

Notebook - Maratona de Programação

Lenhadoras de Segtree

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1 Math 38 // How to use: $39 // vector < vector < 11>> v = {{1, 1}, {1, 0}};$ 40 // Matriz transition = Matriz(v); 1.1 Ceil 41 // cout << fexp(transition, n)[0][1] << '\n'; 1 long long division_ceil(long long a, long long b) { 43 using ll = long long; return 1 + ((a - 1) / b); // if a != 0 45 const int MOD = 1e9+7; 3 } 46 1.2 To Decimal 47 struct Matriz{ vector < vector < 11 >> mat; 48 int rows, columns; const string digits { "0123456789 50 ABCDEFGHIJKLMNOPQRSTUVWXYZ" }; vector<ll> operator[](int i){ 51 52 return mat[i]; 3 long long to_decimal(const string& rep, long long 53 base) { long long n = 0; Matriz(vector < vector < 11 >> & matriz) { 55 mat = matriz; for (auto c : rep) { rows = mat.size(); 57 n *= base; columns = mat[0].size(); 58 n += digits.find(c); 59 60 Matriz(int row, int column, bool identity=false){ 61 return n; rows = row; columns = column; 62 12 } 63 mat.assign(rows, vector<11>(columns, 0)); 64 if(identity) { 1.3 Matrix Exponentiation for(int i = 0; i < min(rows, columns); i</pre> 65 ++) { mat[i][i] = 1; 1 // Description: 66 } $_{2}$ // Calculate the nth term of a linear recursion 67 } 68 4 // Example Fibonacci: 69 5 // Given a linear recurrence, for example fibonacci Matriz operator * (Matriz a) { 6 // F(n) = n, x <= 171 assert(columns == a.rows); 7 // F(n) = F(n - 1) + F(n - 2), x > 1vector < vector < 11 >> resp(rows, vector < 11 > (a. 73 $_{\rm 9}$ // The recurrence has two terms, so we can build a columns, 0)); matrix 2 x 1 so that for(int i = 0; i < rows; i++){</pre> $_{10}$ // n + 1 = transition * n 75 76 for (int j = 0; j < a.columns; j++) { for (int k = 0; k < a.rows; k++) { $_{12}$ // (2 x 1) = (2 x 2) * (2 x 1) 77 resp[i][j] = (resp[i][j] + (mat[i $_{13}$ // F(n) = a b * F(n - 1) 78 $_{14}$ // F(n - 1) c d F(n - 2)][k] * 1LL * a[k][j]) % MOD) % MOD; 79 } 16 // Another Example: } $_{\rm 17}$ // Given a grid 3 x n, you want to color it using 3 81 return Matriz(resp); distinct colors so that $_{18}$ // no adjacent place has the same color. In how many 83 different ways can you do that? Matriz operator + (Matriz a) { 19 // There are 6 ways for the first column to be assert(rows == a.rows && columns == a.columns colored using 3 distinct colors 86 20 // ans 6 ways using 2 equal colors and 1 distinct one vector < vector < ll >> resp(rows, vector < ll > (87 columns,0)); $_{22}$ // Adding another column, there are: for(int i = 0; i < rows; i++){</pre> 23 // 3 ways to go from 2 equal to 2 equal for(int j = 0; j < columns; j++){</pre> 89 24 // 2 ways to go from 2 equal to 3 distinct resp[i][j] = (resp[i][j] + mat[i][j] $_{25}$ // 2 ways to go from 3 distinct to 2 equal $_{26}$ // 2 ways to go from 3 distinct to 3 distinct + a[i][j]) % MOD; 91 $_{28}$ // So we star with matrix 6 6 and multiply it by the 92 return Matriz(resp); 93 transition 3 2 and get $18\ 12$ 6 6 2 2 95 }: 12 12 $_{ m 30}$ // the we can exponentiate this matrix to find the 97 Matriz fexp(Matriz base, 11 exponent){ nth column Matriz result = Matriz(base.rows, base.rows, 1); 98 while(exponent > 0){ 32 // Problem: 99 if(exponent & 1LL) result = result * base; 33 // https://cses.fi/problemset/task/1722/ 100 base = base * base; 101

9

10

35 // Complexity:

36 // O(log n)

102

103 104 exponent = exponent >> 1;

return result;

```
105
                                                           6 // }
                                                           7 // else if (a == 0) {
   1.4 Crt
                                                                if (c % b == 0 && y1 <= c / b && y2 >= c / b)
                                                           8 //
                                                                 ans = (x2 - x1 + 1);
                                                                   else ans = 0;
 1 ll crt(const vector < pair < ll, ll >> & vet) {
                                                          10 // }
       11 \text{ ans} = 0, 1cm = 1;
                                                          11 // else if (b == 0) {
       ll a, b, g, x, y;
                                                          12 //
                                                                if (c % a == 0 && x1 <= c / a && x2 >= c / a)
       for(const auto &p : vet) {
                                                               ans = (y2 - y1 + 1);
           tie(a, b) = p;
                                                          13 //
                                                                   else ans = 0;
           tie(g, x, y) = gcd(lcm, b);
                                                          14 // }
           if((a - ans) % g != 0) return -1; // no
       solution
                                                          16 // Careful when a or b are negative or zero
         ans = ans + x * ((a - ans) / g) % (b / g) *
                                                          _{18} // if (ans == -1) ans = find_all_solutions(a, b, c,
           lcm = lcm * (b / g);
 a
                                                                x1, x2, y1, y2);
           ans = (ans \% lcm + lcm) \% lcm;
10
                                                          19 // cout << ans << '\n';
11
       return ans:
12
                                                          21 // Problems:
13 }
                                                          22 // https://www.spoj.com/problems/CEQU/
                                                          23 // http://codeforces.com/problemsets/acmsguru/problem
         Binary To Decimal
                                                                /99999/106
                                                          _{25} // consider trivial case a or b is 0
 int binary_to_decimal(long long n) {
                                                          26 int gcd(int a, int b, int& x, int& y) {
    int dec = 0, i = 0, rem;
                                                          27
                                                                 if (b == 0) {
                                                                     x = 1;
     while (n!=0) {
                                                          28
                                                                     y = 0;
      rem = n \% 10;
                                                          29
       n /= 10;
                                                                     return a;
                                                          30
                                                                 }
      dec += rem * pow(2, i);
                                                          31
       ++i;
                                                          32
                                                                 int x1, y1;
                                                                int d = gcd(b, a % b, x1, y1);
                                                          33
                                                                 x = y1;
                                                          34
10
    return dec:
                                                          35
                                                                 y = x1 - y1 * (a / b);
                                                                 return d:
                                                          36
12 }
                                                          37 }
13
14 long long decimal_to_binary(int n) {
                                                          38
   long long bin = 0;
                                                          39 // x and y are one solution and g is the gcd, all
15
    int rem, i = 1;
                                                                passed as reference
                                                          _{40} // minx <= x <= maxx miny <= y <= maxy
17
    while (n!=0) {
                                                          41 bool find_any_solution(int a, int b, int c, int &x0,
18
      rem = n \% 2;
                                                                int &y0, int &g) {
19
      n /= 2;
                                                                 g = gcd(abs(a), abs(b), x0, y0);
20
      bin += rem * i;
                                                          43
                                                                 if (c % g) {
       i *= 10;
                                                                    return false;
                                                          44
22
                                                          45
                                                                 }
23
24
                                                          46
     return bin;
                                                          47
                                                                x0 *= c / g;
25
                                                                 y0 *= c / g;
26 }
                                                          48
                                                          49
                                                                 if (a < 0) x0 = -x0;
   1.6 Fast Exponentiation
                                                          50
                                                                 if (b < 0) y0 = -y0;
                                                                 return true;
                                                          51
                                                          52 }
 1 11 fexp(11 b, 11 e, 11 mod) {
                                                          53
      ll res = 1;
                                                          54 void shift_solution(int & x, int & y, int a, int b,
       b \% = mod;
 3
                                                                int cnt) {
       while(e){
                                                                x += cnt * b;
                                                          55
          if(e & 1LL)
                                                                 y -= cnt * a;
                                                          56
              res = (res * b) % mod;
                                                          57 }
           e = e >> 1LL;
           b = (b * b) \% mod;
                                                          59 // return number of solutions in the interval
       }
 9
                                                          60 int find_all_solutions(int a, int b, int c, int minx,
       return res;
10
                                                                 int maxx, int miny, int maxy) {
11 }
                                                                 int x, y, g;
                                                          61
                                                          62
                                                                 if (!find_any_solution(a, b, c, x, y, g))
   1.7 Linear Diophantine Equation
                                                                    return 0:
                                                          63
                                                                 a /= g;
 _1 // int a, b, c, x1, x2, y1, y2; cin >> a >> b >> c >> ^{65}
                                                                 b /= g;
                                                          66
        x1 >> x2 >> y1 >> y2;
                                                                 int sign_a = a > 0 ? +1 : -1;
 _2 // int ans = -1;
                                                          67
                                                                int sign_b = b > 0 ? +1 : -1;
 _3 // if (a == 0 && b == 0) {
                                                          68
 4 //
         if (c != 0) ans = 0;
          else ans = (x2 - x1 + 1) * (y2 - y1 + 1);
                                                          70
                                                                 shift_solution(x, y, a, b, (minx - x) / b);
```

```
if (x < minx)
                                                                 for (int i = 2; i < MAX; i++) {
71
                                                           6
72
           shift_solution(x, y, a, b, sign_b);
                                                           7
                                                                     if (is_prime[i]) {
       if (x > maxx)
73
                                                                         primes.push_back(i);
74
          return 0;
       int lx1 = x;
                                                                          for (int j = i + i; j < MAX; j += i)
                                                                              is_prime[j] = false;
76
                                                          11
       shift_solution(x, y, a, b, (maxx - x) / b);
                                                                     }
                                                          12
       if (x > maxx)
78
                                                          13
          shift_solution(x, y, a, b, -sign_b);
                                                          14 }
79
       int rx1 = x;
80
                                                                    Horner Algorithm
                                                             1.10
81
       shift_solution(x, y, a, b, -(miny - y) / a);
       if (y < miny)</pre>
83
                                                           1 // Description:
           shift_solution(x, y, a, b, -sign_a);
                                                           _2 // Evaluates y = f(x)
84
85
       if (y > maxy)
          return 0;
86
                                                           4 // Problem:
87
       int 1x2 = x;
                                                           5 // https://onlinejudge.org/index.php?option=
88
                                                                 com_onlinejudge&Itemid=8&page=show_problem&
       shift_solution(x, y, a, b, -(maxy - y) / a);
                                                                 problem=439
90
       if (y > maxy)
           shift_solution(x, y, a, b, sign_a);
                                                           7 // Complexity:
91
       int rx2 = x;
92
                                                           8 // O(n)
93
       if (1x2 > rx2)
                                                          10 using polynomial = std::vector<int>;
          swap(1x2, rx2);
95
                                                          11
       int 1x = max(1x1, 1x2);
96
                                                          12 polynomial p \{6, -5, 2\}; // p(x) = x^2 - 5x + 6;
       int rx = min(rx1, rx2);
97
                                                          13
98
                                                          14 int degree(const polynomial& p) {
       if (lx > rx)
99
                                                              return p.size() - 1;
                                                          15
          return 0:
100
                                                          16 }
       return (rx - lx) / abs(b) + 1;
101
                                                          17
102 }
                                                          18 int evaluate(const polynomial& p, int x) {
                                                              int y = 0, N = degree(p);
       Function Root
                                                               for (int i = N; i >= 0; --i) {
                                                              y *= x;
                                                          22
 const ld EPS1 = 1e-9; // iteration precision error
                                                                 y += p[i];
                                                          23
 2 const ld EPS2 = 1e-4; // output precision error
                                                          24
 4 ld f(ld x) {
                                                               return y;
    // \exp(-x) == e^{-x}
     return p * exp(-x) + q * sin(x) + r * cos(x) + s * 27 }
       tan(x) + t * x * x + u;
                                                             1.11 Multiplicative Inverse
                                                           1 ll extend_euclid(ll a, ll b, ll &x, ll &y) {
 9 ld root(ld a, ld b) {
                                                           2
                                                                 if (a == 0)
    while (b - a >= EPS1) {
                                                                 {
      1d c = (a + b) / 2.0;
                                                           3
11
                                                                     x = 0; y = 1;
                                                           4
       1d y = f(c);
                                                           5
                                                                     return b:
13
                                                           6
       if (y < 0) b = c;
14
                                                                 11 x1, y1;
                                                           7
      else a = c;
15
                                                                 11 d = extend_euclid(b%a, a, x1, y1);
                                                           8
16
                                                                 x = y1 - (b / a) * x1;
                                                           9
17
                                                                 y = x1;
                                                          10
     return (a + b) / 2;
18
                                                          11
                                                                 return d;
19 }
                                                          12 }
20
                                                          13
21 int main() {
                                                          14 // gcd(a, m) = 1 para existir solucao
   ld ans = root(0, 1);
                                                          _{15} // ax + my = 1, ou a*x = 1 (mod m)
    if (abs(f(ans)) <= EPS2) cout << fixed <<</pre>
                                                          16 ll inv_gcd(ll a, ll m) { // com gcd
      setprecision(4) << ans << '\n';</pre>
     else cout << "No solution\n";</pre>
                                                          17 11 x, y;
                                                               extend_euclid(a, m, x, y);
                                                          18
25
                                                               return (((x \% m) + m) \%m);
                                                          19
     return 0;
26
                                                          20 }
                                                          22 ll inv(ll a, ll phim) { // com phi(m), se m for primo
         Sieve Of Eratosthenes
                                                                  entao phi(m) = p-1
                                                              11 e = phim - 1;
 1 vector < bool > is_prime(MAX, true);
                                                               return fexp(a, e, MOD);
                                                          24
 vector < int > primes;
```

25 }

4 void sieve() {

is_prime[0] = is_prime[1] = false;

Representation Arbitrary Base

```
for (i = 0; i \le n; i++) {
     ABCDEFGHIJKLMNOPQRSTUVWXYZ" };
                                                         6
                                                                   for (w = 0; w \le W; w++) {
                                                                       if (i == 0 | | w == 0)
                                                                           K[i][w] = 0;
3 string representation(int n, int b) {
                                                                       else if (wt[i - 1] \le w)
  string rep;
                                                                           K[i][w] = max(val[i - 1] +
                                                        10
                                                                               K[i - 1][w - wt[i - 1]], K[i -
                                                        11
     rep.push_back(digits[n % b]);
                                                               17[w]);
      n /= b;
                                                        12
                                                                           K[i][w] = K[i - 1][w];
    } while (n);
                                                        13
                                                                   }
10
                                                        14
   reverse(rep.begin(), rep.end());
                                                        16
                                                               int res = K[n][W];
   return rep;
                                                        17
14 }
                                                        18
                                                               cout << res << endl;</pre>
                                                        19
        Divisors
  1.13
                                                               w = W;
                                                               for (i = n; i > 0 \&\& res > 0; i--) {
                                                        21
                                                                   if (res == K[i - 1][w])
vector < long long > all_divisors(long long n) {
                                                                       continue;
                                                        23
   vector < long long > ans;
                                                                   else {
                                                        24
    for(long long a = 1; a*a <= n; a++){
                                                                       cout << " " << wt[i - 1];
                                                        25
     if(n \% a == 0) {
4
                                                                       res = res - val[i - 1];
                                                        26
        long long b = n / a;
                                                                       w = w - wt[i - 1];
                                                        27
        ans.push_back(a);
                                                        28
        if(a != b) ans.push_back(b);
                                                        29
                                                        30 }
   }
9
                                                        31
   sort(ans.begin(), ans.end());
                                                        32 int main()
   return ans;
                                                        33 ₹
                                                               int val[] = { 60, 100, 120 };
                                                        34
                                                               int wt[] = { 10, 20, 30 };
                                                        35
  1.14 Check If Bit Is On
                                                               int W = 50;
                                                        36
                                                               int n = sizeof(val) / sizeof(val[0]);
1 // msb de 0 é undefined
                                                        38
                                                               knapsack(W, wt, val, n);
_2 #define msb(n) (32 - __builtin_clz(n))
_3 // #define msb(n) (64 - __builtin_clzll(n) )
                                                        40
4 // popcount
                                                        41
                                                               return 0;
5 // turn bit off
                                                        42 }
                                                           2.2 Substr Palindrome
7 bool bit_on(int n, int bit) {
      if(1 & (n >> bit)) return true;
      else return false;
                                                         1 // êvoc deve informar se a substring de S formada
10 }
                                                               pelos elementos entre os indices i e j
                                                         2 // é um palindromo ou ãno.
  1.15 Prime Factors
                                                         4 char s[MAX];
                                                         5 int calculado[MAX][MAX]; // inciado com false, ou 0
vector < pair < long long, int >> fatora(long long n) {
                                                         6 int tabela[MAX][MAX];
   vector < pair < long long, int >> ans;
    for(long long p = 2; p*p <= n; p++) {
                                                         8 int is_palin(int i, int j){
      if(n \% p == 0) {
                                                         9 if(calculado[i][j]){
        int expoente = 0;
                                                              return tabela[i][j];
                                                        10
        while (n \% p == 0) {
                                                             }
                                                        11
        n /= p;
                                                             if(i == j) return true;
                                                        12
          expoente++;
                                                             if(i + 1 == j) return s[i] == s[j];
                                                        13
        }
        ans.emplace_back(p, expoente);
10
                                                             int ans = false;
                                                        15
11
                                                        16
                                                            if(s[i] == s[j]){
12
    }
                                                              if(is_palin(i+1, j-1)){
                                                        17
    if(n > 1) ans.emplace_back(n, 1);
13
                                                                 ans = true;
                                                        18
    return ans;
                                                        19
15 }
                                                             }
                                                             calculado[i][j] = true;
                                                        21
       DP
                                                             tabela[i][j] = ans;
                                                        22
                                                        23
                                                             return ans;
  2.1 Knapsack With Index
                                                                Edit Distance
                                                           2.3
void knapsack(int W, int wt[], int val[], int n) {
      int i, w;
                                                         1 // Description:
```

1 const string digits { "0123456789

int K[n + 1][W + 1];

3

 $_{2}$ // Minimum number of operations required to transform

a string into another

```
3 // Operations allowed: add character, remove
                                                         10 // menor - ja pegou um numero menor que um digito de
      character, replace character
                                                          _{\rm 11} // qt - quantidade de digitos nao nulos
                                                          12 int dp(int i, bool menor, int qt){
5 // Parameters:
_{6} // str1 - string to be transformed into str2
                                                                 if(qt > 3) return 0;
                                                                 if(i >= r.size()) return 1;
7 // str2 - string that str1 will be transformed into
                                                          14
8 // m - size of str1
                                                                 if(tab[i][menor][qt] != -1) return tab[i][menor][
                                                          15
9 // n - size of str2
                                                                 qt];
                                                          16
11 // Problem:
                                                                 int dr = r[i]-'0';
                                                          17
12 // https://cses.fi/problemset/task/1639
                                                                 int res = 0;
                                                          18
                                                          19
14 // Complexity:
                                                                 for(int d = 0; d <= 9; d++) {</pre>
                                                          20
15 // O(m x n)
                                                                     int dnn = qt + (d > 0);
                                                          21
                                                                     if(menor == true) {
                                                          22
17 // How to use:
                                                                         res += dp(i+1, true, dnn);
                                                          23
18 // memset(dp, -1, sizeof(dp));
                                                                     }
19 // string a, b;
                                                                     else if(d < dr) {</pre>
20 // edit_distance(a, b, (int)a.size(), (int)b.size()); 26
                                                                         res += dp(i+1, true, dnn);
22 // Notes:
                                                                     else if(d == dr) {
                                                          28
_{23} // Size of dp matriz is m x n
                                                                         res += dp(i+1, false, dnn);
                                                          29
                                                          30
25 int dp[MAX][MAX];
                                                          32
27 int edit_distance(string &str1, string &str2, int m, 33
                                                                 return tab[i][menor][qt] = res;
      int n) {
      if (m == 0) return n;
      if (n == 0) return m;
                                                                  Coins
29
                                                            2.6
30
      if (dp[m][n] != -1) return dp[m][n];
                                                          1 int tb[1005];
32
      if (str1[m - 1] == str2[n - 1]) return dp[m][n] = 2 int n;
33
                                                          3 vector <int> moedas;
       edit_distance(str1, str2, m - 1, n - 1);
      return dp[m][n] = 1 + min({edit_distance(str1,
34
      str2, m, n - 1), edit_distance(str1, str2, m - 1, 5 int dp(int i){
                                                           6 \quad if(i >= n)
       n), edit_distance(str1, str2, m - 1, n - 1)});
                                                              if(tb[i] != -1)
                                                                return tb[i];
  2.4 Knapsack
                                                              tb[i] = max(dp(i+1), dp(i+2) + moedas[i]);
                                                          1.1
int val[MAXN], peso[MAXN], dp[MAXN][MAXS];
                                                          12
                                                              return tb[i];
                                                          13 }
3 int knapsack(int n, int m){ // n Objetos | Peso max
                                                          14
      for(int i=0;i<=n;i++){
                                                          15 int main(){
         for (int j=0; j <= m; j++) {
                                                             memset(tb,-1,sizeof(tb));
                                                          16
              if(i==0 \text{ or } j==0)
                   dp[i][j] = 0;
               else if(peso[i-1]<=j)</pre>
                                                                 Minimum Coin Change
                                                            2.7
                   dp[i][j] = max(val[i-1]+dp[i-1][j-
9
      peso[i-1]], dp[i-1][j]);
10
              else
                                                          vector <int> valores;
                   dp[i][j] = dp[i-1][j];
         }
12
                                                          4 int tabela[1005];
13
      return dp[n][m];
14
15 }
                                                           6 int dp(int k){
                                                              if(k == 0){
  2.5 Digits
                                                                 return 0;
                                                              if(tabela[k] != -1)
                                                          10
_{1} // achar a quantidade de numeros menores que R que
                                                                return tabela[k];
                                                          11
      possuem no maximo 3 digitos nao nulos
                                                               int melhor = 1e9;
                                                          12
2 // a ideia eh utilizar da ordem lexicografica para
                                                              for(int i = 0; i < n; i++){
                                                          13
      checar isso pois se temos por exemplo
                                                                 if(valores[i] <= k)</pre>
                                                          14
_3 // o numero 8500, a gente sabe que se pegarmos o
                                                                   melhor = min(melhor,1 + dp(k - valores[i]));
                                                          15
      numero 7... qualquer digito depois do 7
                                                              }
                                                          16
_4 // sera necessariamente menor q 8500
                                                              return tabela[k] = melhor;
                                                          17
                                                          18 }
6 string r;
7 int tab[20][2][5];
                                                            2.8
                                                                   Kadane
```

 $_{9}$ // i - digito de R

```
1 // achar uma subsequencia continua no array que a
      soma seja a maior possivel
2 // nesse caso vc precisa multiplicar exatamente 1
      elemento da subsequencia
3 // e achar a maior soma com isso
5 int n, x, arr[MAX], tab[MAX][2]; // tab[maior
      resposta no intervalo][foi multiplicado ou ãno] 13 #define MOD 1000000007
7 int dp(int i, bool mult) {
      if (i == n-1) {
          if (!mult) return arr[n-1]*x;
          return arr[n-1];
10
11
      if (tab[i][mult] != -1) return tab[i][mult];
13
14
      int res;
15
      if (mult) {
          res = max(arr[i], arr[i] + dp(i+1, 1));
17
18
      else {
19
         res = max({
20
             arr[i]*x,
              arr[i]*x + dp(i+1, 1),
22
              arr[i] + dp(i+1, 0)
23
24
          });
25
      return tab[i][mult] = res;
27
28 }
29
30 int main() {
      memset(tab, -1, sizeof(tab));
32
      int ans = -00:
34
     for (int i = 0; i < n; i++) {
35
          ans = max(ans, dp(i, 0));
36
37
38
      return 0;
39
40 }
41
44 int ans = a[0], ans_1 = 0, ans_r = 0;
45 int sum = 0, minus_pos = -1;
47 for (int r = 0; r < n; ++r) {
      sum += a[r];
      if (sum > ans) {
49
         ans = sum;
          ans_l = minus_pos + 1;
51
          ans_r = r;
52
53
     if (sum < 0) {
54
          sum = 0;
55
56
          minus_pos = r;
58 }
```

3 Template

Template 3.1

```
#include <bits/stdc++.h>
2 using namespace std;
4 #define int long long
5 #define optimize std::ios::sync_with_stdio(false);
     cin.tie(NULL);
```

```
6 #define vi vector<int>
 7 #define ll long long
 8 #define pb push_back
 9 #define mp make_pair
 10 #define ff first
 11 #define ss second
 12 #define pii pair <int, int>
 14 #define sqr(x) ((x) * (x))
 15 #define all(x) (x).begin(), (x).end()
 _{16} #define FOR(i, j, n) for (int i = j; i < n; i++) _{\phantom{0}}
 17 #define qle(i, n) (i == n ? "\n" : "
 18 #define endl "\n"
 19 const int oo = 1e9;
20 const int MAX = 1e6;
 22 int32_t main(){ optimize;
        return 0;
 25 }
    3.2
          Template Clean
```

```
1 // Notes:
2 // Compile and execute
_3 // g++ teste.cpp -o teste -std=c++17
4 // ./teste < teste.txt
6 // Print with precision
7 // cout << fixed << setprecision(12) << value << endl
9 // File as input and output
10 // freopen("input.txt", "r", stdin);
11 // freopen("output.txt", "w", stdout);
13 #include <bits/stdc++.h>
14 using namespace std;
15
16 int main() {
    ios::sync_with_stdio(false);
17
       cin.tie(NULL);
19
21
22
       return 0;
23 }
```

Strings

4.1 Kmp

```
1 vector < int > prefix_function(string s) {
    int n = (int)s.length();
      vector < int > pi(n);
3
      for (int i = 1; i < n; i++) {
4
          int j = pi[i-1];
5
          while (j > 0 && s[i] != s[j])
              j = pi[j-1];
           if (s[i] == s[j])
8
9
          pi[i] = j;
10
      }
11
12
      return pi;
```

4.2 Generate All Permutations

```
vector < string > generate_permutations(string s) {
int n = s.size();
     vector < string > ans;
```

```
35
5
      sort(s.begin(), s.end());
                                                           36
                                                                  else if (LCS_table[i - 1][j] > LCS_table[i][j -
                                                           37
      do {
           ans.push_back(s);
                                                                    i --;
      } while (next_permutation(s.begin(), s.end()));
                                                                  else
9
                                                           39
10
                                                                    j --;
                                                                }
11
      return ans:
                                                           41
12 }
                                                           42
                                                                return lcsAlgo;
                                                           43
        Generate All Sequences Length K
                                                                    Trie
1 // gera todas as ípossveis êsequncias usando as letras
       em set (de comprimento n) e que tenham tamanho k
2 // sequence = ""
                                                            1 const int K = 26;
3 vector < string > generate_sequences (char set[], string
      sequence, int n, int k) {
                                                            3 struct Vertex {
                                                                  int next[K];
     if (k == 0){
         return { sequence };
                                                                  bool output = false;
                                                                  int p = -1;
                                                                  char pch;
                                                                  int link = -1;
     vector<string> ans;
     for (int i = 0; i < n; i++) {
                                                                  int go[K];
9
          auto aux = generate_sequences(set, sequence + 10
10
                                                                  Vertex(int p=-1, char ch='$') : p(p), pch(ch) {
       set[i], n, k - 1);
          ans.insert(ans.end(), aux.begin(), aux.end()) 12
                                                                      fill(begin(next), end(next), -1);
11
                                                                      fill(begin(go), end(go), -1);
           // for (auto e : aux) ans.push_back(e);
12
                                                           14
     }
                                                           15 };
13
14
                                                           16
                                                           17 vector < Vertex > t(1);
15
     return ans;
16 }
                                                           19 void add_string(string const& s) {
  4.4 Lcs
                                                                  int v = 0;
                                                                  for (char ch : s) {
                                                           21
                                                                      int c = ch - 'a';
                                                           22
1 // Description:
                                                                      if (t[v].next[c] == -1) {
                                                           23
_{\mathrm{2}} // Finds the longest common subsquence between two
                                                                          t[v].next[c] = t.size();
                                                           24
      string
                                                                           t.emplace_back(v, ch);
                                                                      }
                                                           26
4 // Problem:
                                                                      v = t[v].next[c];
5 // https://codeforces.com/gym/103134/problem/B
                                                           29
                                                                  t[v].output = true;
7 // Complexity:
                                                           30 }
_{8} // O(mn) where m and n are the length of the strings
                                                           32 int go(int v, char ch);
10 string lcsAlgo(string s1, string s2, int m, int n) {
                                                           33
    int LCS_table[m + 1][n + 1];
11
                                                           34 int get_link(int v) {
12
                                                           35
                                                                  if (t[v].link == -1) {
    for (int i = 0; i \le m; i++) {
13
                                                                      if (v == 0 || t[v].p == 0)
                                                           36
      for (int j = 0; j \le n; j++) {
14
                                                           37
                                                                           t[v].link = 0;
        if (i == 0 ||
                        j == 0)
                                                                      else
                                                           38
          LCS_table[i][j] = 0;
16
                                                                           t[v].link = go(get_link(t[v].p), t[v].pch
         else if (s1[i - 1] == s2[j - 1])
17
                                                                  );
          LCS_{table}[i][j] = LCS_{table}[i - 1][j - 1] +
18
                                                           40
                                                           41
                                                                  return t[v].link;
                                                           42 }
          LCS_table[i][j] = max(LCS_table[i - 1][j],
20
      LCS_table[i][j - 1]);
                                                           _{\rm 44} int go(int v, char ch) {
21
                                                                  int c = ch - 'a';
                                                           45
    }
22
                                                                  if (t[v].go[c] == -1) {
                                                           46
23
                                                                      if (t[v].next[c] != -1)
                                                           47
    int index = LCS_table[m][n];
24
                                                                           t[v].go[c] = t[v].next[c];
                                                           48
    char lcsAlgo[index + 1];
                                                           49
    lcsAlgo[index] = '\0';
26
                                                                           t[v].go[c] = v == 0 ? 0 : go(get_link(v),
                                                                   ch);
28
    int i = m, j = n;
                                                           51
    while (i > 0 \&\& j > 0) {
29
                                                           52
                                                                  return t[v].go[c];
      if (s1[i - 1] == s2[j - 1]) {
                                                           53 }
        lcsAlgo[index - 1] = s1[i - 1];
31
                                                                    Z-function
                                                              4.6
         j--;
33
```

index --;

```
vector <int> z_function(string s) {
                                                           1 // Description:
      int n = (int) s.length();
                                                           2 // Indexed at zero
      vector < int > z(n);
                                                           _{\rm 3} // Find a centroid, that is a node such that when it
      for (int i = 1, 1 = 0, r = 0; i < n; ++i) {
                                                                 is appointed the root of the tree,
           if (i \le r)
                                                           _4 // each subtree has at most floor(n/2) nodes.
               z[i] = min (r - i + 1, z[i - 1]);
           while (i + z[i] < n && s[z[i]] == s[i + z[i]]
                                                           6 // Problem:
      11)
                                                           7 // https://cses.fi/problemset/task/2079/
               ++z[i];
                                                           9 // Complexity:
           if (i + z[i] - 1 > r)
              1 = i, r = i + z[i] - 1;
                                                          10 // O(n)
10
11
      }
                                                          _{12} // How to use:
12
      return z;
13 }
                                                          13 // get_subtree_size(0);
                                                          14 // cout << get_centroid(0) + 1 << endl;</pre>
  5
       Misc
                                                          16 int n;
                                                          17 vector < int > adj [MAX];
  5.1 Split
                                                          18 int subtree_size[MAX];
                                                          20 int get_subtree_size(int node, int par = -1) {
vector<string> split(string txt, char key = ' '){
                                                              int &res = subtree_size[node];
      vector < string > ans;
                                                               res = 1:
                                                          22
                                                               for (int i : adj[node]) {
      string palTemp = "";
                                                               if (i == par) continue;
                                                          24
      for(int i = 0; i < txt.size(); i++){
                                                          25
                                                                 res += get_subtree_size(i, node);
                                                               }
                                                          26
           if(txt[i] == key){
                                                          27
                                                               return res;
              if(palTemp.size() > 0){
                                                          28 }
                   ans.push_back(palTemp);
                                                          29
                   palTemp = "";
10
                                                          30 int get_centroid(int node, int par = -1) {
               }
11
                                                              for (int i : adj[node]) {
                                                          31
          } else{
12
                                                                 if (i == par) continue;
                                                          32
              palTemp += txt[i];
13
                                                          33
           }
                                                                 if (subtree_size[i] * 2 > n) { return
                                                          34
15
                                                                 get_centroid(i, node); }
16
                                                          35
17
                                                          36
                                                               return node;
      if(palTemp.size() > 0)
18
                                                          37 }
          ans.push_back(palTemp);
                                                          38
20
                                                          39 int main() {
21
      return ans;
                                                              cin >> n;
                                                          40
22 }
                                                               for (int i = 0; i < n - 1; i++) {
                                                          41
                                                          42
                                                               int u, v; cin >> u >> v;
  5.2 Int128
                                                                 u--; v--;
                                                          43
                                                                 adj[u].push_back(v);
                                                          44
                                                                 adj[v].push_back(u);
1 __int128 read() {
                                                          45
      _{-int128} x = 0, f = 1;
      char ch = getchar();
                                                          47
                                                               get_subtree_size(0);
                                                          48
      while (ch < '0' || ch > '9') {
                                                          49
                                                               cout << get_centroid(0) + 1 << endl;</pre>
         if (ch == '-') f = -1;
                                                          50 }
          ch = getchar();
6
                                                                   Bipartite
      while (ch >= '0' && ch <= '9') {
          x = x * 10 + ch - '0';
                                                           1 const int NONE = 0, BLUE = 1, RED = 2;
10
          ch = getchar();
                                                           vector < vector < int >> graph (100005);
11
                                                           3 vector <bool> visited(100005);
12
      return x * f;
13 }
                                                           4 int color[100005];
14 void print(__int128 x) {
      if (x < 0) {
                                                           6 bool bfs(int s = 1){
15
16
          putchar('-');
                                                                 queue <int> q;
          x = -x;
17
                                                           9
                                                                 q.push(s);
18
                                                                 color[s] = BLUE;
      if (x > 9) print(x / 10);
                                                          10
19
      putchar(x % 10 + '0');
                                                          11
20
                                                                 while (not q.empty()){
21 }
                                                          12
                                                          13
                                                                     auto u = q.front(); q.pop();
  6
       Graphs
                                                                     for (auto v : graph[u]){
                                                          15
                                                                          if (color[v] == NONE){
                                                                             color[v] = 3 - color[u];
  6.1 Centroid Find
                                                          17
                                                                              q.push(v);
                                                          18
```

```
_{5} // O(V * E^2) where V is the number of vertex and E
19
20
               else if (color[v] == color[u]){
                                                                  is the number of edges
21
                   return false;
                                                            7 int n;
22
          }
                                                            8 vector < vector < int >> capacity;
                                                           9 vector < vector < int >> adj;
      }
24
                                                           10
      return true:
                                                           int bfs(int s, int t, vector < int >& parent) {
26
27 }
                                                                  fill(parent.begin(), parent.end(), -1);
                                                           12
                                                                  parent[s] = -2;
                                                           13
29 bool is_bipartite(int n){
                                                                  queue < pair < int , int >> q;
                                                           14
                                                                  q.push({s, INF});
      for (int i = 1; i <= n; i++)
31
                                                           16
          if (color[i] == NONE and not bfs(i))
                                                                  while (!q.empty()) {
                                                           17
                                                                      int cur = q.front().first;
33
              return false;
                                                           18
                                                                      int flow = q.front().second;
34
                                                           19
                                                                      q.pop();
35
      return true;
                                                           20
36 }
                                                           21
                                                                      for (int next : adj[cur]) {
  6.3 Prim
                                                                          if (parent[next] == -1 && capacity[cur][
                                                           23
                                                                  next]) {
                                                                               parent[next] = cur;
1 int n;
                                                                               int new_flow = min(flow, capacity[cur
_{2} vector<vector<int>> adj; // adjacency matrix of graph ^{25}
                                                                  ][next]);
_3 const int INF = 1000000000; // weight INF means there _{26}
                                                                               if (next == t)
      is no edge
                                                                                   return new_flow;
                                                           27
                                                                               q.push({next, new_flow});
5 struct Edge {
                                                                          }
                                                           29
      int w = INF, to = -1;
                                                                      }
                                                           30
7 };
                                                                  }
                                                           31
                                                           32
9 void prim() {
                                                           33
                                                                  return 0:
      int total_weight = 0;
10
                                                          34 }
      vector < bool > selected(n, false);
11
                                                           35
      vector < Edge > min_e(n);
                                                           36 int maxflow(int s, int t) {
      min_e[0].w = 0;
13
                                                                  int flow = 0;
                                                           37
14
                                                                  vector < int > parent(n);
                                                           38
      for (int i=0; i < n; ++i) {
15
                                                           39
                                                                  int new_flow;
          int v = -1;
16
           for (int j = 0; j < n; ++j) {
                                                                  while (new_flow = bfs(s, t, parent)) {
                                                           41
              if (!selected[j] && (v == -1 || min_e[j]. 42
18
                                                                      flow += new_flow;
      w < min_e[v].w)
                                                                      int cur = t;
                                                           43
19
                   v = j;
                                                                      while (cur != s) {
          }
20
                                                                          int prev = parent[cur];
                                                           45
21
                                                                           capacity[prev][cur] -= new_flow;
                                                           46
          if (min_e[v].w == INF) {
22
                                                                           capacity[cur][prev] += new_flow;
                                                           47
               cout << "No MST!" << endl;</pre>
                                                                           cur = prev;
                                                           48
               exit(0);
24
          }
                                                                  }
                                                           50
26
                                                           51
          selected[v] = true;
27
                                                           52
                                                                  return flow;
           total_weight += min_e[v].w;
                                                           53 }
           if (min_e[v].to != -1)
29
               cout << v << " " << min_e[v].to << endl;</pre>
                                                                    Floyd Warshall
                                                              6.5
31
           for (int to = 0; to < n; ++to) {
32
                                                            1 #include <bits/stdc++.h>
               if (adj[v][to] < min_e[to].w)</pre>
33
                   min_e[to] = {adj[v][to], v};
34
                                                            3 using namespace std:
           }
                                                            4 using ll = long long;
      }
36
                                                            6 const int MAX = 507;
38
      cout << total_weight << endl;</pre>
                                                            7 const long long INF = 0x3f3f3f3f3f3f3f3f3fLL;
39 }
                                                           9 11 dist[MAX][MAX];
  6.4 Ford Fulkerson Edmonds Karp
                                                           10 int n;
1 // Description:
                                                           12 void floyd_warshall() {
_{2} // Obtains the maximum possible flow rate given a
                                                                for (int i = 0; i < n; i++) {
                                                           13
                                                                      for (int j = 0; j < n; j++) {
      network. A network is a graph with a single
                                                                           if (i == j) dist[i][j] = 0;
      source vertex and a single sink vertex in which
                                                           15
      each edge has a capacity
                                                                           else if (!dist[i][j]) dist[i][j] = INF;
                                                           16
                                                                      }
                                                           17
4 // Complexity:
                                                                  }
                                                           18
```

```
visited[1] = true;
19
                                                            53
20
       for (int k = 0; k < n; k++) {
                                                            54
           for (int i = 0; i < n; i++) {
                                                                while (!q.empty()) {
21
                                                            55
               for (int j = 0; j < n; j++) {
                                                                 auto [v, depth] = q.front();
                                                            56
22
                                                                  q.pop();
                   // trata o caso no qual o grafo tem
                                                                  level_peso[v] = depth;
       arestas com peso negativo
                                                            58
                   if (dist[i][k] < INF && dist[k][j] < 59
       TNF){
                                                                   for (auto [u,d] : adj[v]) {
                        dist[i][j] = min(dist[i][j], dist 61
                                                                     if (!visited[u]) {
25
       [i][k] + dist[k][j]);
                                                                       visited[u] = true;
                   }
                                                                       up[u][0] = v;
26
                                                            63
               }
                                                            64
                                                                       q.push(mp(u, depth + d));
           }
28
                                                            65
       }
                                                                   }
                                                            66
29
30 }
                                                            67
                                                                }
                                                            68 }
  6.6 Lca
                                                            70 int lca(int a, int b) {
1 // Description:
                                                            71
                                                                  // get the nodes to the same level
                                                                  int mn = min(level[a], level[b]);
_{\rm 2} // Find the lowest common ancestor between two nodes ^{\rm 72}
      in a tree
                                                            73
                                                                   for (int j = 0; j \le BITS; j++) {
                                                            74
                                                                    if (a != -1 && ((level[a] - mn) & (1 << j))) a
4 // Problem:
                                                            75
                                                                   = up[a][j];
5 // https://cses.fi/problemset/task/1135
                                                                    if (b != -1 && ((level[b] - mn) & (1 << j))) b
                                                            76
                                                                   = up[b][j];
7 // Complexity:
8 // O(log n)
                                                            77
                                                            78
                                                                   // special case
10 // How to use:
                                                            79
                                                                   if (a == b) return a;
11 // preprocess();
                                                            80
12 // lca(a, b);
                                                            81
                                                                   // binary search
                                                            82
_{14} // Notes
                                                                   for (int j = BITS; j \ge 0; j--) {
                                                            83
_{15} // To calculate the distance between two nodes use
                                                                     if (up[a][j] != up[b][j]) {
                                                                       a = up[a][j];
      the following formula
                                                            85
_{16} // level_peso[a] + level_peso[b] - 2*level_peso[lca(a ^{86}
                                                                       b = up[b][j];
                                                                     }
      , b)]
                                                            87
                                                                   }
18 const int MAX = 2e5+10;
                                                                   return up[a][0];
                                                            89
                                                            90 }
19 const int BITS = 30;
                                                            91
                                                            92 void preprocess() {
21 vector < pii > adj [MAX];
                                                                visited = vector < bool > (MAX, false);
22 vector < bool > visited(MAX);
                                                            93
                                                            94
                                                                find_level();
                                                                visited = vector < bool > (MAX, false);
24 int up[MAX][BITS + 1];
                                                            95
                                                                find_level_peso();
25 int level[MAX];
                                                            96
26 int level_peso[MAX];
                                                            97
                                                                for (int j = 1; j \le BITS; j++) {
                                                                   for (int i = 1; i <= n; i++) {
28 void find_level() {
                                                            99
                                                                     if (up[i][j - 1] != -1) up[i][j] = up[up[i][j -
                                                           100
   queue <pii > q;
29
                                                                    1]][j - 1];
30
    q.push(mp(1, 0));
                                                           101
                                                                }
    visited[1] = true;
                                                           102
32
                                                           103
33
34
    while (!q.empty()) {
                                                                     Bellman Ford
      auto [v, depth] = q.front();
35
       q.pop();
36
       level[v] = depth;
                                                            1 struct edge
37
39
      for (auto [u,d] : adj[v]) {
                                                            3
                                                                   int a, b, cost;
        if (!visited[u]) {
                                                            4 };
40
41
           visited[u] = true;
           up[u][0] = v;
                                                            6 int n. m. v:
42
           q.push(mp(u, depth + 1));
                                                            7 vector <edge > e;
                                                            8 const int INF = 1000000000;
44
      }
45
46
    }
                                                            10 void solve()
47 }
                                                            11 {
                                                                   vector < int > d (n, INF);
                                                            12
49 void find_level_peso() {
                                                                   d[v] = 0;
                                                            13
                                                                   for (int i=0; i < n-1; ++i)
    queue <pii > q;
                                                            14
                                                                       for (int j=0; j < m; ++j)
51
                                                            15
                                                                           if (d[e[j].a] < INF)</pre>
    q.push(mp(1, 0));
52
                                                            16
```

```
d[e[j].b] = min (d[e[j].b], d[e[j].a] 57
                                                                   void augment(ll bottleneck) {
        + e[j].cost);
                                                                       flow += bottleneck;
18 }
                                                                       residual ->flow -= bottleneck;
                                                            59
                                                            60
  6.8 Dinic
                                                            61
                                                                   void reverse(ll bottleneck) {
                                                            62
                                                                       flow -= bottleneck;
1 // Description:
                                                                       residual ->flow += bottleneck;
_{2} // Obtains the maximum possible flow rate given a
                                                            64
       network. A network is a graph with a single
                                                            65
       source vertex and a single sink vertex in which
                                                                   bool operator < (const Edge& e) const {
       each edge has a capacity
                                                            67
                                                            68
                                                                       return true;
4 // Problem:
                                                            69
                                                            70 }:
5 // https://codeforces.com/gym/103708/problem/J
                                                            71
                                                            72 struct Dinic {
7 // Complexity:
_{8} // O(V^2 * E) where V is the number of vertex and E
                                                            73
                                                                   int source;
                                                                   int sink:
       is the number of edges
                                                            74
                                                            75
                                                                   int nodes:
                                                                   11 flow;
10 // Unit network
                                                            76
                                                                   vector < vector < Edge *>> adj;
11 // A unit network is a network in which for any
                                                            77
                                                                   vector <int > level;
       vertex except source and sink either incoming or
                                                            78
                                                                   vector < int > next;
       outgoing edge is unique and has unit capacity (
                                                            79
                                                                   vector < int > reach;
       matching problem).
                                                                   vector < bool > visited;
_{12} // Complexity on unit networks: O(E * sqrt(V))
                                                            81
                                                                   vector < vector < int >> path;
                                                            82
13
14 // Unity capacity networks
                                                            83
                                                                   Dinic(int source, int sink, int nodes) : source(
15 // A more generic settings when all edges have unit
                                                                   source), sink(sink), nodes(nodes) {
       capacities, but the number of incoming and
                                                                       adj.resize(nodes + 1);
       outgoing edges is unbounded
                                                            85
_{16} // Complexity on unity capacity networks: O(E * sqrt( ^{86}
      E))
                                                            87
                                                                   void add_edge(int from, int to, ll capacity) {
                                                            88
18 // How to use:
                                                                       Edge* e1 = new Edge(from, to, capacity);
                                                                       Edge* e2 = new Edge(to, from, 0);
19 // Dinic dinic = Dinic(num_vertex, source, sink);
                                                            90
                                                                       // Edge* e2 = new Edge(to, from, capacity);
20 // dinic.add_edge(vertex1, vertex2, capacity);
                                                            91
                                                                       e1->residual = e2;
21 // cout << dinic.max_flow() << '\n';</pre>
                                                            92
                                                                       e2->residual = e1;
                                                            93
23 #include <bits/stdc++.h>
                                                                       adj[from].pb(e1);
                                                            94
                                                                       adj[to].pb(e2);
                                                            95
                                                            96
                                                                   }
25 #define pb push_back
26 #define mp make_pair
                                                            97
                                                                   bool bfs() {
                                                            98
27 #define pii pair <int, int>
                                                            aa
                                                                       level.assign(nodes + 1, -1);
28 #define ff first
                                                                       queue < int > q;
                                                           100
29 #define ss second
30 #define ll long long
                                                                       q.push(source);
                                                            101
                                                                       level[source] = 0;
                                                           102
32 using namespace std;
                                                                       while (!q.empty()) {
                                                           104
                                                            105
                                                                            int node = q.front();
34 const 11 INF = 1e18+10;
                                                                            q.pop();
                                                            106
35
36 struct Edge {
                                                           107
                                                                            for (auto e : adj[node]) {
      int from;
                                                            108
37
                                                                                if (level[e->to] == -1 && e->
                                                           109
       int to:
                                                                   get_capacity() > 0) {
      11 capacity;
39
                                                                                    level[e->to] = level[e->from] +
                                                            110
       11 flow;
40
                                                                   1;
       Edge* residual;
41
                                                                                    q.push(e->to);
                                                            111
42
       Edge() {}
                                                            112
                                                                                }
                                                                            }
                                                           113
44
                                                                       }
       Edge (int from, int to, ll capacity) : from (from), 114
45
                                                           115
       to(to), capacity(capacity) {
                                                                       return level[sink] != -1;
           flow = 0;
                                                           116
46
47
                                                           117
                                                            118
48
                                                                   11 dfs(int v, 11 flow) {
                                                           119
49
       11 get_capacity() {
                                                                       if (v == sink)
           return capacity - flow;
                                                           120
50
                                                                            return flow;
51
                                                           121
                                                           122
52
                                                                       int sz = adj[v].size();
       11 get_flow() {
                                                            123
53
                                                                       for (int i = next[v]; i < sz; i++) {
           return flow;
                                                           124
                                                                            Edge* e = adj[v][i];
       }
55
                                                            126
                                                                            if (level[e->to] == level[e->from] + 1 &&
56
```

```
e->get_capacity() > 0) {
                                                                                       return bottleneck;
127
                    11 bottleneck = dfs(e->to, min(flow, 194
                                                                                   }
                                                                              }
       e->get_capacity()));
                                                              195
                    if (bottleneck > 0) {
                                                                          }
128
                                                              196
                         e->augment(bottleneck);
                                                              197
                         return bottleneck;
                                                                          return 0:
130
                                                              198
                     }
131
                                                              199
                }
132
                                                              200
                                                                     void print_flow_path() {
133
                                                              201
                next[v] = i + 1;
                                                                          path.clear();
134
                                                              202
            }
                                                                          11 \text{ sent = } -1;
135
                                                              203
                                                                          int id = -1;
136
                                                              204
                                                                          while (sent != 0) {
137
            return 0;
                                                             205
                                                                              visited.assign(nodes + 1, false);
                                                             206
138
139
                                                                              path.pb(vector<int>{});
                                                             207
        11 max_flow() {
                                                                              sent = build_path(source, ++id, INF);
140
                                                             208
141
            flow = 0;
                                                              209
                                                                              path[id].pb(source);
            while(bfs()) {
142
                                                             210
                                                                          path.pop_back();
                next.assign(nodes + 1, 0);
                11 \text{ sent} = -1;
144
                                                             212
                while (sent != 0) {
                                                                          for (int i = 0; i < id; i++) {
                                                             213
145
                     sent = dfs(source, INF);
                                                                               cout << path[i].size() << '\n';</pre>
                                                              214
146
                                                                              reverse(path[i].begin(), path[i].end());
                     flow += sent;
                                                             215
147
                }
                                                                              for (auto e : path[i]) {
                                                              216
            }
                                                                                   cout << e << ' ';
149
                                                             217
            return flow;
                                                              218
150
       }
                                                                              cout << '\n';
151
                                                             219
                                                                          }
                                                              220
       void reachable(int v) {
                                                                     }
153
                                                              221
            visited[v] = true;
                                                             222 }:
154
                                                              223
            for (auto e : adj[v]) {
                                                              224 int main() {
156
                if (!visited[e->to] && e->get_capacity() 225
                                                                      ios::sync_with_stdio(false);
157
       > 0) {
                                                              226
                                                                     cin.tie(NULL);
                     reach.pb(e->to);
158
                                                             227
                     visited[e->to] = true;
                                                                      int n, m; cin >> n >> m;
159
                                                              228
                     reachable(e->to);
160
                                                             229
                                                                     Dinic dinic = Dinic(1, n, n);
                }
                                                             230
161
            }
                                                              231
162
       }
                                                                     for (int i = 1; i \le m; i++) {
                                                              232
163
164
                                                              233
                                                                          int v, u; cin >> v >> u;
        void print_min_cut() {
                                                                          dinic.add_edge(v, u, 1);
165
                                                              234
            reach.clear();
                                                              235
166
167
            visited.assign(nodes + 1, false);
                                                             236
                                                                     cout << dinic.max_flow() << '\n';</pre>
            reach.pb(source);
                                                              237
168
            reachable(source);
                                                              238
                                                                     // dinic.print_min_cut();
169
                                                                     // dinic.print_flow_path();
170
                                                             239
            for (auto v : reach) {
                                                              240
                for (auto e : adj[v]) {
                                                                     return 0;
172
                                                             241
173
                     if (!visited[e->to] && e->
       get_capacity() == 0) {
                                                                      2sat
                                                                 6.9
                         cout << e->from << ' ' ' << e->to
174
        << '\n';
                     }
175
                                                               1 // Description:
                }
176
                                                               _{2} // Solves expression of the type (a v b) ^ (c v d) ^
            }
177
                                                                     (e v f)
178
179
                                                               4 // Problem:
180
       ll build_path(int v, int id, ll flow) {
                                                               5 // https://cses.fi/problemset/task/1684
            visited[v] = true;
181
            if (v == sink) {
182
                                                               7 // Complexity:
                return flow;
183
                                                               _{\rm 8} // O(n + m) where n is the number of variables and m
            }
                                                                     is the number of clauses
184
185
186
            for (auto e : adj[v]) {
                                                              10 #include <bits/stdc++.h>
                if (!visited[e->to] && e->get_flow() > 0) 11 #define pb push_back
187
         {
                                                              12 #define mp make_pair
                     visited[e->to] = true;
188
                                                              13 #define pii pair <int, int>
                     ll bottleneck = build_path(e->to, id, 14 #define ff first
189
         min(flow, e->get_flow()));
                                                              15 #define ss second
                    if (bottleneck > 0) {
190
                         path[id].pb(e->to);
191
                                                              17 using namespace std;
                         e->reverse(bottleneck);
192
                                                              18
```

```
19 struct SAT {
                                                                         scc[v] = component;
                                                             92
20
       int nodes;
                                                             93
                                                                         visited[v] = true;
       int curr = 0;
21
                                                             94
       int component = 0;
                                                             95
                                                                         for (auto u : rev[v]) {
22
                                                                             if (!visited[u]) find_component(u,
       vector < vector < int >> adj;
       vector < vector < int >> rev;
                                                                    component);
24
       vector < vector < int >> condensed;
                                                                         }
       vector<pii> departure;
26
                                                             98
       vector < bool > visited;
27
                                                             99
       vector < int > scc;
                                                                    void topological_order(int v) {
28
                                                             100
       vector < int > order;
                                                                         visited[v] = true;
29
                                                             101
30
       // 1 to nodes
31
                                                             103
                                                                         for (auto u : condensed[v]) {
       // nodes + 1 to 2 * nodes
                                                                             if (!visited[u]) topological_order(u);
32
                                                             104
       SAT(int nodes) : nodes(nodes) {
33
                                                            105
           adj.resize(2 * nodes + 1);
34
                                                             106
35
           rev.resize(2 * nodes + 1);
                                                             107
                                                                         order.pb(v);
                                                                    }
           visited.resize(2 * nodes + 1);
36
                                                             108
           scc.resize(2 * nodes + 1);
                                                                    bool is_possible() {
       }
38
                                                            110
                                                                         component = 0;
39
                                                            111
       void add_imp(int a, int b) {
                                                                         for (int i = 1; i <= 2 * nodes; i++) {
40
                                                             112
           adj[a].pb(b);
                                                                             if (!visited[i]) departure_time(i);
41
                                                            113
           rev[b].pb(a);
42
                                                             114
       }
43
                                                            115
                                                                         sort(departure.begin(), departure.end(),
44
                                                             116
45
       int get_not(int a) {
                                                                    greater < pii > () );
           if (a > nodes) return a - nodes;
46
                                                            117
           return a + nodes;
                                                                         visited.assign(2 * nodes + 1, false);
47
                                                             118
       }
48
                                                             119
                                                                         for (auto [_, node] : departure) {
49
                                                             120
       void add_or(int a, int b) {
                                                                             if (!visited[node]) find_component(node,
50
                                                             121
           add_imp(get_not(a), b);
                                                                    ++component);
51
52
           add_imp(get_not(b), a);
                                                             122
                                                                        }
       }
53
                                                            123
                                                                         for (int i = 1; i <= nodes; i++) {</pre>
                                                             124
                                                                             if (scc[i] == scc[i + nodes]) return
       void add_nor(int a, int b) {
55
                                                             125
56
           add_or(get_not(a), get_not(b));
                                                                    false:
       }
                                                                         }
57
                                                             126
58
                                                             127
59
       void add_and(int a, int b) {
                                                             128
                                                                         return true;
           add_or(get_not(a), b);
60
                                                            129
           add_or(a, get_not(b));
                                                            130
61
           add_or(a, b);
                                                             131
                                                                     int find_value(int e, vector<int> &ans) {
62
                                                                         if (e > nodes && ans[e - nodes] != 2) return
63
                                                             132
                                                                     !ans[e - nodes];
64
                                                                        if (e <= nodes && ans[e + nodes] != 2) return
       void add_nand(int a, int b) {
65
                                                             133
           add_or(get_not(a), b);
                                                                      !ans[e + nodes];
           add_or(a, get_not(b));
67
                                                             134
                                                                         return 0;
           add_or(get_not(a), get_not(b));
68
                                                             135
       }
69
                                                             136
                                                                     vector < int > find_ans() {
70
                                                            137
       void add_xor(int a, int b) {
                                                                         condensed.resize(component + 1);
71
                                                            138
           add_or(a, b);
72
                                                            139
73
           add_or(get_not(a), get_not(b));
                                                                         for (int i = 1; i <= 2 * nodes; i++) {
                                                             140
                                                                             for (auto u : adj[i]) {
74
                                                             141
                                                                                  if (scc[i] != scc[u]) condensed[scc[i
75
                                                             142
       void add_xnor(int a, int b) {
                                                                    ]].pb(scc[u]);
76
77
           add_or(get_not(a), b);
                                                            143
                                                                             }
                                                                         }
           add_or(a, get_not(b));
78
                                                             144
       }
79
                                                             145
                                                                         visited.assign(component + 1, false);
                                                            146
80
       void departure_time(int v) {
81
                                                             147
           visited[v] = true;
                                                                         for (int i = 1; i <= component; i++) {</pre>
82
                                                             148
                                                                             if (!visited[i]) topological_order(i);
           for (auto u : adi[v]) {
84
                                                             150
                if (!visited[u]) departure_time(u);
85
                                                             151
           }
                                                                         reverse(order.begin(), order.end());
86
                                                             152
                                                             153
87
                                                                         // 0 - false
           departure.pb(mp(++curr, v));
                                                             154
       }
                                                                         // 1 - true
89
                                                             155
                                                                         // 2 - no value yet
                                                             156
90
                                                                         vector <int> ans(2 * nodes + 1, 2);
91
       void find_component(int v, int component) {
                                                             157
```

```
22 }
158
            vector < vector < int >> belong (component + 1);
159
                                                             23
                                                             24 bool has_cycle(int N){
160
161
            for (int i = 1; i <= 2 * nodes; i++) {
                                                             25
                belong[scc[i]].pb(i);
                                                                    visited.reset();
163
                                                             27
                                                                     for (int u = 1; u \le N; ++u){
164
                                                             28
            for (auto p : order) {
                                                                         path.clear():
165
                                                             29
                for (auto e : belong[p]) {
                                                                         if (not visited[u] and dfs(u,-1))
166
                                                             30
                    ans[e] = find_value(e, ans);
                                                                             return true;
                                                             31
168
                                                             32
169
            }
                                                             33
170
                                                             34
            return ans;
                                                             35
                                                                    return false;
171
172
       }
                                                             36 }
173 };
                                                                        Cycle Path Recovery
174
175 int main() {
       ios::sync_with_stdio(false);
                                                              1 int n;
       cin.tie(NULL);
177
                                                              vector < vector < int >> adj;
178
                                                              3 vector < char > color;
       int n, m; cin >> n >> m;
179
                                                              4 vector <int> parent;
180
                                                              5 int cycle_start, cycle_end;
       SAT sat = SAT(m);
182
                                                              7 bool dfs(int v) {
       for (int i = 0; i < n; i++) {
183
                                                                    color[v] = 1;
184
            char op1, op2; int a, b; cin >> op1 >> a >>
                                                                    for (int u : adj[v]) {
       op2 >> b;
                                                                         if (color[u] == 0) {
           if (op1 == '+' && op2 == '+') sat.add_or(a, b 10
                                                                             parent[u] = v;
       ):
                                                                             if (dfs(u))
            if (op1 == '-' && op2 == '-') sat.add_or(sat. 12
186
                                                                                 return true;
       get_not(a), sat.get_not(b));
                                                                         } else if (color[u] == 1) {
           if (op1 == '+' && op2 == '-') sat.add_or(a,
187
                                                                             cycle_end = v;
                                                             15
       sat.get_not(b));
                                                                             cycle_start = u;
           if (op1 == '-' && op2 == '+') sat.add_or(sat.
188
                                                                             return true;
                                                             17
       get_not(a), b);
                                                             18
189
                                                                    }
                                                             19
190
                                                                    color[v] = 2;
                                                             20
       if (!sat.is_possible()) cout << "IMPOSSIBLE\n";</pre>
191
                                                             21
                                                                    return false;
       else {
192
                                                             22 }
193
            vector < int > ans = sat.find_ans();
            for (int i = 1; i <= m; i++) {
194
                cout << (ans[i] == 1 ? '+' : '-') << ' '; 24 void find_cycle() {</pre>
195
                                                                    color.assign(n, 0);
196
           7
                                                             26
                                                                    parent.assign(n, -1);
            cout << '\n';</pre>
197
                                                                    cycle_start = -1;
                                                             27
       }
198
                                                             28
199
                                                                     for (int v = 0; v < n; v++) {
                                                             29
200
       return 0;
                                                                         if (color[v] == 0 && dfs(v))
201 }
                                                             31
                                                                             break;
   6.10
          Find Cycle
                                                             32
                                                             33
                                                                    if (cycle_start == -1) {
                                                             34
 1 bitset < MAX > visited;
                                                                         cout << "Acyclic" << endl;</pre>
                                                             35
 vector <int > path;
                                                                    } else {
                                                             36
 3 vector < int > adj[MAX];
                                                             37
                                                                         vector < int > cycle;
                                                                         cycle.push_back(cycle_start);
                                                             38
 5 bool dfs(int u, int p){
                                                                         for (int v = cycle_end; v != cycle_start; v =
                                                             39
                                                                      parent[v])
       if (visited[u]) return false;
                                                                             cycle.push_back(v);
                                                             40
                                                                         cycle.push_back(cycle_start);
                                                             41
       path.pb(u);
 9
                                                                         reverse(cycle.begin(), cycle.end());
                                                             42
10
       visited[u] = true;
                                                             43
11
                                                                         cout << "Cycle found: ";</pre>
       for (auto v : adj[u]){
                                                                         for (int v : cycle)
                                                             45
           if (visited[v] and u != v and p != v){
13
                                                                             cout << v << " ";
14
                path.pb(v); return true;
                                                             47
                                                                         cout << endl;</pre>
15
                                                             48
16
                                                             49 }
            if (dfs(v, u)) return true;
       }
18
                                                                6.12
                                                                        Centroid Decomposition
       path.pop_back();
20
       return false;
                                                              1 int n;
21
```

```
vector<set<int>> adj;
                                                                 if (!flag) cout << "Impossible!\n";</pre>
                                                          75
3 vector < char > ans;
                                                           76
                                                                 else {
                                                                     for (int i = 1; i <= n; i++) {
                                                           77
                                                                         cout << ans[i] << ' ';
5 vector < bool > removed;
                                                           78
                                                                      }
                                                           79
7 vector < int > subtree_size;
                                                                      cout << '\n';
                                                          80
                                                                 }
                                                           81
9 int dfs(int u, int p = 0) {
                                                          82
subtree_size[u] = 1;
                                                                 return 0;
                                                          83
                                                           84 }
    for(int v : adj[u]) {
12
                                                                     Tarjan Bridge
                                                             6.13
      if(v != p && !removed[v]) {
        subtree_size[u] += dfs(v, u);
14
                                                           1 // Description:
15
16
                                                           2 // Find a bridge in a connected unidirected graph
                                                           _{\rm 3} // A bridge is an edge so that if you remove that
17
18
    return subtree_size[u];
                                                                 edge the graph is no longer connected
19 }
                                                           5 // Problem:
21 int get_centroid(int u, int sz, int p = 0) {
                                                           6 // https://cses.fi/problemset/task/2177/
   for(int v : adj[u]) {
22
      if(v != p && !removed[v]) {
                                                           8 // Complexity:
23
        if(subtree_size[v]*2 > sz) {
                                                           _{9} // O(V + E) where V is the number of vertices and E
24
          return get_centroid(v, sz, u);
                                                                 is the number of edges
               }
26
27
                                                          11 int n;
      }
28
                                                           12 vector < vector < int >> adj;
29
                                                          13
    return u;
                                                          14 vector < bool > visited;
30
31 }
                                                          15 vector < int > tin, low;
                                                          16 int timer;
33 char get_next(char c) {
                                                          17
     if (c != 'Z') return c + 1;
                                                          18 void dfs(int v, int p) {
      return '$';
                                                                 visited[v] = true;
36 }
                                                                 tin[v] = low[v] = timer++;
                                                          20
                                                          21
                                                                 for (int to : adj[v]) {
38 bool flag = true;
                                                                     if (to == p) continue;
                                                          22
                                                                     if (visited[to]) {
                                                          23
40 void solve(int node, char c) {
                                                                          low[v] = min(low[v], tin[to]);
    int center = get_centroid(node, dfs(node));
                                                                     } else {
41
                                                          25
      ans[center] = c;
42
                                                                          dfs(to, v);
                                                           26
                                                                          low[v] = min(low[v], low[to]);
      removed[center] = true;
43
                                                          27
                                                                          if (low[to] > tin[v]) {
                                                          28
45
      for (auto u : adj[center]) {
                                                                              IS_BRIDGE(v, to);
           if (!removed[u]) {
46
                                                          30
47
               char next = get_next(c);
                                                                     }
                                                          31
               if (next == '$') {
48
                                                          32
                   flag = false;
                                                          33 }
                   return;
50
                                                          34
51
                                                          35 void find_bridges() {
52
               solve(u, next);
                                                                 timer = 0;
                                                          36
          }
53
                                                          37
                                                                 visited.assign(n, false);
                                                                 tin.assign(n, -1);
      }
                                                          38
55 }
                                                                 low.assign(n, -1);
                                                          39
                                                                 for (int i = 0; i < n; ++i) {
56
                                                           40
57 int32_t main(){
                                                                      if (!visited[i])
                                                           41
      ios::sync_with_stdio(false);
58
                                                                          dfs(i, -1);
                                                          42
      cin.tie(NULL);
59
                                                          43
60
                                                           44 }
61
      cin >> n;
                                                                    Small To Large
                                                             6.14
      adj.resize(n + 1);
62
      ans.resize(n + 1);
63
      removed.resize(n + 1);
      subtree_size.resize(n + 1);
                                                          2 // https://codeforces.com/contest/600/problem/E
65
      for (int i = 1; i \le n - 1; i++) {
67
                                                           4 void process_colors(int curr, int parent) {
          int u, v; cin >> u >> v;
68
           adj[u].insert(v);
                                                               for (int n : adj[curr]) {
69
                                                           6
          adj[v].insert(u);
70
                                                                 if (n != parent) {
                                                                   process_colors(n, curr);
                                                           8
72
      solve(1, 'A');
73
                                                                          if (colors[curr].size() < colors[n].size</pre>
                                                           10
74
                                                                 ()) {
```

```
sum_num[curr] = sum_num[n];
                                                                   }
11
                                                            18
12
                    vmax[curr] = vmax[n];
                                                            19
           swap(colors[curr], colors[n]);
                                                                   for (auto u : adj[v]) {
13
                                                            20
                                                                       if (!visited[u]) dfs(u, depth + 1);
                                                            21
14
                                                            22
         for (auto [item, vzs] : colors[n]) {
16
                                                            23 }
                    if(colors[curr][item]+vzs > vmax[curr 24
17
      1){
                                                            25 int tree_diameter() {
                        vmax[curr] = colors[curr][item] + 26
                                                                   dfs(1, 0);
18
        vzs;
                                                                   max_depth = 0;
                                                            27
                                                                   for (int i = 0; i < MAX; i++) visited[i] = false;</pre>
                        sum_num[curr] = item;
19
                                                            28
20
                   }
                                                            29
                                                                   dfs(max_node, 0);
21
                    else if(colors[curr][item]+vzs ==
                                                            30
                                                                   return max_depth;
       vmax[curr]){
                                                            31 }
22
                        sum_num[curr] += item;
                                                               6.16 Dijkstra
23
24
                    colors[curr][item] += vzs;
25
                                                             1 const int MAX = 2e5+7;
                                                             2 const int INF = 1000000000;
      }
27
                                                             3 vector < vector < pair < int , int >>> adj(MAX);
    }
28
29
                                                             5 void dijkstra(int s, vector<int> & d, vector<int> & p
30 }
                                                                   ) {
                                                                   int n = adj.size();
                                                             6
32
                                                                   d.assign(n, INF);
33 int32_t main() {
                                                             8
                                                                   p.assign(n, -1);
34
                                                             9
    int n; cin >> n;
35
                                                                   d[s] = 0;
                                                            10
36
                                                                   set < pair < int , int >> q;
                                                            11
    for (int i = 1; i <= n; i++) {
37
                                                            12
                                                                   q.insert({0, s});
      int a; cin >> a;
38
                                                                   while (!q.empty()) {
                                                            13
       colors[i][a] = 1;
39
                                                                       int v = q.begin()->second;
                                                            14
           vmax[i] = 1;
40
                                                            15
                                                                        q.erase(q.begin());
41
           sum_num[i] = a;
                                                            16
    }
42
                                                                        for (auto edge : adj[v]) {
                                                            17
43
                                                                            int to = edge.first;
                                                            18
    for (int i = 1; i < n; i++) {
44
                                                                            int len = edge.second;
                                                            19
      int a, b; cin >> a >> b;
45
                                                            20
46
                                                                            if (d[v] + len < d[to]) {</pre>
                                                            21
       adj[a].push_back(b);
47
                                                                                q.erase({d[to], to});
                                                            22
       adj[b].push_back(a);
                                                                                d[to] = d[v] + len;
                                                            23
49
                                                                                p[to] = v;
                                                            24
50
                                                                                q.insert({d[to], to});
                                                            25
    process_colors(1, 0);
51
                                                                            }
                                                            26
52
                                                            27
                                                                        }
    for (int i = 1; i \le n; i++) {
53
                                                                   }
                                                            28
      cout << sum_num[i] << (i < n ? " " : "\n");</pre>
54
                                                            29 }
56
                                                            31 vector < int > restore_path(int s, int t) {
57
      return 0;
                                                            32
                                                                   vector < int > path;
58
                                                            33
59 }
                                                                    for (int v = t; v != s; v = p[v])
                                                            34
60
                                                                       path.push_back(v);
                                                            35
                                                                   path.push_back(s);
                                                            36
          Tree Diameter
  6.15
                                                            37
                                                            38
                                                                   reverse(path.begin(), path.end());
1 #include <bits/stdc++.h>
                                                            39
                                                                   return path;
                                                            40 }
3 using namespace std;
                                                            41
                                                            42 int adj[MAX][MAX];
5 const int MAX = 3e5+17;
                                                            43 int dist[MAX];
                                                            44 int minDistance(int dist[], bool sptSet[], int V) {
                                                                   int min = INT_MAX, min_index;
7 vector < int > adj[MAX];
                                                            45
8 bool visited[MAX];
                                                            46
                                                                    for (int v = 0; v < V; v++)
                                                            47
int max_depth = 0, max_node = 1;
                                                                        if (sptSet[v] == false && dist[v] <= min)</pre>
                                                            48
                                                                            min = dist[v], min_index = v;
11
                                                            49
12 void dfs (int v, int depth) {
                                                            50
       visited[v] = true;
                                                            51
                                                                   return min_index;
                                                            52 }
14
       if (depth > max_depth) {
15
          max_depth = depth;
                                                            54 void dijkstra(int src, int V) {
16
           max_node = v;
                                                            55
17
```

```
bool sptSet[V];
                                                                  bool operator > (const Edge& other) const {
56
                                                           51
57
       for (int i = 0; i < V; i++)
                                                           52
                                                                     return weight > other.weight;
           dist[i] = INT_MAX, sptSet[i] = false;
58
                                                           53
59
                                                           54 };
      dist[src] = 0;
                                                           56 vector < Edge > kruskal (vector < Edge > edges, int n) {
61
       for (int count = 0; count < V - 1; count++) {</pre>
                                                                   vector < Edge > result; // arestas da MST
62
                                                                  long long cost = 0;
           int u = minDistance(dist, sptSet, V);
63
                                                           58
64
                                                           59
           sptSet[u] = true;
                                                           60
                                                                  sort(edges.begin(), edges.end());
66
                                                           61
                                                           62
                                                                  DSU dsu(n);
           for (int v = 0; v < V; v++)
68
                                                           63
               if (!sptSet[v] && adj[u][v]
                                                                   for (auto e : edges) {
                                                           64
                   && dist[u] != INT_MAX
                                                                       if (!dsu.same(e.u, e.v)) {
70
                                                           65
                   && dist[u] + adj[u][v] < dist[v])
                                                                           cost += e.weight;
71
                                                           66
72
                   dist[v] = dist[u] + adj[u][v];
                                                           67
                                                                           result.push_back(e);
                                                                           dsu.unite(e.u, e.v);
73
                                                           68
74 }
                                                                       }
                                                                  }
                                                           70
  6.17
          Kruskall
                                                           71
                                                           72
                                                                  return result;
                                                           73 }
1 struct DSU {
2
      int n;
      vector<int> link, sizes;
                                                                   Geometry
      DSU(int n) {
5
                                                              7.1
                                                                    2d
           this ->n = n;
           link.assign(n+1, 0);
           sizes.assign(n+1, 1);
                                                            1 #define vp vector<point>
                                                            2 #define ld long double
9
           for (int i = 0; i \le n; i++)
                                                            3 const ld EPS = 1e-6;
10
               link[i] = i;
                                                            4 const ld PI = acos(-1);
11
12
                                                            6 // typedef ll cod;
      int find(int x) {
                                                            7 // bool eq(cod a, cod b){ return (a==b); }
14
           while (x != link[x])
                                                            8 typedef ld cod;
15
                                                            9 bool eq(cod a, cod b){ return abs(a - b) <= EPS; }</pre>
              x = link[x];
16
17
                                                           10
           return x;
                                                           11 struct point{
      }
                                                                  cod x, y;
19
                                                           12
                                                                  int id;
20
                                                           13
      bool same(int a, int b) {
                                                                  point(cod x=0, cod y=0): x(x), y(y){}
21
                                                           14
          return find(a) == find(b);
22
                                                           15
                                                                  point operator+(const point &o) const{ return {x+
23
                                                           16
                                                                  o.x, y+o.y}; }
24
25
      void unite(int a, int b) {
                                                            17
                                                                  point operator-(const point &o) const{ return {x-
          a = find(a):
                                                                  o.x, y-o.y}; }
26
           b = find(b);
                                                           18
                                                                  point operator*(cod t) const{ return {x*t, y*t};
28
           if (a == b) return;
                                                                  point operator/(cod t) const{ return {x/t, y/t};
                                                           19
29
           if (sizes[a] < sizes[b])</pre>
                                                                  cod operator*(const point &o) const{ return x * o
31
                                                           20
              swap(a, b);
                                                                  .x + y * o.y; }
32
                                                                  cod operator^(const point &o) const{ return x * o
33
                                                           21
           sizes[a] += sizes[b];
                                                                  .y - y * o.x; }
34
           link[b] = a;
                                                                  bool operator < (const point &o) const{</pre>
35
                                                           22
                                                                      return (eq(x, o.x) ? y < o.y : x < o.x);
36
                                                           23
37 };
                                                                  7
                                                           24
38
                                                           25
                                                                  bool operator == (const point &o) const{
39 struct Edge {
                                                                      return eq(x, o.x) and eq(y, o.y);
                                                           26
40
      int u, v;
                                                           27
      long long weight;
                                                           28
                                                                friend ostream& operator << (ostream& os, point p) {
41
42
                                                           29
                                                                   return os << "(" << p.x << "," << p.y << ")"; }
      Edge() {}
43
                                                           30 }:
44
      Edge(int u, int v, long long weight): u(u), v(v) 32 int ccw(point a, point b, point e){ // -1=dir; 0=
45
       , weight(weight) {}
                                                                  collinear; 1=esq;
                                                                  cod tmp = (b-a)^{-} (e-a); // vector from a to b
46
      bool operator < (const Edge & other) const {</pre>
                                                           34
                                                                  return (tmp > EPS) - (tmp < -EPS);
47
                                                           35 }
          return weight < other.weight;</pre>
49
50
                                                           37 ld norm(point a){ // Modulo
```

```
for(int i=0;i< n/2;i++)
       return sqrt(a * a);
38
                                                           108
39 }
                                                           109
                                                                       if(ccw(a[i], a[i+n/2], c) != 0)
40 cod norm2(point a){
                                                                           return false;
                                                           110
41
       return a * a;
                                                           111
                                                                   return true;
42 }
                                                           112 }
43 bool nulo(point a){
                                                           113
       return (eq(a.x, 0) and eq(a.y, 0));
                                                           114 point mirror(point m1, point m2, point p){
44
45 }
                                                                  // mirror point p around segment m1m2
                                                           115
46 point rotccw(point p, ld a){
                                                                   point seg = m2-m1;
                                                           116
       // a = PI*a/180; // graus
                                                                   1d t0 = ((p-m1)*seg) / (seg*seg);
       return point((p.x*cos(a)-p.y*sin(a)), (p.y*cos(a)118
                                                                   point ort = m1 + seg*t0;
48
       +p.x*sin(a)));
                                                                   point pm = ort-(p-ort);
49 }
                                                            120
                                                                   return pm;
50 point rot90cw(point a) { return point(a.y, -a.x); }; 121 }
51 point rot90ccw(point a) { return point(-a.y, a.x); };122
52
53 ld proj(point a, point b){ // a sobre b
                                                           124 ///////////
       return a*b/norm(b);
                                                           125 // Line //
54
55 }
                                                           126 ///////////
56 ld angle(point a, point b){ // em radianos
                                                           127
       ld ang = a*b / norm(a) / norm(b);
                                                           128 struct line{
57
       return acos(max(min(ang, (ld)1), (ld)-1));
                                                                   point p1, p2;
58
                                                           129
                                                                   cod a, b, c; // ax+by+c = 0;
59 }
                                                           130
60 ld angle_vec(point v){
                                                                   // y-y1 = ((y2-y1)/(x2-x1))(x-x1)
       // return 180/PI*atan2(v.x, v.y); // graus
                                                                   line(point p1=0, point p2=0): p1(p1), p2(p2){
61
                                                           132
                                                                       a = p1.y - p2.y;
b = p2.x - p1.x;
       return atan2(v.x, v.y);
62
                                                           133
63 }
                                                           134
                                                                       c = p1 ^p2;
64 ld order_angle(point a, point b){ // from a to b ccw 135
       (a in front of b)
                                                                   }
       ld aux = angle(a,b)*180/PI;
                                                                   line (cod a=0, cod b=0, cod c=0): a(a), b(b), c(c)
65
                                                            137
       return ((a^b) <= 0 ? aux:360-aux);
66
67 }
                                                                       // Gera os pontos p1 p2 dados os coeficientes
                                                            138
68 bool angle_less(point a1, point b1, point a2, point 139
                                                                       // isso aqui eh um lixo mas quebra um galho
       b2) { // ang(a1,b1) <= ang(a2,b2)
                                                                   kkkkkk
       point p1((a1*b1), abs((a1^b1)));
                                                                       if(b==0){
69
                                                           140
       point p2((a2*b2), abs((a2^b2)));
                                                                           p1 = point(1, -c/a);
70
                                                           141
       return (p1^p2) <= 0;
                                                                           p2 = point(0, -c/a);
71
                                                           142
72 }
                                                           143
                                                                           p1 = point(1, (-c-a*1)/b);
73
                                                           144
74 ld area(vp &p){ // (points sorted)
                                                                           p2 = point(0, -c/b);
                                                           145
75
       1d ret = 0;
                                                           146
                                                                       }
       for(int i=2;i<(int)p.size();i++)</pre>
                                                                   }
76
                                                           147
          ret += (p[i]-p[0])^(p[i-1]-p[0]);
77
                                                           148
78
       return abs(ret/2);
                                                           149
                                                                   cod eval(point p){
79 }
                                                                       return a*p.x+b*p.y+c;
                                                           150
80 ld areaT(point &a, point &b, point &c){
                                                           151
       return abs((b-a)^(c-a))/2.0;
                                                                   bool inside(point p){
81
                                                           152
82 }
                                                                       return eq(eval(p), 0);
83
                                                           154
84 point center(vp &A){
                                                           155
                                                                   point normal(){
       point c = point();
                                                           156
                                                                       return point(a, b);
85
       int len = A.size();
86
                                                           157
       for(int i=0;i<len;i++)</pre>
                                                           158
           c=c+A[i];
                                                                   bool inside_seg(point p){
88
                                                           159
89
       return c/len;
                                                                       return (
                                                           160
                                                                            ((p1-p) ^ (p2-p)) == 0  and
90 }
                                                           161
                                                                            ((p1-p) * (p2-p)) <= 0
91
                                                           162
92 point forca_mod(point p, ld m){
                                                                       ):
                                                           163
93
       1d cm = norm(p):
                                                           164
                                                                   }
94
       if(cm<EPS) return point();</pre>
                                                           165
95
       return point(p.x*m/cm,p.y*m/cm);
                                                           166 };
96 }
                                                           167
                                                           168 // be careful with precision error
97
                                                           169 vp inter_line(line l1, line l2){
98 ld param(point a, point b, point v){
99
       // v = t*(b-a) + a // return t;
                                                           170
                                                                   ld det = l1.a*l2.b - l1.b*l2.a;
                                                                   if(det==0) return {};
       // assert(line(a, b).inside_seg(v));
100
                                                           171
       return ((v-a) * (b-a)) / ((b-a) * (b-a));
                                                           172
                                                                   1d x = (11.b*12.c - 11.c*12.b)/det;
101
102 }
                                                           173
                                                                   1d y = (11.c*12.a - 11.a*12.c)/det;
                                                                   return {point(x, y)};
103
                                                           174
104 bool simetric(vp &a){ //ordered
                                                           175 }
      int n = a.size();
105
                                                           176
       point c = center(a);
                                                           177 // segments not collinear
106
107
       if(n&1) return false;
                                                           178 vp inter_seg(line 11, line 12){
```

```
vp ans = inter_line(l1, l2);
                                                                   1d m2 = norm(p1-p3);
179
                                                           244
                                                                   ld m3 = norm(p1-p2);
       if(ans.empty() or !11.inside_seg(ans[0]) or !12. 245
180
                                                                   point c = (p1*m1 + p2*m2 + p3*m3)*(1/(m1+m2+m3));
       inside_seg(ans[0]))
                                                           246
           return {};
                                                            247
                                                                   ld s = 0.5*(m1+m2+m3);
181
       return ans;
                                                            248
                                                                   1d r = sqrt(s*(s-m1)*(s-m2)*(s-m3)) / s;
                                                                   return circle(c, r);
183 }
                                                            249
184 bool seg_has_inter(line 11, line 12){
                                                            250 }
       return ccw(11.p1, 11.p2, 12.p1) * ccw(11.p1, 11. 251
185
       p2, 12.p2) < 0 and
                                                            252 circle circumcircle(point a, point b, point c) {
               ccw(12.p1, 12.p2, 11.p1) * ccw(12.p1, 12.253
                                                                   circle ans;
           11.p2) < 0;
                                                                   point u = point((b-a).y, -(b-a).x);
                                                            254
187 }
                                                            255
                                                                   point v = point((c-a).y, -(c-a).x);
                                                                   point n = (c-b)*0.5;
188
                                                            256
                                                                   1d t = (u^n)/(v^u);
189 ld dist_seg(point p, point a, point b){ // point -
                                                            257
                                                                   ans.c = ((a+c)*0.5) + (v*t);
                                                            258
       if((p-a)*(b-a) < EPS) return norm(p-a);
                                                                   ans.r = norm(ans.c-a);
190
                                                            259
191
       if((p-b)*(a-b) < EPS) return norm(p-b);
                                                            260
                                                                   return ans;
       return abs((p-a)^(b-a)) / norm(b-a);
                                                            261
192
193 }
                                                            263 vp inter_circle_line(circle C, line L){
194
195 ld dist_line(point p, line l){ // point - line
                                                                   point ab = L.p2 - L.p1, p = L.p1 + ab * ((C.c-L.
                                                            264
                                                                   p1)*(ab) / (ab*ab));
       return abs(1.eval(p))/sqrt(1.a*1.a + 1.b*1.b);
196
197
                                                                   ld s = (L.p2-L.p1)^(C.c-L.p1), h2 = C.r*C.r - s*s
                                                            265
                                                                    / (ab*ab);
                                                                   if (h2 < -EPS) return {};</pre>
199 line bisector(point a, point b){
                                                            266
       point d = (b-a)*2;
                                                                   if (eq(h2, 0)) return {p};
200
                                                            267
       return line(d.x, d.y, a*a - b*b);
                                                                   point h = (ab/norm(ab)) * sqrt(h2);
201
                                                            268
202 }
                                                                   return \{p - h, p + h\};
                                                            269
                                                            270 }
203
_{\rm 204} line perpendicular(line 1, point p){ // passes
                                                            271
       through p
                                                            272 vp inter_circle(circle C1, circle C2){
                                                                   if(C1.c == C2.c) { assert(C1.r != C2.r); return
       return line(1.b, -1.a, -1.b*p.x + 1.a*p.y);
205
                                                            273
206 }
                                                                   {}; }
207
                                                            274
                                                                   point vec = C2.c - C1.c;
                                                                   1d d2 = vec*vec, sum = C1.r+C2.r, dif = C1.r-C2.r
208
                                                            275
209 //////////
210 // Circle //
                                                                   1d p = (d2 + C1.r*C1.r - C2.r*C2.r)/(d2*2), h2 =
                                                            276
211 ///////////
                                                                   C1.r*C1.r - p*p*d2;
                                                                   if (sum*sum < d2 or dif*dif > d2) return {};
                                                            277
213 struct circle{
                                                                   point mid = C1.c + vec*p, per = point(-vec.y, vec
                                                            278
214
       point c; cod r;
                                                                   .x) * sqrt(max((1d)0, h2) / d2);
       circle() : c(0, 0), r(0){}
                                                                   if(eq(per.x, 0) and eq(per.y, 0)) return {mid};
215
                                                            279
       circle(const point o) : c(o), r(0){}
                                                                   return {mid + per, mid - per};
216
                                                           280
       circle(const point a, const point b){
                                                           281 }
217
           c = (a+b)/2;
218
                                                           282
            r = norm(a-c);
                                                            _{283} // minimum circle cover O(n) amortizado
219
                                                            284 circle min_circle_cover(vp v){
220
       circle(const point a, const point b, const point 285
                                                                   random_shuffle(v.begin(), v.end());
                                                                   circle ans;
           assert(ccw(a, b, cc) != 0);
                                                                   int n = v.size();
222
                                                                   for(int i=0;i<n;i++) if(!ans.inside(v[i])){</pre>
           c = inter_line(bisector(a, b), bisector(b, cc288
223
       ))[0];
                                                                        ans = circle(v[i]);
                                                           289
           r = norm(a-c);
                                                                        for(int j=0;j<i;j++) if(!ans.inside(v[j])){</pre>
224
                                                                            ans = circle(v[i], v[j]);
       }
225
                                                            291
       bool inside(const point &a) const{
                                                                            for(int k=0;k<j;k++) if(!ans.inside(v[k])</pre>
226
                                                            292
           return norm(a - c) <= r + EPS;
                                                                   ) {
227
                                                                                ans = circle(v[i], v[j], v[k]);
228
                                                            293
229 };
                                                                            }
230
                                                            295
                                                                        }
                                                                   }
231 pair < point, point > tangent_points (circle cr, point p)296
                                                            297
                                                                   return ans;
       1d d1 = norm(p-cr.c), theta = asin(cr.r/d1);
                                                            298
232
       point p1 = rotccw(cr.c-p, -theta);
       point p2 = rotccw(cr.c-p, theta);
                                                                    Algorithms
234
235
       assert(d1 >= cr.r);
       p1 = p1 * (sqrt(d1*d1-cr.r*cr.r) / d1) + p;
236
                                                               8.1
                                                                    {f Lis}
       p2 = p2 * (sqrt(d1*d1-cr.r*cr.r) / d1) + p;
237
       return {p1, p2};
238
239 }
                                                             int lis(vector<int> const& a) {
240
                                                                   int n = a.size();
                                                             2
241
                                                                   vector < int > d(n, 1);
                                                             3
242 circle incircle(point p1, point p2, point p3){
                                                                   for (int i = 0; i < n; i++) {
       1d m1 = norm(p2-p3);
                                                                        for (int j = 0; j < i; j++) {
```

```
}
              if (a[j] < a[i])
                                                       10
                 d[i] = max(d[i], d[j] + 1);
                                                       11
                                                           return lo;
                                                       12 }
          }
                                                                Ternary Search
                                                          8.5
      int ans = d[0];
11
      for (int i = 1; i < n; i++) {
                                                        1 double ternary_search(double 1, double r) {
          ans = max(ans, d[i]);
13
                                                              double eps = 1e-9; //set the error
14
                                                              limit here
      return ans;
                                                              while (r - 1 > eps) {
                                                        3
16 }
                                                                  double m1 = 1 + (r - 1) / 3;
                                                        4
                                                                  double m2 = r - (r - 1) / 3;
                                                        5
  8.2 Delta-encoding
                                                                 double f1 = f(m1);
                                                                                       //evaluates the
                                                              function at m1
1 #include <bits/stdc++.h>
                                                                 double f2 = f(m2);
                                                                                        //evaluates the
2 using namespace std;
                                                              function at m2
                                                               if (f1 < f2)
4 int main(){
                                                        9
                                                                      1 = m1:
      int n, q;
                                                                  else
                                                       10
      cin >> n >> q;
                                                       11
                                                                     r = m2;
      int [n];
                                                       12
                                                             return f(1);
      int delta[n+2];
                                                                                              //return the
                                                       13
                                                              maximum of f(x) in [1, r]
      while(q--){
                                                       14 }
10
       int 1, r, x;
11
          cin >> 1 >> r >> x;
                                                               Binary Search First True
12
         delta[1] += x;
13
          delta[r+1] -= x;
14
                                                        1 int first_true(int lo, int hi, function < bool(int) > f)
15
                                                        2 hi++;
      int curr = 0;
17
                                                        3 while (lo < hi) {</pre>
      for(int i=0; i < n; i++){
                                                            int mid = lo + (hi - lo) / 2;
                                                        4
         curr += delta[i];
19
                                                              if (f(mid)) {
          v[i] = curr;
20
                                                              hi = mid;
21
                                                             } else {
22
                                                                lo = mid + 1;
      for(int i=0; i < n; i++){
                                                              }
                                                        9
         cout << v[i] << '';
24
                                                           }
                                                       10
                                                           return lo;
                                                       11
      cout << '\n';
26
      return 0;
                                                               Biggest K
29 }
                                                        _{\rm 1} // Description: Gets sum of k biggest or k smallest
  8.3 Subsets
                                                              elements in an array
void subsets(vector < int > % nums) {
                                                        3 // Problem: https://atcoder.jp/contests/abc306/tasks/
   int n = nums.size();
   int powSize = 1 << n;</pre>
                                                        5 // Complexity: O(log n)
    for(int counter = 0; counter < powSize; counter++){
    6</pre>
     for(int j = 0; j < n; j++){
                                                        7 struct SetSum {
       if((counter & (1LL << j)) != 0) {
                                                           11 s = 0;
          cout << nums[j] << ' ';
                                                             multiset <11> mt;
                                                       9
        }
                                                       10
                                                              void add(ll x){
      }
10
                                                       11
                                                                mt.insert(x);
      cout << '\n';</pre>
                                                                  s += x;
                                                       12
12
                                                              }
13 }
                                                       14
                                                              int pop(11 x){
                                                       15
                                                              auto f = mt.find(x);
  8.4 Binary Search Last True
                                                                  if(f == mt.end()) return 0;
                                                       16
                                                                mt.erase(f);
                                                       17
int last_true(int lo, int hi, function < bool(int) > f) 18
                                                                 s -= x;
                                                                  return 1;
     {
                                                       19
   lo--;
                                                       20
    while (lo < hi) {
                                                       21 };
     int mid = lo + (hi - lo + 1) / 2;
     if (f(mid)) {
                                                       23 struct BigK {
       lo = mid;
                                                           int k;
                                                       24
      } else {
                                                              SetSum gt, mt;
                                                       25
        hi = mid - 1;
                                                              BigK(int _k){
                                                       26
```

 $k = _k;$

```
28
29
       void balancear(){
          while((int)gt.mt.size() < k && (int)mt.mt.
30
       size()){
                auto p = (prev(mt.mt.end()));
               gt.add(*p);
32
               mt.pop(*p);
34
35
           *(gt.mt.begin()) < *(prev(mt.mt.end())) ){
36
37
               11 u = *(gt.mt.begin());
               11 v = *(prev(mt.mt.end()));
38
               gt.pop(u); mt.pop(v);
39
                gt.add(v); mt.add(u);
40
           }
41
42
       }
       void add(11 x){
43
           mt.add(x);
           balancear();
45
46
       void rem(ll x){
47
          //x = -x;
48
           if(mt.pop(x) == 0)
               gt.pop(x);
50
51
           balancear();
       }
52
53 };
55 int main() {
       ios::sync_with_stdio(false);
56
       cin.tie(NULL);
57
58
       int n, k, q; cin >> n >> k >> q;
60
       BigK big = BigK(k);
61
62
       int arr[n] = {};
63
64
       while (q--) {
65
66
           int pos, num; cin >> pos >> num;
67
           pos - - :
           big.rem(arr[pos]);
68
60
           arr[pos] = num;
           big.add(arr[pos]);
70
           cout << big.gt.s << '\n';</pre>
72
       }
74
75
       return 0;
76 }
```

9 Data Structures

9.1 Ordered Set

```
1 // Description:
2 // insert(k) - add element k to the ordered set
4 // erase(k) - remove element k from the ordered set
5 // erase(it) - remove element it points to from the
ordered set
5 // order_of_key(k) - returns number of elements
strictly smaller than k
9 6 // find_by_order(n) - return an iterator pointing to 10
the k-th element in the ordered set (counting
from zero).
12
7
8 // Problem:
9 // https://cses.fi/problemset/task/2169/
15
10
11 // Complexity:
17
12 // O(log n) for all operations
```

```
_{14} // How to use:
                                               15 // ordered_set <int > os;
                                               16 // cout << os.order_of_key(1) << '\n;</pre>
                                               17 // cout << os.find_by_order(1) << '\n;</pre>
                                               19 // Notes
                                               20 // The ordered set only contains different elements
while((int)mt.mt.size() && (int)gt.mt.size() 21 // By using less_equal <T > instead of less <T > on using
                                                       ordered_set declaration
                                               22 // The ordered_set becomes an ordered_multiset
                                               23 // So the set can contain elements that are equal
                                               25 #include <ext/pb_ds/assoc_container.hpp>
                                               26 #include <ext/pb_ds/tree_policy.hpp>
                                               28 using namespace __gnu_pbds;
                                               29 template <typename T>
                                               30 using ordered_set = tree<T,null_type,less<T>,
                                                      rb_tree_tag,tree_order_statistics_node_update>;
                                               31
                                               32 void Erase(ordered_set < int >& a, int x){
                                                     int r = a.order_of_key(x);
                                               33
                                                      auto it = a.find_by_order(r);
                                                      a.erase(it);
                                               35
```

9.2 Priority Queue

```
1 // Description:
2 // Keeps the largest (by default) element at the top
      of the queue
4 // Problem:
5 // https://cses.fi/problemset/task/1164/
7 // Complexity:
8 // O(\log n) for push and pop
_{9} // O (1) for looking at the element at the top
11 // How to use:
12 // prioriy_queue <int > pq;
13 // pq.push(1);
14 // pq.top();
15 // pq.pop()
17 // Notes
18 // To use the priority queue keeping the smallest
      element at the top
19
20 priority_queue <int, vector <int>, greater <int>> pq;
```

9.3 Dsu

```
# #include <bits/stdc++.h>
3 using namespace std:
5 const int MAX = 1e6+17;
7 struct DSU {
     int n:
      vector < int > link, sizes;
      DSU(int n) {
          this ->n = n;
13
           link.assign(n+1, 0);
           sizes.assign(n+1, 1);
15
           for (int i = 0; i \le n; i++)
               link[i] = i;
17
18
```

```
19
20
       int find(int x) {
                                                            10 // Complexity:
                                                            _{11} // Add and remove elements - O(log n)
           while (x != link[x])
21
              x = link[x];
                                                            12 // Return sum of biggest or smallest set or return
22
                                                                   the median - 0(1)
           return x:
24
                                                            13
       }
                                                            14 using ll = long long;
26
                                                            1.5
       bool same(int a, int b) {
                                                            16 struct TwoSets {
27
          return find(a) == find(b);
                                                            17 multiset <int > small;
28
                                                                 multiset <int > big;
29
                                                            18
30
                                                                 11 \text{ sums} = 0;
       void unite(int a, int b) {
                                                                 11 \text{ sumb} = 0;
31
                                                            20
          a = find(a);
                                                                 int n = 0;
32
                                                            21
           b = find(b);
33
                                                            22
                                                                 int size_small() {
34
                                                            23
35
           if (a == b) return;
                                                            24
                                                                 return small.size();
36
                                                            25
           if (sizes[a] < sizes[b])</pre>
               swap(a, b);
                                                                 int size_big() {
38
                                                            27
                                                                  return big.size();
                                                            28
39
           sizes[a] += sizes[b];
                                                            29
40
           link[b] = a;
41
                                                            30
      }
                                                                 void balance() {
                                                            31
                                                                   while (size_small() > n / 2) {
43
                                                            32
       int size(int x) {
                                                            33
                                                                     int v = *small.rbegin();
44
                                                                     small.erase(prev(small.end()));
45
           return sizes[x];
                                                            34
                                                                     big.insert(v);
46
                                                            35
47 };
                                                                     sums -= v;
                                                            36
                                                                     sumb += v;
48
                                                            37
49 int main() {
                                                                   }
                                                            38
                                                                   while (size_big() > n - n / 2) {
      ios::sync_with_stdio(false);
50
                                                            39
       cin.tie(NULL);
                                                                     int v = *big.begin();
51
                                                            40
                                                            41
                                                                     big.erase(big.begin());
       int cities, roads; cin >> cities >> roads;
                                                                     small.insert(v);
53
                                                            42
       vector<int> final_roads;
                                                                     sumb -= v;
                                                                     sums += v;
       int ans = 0:
55
                                                            44
       DSU dsu = DSU(cities);
56
                                                            45
                                                                 }
       for (int i = 0, a, b; i < roads; i++) {
                                                            46
           cin >> a >> b;
58
                                                            47
59
           dsu.unite(a, b);
                                                                 void add(int x) {
60
                                                            49
                                                                  n++;
                                                            50
                                                                   small.insert(x);
61
      for (int i = 2; i <= cities; i++) {</pre>
                                                            51
                                                                   sums += x;
62
                                                                   while (!small.empty() && *small.rbegin() > *big.
           if (!dsu.same(1, i)) {
                                                            52
63
               ans++;
                                                                   begin()) {
64
                                                                     int v = *small.rbegin();
               final_roads.push_back(i);
65
                                                           53
               dsu.unite(1,i);
                                                                     small.erase(prev(small.end()));
           }
                                                                     big.insert(v);
67
                                                            55
                                                            56
                                                                     sums -= v;
68
                                                                     sumb += v;
                                                            57
69
       cout << ans << '\n';
70
                                                            58
       for (auto e : final_roads) {
                                                                   balance();
                                                            59
           cout << "1 " << e << '\n';</pre>
                                                                 }
72
                                                            60
73
                                                            61
                                                                 bool rem(int x) {
74
                                                            62
75 }
                                                            63
                                                                   auto it1 = small.find(x);
                                                            64
  9.4 Two Sets
                                                                   auto it2 = big.find(x);
                                                            65
                                                                   bool flag = false;
                                                            66
                                                                   if (it1 != small.end()) {
                                                            67
1 // Description
                                                                    sums -= *it1;
_{2} // THe values are divided in two multisets so that
                                                            68
                                                                     small.erase(it1);
      one of them contain all values that are
                                                                     flag = true;
_{
m 3} // smaller than the median and the other one contains ^{
m 70}
                                                                   } else if (it2 != big.end()) {
       all values that are greater or equal to the
                                                                     sumb -= *it2:
      median.
                                                            72
                                                                     big.erase(it2);
                                                            73
5 // Problem:
                                                            74
                                                                     flag = true;
_6 // https://atcoder.jp/contests/abc306/tasks/abc306_e ^{75}
                                                                   balance();
7 // Problem I - Maratona Feminina de çãProgramao da
                                                            76
                                                                   return flag;
                                                            77
       Unicamp 2023
                                                                 }
                                                            78
8 // https://codeforces.com/group/WYIydkiPyE/contest
                                                            79
       /450037/attachments
```

```
11 sum_small() {
                                                                      if (p <= ini && fim <= q) return seg[pos];</pre>
80
                                                           52
81
      return sums;
                                                           53
                                                                      int m = (ini + fim) >> 1;
                                                                      return f(query(e[pos], ini, m, p, q), query(d
82
                                                           54
                                                                  [pos], m + 1, fim, p, q));
83
    11 sum_big() {
     return sumb;
85
                                                           56
                                                                  void update(int pos, int ini, int fim, int id,
                                                                  int val) {
87
                                                                      if (ini > id || fim < id) {</pre>
    int median() {
88
                                                           58
                                                                           return;
      return *big.begin();
89
                                                           59
90
                                                           60
91 };
                                                           61
                                                                      if (ini == fim) {
                                                           62
        Dynamic Implicit Sparse
  9.5
                                                                           seg[pos] = val;
                                                           63
                                                           64
                                                                           return;
                                                           65
1 // Description:
2 // Indexed at one
                                                                      }
                                                           67
_{\rm 4} // When the indexes of the nodes are too big to be
                                                                      int m = (ini + fim) >> 1;
      stored in an array
                                                           69
                                                                      if (id <= m) {
_{5} // and the queries need to be answered online so we
                                                           70
                                                                           if (e[pos] == 0) e[pos] = create();
      can't sort the nodes and compress them
                                                           71
                                                                           update(e[pos], ini, m, id, val);
_{\rm 6} // we create nodes only when they are needed so there ^{72}
                                                                      } else {
      'll be (Q*log(MAX)) nodes
                                                                           if (d[pos] == 0) d[pos] = create();
_{7} // where Q is the number of queries and MAX is the
                                                           74
                                                           75
                                                                           update(d[pos], m + 1, fim, id, val);
      maximum index a node can assume
                                                           76
9 // Query - get sum of elements from range (1, r)
                                                           77
                                                                      seg[pos] = f(seg[e[pos]], seg[d[pos]]);
      inclusive
_{10} // Update - update element at position id to a value _{79}
                                                           80
                                                                  ftype query(int p, int q) {
                                                           81
                                                                      return query(1, 1, n, p, q);
12 // Problem:
                                                           82
13 // https://cses.fi/problemset/task/1648
                                                           83
                                                           84
                                                                  void update(int id, int val) {
15 // Complexity:
                                                                      update(1, 1, n, id, val);
_{16} // O(log n) for both query and update
                                                           86
                                                           87
                                                           88 };
18 // How to use:
_{19} // MAX is the maximum index a node can assume
                                                                   Segtree2d
                                                              9.6
21 // Segtree seg = Segtree(MAX);
                                                            1 // Description:
23 typedef long long ftype;
                                                            2 // Indexed at zero
24
                                                            _{3} // Given a N x M grid, where i represents the row and
                                                                   j the column, perform the following operations
25 const int MAX = 1e9+17;
                                                            4 // update(j, i) - update the value of grid[i][j]
                                                            _{5} // query(j1, j2, i1, i2) - return the sum of values
27 struct Segtree {
      vector < ftype > seg, d, e;
                                                                  inside the rectangle
28
      const ftype NEUTRAL = 0;
                                                            6 // defined by grid[i1][j1] and grid[i2][j2] inclusive
29
      int n;
30
                                                            8 // Problem:
31
      Segtree(int n) {
                                                            9 // https://cses.fi/problemset/task/1739/
32
          this ->n = n;
33
                                                           10
           create();
                                                           11 // Complexity:
34
           create();
                                                           12 // Time complexity:
35
                                                           _{13} // O(log N * log M) for both query and update
      }
36
                                                           _{14} // O(N * M) for build
37
      ftype f(ftype a, ftype b) {
                                                           15 // Memory complexity:
                                                           16 // 4 * M * N
39
          return a + b;
                                                           17
40
                                                           _{18} // How to use:
41
      ftype create() {
                                                           19 // Segtree2D seg = Segtree2D(n, n);
42
43
          seg.push_back(0);
                                                           20 // vector < vector < int >> v(n, vector < int >(n));
                                                           21 // seg.build(v);
           e.push_back(0);
44
45
           d.push_back(0);
                                                           23 // Notes
           return seg.size() - 1;
46
                                                           _{24} // Indexed at zero
47
                                                           25
      ftype query(int pos, int ini, int fim, int p, int 26 struct Segtree2D {
49
                                                                 const int MAXN = 1025;
                                                           27
                                                                  int N, M;
           if (q < ini || p > fim) return NEUTRAL;
50
                                                           28
           if (pos == 0) return 0;
51
                                                           29
```

```
updateX(2*noX+2, m+1, rX, x, y);
vector < vector < int >> seg:
                                                   93
                                                                   }
                                                   94
                                                               }
Segtree2D(int N, int M) {
                                                   95
    this -> N = N;
                                                   96
    this ->M = M;
                                                               updateY(noX, 1X, rX, 0, 0, M - 1, y);
    seg.resize(2*MAXN, vector < int > (2*MAXN));
                                                   98
                                                          int queryY(int noX, int noY, int lY, int rY, int
                                                   100
                                                          aY, int bY){
void buildY(int noX, int lX, int rX, int noY, int
1Y, int rY, vector < vector < int >> &v) {
                                                               if(aY <= 1Y && rY <= bY) return seg[noX][noY</pre>
    if(1Y == rY){
                                                          1:
        if(1X == rX){
            seg[noX][noY] = v[rX][rY];
                                                               int m = (1Y+rY)/2;
                                                   103
                                                   104
                                                              if(bY <= m) return queryY(noX, 2*noY+1, 1Y, m</pre>
            seg[noX][noY] = seg[2*noX+1][noY] +
seg[2*noX+2][noY];
                                                          , aY, bY);
        }
                                                               if (m < aY) return queryY(noX, 2*noY+2, m+1,
    }else{
                                                          rY, aY, bY);
        int m = (1Y+rY)/2;
                                                              return queryY(noX, 2*noY+1, 1Y, m, aY, bY) +
                                                   108
        buildY(noX, 1X, rX, 2*noY+1, 1Y, m, v);
                                                          queryY(noX, 2*noY+2, m+1, rY, aY, bY);
        buildY(noX, 1X, rX, 2*noY+2, m+1, rY, v);109
        seg[noX][noY] = seg[noX][2*noY+1] + seg[_{111}
                                                          int queryX(int noX, int lX, int rX, int aX, int
noX1[2*noY+2]:
                                                          bX, int aY, int bY){
   }
                                                               if (aX <= 1X && rX <= bX) return queryY(noX,
                                                   112
}
                                                          0, 0, M - 1, aY, bY);
                                                   113
void buildX(int noX, int lX, int rX, vector<</pre>
                                                               int m = (1X+rX)/2:
vector <int>> &v){
                                                   115
   if(1X != rX){
                                                               if (bX <= m) return queryX(2*noX+1, lX, m, aX,
                                                   116
        int m = (1X+rX)/2;
                                                           bX, aY, bY);
                                                              if (m < aX) return queryX(2*noX+2, m+1, rX, aX
                                                   117
        buildX(2*noX+1, 1X, m, v);
                                                           , bX, aY, bY);
        buildX(2*noX+2, m+1, rX, v);
                                                   118
    }
                                                               return queryX(2*noX+1, lX, m, aX, bX, aY, bY)
                                                   119
                                                           + queryX(2*noX+2, m+1, rX, aX, bX, aY, bY);
    buildY(noX, 1X, rX, 0, 0, M - 1, v);
                                                   120
}
                                                   121
                                                          void build(vector < vector < int >> &v) {
                                                   122
void updateY(int noX, int 1X, int rX, int noY,
                                                   123
                                                              buildX(0, 0, N - 1, v);
int lY, int rY, int y){
                                                   124
    if(1Y == rY){
                                                   125
        if(1X == rX){
                                                          int query(int aX, int bX, int aY, int bY) {
                                                   126
            seg[noX][noY] = !seg[noX][noY];
                                                               return queryX(0, 0, N - 1, aX, bX, aY, bY);
                                                   127
            seg[noX][noY] = seg[2*noX+1][noY] +
                                                  129
seg[2*noX+2][noY];
                                                   130
                                                          void update(int x, int y) {
                                                              updateX(0, 0, N - 1, x, y);
        }
                                                   131
    }else{
                                                   132
        int m = (1Y+rY)/2;
                                                   133 };
                                                           Minimum And Amount
        if(y <= m){
            updateY(noX, 1X, rX, 2*noY+1,1Y, m, y
);
                                                    1 // Description:
        else if(m < y)
                                                    2 // Query - get minimum element in a range (1, r)
            updateY(noX, 1X, rX, 2*noY+2, m+1, rY
                                                          inclusive
, y);
                                                    _{3} // and also the number of times it appears in that
        }
                                                    4 // Update - update element at position id to a value
        seg[noX][noY] = seg[noX][2*noY+1] + seg[
                                                          val
noX][2*noY+2];
                                                    6 // Problem:
   }
}
                                                    7 // https://codeforces.com/edu/course/2/lesson/4/1/
                                                          practice/contest/273169/problem/C
void updateX(int noX, int lX, int rX, int x, int
                                                    9 // Complexity:
y){
    int m = (1X+rX)/2;
                                                    10 // O(\log n) for both query and update
    if(1X != rX){
                                                    12 // How to use:
       if(x <= m){
                                                    13 // Segtree seg = Segtree(n);
            updateX(2*noX+1, 1X, m, x, y);
                                                   14 // seg.build(v);
        else if(m < x)
                                                   15
```

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```
16 #define pii pair<int, int>
                                                                             seg[pos] = mp(v[ini], 1);
                                                          85
17 #define mp make_pair
                                                          86
                                                                         }
18 #define ff first
                                                                         return:
                                                          87
                                                                     }
19 #define ss second
                                                          88
21 const int INF = 1e9+17;
                                                                     int e = 2*pos + 1;
                                                          90
                                                                     int d = 2*pos + 2;
23 typedef pii ftype;
                                                                     int m = ini + (fim - ini) / 2;
                                                          92
24
                                                          93
25 struct Segtree {
                                                          94
                                                                     build(e, ini, m, v);
                                                                     build(d, m + 1, fim, v);
      vector <ftype > seg;
26
                                                          95
      int n;
                                                          96
      const ftype NEUTRAL = mp(INF, 0);
                                                                     seg[pos] = f(seg[e], seg[d]);
28
                                                         97
                                                         98
30
      Segtree(int n) {
                                                          99
          int sz = 1;
                                                                 ftype query(int p, int q) {
31
                                                         100
                                                                     return query(0, 0, n - 1, p, q);
32
          while (sz < n) sz *= 2;
                                                         101
          this->n = sz;
33
                                                         102
          seg.assign(2*sz, NEUTRAL);
                                                                 void update(int id, int val) {
35
                                                         104
                                                         105
                                                                     update(0, 0, n - 1, id, val);
36
                                                         106
37
      ftype f(ftype a, ftype b) {
                                                         107
38
          if (a.ff < b.ff) return a;</pre>
                                                                 void build(vector<int> &v) {
                                                         108
          if (b.ff < a.ff) return b;
                                                                     build(0, 0, n - 1, v);
40
                                                         109
                                                         110
41
          return mp(a.ff, a.ss + b.ss);
42
                                                         111
                                                                 void debug() {
43
                                                         112
                                                                     for (auto e : seg) {
                                                                         cout << e.ff << ' ' << e.ss << '\n';</pre>
      ftype query(int pos, int ini, int fim, int p, int114
45
                                                         115
          if (ini >= p && fim <= q) {
                                                                     cout << '\n';
46
                                                         116
              return seg[pos];
                                                         117
47
          }
                                                         118 };
49
                                                                  Lazy Addition To Segment
                                                            9.8
          if (q < ini || p > fim) {
              return NEUTRAL;
51
                                                          1 // Description:
52
                                                          2 // Query - get sum of elements from range (1, r)
          int e = 2*pos + 1;
54
                                                                inclusive
           int d = 2*pos + 2;
                                                           3 // Update - add a value val to elementos from range (
          int m = ini + (fim - ini) / 2;
56
                                                                l, r) inclusive
          return f(query(e, ini, m, p, q), query(d, m + 5 // Problem:
       1, fim, p, q));
                                                           6 // https://codeforces.com/edu/course/2/lesson/5/1/
59
                                                                practice/contest/279634/problem/A
60
      void update(int pos, int ini, int fim, int id,
                                                          8 // Complexity:
      int val) {
                                                           9 // O(log n) for both query and update
62
          if (ini > id || fim < id) {</pre>
                                                          10
              return;
                                                          _{11} // How to use:
63
64
                                                          12 // Segtree seg = Segtree(n);
                                                          13 // seg.build(v);
          if (ini == id && fim == id) {
66
                                                          14
               seg[pos] = mp(val, 1);
                                                          15 // Notes
67
68
                                                          16 // Change neutral element and f function to perform a
               return;
69
                                                                 different operation
          }
70
                                                          17
71
                                                          18 const long long INF = 1e18+10;
           int e = 2*pos + 1;
72
                                                          19
          int d = 2*pos + 2;
73
                                                          20 typedef long long ftype;
          int m = ini + (fim - ini) / 2;
74
                                                          21
                                                         22 struct Segtree {
          update(e, ini, m, id, val);
76
                                                         23
                                                             vector<ftype> seg;
          update(d, m + 1, fim, id, val);
                                                                vector<ftype> lazy;
                                                          24
78
                                                          25
                                                                int n:
          seg[pos] = f(seg[e], seg[d]);
79
                                                                const ftype NEUTRAL = 0;
                                                          26
      }
                                                                const ftype NEUTRAL_LAZY = -1; // change to -INF
80
81
                                                                if there are negative numbers
      void build(int pos, int ini, int fim, vector<int>28
82
       &v) {
                                                                 Segtree(int n) {
           if (ini == fim) {
83
                                                                    int sz = 1;
                                                          30
               if (ini < (int)v.size()) {</pre>
84
                                                                     while (sz < n) sz *= 2;
                                                          31
```

```
this ->n = sz;
                                                               int e = 2*pos + 1;
                                                   98
                                                               int d = 2*pos + 2;
                                                   99
    seg.assign(2*sz, NEUTRAL);
                                                               int m = ini + (fim - ini) / 2;
                                                   100
    lazy.assign(2*sz, NEUTRAL_LAZY);
                                                   101
                                                               update(e, ini, m, p, q, val);
                                                               update(d, m + 1, fim, p, q, val);
                                                   103
ftype apply_lazy(ftype a, ftype b, int len) {
                                                   104
    if (b == NEUTRAL_LAZY) return a;
                                                               seg[pos] = f(seg[e], seg[d]);
                                                   105
    if (a == NEUTRAL_LAZY) return b * len;
                                                   106
    else return a + b * len;
                                                   107
}
                                                          void build(int pos, int ini, int fim, vector<int>
                                                   108
                                                           &v) {
void propagate(int pos, int ini, int fim) {
                                                              if (ini == fim) {
                                                   109
    if (ini == fim) {
                                                                   if (ini < (int)v.size()) {</pre>
                                                   110
        return;
                                                   111
                                                                       seg[pos] = v[ini];
    }
                                                   112
                                                   113
                                                                   return;
    int e = 2*pos + 1;
                                                               }
                                                   114
    int d = 2*pos + 2;
    int m = ini + (fim - ini) / 2;
                                                               int e = 2*pos + 1;
                                                   116
                                                               int d = 2*pos + 2;
                                                   117
    lazy[e] = apply_lazy(lazy[e], lazy[pos], 1); 118
                                                               int m = ini + (fim - ini) / 2;
    lazy[d] = apply_lazy(lazy[d], lazy[pos], 1); 119
                                                               build(e, ini, m, v);
    seg[e] = apply_lazy(seg[e], lazy[pos], m -
                                                               build(d, m + 1, fim, v);
                                                   121
ini + 1);
                                                   122
    seg[d] = apply_lazy(seg[d], lazy[pos], fim - 123
                                                               seg[pos] = f(seg[e], seg[d]);
m):
                                                   124
    lazy[pos] = NEUTRAL_LAZY;
                                                          ftype query(int p, int q) {
                                                   126
                                                               return query(0, 0, n - 1, p, q);
                                                   127
                                                   128
ftype f(ftype a, ftype b) {
                                                   129
    return a + b;
                                                   130
                                                           void update(int p, int q, int val) {
                                                               update(0, 0, n - 1, p, q, val);
                                                   131
                                                   132
ftype query(int pos, int ini, int fim, int p, int133
                                                          void build(vector<int> &v) {
                                                   134
    propagate(pos, ini, fim);
                                                               build(0, 0, n - 1, v);
                                                   135
                                                   136
    if (ini >= p && fim <= q) {
                                                   137
                                                          void debug() {
       return seg[pos];
                                                   138
                                                   139
                                                               for (auto e : seg) {
                                                   140
                                                                   cout << e << ' ';
    if (q < ini || p > fim) {
                                                   141
        return NEUTRAL;
                                                               cout << '\n';</pre>
                                                   142
                                                               for (auto e : lazy) {
                                                   143
                                                                   cout << e << ' ';
    int e = 2*pos + 1;
                                                   145
                                                               cout << '\n';
    int d = 2*pos + 2;
    int m = ini + (fim - ini) / 2;
                                                               cout << '\n';</pre>
                                                   147
                                                   148
    return f(query(e, ini, m, p, q), query(d, m +149 );
 1, fim, p, q));
                                                            Segment With Maximum Sum
void update(int pos, int ini, int fim, int p, int _1 // Description:
 q, int val) {
                                                    2 // Query - get sum of segment that is maximum among
    propagate(pos, ini, fim);
                                                          all segments
                                                    3 // E.g
    if (ini > q || fim < p) {</pre>
                                                    4 // Array: 5 -4 4 3 -5
        return;
                                                    _{5} // Maximum segment sum: 8 because 5 + (-4) + 4 = 8
    7
                                                    6 // Update - update element at position id to a value
                                                          val
    if (ini >= p && fim <= q) {
        lazy[pos] = apply_lazy(lazy[pos], val, 1) 8 // Problem:
                                                    9 // https://codeforces.com/edu/course/2/lesson/4/2/
        seg[pos] = apply_lazy(seg[pos], val, fim
                                                          practice/contest/273278/problem/A
- ini + 1);
                                                    11 // Complexity:
        return:
                                                    12 // O(log n) for both query and update
    }
                                                    _{14} // How to use:
```

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```
15 // Segtree seg = Segtree(n);
                                                                  int val) {
16 // seg.build(v);
                                                                    if (ini > id || fim < id) {
                                                           80
                                                           81
                                                                          return;
18 // Notes
                                                           82
19 // The maximum segment sum can be a negative number
20 // In that case, taking zero elements is the best
                                                                      if (ini == id && fim == id) {
                                                           84
                                                                           seg[pos] = Node(val, val, val, val);
21 // So we need to take the maximum between 0 and the
                                                           86
      query
                                                                          return;
                                                           87
                                                                      }
22 // max(OLL, seg.query(0, n).max_seg)
                                                           89
                                                                      int e = 2*pos + 1;
24 using ll = long long;
                                                                      int d = 2*pos + 2;
                                                           91
26 typedef ll ftype_node;
                                                                      int m = ini + (fim - ini) / 2;
                                                           92
27
                                                           93
28 struct Node {
                                                                      update(e, ini, m, id, val);
                                                           94
29
      ftype_node max_seg;
                                                           95
                                                                      update(d, m + 1, fim, id, val);
      ftype_node pref;
30
                                                           96
      ftype_node suf;
                                                                      seg[pos] = f(seg[e], seg[d]);
      ftype_node sum;
                                                                  }
32
                                                           98
                                                           99
33
      Node(ftype_node max_seg, ftype_node pref,
                                                                  void build(int pos, int ini, int fim, vector<int>
34
      ftype_node suf, ftype_node sum) : max_seg(max_seg
                                                                   &v) {
      ), pref(pref), suf(suf), sum(sum) {};
                                                                      if (ini == fim) {
                                                                           // se a \varsigma \tilde{a}posio existir no array original
35 };
                                                          102
                                                          103
                                                                          // seg tamanho potencia de dois
36
37 typedef Node ftype;
                                                                          if (ini < (int)v.size()) {</pre>
                                                          104
                                                                               seg[pos] = Node(v[ini], v[ini], v[ini
38
39 struct Segtree {
                                                                  ], v[ini]);
      vector<ftype> seg;
                                                                          }
40
                                                          106
41
       int n;
                                                          107
                                                                          return;
      const ftype NEUTRAL = Node(0, 0, 0, 0);
                                                                      }
42
                                                          108
                                                          109
43
      Segtree(int n) {
                                                          110
                                                                      int e = 2*pos + 1;
          int sz = 1;
                                                                      int d = 2*pos + 2;
45
                                                          111
           // potencia de dois mais proxima
                                                                      int m = ini + (fim - ini) / 2;
                                                          112
           while (sz < n) sz *= 2;
47
                                                          113
           this ->n = sz;
                                                          114
                                                                      build(e, ini, m, v);
48
                                                                      build(d, m + 1, fim, v);
49
                                                          115
           // numero de nos da seg
50
                                                          116
51
           seg.assign(2*sz, NEUTRAL);
                                                          117
                                                                      seg[pos] = f(seg[e], seg[d]);
                                                                  }
52
                                                          118
                                                          119
53
      ftype f(ftype a, ftype b) {
                                                                  ftype query(int p, int q) {
54
                                                          120
           ftype_node max_seg = max({a.max_seg, b.
                                                                      return query (0, 0, n - 1, p, q);
                                                          121
55
      max_seg, a.suf + b.pref});
                                                          122
           ftype_node pref = max(a.pref, a.sum + b.pref)123
56
                                                                  void update(int id, int val) {
           ftype_node suf = max(b.suf, b.sum + a.suf); 125
                                                                      update(0, 0, n - 1, id, val);
57
           ftype_node sum = a.sum + b.sum;
58
59
                                                          127
                                                                  void build(vector<int> &v) {
           return Node(max_seg, pref, suf, sum);
60
                                                          128
      }
                                                                      build(0, 0, n - 1, v);
62
                                                          130
       ftype query(int pos, int ini, int fim, int p, int131
63
                                                                  void debug() {
                                                          132
           if (ini >= p && fim <= q) {
                                                                      for (auto e : seg) {
                                                          133
64
                                                                          cout << e.max_seg << ' ' ' << e.pref << ' '</pre>
               return seg[pos];
65
                                                          134
                                                                   << e.suf << ' ' << e.sum << '\n';
66
           }
                                                          135
67
           if (q < ini || p > fim) {
                                                                      cout << '\n';
                                                          136
68
              return NEUTRAL;
                                                          137
69
                                                          138 };
71
                                                                     Range Query Point Update
                                                              9.10
           int e = 2*pos + 1;
           int d = 2*pos + 2;
73
           int m = ini + (fim - ini) / 2;
                                                           1 // Description:
74
                                                           2 // Indexed at zero
           return f(query(e, ini, m, p, q), query(d, m + _3 // Query - get sum of elements from range (1, r)
76
       1, fim, p, q));
                                                                  inclusive
77
                                                            4 // Update - update element at position id to a value
                                                                 val
      void update(int pos, int ini, int fim, int id,
79
```

```
6 // Problem:
                                                                     int m = ini + (fim - ini) / 2;
                                                          72
7 // https://codeforces.com/edu/course/2/lesson/4/1/
                                                          73
      practice/contest/273169/problem/B
                                                                     update(e, ini, m, id, val);
                                                          74
                                                                     update(d, m + 1, fim, id, val);
                                                          75
9 // Complexity:
10 // O(log n) for both query and update
                                                                     seg[pos] = f(seg[e], seg[d]);
                                                          77
12 // How to use:
                                                          79
13 // Segtree seg = Segtree(n);
                                                                 void build(int pos, int ini, int fim, vector<int>
                                                          80
14 // seg.build(v);
                                                                  &v) {
                                                                     if (ini == fim) {
                                                          81
16 // Notes
                                                                         if (ini < (int)v.size()) {</pre>
17 // Change neutral element and f function to perform a 83
                                                                             seg[pos] = v[ini];
       different operation
18
                                                                          return:
19 // If you want to change the operations to point
                                                          86
      query and range update
                                                                     int e = 2*pos + 1;
_{20} // Use the same segtree, but perform the following
                                                          88
      operations
                                                                     int d = 2*pos + 2;
                                                                     int m = ini + (fim - ini) / 2;
21 // Query - seg.query(0, id);
                                                          90
22 // Update - seg.update(1, v); seg.update(r + 1, -v); 91
                                                                     build(e, ini, m, v);
24 typedef long long ftype;
                                                                     build(d, m + 1, fim, v);
                                                          93
26 struct Segtree {
                                                                     seg[pos] = f(seg[e], seg[d]);
                                                          95
      vector < ftype > seg;
27
                                                          96
28
      int n;
                                                          97
      const ftype NEUTRAL = 0;
                                                                 ftype query(int p, int q) {
29
                                                          98
                                                          99
                                                                     return query(0, 0, n - 1, p, q);
      Segtree(int n) {
31
                                                          100
          int sz = 1;
                                                          101
32
                                                                 void update(int id, int val) {
          while (sz < n) sz *= 2;
33
                                                          102
          this->n = sz;
                                                                     update(0, 0, n - 1, id, val);
                                                         103
34
                                                          104
          seg.assign(2*sz, NEUTRAL);
36
                                                          105
                                                                 void build(vector<int> &v) {
                                                                     build(0, 0, n - 1, v);
38
                                                          107
       ftype f(ftype a, ftype b) {
                                                          108
39
          return a + b;
40
                                                          109
                                                                 void debug() {
                                                          110
41
42
                                                                     for (auto e : seg) {
       ftype query(int pos, int ini, int fim, int p, int112
                                                                         cout << e << ' ';
43
                                                         113
44
          if (ini >= p && fim <= q) {
                                                          114
                                                                     cout << '\n';</pre>
              return seg[pos];
                                                          115
45
          }
                                                          116 };
46
                                                                    Lazy Assignment To Segment
           if (q < ini || p > fim) {
              return NEUTRAL;
49
50
                                                           const long long INF = 1e18+10;
51
          int e = 2*pos + 1;
52
                                                           3 typedef long long ftype;
          int d = 2*pos + 2;
          int m = ini + (fim - ini) / 2;
54
                                                           5 struct Segtree {
55
                                                                vector<ftype> seg;
          return f(query(e, ini, m, p, q), query(d, m + 7
56
                                                                 vector <ftype > lazy;
       1, fim, p, q));
                                                                 int n;
57
                                                                 const ftype NEUTRAL = 0;
58
                                                                 const ftype NEUTRAL_LAZY = -1; // Change to -INF
       void update(int pos, int ini, int fim, int id,
59
                                                                 if there are negative numbers
      int val) {
                                                          11
          if (ini > id || fim < id) {
60
                                                          12
                                                                 Segtree(int n) {
              return;
                                                                     int sz = 1;
                                                          13
          }
62
                                                          14
                                                                     // potencia de dois mais proxima
                                                                     while (sz < n) sz *= 2;
                                                          15
           if (ini == id && fim == id) {
64
                                                                     this ->n = sz;
                                                          16
               seg[pos] = val;
65
                                                          17
                                                                     // numero de nos da seg
                                                          18
               return;
67
                                                                     seg.assign(2*sz, NEUTRAL);
                                                          19
          }
                                                                     lazy.assign(2*sz, NEUTRAL_LAZY);
                                                          20
69
                                                          21
           int e = 2*pos + 1;
                                                          22
71
          int d = 2*pos + 2;
                                                                 ftype apply_lazy(ftype a, ftype b, int len) {
                                                          23
```

```
if (b == NEUTRAL_LAZY) return a;
                                                                       seg[pos] = f(seg[e], seg[d]);
24
                                                           90
25
           if (a == NEUTRAL_LAZY) return b * len;
                                                           91
           else return b * len;
26
                                                           92
                                                                   void build(int pos, int ini, int fim, vector<int>
                                                            93
                                                                   &v) {
      void propagate(int pos, int ini, int fim) {
                                                                       if (ini == fim) {
29
                                                           94
           if (ini == fim) {
                                                                           // se a çãposio existir no array original
30
                                                            95
               return:
                                                                           // seg tamanho potencia de dois
31
                                                           96
                                                                           if (ini < (int)v.size()) {</pre>
           }
32
                                                           97
                                                                               seg[pos] = v[ini];
33
                                                           98
           int e = 2*pos + 1;
34
                                                           99
           int d = 2*pos + 2;
                                                                           return;
           int m = ini + (fim - ini) / 2;
                                                                       }
36
                                                           101
           \label{lazy} \mbox{[e] = apply\_lazy(lazy[e], lazy[pos], 1); $_{103}$}
                                                                       int e = 2*pos + 1;
38
                                                                       int d = 2*pos + 2;
           lazy[d] = apply_lazy(lazy[d], lazy[pos], 1); 104
39
                                                                       int m = ini + (fim - ini) / 2;
           seg[e] = apply_lazy(seg[e], lazy[pos], m -
41
                                                           106
                                                                       build(e, ini, m, v);
           seg[d] = apply_lazy(seg[d], lazy[pos], fim - 108
                                                                       build(d, m + 1, fim, v);
42
      m);
                                                           109
                                                                       seg[pos] = f(seg[e], seg[d]);
43
                                                           110
           lazy[pos] = NEUTRAL_LAZY;
44
                                                           111
      }
45
                                                           112
                                                                   ftype query(int p, int q) {
46
                                                           113
                                                                       return query(0, 0, n - 1, p, q);
      ftype f(ftype a, ftype b) {
47
                                                           114
48
           return a + b;
                                                           115
49
                                                           116
                                                                   void update(int p, int q, int val) {
50
      ftype query(int pos, int ini, int fim, int p, int118
                                                                       update(0, 0, n - 1, p, q, val);
51
                                                           119
52
           propagate(pos, ini, fim);
                                                           120
                                                                   void build(vector<int> &v) {
                                                          121
53
           if (ini >= p && fim <= q) {
                                                          122
                                                                       build(0, 0, n - 1, v);
               return seg[pos];
55
                                                           123
                                                           124
                                                                   void debug() {
57
                                                           125
           if (q < ini || p > fim) {
                                                           126
                                                                       for (auto e : seg) {
58
               return NEUTRAL;
                                                                           cout << e << '';
59
                                                           127
60
                                                           128
61
                                                           129
                                                                       cout << '\n';
           int e = 2*pos + 1;
                                                                       for (auto e : lazy) {
62
                                                           130
           int d = 2*pos + 2;
                                                                           cout << e << '';
                                                           131
63
           int m = ini + (fim - ini) / 2;
                                                           132
                                                                       7
64
                                                                       cout << '\n';
                                                           133
65
           return f(query(e, ini, m, p, q), query(d, m +134
                                                                       cout << '\n';</pre>
66
       1, fim, p, q));
                                                           135
                                                           136 };
68
       void update (int pos, int ini, int fim, int p, int 9.12 Lazy Dynamic Implicit Sparse
69
       q, int val) {
           propagate(pos, ini, fim);
70
                                                            1 // Description:
                                                            2 // Indexed at one
71
           if (ini > q || fim < p) {</pre>
72
               return;
73
                                                            _{4} // When the indexes of the nodes are too big to be
74
                                                                  stored in an array
                                                            5 // and the queries need to be answered online so we
           if (ini >= p && fim <= q) {</pre>
76
                                                                  can't sort the nodes and compress them
               lazy[pos] = apply_lazy(lazy[pos], val, 1) 6 // we create nodes only when they are needed so there
77
                                                                  'll be (Q*log(MAX)) nodes
               seg[pos] = apply\_lazy(seg[pos], val, fim _7 // where Q is the number of queries and MAX is the
78
       - ini + 1);
                                                                  maximum index a node can assume
79
               return:
80
                                                            9 // Query - get sum of elements from range (1, r)
81
           }
                                                                  inclusive
82
                                                            _{
m 10} // Update - update element at position id to a value
           int e = 2*pos + 1;
83
                                                                  val
           int d = 2*pos + 2;
84
                                                           11
           int m = ini + (fim - ini) / 2;
                                                           12 // Problem:
85
                                                           13 // https://oj.uz/problem/view/IZhO12_apple
           update(e, ini, m, p, q, val);
87
                                                           15 // Complexity:
           update(d, m + 1, fim, p, q, val);
88
89
                                                            _{16} // O(log n) for both query and update
```

```
if (pos == 0) return 0;
                                                           83
_{18} // How to use:
                                                                      if (p <= ini && fim <= q) return seg[pos];</pre>
                                                           84
                                                                      int m = (ini + fim) >> 1;
_{19} // MAX is the maximum index a node can assume
                                                           85
20 // Create a default null node
                                                                      return f(query(e[pos], ini, m, p, q), query(d
                                                           86
21 // Create a node to be the root of the segtree
                                                                  [pos], m + 1, fim, p, q));
                                                           87
23 // Segtree seg = Segtree(MAX);
                                                           88
                                                                  void update(int pos, int ini, int fim, int p, int
                                                           89
25 const int MAX = 1e9+10;
                                                                   q, int val) {
26 const long long INF = 1e18+10;
                                                                      propagate(pos, ini, fim);
                                                           90
                                                                      if (ini > q || fim < p) {</pre>
                                                           91
28 typedef long long ftype;
                                                           92
                                                                           return;
                                                                      }
                                                           93
30 struct Segtree {
31
      vector<ftype> seg, d, e, lazy;
                                                                      if (ini >= p && fim <= q) {
      const ftype NEUTRAL = 0;
                                                                           lazy[pos] = apply_lazy(lazy[pos], val, 1)
32
       const ftype NEUTRAL_LAZY = -1; // change to -INF
      if the elements can be negative
                                                                           seg[pos] = apply_lazy(seg[pos], val, fim
      int n:
                                                                  - ini + 1);
35
                                                           98
      Segtree(int n) {
                                                                          return;
36
                                                           99
           this ->n = n;
                                                                      }
37
                                                           100
           create();
38
                                                          101
           create();
                                                                      int m = (ini + fim) >> 1;
40
                                                          103
                                                                      if (e[pos] == 0) e[pos] = create();
41
                                                           104
       ftype apply_lazy(ftype a, ftype b, int len) {
42
                                                          105
                                                                      update(e[pos], ini, m, p, q, val);
           if (b == NEUTRAL_LAZY) return a;
43
                                                          106
           else return b * len; // change to a + b * lem_{07}
                                                                      if (d[pos] == 0) d[pos] = create();
                                                                      update(d[pos], m + 1, fim, p, q, val);
       to add to an element instead of updating it
                                                          108
45
                                                           109
                                                                      seg[pos] = f(seg[e[pos]], seg[d[pos]]);
46
                                                           110
      void propagate(int pos, int ini, int fim) {
47
                                                          111
           if (seg[pos] == 0) return;
                                                          112
                                                                  ftype query(int p, int q) {
49
                                                          113
           if (ini == fim) {
                                                                      return query(1, 1, n, p, q);
                                                           114
51
               return:
                                                          115
                                                          116
52
                                                                  void update(int p, int q, int val) {
                                                           117
           int m = (ini + fim) >> 1;
                                                                      update(1, 1, n, p, q, val);
54
                                                          118
                                                           119
           if (e[pos] == 0) e[pos] = create();
                                                          120 };
56
           if (d[pos] == 0) d[pos] = create();
                                                              9.13 Persistent
58
           lazy[e[pos]] = apply_lazy(lazy[e[pos]], lazy[
59
      pos], 1);
                                                            1 // Description:
          lazy[d[pos]] = apply_lazy(lazy[d[pos]], lazy[ 2 // Persistent segtree allows for you to save the
60
      pos], 1);
                                                                  different versions of the segtree between each
61
                                                                  update
           seg[e[pos]] = apply_lazy(seg[e[pos]], lazy[
62
                                                            _{\rm 3} // Indexed at one
      pos], m - ini + 1);
                                                            4 // Query - get sum of elements from range (1, r)
           seg[d[pos]] = apply_lazy(seg[d[pos]], lazy[
63
                                                                  inclusive
      pos], fim - m);
                                                            _{5} // Update - update element at position id to a value
64
                                                                  val
           lazy[pos] = NEUTRAL_LAZY;
65
                                                            6
                                                            7 // Problem:
66
67
                                                            8 // https://cses.fi/problemset/task/1737/
       ftype f(ftype a, ftype b) {
68
69
          return a + b;
                                                           10 // Complexity:
70
                                                           11 // O(log n) for both query and update
71
                                                           12
       ftype create() {
72
                                                           _{13} // How to use:
           seg.push_back(0);
                                                           14 // vector <int > raiz(MAX); // vector to store the
           e.push_back(0);
74
                                                                  roots of each version
           d.push_back(0);
                                                           15 // Segtree seg = Segtree(INF);
           lazy.push_back(-1);
76
                                                           16 // raiz[0] = seg.create(); // null node
           return seg.size() - 1;
                                                           _{\rm 17} // curr = 1; // keep track of the last version
77
      }
78
79
                                                           19 // raiz[k] = seg.update(raiz[k], idx, val); //
       ftype query(int pos, int ini, int fim, int p, int
80
                                                                 updating version k
                                                           20 // seg.query(raiz[k], l, r) // querying version k
           propagate(pos, ini, fim);
81
                                                           21 // raiz[++curr] = raiz[k]; // create a new version
           if (q < ini || p > fim) return NEUTRAL;
82
                                                                  based on version k
```

```
55
23 const int MAX = 2e5+17;
                                                           56
                                                                  int update(int pos, int ini, int fim, int id, int
24 const int INF = 1e9+17;
                                                                  val) {
                                                                      int novo = create();
                                                           57
26 typedef long long ftype;
                                                                      seg[novo] = seg[pos];
27
                                                           59
28 struct Segtree {
                                                                      e[novo] = e[pos];
      vector < ftype > seg, d, e;
                                                                      d[novo] = d[pos];
29
                                                           61
      const ftype NEUTRAL = 0;
                                                           62
30
                                                                      if (ini == fim) {
31
      int n;
                                                           63
                                                                          seg[novo] = val;
32
                                                           64
33
      Segtree(int n) {
                                                           65
                                                                          return novo;
                                                                      }
         this ->n = n;
34
                                                           66
                                                           67
35
                                                                      int m = (ini + fim) >> 1;
36
                                                           68
      ftype f(ftype a, ftype b) {
37
                                                           69
                                                                      if (id <= m) e[novo] = update(e[novo], ini, m</pre>
          return a + b;
                                                                  , id, val);
39
                                                                      else d[novo] = update(d[novo], m + 1, fim, id
40
      ftype create() {
                                                                  , val);
41
          seg.push_back(0);
                                                           72
42
                                                                      seg[novo] = f(seg[e[novo]], seg[d[novo]]);
43
           e.push_back(0);
                                                           73
          d.push_back(0);
                                                           74
44
          return seg.size() - 1;
                                                           75
                                                                      return novo;
                                                           76
46
47
      ftype query(int pos, int ini, int fim, int p, int 78
                                                                  ftype query(int pos, int p, int q) {
48
       q) {
                                                                      return query(pos, 1, n, p, q);
49
          if (q < ini || p > fim) return NEUTRAL;
           if (pos == 0) return 0;
50
                                                           81
           if (p <= ini && fim <= q) return seg[pos];</pre>
                                                                  int update(int pos, int id, int val) {
51
                                                           82
          int m = (ini + fim) >> 1;
                                                                      return update(pos, 1, n, id, val);
52
                                                           83
          return f(query(e[pos], ini, m, p, q), query(d84
53
       [pos], m + 1, fim, p, q));
                                                           85 };
54
```