

Notebook - Maratona de Programação

Lenhadoras de Segtree

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1 Misc

1.1 Split

```
vector < string > split(string txt, char key = ', '){
      vector < string > ans;
       string palTemp = "";
      for(int i = 0; i < txt.size(); i++){</pre>
           if(txt[i] == key){
              if(palTemp.size() > 0){
                   ans.push_back(palTemp);
                   palTemp = "";
1.0
               }
11
12
           } else{
               palTemp += txt[i];
13
           }
1.5
16
17
18
       if(palTemp.size() > 0)
          ans.push_back(palTemp);
2.0
       return ans;
22 }
  1.2 Int128
1 __int128 read() {
       _{-}int128 x = 0, f = 1;
       char ch = getchar();
       while (ch < '0' || ch > '9') {
```

```
if (ch == '-') f = -1;
          ch = getchar();
      while (ch >= '0' && ch <= '9') {
         x = x * 10 + ch - '0';
          ch = getchar();
10
11
      return x * f;
12
13 }
14 void print(__int128 x) {
      if (x < 0) {
15
          putchar('-');
16
          x = -x;
1.7
      if (x > 9) print(x / 10);
1.9
      putchar(x % 10 + '0');
20
21 }
```

2 Geometry

3 Data Structures

3.1 Range Query Point Update

```
10 // O(log n) for both query and update
12 // How to use:
13 // Segtree seg = Segtree(n);
14 // seg.build(v);
16 // Notes
_{
m 17} // Change neutral element and f function to perform a
       different operation
19 // If you want to change the operations to point
       query and range update
_{20} // Use the same segtree, but perform the following
      operations
21 // Query - seg.query(0, id);
22 // Update - seg.update(1, v); seg.update(r + 1, -v);
24 typedef long long ftype;
26 struct Segtree {
      vector < ftype > seg;
27
       int n;
28
      const ftype NEUTRAL = 0;
29
       Segtree(int n) {
3.1
32
           int sz = 1;
           while (sz < n) sz *= 2;
33
           this -> n = sz;
34
35
           seg.assign(2*sz, NEUTRAL);
3.6
37
38
39
       ftype f(ftype a, ftype b) {
40
          return a + b;
41
       ftype query(int pos, int ini, int fim, int p, int
43
        q) {
44
           if (ini >= p && fim <= q) {</pre>
               return seg[pos];
45
46
47
           if (q < ini || p > fim) {
49
               return NEUTRAL;
50
51
           int e = 2*pos + 1;
52
           int d = 2*pos + 2;
           int m = ini + (fim - ini) / 2;
5.4
55
56
           return f(query(e, ini, m, p, q), query(d, m +
        1, fim, p, q));
57
5.8
59
       void update(int pos, int ini, int fim, int id,
       int val) {
           if (ini > id || fim < id) {</pre>
6.0
               return;
61
62
           if (ini == id && fim == id) {
64
               seg[pos] = val;
6.5
               return:
           int e = 2*pos + 1;
70
           int d = 2*pos + 2;
           int m = ini + (fim - ini) / 2;
72
           update(e, ini, m, id, val);
74
           update(d, m + 1, fim, id, val);
```

```
seg[pos] = f(seg[e], seg[d]);
                                                                   vector < ftype > seg;
                                                            26
78
                                                            27
                                                                   int n;
                                                                   const ftype NEUTRAL = mp(INF, 0);
79
                                                            28
       void build(int pos, int ini, int fim, vector<int>29
80
                                                                   Segtree(int n) {
           if (ini == fim) {
                                                                       int sz = 1;
81
                                                            31
                if (ini < (int)v.size()) {</pre>
                                                                        while (sz < n) sz *= 2;
82
                    seg[pos] = v[ini];
                                                                       this - > n = sz:
83
                                                            3.3
84
                                                            34
                return;
                                                            35
                                                                       seg.assign(2*sz, NEUTRAL);
           }
86
                                                            36
                                                            37
           int e = 2*pos + 1;
                                                                   ftype f(ftype a, ftype b) {
                                                            38
           int d = 2*pos + 2;
                                                                       if (a.ff < b.ff) return a;</pre>
                                                            39
           int m = ini + (fim - ini) / 2;
                                                                       if (b.ff < a.ff) return b;</pre>
9.0
                                                            40
91
                                                            41
92
           build(e, ini, m, v);
                                                            42
                                                                        return mp(a.ff, a.ss + b.ss);
           build(d, m + 1, fim, v);
93
                                                            43
           seg[pos] = f(seg[e], seg[d]);
                                                                   ftype query(int pos, int ini, int fim, int p, int
9.5
                                                            45
96
                                                                    q) {
                                                                       if (ini >= p && fim <= q) {</pre>
                                                            46
97
       ftype query(int p, int q) {
                                                                           return seg[pos];
98
                                                            47
          return query(0, 0, n - 1, p, q);
100
                                                            49
                                                            5.0
                                                                       if (q < ini || p > fim) {
       void update(int id, int val) {
                                                                            return NEUTRAL;
102
                                                            51
           update(0, 0, n - 1, id, val);
                                                            52
103
                                                            53
104
                                                                       int e = 2*pos + 1;
105
                                                            5.4
       void build(vector<int> &v) {
                                                                        int d = 2*pos + 2;
106
                                                            55
                                                                       int m = ini + (fim - ini) / 2;
           build(0, 0, n - 1, v);
                                                            5.6
                                                            5.7
108
109
                                                            58
                                                                        return f(query(e, ini, m, p, q), query(d, m +
       void debug() {
                                                                    1, fim, p, q));
110
           for (auto e : seg) {
                                                            59
                cout << e << ' ';
                                                            60
                                                                   void update(int pos, int ini, int fim, int id,
113
                                                            61
            cout << '\n';
                                                                   int val) {
114
                                                                      if (ini > id || fim < id) {</pre>
115
                                                            62
116 };
                                                            63
                                                                            return;
                                                            64
   3.2 Minimum And Amount
                                                                        if (ini == id && fim == id) {
                                                            66
                                                                            seg[pos] = mp(val, 1);
                                                            67
 1 // Description:
 2 // Query - get minimum element in a range (1, r)
                                                            68
                                                                            return:
       inclusive
                                                            6.9
 _{\rm 3} // and also the number of times it appears in that
       range
                                                                       int e = 2*pos + 1;
 _4 // Update - update element at position id to a value ^{72}
                                                                        int d = 2*pos + 2;
                                                            73
       val
                                                                       int m = ini + (fim - ini) / 2;
                                                            74
 6 // Problem:
                                                            75
                                                                        update(e, ini, m, id, val);
 7 // https://codeforces.com/edu/course/2/lesson/4/1/
                                                            7.6
                                                            7.7
                                                                        update(d, m + 1, fim, id, val);
      practice/contest/273169/problem/C
                                                            78
                                                                        seg[pos] = f(seg[e], seg[d]);
 9 // Complexity:
                                                            79
                                                            80
_{10} // O(log n) for both query and update
                                                            81
                                                                   void build(int pos, int ini, int fim, vector<int>
                                                            82
12 // How to use:
13 // Segtree seg = Segtree(n);
                                                                    &v) {
                                                                       if (ini == fim) {
14 // seg.build(v);
                                                            83
                                                                            if (ini < (int)v.size()) {</pre>
                                                            84
                                                                                seg[pos] = mp(v[ini], 1);
16 #define pii pair<int, int>
                                                            85
17 #define mp make_pair
18 #define ff first
                                                            87
                                                                            return:
                                                            88
19 #define ss second
                                                            89
                                                                        int e = 2*pos + 1;
                                                            90
21 const int INF = 1e9+17;
                                                                        int d = 2*pos + 2;
                                                            91
                                                                       int m = ini + (fim - ini) / 2;
                                                            92
23 typedef pii ftype;
                                                            93
```

94

25 struct Segtree {

build(e, ini, m, v);

```
build(d, m + 1, fim, v);
                                                                      return a + b:
9.5
                                                           4.1
96
                                                           42
           seg[pos] = f(seg[e], seg[d]);
97
                                                           43
98
                                                           44
                                                                  ftype create() {
                                                                      seg.push_back(0);
                                                          45
       ftype query(int p, int q) {
                                                                      e.push_back(0);
100
                                                           46
           return query(0, 0, n - 1, p, q);
                                                           47
                                                                      d.push_back(0);
                                                                      return seg.size() - 1;
                                                           48
103
                                                          49
       void update(int id, int val) {
                                                           50
104
           update(0, 0, n - 1, id, val);
                                                                  ftype query(int pos, int ini, int fim, int p, int
105
                                                           51
106
                                                                      if (q < ini || p > fim) return NEUTRAL;
                                                           5.2
       void build(vector<int> &v) {
                                                                      if (pos == 0) return 0;
                                                           53
108
                                                                      if (p <= ini && fim <= q) return seg[pos];</pre>
109
           build(0, 0, n - 1, v);
                                                           5.4
                                                           55
                                                                      int m = (ini + fim) >> 1;
110
                                                           56
                                                                      return f(query(e[pos], ini, m, p, q), query(d
       void debug() {
                                                                  [pos], m + 1, fim, p, q));
112
           for (auto e : seg) {
                                                           57
               cout << e.ff << ' ' << e.ss << '\n';
114
                                                           5.8
                                                                  void update(int pos, int ini, int fim, int id,
115
                                                           59
           cout << '\n';</pre>
                                                                  int val) {
116
                                                                      if (ini > id || fim < id) {</pre>
117
                                                           6.0
118 };
                                                           61
                                                                          return;
                                                           62
   3.3 Dynamic Implicit Sparse
                                                           63
                                                                      if (ini == fim) {
                                                           64
                                                                          seg[pos] = val;
 1 // Description:
                                                           6.5
 2 // Indexed at one
                                                                          return:
                                                           6.7
                                                           68
 _{4} // When the indexes of the nodes are too big to be
       stored in an array
                                                           69
                                                                      int m = (ini + fim) >> 1;
                                                           7.0
 _{5} // and the queries need to be answered online so we
       can't sort the nodes and compress them
                                                           7.1
                                                                      if (id <= m) {
 _{6} // we create nodes only when they are needed so there ^{72}
                                                                          if (e[pos] == 0) e[pos] = create();
       'll be (Q*log(MAX)) nodes
                                                                          update(e[pos], ini, m, id, val);
 _{7} // where Q is the number of queries and MAX is the
                                                           7.4
                                                           7.5
       maximum index a node can assume
                                                                          if (d[pos] == 0) d[pos] = create();
                                                                          update(d[pos], m + 1, fim, id, val);
                                                           7.7
 9 // Query - get sum of elements from range (1, r)
       inclusive
_{10} // Update - update element at position id to a value ^{79}
                                                                      seg[pos] = f(seg[e[pos]], seg[d[pos]]);
       val
                                                           8.1
12 // Problem:
                                                           82
                                                           83
                                                                  ftype query(int p, int q) {
13 // https://cses.fi/problemset/task/1648
                                                                      return query(1, 1, n, p, q);
                                                           84
15 // Complexity:
16 // O(log n) for both query and update
                                                           86
                                                                  void update(int id, int val) {
                                                                      update(1, 1, n, id, val);
                                                           88
18 // How to use:
_{19} // MAX is the maximum index a node can assume
                                                           89
                                                           90 };
20 // Create a default null node
_{21} // Create a node to be the root of the segtree
                                                                   Lazy Dynamic Implicit Sparse
22
23 // Segtree seg = Segtree(MAX);
24 // seg.create();
                                                            1 // Description:
25 // seg.create();
                                                            2 // Indexed at one
                                                            _{4} // When the indexes of the nodes are too big to be
27 typedef long long ftype;
                                                                  stored in an array
                                                            _{5} // and the queries need to be answered online so we
29 const int MAX = 1e9+17;
                                                                  can't sort the nodes and compress them
31 struct Segtree {
                                                            6 // we create nodes only when they are needed so there
       vector < ftype > seg, d, e, lazy;
                                                                  'll be (Q*log(MAX)) nodes
32
       const ftype NEUTRAL = 0;
                                                            _{7} // where Q is the number of queries and MAX is the
33
34
       int n;
                                                                  maximum index a node can assume
35
       Segtree(int n) {
                                                            9 // Query - get sum of elements from range (1, r)
           this -> n = n;
                                                                  inclusive
3.7
```

val

3.9

40

ftype f(ftype a, ftype b) {

10 // Update - update element at position id to a value

```
12 // Problem:
                                                           8.1
13 // https://oj.uz/problem/view/IZhO12_apple
                                                           82
                                                                  ftype query(int pos, int ini, int fim, int p, int
                                                           8.3
15 // Complexity:
                                                                   q) {
16 // O(log n) for both query and update
                                                           84
                                                                      propagate(pos, ini, fim);
                                                                      if (q < ini || p > fim) return NEUTRAL;
17
                                                           85
18 // How to use:
                                                                      if (pos == 0) return 0;
_{19} // MAX is the maximum index a node can assume
                                                                      if (p <= ini && fim <= q) return seg[pos];</pre>
                                                           87
                                                                      int m = (ini + fim) >> 1;
20 // Create a default null node
                                                           88
_{21} // Create a node to be the root of the segtree
                                                                      return f(query(e[pos], ini, m, p, q), query(d
                                                           89
                                                                  [pos], m + 1, fim, p, q));
23 // Segtree seg = Segtree(MAX);
                                                           90
24 // seg.create();
                                                           91
25 // seg.create();
                                                                  void update(int pos, int ini, int fim, int p, int
                                                           92
26
                                                                   q, int val) {
                                                                      propagate(pos, ini, fim);
27 typedef long long ftype;
                                                           93
                                                           94
                                                                      if (ini > q || fim < p) {</pre>
29 const int MAX = 1e9+17;
                                                           9.5
                                                                           return:
31 typedef long long ftype;
                                                           97
                                                           98
                                                                      if (ini >= p && fim <= q) {</pre>
32
33 const int MAX = 1e9+17:
                                                           99
                                                                           lazy[pos] = apply_lazy(lazy[pos], val, 1)
3.4
35 struct Segtree {
                                                                           seg[pos] = apply_lazy(seg[pos], val, fim
      vector < ftype > seg, d, e, lazy;
                                                                  - ini + 1):
36
37
       const ftype NEUTRAL = 0;
38
      const ftype NEUTRAL_LAZY = -1;
                                                           102
                                                                           return;
39
      int n;
                                                           103
40
                                                           104
                                                                      int m = (ini + fim) >> 1:
      Segtree(int n) {
4.1
                                                           105
42
          this -> n = n;
                                                                      if (e[pos] == 0) e[pos] = create();
43
                                                                      update(e[pos], ini, m, p, q, val);
                                                           108
44
45
      ftype apply_lazy(ftype a, ftype b, int len) {
           if (b == NEUTRAL_LAZY) return a;
                                                                      if (d[pos] == 0) d[pos] = create();
46
                                                          110
           else return b * len;
                                                                      update(d[pos], m + 1, fim, p, q, val);
48
                                                           113
                                                                      seg[pos] = f(seg[e[pos]], seg[d[pos]]);
49
      void propagate(int pos, int ini, int fim) {
                                                                  }
50
                                                          114
          if (seg[pos] == 0) return;
51
                                                           115
52
                                                           116
                                                                  ftype query(int p, int q) {
           if (ini == fim) {
                                                                      return query(1, 1, n, p, q);
53
54
               return;
                                                          118
5.5
           }
                                                          119
                                                                  void update(int p, int q, int val) {
56
                                                           120
           int m = (ini + fim) >> 1;
                                                                      update(1, 1, n, p, q, val);
57
                                                          122
           if (e[pos] == 0) e[pos] = create();
                                                          123 };
           if (d[pos] == 0) d[pos] = create();
6.0
                                                              3.5 Lazy
61
          lazy[e[pos]] = apply_lazy(lazy[e[pos]], lazy[
62
      pos], 1);
                                                            1 // Description:
          lazy[d[pos]] = apply\_lazy(lazy[d[pos]], lazy[$_2$ // Query - get sum of elements from range (1, r) \\
      pos], 1);
                                                                  inclusive
                                                            _{3} // Update - add a value val to elementos from range (
64
           seg[e[pos]] = apply_lazy(seg[e[pos]], lazy[
65
                                                                 l, r) inclusive
      pos], m - ini + 1);
           seg[d[pos]] = apply_lazy(seg[d[pos]], lazy[
66
                                                            5 // Problem:
      pos], fim - m);
                                                            6 // https://codeforces.com/edu/course/2/lesson/5/1/
                                                                 practice/contest/279634/problem/A
           lazy[pos] = NEUTRAL_LAZY;
68
69
                                                            8 // Complexity:
70
                                                            9 // O(log n) for both query and update
      ftype f(ftype a, ftype b) {
71
          return a + b;
                                                           _{11} // How to use:
73
                                                           12 // Segtree seg = Segtree(n);
                                                           13 // seg.build(v);
74
      ftype create() {
75
7.6
           seg.push_back(0);
                                                           15 // Notes
           e.push_back(0);
                                                           _{16} // Change neutral element and f function to perform a
           d.push_back(0);
78
                                                                   different operation
           lazy.push_back(-1);
80
           return seg.size() - 1;
                                                           18 typedef long long ftype;
```

```
19
                                                           87
20 struct Segtree {
                                                           88
      vector < ftype > seg;
                                                                       if (ini >= p && fim <= q) {</pre>
                                                           8.9
       vector < ftype > lazy;
                                                           90
                                                                           lazy[pos] = apply_lazy(lazy[pos], val, 1)
22
       const ftype NEUTRAL = 0;
                                                                           seg[pos] = apply_lazy(seg[pos], val, fim
24
                                                           91
       const ftype NEUTRAL_LAZY = -1;
                                                                   - ini + 1);
26
                                                           92
       Segtree(int n) {
                                                                           return;
27
                                                           93
                                                                       }
           int sz = 1;
                                                           94
           while (sz < n) sz *= 2;
29
                                                           95
                                                                       int e = 2*pos + 1;
           this -> n = sz;
                                                           96
                                                                       int d = 2*pos + 2;
3.1
                                                           97
           seg.assign(2*sz, NEUTRAL);
                                                                       int m = ini + (fim - ini) / 2;
32
33
           lazy.assign(2*sz, NEUTRAL_LAZY);
                                                           99
                                                                       update(e, ini, m, p, q, val);
34
                                                           100
35
                                                                       update(d, m + 1, fim, p, q, val);
       ftype apply_lazy(ftype a, ftype b, int len) {
36
                                                           102
           if (b == NEUTRAL_LAZY) return a;
                                                                       seg[pos] = f(seg[e], seg[d]);
           if (a == NEUTRAL_LAZY) return b * len;
38
                                                           104
           else return a + b * len;
39
                                                                   void build(int pos, int ini, int fim, vector<int>
40
                                                           106
                                                                   &v) {
41
       void propagate(int pos, int ini, int fim) {
                                                                       if (ini == fim) {
          if (ini == fim) {
                                                                           if (ini < (int)v.size()) {</pre>
43
                                                           108
               return;
                                                                               seg[pos] = v[ini];
44
                                                           109
45
                                                           110
46
                                                                           return:
           int e = 2*pos + 1;
                                                                       }
                                                           112
           int d = 2*pos + 2;
48
                                                           113
           int m = ini + (fim - ini) / 2;
                                                                       int e = 2*pos + 1;
49
                                                           114
                                                                       int d = 2*pos + 2;
50
                                                           115
           lazy[e] = apply_lazy(lazy[e], lazy[pos], 1); 116
                                                                       int m = ini + (fim - ini) / 2;
5.1
           lazy[d] = apply_lazy(lazy[d], lazy[pos], 1); 117
                                                                       build(e, ini, m, v);
53
                                                           118
           seg[e] = apply_lazy(seg[e], lazy[pos], m -
                                                                       build(d, m + 1, fim, v);
                                                           119
      ini + 1):
                                                           120
55
           seg[d] = apply_lazy(seg[d], lazy[pos], fim - 121
                                                                       seg[pos] = f(seg[e], seg[d]);
      m);
56
                                                           123
           lazy[pos] = NEUTRAL_LAZY;
                                                           124
                                                                  ftype query(int p, int q) {
                                                                      return query(0, 0, n - 1, p, q);
58
                                                           125
59
                                                           126
6.0
       ftype f(ftype a, ftype b) {
                                                           127
           return a + b;
                                                                  void update(int p, int q, int val) {
61
                                                           128
                                                                       update(0, 0, n - 1, p, q, val);
62
                                                           129
63
       ftype query(int pos, int ini, int fim, int p, int131
                                                                  void build(vector<int> &v) {
                                                           132
          propagate(pos, ini, fim);
                                                           133
                                                                       build(0, 0, n - 1, v);
                                                           134
66
           if (ini >= p && fim <= q) {</pre>
67
                                                           135
              return seg[pos];
                                                                   void debug() {
                                                           136
                                                                       for (auto e : seg) {
69
                                                           137
                                                           138
                                                                           cout << e << ' ';
7.0
           if (q < ini || p > fim) {
71
                                                           139
                                                                       cout << '\n';
               return NEUTRAL;
                                                           140
                                                                       for (auto e : lazy) {
                                                           141
                                                                           cout << e << ' ';
74
                                                           142
           int e = 2*pos + 1;
                                                                       cout << '\n';
           int d = 2*pos + 2;
7.6
                                                           144
           int m = ini + (fim - ini) / 2;
                                                                       cout << '\n';
                                                           145
           return f(query(e, ini, m, p, q), query(d, m +147 );
79
       1, fim, p, q));
                                                              3.6 Segment With Maximum Sum
80
81
       void update(int pos, int ini, int fim, int p, int 1 // Description:
       q, int val) {
                                                           2 // Query - get sum of segment that is maximum among
           propagate(pos, ini, fim);
                                                                  all segments
                                                            3 // E.g
84
           if (ini > q || fim < p) {</pre>
85
                                                            4 // Array: 5 -4 4 3 -5
86
               return;
                                                            _{5} // Maximum segment sum: 8 because 5 + (-4) + 4 = 8
```

```
6 // Update - update element at position id to a value 70
                                                                      int e = 2*pos + 1;
                                                           7.2
8 // Problem:
                                                                      int d = 2*pos + 2;
                                                           7.3
9 // https://codeforces.com/edu/course/2/lesson/4/2/
                                                           74
                                                                      int m = ini + (fim - ini) / 2;
      practice/contest/273278/problem/A
                                                           7.5
                                                                      return f(query(e, ini, m, p, q), query(d, m +
11 // Complexity:
                                                                   1, fim, p, q));
12 // O(log n) for both query and update
                                                                  }
                                                           78
14 // How to use:
                                                                  void update(int pos, int ini, int fim, int id,
                                                           79
15 // Segtree seg = Segtree(n);
                                                                  int val) {
                                                                      if (ini > id || fim < id) {</pre>
16 // seg.build(v);
                                                           8.0
                                                                          return:
                                                           81
18 // Notes
                                                           82
19 // The maximum segment sum can be a negative number
                                                           83
                                                                      if (ini == id && fim == id) {
20 // In that case, taking zero elements is the best
                                                           84
                                                                           seg[pos] = Node(val, val, val, val);
      choice
                                                           8.5
21 // So we need to take the maximum between 0 and the
                                                                          return:
      query
                                                           87
22 // max(OLL, seg.query(0, n).max_seg)
                                                           88
                                                           89
24 using ll = long long;
                                                                      int e = 2*pos + 1;
                                                           9.0
                                                                      int d = 2*pos + 2;
                                                           91
26 typedef ll ftype_node;
                                                                      int m = ini + (fim - ini) / 2;
                                                           92
                                                           93
28 struct Node {
                                                           94
                                                                      update(e, ini, m, id, val);
      ftype_node max_seg;
                                                                      update(d, m + 1, fim, id, val);
29
                                                           95
      ftype_node pref;
30
                                                           96
      ftype_node suf;
                                                                      seg[pos] = f(seg[e], seg[d]);
3.1
                                                           97
32
      ftype_node sum;
                                                           98
3.3
                                                           99
      Node(ftype_node max_seg, ftype_node pref,
                                                                  void build(int pos, int ini, int fim, vector<int>
34
                                                          100
      ftype_node suf, ftype_node sum) : max_seg(max_seg
                                                                   &v) {
                                                                      if (ini == fim) {
      ), pref(pref), suf(suf), sum(sum) {};
                                                                           // se a çãposio existir no array original
35 }:
                                                                           // seg tamanho potencia de dois
36
                                                                           if (ini < (int)v.size()) {</pre>
37 typedef Node ftype;
                                                          104
                                                                               seg[pos] = Node(v[ini], v[ini], v[ini
39 struct Segtree {
                                                                  ], v[ini]);
40
      vector < ftype > seg;
                                                                          }
      int n;
41
                                                                          return;
      const ftype NEUTRAL = Node(0, 0, 0, 0);
                                                          108
42
43
                                                          109
                                                                      int e = 2*pos + 1;
      Segtree(int n) {
                                                          110
44
           int sz = 1;
                                                                      int d = 2*pos + 2;
45
           // potencia de dois mais proxima
                                                                      int m = ini + (fim - ini) / 2;
46
                                                          112
           while (sz < n) sz *= 2;
                                                          113
           this -> n = sz;
                                                                      build(e, ini, m, v);
48
                                                          114
                                                          115
                                                                      build(d, m + 1, fim, v);
49
           // numero de nos da seg
                                                          116
50
           seg.assign(2*sz, NEUTRAL);
                                                                      seg[pos] = f(seg[e], seg[d]);
51
                                                          117
52
                                                          118
53
                                                          119
      ftype f(ftype a, ftype b) {
                                                                  ftype query(int p, int q) {
54
                                                          120
           ftype_node max_seg = max({a.max_seg, b.
                                                                      return query(0, 0, n - 1, p, q);
5.5
      max_seg, a.suf + b.pref});
           ftype_node pref = max(a.pref, a.sum + b.pref)123
56
                                                                  void update(int id, int val) {
                                                          124
           ftype_node suf = max(b.suf, b.sum + a.suf);
                                                                      update(0, 0, n - 1, id, val);
           ftype_node sum = a.sum + b.sum;
5.8
                                                           126
59
           return Node(max_seg, pref, suf, sum);
                                                                  void build(vector<int> &v) {
60
                                                          128
      }
                                                                      build(0, 0, n - 1, v);
                                                          129
61
      ftype query(int pos, int ini, int fim, int p, int131
63
       q) {
                                                                  void debug() {
                                                          132
          if (ini >= p && fim <= q) {</pre>
                                                          133
                                                                      for (auto e : seg) {
64
                                                                          cout << e.max_seg << ', ' << e.pref << ', '
               return seg[pos];
                                                          134
6.5
                                                                   << e.suf << ' ' << e.sum << '\n';
           }
                                                          135
67
           if (q < ini || p > fim) {
                                                                      cout << '\n';
69
               return NEUTRAL;
                                                          137
```

```
138 };
                                                            64
   3.7
         Segtree2d
                                                                    void updateY(int noX, int lX, int rX, int noY,
                                                            66
                                                                    int lY, int rY, int y){
                                                                        if(1Y == rY){
 1 // Description:
                                                                            if(1X == rX){
 2 // Indexed at zero
                                                            68
                                                                                seg[noX][noY] = !seg[noX][noY];
 _{\rm 3} // Given a N x M grid, where i represents the row and ^{69}
                                                                            }else{
        j the column, perform the following operations
                                                                                seg[noX][noY] = seg[2*noX+1][noY] +
 4 // update(j, i) - update the value of grid[i][j]
                                                                    seg[2*noX+2][noY];
 5 // query(j1, j2, i1, i2) - return the sum of values
       inside the rectangle
 _{6} // defined by grid[i1][j1] and grid[i2][j2] inclusive ^{73}
                                                                        }else{
                                                                            int m = (1Y+rY)/2;
 8 // Problem:
                                                            7.5
 9 // https://cses.fi/problemset/task/1739/
                                                            7.6
                                                                            if(y \le m){
                                                                                updateY(noX, 1X, rX, 2*noY+1,1Y, m, y
11 // Complexity:
                                                                            else if(m < y)
12 // Time complexity:
                                                                                updateY(noX, 1X, rX, 2*noY+2, m+1, rY
13 // O(\log N * \log M) for both query and update
_{14} // O(N * M) for build
                                                                    , y);
                                                            80
15 // Memory complexity:
16 // 4 * M * N
                                                             81
                                                                            seg[noX][noY] = seg[noX][2*noY+1] + seg[
                                                            82
                                                                   noX][2*noY+2];
18 // How to use:
19 // Segtree2D seg = Segtree2D(n, n);
                                                            83
                                                                        }
20 // vector<vector<int>> v(n, vector<int>(n));
                                                            84
21 // seg.build(v);
                                                            85
                                                                   void updateX(int noX, int lX, int rX, int x, int
                                                            86
23 // Notes
                                                                        int m = (1X+rX)/2:
24 // Indexed at zero
                                                            87
                                                            88
                                                                        if(1X != rX){
26 struct Segtree 2D {
                                                            89
                                                                            if(x <= m){
                                                            90
       const int MAXN = 1025;
27
                                                                                updateX(2*noX+1, 1X, m, x, y);
       int N, M;
                                                            91
28
                                                                            else if(m < x)
                                                            92
                                                                                updateX(2*noX+2, m+1, rX, x, y);
                                                            93
       vector < vector < int >> seg;
3.0
                                                            94
31
                                                                        }
                                                            95
32
       Segtree2D(int N, int M) {
           this -> N = N;
                                                            96
33
                                                                        updateY(noX, 1X, rX, 0, 0, M - 1, y);
                                                            97
            this -> M = M;
34
                                                            98
                                                                   }
            seg.resize(2*MAXN, vector<int>(2*MAXN));
3.5
                                                            99
                                                                    int queryY(int noX, int noY, int lY, int rY, int
37
                                                                   aY, int bY){
       void buildY(int noX, int lX, int rX, int noY, int
38
                                                                        if(aY <= 1Y && rY <= bY) return seg[noX][noY</pre>
        1Y, int rY, vector < vector < int >> &v) {
                                                                   ];
           if(1Y == rY){
39
40
                if(1X == rX){
                    seg[noX][noY] = v[rX][rY];
                                                                        int m = (1Y+rY)/2;
41
                                                            104
42
                                                                        if(bY <= m) return queryY(noX, 2*noY+1, 1Y, m</pre>
                    seg[noX][noY] = seg[2*noX+1][noY] +
43
                                                                    , aY, bY);
       seg[2*noX+2][noY];
                                                                       if(m < aY) return queryY(noX, 2*noY+2, m+1,</pre>
44
                }
                                                                    rY, aY, bY);
           }else{
45
                int m = (1Y+rY)/2;
46
                                                                        return queryY(noX, 2*noY+1, 1Y, m, aY, bY) +
                                                            108
47
                                                                    queryY(noX, 2*noY+2, m+1, rY, aY, bY);
                buildY(noX, 1X, rX, 2*noY+1, 1Y, m, v);
48
                buildY(noX, 1X, rX, 2*noY+2, m+1, rY, v);109
49
50
                                                                    int queryX(int noX, int 1X, int rX, int aX, int
                seg[noX][noY] = seg[noX][2*noY+1] + seg[111]
                                                                   bX, int aY, int bY){
       noX][2*noY+2];
                                                                        if(aX <= lX && rX <= bX) return queryY(noX,</pre>
           }
                                                                    0, 0, M - 1, aY, bY);
53
5.4
                                                                        int m = (1X+rX)/2;
55
       void buildX(int noX, int 1X, int rX, vector<</pre>
                                                            114
       vector < int >> &v) {
           if(1X != rX){
                                                                        if(bX <= m) return queryX(2*noX+1, lX, m, aX,</pre>
                                                                    bX, aY, bY);
                int m = (1X+rX)/2;
57
                                                                        if(m < aX) return queryX(2*noX+2, m+1, rX, aX</pre>
58
                                                                    , bX, aY, bY);
                buildX(2*noX+1, lX, m, v);
                buildX(2*noX+2, m+1, rX, v);
60
                                                                        return queryX(2*noX+1, 1X, m, aX, bX, aY, bY)
            }
                                                            119
                                                                      queryX(2*noX+2, m+1, rX, aX, bX, aY, bY);
                                                            120
            buildY(noX, 1X, rX, 0, 0, M - 1, v);
```

```
if (pos == 0) return 0;
                                                            5.0
       void build(vector<vector<int>> &v) {
                                                            51
                                                                       if (p <= ini && fim <= q) return seg[pos];</pre>
                                                                       int m = (ini + fim) >> 1;
           buildX(0, 0, N - 1, v);
                                                            5.2
124
                                                                       return f(query(e[pos], ini, m, p, q), query(d
                                                                   [pos], m + 1, fim, p, q));
       int query(int aX, int bX, int aY, int bY) {
126
                                                            54
           return queryX(0, 0, N - 1, aX, bX, aY, bY);
                                                                   int update(int pos, int ini, int fim, int id, int
128
                                                            56
                                                                    val) {
129
       void update(int x, int y) {
                                                                       int novo = create();
130
                                                            5.7
           updateX(0, 0, N - 1, x, y);
131
                                                            58
132
                                                            59
                                                                       seg[novo] = seg[pos];
133 };
                                                            6.0
                                                                       e[novo] = e[pos];
                                                                       d[novo] = d[pos];
                                                            61
   3.8 Persistent
                                                            62
                                                                       if (ini == fim) {
                                                            63
                                                                           seg[novo] = val;
 1 // Description:
                                                                           return novo;
 2 // Persistent segtree allows for you to save the
                                                            6.5
       different versions of the segtree between each
       update
                                                            6.7
 _3 // Indexed at one
                                                                       int m = (ini + fim) >> 1;
                                                            68
 4 // Query - get sum of elements from range (1, r)
                                                                       if (id <= m) e[novo] = update(e[novo], ini, m</pre>
       inclusive
                                                            7.0
                                                                   , id, val);
 5 // Update - update element at position id to a value
                                                                       else d[novo] = update(d[novo], m + 1, fim, id
       val
                                                                   , val);
 7 // Problem:
                                                                       seg[novo] = f(seg[e[novo]], seg[d[novo]]);
                                                            73
 8 // https://cses.fi/problemset/task/1737/
                                                            74
10 // Complexity:
                                                                       return novo:
                                                            7.5
                                                            76
11 // O(log n) for both query and update
                                                            7.7
                                                                   ftype query(int pos, int p, int q) {
                                                            7.8
13 // How to use:
14 // vector <int > raiz(MAX); // vector to store the
                                                            79
                                                                       return query(pos, 1, n, p, q);
       roots of each version
                                                            80
15 // Segtree seg = Segtree(INF);
                                                                   int update(int pos, int id, int val) {
16 // raiz[0] = seg.create(); // null node
                                                            82
_{17} // curr = 1; // keep track of the last version
                                                            83
                                                                       return update(pos, 1, n, id, val);
                                                            84
                                                            85 };
19 // raiz[k] = seg.update(raiz[k], idx, val); //
      updating version k
                                                                   \mathbf{Dsu}
                                                              3.9
20 // seg.query(raiz[k], l, r) // querying version k
21 // raiz[++curr] = raiz[k]; // create a new version
       based on version k
                                                             # #include <bits/stdc++.h>
23 const int MAX = 2e5+17;
                                                            3 using namespace std;
24 const int INF = 1e9+17;
                                                            5 const int MAX = 1e6+17;
26 typedef long long ftype;
                                                            7 struct DSU {
27
28 struct Segtree {
                                                                  int n;
       vector < ftype > seg, d, e;
                                                                   vector < int > link, sizes;
       const ftype NEUTRAL = 0;
30
                                                            10
                                                                   DSU(int n) {
31
       int n;
                                                                       this -> n = n:
32
                                                            12
33
       Segtree(int n) {
                                                            13
                                                                       link.assign(n+1, 0);
           this -> n = n;
                                                                       sizes.assign(n+1, 1);
34
                                                            14
35
                                                            15
                                                                       for (int i = 0; i <= n; i++)
       ftype f(ftype a, ftype b) {
3.7
                                                            17
                                                                           link[i] = i;
                                                                   }
           return a + b;
                                                            18
38
39
                                                            19
                                                                   int find(int x) {
40
                                                            20
41
       ftype create() {
                                                            21
                                                                       while (x != link[x])
           seg.push_back(0);
                                                                           x = link[x];
42
                                                            22
43
           e.push_back(0);
                                                            23
44
           d.push_back(0);
                                                            24
                                                                       return x;
45
           return seg.size() - 1;
                                                            25
46
                                                                   bool same(int a, int b) {
47
                                                            27
       ftype query(int pos, int ini, int fim, int p, int 28
                                                                       return find(a) == find(b);
        q) {
```

3.0

if (q < ini || p > fim) return NEUTRAL;

49

```
void unite(int a, int b) {
                                                           21 // By using less_equal <T> instead of less <T> on using
3.1
32
          a = find(a);
                                                                  ordered_set declaration
          b = find(b);
                                                           22 // The ordered_set becomes an ordered_multiset
3.3
                                                           _{23} // So the set can contain elements that are equal
34
          if (a == b) return;
                                                          25 #include <ext/pb_ds/assoc_container.hpp>
36
          if (sizes[a] < sizes[b])</pre>
                                                          26 #include <ext/pb_ds/tree_policy.hpp>
               swap(a, b);
3.8
                                                          28 using namespace __gnu_pbds;
39
           sizes[a] += sizes[b];
                                                           29 template <typename T>
          link[b] = a;
                                                           30 using ordered_set = tree<T,null_type,less<T>,
41
      }
                                                                 rb_tree_tag, tree_order_statistics_node_update>;
43
      int size(int x) {
                                                             3.11 Priority Queue
44
45
          return sizes[x];
46
                                                           1 // Description:
47 };
                                                           _{2} // Keeps the largest (by default) element at the top
48
                                                                 of the queue
49 int main() {
      ios::sync_with_stdio(false);
5.0
                                                           4 // Problem:
      cin.tie(NULL);
51
                                                           5 // https://cses.fi/problemset/task/1164/
52
      int cities, roads; cin >> cities >> roads;
5.3
                                                           7 // Complexity:
      vector < int > final_roads;
                                                           8 // O(log n) for push and pop
      int ans = 0;
5.5
                                                           _{9} // _{0} (1) for looking at the element at the top
      DSU dsu = DSU(cities);
56
      for (int i = 0, a, b; i < roads; i++) {</pre>
5.7
                                                           11 // How to use:
          cin >> a >> b;
5.8
                                                           12 // prioriy_queue < int > pq;
           dsu.unite(a, b);
59
                                                           13 // pq.push(1);
60
                                                           14 // pq.top();
61
                                                           15 // pq.pop()
      for (int i = 2; i <= cities; i++) {</pre>
62
          if (!dsu.same(1, i)) {
63
                                                          17 // Notes
               ans++;
                                                           _{\rm 18} // To use the priority queue keeping the smallest
               final_roads.push_back(i);
65
                                                                 element at the top
               dsu.unite(1,i);
          }
67
                                                           20 priority_queue < int , vector < int > , greater < int >> pq;
68
69
                                                                  Template
      cout << ans << '\n';
70
      for (auto e : final_roads) {
           cout << "1 " << e << '\n';
72
                                                             4.1
                                                                    Template
73
74
75 }
                                                           # # include < bits/stdc++.h>
                                                           2 using namespace std;
  3.10 Ordered Set
                                                           4 #define int long long
                                                           5 #define optimize std::ios::sync_with_stdio(false);
                                                                 cin.tie(NULL);
1 // Description:
                                                           6 #define vi vector<int>
2 // insert(k) - add element k to the ordered set
                                                           7 #define 11 long long
3 // erase(k) - remove element k from the ordered set
4 // erase(it) - remove element it points to from the
                                                           8 #define pb push_back
                                                           9 #define mp make_pair
      ordered set
                                                           10 #define ff first
5 // order_of_key(k) - returns number of elements
                                                           11 #define ss second
      strictly smaller than k
6 // find_by_order(n) - return an iterator pointing to 12 #define pii pair<int, int>
      the k-th element in the ordered set (counting
                                                           13 #define MOD 100000007
      from zero).
                                                           14 #define sqr(x) ((x) * (x))
                                                           15 #define all(x) (x).begin(), (x).end()
8 // Problem:
                                                           <sup>16</sup> #define FOR(i, j, n) for (int i = j; i < n; i++)
                                                           17 #define qle(i, n) (i == n ? "\n" : " ")
9 // https://cses.fi/problemset/task/2169/
                                                           18 #define endl "\n"
11 // Complexity:
                                                           19 const int oo = 1e9;
                                                           20 const int MAX = 1e6;
_{12} // O(log n) for all operations
                                                          2.1
```

4.2 Template Clean

22 int32_t main(){ optimize;

return 0;

23

24 25 }

14 // How to use:

19 // Notes

15 // ordered_set < int > os;

16 // cout << os.order_of_key(1) << '\n;</pre>

17 // cout << os.find_by_order(1) << '\n;</pre>

20 // The ordered set only contains different elements

```
1 // Notes:
                                                             7 vector < int > adj [MAX];
2 // Compile and execute
                                                              8 bool visited[MAX];
_3 // g++ teste.cpp -o teste -std=c++17
4 // ./teste < teste.txt
                                                             int max_depth = 0, max_node = 1;
6 // Print with precision
                                                             12 void dfs (int v, int depth) {
7 // cout << fixed << setprecision(12) << value << endl 13
                                                                    visited[v] = true;
                                                                    if (depth > max_depth) {
9 // File as input and output
                                                                         max_depth = depth;
10 // freopen("input.txt", "r", stdin);
11 // freopen("output.txt", "w", stdout);
                                                                         max_node = v;
                                                             17
                                                             18
                                                             19
13 #include <bits/stdc++.h>
                                                             20
                                                                    for (auto u : adj[v]) {
                                                                        if (!visited[u]) dfs(u, depth + 1);
14 using namespace std;
                                                             21
                                                             22
15
16 int main() {
                                                             23 }
      ios::sync_with_stdio(false);
1.7
                                                             24
       cin.tie(NULL);
                                                             25 int tree_diameter() {
                                                                    dfs(1, 0);
1.9
                                                             26
                                                             27
                                                                    max_depth = 0;
20
                                                                    for (int i = 0; i < MAX; i++) visited[i] = false;</pre>
21
                                                             28
       return 0:
                                                             29
                                                                    dfs(max_node, 0);
22
23 }
                                                                    return max_depth;
                                                             30
                                                             31 }
```

Graphs

Floyd Warshall

```
#include <bits/stdc++.h>
3 using namespace std;
4 using ll = long long;
                                                            8
6 const int MAX = 507;
                                                             9
7 const long long INF = 0x3f3f3f3f3f3f3f3f3fLL;
                                                            1.0
                                                            11
9 ll dist[MAX][MAX];
10 int n:
                                                            1.3
12 void floyd_warshall() {
                                                            1.5
       for (int i = 0; i < n; i++) {</pre>
                                                            16
          for (int j = 0; j < n; j++) {
14
               if (i == j) dist[i][j] = 0;
15
                                                            18
                else if (!dist[i][j]) dist[i][j] = INF;
                                                            19
           }
1.7
                                                            20
                                                            21
19
                                                            22 }
      for (int k = 0; k < n; k++) {
20
                                                            23
           for (int i = 0; i < n; i++) {
               for (int j = 0; j < n; j++) {
22
                                                           25
                   // trata o caso no qual o grafo tem
       arestas com peso negativo
                   if (dist[i][k] < INF && dist[k][j] < ^{27}
24
                        {\tt dist[i][j] = min(dist[i][j], dist}^{29}
       [i][k] + dist[k][j]);
26
                   }
                                                            32
               }
27
                                                            33
           }
28
                                                            34
29
       }
                                                            35
30 }
                                                            36
                                                            3.7
                                                            38
```

Tree Diameter

```
#include <bits/stdc++.h>
3 using namespace std;
5 const int MAX = 3e5+17;
```

5.3 Cycle Path Recovery

```
vector < vector < int >> adj;
3 vector < char > color;
4 vector <int> parent;
5 int cycle_start, cycle_end;
7 bool dfs(int v) {
     color[v] = 1;
       for (int u : adj[v]) {
           if (color[u] == 0) {
               parent[u] = v;
               if (dfs(u))
                   return true;
           } else if (color[u] == 1) {
               cycle_end = v;
               cycle_start = u;
               return true;
      color[v] = 2;
       return false;
24 void find_cycle() {
    color.assign(n, 0);
      parent.assign(n, -1);
      cycle_start = -1;
       for (int v = 0; v < n; v++) {
           if (color[v] == 0 && dfs(v))
               break;
       if (cycle_start == -1) {
          cout << "Acyclic" << endl;</pre>
       } else {
           vector < int > cycle;
           cycle.push_back(cycle_start);
           for (int v = cycle_end; v != cycle_start; v =
        parent[v])
               cycle.push_back(v);
           cycle.push_back(cycle_start);
           reverse(cycle.begin(), cycle.end());
           cout << "Cycle found: ";</pre>
```

3.9

40

41

43

44

```
for (int v : cycle)
                                                                  visited.reset();
45
                                                           26
46
              cout << v << " ";
                                                           27
           cout << endl;
                                                                  for (int u = 1; u <= N; ++u){</pre>
47
                                                           28
                                                                      path.clear();
48
      }
                                                           29
                                                                       if (not visited[u] and dfs(u,-1))
49 }
                                                           30
                                                                           return true:
                                                           31
  5.4 Bipartite
                                                           32
                                                           3.3
                                                           34
const int NONE = 0, BLUE = 1, RED = 2;
                                                                  return false;
                                                           35
vector < vector < int >> graph (100005);
                                                           36 }
3 vector < bool > visited(100005);
4 int color [100005];
                                                             5.6 Dinic
6 bool bfs(int s = 1){
                                                           1 const int N = 300;
       queue < int > q;
                                                            3 struct Dinic {
       q.push(s);
9
                                                                  struct Edge {
                                                            4
       color[s] = BLUE;
1.0
                                                                       int from, to; ll flow, cap;
                                                            5
                                                            6
       while (not q.empty()){
                                                                  vector < Edge > edge;
                                                            7
          auto u = q.front(); q.pop();
13
                                                            8
14
                                                                  vector < int > g[N];
           for (auto v : graph[u]){
15
                                                                  int ne = 0;
                                                           10
               if (color[v] == NONE){
                                                                  int lvl[N], vis[N], pass;
                                                           11
                    color[v] = 3 - color[u];
1.7
                                                                  int qu[N], px[N], qt;
                                                           12
18
                    q.push(v);
                                                           13
19
                                                           14
                                                                  ll run(int s, int sink, ll minE) {
               else if (color[v] == color[u]){
20
                                                                       if(s == sink) return minE;
                                                           15
                   return false;
                                                           16
22
                                                           1.7
                                                                       11 \text{ ans} = 0:
           }
                                                           18
       }
24
                                                                       for(; px[s] < (int)g[s].size(); px[s]++) {</pre>
                                                           19
2.5
                                                           20
                                                                           int e = g[s][ px[s] ];
       return true;
                                                                           auto &v = edge[e], &rev = edge[e^1];
                                                           21
27 }
                                                                           if(lvl[v.to] != lvl[s]+1 || v.flow >= v.
                                                           22
                                                                   cap)
29 bool is_bipartite(int n){
                                                                                                    // v.cap - v.flow
                                                                                continue:
                                                                    < lim
      for (int i = 1; i<=n; i++)
                                                                           11 tmp = run(v.to, sink,min(minE, v.cap-v
           if (color[i] == NONE and not bfs(i))
32
                                                                   .flow));
33
               return false;
                                                                           v.flow += tmp, rev.flow -= tmp;
3.4
                                                                           ans += tmp, minE -= tmp;
                                                           26
      return true;
                                                                           if(minE == 0) break;
                                                           27
36
                                                                       }
                                                           28
                                                                       return ans;
                                                           29
  5.5 Find Cycle
                                                           30
                                                                   bool bfs(int source, int sink) {
                                                           3.1
1 bitset < MAX > visited;
                                                           32
                                                                       qt = 0;
vector < int > path;
                                                                       qu[qt++] = source;
                                                           3.3
s vector < int > adj[MAX];
                                                           34
                                                                       lvl[source] = 1;
                                                           35
                                                                       vis[source] = ++pass;
                                                                       for(int i = 0; i < qt; i++) {</pre>
5 bool dfs(int u, int p){
                                                           36
                                                                           int u = qu[i];
                                                           37
                                                                           px[u] = 0;
      if (visited[u]) return false;
                                                           3.8
                                                                           if(u == sink) return true;
                                                           3.9
       path.pb(u);
                                                           40
                                                                           for(auto& ed : g[u]) {
9
       visited[u] = true;
                                                                               auto v = edge[ed];
10
                                                           41
                                                                               if(v.flow >= v.cap || vis[v.to] ==
                                                                  pass)
12
      for (auto v : adj[u]){
           if (visited[v] and u != v and p != v){
13
                                                           43
                                                                                    continue; // v.cap - v.flow < lim</pre>
               path.pb(v); return true;
                                                                               vis[v.to] = pass;
14
                                                           44
                                                                               lvl[v.to] = lvl[u]+1;
1.5
                                                           45
16
                                                           46
                                                                               qu[qt++] = v.to;
           if (dfs(v, u)) return true;
1.7
                                                           47
                                                                       }
                                                            48
19
                                                           49
                                                                       return false;
      path.pop_back();
20
                                                           50
21
       return false;
                                                           51
                                                                  11 flow(int source, int sink) {
22 }
                                                           52
                                                                      reset_flow();
                                                                       11 \text{ ans} = 0;
                                                            53
24 bool has_cycle(int N){
                                                                       //for(lim = (1LL << 62); lim >= 1; lim /= 2)
                                                           5.4
                                                            5.5
                                                                       while(bfs(source, sink))
```

```
ans += run(source, sink, LLINF);
                                                                               q.insert({d[to], to});
56
                                                           2.5
57
          return ans;
                                                           26
                                                                           }
                                                                      }
5.8
                                                           2.7
      void addEdge(int u, int v, ll c, ll rc) {
59
                                                           28
          Edge e = {u, v, 0, c};
                                                           29 }
           edge pb(e);
61
                                                           30
           g[u].push_back(ne++);
                                                           31 vector<int> restore_path(int s, int t) {
                                                                  vector < int > path;
63
                                                           3.2
           e = \{v, u, 0, rc\};
64
                                                           33
           edge.pb(e);
                                                           34
                                                                  for (int v = t; v != s; v = p[v])
           g[v].push_back(ne++);
                                                                      path.push_back(v);
66
                                                           35
                                                           36
                                                                  path.push_back(s);
68
      void reset_flow() {
                                                           3.7
          for(int i = 0; i < ne; i++)
                                                           38
                                                                  reverse(path.begin(), path.end());
69
               edge[i].flow = 0;
7.0
                                                           39
                                                                  return path;
           memset(lvl, 0, sizeof(lvl));
                                                           40 }
71
           memset(vis, 0, sizeof(vis));
           memset(qu, 0, sizeof(qu));
                                                           42 int adj[MAX][MAX];
7.3
           memset(px, 0, sizeof(px));
                                                           43 int dist[MAX]:
                                                           44 int minDistance(int dist[], bool sptSet[], int V) {
           qt = 0; pass = 0;
7.5
76
                                                                  int min = INT_MAX, min_index;
                                                           45
77 };
                                                           46
                                                           47
                                                                  for (int v = 0; v < V; v++)
  5.7 Bellman Ford
                                                                       if (sptSet[v] == false && dist[v] <= min)</pre>
                                                           48
                                                                           min = dist[v], min_index = v;
                                                           49
                                                           5.0
1 struct edge
                                                           51
                                                                  return min_index;
                                                           52 }
      int a, b, cost;
3
                                                           53
                                                           54 void dijkstra(int src, int V) {
6 int n, m, v;
                                                                  bool sptSet[V];
                                                           5.6
7 vector < edge > e;
                                                           5.7
                                                                  for (int i = 0; i < V; i++)</pre>
8 const int INF = 1000000000;
                                                           58
                                                                       dist[i] = INT_MAX, sptSet[i] = false;
10 void solve()
                                                                  dist[src] = 0;
11
                                                           6.1
      vector < int > d (n, INF);
12
                                                           62
                                                                  for (int count = 0; count < V - 1; count++) {</pre>
      d[v] = 0;
13
                                                           63
                                                                      int u = minDistance(dist, sptSet, V);
      for (int i=0; i<n-1; ++i)
                                                           64
           for (int j=0; j < m; ++j)
1.5
                                                                       sptSet[u] = true;
               if (d[e[j].a] < INF)</pre>
                   d[e[j].b] = min (d[e[j].b], d[e[j].a]_{67}
1.7
        + e[j].cost);
                                                           68
                                                                       for (int v = 0; v < V; v++)
18 }
                                                                           if (!sptSet[v] && adj[u][v]
                                                           69
                                                           7.0
                                                                               && dist[u] ! = INT_MAX
  5.8 Dijkstra
                                                                               && dist[u] + adj[u][v] < dist[v])
                                                                               dist[v] = dist[u] + adj[u][v];
                                                                  }
1 const int MAX = 2e5+7;
                                                           7.3
2 const int INF = 1000000000;
3 vector < vector < pair < int , int >>> adj(MAX);
                                                                   Tarjan Bridge
                                                              5.9
5 void dijkstra(int s, vector<int> & d, vector<int> & p
      ) {
                                                            1 // Description:
      int n = adj.size();
                                                            _{2} // Find a bridge in a connected unidirected graph
                                                            3 // A bridge is an edge so that if you remove that
7
      d.assign(n, INF);
      p.assign(n, -1);
                                                                  edge the graph is no longer connected
      d[s] = 0;
                                                            5 // Problem:
                                                            6 // https://cses.fi/problemset/task/2177/
      set <pair < int , int >> q;
      q.insert({0, s});
12
                                                            8 // Complexity:
13
      while (!q.empty()) {
          int v = q.begin()->second;
                                                           _{9} // O(V + E) where V is the number of vertices and E
14
           q.erase(q.begin());
                                                                  is the number of edges
16
                                                           10
           for (auto edge : adj[v]) {
                                                           11 int n;
               int to = edge.first;
                                                           12 vector < vector < int >> adj;
18
               int len = edge.second;
                                                           13
19
                                                           14 vector < bool > visited;
               if (d[v] + len < d[to]) {</pre>
                                                           15 vector < int > tin , low;
21
                   q.erase({d[to], to});
                                                           16 int timer;
                   d[to] = d[v] + len;
23
                   p[to] = v;
                                                           18 void dfs(int v, int p) {
24
```

```
visited[v] = true;
                                                                       u --; v--;
19
                                                           43
20
       tin[v] = low[v] = timer++;
                                                           44
                                                                       adj[u].push_back(v);
      for (int to : adj[v]) {
                                                                       adj[v].push_back(u);
                                                           45
          if (to == p) continue;
22
                                                           46
           if (visited[to]) {
                                                           47
               low[v] = min(low[v], tin[to]);
                                                                  get_subtree_size(0);
24
                                                           48
                                                                  cout << get_centroid(0) + 1 << endl;</pre>
                                                           49
               dfs(to, v);
                                                           50 }
26
               low[v] = min(low[v], low[to]);
27
                                                              5.11 Small To Large
               if (low[to] > tin[v]) {
                   IS_BRIDGE(v, to);
29
30
                                                            1 // Problem:
           }
3.1
                                                            2 // https://codeforces.com/contest/600/problem/E
32
33 }
                                                            4 void process_colors(int curr, int parent) {
34
35 void find_bridges() {
                                                                  for (int n : adj[curr]) {
      timer = 0:
3.6
                                                                       if (n != parent) {
      visited.assign(n, false);
                                                                           process_colors(n, curr);
      tin.assign(n, -1);
38
                                                            9
      low.assign(n, -1);
                                                                           if (colors[curr].size() < colors[n].size</pre>
39
                                                           10
      for (int i = 0; i < n; ++i) {</pre>
                                                                  ()) {
40
          if (!visited[i])
41
                                                                                sum_num[curr] = sum_num[n];
               dfs(i, -1);
                                                                               vmax[curr] = vmax[n];
                                                           12
43
                                                                               swap(colors[curr], colors[n]);
                                                           13
44 }
                                                           1.4
                                                           15
  5.10 Centroid Find
                                                                           for (auto [item, vzs] : colors[n]) {
                                                            16
                                                                               if(colors[curr][item]+vzs > vmax[curr
                                                           17
1 // Description:
                                                                  ]){
2 // Indexed at zero
                                                                                    vmax[curr] = colors[curr][item] +
_{3} // Find a centroid, that is a node such that when it
                                                                    vzs:
      is appointed the root of the tree,
                                                                                    sum_num[curr] = item;
_4 // each subtree has at most floor(n/2) nodes.
                                                           2.0
                                                                               else if(colors[curr][item]+vzs ==
6 // Problem:
                                                                  vmax[curr]){
7 // https://cses.fi/problemset/task/2079/
                                                                                    sum_num[curr] += item;
                                                           23
9 // Complexity:
                                                           24
                                                                               colors[curr][item] += vzs;
10 // O(n)
                                                           25
                                                                           }
                                                           26
12 // How to use:
                                                                       }
                                                           27
13 // get_subtree_size(0);
                                                           28
14 // cout << get_centroid(0) + 1 << endl;</pre>
                                                           29
                                                           30 }
16 int n;
                                                           31
17 vector < int > adj [MAX];
                                                           32
18 int subtree_size[MAX];
                                                           33 int32_t main() {
                                                           3.4
20 int get_subtree_size(int node, int par = -1) {
                                                                  int n; cin >> n;
                                                           3.5
      int &res = subtree_size[node];
                                                           36
21
      res = 1;
                                                                   for (int i = 1; i <= n; i++) {
                                                           37
      for (int i : adj[node]) {
                                                                      int a; cin >> a;
23
                                                           38
           if (i == par) continue;
                                                                       colors[i][a] = 1;
                                                           39
           res += get_subtree_size(i, node);
                                                                       vmax[i] = 1;
2.5
                                                           40
26
                                                           41
                                                                       sum_num[i] = a;
27
                                                           42
                                                                  }
      return res;
28 }
                                                           43
                                                                  for (int i = 1; i < n; i++) {
30 int get_centroid(int node, int par = -1) {
                                                                       int a, b; cin >> a >> b;
                                                           45
      for (int i : adj[node]) {
31
                                                           46
32
          if (i == par) continue;
                                                           47
                                                                       adj[a].push_back(b);
                                                                       adj[b].push_back(a);
3.3
                                                           48
           if (subtree_size[i] * 2 > n) { return
34
                                                           49
       get_centroid(i, node); }
                                                           5.0
                                                                  process_colors(1, 0);
                                                           51
36
      return node;
                                                           52
37 }
                                                                  for (int i = 1; i <= n; i++) {</pre>
                                                           53
                                                                       cout << sum_num[i] << (i < n ? " " : "\n");
                                                           54
39 int main() {
                                                           5.5
      cin >> n;
                                                           56
      for (int i = 0; i < n - 1; i++) {</pre>
                                                                  return 0;
41
                                                           5.7
          int u, v; cin >> u >> v;
                                                           5.8
42
```

```
59 }
                                                            24 }
                                                            26 struct Edge {
  5.12 Prim
                                                            27
                                                               int u, v, weight;
                                                                   bool operator < (Edge const& other) {</pre>
                                                                       return weight < other.weight;</pre>
                                                            29
1 int n:
vector < vector < int>> adj; // adjacency matrix of graph 31 };
_3 const int INF = 1000000000; // weight INF means there _{32}^{\circ}
       is no edge
                                                            84 vector < Edge > edges;
5 struct Edge {
      int w = INF, to = -1;
                                                           36 int cost = 0;
7 };
                                                            37 vector < Edge > result;
                                                            38 parent.resize(n);
9 void prim() {
                                                            39 rank.resize(n);
      int total_weight = 0;
10
                                                            40 for (int i = 0; i < n; i++)
       vector < bool > selected(n, false);
                                                                   make_set(i);
                                                           41
      vector < Edge > min_e(n);
12
      min_e[0].w = 0;
13
                                                            43 sort(edges.begin(), edges.end());
14
                                                            44
      for (int i=0; i<n; ++i) {</pre>
15
                                                            45 for (Edge e : edges) {
           int v = -1;
16
                                                                if (find_set(e.u) != find_set(e.v)) {
                                                            46
           for (int j = 0; j < n; ++j) {
                                                                       cost += e.weight;
              if (!selected[j] && (v == -1 || min_e[j].
                                                                       result.push_back(e);
      w < min_e[v].w))
                                                                       union_sets(e.u, e.v);
                                                            49
19
                  v = j;
                                                            50
20
                                                            51 }
21
           if (min_e[v].w == INF) {
                                                              5.14 Lca
               cout << "No MST!" << endl;</pre>
               exit(0);
                                                            1 // Description:
           }
25
                                                             _{2} // Find the lowest common ancestor between two nodes
26
                                                                   in a tree
           selected[v] = true;
           total_weight += min_e[v].w;
28
                                                             4 // Problem:
           if (min_e[v].to != -1)
                                                            5 // https://cses.fi/problemset/task/1688/
               cout << v << " " << min_e[v].to << endl;
3.0
31
                                                            7 // Complexity:
           for (int to = 0; to < n; ++to) {
                                                            8 // O(log n)
               if (adj[v][to] < min_e[to].w)</pre>
33
                    min_e[to] = {adj[v][to], v};
                                                            10 // How to use:
3.5
                                                            11 // preprocess(1);
                                                            12 // lca(a, b);
3.7
       cout << total_weight << endl;</pre>
38
                                                            14 // Notes
39 }
                                                            _{15} // To calculate the distance between two nodes use
                                                                  the following formula
  5.13 Kruskall
                                                            16 // dist[a] + dist[b] - 2*dist[lca(a, b)]
                                                            17
vector < int > parent, rank;
                                                            18 const int MAX = 2e5+17;
3 void make_set(int v) {
                                                            20 const int BITS = 32;
      parent[v] = v;
                                                            21
      rank[v] = 0;
                                                            22 vector < int > adj [MAX];
6 }
                                                            23 // vector<pair<int, int>> adj[MAX];
                                                            24 // int dist[MAX];
8 int find_set(int v) {
      if (v == parent[v])
                                                           26 int timer;
                                                           27 vector < int > tin, tout;
1.0
          return v;
      return parent[v] = find_set(parent[v]);
                                                            28 vector < vector < int >> up;
11
12 }
                                                           30 void dfs(int v, int p)
14 void union_sets(int a, int b) {
                                                           31 {
      a = find_set(a);
                                                                   tin[v] = ++timer;
1.5
                                                           3.2
      b = find_set(b);
                                                                   up[v][0] = p;
16
                                                            33
      if (a != b) {
17
                                                           34
          if (rank[a] < rank[b])</pre>
                                                                   for (int i = 1; i <= BITS; ++i) {</pre>
18
                                                           35
               swap(a, b);
                                                            36
                                                                       up[v][i] = up[up[v][i-1]][i-1];
           parent[b] = a;
20
                                                            3.7
           if (rank[a] == rank[b])
                                                            38
               rank[a]++;
                                                                   for (auto u : adj[v]) {
22
                                                            3.9
      }
                                                                       if (u != p) {
23
                                                            40
```

```
dfs(u, v);
4.1
                                                           3.2
          }
42
                                                           ss char get_next(char c) {
      }
                                                                if (c != 'Z') return c + 1;
43
                                                           34
                                                                  return '$';
                                                           35
44
      /*for (auto [u, peso] : adj[v]) {
                                                           36 }
         if (u != p) {
46
                                                           37
               dist[u] = dist[v] + peso;
                                                           38 bool flag = true;
               dfs(u, v);
48
                                                           3.9
                                                           40 void solve(int node, char c) {
49
      } * /
                                                           41
                                                                 int center = get_centroid(node, dfs(node));
50
                                                                  ans[center] = c;
51
                                                           42
52
      tout[v] = ++timer;
                                                           43
                                                                  removed[center] = true;
53 }
                                                           44
                                                                  for (auto u : adj[center]) {
                                                           45
55 bool is_ancestor(int u, int v)
                                                                      if (!removed[u]) {
                                                           46
                                                                           char next = get_next(c);
if (next == '$') {
56 €
                                                           47
      return tin[u] <= tin[v] && tout[u] >= tout[v];
57
58 }
                                                                               flag = false;
                                                           49
                                                                               return;
60 int lca(int u, int v)
                                                           5.1
61 {
                                                           52
                                                                           solve(u, next);
      if (is_ancestor(u, v))
                                                                      }
                                                           53
62
          return u;
                                                           5.4
6.3
      if (is_ancestor(v, u))
                                                           55 }
          return v;
6.5
                                                           56
66
      for (int i = BITS; i >= 0; --i) {
                                                           57 int32_t main(){
          if (!is_ancestor(up[u][i], v))
                                                                  ios::sync_with_stdio(false);
6.7
                                                           58
               u = up[u][i];
                                                           59
                                                                  cin.tie(NULL);
68
                                                           60
69
                                                                  cin >> n;
7.0
      return up[u][0];
                                                           6.1
71 }
                                                                  adj.resize(n + 1);
                                                           62
                                                                  ans.resize(n + 1);
                                                           63
73 void preprocess(int root) {
                                                           64
                                                                  removed.resize(n + 1);
      tin.resize(MAX);
                                                           65
                                                                  subtree_size.resize(n + 1);
      tout.resize(MAX);
7.5
                                                           66
      timer = 0;
                                                                  for (int i = 1; i <= n - 1; i++) {
76
                                                           67
      up.assign(MAX, vector<int>(BITS + 1));
                                                                      int u, v; cin >> u >> v;
7.7
                                                           68
                                                                       adj[u].insert(v);
78
      dfs(root, root);
                                                           69
79 }
                                                           70
                                                                       adj[v].insert(u);
                                                           7.1
  5.15 Centroid Decomposition
                                                           72
                                                                  solve(1, 'A');
                                                           73
                                                           74
                                                           7.5
                                                                  if (!flag) cout << "Impossible!\n";</pre>
vector < set < int >> adj;
                                                           76
                                                                  else {
3 vector < char > ans:
                                                           7.7
                                                                      for (int i = 1; i <= n; i++) {
                                                                           cout << ans[i] << ' ';
                                                           7.8
5 vector < bool > removed;
                                                           79
                                                                       cout << '\n';</pre>
7 vector < int > subtree_size;
                                                           8.0
                                                           81
9 int dfs(int u, int p = 0) {
                                                           82
                                                                  return 0;
      subtree_size[u] = 1;
                                                           83
                                                           84 }
11
      for(int v : adj[u]) {
          if(v != p && !removed[v]) {
                                                                   Strings
1.3
14
               subtree_size[u] += dfs(v, u);
           }
15
                                                              6.1 Kmp
16
18
      return subtree_size[u];
                                                            vector <int> prefix_function(string s) {
19 }
                                                                int n = (int)s.length();
                                                            2
                                                                  vector < int > pi(n);
20
                                                            3
21 int get_centroid(int u, int sz, int p = 0) {
                                                                  for (int i = 1; i < n; i++) {
      for(int v : adj[u]) {
                                                                      int j = pi[i-1];
          if(v != p && !removed[v]) {
                                                                      while (j > 0 && s[i] != s[j])
23
               if(subtree_size[v]*2 > sz) {
                                                                          j = pi[j-1];
                   return get_centroid(v, sz, u);
25
                                                                       if (s[i] == s[j])
               }
                                                                           j++;
           }
27
                                                                      pi[i] = j;
                                                           10
      }
                                                                  }
28
                                                           11
29
                                                                  return pi;
                                                           12
30
      return u;
                                                           13 }
```

31 }

sequence, int n, int k) { $if (k == 0){$ 1 // Description: return { sequence }; $_{2}$ // Finds the longest common subsquence between two string vector<string> ans; 4 // Problem: for (int i = 0; i < n; i++) {</pre> g 5 // https://codeforces.com/gym/103134/problem/B auto aux = generate_sequences(set, sequence + set[i], n, k - 1); 7 // Complexity: ans.insert(ans.end(), aux.begin(), aux.end()) $_{8}$ // O(mn) where m and n are the length of the strings // for (auto e : aux) ans.push_back(e); string lcsAlgo(string s1, string s2, int m, int n) { int LCS_table[m + 1][n + 1]; 12 return ans; 15 for (int i = 0; i <= m; i++) { 13 16 } for (int j = 0; j <= n; j++) { 14 if (i == 0 || j == 0) 15 6.5 Z-function 16 $LCS_table[i][j] = 0;$ else if (s1[i - 1] == s2[j - 1])17 $LCS_table[i][j] = LCS_table[i - 1][j - 1] +$ vector < int > z_function(string s) { int n = (int) s.length(); vector < int > z(n); for (int i = 1, l = 0, r = 0; i < n; ++i) { LCS_table[i][j] = max(LCS_table[i - 1][j], LCS_table[i][j - 1]); **if** (i <= r) z[i] = min (r - i + 1, z[i - 1]);21 while (i + z[i] < n && s[z[i]] == s[i + z[i]]} 22 11) 23 ++z[i]; int index = LCS_table[m][n]; 24 if (i + z[i] - 1 > r)25 char lcsAlgo[index + 1]; 9 1 = i, r = i + z[i] - 1;lcsAlgo[index] = '\0'; 1.0 } 11 int i = m, j = n; 12 return z: 13 } while (i > 0 && j > 0) { 29 if (s1[i - 1] == s2[j - 1]) { 30 31 lcsAlgo[index - 1] = s1[i - 1]; DPi - - ; 32 j --; 7.1Knapsack 34 index --; 3.5 36 int val[MAXN], peso[MAXN], dp[MAXN][MAXS]; else if (LCS_table[i - 1][j] > LCS_table[i][j -37 1]) 3 int knapsack(int n, int m){ // n Objetos | Peso max i - -: 38 for(int i=0;i<=n;i++){</pre> 39 else for(int j=0;j<=m;j++){</pre> 40 j --; if(i==0 or j==0) 41 dp[i][j] = 0;else if(peso[i-1]<=j)</pre> return lcsAlgo; 43 dp[i][j] = max(val[i-1]+dp[i-1][j-1]44 } peso[i-1]], dp[i-1][j]); 10 Generate All Permutations 11 dp[i][j] = dp[i-1][j]; } 12 vector < string > generate_permutations(string s) { 14 return dp[n][m]; int n = s.size(); 15 } vector < string > ans; 7.2 Substr Palindrome sort(s.begin(), s.end()); 1 // êvoc deve informar se a substring de S formada do { pelos elementos entre os indices i e j ans.push_back(s); 2 // é um palindromo ou ãno. } while (next_permutation(s.begin(), s.end())); 1.0 4 char s[MAX]; return ans; 5 int calculado[MAX][MAX]; // inciado com false, ou 0 12 } 6 int tabela[MAX][MAX]; 6.4 Generate All Sequences Length K 8 int is_palin(int i, int j){ if(calculado[i][j]){ 1 // gera todas as ípossveis êsequncias usando as letras10 return tabela[i][j]; em set (de comprimento n) e que tenham tamanho k ${\scriptstyle 11}$ $_2$ // sequence = "" if(i == j) return true;

3 vector<string> generate_sequences(char set[], string

6.2 Lcs

```
if(i + 1 == j) return s[i] == s[j];
                                                                             K[i][w] = K[i - 1][w];
1.3
                                                         1.3
14
                                                         14
                                                                    }
      int ans = false:
1.5
                                                         15
      if(s[i] == s[j]){
                                                         16
16
          if(is_palin(i+1, j-1)){
                                                         17
                                                                int res = K[n][W];
              ans = true;
                                                                cout << res << endl:
18
                                                         18
19
                                                         19
                                                                w = W:
2.0
                                                         2.0
      calculado[i][j] = true;
                                                                for (i = n; i > 0 \&\& res > 0; i--) {
                                                         21
21
                                                                    if (res == K[i - 1][w])
      tabela[i][j] = ans;
                                                         22
22
      return ans;
                                                                        continue;
                                                         23
23
24 }
                                                         24
                                                                    else {
                                                                       cout < < " " < < wt[i - 1] ;
                                                         2.5
  7.3 Edit Distance
                                                                        res = res - val[i - 1];
                                                         26
                                                                        w = w - wt[i - 1];
                                                         27
                                                         28
1 // Description:
^{\prime\prime}_{2} // Minimum number of operations required to transform ^{\circ\circ}_{30} }
      a string into another
3 // Operations allowed: add character, remove
                                                         32 int main()
      character, replace character
                                                         33 {
                                                                int val[] = { 60, 100, 120 };
                                                         34
5 // Parameters:
                                                                int wt[] = { 10, 20, 30 };
                                                         3.5
6 // str1 - string to be transformed into str2
                                                                int W = 50;
7 // str2 - string that str1 will be transformed into
                                                                int n = sizeof(val) / sizeof(val[0]);
                                                         3.7
\rm s // m - size of str1
9 // n - size of str2
                                                                knapsack(W, wt, val, n);
                                                         39
                                                         40
11 // Problem:
                                                         41
                                                                return 0:
12 // https://cses.fi/problemset/task/1639
                                                         42 }
14 // Complexity:
                                                            7.5 Minimum Coin Change
15 // O(m x n)
17 // How to use:
                                                         1 int n;
18 // memset(dp, -1, sizeof(dp));
                                                          vector<int> valores;
19 // string a, b;
20 // edit_distance(a, b, (int)a.size(), (int)b.size()); 4 int tabela[1005];
22 // Notes:
                                                          6 int dp(int k){
23 // Size of dp matriz is m x n
                                                                if(k == 0){
                                                                    return 0;
25 int dp[MAX][MAX];
                                                               if(tabela[k] != -1)
27 int edit_distance(string &str1, string &str2, int m, 11
                                                                   return tabela[k];
      int n) {
                                                                int melhor = 1e9;
                                                          12
      if (m == 0) return n;
                                                                for(int i = 0; i < n; i++){
                                                          13
      if (n == 0) return m;
                                                                  if(valores[i] <= k)</pre>
29
                                                         14
                                                                         melhor = min(melhor,1 + dp(k - valores[i
      if (dp[m][n] != -1) return dp[m][n];
                                                                1)):
31
                                                         16
      if (str1[m - 1] == str2[n - 1]) return dp[m][n] = 17
                                                                return tabela[k] = melhor;
33
      edit_distance(str1, str2, m - 1, n - 1);
                                                         18 }
      return dp[m][n] = 1 + min({edit_distance(str1,
      str2, m, n - 1), edit_distance(str1, str2, m - 1, 7.6 Digits
       n), edit_distance(str1, str2, m - 1, n - 1)});
35
                                                          1 // achar a quantidade de numeros menores que R que
                                                               possuem no maximo 3 digitos nao nulos
  7.4 Knapsack With Index
                                                          _{2} // a ideia eh utilizar da ordem lexicografica para
                                                               checar isso pois se temos por exemplo
1 void knapsack(int W, int wt[], int val[], int n) { 3 // o numero 8500, a gente sabe que se pegarmos o
                                                               numero 7... qualquer digito depois do 7
      int i, w;
      int K[n + 1][W + 1];
                                                          4 // sera necessariamente menor q 8500
      for (i = 0; i <= n; i++) {
                                                          6 string r;
          for (w = 0; w \le W; w++) {
                                                          7 int tab[20][2][5];
               if (i == 0 || w == 0)
                  K[i][w] = 0;
                                                          9 // i - digito de R
               else if (wt[i - 1] <= w)
                                                         10 // menor - ja pegou um numero menor que um digito de
                  K[i][w] = max(val[i - 1] +
1.0
                       K[i - 1][w - wt[i - 1]], K[i -
                                                         _{11} // qt - quantidade de digitos nao nulos
                                                         12 int dp(int i, bool menor, int qt){
      1][w]):
                                                               if(qt > 3) return 0;
               else
```

```
if(i >= r.size()) return 1;
1.4
15
      if(tab[i][menor][qt] != -1) return tab[i][menor][26
                                                                return tab[i][mult] = res;
      qt];
                                                         28 }
      int dr = r[i] - '0';
      int res = 0;
                                                         30 int main() {
18
      for(int d = 0; d <= 9; d++) {
                                                                memset(tab, -1, sizeof(tab));
20
                                                         32
          int dnn = qt + (d > 0);
21
                                                         33
          if(menor == true) {
                                                        34
                                                                int ans = -oo;
              res += dp(i+1, true, dnn);
                                                                for (int i = 0; i < n; i++) {
23
                                                         35
                                                         36
                                                                    ans = max(ans, dp(i, 0));
25
          else if(d < dr) {</pre>
                                                         3.7
              res += dp(i+1, true, dnn);
                                                         38
          }
                                                         39
                                                                return 0;
          else if(d == dr) {
                                                         40 }
28
              res += dp(i+1, false, dnn);
3.0
                                                         44 int ans = a[0], ans_1 = 0, ans_r = 0;
3.2
      return tab[i][menor][qt] = res;
                                                         45 int sum = 0, minus_pos = -1;
33
34 }
                                                         47 for (int r = 0; r < n; ++r) {
 7.7 Coins
                                                                sum += a[r];
                                                         48
                                                                if (sum > ans) {
                                                         49
                                                                    ans = sum;
                                                         5.0
int tb[1005];
                                                                    ans_l = minus_pos + 1;
                                                         51
2 int n;
                                                         52
                                                                    ans_r = r;
3 vector < int > moedas;
                                                                }
                                                         53
                                                                if (sum < 0) {
                                                         5.4
5 int dp(int i){
                                                                    sum = 0;
      if(i >= n)
                                                         5.6
                                                                    minus_pos = r;
         return 0;
                                                         5.7
      if(tb[i] != -1)
                                                         58 }
         return tb[i];
10
                                                                Math
                                                          8
      tb[i] = max(dp(i+1), dp(i+2) + moedas[i]);
11
12
      return tb[i];
13 }
                                                                  Multiplicative Inverse
                                                            8.1
15 int main() {
                                                          1 ll extend_euclid(ll a, ll b, ll &x, ll &y) {
      memset(tb,-1,sizeof(tb));
17 }
                                                               if (a == 0)
                                                                {
  7.8 Kadane
                                                                    x = 0; y = 1;
                                                                    return b:
_{1} // achar uma subsequencia continua no array que a
                                                               ll x1, y1;
      soma seja a maior possivel
                                                               ll d = extend_euclid(b%a, a, x1, y1);
2 // nesse caso vc precisa multiplicar exatamente 1
                                                               x = y1 - (b / a) * x1;
                                                          Q
      elemento da subsequencia
                                                                v = x1;
                                                         10
3 // e achar a maior soma com isso
                                                                return d;
                                                         11
                                                         12 }
5 int n, x, arr[MAX], tab[MAX][2]; // tab[maior
      resposta no intervalo][foi multiplicado ou ano]
                                                         _{14} // gcd(a, m) = 1 para existir solucao
                                                         15 // ax + my = 1, ou a*x = 1 (mod m)
7 int dp(int i, bool mult) {
                                                         16 ll inv_gcd(ll a, ll m) { // com gcd
      if (i == n-1) {
                                                              11 x, y;
                                                         17
          if (!mult) return arr[n-1]*x;
9
                                                                extend_euclid(a, m, x, y);
          return arr[n-1];
                                                               return (((x % m) +m) %m);
                                                         19
                                                         20 }
      if (tab[i][mult] != -1) return tab[i][mult];
12
                                                         21
13
                                                         22 ll inv(ll a, ll phim) { // com phi(m), se m for primo
      int res;
14
                                                                entao phi(m) = p-1
                                                                ll e = phim - 1;
                                                         23
      if (mult) {
16
                                                                return fexp(a, e, MOD);
          res = max(arr[i], arr[i] + dp(i+1, 1));
17
                                                         25
18
19
      else {
                                                           8.2 Divisors
          res = max({
```

vector < long long > all_divisors(long long n) {

for(long long a = 1; a*a <= n; a++) {</pre>

vector < long long > ans;

arr[i]*x,

arr[i]*x + dp(i+1, 1),

arr[i] + dp(i+1, 0)

2.1

23

24

```
4    if(n % a == 0) {
5        long long b = n / a;
6        ans.push_back(a);
7        if(a != b) ans.push_back(b);
8    }
9    }
10    sort(ans.begin(), ans.end());
11    return ans;
12 }
```

8.3 Prime Factors

8.4 Binary To Decimal

```
int binary_to_decimal(long long n) {
    int dec = 0, i = 0, rem;
    while (n!=0) {
      rem = n % 10;
      n /= 10;
      dec += rem * pow(2, i);
      ++i:
9
10
11
    return dec;
12 }
13
14 long long decimal_to_binary(int n) {
   long long bin = 0;
    int rem, i = 1;
17
    while (n!=0) {
18
     rem = n % 2;
19
      n /= 2;
20
     bin += rem * i;
      i *= 10;
22
23
24
    return bin;
25
```

8.5 Sieve Of Eratosthenes

8.6 Check If Bit Is On

```
1 // msb de 0 é undefined
2 #define msb(n) (32 - __builtin_clz(n))
3 // #define msb(n) (64 - __builtin_clzll(n) )
4 // popcount
5 // turn bit off
6
7 bool bit_on(int n, int bit) {
8     if(1 & (n >> bit)) return true;
9     else return false;
10 }
```

8.7 Crt.

```
1 ll crt(const vector<pair<ll, ll>> &vet){
      ll ans = 0, lcm = 1;
      ll a, b, g, x, y;
      for(const auto &p : vet) {
          tie(a, b) = p;
6
          tie(g, x, y) = gcd(lcm, b);
          if((a - ans) % g != 0) return -1; // no
      solution
          ans = ans + x * ((a - ans) / g) % (b / g) *
          lcm = lcm * (b / g);
9
10
          ans = (ans % lcm + lcm) % lcm;
11
12
      return ans;
13 }
```

8.8 Ceil

```
1 long long division_ceil(long long a, long long b) {
2    return 1 + ((a - 1) / b); // if a != 0
3 }
```

8.9 Matrix Exponentiation

```
1 // Description:
2 // Calculate the nth term of a linear recursion
4 // Example Fibonacci:
5 // Given a linear recurrence, for example fibonacci
6 // F(n) = n, x <= 1
7 // F(n) = F(n - 1) + F(n - 2), x > 1
9 // The recurrence has two terms, so we can build a
      matrix 2 x 1 so that
_{10} // n + 1 = transition * n
_{12} // (2 x 1) = (2 x 2) * (2 x 1)
_{13} // F(n) = a b * F(n - 1)

_{14} // F(n - 1) c d F(n - 2)
16 // Another Example:
_{
m 17} // Given a grid 3 x n, you want to color it using 3
      distinct colors so that
_{18} // no adjacent place has the same color. In how many
      different ways can you do that?
_{\rm 19} // There are 6 ways for the first column to be
      colored using 3 distinct colors
20 // ans 6 ways using 2 equal colors and 1 distinct one
22 // Adding another column, there are:
_{23} // 3 ways to go from 2 equal to 2 equal
_{24} // 2 ways to go from 2 equal to 3 distinct
_{25} // 2 ways to go from 3 distinct to 2 equal
_{26} // _{2} ways to go from 3 distinct to 3 distinct
28 // So we star with matrix 6 6 and multiply it by the
      transition 3 2 and get 18 12
                             6 6
                  2 2
                              12 12
```

```
30 // the we can exponentiate this matrix to find the
                                                          96
      nth column
                                                          97 Matriz fexp(Matriz base, ll exponent){
                                                                 Matriz result = Matriz(base.rows, base.rows, 1);
                                                          9.8
32 // Problem:
                                                                 while(exponent > 0){
                                                          99
33 // https://cses.fi/problemset/task/1722/
                                                                     if(exponent & 1LL) result = result * base;
                                                                     base = base * base;
34
35 // Complexity:
                                                                      exponent = exponent >> 1;
36 // O(log n)
                                                          103
                                                          104
                                                                 return result;
38 // How to use:
                                                          105 }
39 // vector<vector<ll>> v = {{1, 1}, {1, 0}};
                                                             8.10 Linear Diophantine Equation
40 // Matriz transition = Matriz(v);
41 // cout << fexp(transition, n)[0][1] << '\n';
                                                           1 // int a, b, c, x1, x2, y1, y2; cin >> a >> b >> c >>
43 using ll = long long;
                                                                  x1 >> x2 >> y1 >> y2;
                                                           2 // int ans = -1;
44
45 const int MOD = 1e9+7;
                                                           3 // if (a == 0 && b == 0) {
                                                           4 //
46
                                                                    if (c != 0) ans = 0;
                                                           5 //
47 struct Matriz{
                                                                    else ans = (x2 - x1 + 1) * (y2 - y1 + 1);
      vector < vector < ll >> mat;
                                                           6 // }
48
      int rows, columns;
                                                           7 // else if (a == 0) {
49
50
                                                           8 //
                                                                   if (c % b == 0 && y1 <= c / b && y2 >= c / b)
      vector<ll> operator[](int i){
                                                                 ans = (x2 - x1 + 1);
5.1
          return mat[i];
                                                           9 //
                                                                   else ans = 0:
                                                          10 // }
53
54
                                                          11 // else if (b == 0) {
55
      Matriz(vector < vector < 11 >> & matriz) {
                                                          12 //
                                                                 if (c % a == 0 && x1 <= c / a && x2 >= c / a)
          mat = matriz;
56
                                                                 ans = (y2 - y1 + 1);
          rows = mat.size();
57
                                                                 else ans = 0;
           columns = mat[0].size();
                                                          14 // }
5.8
59
                                                          1.5
60
                                                           16 // Careful when a or b are negative or zero
      Matriz(int row, int column, bool identity=false){ _{17}
6.1
          rows = row; columns = column;
                                                          18 // if (ans == -1) ans = find_all_solutions(a, b, c,
          mat.assign(rows, vector<11>(columns, 0));
63
                                                                x1, x2, y1, y2);
64
          if(identity) {
                                                          19 // cout << ans << '\n';
              for(int i = 0; i < min(rows, columns); i</pre>
6.5
                                                          21 // Problems:
                   mat[i][i] = 1;
                                                          22 // https://www.spoj.com/problems/CEQU/
66
               }
67
                                                          23 // http://codeforces.com/problemsets/acmsguru/problem
          }
                                                                 /99999/106
      }
69
70
                                                          25 // consider trivial case a or b is 0
      Matriz operator * (Matriz a) {
                                                          26 int gcd(int a, int b, int& x, int& y) {
          assert(columns == a.rows);
72
                                                          27
                                                                 if (b == 0) {
           vector<vector<11>> resp(rows, vector<11>(a.
73
                                                                     x = 1;
                                                          28
      columns, 0));
                                                          29
                                                                     y = 0;
                                                          3.0
                                                                     return a;
          for(int i = 0; i < rows; i++){</pre>
7.5
                                                          3.1
76
               for(int j = 0; j < a.columns; j++){</pre>
                                                          32
                                                                 int x1, y1;
                  for(int k = 0; k < a.rows; k++){</pre>
                                                          33
                                                                 int d = gcd(b, a % b, x1, y1);
                       resp[i][j] = (resp[i][j] + (mat[i]_{34})
78
                                                                 x = y1;
      [k] * 1LL * a[k][j]) % MOD) % MOD;
                                                                 y = x1 - y1 * (a / b);
                                                          35
                   }
7.9
                                                          36
                                                                 return d;
80
                                                          37 }
          }
81
                                                          3.8
          return Matriz(resp);
82
                                                          _{39} // x and y are one solution and g is the gcd, all
83
                                                                 passed as reference
84
                                                           40 // minx <= x <= maxx miny <= y <= maxy
      Matriz operator + (Matriz a) {
85
                                                          41 bool find_any_solution(int a, int b, int c, int &x0,
          assert(rows == a.rows && columns == a.columns
86
                                                                int &y0, int &g) {
                                                                 g = gcd(abs(a), abs(b), x0, y0);
          vector<vector<ll>> resp(rows, vector<ll>(
                                                                 if (c % g) {
                                                          43
      columns,0));
                                                          44
                                                                     return false;
           for(int i = 0; i < rows; i++){</pre>
                                                           45
              for(int j = 0; j < columns; j++){</pre>
89
                   resp[i][j] = (resp[i][j] + mat[i][j] 47
90
                                                                 x0 *= c / g;
                                                                 y0 *= c / g;
      + a[i][j]) % MOD;
91
                                                                 if (a < 0) x0 = -x0;
                                                                 if (b < 0) y0 = -y0;
92
                                                          5.0
          return Matriz(resp);
93
                                                                 return true;
                                                          51
94
                                                          52 }
95 }:
                                                          53
```

```
54 void shift_solution(int & x, int & y, int a, int b, 2
      int cnt) {
       x += cnt * b;
       y -= cnt * a;
56
57 }
_{\rm 59} // return number of solutions in the interval
60 int find_all_solutions(int a, int b, int c, int minx, 9
       int maxx, int miny, int maxy) {
       int x, y, g;
       if (!find_any_solution(a, b, c, x, y, g))
62
63
           return 0;
       a /= g;
64
       b /= g;
65
66
       int sign_a = a > 0 ? +1 : -1;
67
       int sign_b = b > 0 ? +1 : -1;
6.9
       shift_solution(x, y, a, b, (minx - x) / b);
       if (x < minx)</pre>
           shift_solution(x, y, a, b, sign_b);
72
       if (x > maxx)
73
7.4
          return 0:
       int lx1 = x;
7.6
       shift_solution(x, y, a, b, (maxx - x) / b);
78
       if (x > maxx)
           shift_solution(x, y, a, b, -sign_b);
79
       int rx1 = x;
80
8.1
       shift_solution(x, y, a, b, -(miny - y) / a);
82
       if (y < miny)
83
           shift_solution(x, y, a, b, -sign_a);
84
       if (y > maxy)
           return 0:
86
       int 1x2 = x;
88
89
       shift_solution(x, y, a, b, -(maxy - y) / a);
       if (y > maxy)
90
           shift_solution(x, y, a, b, sign_a);
91
92
       int rx2 = x;
93
       if (1x2 > rx2)
9.5
          swap(1x2, rx2);
       int lx = max(lx1, lx2);
96
97
       int rx = min(rx1, rx2);
       if (lx > rx)
100
          return 0;
       return (rx - lx) / abs(b) + 1;
102 }
   8.11 Fast Exponentiation
```

9 Algorithms

9.1 Lis

```
int lis(vector<int> const& a) {
```

9.2 Ternary Search

```
double ternary_search(double 1, double r) {
      double eps = 1e-9;
                                     //set the error
      limit here
      while (r - 1 > eps) {
          double m1 = 1 + (r - 1) / 3;
          double m2 = r - (r - 1) / 3;
          double f1 = f(m1);
                                 //evaluates the
      function at m1
         double f2 = f(m2);
                                 //evaluates the
      function at m2
         if (f1 < f2)
              1 = m1;
          else
1.0
              r = m2;
11
12
                                      //return the
      return f(1);
      maximum of f(x) in [1, r]
14 }
```

9.3 Binary Search First True

```
int first_true(int lo, int hi, function < bool(int) > f)
      {
2
      hi++;
      while (lo < hi) {
3
         int mid = lo + (hi - lo) / 2;
4
          if (f(mid)) {
6
             hi = mid;
7
           else {
              lo = mid + 1;
9
      }
      return lo;
```

9.4 Delta-encoding

```
# # include < bits/stdc++.h>
2 using namespace std;
4 int main(){
      int n, q;
5
      cin >> n >> q;
      int [n];
      int delta[n+2];
      while(q--){
10
          int 1, r, x;
           cin >> 1 >> r >> x;
12
           delta[1] += x;
13
           delta[r+1] -= x;
14
15
16
      int curr = 0;
17
```

```
for(int i=0; i < n; i++){
18
    curr += delta[i];
19
         v[i] = curr;
20
21
    for(int i=0; i< n; i++){
23
         cout << v[i] << ' ';
25
     cout << '\n';
26
27
     return 0;
28
29 }
```

9.5 Binary Search Last True