == fim) {
                                                                ftype_node max_seg;
81
                                                           29
               if (ini < (int)v size()) {
                                                           30
                                                                  ftype_node pref;
                   seg[pos] = v[ini];
                                                                  ftype_node suf;
83
                                                           31
               }
84
                                                           32
                                                                  ftype_node sum;
85
               return:
                                                           3.3
           }
                                                           34
                                                                  Node(ftype_node max_seg, ftype_node pref,
86
                                                                  ftype_node suf, ftype_node sum) : max_seg(max_seg
           int e = 2*pos + 1;
                                                                  ), pref(pref), suf(suf), sum(sum) {};
88
           int d = 2*pos + 2;
89
                                                           35 };
           int m = ini + (fim - ini) / 2;
90
                                                           36
                                                           37 typedef Node ftype;
92
           build(e, ini, m, v);
                                                           38
           build(d, m + 1, fim, v);
                                                           39 struct Segtree {
93
                                                           40
                                                                  vector < ftype > seg;
94
           seg[pos] = f(seg[e], seg[d]);
                                                                  int n;
9.5
                                                           41
       }
                                                           42
                                                                  const ftype NEUTRAL = Node(0, 0, 0, 0);
97
                                                           43
       ftype query(int p, int q) {
                                                           44
                                                                  Segtree(int n) {
98
           return query(0, 0, n - 1, p, q);
                                                                      int sz = 1;
99
                                                           45
                                                                      // potencia de dois mais proxima
100
                                                           46
                                                                      while (sz < n) sz *= 2;
                                                           47
       void update(int id, int val) {
                                                                      this -> n = sz:
102
                                                           48
           update(0, 0, n - 1, id, val);
103
                                                           49
                                                                      // numero de nos da seg
104
                                                           5.0
                                                                      seg assign(2*sz, NEUTRAL);
                                                           51
105
       void build(vector<int> &v) {
                                                           52
106
107
          build(0, 0, n - 1, v);
                                                           53
                                                                  ftype f(ftype a, ftype b) {
108
                                                           54
                                                                      ftype_node max_seg = max({a.max_seg, b.
109
                                                           55
       void debug() {
                                                                  max_seg, a suf + b pref});
110
           for (auto e : seg) {
                                                                      ftype_node pref = max(a.pref, a.sum + b.pref)
111
                                                           56
               cout << e << ' ';
112
113
                                                                      ftype_node suf = max(b.suf, b.sum + a.suf);
           cout << '\n';
                                                                      ftype_node sum = a sum + b sum;
114
                                                           58
                                                           59
115
116 };
                                                                      return Node(max_seg, pref, suf, sum);
                                                           60
                                                           61
         Segment With Maximum Sum
                                                           62
                                                                  ftype query(int pos, int ini, int fim, int p, int
                                                           63
                                                                      if (ini >= p && fim <= q) {
                                                           64
 1 // Description:
```

```
cout << e max_seg << ' ' ' << e pref << ' '</pre>
        return seg[pos];
                                                   134
    }
                                                            << e.suf << ' ' << e.sum << '\n';
                                                   135
    if (q < ini || p > fim) {
                                                               cout << '\n';
                                                   136
        return NEUTRAL;
                                                   137
                                                   138 }:
                                                           Dynamic Implicit Sparse
    int e = 2*pos + 1;
    int d = 2*pos + 2;
    int m = ini + (fim - ini) / 2;
                                                    1 // Description:
                                                    2 // Indexed at one
    return f(query(e, ini, m, p, q), query(d, m + 3
1, fim, p, q));
                                                    4 // When the indexes of the nodes are too big to be
                                                          stored in an array
                                                    5 // and the queries need to be answered online so we
void update(int pos, int ini, int fim, int id,
                                                          can't sort the nodes and compress them
int val) {
                                                    _{6} // we create nodes only when they are needed so there
    if (ini > id || fim < id) {
                                                          'll be (Q*log(MAX)) nodes
        return:
                                                    _{7} // where Q is the number of queries and MAX is the
                                                          maximum index a node can assume
    if (ini == id && fim == id) {
                                                    9 // Query - get sum of elements from range (1, r)
        seg[pos] = Node(val, val, val, val);
                                                          inclusive
                                                    10 // Update - update element at position id to a value
        return:
                                                          val
    }
                                                    1.1
                                                    12 // Problem:
    int e = 2*pos + 1;
                                                   13 // https://cses.fi/problemset/task/1648
    int d = 2*pos + 2;
    int m = ini + (fim - ini) / 2;
                                                   15 // Complexity:
                                                   _{16} // O(log n) for both query and update
    update(e, ini, m, id, val);
                                                    17
    update(d, m + 1, fim, id, val);
                                                    _{18} // How to use:
                                                    19 // MAX is the maximum index a node can assume
    seg[pos] = f(seg[e], seg[d]);
                                                    20 // Create a default null node
                                                    21 // Create a node to be the root of the segtree
void build(int pos, int ini, int fim, vector \langle int \rangle_{23} // Segtree seg = Segtree(MAX);
 &v) {
                                                   24 // seg.create();
    if (ini == fim) {
                                                   25 // seg.create();
        // se a caposio existir no array original cap 26
        // seg tamanho potencia de dois
                                                   27 typedef long long ftype;
        if (ini < (int)v.size()) {</pre>
            seg[pos] = Node(v[ini], v[ini], v[ini<sub>29</sub> const int MAX = 1e9+17;
], v[ini]);
                                                   30
        }
                                                   31 struct Segtree {
        return:
                                                   32
                                                          vector < ftype > seg, d, e, lazy;
    }
                                                          const ftype NEUTRAL = 0;
                                                   3.3
                                                   34
                                                          int n:
    int e = 2*pos + 1;
                                                   3.5
    int d = 2*pos + 2;
                                                   36
                                                          Segtree(int n) {
    int m = ini + (fim - ini) / 2;
                                                   37
                                                              this -> n = n;
                                                   38
    build(e, ini, m, v);
                                                   39
    build(d, m + 1, fim, v);
                                                          ftype f(ftype a, ftype b) {
                                                   40
                                                   41
                                                              return a + b;
    seg[pos] = f(seg[e], seg[d]);
                                                   42
}
                                                   43
                                                          ftype create() {
                                                   44
ftype query(int p, int q) {
                                                   45
                                                              seg.push_back(0);
   return query(0, 0, n - 1, p, q);
                                                   46
                                                              e.push_back(0);
                                                   47
                                                              d.push_back(0);
                                                   48
                                                              return seg.size() - 1;
void update(int id, int val) {
                                                   49
    update(0, 0, n - 1, id, val);
                                                   5.0
                                                          ftype query(int pos, int ini, int fim, int p, int
                                                   51
                                                           q) {
void build(vector<int> &v) {
                                                              if (q < ini || p > fim) return NEUTRAL;
   build(0, 0, n - 1, v);
                                                   53
                                                              if (pos == 0) return 0;
                                                               if (p <= ini && fim <= q) return seg[pos];</pre>
                                                   54
                                                               int m = (ini + fim) >> 1;
                                                    55
void debug() {
                                                               return f(query(e[pos], ini, m, p, q), query(d
                                                    56
   for (auto e : seg) {
                                                           [pos], m + 1, fim, p, q));
```

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7.2

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7.5

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126

127

128

129

130

131

132

```
}
                                                                       seg.assign(2*sz, NEUTRAL);
5.7
                                                           32
                                                           33
                                                                       lazy.assign(2*sz, NEUTRAL_LAZY);
58
       void update(int pos, int ini, int fim, int id,
59
                                                           34
      int val) {
                                                           3.5
                                                                   ftype apply_lazy(ftype a, ftype b, int len) {
           if (ini > id || fim < id) {
               return:
                                                                       if (b == NEUTRAL_LAZY) return a;
61
                                                           37
                                                                       if (a == NEUTRAL_LAZY) return b * len;
62
                                                           38
                                                                       else return a + b * len;
63
                                                           3.9
           if (ini == fim) {
64
                                                           40
               seg[pos] = val;
                                                           41
                                                                  void propagate(int pos, int ini, int fim) {
66
                                                           42
               return;
                                                           43
                                                                      if (ini == fim) {
           }
68
                                                           44
                                                                           return:
                                                           45
69
           int m = (ini + fim) >> 1;
7.0
                                                           46
                                                                       int e = 2*pos + 1;
71
                                                           47
                                                                       int d = 2*pos + 2;
72
           if (id <= m) {
               if (e[pos] == 0) e[pos] = create();
                                                                       int m = ini + (fim - ini) / 2;
7.3
                                                           49
               update(e[pos], ini, m, id, val);
           } else {
                                                                       lazy[e] = apply_lazy(lazy[e], lazy[pos], 1);
7.5
                                                           5.1
               if (d[pos] == 0) d[pos] = create();
                                                           52
                                                                       lazy[d] = apply_lazy(lazy[d], lazy[pos], 1);
76
               update(d[pos], m + 1, fim, id, val);
                                                           53
77
                                                                      seg[e] = apply_lazy(seg[e], lazy[pos], m -
78
                                                           54
                                                                  ini + 1);
           seg[pos] = f(seg[e[pos]], seg[d[pos]]);
                                                                       seg[d] = apply_lazy(seg[d], lazy[pos], fim -
80
                                                           5.5
                                                                  m):
81
82
                                                           56
      ftype query(int p, int q) {
                                                                       lazy[pos] = NEUTRAL_LAZY;
83
                                                           57
          return query(1, 1, n, p, q);
                                                           58
                                                                  }
84
8.5
                                                           5.9
                                                                  ftype f(ftype a, ftype b) {
                                                           60
86
       void update(int id, int val) {
87
                                                           6.1
                                                                      return a + b;
          update(1, 1, n, id, val);
88
                                                           62
89
                                                           63
90 }:
                                                                  ftype query(int pos, int ini, int fim, int p, int
                                                           64
  3.9 Lazy
                                                                       propagate(pos, ini, fim);
                                                           6.5
                                                           66
                                                                       if (ini >= p && fim <= q) {
1 // Description:
                                                                           return seg[pos];
2 // Query - get sum of elements from range (1, r)
                                                           68
      inclusive
_3 // Update - add a value val to elementos from range ( ^{70}
      l, r) inclusive
                                                                       if (q < ini || p > fim) {
                                                           71
                                                           72
                                                                           return NEUTRAL;
5 // Problem:
                                                           73
6 // https://codeforces.com/edu/course/2/lesson/5/1/
                                                           74
                                                                       int e = 2*pos + 1;
      practice/contest/279634/problem/A
                                                           7.5
                                                                       int d = 2*pos + 2;
                                                                       int m = ini + (fim - ini) / 2;
8 // Complexity:
                                                           7.7
                                                           78
9 // O(log n) for both query and update
                                                           79
                                                                       return f(query(e, ini, m, p, q), query(d, m +
11 // How to use:
                                                                   1, fim, p, q));
12 // Segtree seg = Segtree(n);
                                                           80
13 // seg.build(v);
                                                           8.1
                                                                  void update (int pos, int ini, int fim, int p, int
14
                                                                   q, int val) {
15 // Notes
                                                                      propagate(pos, ini, fim);
_{16} // Change neutral element and f function to perform a ^{83}
                                                           84
       different operation
                                                           85
                                                                       if (ini > q || fim < p) {
                                                           86
                                                                           return;
18 typedef long long ftype;
                                                                       }
                                                           87
19
                                                           88
20 struct Segtree {
                                                           89
                                                                       if (ini >= p && fim <= q) {
      vector < ftype > seg;
2.1
                                                                           lazy[pos] = apply_lazy(lazy[pos], val, 1)
      vector < ftype > lazy;
                                                           90
23
      int n;
       const ftype NEUTRAL = 0;
                                                                           seg[pos] = apply_lazy(seg[pos], val, fim
                                                           91
                                                                   - ini + 1);
25
       const ftype NEUTRAL_LAZY = -1;
                                                           92
                                                                           return;
                                                           93
      Segtree(int n) {
                                                                       }
          int sz = 1;
                                                           94
28
           while (sz < n) sz *= 2;
                                                           95
                                                                       int e = 2*pos + 1;
           this -> n = sz;
3.0
                                                           97
                                                                       int d = 2*pos + 2;
31
```

```
int m = ini + (fim - ini) / 2:
98
                                                            15 // Complexity:
99
                                                            _{16} // O(log n) for both query and update
           update(e, ini, m, p, q, val);
100
           update(d, m + 1, fim, p, q, val);
101
                                                            1.7
                                                            18 // How to use:
                                                            _{
m 19} // MAX is the maximum index a node can assume
           seg[pos] = f(seg[e], seg[d]);
103
                                                            20 // Create a default null node
104
                                                            21 // Create a node to be the root of the segtree
105
       void build(int pos, int ini, int fim, vector < int > 22
106
        &v) {
                                                            23 // Segtree seg = Segtree(MAX);
           if (ini == fim) {
                                                            24 // seg.create();
107
                if (ini < (int)v.size()) {</pre>
                                                            25 // seg.create();
                    seg[pos] = v[ini];
109
                                                            26
                                                            27 typedef long long ftype;
110
111
                return:
                                                            28
           }
                                                            29 const int MAX = 1e9+17;
112
113
           int e = 2*pos + 1;
                                                            31 typedef long long ftype;
114
           int d = 2*pos + 2;
           int m = ini + (fim - ini) / 2;
                                                            33 const int MAX = 1e9+17;
116
117
                                                            34
           build(e, ini, m, v);
                                                            35 struct Segtree {
118
                                                                  vector < ftype > seg, d, e, lazy;
           build(d, m + 1, fim, v);
119
                                                            36
                                                                   const ftype NEUTRAL = 0;
                                                            37
           seg[pos] = f(seg[e], seg[d]);
                                                                   const ftype NEUTRAL_LAZY = -1;
121
                                                            38
                                                            3.9
                                                                   int n:
122
123
                                                            40
       ftype query(int p, int q) {
                                                                   Segtree(int n) {
124
                                                            41
           return query(0, 0, n - 1, p, q);
                                                                       this \rightarrow n = n:
                                                            42
126
                                                            43
127
                                                            44
                                                                   ftype apply_lazy(ftype a, ftype b, int len) {
       void update(int p, int q, int val) {
128
                                                            45
           update(0, 0, n - 1, p, q, val);
                                                                       if (b == NEUTRAL_LAZY) return a;
129
                                                            46
                                                            47
                                                                        else return b * len;
131
                                                            48
       void build(vector<int> &v) {
132
           build(0, 0, n - 1, v);
                                                                   void propagate(int pos, int ini, int fim) {
133
                                                            5.0
                                                                        if (seg[pos] == 0) return;
134
                                                            51
                                                            52
135
       void debug() {
                                                                        if (ini == fim) {
                                                            53
136
137
           for (auto e : seg) {
                                                            54
                                                                            return;
               cout << e << ' ';
138
                                                            5.5
           cout << '\n';
                                                                        int m = (ini + fim) >> 1;
140
                                                            5.7
           for (auto e : lazy) {
                                                            58
141
                cout << e << ' ';
                                                            59
                                                                        if (e[pos] == 0) e[pos] = create();
142
                                                                        if (d[pos] == 0) d[pos] = create();
143
                                                            6.0
           cout << '\n';
                                                            61
           cout << '\n';</pre>
                                                                       lazy[e[pos]] = apply_lazy(lazy[e[pos]], lazy[
145
                                                            62
                                                                   pos], 1);
146
                                                                       lazy[d[pos]] = apply_lazy(lazy[d[pos]], lazy[
147 };
                                                                   pos], 1);
          Lazy Dynamic Implicit Sparse
                                                            64
                                                                       seg[e[pos]] = apply_lazy(seg[e[pos]], lazy[
                                                            65
                                                                   pos], m - ini + 1);
 1 // Description:
                                                                        seg[d[pos]] = apply_lazy(seg[d[pos]], lazy[
 2 // Indexed at one
                                                                   pos], fim - m);
 _4 // When the indexes of the nodes are too big to be
                                                            67
                                                                        lazy[pos] = NEUTRAL_LAZY;
       stored in an array
                                                            68
                                                            69
 _{5} // and the queries need to be answered online so we
                                                            7.0
       can't sort the nodes and compress them
                                                                   ftype f(ftype a, ftype b) {
 _{6} // we create nodes only when they are needed so there ^{71}
                                                                       return a + b;
       'll be (Q*log(MAX)) nodes
                                                            72
 _{7} // where Q is the number of queries and MAX is the
                                                            73
       maximum index a node can assume
                                                                   ftype create() {
                                                            75
                                                                       seg.push_back(0);
                                                            76
 9 // Query - get sum of elements from range (1, r)
                                                                        e.push_back(0);
       inclusive
                                                                        d.push_back(0);
_{\rm 10} // Update - update element at position id to a value ^{\rm 78}
                                                                        lazy.push_back(-1);
       val
                                                                        return seg.size() - 1;
                                                            80
12 // Problem:
                                                             81
                                                            82
13 // https://oj.uz/problem/view/IZh012_apple
```

```
ftype query(int pos, int ini, int fim, int p, int ^{23} // Notes
83
        q) {
                                                             24 // Indexed at zero
            propagate(pos, ini, fim);
84
                                                             2.5
            if (q < ini || p > fim) return NEUTRAL;
                                                             26 struct Segtree2D {
85
            if (pos == 0) return 0;
                                                                    const int MAXN = 1025;
            if (p <= ini && fim <= q) return seg[pos];</pre>
                                                                    int N, M;
87
                                                             28
            int m = (ini + fim) >> 1;
           return f(query(e[pos], ini, m, p, q), query(d30
                                                                    vector < vector < int >> seg:
89
       [pos], m + 1, fim, p, q));
                                                             31
                                                                    Segtree2D(int N, int M) {
90
                                                             32
                                                                        this -> N = N;
91
                                                             33
        void update(int pos, int ini, int fim, int p, int 34
                                                                         this -> M = M;
        q, int val) {
                                                                         seg.resize(2*MAXN, vector<int>(2*MAXN));
            propagate(pos, ini, fim);
93
                                                             36
            if (ini > q || fim < p) {
94
                                                             37
                return;
                                                                    void buildY (int noX, int lX, int rX, int noY, int
95
                                                             38
96
            }
                                                                     1Y, int rY, vector < vector < int >> &v) {
                                                                         if(1Y == rY){
97
                                                             39
            if (ini >= p && fim <= q) {
                                                                             if(1X == rX){
                lazy[pos] = apply_lazy(lazy[pos], val, 1) 41
                                                                                 seg[noX][noY] = v[rX][rY];
99
                                                                             }else{
                                                                                  seg[noX][noY] = seg[2*noX+1][noY] +
                seg[pos] = apply_lazy(seg[pos], val, fim 43
100
       - ini + 1);
                                                                    seg[2*noX+2][noY];
                                                                             }
                                                                         lelse (
102
                return:
                                                             45
           }
                                                                             int m = (1Y+rY)/2;
103
                                                             46
104
                                                             47
            int m = (ini + fim) >> 1;
                                                                             buildY(noX, 1X, rX, 2*noY+1, 1Y, m, v);
105
                                                             48
                                                                             buildY(noX, 1X, rX, 2*noY+2, m+1, rY, v);
106
                                                             49
            if (e[pos] == 0) e[pos] = create();
107
                                                             5.0
            update(e[pos], ini, m, p, q, val);
                                                                             seg[noX][noY] = seg[noX][2*noY+1] + seg[
108
                                                             51
                                                                    noX][2*noY+2];
109
            if (d[pos] == 0) d[pos] = create();
                                                                        }
110
                                                             52
111
            update(d[pos], m + 1, fim, p, q, val);
                                                             53
112
                                                             54
            seg[pos] = f(seg[e[pos]], seg[d[pos]]);
                                                                    void buildX(int noX, int lX, int rX, vector<</pre>
113
       }
                                                                    vector < int >> &v) {
114
                                                                         if(1X != rX){
115
       ftype query(int p, int q) {
                                                                             int m = (1X+rX)/2;
116
                                                             57
           return query(1, 1, n, p, q);
                                                             58
117
118
                                                             59
                                                                             buildX(2*noX+1, 1X, m, v);
                                                                             buildX(2*noX+2, m+1, rX, v);
119
                                                             6.0
        void update(int p, int q, int val) {
                                                             61
120
121
           update(1, 1, n, p, q, val);
                                                             62
                                                                         buildY(noX, 1X, rX, 0, 0, M - 1, v);
122
                                                             63
123 };
                                                             64
                                                                    }
                                                             65
         Segtree2d
   3.11
                                                                    void updateY(int noX, int 1X, int rX, int noY,
                                                                    int lY, int rY, int y){
                                                                         if(1Y == rY){
                                                             67
 1 // Description:
                                                                             if(1X == rX){
 2 // Indexed at zero
                                                             68
                                                                                 seg[noX][noY] = !seg[noX][noY];
 _{\rm 3} // Given a N x M grid, where i represents the row and ^{\rm 69}
        j the column, perform the following operations \phantom{0000}70\phantom{000}
                                                                                 seg[noX][noY] = seg[2*noX+1][noY] +
 4 // update(j, i) - update the value of grid[i][j]
                                                             7.1
                                                                    seg[2*noX+2][noY];
 _{5} // query(j1, j2, i1, i2) - return the sum of values
                                                                            }
       inside the rectangle
                                                                         }else{
 6 // defined by grid[i1][j1] and grid[i2][j2] inclusive 73
                                                                             int m = (1Y+rY)/2;
                                                             74
 8 // Problem:
                                                             75
                                                                             if(v \le m)
 9 // https://cses.fi/problemset/task/1739/
                                                             76
                                                                                 updateY(noX, 1X, rX, 2*noY+1,1Y, m, y
10
                                                                    );
11 // Complexity:
                                                                             else if(m < y)
12 // Time complexity:
                                                                                 updateY(noX, 1X, rX, 2*noY+2, m+1, rY
13 // O(\log N * \log M) for both query and update
                                                             79
                                                                    , y);
_{14} // O(N * M) for build
                                                                             }
                                                             80
15 // Memory complexity:
16 // 4 * M * N
                                                             81
                                                                             seg[noX][noY] = seg[noX][2*noY+1] + seg[
                                                             82
                                                                    noX][2*noY+2];
18 // How to use:
19 // Segtree2D seg = Segtree2D(n, n);
                                                                        }
20 // vector<vector<int>> v(n, vector<int>(n));
                                                             84
                                                             85
21 // seg.build(v);
                                                                    void updateX(int noX, int 1X, int rX, int x, int
                                                             86
22
```

```
y){
87
           int m = (1X+rX)/2;
                                                            10 string lcsAlgo(string s1, string s2, int m, int n) {
                                                                int LCS_table[m + 1][n + 1];
88
                                                            11
           if(1X != rX){
89
                                                            12
                if(x \le m)
                                                                 for (int i = 0; i <= m; i++) {
                    updateX(2*noX+1, 1X, m, x, y);
                                                                  for (int j = 0; j <= n; j++) {
91
                                                            14
                                                                    if (i == 0 || j == 0)
                else if(m < x)
92
                                                            15
                                                                      LCS_table[i][j] = 0;
                    updateX(2*noX+2, m+1, rX, x, y);
93
                                                            16
                                                                     else if (s1[i - 1] == s2[j - 1])
94
                                                            17
           }
                                                                       LCS_{table}[i][j] = LCS_{table}[i - 1][j - 1] +
                                                                  1:
96
           updateY(noX, 1X, rX, 0, 0, M - 1, y);
                                                                    else
                                                                       LCS_table[i][j] = max(LCS_table[i - 1][j],
98
                                                                  LCS_table[i][j - 1]);
99
       int queryY(int noX, int noY, int lY, int rY, int 21
       aY, int bY) {
           if(aY <= lY && rY <= bY) return seg[noX][noY</pre>
                                                                 int index = LCS_table[m][n];
       1:
                                                                 char lcsAlgo[index + 1];
                                                                lcsAlgo[index] = '\0';
           int m = (1Y + rY)/2;
103
                                                           26
104
                                                                 int i = m, j = n;
           if(bY <= m) return queryY(noX, 2*noY+1, 1Y, m 28
105
       , aY , bY);
                                                                 while (i > 0 & k & j > 0) {
                                                            29
           if(m < aY) return queryY(noX, 2*noY+2, m+1,
                                                                   if (s1[i - 1] == s2[j - 1]) {
       rY, aY, bY);
                                                                    lcsAlgo[index - 1] = s1[i - 1];
                                                            3.1
                                                            32
                                                                     i --:
108
           return queryY(noX, 2*noY+1, lY, m, aY, bY) +
                                                           33
                                                                    j --;
       queryY(noX, 2*noY+2, m+1, rY, aY, bY);
                                                           34
                                                                    index --;
109
                                                            35
110
                                                            36
                                                                   else if (LCS_table[i - 1][j] > LCS_table[i][j -
111
       int queryX(int noX, int 1X, int rX, int aX, int
       bX, int aY, int bY){
                                                                  17)
           if(aX <= 1X && rX <= bX) return queryY(noX,
                                                                    i - - ;
       0, 0, M - 1, aY, bY);
                                                                   else
113
                                                            40
                                                                    j - - ;
           int m = (1X+rX)/2;
                                                                }
114
                                                            41
115
           if(bX <= m) return queryX(2*noX+1, lX, m, aX, 43</pre>
                                                                return lcsAlgo;
116
        bX, aY, bY);
           if (m < aX) return queryX(2*noX+2, m+1, rX, aX
117
       , bX, aY, bY);
                                                              4.2
                                                                   Kmp
118
           return queryX(2*noX+1, lX, m, aX, bX, aY, bY)
119
                                                            1 vector < int > prefix_function(string s) {
        + queryX(2*noX+2, m+1, rX, aX, bX, aY, bY);
                                                                  int n = (int)s.length();
120
                                                                  vector < int > pi(n);
121
                                                                  for (int i = 1; i < n; i++) {
       void build(vector<vector<int>> &v) {
122
                                                                       int j = pi[i-1];
           buildX(0, 0, N - 1, v);
                                                                       while (j > 0 && s[i] != s[j])
124
                                                                           j = pi[j-1];
                                                                       if (s[i] == s[j])
       int query(int aX, int bX, int aY, int bY) {
           return queryX(0, 0, N - 1, aX, bX, aY, bY);
127
                                                                       pi[i] = j;
                                                            10
                                                                  }
                                                            11
129
                                                            12
                                                                  return pi;
       void update(int x, int y) {
130
                                                            13 }
           updateX(0, 0, N - 1, x, y);
131
132
                                                              4.3
                                                                    Trie
133 };
        Strings
                                                            1 const int K = 26;
                                                            3 struct Vertex {
   4.1 Lcs
                                                                  int next[K];
                                                                  bool output = false;
 1 // Description:
                                                                  int p = -1;
 2 // Finds the longest common subsquence between two
                                                                  char pch;
                                                                  int link = -1;
       string
                                                                  int go[K];
 4 // Problem:
                                                                  Vertex(int p=-1, char ch='$') : p(p), pch(ch) {
 _{5} // https://codeforces.com/gym/103134/problem/B
                                                            1.1
                                                                       fill(begin(next), end(next), -1);
 7 // Complexity:
                                                                       fill(begin(go), end(go), -1);
                                                            13
 _{8} // O(mn) where m and n are the length of the strings _{14}
```

```
15 };
                                                                      auto aux = generate_sequences(set, sequence +
                                                           1.0
16
                                                                   set[i], n, k - 1);
17 vector < Vertex > t(1):
                                                                      ans.insert(ans.end(), aux.begin(), aux.end())
                                                           11
18
                                                                      // for (auto e : aux) ans.push_back(e);
19 void add_string(string const& s) {
      int v = 0:
20
                                                           13
      for (char ch : s) {
21
                                                           14
          int c = ch - 'a';
                                                                 return ans:
22
                                                           1.5
           if (t[v].next[c] == -1) {
                                                           16 }
23
               t[v].next[c] = t.size();
^{24}
               t.emplace_back(v, ch);
                                                                    Generate All Permutations
25
26
           }
27
           v = t[v].next[c];
                                                            vector < string > generate_permutations(string s) {
28
                                                                 int n = s.size();
29
       t[v].output = true;
                                                            3
                                                                  vector < string > ans;
30 }
                                                            4
31
                                                                  sort(s.begin(), s.end());
32 int go(int v, char ch);
34 int get_link(int v) {
                                                                      ans.push_back(s);
      if (t[v].link == -1) {
   if (v == 0 || t[v].p == 0)
35
                                                                  } while (next_permutation(s.begin(), s.end()));
                                                           9
36
              t[v].link = 0;
37
                                                                  return ans:
           else
               t[v].link = go(get_link(t[v].p), t[v].pch 12 }
39
      );
                                                                   Algorithms
40
      return t[v].link;
41
42 }
                                                                   Biggest K
                                                             5.1
43
44 int go(int v, char ch) {
      int c = ch - 'a';
45
                                                            1 // Description: Gets sum of k biggest or k smallest
      if (t[v].go[c] == -1) {
46
                                                                  elements in an array
47
           if (t[v].next[c] != -1)
               t[v].go[c] = t[v].next[c];
48
                                                            3 // Problem: https://atcoder.jp/contests/abc306/tasks/
49
                                                                 abc306_e
               t[v].go[c] = v == 0 ? 0 : go(get_link(v), 4
50
        ch);
                                                            5 // Complexity: O(log n)
51
      }
      return t[v].go[c];
52
                                                            7 struct SetSum {
53 }
                                                                 11 s = 0:
                                                                  multiset <11> mt;
                                                            9
  4.4 Z-function
                                                                  void add(11 x){
                                                           10
                                                                      mt.insert(x);
                                                           11
                                                           12
                                                                      s += x;
vector < int > z_function(string s) {
                                                                  }
                                                           13
      int n = (int) s.length();
                                                           14
                                                                  int pop(11 x){
      vector < int > z(n);
                                                                      auto f = mt.find(x);
                                                           1.5
      for (int i = 1, l = 0, r = 0; i < n; ++i) {
                                                           16
                                                                      if(f == mt.end()) return 0;
           if (i \le r)
                                                           17
                                                                      mt.erase(f);
               z[i] = min (r - i + 1, z[i - 1]);
6
                                                                      s -= x;
                                                           18
           while (i + z[i] < n && s[z[i]] == s[i + z[i]]
                                                                      return 1;
                                                           19
      ]])
                                                           20
               ++z[i];
                                                           21 };
           if (i + z[i] - 1 > r)
9
                                                           22
1.0
               1 = i, r = i + z[i] - 1;
                                                           23 struct BigK {
      }
11
                                                           24
                                                                  int k;
      return z:
12
                                                                  SetSum gt, mt;
                                                           25
13 }
                                                                  BigK(int _k){
                                                                      k = _k;
  4.5 Generate All Sequences Length K
                                                           28
                                                                  void balancear(){
1 // gera todas as ípossveis êsequncias usando as letras30
                                                                     while((int)gt.mt.size() < k && (int)mt.mt.
       em set (de comprimento n) e que tenham tamanho k
                                                                  size()){
2 // sequence = ""
                                                                          auto p = (prev(mt.mt.end()));
3 vector<string> generate_sequences(char set[], string 32
                                                                          gt.add(*p);
      sequence, int n, int k) {
                                                           33
                                                                          mt.pop(*p);
     if (k == 0) {
                                                           34
          return { sequence };
                                                                      while((int)mt.mt.size() && (int)gt.mt.size()
                                                           35
                                                                  & &
6
                                                                      *(gt.mt.begin()) < *(prev(mt.mt.end())) ){
     vector < string > ans;
                                                                          11 u = *(gt.mt.begin());
                                                           37
     for (int i = 0; i < n; i++) {
                                                                          11 v = *(prev(mt.mt.end()));
                                                           38
```

```
gt pop(u); mt pop(v);
                                                             return f(1);
                                                                                             //return the
39
40
              gt add(v); mt add(u);
                                                             maximum of f(x) in [1, r]
                                                       14 }
41
      }
42
      void add(ll x){
                                                          5.4 Delta-encoding
      mt.add(x);
44
          balancear();
45
                                                       1 #include <bits/stdc++.h>
46
                                                        2 using namespace std;
      void rem(ll x){
47
         //x = -x;
                                                        4 int main(){
          if(mt.pop(x) == 0)
49
                                                           int n, q;
50
             gt.pop(x);
                                                             cin >> n >> q;
                                                        6
5.1
          balancear();
                                                             int [n];
                                                             int delta[n+2];
53 };
54
                                                       10
                                                             while (q - -) {
55 int main() {
                                                              int 1, r, x;
      ios::sync_with_stdio(false);
                                                       11
56
                                                                  cin >> 1 >> r >> x;
                                                       12
      cin . tie(NULL);
                                                                  delta[1] += x;
                                                       13
                                                                  delta[r+1] -= x;
                                                       14
      int n, k, q; cin >> n >> k >> q;
59
                                                       15
60
                                                       16
      BigK big = BigK(k);
6.1
                                                       17
                                                              int curr = 0;
                                                              for(int i=0; i < n; i++){
                                                       18
      int arr[n] = {};
63
                                                                curr += delta[i];
                                                      19
64
                                                                  v[i] = curr;
                                                      20
      while (q--) {
65
                                                       21
        int pos, num; cin >> pos >> num;
66
                                                       22
          pos --;
                                                              for(int i=0; i < n; i++) {
                                                       23
          big.rem(arr[pos]);
68
                                                                cout << v[i] << '';
                                                      24
          arr[pos] = num;
                                                       2.5
          big.add(arr[pos]);
70
                                                              cout << '\n';
                                                       26
                                                       27
          cout << big gt s << '\n';</pre>
                                                       28
                                                              return 0;
73
                                                       29 }
      return 0;
7.5
                                                          5.5 Lis
76 }
  5.2 Binary Search Last True
                                                       1 int lis(vector < int > const& a) {
                                                        1 int last_true(int lo, int hi, function < bool(int) > f)
                                                             vector < int > d(n, 1);
                                                            for (int i = 0; i < n; i++) {
                                                        4
      {
                                                                 for (int j = 0; j < i; j++) {
                                                        5
    lo--:
                                                                     if (a[j] < a[i])
    while (lo < hi) {
                                                                         d[i] = max(d[i], d[j] + 1);
      int mid = lo + (hi - lo + 1) / 2;
      if (f(mid)) {
                                                                  }
                                                        9
       lo = mid;
                                                       10
      } else {
                                                             int ans = d[0];
                                                       11
        hi = mid - 1;
                                                             for (int i = 1; i < n; i++) {
9
      }
                                                       12
                                                                 ans = max(ans, d[i]);
                                                       13
10
                                                       14
    return lo;
                                                              return ans;
12 }
                                                       15
                                                       16 }
  5.3 Ternary Search
                                                          5.6 Binary Search First True
1 double ternary_search(double 1, double r) {
```


double m1 = 1 + (r - 1) / 3;

double eps = 1e-9;

while (r - 1 > eps) {

r = m2;

limit here

11

}

```
//set the error 1 int first_true(int lo, int hi, function < bool(int) > f)
                               {
                         2 hi++;
                        3 while (lo < hi) {</pre>
                             int mid = lo + (hi - lo) / 2;
                             if (f(mid)) {
                        5
                               hi = mid;
                              } else {
                                lo = mid + 1;
                              }
                        9
                            }
                        10
                        11
                            return lo;
                        12 }
```

Math 6 $_{13}$ // F(n) = a b * F(n - 1) $_{14}$ // F(n - 1) c d F(n - 2) 6.1 Ceil 16 // Another Example: $_{\rm 17}$ // Given a grid 3 x n, you want to color it using 3 1 long long division_ceil(long long a, long long b) { distinct colors so that return 1 + ((a - 1) / b); // if a != 0 $_{18}$ // no adjacent place has the same color. In how many 3 } different ways can you do that? 19 // There are 6 ways for the first column to be 6.2 Sieve Of Eratosthenes colored using 3 distinct colors 20 // ans 6 ways using 2 equal colors and 1 distinct one vector < bool > is_prime(MAX, true); 22 // Adding another column, there are: vector < int > primes; 23 // 3 ways to go from 2 equal to 2 equal $_{\rm 24}$ // 2 ways to go from 2 equal to 3 distinct 4 void sieve() { $_{25}$ // 2 ways to go from 3 distinct to 2 equal is_prime[0] = is_prime[1] = false; for (int i = 2; i < MAX; i++) { 26 // 2 ways to go from 3 distinct to 3 distinct if (is_prime[i]) { primes push_back(i); $_{28}$ // So we star with matrix 6 6 and multiply it by the transition 3 2 and get 18 12 6 6 for (int j = i + i; j < MAX; j += i) 29 // 2 2 is_prime[j] = false; 12 12 } 30 // the we can exponentiate this matrix to find the nth column } 14 } 3.1 32 // Problem: 33 // https://cses.fi/problemset/task/1722/ 6.3 Crt 35 // Complexity: 1 ll crt(const vector < pair < ll, ll >> &vet) { 36 // O(log n) 11 ans = 0, 1 cm = 1;11 a, b, g, x, y; 38 // How to use: for(const auto &p : vet) { $39 // vector < vector < 11 >> v = {{1, 1}, {1, 0}};$ tie(a, b) = p;40 // Matriz transition = Matriz(v); tie(g, x, y) = gcd(lcm, b);41 // cout << fexp(transition, n)[0][1] << '\n'; if((a - ans) % g != 0) return -1; // no solution 43 using ll = long long; ans = ans + x * ((a - ans) / g) % (b / g) *44 45 const int MOD = 1e9+7; lcm = lcm * (b / g);46 ans = (ans % lcm + lcm) % lcm; 47 struct Matriz{ vector < vector < 11 >> mat; 48 return ans; int rows, columns; 13 } 5.0 vector<ll> operator[](int i){ 51 6.4 Check If Bit Is On 52 return mat[i]; 5.3 1 // msb de 0 é undefined 2 #define msb(n) (32 - __builtin_clz(n)) Matriz(vector<vector<11>>& matriz){ 55 3 // #define msb(n) (64 - __builtin_clzll(n)) 56 mat = matriz; 4 // popcount rows = mat.size(); 5.7 5 // turn bit off columns = mat[0].size(); 58 59 7 bool bit_on(int n, int bit) { 6.0 if(1 & (n >> bit)) return true; 6.1 Matriz(int row, int column, bool identity=false){ else return false; rows = row; columns = column; 62 10 } mat.assign(rows, vector<11>(columns, 0)); 63 if(identity) { 64 6.5 Matrix Exponentiation for(int i = 0; i < min(rows,columns); i</pre> 65 ++) { mat[i][i] = 1; 66 1 // Description: 67 $_{2}$ // Calculate the nth term of a linear recursion } 4 // Example Fibonacci: 69 5 // Given a linear recurrence, for example fibonacci Matriz operator * (Matriz a) { 6 // F(n) = n, x <= 17.1 7 // F(n) = F(n - 1) + F(n - 2), x > 1assert(columns == a.rows); 72 vector < vector < ll >> resp(rows, vector < ll > (a. columns, 0)); 9 // The recurrence has two terms, so we can build a matrix 2 x 1 so that for(int i = 0; i < rows; i++){ $_{10}$ // n + 1 = transition * n 75 for(int j = 0; j < a.columns; j++){ for(int k = 0; k < a.rows; k++){ $_{12}$ // (2 x 1) = (2 x 2) * (2 x 1) 7.7

1.0

11

12

13

9

10

1.1

```
resp[i][j] = (resp[i][j] + (mat[i 9
       ][k] * 1LL * a[k][j]) % MOD) % MOD;
79
                                                          11
                                                              return dec;
               }
                                                          12 }
80
           }
                                                          14 long long decimal_to_binary(int n) {
           return Matriz(resp);
82
                                                              long long bin = 0;
83
                                                              int rem, i = 1;
84
                                                          16
       Matriz operator + (Matriz a) {
85
           assert(rows == a.rows && columns == a.columns 18
                                                              while (n!=0) {
                                                               rem = n \% 2;
                                                          19
           vector<vector<ll>> resp(rows, vector<ll>(
                                                                 n /= 2;
       columns,0));
                                                                bin += rem * i;
                                                          21
          for(int i = 0; i < rows; i++){
                                                                i *= 10;
               for(int j = 0; j < columns; j++){</pre>
                                                              }
89
                                                          23
                   resp[i][j] = (resp[i][j] + mat[i][j] 24
90
       + a[i][j]) % MOD;
                                                              return bin;
                                                          26 }
91
                                                                  Multiplicative Inverse
                                                            6.9
           return Matriz(resp);
93
94
95 };
                                                           1 ll extend_euclid(ll a, ll b, ll &x, ll &y) {
96
                                                                if (a == 0)
97 Matriz fexp(Matriz base, 11 exponent){
                                                                 {
                                                           3
       Matriz result = Matriz(base.rows, base.rows, 1);
98
                                                                     x = 0; y = 1;
99
       while(exponent > 0){
                                                                     return b;
           if(exponent & 1LL) result = result * base;
100
                                                                 }
           base = base * base;
101
                                                                11 x1, y1;
           exponent = exponent >> 1;
                                                                11 d = extend_euclid(b%a, a, x1, y1);
       }
103
                                                                x = y1 - (b / a) * x1;
                                                           9
104
       return result;
                                                                 y = x1;
                                                          1.0
105 }
                                                                return d:
                                                          12 }
   6.6 Fast Exponentiation
                                                          13
                                                          14 // gcd(a, m) = 1 para existir solucao
 1 ll fexp(ll b, ll e, ll mod) {
                                                          _{15} // ax + my = 1, ou a*x = 1 (mod m)
      11 res = 1;
                                                          16 ll inv_gcd(ll a, ll m) { // com gcd
       b \% = mod;
                                                          17 11 x, y;
       while(e){
                                                              extend_euclid(a, m, x, y);
                                                          18
          if(e & 1LL)
                                                          19
                                                              return (((x % m) +m) %m);
              res = (res * b) % mod;
                                                          20 }
           e = e >> 1LL;
                                                          21
           b = (b * b) \% mod;
                                                          22 ll inv(ll a, ll phim) { // com phi(m), se m for primo}
 9
       }
                                                                 entao phi(m) = p-1
                                                              ll e = phim -1;
10
       return res;
                                                             return fexp(a, e, MOD);
                                                          24
         Divisors
                                                            6.10 Prime Factors
 vector < long long > all_divisors(long long n) {
    vector < long long > ans;
                                                           1 vector < pair < long long, int >> fatora(long long n) {
     for(long long a = 1; a*a <= n; a++){
                                                              vector < pair < long long, int >> ans;
      if(n % a == 0) {
                                                              for(long long p = 2; p*p <= n; p++) {
 4
                                                           3
         long long b = n / a;
                                                                if(n \% p == 0) {
                                                           4
         ans.push_back(a);
                                                                   int expoente = 0;
         if(a != b) ans.push_back(b);
                                                                   while (n \% p == 0) {
 7
                                                           6
                                                                    n /= p;
    }
 9
                                                           8
                                                                     expoente++;
    sort(ans.begin(), ans.end());
10
                                                          9
11
    return ans;
                                                          10
                                                                   ans.emplace_back(p, expoente);
                                                          11
                                                              }
                                                          12
         Binary To Decimal
                                                              if(n > 1) ans.emplace_back(n, 1);
                                                          1.3
                                                          14
                                                               return ans;
                                                          15 }
 1 int binary_to_decimal(long long n) {
    int dec = 0, i = 0, rem;
                                                                    Linear Diophantine Equation
     while (n!=0) {
                                                          _{1} // int a, b, c, x1, x2, y1, y2; cin >> a >> b >> c >>
      rem = n \% 10;
       n /= 10;
                                                                 x1 >> x2 >> y1 >> y2;
                                                           _2 // int ans = -1;
       dec += rem * pow(2, i);
                                                           _3 // if (a == 0 && b == 0) {
       ++i;
```

```
4 //
         if (c != 0) ans = 0;
                                                          69
5 //
         else ans = (x2 - x1 + 1) * (y2 - y1 + 1);
                                                          70
                                                                 shift_solution(x, y, a, b, (minx - x) / b);
6 // }
                                                                 if (x < minx)</pre>
                                                          7.1
7 // else if (a == 0) {
                                                          72
                                                                     shift_solution(x, y, a, b, sign_b);
                                                                 if (x > maxx)
8 //
        if (c % b == 0 && y1 <= c / b && y2 >= c / b) 73
      ans = (x2 - x1 + 1);
                                                                     return 0:
                                                          74
9 //
                                                                 int 1x1 = x;
         else ans = 0;
                                                          75
10 // }
                                                          7.6
11 // else if (b == 0) {
                                                                 shift_solution(x, y, a, b, (maxx - x) / b);
                                                          7.7
      if (c % a == 0 && x1 <= c / a && x2 >= c / a) 78
                                                                 if (x > maxx)
      ans = (y2 - y1 + 1);
                                                                    shift_solution(x, y, a, b, -sign_b);
                                                          79
13 //
         else ans = 0;
                                                          80
                                                                 int rx1 = x;
14 // }
                                                          8.1
                                                                 shift_solution(x, y, a, b, -(miny - y) / a);
                                                          82
_{16} // Careful when a or b are negative or zero
                                                          83
                                                                 if (y < miny)
                                                                     shift_solution(x, y, a, b, -sign_a);
                                                          84
_{18} // if (ans == -1) ans = find_all_solutions(a, b, c, _{85}
                                                                 if (y > maxy)
      x1, x2, y1, y2);
                                                                     return 0;
                                                          86
19 // cout << ans << '\n';
                                                                 int 1x2 = x;
20
                                                          88
21 // Problems:
                                                                 shift_solution(x, y, a, b, -(maxy - y) / a);
                                                          89
22 // https://www.spoj.com/problems/CEQU/
                                                                 if (y > maxy)
                                                          90
23 // http://codeforces.com/problemsets/acmsguru/problem91
                                                                     shift_solution(x, y, a, b, sign_a);
      /99999/106
                                                                 int rx2 = x;
24
                                                          93
25 // consider trivial case a or b is 0
                                                                 if (1x2 > rx2)
                                                          94
26 int gcd(int a, int b, int& x, int& y) {
                                                          9.5
                                                                     swap(1x2, rx2);
                                                                 int lx = max(lx1, lx2);
      if (b == 0) {
27
                                                          96
          x = 1;
                                                          97
                                                                 int rx = min(rx1, rx2);
          y = 0;
29
                                                          98
                                                                 if (1x > rx)
30
          return a;
      }
3.1
                                                          100
                                                                     return 0;
      int x1, y1;
                                                         101
                                                                 return (rx - lx) / abs(b) + 1;
32
      int d = gcd(b, a \% b, x1, y1);
                                                         102 }
      x = y1;
34
      y = x1 - y1 * (a / b);
                                                                 Misc
                                                             7
      return d:
36
37 }
                                                             7.1 Split
_{\rm 39} // x and y are one solution and g is the gcd, all
      passed as reference
                                                           vector < string > split(string txt, char key = ' '){
40 // minx <= x <= maxx miny <= y <= maxy
                                                                 vector < string > ans;
41 bool find_any_solution(int a, int b, int c, int &x0,
      int &y0, int &g) {
                                                                 string palTemp = "";
      g = gcd(abs(a), abs(b), x0, y0);
42
                                                                 for(int i = 0; i < txt.size(); i++){
                                                           5
      if (c % g) {
43
          return false;
44
                                                                     if(txt[i] == key){
                                                                         if(palTemp.size() > 0){
46
                                                           9
                                                                              ans push_back(palTemp);
47
      x0 *= c / g;
                                                                              palTemp = "";
                                                          10
      y0 *= c / g;
48
                                                                         }
                                                          11
      if (a < 0) x0 = -x0;
49
                                                                     } else{
                                                          12
      if (b < 0) y0 = -y0;
50
                                                                         palTemp += txt[i];
      return true:
5.1
                                                          1.4
52 }
                                                          1.5
53
54 void shift_solution(int & x, int & y, int a, int b,
                                                          17
      int cnt) {
                                                                 if(palTemp.size() > 0)
55
      x += cnt * b;
                                                                     ans.push_back(palTemp);
                                                          19
      y -= cnt * a;
56
                                                          20
57
                                                          21
                                                                 return ans;
                                                          22 }
59 // return number of solutions in the interval
60 int find_all_solutions(int a, int b, int c, int minx,
                                                             7.2
                                                                  Int 128
       int maxx, int miny, int maxy) {
61
      int x, y, g;
      if (!find_any_solution(a, b, c, x, y, g))
62
                                                           1 __int128 read() {
          return 0;
63
                                                                _{-int128} x = 0, f = 1;
      a /= g;
64
                                                                 char ch = getchar();
      b /= g;
65
                                                                 while (ch < '0' || ch > '9') {
                                                                     if (ch == '-') f = -1;
66
      int sign_a = a > 0 ? +1 : -1;
                                                                     ch = getchar();
                                                           6
      int sign_b = b > 0 ? +1 : -1;
```

```
while (ch >= '0' && ch <= '9') {
    x = x * 10 + ch - '0';
9
         ch = getchar();
10
11
     return x * f;
13 }
14 void print(__int128 x) {
if (x < 0) {
      putchar('-');
16
        x = -x;
18
     if (x > 9) print(x / 10);
19
     putchar(x % 10 + '0');
20
```

Template

Template Clean 8.1

```
8 #define pb push_back
                                                            9 #define mp make_pair
                                                            10 #define ff first
1 // Notes:
2 // Compile and execute
                                                            11 #define ss second
3 // g++ teste.cpp -o teste -std=c++17
                                                           12 #define pii pair <int, int>
4 // ./teste < teste.txt
                                                           13 #define MOD 100000007
                                                            14 #define sqr(x) ((x) * (x))
                                                            15 #define all(x) (x).begin(), (x).end()
6 // Print with precision
_{7} // cout << fixed << setprecision(12) << value << endl _{16} #define FOR(i, j, n) for (int i = j; i < n; i++)
                                                           17 #define qle(i, n) (i == n ? "\n" : " ")
                                                           18 #define endl "\n"
9 // File as input and output
                                                           19 const int oo = 1e9;
10 // freopen("input.txt", "r", stdin);
11 // freopen("output.txt", "w", stdout);
                                                           20 const int MAX = 1e6;
                                                           21
                                                           22 int32_t main(){ optimize;
13 #include <bits/stdc++.h>
                                                           23
14 using namespace std;
                                                           24
                                                                 return 0;
                                                           25 }
16 int main() {
```

17

18

19

21

22

23 }

ios::sync_with_stdio(false);

5 #define optimize std::ios::sync_with_stdio(false);

cin.tie(NULL);

return 0;

8.2 Template

2 using namespace std;

4 #define int long long

cin.tie(NULL); 6 #define vi vector <int> 7 #define ll long long

1 #include <bits/stdc++.h>