

Notebook - Maratona de Programação

Lenhadoras de Segtree

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1 Math 22 // Adding another column, there are: $_{23}$ // 3 ways to go from 2 equal to 2 equal 1.1 Ceil 24 // 2 ways to go from 2 equal to 3 distinct $_{25}$ // 2 ways to go from 3 distinct to 2 equal 1 long long division_ceil(long long a, long long b) { $_{26}$ // 2 ways to go from 3 distinct to 3 distinct return 1 + ((a - 1) / b); // if a != 0 3 } 28 // So we star with matrix 6 6 and multiply it by the transition 3 2 and get 18 12 1.2 To Decimal 6 6 2 2 12 12 30 // the we can exponentiate this matrix to find the 1 const string digits { "0123456789 ABCDEFGHIJKLMNOPQRSTUVWXYZ" }; nth column 32 // Problem: 3 long long to_decimal(const string& rep, long long 33 // https://cses.fi/problemset/task/1722/ base) { long long n = 0; 35 // Complexity: 36 // O(log n) for (auto c : rep) { // if the number can't be represented in this 38 // How to use: $_{39}$ // vector<vector<ll>> v = {{1, 1}, {1, 0}}; if (c > digits[base - 1]) return -1; 40 // Matriz transition = Matriz(v); n *= base;41 // cout << fexp(transition, n)[0][1] << '\n'; n += digits.find(c); 42 43 using ll = long long; 44 return n; 45 const int MOD = 1e9+7; 14 } 46 47 struct Matriz{ Subsets vector < vector < 11 >> mat; 48 int rows, columns; 49 void subsets(vector<int>& nums){ 50 int n = nums.size(); vector<ll> operator[](int i){ int powSize = 1 << n;</pre> return mat[i]; 52 53 for(int counter = 0; counter < powSize; counter++) $_{54}$ Matriz(vector<vector<11>>& matriz){ 55 for(int j = 0; j < n; j++) { mat = matriz; if((counter & (1LL << j)) != 0) { rows = mat.size(); 57 cout << nums[j] << '';</pre> 58 columns = mat[0].size(); 59 cout << '\n'; 60 } 61 Matriz(int row, int column, bool identity=false){ rows = row; columns = column; 62 13 } 63 mat.assign(rows, vector<11>(columns, 0)); if(identity) { 64 1.4 Matrix Exponentiation for(int i = 0; i < min(rows, columns); i</pre> ++) { mat[i][i] = 1; 1 // Description: 66 } $_{2}$ // Calculate the nth term of a linear recursion 67 } 68 4 // Example Fibonacci: $_{5}$ // Given a linear recurrence, for example fibonacci 70 Matriz operator * (Matriz a) { $_{6}$ // F(n) = n, x <= 1 71 assert(columns == a.rows); 7 // F(n) = F(n - 1) + F(n - 2), x > 172 vector < vector < ll >> resp(rows, vector < ll > (a. columns, 0)); $_{9}$ // The recurrence has two terms, so we can build a matrix 2 x 1 so that 74 for(int i = 0; i < rows; i++){</pre> $_{10}$ // n + 1 = transition * n 75 for(int j = 0; j < a.columns; j++){ 76 77 for(int k = 0; k < a.rows; k++){ $_{12}$ // (2 x 1) = (2 x 2) * (2 x 1) $_{13} // F(n) = a b * F(n - 1)$ resp[i][j] = (resp[i][j] + (mat[i][k] * 1LL * a[k][j]) % MOD) % MOD; 14 // F(n - 1) c d F(n - 2)} } 16 // Another Example: } $_{17}$ // Given a grid 3 x n, you want to color it using 3 return Matriz(resp); distinct colors so that $_{18}$ // no adjacent place has the same color. In how many $_{83}$ different ways can you do that? Matriz operator + (Matriz a) { 19 // There are 6 ways for the first column to be 85 assert(rows == a.rows && columns == a.columns colored using 3 distinct colors $_{20}$ // ans 6 ways using 2 equal colors and 1 distinct one

5

9

10

11

12

13

3

5

9

11

```
87
       columns, 0));
                                                              11 res = 1;
          for(int i = 0; i < rows; i++){
                                                              b %= mod;
88
              for(int j = 0; j < columns; j++){
                                                              while(e){
89
                                                                  if(e & 1LL)
                  resp[i][j] = (resp[i][j] + mat[i][j] 5
       + a[i][j]) % MOD;
                                                                     res = (res * b) % mod;
                                                                   e = e >> 1LL;
                                                                  b = (b * b) \% mod;
92
          return Matriz(resp);
93
                                                         9
                                                              return res;
94
                                                        10
                                                        11 }
95 }:
                                                               Linear Diophantine Equation
97 Matriz fexp(Matriz base, 11 exponent){
      Matriz result = Matriz(base.rows, base.rows, 1);
99
       while(exponent > 0){
                                                         _{1} // int a, b, c, x1, x2, y1, y2; cin >> a >> b >> c >>
          if(exponent & 1LL) result = result * base;
100
                                                               x1 >> x2 >> y1 >> y2;
          base = base * base;
                                                         _2 // int ans = -1;
          exponent = exponent >> 1;
102
                                                         _3 // if (a == 0 && b == 0) {
                                                         4 //
                                                                 if (c != 0) ans = 0;
                                                         5 //
104
      return result;
                                                                 else ans = (x2 - x1 + 1) * (y2 - y1 + 1);
                                                         6 // }
105 }
                                                         7 // else if (a == 0) {
  1.5 Crt
                                                                if (c % b == 0 && y1 <= c / b && y2 >= c / b)
                                                              ans = (x2 - x1 + 1);
                                                                 else ans = 0;
 1 ll crt(const vector <pair <ll, ll >> &vet) {
                                                        10 // }
      ll ans = 0, lcm = 1;
                                                        11 // else if (b == 0) {
      11 a, b, g, x, y;
                                                              if (c \% a == 0 && x1 <= c / a && x2 >= c / a)
      for(const auto &p : vet) {
                                                              ans = (y2 - y1 + 1);
          tie(a, b) = p;
                                                        13 //
                                                                 else ans = 0;
          tie(g, x, y) = gcd(lcm, b);
                                                        14 // }
          if((a - ans) % g != 0) return -1; // no
                                                        15
       solution
                                                        16 // Careful when a or b are negative or zero
          ans = ans + x * ((a - ans) / g) % (b / g) *
                                                        17
                                                        18 // if (ans == -1) ans = find_all_solutions(a, b, c,
          lcm = lcm * (b / g);
                                                              x1, x2, y1, y2);
          ans = (ans \% lcm + lcm) \% lcm;
10
                                                        19 // cout << ans << '\n';
       return ans:
12
                                                        21 // Problems:
13 }
                                                        22 // https://www.spoj.com/problems/CEQU/
                                                        23 // http://codeforces.com/problemsets/acmsguru/problem
       Binary To Decimal
                                                              /99999/106
                                                        25 // consider trivial case a or b is 0
 int binary_to_decimal(long long n) {
                                                        26 int gcd(int a, int b, int& x, int& y) {
    int dec = 0, i = 0, rem;
                                                              if (b == 0) {
                                                        27
                                                                  x = 1;
                                                        28
    while (n!=0) {
 4
                                                                  y = 0;
                                                        29
      rem = n \% 10;
                                                        30
                                                                  return a;
      n /= 10;
                                                              }
                                                        31
      dec += rem * pow(2, i);
                                                        32
                                                              int x1, y1;
      ++i;
                                                              int d = gcd(b, a % b, x1, y1);
                                                        33
 9
                                                              x = y1;
                                                        34
10
                                                              y = x1 - y1 * (a / b);
    return dec;
11
                                                              return d;
                                                        36
12 }
                                                        37 }
13
14 long long decimal_to_binary(int n) {
                                                        _{39} // x and y are one solution and g is the gcd, all
    long long bin = 0;
15
                                                              passed as reference
    int rem, i = 1;
16
                                                        _{\rm 40} // minx <= x <= maxx miny <= y <= maxy
                                                        41 bool find_any_solution(int a, int b, int c, int &x0,
     while (n!=0) {
18
                                                              int &y0, int &g) {
      rem = n \% 2;
19
                                                              g = gcd(abs(a), abs(b), x0, y0);
                                                        42
      n /= 2;
20
                                                        43
                                                              if (c % g) {
      bin += rem * i;
21
                                                                  return false;
                                                        44
      i *= 10;
                                                        45
23
                                                        46
                                                              x0 *= c / g;
                                                        47
25
    return bin;
                                                              y0 *= c / g;
                                                              if (a < 0) x0 = -x0;
                                                        49
                                                              if (b < 0) y0 = -y0;
        Fast Exponentiation
                                                              return true;
                                                        51
```

52 }

```
return (a + b) / 2;
                                                           18
54 void shift_solution(int & x, int & y, int a, int b,
                                                           19 }
       int cnt) {
                                                           20
       x += cnt * b;
                                                           21 int main() {
       y -= cnt * a;
                                                               ld ans = root(0, 1);
                                                               if (abs(f(ans)) <= EPS2) cout << fixed <<</pre>
57 }
                                                                 setprecision(4) << ans << '\n';</pre>
59 // return number of solutions in the interval
                                                               else cout << "No solution\n";</pre>
60 int find_all_solutions(int a, int b, int c, int minx, 25
        int maxx, int miny, int maxy) {
                                                               return 0;
       int x, y, g;
61
62
       if (!find_any_solution(a, b, c, x, y, g))
                                                             1.10 Sieve Of Eratosthenes
63
           return 0;
       a /= g;
64
       b /= g;
65
                                                           vector < bool > is_prime(MAX, true);
66
                                                           vector <int> primes;
67
       int sign_a = a > 0 ? +1 : -1;
       int sign_b = b > 0 ? +1 : -1;
68
                                                           4 void sieve() {
                                                                 is_prime[0] = is_prime[1] = false;
                                                            5
       shift_solution(x, y, a, b, (minx - x) / b);
70
                                                                  for (int i = 2; i < MAX; i++) {
       if (x < minx)
71
                                                                      if (is_prime[i]) {
           shift_solution(x, y, a, b, sign_b);
72
                                                                          primes.push_back(i);
       if (x > maxx)
73
           return 0;
                                                                          for (int j = i + i; j < MAX; j += i)
                                                           10
       int 1x1 = x;
75
                                                           11
                                                                              is_prime[j] = false;
76
                                                                      }
                                                           12
       shift_solution(x, y, a, b, (maxx - x) / b);
77
                                                           13
       if (x > maxx)
78
                                                           14 }
           shift_solution(x, y, a, b, -sign_b);
79
       int rx1 = x;
80
                                                             1.11 Horner Algorithm
81
       shift_solution(x, y, a, b, -(miny - y) / a);
82
                                                            1 // Description:
       if (y < miny)</pre>
83
                                                           _2 // Evaluates y = f(x)
           shift_solution(x, y, a, b, -sign_a);
       if (y > maxy)
85
                                                            4 // Problem:
           return 0;
                                                            5 // https://onlinejudge.org/index.php?option=
       int 1x2 = x;
87
                                                                 com_onlinejudge&Itemid=8&page=show_problem&
88
                                                                  problem=439
       shift_solution(x, y, a, b, -(maxy - y) / a);
89
       if (v > maxv)
90
                                                            7 // Complexity:
91
           shift_solution(x, y, a, b, sign_a);
                                                            8 // O(n)
       int rx2 = x;
92
93
                                                           10 using polynomial = std::vector<int>;
       if (1x2 > rx2)
94
                                                           11
           swap(1x2, rx2);
95
                                                           12 polynomial p \{6, -5, 2\}; // p(x) = x^2 - 5x + 6;
       int 1x = max(1x1, 1x2);
96
                                                           13
       int rx = min(rx1, rx2);
97
                                                           14 int degree(const polynomial& p) {
                                                           15
                                                               return p.size() - 1;
       if (1x > rx)
99
                                                           16 }
100
           return 0:
       return (rx - lx) / abs(b) + 1;
101
                                                           18 int evaluate(const polynomial& p, int x) {
102 }
                                                               int y = 0, N = degree(p);
         Function Root
                                                               for (int i = N; i >= 0; --i) {
                                                           21
                                                                 y *= x;
 const ld EPS1 = 1e-9; // iteration precision error
                                                                  y += p[i];
                                                           23
 2 const ld EPS2 = 1e-4; // output precision error
                                                               }
                                                           25
 4 ld f(ld x) {
                                                               return y;
    // \exp(-x) == e^{-x}
     return p * exp(-x) + q * sin(x) + r * cos(x) + s * 27 }
       tan(x) + t * x * x + u;
                                                                     Multiplicative Inverse
 7 }
                                                           1 ll extend_euclid(ll a, ll b, ll &x, ll &y) {
 9 ld root(ld a, ld b) {
     while (b - a \ge EPS1) {
                                                                 if (a == 0)
10
                                                            2
       1d c = (a + b) / 2.0;
11
                                                           3
       1d y = f(c);
                                                                      x = 0; y = 1;
12
                                                            4
                                                                      return b;
       if (y < 0) b = c;
14
                                                            6
                                                                  11 x1, y1;
       else a = c;
15
     }
                                                                 11 d = extend_euclid(b%a, a, x1, y1);
16
```

x = y1 - (b / a) * x1;

```
1 // msb de 0 é undefined
      v = x1:
10
                                                          2 #define msb(n) (32 - __builtin_clz(n))
11
      return d;
                                                          3 // #define msb(n) (64 - __builtin_clzll(n) )
12 }
                                                          4 // popcount
13
                                                         5 // turn bit off
14 // \gcd(a, m) = 1 para existir solução
_{15} // ax + my = 1, ou a*x = 1 (mod m)
16 ll inv_gcd(ll a, ll m) { // com gcd
                                                          7 bool bit_on(int n, int bit) {
17 11 x, y;
                                                               if(1 & (n >> bit)) return true;
18 extend_euclid(a, m, x, y);
                                                                else return false;
                                                          9
   return (((x \% m) + m) \%m);
20 }
                                                            1.17 Prime Factors
22 ll inv(ll a, ll phim) { // com phi(m), se m for primo
      entao phi(m) = p-1
                                                          1 vector < pair < long long, int >> fatora(long long n) {
   11 e = phim - 1;
                                                             vector < pair < long long, int >> ans;
   return fexp(a, e, MOD);
24
                                                              for(long long p = 2; p*p <= n; p++) {
25 }
                                                                if(n % p == 0) {
                                                                  int expoente = 0;
         Representation Arbitrary Base
                                                                  while(n \% p == 0) {
                                                          6
                                                                    n /= p;
1 const string digits { "0123456789
                                                                    expoente++;
                                                          8
      ABCDEFGHIJKLMNOPQRSTUVWXYZ" };
                                                          9
                                                                  }
                                                                  ans.emplace_back(p, expoente);
                                                         10
3 string representation(int n, int b) {
                                                         11
    string rep;
                                                              }
                                                         12
                                                         13
                                                              if(n > 1) ans.emplace_back(n, 1);
                                                         14
                                                              return ans;
      rep.push_back(digits[n % b]);
                                                         15 }
      n /= b:
    } while (n);
                                                            2
                                                                 DP
   reverse(rep.begin(), rep.end());
11
                                                            2.1
                                                                 Knapsack With Index
    return rep;
13
                                                          void knapsack(int W, int wt[], int val[], int n) {
                                                          2
                                                                int i, w;
  1.14 Set Operations
                                                                int K[n + 1][W + 1];
1 // Complexity;
                                                                for (i = 0; i \le n; i++) {
_{\rm 2} // O(n * m) being n and m the sizes of the two sets
                                                                    for (w = 0; w \le W; w++) {
3 // 2*(count1+count2)-1 (where countX is the distance
                                                                         if (i == 0 || w == 0)
      between firstX and lastX):
                                                                            K[i][w] = 0;
                                                                         else if (wt[i - 1] <= w)
5 vector < int > res;
                                                                             K[i][w] = max(val[i - 1] +
6 set_union(s1.begin(), s1.end(), s2.begin(), s2.end(), 11
                                                                                 K[i - 1][w - wt[i - 1]], K[i -
       inserter(res, res.begin()));
                                                                1][w]);
7 set_intersection(s1.begin(), s1.end(), s2.begin(), s2
12
                                                                         else
      .end(), inserter(res, res.begin()));
                                                                             K[i][w] = K[i - 1][w];
_{8} // present in the first set, but not in the second
                                                                    }
9 set_difference(s1.begin(), s1.end(), s2.begin(), s2. _{15}
      end(), inserter(res, res.begin()));
_{\rm 10} // present in one of the sets, but not in the other
                                                                int res = K[n][W]:
                                                         17
set_symmetric_difference(s1.begin(), s1.end(), s2.
                                                                cout << res << endl;</pre>
                                                         18
      begin(), s2.end(), inserter(res, res.begin()));
                                                         19
                                                         20
  1.15 Divisors
                                                                for (i = n; i > 0 && res > 0; i--) {
                                                         21
                                                                    if (res == K[i - 1][w])
                                                         22
                                                                        continue;
1 vector<long long> all_divisors(long long n) {
    vector < long long > ans;
                                                         24
                                                                    else {
                                                                        cout << " " << wt[i - 1];</pre>
                                                         25
    for (long long a = 1; a*a <= n; a++) {
                                                                        res = res - val[i - 1];
      if(n \% a == 0) {
                                                         26
                                                                        w = w - wt[i - 1];
                                                         27
        long long b = n / a;
                                                         28
                                                                    }
        ans.push_back(a);
                                                         29
        if(a != b) ans.push_back(b);
                                                         30 }
      }
                                                         31
    }
9
                                                         32 int main()
    sort(ans.begin(), ans.end());
                                                         33 {
11
    return ans;
                                                                int val[] = { 60, 100, 120 };
12 }
                                                         34
                                                                int wt[] = { 10, 20, 30 };
  1.16 Check If Bit Is On
                                                                int W = 50;
                                                         36
```

int n = sizeof(val) / sizeof(val[0]);

```
return dp[m][n] = 1 + min({edit_distance(str1,
38
                                                                str2, m, n - 1), edit_distance(str1, str2, m - 1,
39
      knapsack(W, wt, val, n);
                                                                 n), edit_distance(str1, str2, m - 1, n - 1)});
40
      return 0;
41
42 }
                                                            2.4 Knapsack
  2.2 Substr Palindrome
                                                          1 int val[MAXN], peso[MAXN], dp[MAXN][MAXS];
1 // êvoc deve informar se a substring de S formada
      pelos elementos entre os indices i e j
                                                          3 int knapsack(int n, int m){ // n Objetos | Peso max
                                                                for(int i=0;i<=n;i++){
2 // é um palindromo ou ano.
                                                                   for (int j=0; j <= m; j++) {
                                                                        if(i==0 \text{ or } j==0)
4 char s[MAX];
5 int calculado[MAX][MAX]; // inciado com false, ou 0
                                                                             dp[i][j] = 0;
6 int tabela[MAX][MAX];
                                                                         else if(peso[i-1]<=j)
                                                                             dp[i][j] = max(val[i-1]+dp[i-1][j-1]
8 int is_palin(int i, int j){
                                                                peso[i-1]], dp[i-1][j]);
   if(calculado[i][j]){
                                                          10
                                                                         else
                                                                             dp[i][j] = dp[i-1][j];
      return tabela[i][j];
                                                          11
10
11
    }
                                                          12
                                                                   }
    if(i == j) return true;
12
                                                          13
    if(i + 1 == j) return s[i] == s[j];
                                                                return dp[n][m];
                                                          14
13
                                                          15 }
14
    int ans = false;
15
                                                            2.5 Digits
    if(s[i] == s[j]){
     if(is_palin(i+1, j-1)){
17
18
        ans = true:
                                                          1 // achar a quantidade de numeros menores que R que
                                                                possuem no maximo 3 digitos nao nulos
19
    }
                                                          2 // a ideia eh utilizar da ordem lexicografica para
20
21
    calculado[i][j] = true;
                                                                checar isso pois se temos por exemplo
                                                          _{\rm 3} // o numero 8500, a gente sabe que se pegarmos o
    tabela[i][j] = ans;
22
    return ans;
                                                                numero 7... qualquer digito depois do 7
24 }
                                                          4 // sera necessariamente menor q 8500
        Edit Distance
                                                          6 string r;
                                                          7 int tab[20][2][5];
1 // Description:
_2 // Minimum number of operations required to transform _9 // i - digito de R \,
                                                          10 // menor - ja pegou um numero menor que um digito de
       a string into another
_3 // Operations allowed: add character, remove
                                                                R
                                                          11 // qt - quantidade de digitos nao nulos
      character, replace character
                                                          12 int dp(int i, bool menor, int qt){
5 // Parameters:
                                                               if(qt > 3) return 0;
                                                          13
                                                                if(i >= r.size()) return 1;
6 // str1 - string to be transformed into str2
                                                          14
7 // str2 - string that str1 will be transformed into
                                                         15
                                                                if(tab[i][menor][qt] != -1) return tab[i][menor][
_{\rm 8} // m - size of str1
                                                                qt];
_9 // n - size of str2
                                                                int dr = r[i] - '0';
                                                          17
11 // Problem:
                                                                int res = 0;
12 // https://cses.fi/problemset/task/1639
                                                          19
                                                                for(int d = 0; d \le 9; d++) {
                                                          20
                                                                    int dnn = qt + (d > 0);
14 // Complexity:
                                                          21
                                                                     if(menor == true) {
15 // O(m x n)
                                                          22
                                                                         res += dp(i+1, true, dnn);
                                                                    }
_{17} // How to use:
                                                          24
                                                                     else if(d < dr) {</pre>
18 // memset(dp, -1, sizeof(dp));
19 // string a, b;
                                                                        res += dp(i+1, true, dnn);
20 // edit_distance(a, b, (int)a.size(), (int)b.size());27
                                                                     else if(d == dr) {
22 // Notes:
                                                                        res += dp(i+1, false, dnn);
                                                          29
_{23} // Size of dp matriz is m x n
                                                                }
                                                          31
25 int dp[MAX][MAX];
                                                                return tab[i][menor][qt] = res;
27 int edit_distance(string &str1, string &str2, int m, 34 }
      int n) {
                                                            2.6 Coins
      if (m == 0) return n;
      if (n == 0) return m;
                                                          1 int tb[1005];
      if (dp[m][n] != -1) return dp[m][n];
                                                          2 int n:
31
                                                          3 vector <int> moedas;
      if (str1[m - 1] == str2[n - 1]) return dp[m][n] = 4
33
       edit_distance(str1, str2, m - 1, n - 1);
                                                          5 int dp(int i){
```

```
if(i >= n)
    return 0;
    if(tb[i] != -1)
    return tb[i];

tb[i] = max(dp(i+1), dp(i+2) + moedas[i]);
    return tb[i];

int main(){
    memset(tb,-1,sizeof(tb));
}

2.7 Minimum Coin Change
```

```
1 int n;
vector<int> valores;
4 int tabela[1005];
6 int dp(int k){
   if(k == 0) {
     return 0;
   if(tabela[k] != -1)
10
11
     return tabela[k];
   int melhor = 1e9;
12
   for (int i = 0; i < n; i++) {
     if(valores[i] <= k)</pre>
        melhor = min(melhor,1 + dp(k - valores[i]));
15
16
17
    return tabela[k] = melhor;
18 }
```

2.8 Kadane

33

```
1 // achar uma subsequencia continua no array que a
      soma seja a maior possivel
2 // nesse caso vc precisa multiplicar exatamente 1
      elemento da subsequencia
3 // e achar a maior soma com isso
5 int n, x, arr[MAX], tab[MAX][2]; // tab[maior
      resposta no intervalo][foi multiplicado ou ano]
6
7 int dp(int i, bool mult) {
      if (i == n-1) {
          if (!mult) return arr[n-1]*x;
          return arr[n-1];
10
11
      if (tab[i][mult] != -1) return tab[i][mult];
13
      int res;
1.5
      if (mult) {
16
          res = max(arr[i], arr[i] + dp(i+1, 1));
18
      else {
          res = max({
20
              arr[i]*x,
21
              arr[i]*x + dp(i+1, 1),
22
              arr[i] + dp(i+1, 0)
23
          });
25
      return tab[i][mult] = res;
27
28 }
30 int main() {
      memset(tab, -1, sizeof(tab));
32
```

```
int ans = -00;
34
35
       for (int i = 0; i < n; i++) {
           ans = max(ans, dp(i, 0));
36
37
       return 0:
39
44 int ans = a[0], ans_1 = 0, ans_r = 0;
45 int sum = 0, minus_pos = -1;
46
47 for (int r = 0; r < n; ++r) {
       sum += a[r];
48
       if (sum > ans) {
49
           ans = sum;
           ans_1 = minus_pos + 1;
51
           ans_r = r;
       }
53
       if (sum < 0) {
54
           sum = 0;
55
           minus_pos = r;
56
       }
57
58 }
```

3 Template

3.1 Template

```
1 #include <bits/stdc++.h>
2 using namespace std;
4 #define int long long
5 #define optimize std::ios::sync_with_stdio(false);
     cin.tie(NULL);
6 #define vi vector<int>
7 #define ll long long
8 #define pb push_back
9 #define mp make_pair
10 #define ff first
11 #define ss second
12 #define pii pair<int, int>
13 #define MOD 100000007
14 #define sqr(x) ((x) * (x))
#define all(x) (x).begin(), (x).end()
16 #define FOR(i, j, n) for (int i = j; i < n; i++)
17 #define qle(i, n) (i == n ? "\n" : " ")
18 #define endl "\n"
19 const int oo = 1e9;
20 const int MAX = 1e6;
22 int32_t main(){ optimize;
23
24
      return 0;
```

3.2 Template Clean

```
1 // Notes:
2 // Compile and execute
3 // g++ teste.cpp -o teste -std=c++17
4 // ./teste < teste.txt
5
6 // Print with precision
7 // cout << fixed << setprecision(12) << value << endl
;
8
9 // File as input and output
10 // freopen("input.txt", "r", stdin);
11 // freopen("output.txt", "w", stdout);</pre>
```

```
1 // Description:
13 #include <bits/stdc++.h>
                                                          2 // Finds the longest common subsquence between two
14 using namespace std;
                                                                string
                                                          4 // Problem:
16 int main() {
      ios::sync_with_stdio(false);
                                                          5 // https://codeforces.com/gym/103134/problem/B
17
      cin.tie(NULL);
                                                          7 // Complexity:
19
                                                          _{8} // O(mn) where m and n are the length of the strings
20
21
      return 0;
                                                         10 string lcsAlgo(string s1, string s2, int m, int n) {
22
23 }
                                                         11
                                                             int LCS_{table}[m + 1][n + 1];
                                                         12
                                                              for (int i = 0; i \le m; i++) {
                                                         13
       Strings
                                                                for (int j = 0; j \le n; j++) {
                                                         14
                                                                  if (i == 0 || i == 0)
                                                         15
  4.1 Kmp
                                                                    LCS_table[i][j] = 0;
                                                                  else if (s1[i - 1] == s2[j - 1])
                                                         17
                                                                    LCS_{table[i][j]} = LCS_{table[i - 1][j - 1]} +
vector < int > prefix_function(string s) {
                                                                1:
      int n = (int)s.length();
                                                                  else
                                                         19
      vector < int > pi(n);
                                                                    LCS_table[i][j] = max(LCS_table[i - 1][j],
                                                         20
      for (int i = 1; i < n; i++) {
                                                                LCS_table[i][j - 1]);
          int j = pi[i-1];
                                                         21
          while (j > 0 \&\& s[i] != s[j])
                                                         22
              j = pi[j-1];
                                                         23
          if (s[i] == s[j])
                                                              int index = LCS_table[m][n];
                                                         24
              j++;
                                                              char lcsAlgo[index + 1];
                                                         25
          pi[i] = j;
                                                              lcsAlgo[index] = '\0';
                                                         26
      }
11
                                                         27
      return pi;
12
                                                         28
                                                              int i = m, j = n;
13 }
                                                              while (i > 0 && j > 0) {
                                                         29
                                                                if (s1[i - 1] == s2[j - 1]) {
                                                         30
       Generate All Permutations
  4.2
                                                                  lcsAlgo[index - 1] = s1[i - 1];
                                                                  i--:
                                                         32
vector < string > generate_permutations(string s) {
                                                                  j --;
                                                         33
      int n = s.size();
                                                                  index --;
                                                         34
      vector<string> ans;
                                                         35
4
                                                         36
      sort(s.begin(), s.end());
                                                                else if (LCS_table[i - 1][j] > LCS_table[i][j -
                                                         37
                                                                1])
      do {
                                                                 i - - :
          ans.push_back(s);
                                                                else
      } while (next_permutation(s.begin(), s.end()));
9
                                                                  j - -;
10
                                                         41
      return ans:
11
12 }
                                                              return lcsAlgo;
                                                         43
                                                         44 }
  4.3 Generate All Sequences Length K
                                                                  Trie
1 // gera todas as ipossveis êsequncias usando as letras
       em set (de comprimento n) e que tenham tamanho k 1 const int K = 26;
_2 // sequence = ""
3 vector<string> generate_sequences(char set[], string 3 struct Vertex {
      sequence, int n, int k) {
                                                             int next[K];
                                                                bool output = false;
     if (k == 0){
                                                                int p = -1;
         return { sequence };
5
                                                                char pch;
6
                                                                int link = -1;
     vector<string> ans;
                                                                int go[K];
                                                         10
     for (int i = 0; i < n; i++) {
9
                                                                Vertex(int p=-1, char ch='$') : p(p), pch(ch) {
          auto aux = generate_sequences(set, sequence + 11
10
                                                                    fill(begin(next), end(next), -1);
       set[i], n, k - 1);
                                                         12
          ans.insert(ans.end(), aux.begin(), aux.end()) 13
                                                                    fill(begin(go), end(go), -1);
11
                                                         14
                                                         15 };
          // for (auto e : aux) ans.push_back(e);
12
13
                                                         17 vector < Vertex > t(1);
     return ans;
15
                                                         19 void add_string(string const& s) {
16 }
                                                                int v = 0;
                                                                for (char ch : s) {
  4.4 Lcs
                                                         21
                                                                    int c = ch - 'a';
                                                         22
```

```
if (t[v].next[c] == -1) {
23
                                                           17
24
               t[v].next[c] = t.size();
                                                           18
                                                                  if(palTemp.size() > 0)
               t.emplace_back(v, ch);
                                                                      ans.push_back(palTemp);
25
                                                           19
           }
                                                           20
           v = t[v].next[c];
                                                           21
                                                                  return ans;
      }
                                                           22 }
28
29
      t[v].output = true;
30 }
                                                             5.2 Int128
31
32 int go(int v, char ch);
                                                           1 __int128 read() {
33
                                                                _{-}int128 x = 0, f = 1;
                                                           2
34 int get_link(int v) {
                                                                  char ch = getchar();
      if (t[v].link == -1) {
35
                                                                  while (ch < '0' || ch > '9') {
                                                           4
          if (v == 0 || t[v].p == 0)
                                                                     if (ch == '-') f = -1;
               t[v].link = 0;
37
                                                                      ch = getchar();
38
               t[v].link = go(get_link(t[v].p), t[v].pch
                                                                  while (ch >= '0' && ch <= '9') {
      );
                                                                     x = x * 10 + ch - '0';
                                                            9
                                                                      ch = getchar();
                                                           10
      return t[v].link;
41
                                                                  }
                                                           11
42 }
                                                                  return x * f;
                                                           12
43
                                                           13 }
44 int go(int v, char ch) {
                                                           14 void print(__int128 x) {
      int c = ch - 'a';
                                                           15
                                                                  if (x < 0) {
      if (t[v].go[c] == -1) {
46
                                                                     putchar('-');
                                                           16
           if (t[v].next[c] != -1)
47
                                                           17
                                                                      x = -x;
               t[v].go[c] = t[v].next[c];
48
                                                           18
           else
49
               t[v].go[c] = v == 0 ? 0 : go(get_link(v), 19 20
                                                                  if (x > 9) print(x / 10);
                                                                  putchar(x % 10 + '0');
       ch);
                                                           21 }
51
      return t[v].go[c];
52
53 }
```

4.6 Z-function

```
vector <int> z_function(string s) {
      int n = (int) s.length();
      vector < int > z(n);
      for (int i = 1, l = 0, r = 0; i < n; ++i) {
           if (i \le r)
              z[i] = min (r - i + 1, z[i - 1]);
           while (i + z[i] < n && s[z[i]] == s[i + z[i]]
      11)
              ++z[i];
8
           if (i + z[i] - 1 > r)
              1 = i, r = i + z[i] - 1;
10
11
      }
12
      return z;
13 }
```

Misc

5.1 Split

```
vector<string> split(string txt, char key = ' '){
      vector<string> ans;
      string palTemp = "";
      for(int i = 0; i < txt.size(); i++){</pre>
          if(txt[i] == key){
               if(palTemp.size() > 0){
                   ans.push_back(palTemp);
                   palTemp = "";
10
              }
11
          } else{
              palTemp += txt[i];
13
15
      }
16
```

Graphs

6.1 Centroid Find

```
1 // Description:
2 // Indexed at zero
_{\rm 3} // Find a centroid, that is a node such that when it
      is appointed the root of the tree,
_4 // each subtree has at most floor(n/2) nodes.
6 // Problem:
7 // https://cses.fi/problemset/task/2079/
9 // Complexity:
10 // O(n)
_{12} // How to use:
13 // get_subtree_size(0);
14 // cout << get_centroid(0) + 1 << endl;</pre>
15
17 vector < int > adj[MAX];
18 int subtree_size[MAX];
20 int get_subtree_size(int node, int par = -1) {
int &res = subtree_size[node];
22
    res = 1;
23
    for (int i : adj[node]) {
     if (i == par) continue;
24
      res += get_subtree_size(i, node);
25
    }
26
27
    return res;
28 }
30 int get_centroid(int node, int par = -1) {
for (int i : adj[node]) {
32
     if (i == par) continue;
33
      if (subtree_size[i] * 2 > n) { return
34
      get_centroid(i, node); }
```

```
7
35
                                                            14
36
    return node;
                                                            15
                                                                   for (int i=0; i<n; ++i) {
                                                                        int v = -1;
37 }
                                                            16
                                                                        for (int j = 0; j < n; ++ j) {
38
                                                            17
                                                                           if (!selected[j] && (v == -1 || min_e[j].
39 int main() {
    cin >> n:
                                                                   w < min_e[v].w))
40
    for (int i = 0; i < n - 1; i++) {
41
                                                            19
     int u, v; cin >> u >> v;
                                                                       }
42
                                                            20
      u--; v--;
43
                                                            21
     adj[u].push_back(v);
                                                                        if (min_e[v].w == INF) {
                                                            22
      adj[v].push_back(u);
                                                                            cout << "No MST!" << endl;</pre>
45
                                                            23
46
                                                            24
                                                                            exit(0);
                                                                       }
47
                                                            25
    get_subtree_size(0);
48
                                                            26
    cout << get_centroid(0) + 1 << endl;</pre>
                                                                        selected[v] = true;
                                                            27
                                                                        total_weight += min_e[v].w;
                                                            28
                                                            29
                                                                        if (min_e[v].to != -1)
                                                                            cout << v << " " << min_e[v].to << endl;</pre>
        Bipartite
  6.2
                                                            30
                                                                        for (int to = 0; to < n; ++to) {
                                                            32
1 const int NONE = 0, BLUE = 1, RED = 2;
                                                                            if (adj[v][to] < min_e[to].w)</pre>
                                                            33
vector < vector < int >> graph (100005);
                                                                                min_e[to] = {adj[v][to], v};
                                                            34
3 vector < bool > visited(100005);
                                                            35
4 int color [100005];
                                                            36
                                                            37
6 bool bfs(int s = 1){
                                                            38
                                                                   cout << total_weight << endl;</pre>
                                                            39 }
       queue < int > q;
       q.push(s);
9
                                                               6.4 Ford Fulkerson Edmonds Karp
       color[s] = BLUE;
11
                                                            1 // Description:
12
       while (not q.empty()){
                                                             2 // Obtains the maximum possible flow rate given a
           auto u = q.front(); q.pop();
13
                                                                   network. A network is a graph with a single
14
                                                                   source vertex and a single sink vertex in which
           for (auto v : graph[u]){
                                                                   each edge has a capacity
               if (color[v] == NONE){
16
                    color[v] = 3 - color[u];
17
                                                             4 // Complexity:
18
                    q.push(v);
                                                             _{5} // O(V * E^2) where V is the number of vertex and E
               }
19
                                                                   is the number of edges
20
                else if (color[v] == color[u]){
                   return false;
21
                                                             7 int n;
               }
                                                             8 vector < vector < int >> capacity;
           }
23
                                                             9 vector < vector < int >> adj;
                                                            10
25
                                                            int bfs(int s, int t, vector<int>& parent) {
26
       return true;
                                                                   fill(parent.begin(), parent.end(), -1);
                                                            12
27 }
                                                            13
                                                                   parent[s] = -2;
                                                                   queue < pair < int , int >> q;
                                                            14
29 bool is_bipartite(int n){
                                                            15
                                                                   q.push({s, INF});
30
                                                            16
31
       for (int i = 1; i <= n; i++)
                                                                   while (!q.empty()) {
                                                            17
           if (color[i] == NONE and not bfs(i))
32
                                                                       int cur = q.front().first;
                                                            18
               return false;
33
                                                                       int flow = q.front().second;
                                                            19
                                                            20
                                                                       q.pop();
       return true;
35
                                                            21
                                                            22
                                                                        for (int next : adj[cur]) {
                                                                            if (parent[next] == -1 && capacity[cur][
  6.3 Prim
                                                                   next]) {
                                                                                parent[next] = cur;
                                                                                int new_flow = min(flow, capacity[cur
1 int n;
2 vector < vector < int >> adj; // adjacency matrix of graph
                                                                   ][next]);
_{\rm 3} const int \underline{\rm INF} = 1000000000; // weight INF means there _{\rm 26}
                                                                                if (next == t)
       is no edge
                                                                                    return new_flow;
                                                                                q.push({next, new_flow});
5 struct Edge {
                                                                            }
                                                            29
       int w = INF, to = -1;
                                                                        }
                                                            30
7 };
                                                            31
                                                            32
9 void prim() {
                                                                   return 0;
                                                            33
      int total_weight = 0;
                                                            34 }
10
       vector < bool > selected(n, false);
      vector < Edge > min_e(n);
                                                            36 int maxflow(int s, int t) {
12
      min_e[0].w = 0;
                                                                   int flow = 0;
                                                            37
13
```

```
vector<int> parent(n);
                                                                   if (p != -1) level[v] = level[p] + 1;
38
                                                            52
39
       int new_flow;
                                                            53
                                                                   for (auto u : adj[v]) {
                                                                     if (u != p) {
40
                                                            54
       while (new_flow = bfs(s, t, parent)) {
                                                            55
                                                                       dfs(u, v);
41
           flow += new_flow;
                                                            56
                                                                       subtree_size[v] += subtree_size[u];
           int cur = t;
                                                                       if (heavy_child[v] == -1 || subtree_size[u] >
43
                                                            57
           while (cur != s) {
                                                                    subtree_size[heavy_child[v]]) heavy_child[v] = u
44
               int prev = parent[cur];
45
               capacity[prev][cur] -= new_flow;
                                                                     }
46
                                                                   }
               capacity[cur][prev] += new_flow;
                                                            59
47
               cur = prev;
                                                                 }
48
                                                            60
49
           }
                                                            61
       }
                                                                 void decompose(int v, int chead) {
50
                                                            62
                                                                   // start a new path
51
                                                            63
                                                                   if (chead == -1) chead = v;
52
       return flow;
                                                            64
53 }
                                                            65
                                                            66
                                                                   // consecutive ids in the hld path
        Hld Edge
                                                                   at[cpos] = v;
                                                            67
                                                                   pos[v] = cpos++;
                                                                   head[v] = chead;
1 // Description:
                                                            69
_{\rm 2} // Make queries and updates between two vertexes on a ^{70}
                                                                   // if not a leaf
       tree
                                                                   if (heavy_child[v] != -1) decompose(heavy_child[v
                                                            72
4 // Problem:
                                                                   ], chead);
5 // https://www.spoj.com/problems/QTREE/
                                                            73
                                                                   // light child
                                                            74
                                                                   for (auto u : adj[v]){
7 // Complexity:
                                                            75
                                                                     // start new path
8 // O(log ^2 n) for both query and update
                                                            76
                                                                     if (u != parent[v] && u != heavy_child[v])
                                                            77
                                                                   decompose(u, -1);
10 // How to use:
                                                            78
_{11} // HLD hld = HLD(n + 1, adj)
                                                                 }
                                                            79
_{13} // Notes
                                                            80
_{14} // Change the root of the tree on the constructor if _{81}
                                                                 11 query_path(int a, int b) {
                                                                   if (a == b) return 0;
      it's different from 1
                                                            82
                                                                   if(pos[a] < pos[b]) swap(a, b);</pre>
15 // Use together with Segtree
                                                            84
16
17 struct HLD {
                                                                   if(head[a] == head[b]) return seg.query(pos[b] +
                                                            85
                                                                   1, pos[a]);
   vector < int > parent;
18
                                                                   return seg.f(seg.query(pos[head[a]], pos[a]),
    vector < int > pos;
                                                            86
    vector < int > head;
                                                                   query_path(parent[head[a]], b));
20
    vector < int > subtree_size;
                                                                 }
                                                            87
    vector <int > level;
                                                            88
22
    vector < int > heavy_child;
                                                            89
                                                                 ftype query_subtree(int a) {
23
                                                                   if (subtree_size[a] == 1) return 0;
                                                            90
24
    vector<ftype> subtree_weight;
    vector < ftype > path_weight;
                                                                   return seg.query(pos[a] + 1, pos[a] +
                                                            91
25
                                                                   subtree_size[a] - 1);
26
    vector < vector < int >> adj;
                                                                 7
    vector < int > at;
27
    Segtree seg = Segtree(0);
                                                            93
28
                                                                 void update_path(int a, int b, int x) {
                                                            94
    int cpos;
29
                                                                   if (a == b) return;
                                                            95
    int n;
30
                                                                   if(pos[a] < pos[b]) swap(a, b);</pre>
                                                            96
31
    int root;
                                                            97
32
                                                                   if(head[a] == head[b]) return (void)seg.update(
    HLD() {}
33
                                                                   pos[b] + 1, pos[a], x);
34
                                                                   seg.update(pos[head[a]], pos[a], x); update_path(
    HLD(int n, vector < vector < int >> & adj, int root = 1) 99
35
                                                                   parent[head[a]], b, x);
       : adj(adj), n(n), root(root) {
       seg = Segtree(n);
                                                            100
36
       cpos = 0;
                                                           101
                                                                 void update_subtree(int a, int val) {
                                                            102
38
       at.assign(n, 0);
                                                                   if (subtree_size[a] == 1) return;
                                                            103
       parent.assign(n, 0);
39
                                                                   seg.update(pos[a] + 1, pos[a] + subtree_size[a] -
                                                           104
40
       pos.assign(n, 0);
       head.assign(n, 0);
                                                                    1, val);
41
                                                                 }
42
       subtree_size.assign(n, 1);
                                                           105
                                                            106
       level.assign(n, 0);
43
                                                                 // vertex
       heavy_child.assign(n, -1);
                                                           107
                                                                 void update(int a, int val) {
       parent[root] = -1;
                                                           108
45
                                                                   seg.update(pos[a], pos[a], val);
      dfs(root, -1);
                                                           109
46
                                                           110
       decompose(root, -1);
47
    }
                                                            111
48
                                                                 //edge
                                                           112
                                                                 void update(int a, int b, int val) {
                                                           113
    void dfs(int v, int p) {
50
                                                           114
                                                                   if (parent[a] == b) swap(a, b);
      parent[v] = p;
51
```

```
22 vector < bool > visited(MAX);
       update(b, val);
115
116
                                                            24 int up[MAX][BITS + 1];
117
     int lca(int a, int b) {
                                                            25 int level[MAX];
118
       if(pos[a] < pos[b]) swap(a, b);
                                                            26 int level_peso[MAX];
       return head[a] == head[b] ? b : lca(parent[head[a27
120
                                                            28 void find_level() {
     }
                                                                queue <pii > q;
121
                                                            29
122 };
                                                            30
                                                                 q.push(mp(1, 0));
                                                            31
                                                                 visited[1] = true;
         Floyd Warshall
   6.6
                                                            32
                                                            33
                                                            34
                                                                 while (!q.empty()) {
 1 #include <bits/stdc++.h>
                                                                   auto [v, depth] = q.front();
                                                            35
                                                            36
                                                                   q.pop();
 3 using namespace std;
                                                                   level[v] = depth;
                                                            37
 4 using ll = long long;
                                                                   for (auto [u,d] : adj[v]) {
                                                            39
 6 const int MAX = 507;
                                                                     if (!visited[u]) {
 7 const long long INF = 0x3f3f3f3f3f3f3f3f3fLL;
                                                            41
                                                                       visited[u] = true;
                                                                       up[u][0] = v;
                                                            42
 9 11 dist[MAX][MAX];
                                                                       q.push(mp(u, depth + 1));
                                                            43
10 int n;
                                                            44
11
                                                                   }
12 void floyd_warshall() {
                                                                 }
                                                            46
       for (int i = 0; i < n; i++) {
13
                                                            47 }
           for (int j = 0; j < n; j + +) {
14
                                                            48
                if (i == j) dist[i][j] = 0;
15
                                                            49 void find_level_peso() {
                else if (!dist[i][j]) dist[i][j] = INF;
16
                                                                 queue <pii > q;
                                                            50
           }
                                                            51
       }
18
                                                                 q.push(mp(1, 0));
                                                            52
19
                                                                 visited[1] = true;
                                                            53
       for (int k = 0; k < n; k++) {
20
                                                            54
            for (int i = 0; i < n; i++) {
21
                                                                 while (!q.empty()) {
                for (int j = 0; j < n; j++) {
                                                                  auto [v, depth] = q.front();
                                                            56
23
                    // trata o caso no qual o grafo tem
                                                                   q.pop();
       arestas com peso negativo
                                                                   level_peso[v] = depth;
                                                            58
                    if (dist[i][k] < INF && dist[k][j] <</pre>
24
                                                                   for (auto [u,d] : adj[v]) {
25
                        dist[i][j] = min(dist[i][j], dist
                                                            61
                                                                     if (!visited[u]) {
       [i][k] + dist[k][j]);
                                                            62
                                                                       visited[u] = true;
                    }
                                                                       up[u][0] = v;
                                                            63
                }
27
                                                                       q.push(mp(u, depth + d));
                                                            64
           }
28
                                                            65
                                                                     7
       }
29
                                                            66
30 }
                                                            67
                                                                 }
                                                            68 }
   6.7 Lca
                                                            70 int lca(int a, int b) {
                                                                  // get the nodes to the same level
                                                            71
 1 // Description:
                                                                   int mn = min(level[a], level[b]);
 _{2} // Find the lowest common ancestor between two nodes
                                                            72
       in a tree
                                                            73
                                                                   for (int j = 0; j \le BITS; j++) {
                                                                     if (a != -1 && ((level[a] - mn) & (1 << j))) a
 4 // Problem:
                                                                     up[a][j];
 5 // https://cses.fi/problemset/task/1135
                                                                     if (b != -1 && ((level[b] - mn) & (1 << j))) b
 7 // Complexity:
                                                                   = up[b][j];
                                                                   }
 8 // O(log n)
                                                            77
                                                            78
_{10} // How to use:
                                                                   // special case
                                                            79
                                                                   if (a == b) return a;
                                                            80
11 // preprocess();
12 // lca(a, b);
                                                            81
                                                                   // binary search
                                                                   for (int j = BITS; j >= 0; j--) {
_{14} // Notes
                                                            83
                                                                     if (up[a][j] != up[b][j]) {
_{15} // To calculate the distance between two nodes use
                                                                       a = up[a][j];
                                                            85
       the following formula
16 // level_peso[a] + level_peso[b] - 2*level_peso[lca(a 86
                                                                       b = up[b][j];
       , b)]
                                                                     }
                                                                   }
                                                            88
                                                                   return up[a][0];
18 const int MAX = 2e5+10;
                                                            90 }
19 const int BITS = 30;
                                                            92 void preprocess() {
21 vector < pii > adj [MAX];
```

```
visited = vector < bool > (MAX, false);
                                                           26 #define mp make_pair
93
94
     find_level();
                                                           27 #define pii pair <int, int>
     visited = vector < bool > (MAX, false);
                                                           28 #define ff first
95
     find_level_peso();
                                                           29 #define ss second
96
                                                           30 #define ll long long
     for (int j = 1; j \le BITS; j++) {
98
                                                           31
       for (int i = 1; i <= n; i++) {
                                                           32 using namespace std;
         if (up[i][j - 1] != -1) up[i][j] = up[up[i][j - 33
100
                                                           34 const 11 INF = 1e18+10;
        1]][i - 1]:
       }
101
     }
                                                            36 struct Edge {
102
103 }
                                                                  int from;
                                                           38
                                                                  int to:
  6.8 Bellman Ford
                                                                  11 capacity;
                                                           39
                                                                  11 flow;
                                                           40
                                                                  Edge* residual;
                                                            41
 1 struct edge
                                                            42
                                                                  Edge() {}
                                                           43
       int a, b, cost;
 4 }:
                                                                  Edge(int from, int to, 11 capacity) : from(from),
                                                           45
                                                                   to(to), capacity(capacity) {
 6 int n, m, v;
                                                                      flow = 0;
                                                            46
 7 vector < edge > e;
                                                           47
 8 const int INF = 1000000000;
                                                                  11 get_capacity() {
                                                           49
10 void solve()
                                                                       return capacity - flow;
                                                            50
11 {
                                                           51
       vector<int> d (n, INF);
12
                                                           52
       d[v] = 0;
13
                                                                  11 get_flow() {
                                                            53
       for (int i=0; i<n-1; ++i)
                                                                      return flow:
                                                           54
           for (int j=0; j < m; ++j)
15
                if (d[e[j].a] < INF)
16
                    d[e[j].b] = min (d[e[j].b], d[e[j].a] 57
                                                                   void augment(ll bottleneck) {
        + e[j].cost);
                                                                       flow += bottleneck;
18 }
                                                                       residual ->flow -= bottleneck;
                                                            59
   6.9 Dinic
                                                            61
                                                                  void reverse(ll bottleneck) {
                                                            62
                                                                      flow -= bottleneck;
 1 // Description:
                                                                       residual ->flow += bottleneck;
 _{2} // Obtains the maximum possible flow rate given a
                                                            64
       network. A network is a graph with a single
       source vertex and a single sink vertex in which
                                                           66
                                                                  bool operator < (const Edge& e) const {</pre>
                                                            67
       each edge has a capacity
                                                            68
                                                                      return true;
 4 // Problem:
                                                            69
                                                            70 };
 5 // https://codeforces.com/gym/103708/problem/J
                                                            71
                                                            72 struct Dinic {
 7 // Complexity:
                                                                 int source;
 _{8} // O(V^2 * E) where V is the number of vertex and E
                                                           73
                                                            74
                                                                  int sink;
       is the number of edges
                                                                  int nodes:
                                                            75
                                                                  11 flow;
10 // Unit network
                                                            76
11 // A unit network is a network in which for any
                                                                  vector < Edge *>> adj;
                                                                  vector < int > level;
       vertex except source and sink either incoming or
                                                           78
                                                                  vector < int > next;
       outgoing edge is unique and has unit capacity (
                                                            79
                                                                  vector < int > reach;
                                                            80
       matching problem).
                                                                  vector < bool > visited;
                                                            81
12 // Complexity on unit networks: O(E * sqrt(V))
                                                                  vector < vector < int >> path;
                                                            82
14 // Unity capacity networks
                                                            83
                                                                  Dinic(int source, int sink, int nodes) : source(
                                                            84
_{15} // A more generic settings when all edges have unit
                                                                  source), sink(sink), nodes(nodes) {
       capacities, but the number of incoming and
                                                                      adj.resize(nodes + 1);
       outgoing edges is unbounded
16 // Complexity on unity capacity networks: O(E * sqrt(86
       E))
                                                            87
                                                                  void add_edge(int from, int to, ll capacity) {
                                                                       Edge* e1 = new Edge(from, to, capacity);
18 // How to use:
                                                            89
19 // Dinic dinic = Dinic(num_vertex, source, sink);
                                                                       Edge* e2 = new Edge(to, from, 0);
                                                           90
                                                                       // Edge* e2 = new Edge(to, from, capacity);
20 // dinic.add_edge(vertex1, vertex2, capacity);
                                                           91
                                                                       e1->residual = e2;
                                                            92
21 // cout << dinic.max_flow() << '\n';</pre>
                                                                       e2->residual = e1;
                                                            93
                                                                       adj[from].pb(e1);
23 #include <bits/stdc++.h>
                                                           94
                                                                       adj[to].pb(e2);
                                                            96
                                                                  }
25 #define pb push_back
```

```
void print_min_cut() {
97
                                                               165
98
        bool bfs() {
                                                               166
                                                                           reach.clear();
            level.assign(nodes + 1, -1);
                                                                           visited.assign(nodes + 1, false);
99
                                                               167
            queue <int > q;
                                                               168
                                                                           reach.pb(source);
100
            q.push(source);
                                                               169
                                                                           reachable (source);
            level[source] = 0;
102
                                                              170
                                                                           for (auto v : reach) {
103
            while (!q.empty()) {
                                                                               for (auto e : adj[v]) {
104
                                                               172
                                                                                    if (!visited[e->to] && e->
                 int node = q.front();
105
                                                               173
                                                                      get_capacity() == 0) {
                 q.pop();
106
                                                                                        cout << e->from << ' ' ' << e->to
107
                                                               174
108
                 for (auto e : adj[node]) {
                                                                       << '\n';
                     if (level[e->to] == -1 && e->
                                                                                    }
109
                                                                               }
        get_capacity() > 0) {
                                                               176
                          level[e->to] = level[e->from] +
                                                                           }
110
                                                               177
        1;
                                                               178
                         q.push(e->to);
                                                               179
                     }
                                                                      ll build_path(int v, int id, ll flow) {
112
                                                               180
113
                 }
                                                                           visited[v] = true;
            }
                                                                           if (v == sink) {
114
                                                               182
                                                                               return flow;
115
                                                               183
                                                                           }
            return level[sink] != -1;
116
                                                               184
117
                                                               185
                                                                           for (auto e : adj[v]) {
        11 dfs(int v, 11 flow) {
                                                                               if (!visited[e->to] && e->get_flow() > 0)
119
                                                               187
            if (v == sink)
                                                                        ₹
120
                 return flow;
                                                                                    visited[e->to] = true;
121
                                                               188
                                                                                    11 bottleneck = build_path(e->to, id,
122
                                                               189
            int sz = adj[v].size();
                                                                        min(flow, e->get_flow()));
123
            for (int i = next[v]; i < sz; i++) {</pre>
                                                                                    if (bottleneck > 0) {
124
                                                              190
                 Edge* e = adj[v][i];
                                                                                        path[id].pb(e->to);
125
                 if (level[e->to] == level[e->from] + 1 &&192
                                                                                        e->reverse(bottleneck);
126
         e->get_capacity() > 0) {
                                                                                        return bottleneck;
                     ll bottleneck = dfs(e->to, min(flow, 194
                                                                                    }
                                                                               }
        e->get_capacity()));
                                                               195
                     if (bottleneck > 0) {
                                                                           }
                          e->augment(bottleneck);
129
                                                              197
                          return bottleneck;
                                                               198
                                                                           return 0;
130
                     }
                                                                      }
131
                                                               199
                }
                                                               200
132
133
                                                               201
                                                                       void print_flow_path() {
                 next[v] = i + 1;
                                                                           path.clear();
134
                                                              202
            }
                                                                           11 \text{ sent} = -1;
135
                                                              203
                                                                           int id = -1;
136
                                                              204
            return 0;
                                                                           while (sent != 0) {
                                                              205
137
        }
                                                                                visited.assign(nodes + 1, false);
138
                                                               206
                                                                               path.pb(vector<int>{});
139
                                                              207
140
        11 max_flow() {
                                                                               sent = build_path(source, ++id, INF);
            flow = 0;
                                                                               path[id].pb(source);
141
                                                              209
            while(bfs()) {
                                                                           }
142
                                                              210
                 next.assign(nodes + 1, 0);
                                                              211
                                                                           path.pop_back();
143
                 11 \text{ sent} = -1;
144
                                                              212
                 while (sent != 0) {
                                                                           for (int i = 0; i < id; i++) {
                                                              213
                     sent = dfs(source, INF);
                                                                               cout << path[i].size() << '\n';</pre>
146
                                                              214
147
                     flow += sent;
                                                              215
                                                                                reverse(path[i].begin(), path[i].end());
                }
148
                                                              216
                                                                               for (auto e : path[i]) {
            }
                                                                                    cout << e << '';
149
                                                              217
                                                                               7
            return flow;
                                                              218
150
151
        }
                                                              219
                                                                               cout << '\n';
                                                                           }
152
                                                               220
        void reachable(int v) {
                                                                      }
153
                                                              221
            visited[v] = true;
                                                              222 };
154
155
                                                               223
            for (auto e : adi[v]) {
                                                              224 int main() {
156
157
                 if (!visited[e->to] && e->get_capacity() 225
                                                                       ios::sync_with_stdio(false);
        > 0) {
                                                                      cin.tie(NULL):
                                                              226
                     reach.pb(e->to);
                                                              227
158
                     visited[e->to] = true;
                                                              228
                                                                      int n, m; cin >> n >> m;
159
                     reachable(e->to);
                                                              229
160
                 }
                                                                      Dinic dinic = Dinic(1, n, n);
161
                                                               230
            }
162
                                                              231
                                                                       for (int i = 1; i <= m; i++) {
        }
163
                                                               232
164
                                                               233
                                                                           int v, u; cin >> v >> u;
```

```
dinic.add_edge(v, u, 1);
                                                                         add_or(get_not(a), b);
234
                                                             60
235
                                                             61
                                                                         add_or(a, get_not(b));
                                                                         add_or(a, b);
236
                                                             62
       cout << dinic.max_flow() << '\n';</pre>
237
                                                             63
       // dinic.print_min_cut();
                                                             64
       // dinic.print_flow_path();
                                                                    void add_nand(int a, int b) {
                                                             65
239
                                                                         add_or(get_not(a), b);
       return 0;
                                                                         add_or(a, get_not(b));
241
                                                             67
242 }
                                                                         add_or(get_not(a), get_not(b));
                                                             68
                                                             69
   6.10 2sat
                                                             70
                                                             71
                                                                    void add_xor(int a, int b) {
                                                                        add_or(a, b);
 1 // Description:
                                                             72
                                                                         add_or(get_not(a), get_not(b));
 _{2} // Solves expression of the type (a v b) ^ (c v d) ^
                                                             73
       (e v f)
                                                             74
                                                             75
 4 // Problem:
                                                                     void add_xnor(int a, int b) {
                                                                         add_or(get_not(a), b);
 5 // https://cses.fi/problemset/task/1684
                                                             77
                                                                         add_or(a, get_not(b));
 7 // Complexity:
                                                             79
 _8 // O(n + m) where n is the number of variables and m _{\rm 80}
                                                                     void departure_time(int v) {
       is the number of clauses
                                                                         visited[v] = true;
                                                             82
10 #include <bits/stdc++.h>
                                                                         for (auto u : adj[v]) {
11 #define pb push_back
                                                             84
12 #define mp make_pair
                                                                             if (!visited[u]) departure_time(u);
                                                             85
13 #define pii pair <int, int>
                                                             86
14 #define ff first
                                                             87
                                                             88
                                                                         departure.pb(mp(++curr, v));
15 #define ss second
                                                                    }
                                                             89
                                                             90
17 using namespace std;
                                                                     void find_component(int v, int component) {
                                                             91
18
                                                                         scc[v] = component;
                                                             92
19 struct SAT {
      int nodes;
                                                             93
                                                                         visited[v] = true;
20
       int curr = 0;
                                                             94
                                                                         for (auto u : rev[v]) {
       int component = 0;
                                                             95
22
                                                                             if (!visited[u]) find_component(u,
       vector < vector < int >> adj;
                                                             96
23
       vector < vector < int >> rev;
                                                                    component);
24
       vector < vector < int >> condensed;
                                                             97
                                                                         }
25
                                                             98
       vector <pii > departure;
       vector < bool > visited;
                                                             99
27
                                                                     void topological_order(int v) {
       vector < int > scc;
                                                             100
                                                                         visited[v] = true;
       vector<int> order;
                                                            101
29
                                                            102
30
                                                                         for (auto u : condensed[v]) {
                                                             103
31
       // 1 to nodes
                                                                             if (!visited[u]) topological_order(u);
       // nodes + 1 to 2 * nodes
                                                             104
32
33
       SAT(int nodes) : nodes(nodes) {
                                                            105
           adj.resize(2 * nodes + 1);
34
                                                                         order.pb(v);
35
           rev.resize(2 * nodes + 1);
                                                            107
                                                             108
            visited.resize(2 * nodes + 1);
36
            scc.resize(2 * nodes + 1);
                                                             109
37
                                                                    bool is_possible() {
                                                            110
                                                                         component = 0;
                                                            111
39
                                                                         for (int i = 1; i <= 2 * nodes; i++) {
       void add_imp(int a, int b) {
                                                            112
40
                                                             113
                                                                             if (!visited[i]) departure_time(i);
            adj[a].pb(b);
41
                                                             114
            rev[b].pb(a);
42
       }
                                                            115
43
                                                                         sort(departure.begin(), departure.end(),
                                                             116
44
       int get_not(int a) {
                                                                    greater < pii > () );
                                                             117
46
            if (a > nodes) return a - nodes;
                                                                         visited.assign(2 * nodes + 1, false);
                                                             118
            return a + nodes;
47
                                                            119
48
                                                                         for (auto [_, node] : departure) {
                                                             120
49
                                                                             if (!visited[node]) find_component(node,
50
       void add_or(int a, int b) {
                                                            121
                                                                     ++component);
            add_imp(get_not(a), b);
51
                                                                        }
                                                            122
52
            add_imp(get_not(b), a);
                                                            123
53
                                                                         for (int i = 1; i <= nodes; i++) {</pre>
54
                                                             124
                                                                             if (scc[i] == scc[i + nodes]) return
                                                            125
       void add_nor(int a, int b) {
55
                                                                    false;
           add_or(get_not(a), get_not(b));
56
                                                             126
                                                             127
58
                                                                         return true;
       void add_and(int a, int b) {
                                                             128
59
```

```
}
                                                                          for (int i = 1; i <= m; i++) {
129
                                                              194
                                                                              cout << (ans[i] == 1 ? '+' : '-') << ' ';</pre>
130
       int find_value(int e, vector<int> &ans) {
131
                                                             196
           if (e > nodes && ans[e - nodes] != 2) return 197
                                                                          cout << '\n';
132
        !ans[e - nodes];
            if (e <= nodes && ans[e + nodes] != 2) return199
133
         !ans[e + nodes];
                                                                     return 0;
            return 0:
                                                             201 }
134
135
                                                                 6.11 Find Cycle
136
       vector < int > find_ans() {
137
            condensed.resize(component + 1);
                                                               1 bitset < MAX > visited;
139
                                                               vector <int > path;
            for (int i = 1; i <= 2 * nodes; i++) {
140
                                                               3 vector <int > adj[MAX];
                for (auto u : adj[i]) {
141
                     if (scc[i] != scc[u]) condensed[scc[i 4
142
                                                               5 bool dfs(int u. int p){
       ]].pb(scc[u]);
143
                                                                     if (visited[u]) return false;
            }
145
                                                                     path.pb(u);
            visited.assign(component + 1, false);
146
                                                                     visited[u] = true;
                                                              10
147
                                                              11
            for (int i = 1; i <= component; i++) {
148
                                                                     for (auto v : adj[u]){
                                                              12
                if (!visited[i]) topological_order(i);
                                                                          if (visited[v] and u != v and p != v){
                                                              13
150
                                                              14
                                                                              path.pb(v); return true;
151
            reverse(order.begin(), order.end());
152
                                                              16
                                                                          if (dfs(v, u)) return true;
                                                              17
            // 0 - false
                                                              18
            // 1 - true
155
                                                              19
            // 2 - no value yet
156
                                                              20
                                                                     path.pop_back();
            vector < int > ans(2 * nodes + 1, 2);
157
                                                              21
                                                                     return false;
158
                                                              22 }
            vector < vector < int >> belong (component + 1);
160
                                                              24 bool has_cycle(int N){
            for (int i = 1; i <= 2 * nodes; i++) {
161
                                                              25
                belong[scc[i]].pb(i);
162
                                                              26
                                                                     visited.reset();
163
                                                              27
164
                                                              28
                                                                     for (int u = 1; u \le N; ++u){
            for (auto p : order) {
165
                                                                          path.clear();
                                                              29
166
                for (auto e : belong[p]) {
                                                                          if (not visited[u] and dfs(u,-1))
                     ans[e] = find_value(e, ans);
167
                                                                              return true;
                                                              31
168
                                                              32
169
            7
                                                              33
170
                                                              34
            return ans;
171
                                                                     return false;
                                                              35
       }
172
                                                              36 }
173 }:
174
                                                                 6.12 Cycle Path Recovery
175 int main() {
       ios::sync_with_stdio(false);
176
       cin.tie(NULL);
177
                                                               1 int n;
                                                               vector < vector < int >> adj;
       int n, m; cin >> n >> m;
179
                                                               3 vector < char > color;
180
                                                               4 vector <int> parent;
       SAT sat = SAT(m);
181
                                                               5 int cycle_start, cycle_end;
182
        for (int i = 0; i < n; i++) {
183
                                                               7 bool dfs(int v) {
            char op1, op2; int a, b; cin >> op1 >> a >>
184
                                                                     color[v] = 1;
       op2 >> b;
                                                                     for (int u : adj[v]) {
            if (op1 == '+' && op2 == '+') sat.add_or(a, b<sub>10</sub>
185
                                                                          if (color[u] == 0) {
                                                                              parent[u] = v;
            if (op1 == '-' && op2 == '-') sat.add_or(sat.<sub>12</sub>
                                                                              if (dfs(u))
       get_not(a), sat.get_not(b));
    if (op1 == '+' && op2 == '-') sat.add_or(a,
                                                                                  return true;
                                                                          } else if (color[u] == 1) {
        sat.get_not(b));
                                                                              cycle_end = v;
           if (op1 == '-' && op2 == '+') sat.add_or(sat.<sub>16</sub>
                                                                              cycle_start = u;
188
        get_not(a), b);
                                                              17
                                                                              return true;
189
                                                                          }
                                                                     }
                                                              19
       if (!sat.is_possible()) cout << "IMPOSSIBLE\n";</pre>
191
                                                                     color[v] = 2;
                                                              20
192
                                                              21
                                                                     return false;
            vector < int > ans = sat.find_ans();
193
                                                              22 }
```

```
removed[center] = true;
                                                           43
24 void find_cycle() {
                                                           44
                                                                 for (auto u : adj[center]) {
      color.assign(n, 0);
25
                                                           45
      parent.assign(n, -1);
                                                                      if (!removed[u]) {
26
                                                          46
                                                                          char next = get_next(c);
      cycle_start = -1;
                                                           47
                                                                          if (next == '$') {
28
                                                           48
      for (int v = 0; v < n; v++) {
                                                                              flag = false;
          if (color[v] == 0 && dfs(v))
30
                                                           50
                                                                              return:
              break:
31
                                                           51
                                                                          solve(u, next);
32
                                                           52
                                                                      }
33
                                                           53
34
      if (cycle_start == -1) {
                                                           54
                                                                 }
          cout << "Acyclic" << endl;</pre>
                                                          55 }
35
      } else {
36
                                                          56
37
          vector < int > cycle;
                                                          57 int32_t main(){
                                                                 ios::sync_with_stdio(false);
          cycle.push_back(cycle_start);
38
                                                          58
          for (int v = cycle_end; v != cycle_start; v = 59
                                                                 cin.tie(NULL);
        parent[v])
                                                          60
              cycle.push_back(v);
                                                                 cin >> n;
          cycle.push_back(cycle_start);
                                                                 adj.resize(n + 1);
41
                                                          62
          reverse(cycle.begin(), cycle.end());
                                                                 ans.resize(n + 1);
                                                          63
42
                                                          64
                                                                 removed.resize(n + 1);
                                                                 subtree_size.resize(n + 1);
          cout << "Cycle found: ";</pre>
                                                          65
44
          for (int v : cycle)
                                                          66
             cout << v << " ";
                                                                 for (int i = 1; i \le n - 1; i++) {
46
                                                           67
                                                                      int u, v; cin >> u >> v;
           cout << endl;</pre>
                                                           68
47
                                                                      adj[u].insert(v);
48
                                                           69
49 }
                                                                      adj[v].insert(u);
                                                           70
                                                           71
         Centroid Decomposition
  6.13
                                                           72
                                                                 solve(1, 'A');
                                                           73
                                                           74
1 int n;
                                                           75
                                                                 if (!flag) cout << "Impossible!\n";</pre>
vector < set < int >> adj;
3 vector < char > ans;
                                                           76
                                                                      for (int i = 1; i \le n; i++) {
                                                           77
                                                                          cout << ans[i] << '';</pre>
5 vector < bool > removed;
                                                           79
                                                           80
                                                                      cout << '\n';
7 vector<int> subtree_size;
                                                                 }
                                                           81
                                                           82
9 int dfs(int u, int p = 0) {
   subtree_size[u] = 1;
                                                           83
                                                                  return 0;
10
                                                           84 }
    for(int v : adj[u]) {
12
                                                                     Tarjan Bridge
                                                             6.14
     if(v != p && !removed[v]) {
13
        subtree_size[u] += dfs(v, u);
          }
                                                           1 // Description:
15
16
                                                           2 // Find a bridge in a connected unidirected graph
                                                           _{\rm 3} // A bridge is an edge so that if you remove that
17
18
    return subtree_size[u];
                                                                 edge the graph is no longer connected
19 }
                                                           5 // Problem:
20
21 int get_centroid(int u, int sz, int p = 0) {
                                                           6 // https://cses.fi/problemset/task/2177/
   for(int v : adj[u]) {
                                                           8 // Complexity:
      if(v != p && !removed[v]) {
                                                           _{9} // O(V + E) where V is the number of vertices and E
        if(subtree_size[v]*2 > sz) {
24
25
          return get_centroid(v, sz, u);
                                                                 is the number of edges
               }
26
                                                           11 int n:
27
      }
                                                           12 vector < vector < int >> adj;
29
                                                          13
    return u;
                                                           14 vector < bool > visited;
30
31 }
                                                           15 vector <int> tin, low;
                                                          16 int timer;
33 char get_next(char c) {
                                                          17
     if (c != 'Z') return c + 1;
                                                          18 void dfs(int v, int p) {
34
      return '$';
                                                                 visited[v] = true;
35
                                                          19
36 }
                                                                 tin[v] = low[v] = timer++;
                                                          20
                                                                 for (int to : adj[v]) {
                                                           21
38 bool flag = true;
                                                                     if (to == p) continue;
                                                           22
                                                                     if (visited[to]) {
                                                           23
40 void solve(int node, char c) {
                                                                          low[v] = min(low[v], tin[to]);
int center = get_centroid(node, dfs(node));
                                                                      } else {
                                                          25
     ans[center] = c;
                                                                          dfs(to, v);
                                                           26
```

```
low[v] = min(low[v], low[to]);
                                                                   head.resize(n):
27
                                                            49
               if (low[to] > tin[v]) {
                                                            50
                                                                   subtree_size.assign(n, 1);
28
                    IS_BRIDGE(v, to);
                                                                   level.assign(n, 0);
29
                                                            51
                                                            52
                                                                   heavy_child.assign(n, -1);
30
           }
                                                            53
                                                                   parent[root] = -1;
       }
                                                                   dfs(root, -1);
32
                                                            54
33 }
                                                                   decompose(root, -1);
                                                            55
34
                                                            56
35 void find_bridges() {
                                                            57
       timer = 0;
                                                                 void dfs(int v, int p) {
                                                            58
       visited.assign(n, false);
                                                                   parent[v] = p;
37
                                                            59
                                                                   if (p != -1) level[v] = level[p] + 1;
       tin.assign(n, -1);
                                                            60
       low.assign(n, -1);
                                                                   for (auto u : adj[v]) {
39
                                                            61
       for (int i = 0; i < n; ++i) {
                                                                     if (u != p) {
                                                            62
40
           if (!visited[i])
41
                                                            63
                                                                       dfs(u, v);
                                                                        subtree_size[v] += subtree_size[u];
               dfs(i, -1);
42
                                                            64
                                                                        if (heavy_child[v] == -1 || subtree_size[u] >
43
44 }
                                                                    subtree_size[heavy_child[v]]) heavy_child[v] = u
          Hld Vertex
  6.15
                                                                     }
                                                            66
                                                                   }
                                                            67
                                                                 }
1 // Description:
_{\rm 2} // Make queries and updates between two vertexes on a ^{69}
                                                                 void decompose(int v, int chead) {
       tree
                                                                  // start a new path
3 // Query path - query path (a, b) inclusive
                                                            71
                                                            72
                                                                   if (chead == -1) chead = v;
_{4} // Update path - update path (a, b) inclusive
_{5} // Query subtree - query subtree of a
                                                            73
6 // Update subtree - update subtree of a
                                                                   // consecutive ids in the hld path
                                                            74
7 // Update - update vertex or edge
                                                                   at[cpos] = v;
                                                            75
                                                                   pos[v] = cpos++;
_{\rm 8} // Lca - get lowest common ancestor of a and b
                                                            76
                                                                   head[v] = chead;
_{\rm 9} // Search - perform a binary search to find the last ^{77}
      node with a certain property
                                                            78
                                                                   // if not a leaf
                                                            79
_{10} // on the path from a to the root
                                                                   if (heavy_child[v] != -1) decompose(heavy_child[v
11
                                                                   ], chead);
12 // Problem:
13 // https://codeforces.com/gym/101908/problem/L
                                                                   // light child
                                                            82
15 // Complexity:
                                                                   for (auto u : adj[v]){
                                                            83
                                                                     // start new path
16 // O(log ^2 n) for both query and update
                                                            84
                                                                     if (u != parent[v] && u != heavy_child[v])
                                                            85
                                                                   decompose(u, -1);
18 // How to use:
_{19} // HLD hld = HLD(n + 1, adj)
                                                            86
                                                            87
21 // Notes
                                                            88
                                                                 11 query_path(int a, int b) {
_{
m 22} // Change the root of the tree on the constructor if ^{
m 89}
                                                                   if(pos[a] < pos[b]) swap(a, b);</pre>
      it's different from 1
23 // Use together with Segtree
                                                            91
                                                                   if(head[a] == head[b]) return seg.query(pos[b],
24
25 struct HLD {
                                                                   pos[a]);
                                                                   return seg.f(seg.query(pos[head[a]], pos[a]),
    vector < int > parent;
                                                            93
    vector <int > pos;
                                                                   query_path(parent[head[a]], b));
27
    vector <int> head;
                                                            94
    vector < int > subtree_size;
29
                                                                 ftype query_subtree(int a) {
    vector < int > level;
                                                            96
                                                                   return seg.query(pos[a], pos[a] + subtree_size[a]
    vector < int > heavy_child;
                                                            97
31
                                                                     - 1);
    vector < ftype > subtree_weight;
32
                                                            98
    vector < ftype > path_weight;
33
    vector < vector < int >> adj;
                                                            99
34
    vector <int > at;
                                                            100
                                                                 void update_path(int a, int b, int x) {
                                                                   if(pos[a] < pos[b]) swap(a, b);</pre>
                                                            101
36
    Segtree seg = Segtree(0);
                                                            102
    int cpos;
37
                                                                   if(head[a] == head[b]) return (void)seg.update(
                                                            103
38
    int n;
                                                                   pos[b], pos[a], x);
    int root;
39
                                                                   seg.update(pos[head[a]], pos[a], x); update_path(
40
                                                            104
                                                                   parent[head[a]], b, x);
    HLD() {}
41
                                                            105
43
    HLD(int n, vector < vector < int >> & adj, int root = 1) 106
      : adj(adj), n(n), root(root) {
                                                                 void update_subtree(int a, int val) {
                                                            107
                                                                   seg.update(pos[a], pos[a] + subtree_size[a] - 1,
                                                            108
       seg = Segtree(n);
44
                                                                   val);
       cpos = 0;
45
       at.resize(n);
                                                            109
       parent.resize(n);
                                                            110
47
                                                                 void update(int a, int val) {
       pos.resize(n);
                                                            111
48
```

```
seg.update(pos[a], pos[a], val);
112
                                                            31
113
     }
                                                            32
                                                            33 int32_t main() {
114
115
     //edge
                                                            34
     void update(int a, int b, int val) {
                                                                 int n; cin >> n;
       if (level[a] > level[b]) swap(a, b);
117
                                                            36
       update(b, val);
                                                                 for (int i = 1; i \le n; i++) {
118
                                                            37
                                                                   int a; cin >> a;
119
                                                            38
                                                                   colors[i][a] = 1;
120
                                                            39
     int lca(int a, int b) {
                                                                       vmax[i] = 1;
121
       if(pos[a] < pos[b]) swap(a, b);
                                                                       sum_num[i] = a;
122
                                                            41
123
       return head[a] == head[b] ? b : lca(parent[head[a 42]
       ]], b);
                                                                 for (int i = 1; i < n; i++) {
124
                                                            44
125
                                                            45
                                                                   int a, b; cin >> a >> b;
     void search(int a) {
126
                                                            46
127
       a = parent[a];
                                                            47
                                                                   adj[a].push_back(b);
       if (a == -1) return;
                                                                   adj[b].push_back(a);
128
                                                            48
       if (seg.query(pos[head[a]], pos[head[a]]+
129
       {\tt subtree\_size[head[a]]-1) + pos[a]-pos[head[a]]+1 \ 50}
       == subtree_size[head[a]]) {
                                                                 process_colors(1, 0);
                                                            51
         seg.update(pos[head[a]], pos[a], 1);
                                                            52
         return search(parent[head[a]]);
                                                            53
                                                                 for (int i = 1; i \le n; i++) {
131
                                                                   cout << sum_num[i] << (i < n ? " " : "\n");</pre>
132
       int l = pos[head[a]], r = pos[a]+1;
                                                            55
133
       while (1 < r) {
134
                                                            56
         int m = (1+r)/2;
135
                                                            57
                                                                   return 0;
         if (seg.query(m, m+subtree_size[at[m]]-1) + pos 58
136
       [a]-m+1 == subtree_size[at[m]]) {
           r = m;
137
138
                                                               6.17
                                                                       Tree Diameter
         else l = m+1;
139
140
141
       seg.update(1, pos[a], 1);
                                                             1 #include <bits/stdc++.h>
142
                                                             2
143 };
                                                             3 using namespace std;
         Small To Large
   6.16
                                                             5 const int MAX = 3e5+17;
                                                             7 vector < int > adj[MAX];
 1 // Problem:
 2 // https://codeforces.com/contest/600/problem/E
                                                             8 bool visited[MAX];
                                                            10 int max_depth = 0, max_node = 1;
 4 void process_colors(int curr, int parent) {
                                                            11
                                                            12 void dfs (int v, int depth) {
     for (int n : adj[curr]) {
                                                                   visited[v] = true;
       if (n != parent) {
                                                            13
         process_colors(n, curr);
                                                            14
                                                                   if (depth > max_depth) {
 9
                                                            15
10
               if (colors[curr].size() < colors[n].size 16</pre>
                                                                       max_depth = depth;
                                                                       max_node = v;
       ()) {
                                                            17
                    sum_num[curr] = sum_num[n];
                                                            18
11
                    vmax[curr] = vmax[n];
                                                            19
12
           swap(colors[curr], colors[n]);
                                                                   for (auto u : adj[v]) {
13
                                                            20
                                                                       if (!visited[u]) dfs(u, depth + 1);
14
                                                            21
                                                            22
15
         for (auto [item, vzs] : colors[n]) {
                                                            23 }
16
                    if(colors[curr][item]+vzs > vmax[curr 24
                                                            25 int tree_diameter() {
       ]){
                        vmax[curr] = colors[curr][item] + 26
                                                                   dfs(1, 0);
                                                                   max_depth = 0;
        vzs:
                                                            27
                                                                   for (int i = 0; i < MAX; i++) visited[i] = false;</pre>
                        sum_num[curr] = item;
                                                            28
19
                                                                   dfs(max_node, 0);
                    }
20
                                                            29
                                                                   return max_depth;
                    else if(colors[curr][item]+vzs ==
21
       vmax[curr]){
                                                            31 }
                        sum_num[curr] += item;
22
                                                               6.18 Dijkstra
23
24
                    colors[curr][item] += vzs;
                                                             1 const int MAX = 2e5+7;
25
                                                             2 const int INF = 1000000000;
                                                             3 vector < vector < pair < int , int >>> adj(MAX);
       }
27
     }
                                                             5 void dijkstra(int s, vector<int> & d, vector<int> & p
29
30 }
```

```
int n = adj.size();
                                                                  int n:
                                                            2
      d.assign(n, INF);
                                                            3
                                                                   vector < int > link, sizes;
      p.assign(n, -1);
                                                            4
                                                            5
                                                                   DSU(int n) {
                                                                       this ->n = n;
      d[s] = 0;
       set < pair < int , int >> q;
                                                                       link.assign(n+1, 0);
                                                            7
11
       q.insert({0, s});
                                                                       sizes.assign(n+1, 1);
12
                                                            8
       while (!q.empty()) {
13
                                                            9
          int v = q.begin()->second;
                                                                       for (int i = 0; i \le n; i++)
14
                                                            10
           q.erase(q.begin());
                                                            11
                                                                           link[i] = i;
                                                                   }
16
                                                            12
           for (auto edge : adj[v]) {
                                                            13
               int to = edge.first;
                                                                   int find(int x) {
18
                                                            14
               int len = edge.second;
                                                                       while (x != link[x])
                                                           15
                                                                           x = link[x];
20
                                                           16
               if (d[v] + len < d[to]) {
21
                                                            17
22
                    q.erase({d[to], to});
                                                            18
                                                                       return x;
                   d[to] = d[v] + len;
23
                                                           19
                    p[to] = v;
                                                            20
                                                                   bool same(int a, int b) {
                    q.insert({d[to], to});
25
                                                            21
               }
                                                                       return find(a) == find(b);
                                                            22
26
           }
                                                            23
27
      }
28
                                                            24
29 }
                                                                   void unite(int a, int b) {
                                                                       a = find(a);
30
                                                            26
31 vector<int> restore_path(int s, int t) {
                                                            27
                                                                       b = find(b);
      vector < int > path;
32
                                                            28
                                                                       if (a == b) return;
33
                                                            29
       for (int v = t; v != s; v = p[v])
34
                                                            30
        path.push_back(v);
                                                                       if (sizes[a] < sizes[b])</pre>
35
                                                            31
      path.push_back(s);
                                                                           swap(a, b);
36
                                                            32
37
                                                            33
      reverse(path.begin(), path.end());
                                                                       sizes[a] += sizes[b];
                                                            34
38
39
      return path;
                                                            35
                                                                       link[b] = a;
40 }
                                                            36
                                                            37 };
42 int adj[MAX][MAX];
43 int dist[MAX];
                                                            39 struct Edge {
44 int minDistance(int dist[], bool sptSet[], int V) { 40
                                                                  int u, v;
      int min = INT_MAX, min_index;
                                                                   long long weight;
45
                                                            41
46
       for (int v = 0; v < V; v++)
                                                                   Edge() {}
47
                                                            43
           if (sptSet[v] == false && dist[v] <= min)</pre>
                                                            44
48
10
               min = dist[v], min_index = v;
                                                            45
                                                                   Edge(int u, int v, long long weight) : u(u), v(v)
                                                                   , weight(weight) {}
50
51
       return min_index;
                                                            46
52 }
                                                                   bool operator < (const Edge & other) const {</pre>
                                                            47
                                                                       return weight < other.weight;</pre>
54 void dijkstra(int src, int V) {
                                                            49
55
                                                            50
       bool sptSet[V];
                                                            51
                                                                   bool operator > (const Edge & other) const {
56
       for (int i = 0; i < V; i++)
                                                                       return weight > other.weight;
57
                                                            52
           dist[i] = INT_MAX, sptSet[i] = false;
                                                            53
                                                            54 };
59
       dist[src] = 0;
60
                                                            56 vector < Edge > kruskal (vector < Edge > edges, int n) {
61
       for (int count = 0; count < V - 1; count++) {</pre>
                                                                   vector < Edge > result; // arestas da MST
                                                            57
62
           int u = minDistance(dist, sptSet, V);
                                                            58
                                                                   long long cost = 0;
64
                                                            59
           sptSet[u] = true;
                                                                   sort(edges.begin(), edges.end());
65
                                                            60
66
                                                            61
                                                                   DSU dsu(n);
                                                            62
           for (int v = 0; v < V; v++)
                                                            63
               if (!sptSet[v] && adj[u][v]
                                                                   for (auto e : edges) {
69
                                                            64
70
                    && dist[u] != INT_MAX
                                                                       if (!dsu.same(e.u, e.v)) {
                                                                           cost += e.weight;
                    && dist[u] + adj[u][v] < dist[v])
71
                                                            66
                    dist[v] = dist[u] + adj[u][v];
                                                                           result.push_back(e);
72
                                                            67
       }
                                                                           dsu.unite(e.u, e.v);
73
                                                            68
                                                                       }
                                                            69
                                                                   }
                                                            70
          Kruskall
  6.19
                                                            71
                                                            72
                                                                   return result;
                                                            73 }
1 struct DSU {
```

7 Geometry

```
63 }
  7.1 2d
                                                          64 ld order_angle(point a, point b){ // from a to b ccw
                                                                (a in front of b)
                                                                 ld aux = angle(a,b)*180/PI;
1 #define vp vector<point>
                                                          65
                                                                 return ((a^b) <= 0 ? aux:360-aux);
_{\rm 2} #define ld long double
                                                          67 }
3 const ld EPS = 1e-6;
4 const ld PI = acos(-1);
                                                          68 bool angle_less(point a1, point b1, point a2, point
                                                                 b2) { // ang(a1,b1) <= ang(a2,b2)
                                                                 point p1((a1*b1), abs((a1^b1)));
6 // typedef ll cod;
                                                          69
7 // bool eq(cod a, cod b){ return (a==b); }
                                                          70
                                                                 point p2((a2*b2), abs((a2^b2)));
                                                                 return (p1^p2) <= 0;
8 typedef ld cod;
                                                          71
                                                          72 }
9 bool eq(cod a, cod b){ return abs(a - b) <= EPS; }</pre>
10
                                                          74 ld area(vp &p){ // (points sorted)
11 struct point{
      cod x, y;
                                                          75
                                                                ld ret = 0;
12
                                                                 for(int i=2;i<(int)p.size();i++)</pre>
      int id;
                                                          76
13
      point(cod x=0, cod y=0): x(x), y(y){}
                                                                  ret += (p[i]-p[0])^(p[i-1]-p[0]);
14
                                                                 return abs(ret/2);
                                                          78
      point operator+(const point &o) const{ return {x+79 }
                                                          80 ld areaT(point &a, point &b, point &c){
      o.x, y+o.y}; }
                                                                return abs((b-a)^(c-a))/2.0;
      point operator-(const point &o) const{ return {x-81
      o.x, y-o.y; }
      point operator*(cod t) const{ return {x*t, y*t}; 83
                                                          84 point center(vp &A){
      point operator/(cod t) const{ return {x/t, y/t}; 85
                                                                point c = point();
19
                                                                int len = A.size();
                                                                for(int i=0;i<len;i++)</pre>
      cod operator*(const point &o) const{ return x * o 87
20
                                                                   c=c+A[i]:
      .x + y * o.y; }
                                                          88
                                                                 return c/len;
      cod operator^(const point &o) const{ return x * o 89
21
                                                          90 }
      .y - y * o.x; }
                                                          91
      bool operator < (const point &o) const{</pre>
         return (eq(x, o.x) ? y < o.y : x < o.x);
                                                          92 point forca_mod(point p, ld m){
23
                                                          93 ld cm = norm(p);
                                                                 if(cm<EPS) return point();</pre>
                                                          94
      bool operator == (const point &o) const{
25
                                                                 return point(p.x*m/cm,p.y*m/cm);
                                                          95
          return eq(x, o.x) and eq(y, o.y);
27
    friend ostream& operator << (ostream& os, point p) { 97
28
                                                          98 ld param(point a, point b, point v){
      return os << "(" << p.x << "," << p.y << ")"; }
                                                          99
                                                                // v = t*(b-a) + a // return t;
30 };
                                                                // assert(line(a, b).inside_seg(v));
                                                          100
                                                                 return ((v-a) * (b-a)) / ((b-a) * (b-a));
32 int ccw(point a, point b, point e){ // -1=dir; 0=
                                                         101
      collinear; 1=esq;
cod tmp = (b-a) ^ (e-a); // vector from a to b
                                                         102 }
                                                         103
33
                                                         104 bool simetric(vp &a){ //ordered
      return (tmp > EPS) - (tmp < -EPS);
34
                                                                int n = a.size();
35 }
                                                         105
                                                                 point c = center(a);
36
                                                                 if (n&1) return false;
37 ld norm(point a){ // Modulo
                                                         107
                                                         108
                                                                 for (int i=0; i < n/2; i++)
38
      return sqrt(a * a);
                                                                    if(ccw(a[i], a[i+n/2], c) != 0)
                                                         109
39 }
                                                                        return false;
40 cod norm2(point a){
                                                         110
                                                                 return true;
                                                         111
41
      return a * a;
                                                         112 }
42 }
43 bool nulo(point a){
                                                         113
                                                         114 point mirror(point m1, point m2, point p){
44
      return (eq(a.x, 0) \text{ and } eq(a.y, 0));
                                                               // mirror point p around segment m1m2
45 }
                                                         115
                                                                 point seg = m2-m1;
46 point rotccw(point p, ld a){
                                                         116
                                                                 1d t0 = ((p-m1)*seg) / (seg*seg);
      // a = PI*a/180; // graus
                                                         117
                                                                 point ort = m1 + seg*t0;
      return point((p.x*cos(a)-p.y*sin(a)), (p.y*cos(a)118
                                                                 point pm = ort-(p-ort);
                                                         119
      +p.x*sin(a)));
                                                                 return pm;
49 }
50 point rot90cw(point a) { return point(a.y, -a.x); }; 121 }
51 point rot90ccw(point a) { return point(-a.y, a.x); };122
                                                         124 //////////
53 ld proj(point a, point b){ // a sobre b
                                                         125 // Line //
54
      return a*b/norm(b);
                                                         126 ///////////
55 }
                                                         127
56 ld angle(point a, point b){ // em radianos
1d ang = a*b / norm(a) / norm(b);
                                                         128 struct line{
                                                         point p1, p2;
      return acos(max(min(ang, (ld)1), (ld)-1));
                                                                cod a, b, c; // ax+by+c = 0;
59 }
                                                         130
                                                         131
                                                                // y-y1 = ((y2-y1)/(x2-x1))(x-x1)
60 ld angle_vec(point v){
```

61 62 // return 180/PI*atan2(v.x, v.y); // graus

return atan2(v.x, v.y);

```
line(point p1=0, point p2=0): p1(p1), p2(p2){
132
                                                           197
133
           a = p1.y - p2.y;
                                                           198 ld dist_line(point p, line l){ // point - line
           b = p2.x - p1.x;
134
                                                           199
                                                                  return abs(1.eval(p))/sqrt(1.a*1.a + 1.b*1.b);
           c = p1 ^p2;
                                                           200 }
135
136
       }
                                                           201
       line(cod a=0, cod b=0, cod c=0): a(a), b(b), c(c)202 line bisector(point a, point b){
137
                                                                  point d = (b-a)*2;
                                                           203
           // Gera os pontos p1 p2 dados os coeficientes204
                                                                  return line(d.x, d.y, a*a - b*b);
138
           // isso aqui eh um lixo mas quebra um galho 205 }
139
       kkkkkk
           if(b==0){
                                                           207 line perpendicular(line 1, point p){ // passes
140
141
               p1 = point(1, -c/a);
                                                                  through p
                                                                  return line(1.b, -1.a, -1.b*p.x + 1.a*p.y);
142
               p2 = point(0, -c/a);
                                                           208
           }else{
                                                           209 }
143
                p1 = point(1, (-c-a*1)/b);
144
                                                           210
                p2 = point(0, -c/b);
145
                                                           211
146
           }
                                                           212 ///////////
       }
                                                           213 // Circle //
147
148
                                                           214 ///////////
       cod eval(point p){
149
                                                           215
           return a*p.x+b*p.y+c;
                                                           216 struct circle{
150
       }
                                                           217
                                                                  point c; cod r;
151
                                                                  circle() : c(0, 0), r(0){}
       bool inside(point p){
                                                           218
152
           return eq(eval(p), 0);
                                                                  circle(const point o) : c(o), r(0){}
                                                           219
       }
                                                                  circle(const point a, const point b){
154
                                                           220
       point normal(){
                                                                       c = (a+b)/2;
                                                           221
                                                                      r = norm(a-c);
156
           return point(a, b);
                                                           222
                                                           223
                                                                  circle(const point a, const point b, const point
158
                                                           224
       bool inside_seg(point p){
                                                                  00){
159
                                                                      assert(ccw(a, b, cc) != 0);
160
           return (
                                                           225
                ((p1-p) ^ (p2-p)) == 0 and
                                                           226
                                                                       c = inter_line(bisector(a, b), bisector(b, cc
161
                ((p1-p) * (p2-p)) <= 0
                                                                  ))[0];
162
163
           );
                                                           227
                                                                      r = norm(a-c);
       }
                                                                  }
164
                                                           228
                                                                  bool inside(const point &a) const{
165
                                                           229
                                                                      return norm(a - c) <= r + EPS;
166 }:
                                                           230
                                                           231
167
_{168} // be careful with precision error
                                                           232 };
169 vp inter_line(line l1, line l2){
                                                           233
170
       ld det = l1.a*l2.b - l1.b*l2.a;
                                                           234 pair < point , point > tangent_points (circle cr, point p)
       if(det==0) return {};
171
       1d x = (11.b*12.c - 11.c*12.b)/det;
                                                                  ld d1 = norm(p-cr.c), theta = asin(cr.r/d1);
                                                           235
172
       1d y = (11.c*12.a - 11.a*12.c)/det;
                                                           236
                                                                  point p1 = rotccw(cr.c-p, -theta);
173
       return {point(x, y)};
                                                                  point p2 = rotccw(cr.c-p, theta);
174
                                                           237
175 }
                                                           238
                                                                  assert(d1 >= cr.r);
                                                                  p1 = p1 * (sqrt(d1*d1-cr.r*cr.r) / d1) + p;
176
                                                           239
177 // segments not collinear
                                                                  p2 = p2 * (sqrt(d1*d1-cr.r*cr.r) / d1) + p;
                                                                  return {p1, p2};
178 vp inter_seg(line 11, line 12){
                                                           241
       vp ans = inter_line(l1, l2);
                                                           242 }
179
       if(ans.empty() or !11.inside_seg(ans[0]) or !12. 243
180
       inside_seg(ans[0]))
                                                           244
           return {};
                                                           245 circle incircle(point p1, point p2, point p3){
                                                                  1d m1 = norm(p2-p3);
       return ans;
182
                                                           246
183 }
                                                           247
                                                                  1d m2 = norm(p1-p3);
                                                                  ld m3 = norm(p1-p2);
184 bool seg_has_inter(line 11, line 12){
                                                           248
       // if collinear
                                                                  point c = (p1*m1 + p2*m2 + p3*m3)*(1/(m1+m2+m3));
185
                                                           249
       if (l1.inside_seg(l2.p1) || l1.inside_seg(l2.p2) 250
                                                                  ld s = 0.5*(m1+m2+m3);
186
       1d r = sqrt(s*(s-m1)*(s-m2)*(s-m3)) / s;
       return true;
                                                           252
                                                                  return circle(c, r);
187
                                                           253
       return ccw(l1.p1, l1.p2, l2.p1) * ccw(l1.p1, l1. 254
188
       p2, 12.p2) < 0 and
                                                           255 circle circumcircle(point a, point b, point c) {
              ccw(12.p1, 12.p2, 11.p1) * ccw(12.p1, 12. 256
                                                                  circle ans;
189
       p2, 11.p2) < 0;
                                                           257
                                                                  point u = point((b-a).y, -(b-a).x);
                                                                  point v = point((c-a).y, -(c-a).x);
190 }
                                                           258
                                                                  point n = (c-b)*0.5;
191
                                                           259
                                                                  1d t = (u^n)/(v^u);
192 ld dist_seg(point p, point a, point b){ // point -
                                                           260
                                                                  ans.c = ((a+c)*0.5) + (v*t);
                                                           261
       if((p-a)*(b-a) < EPS) return norm(p-a);
                                                                  ans.r = norm(ans.c-a);
                                                           262
       if((p-b)*(a-b) < EPS) return norm(p-b);
                                                                  return ans;
194
                                                           263
       return abs((p-a)^(b-a)) / norm(b-a);
195
                                                           264 }
196
                                                           265
```

```
266 vp inter_circle_line(circle C, line L){
       point ab = L.p2 - L.p1, p = L.p1 + ab * ((C.c-L. 6)
       p1)*(ab) / (ab*ab));
       1d s = (L.p2-L.p1)^{(C.c-L.p1)}, h2 = C.r*C.r - s*s 8
        / (ab*ab);
       if (h2 < -EPS) return {};</pre>
269
       if (eq(h2, 0)) return {p};
       point h = (ab/norm(ab)) * sqrt(h2);
271
                                                           12
       return \{p - h, p + h\};
272
                                                           13
273 }
274
                                                            15
275 vp inter_circle(circle C1, circle C2){
       if(C1.c == C2.c) { assert(C1.r != C2.r); return
                                                           17
       {}: }
       point vec = C2.c - C1.c;
       1d d2 = vec*vec, sum = C1.r+C2.r, dif = C1.r-C2.r_{20}
       1d p = (d2 + C1.r*C1.r - C2.r*C2.r)/(d2*2), h2 = 22
       C1.r*C1.r - p*p*d2;
       if (sum*sum < d2 or dif*dif > d2) return {};
280
                                                           24
       point mid = C1.c + vec*p, per = point(-vec.y, vec 25
281
       .x) * sqrt(max((ld)0, h2) / d2);
       if(eq(per.x, 0) and eq(per.y, 0)) return {mid}; 27
282
       return {mid + per, mid - per};
284 }
285
286 // minimum circle cover O(n) amortizado
287 circle min_circle_cover(vp v){
       random_shuffle(v.begin(), v.end());
       circle ans;
289
       int n = v.size();
       for(int i=0;i<n;i++) if(!ans.inside(v[i])){</pre>
291
           ans = circle(v[i]);
292
           for(int j=0;j<i;j++) if(!ans.inside(v[j])){</pre>
               ans = circle(v[i], v[j]);
294
                for(int k=0;k<j;k++) if(!ans.inside(v[k])</pre>
       ) {
                    ans = circle(v[i], v[j], v[k]);
               }
           }
298
299
       }
300
       return ans;
301 }
```

8 Algorithms

8.1 Lis

```
int lis(vector < int > const& a) {
      int n = a.size();
      vector < int > d(n, 1);
      for (int i = 0; i < n; i++) {
          for (int j = 0; j < i; j++) {
              if (a[j] < a[i])
                  d[i] = max(d[i], d[j] + 1);
10
      int ans = d[0];
11
      for (int i = 1; i < n; i++) {
12
13
          ans = max(ans, d[i]);
      return ans;
15
16 }
```

8.2 Delta-encoding

```
1 #include <bits/stdc++.h>
2 using namespace std;
3
4 int main(){
```

return 0; }

8.3

int n, q;

int [n];

cin >> n >> q;

while (q--) {

int curr = 0;

cout << '\n';

Subsets

int 1, r, x;

delta[1] += x;

delta[r+1] -= x;

for(int i=0; i < n; i++){

curr += delta[i];

for(int i=0; i < n; i++){

cout << v[i] << '';

v[i] = curr;

cin >> 1 >> r >> x;

```
void subsets(vector<int>& nums){
  int n = nums.size();
  int powSize = 1 << n;

for(int counter = 0; counter < powSize; counter++){
  for(int j = 0; j < n; j++){
   if((counter & (1LL << j)) != 0) {
      cout << nums[j] << '';
   }
}
cout << '\n';
}
</pre>
```

8.4 Binary Search Last True

8.5 Ternary Search

```
mt.add(x);
          else
10
                                                          44
11
             r = m2;
                                                          45
                                                                     balancear();
                                                                 }
12
                                                          46
      return f(1);
                                        //return the
                                                          47
                                                                 void rem(ll x){
13
      maximum of f(x) in [1, r]
                                                                     //x = -x;
                                                                     if(mt.pop(x) == 0)
14 }
                                                          49
                                                                         gt.pop(x);
  8.6 Binary Search First True
                                                                     balancear():
                                                          51
                                                          52
int first_true(int lo, int hi, function < bool(int) > f) 53 };
                                                          55 int main() {
    hi++;
                                                                 ios::sync_with_stdio(false);
                                                          56
    while (lo < hi) {
3
                                                                 cin.tie(NULL);
                                                          57
      int mid = lo + (hi - lo) / 2;
                                                          58
      if (f(mid)) {
                                                                 int n, k, q; cin >> n >> k >> q;
                                                          59
        hi = mid;
      } else {
                                                                 BigK big = BigK(k);
                                                          61
        lo = mid + 1;
                                                                 int arr[n] = {};
                                                          63
    }
10
                                                          64
    return lo;
11
                                                                 while (q--) {
                                                          65
12 }
                                                                     int pos, num; cin >> pos >> num;
                                                          66
  8.7 Biggest K
                                                                     big.rem(arr[pos]);
                                                          68
                                                                     arr[pos] = num;
                                                          69
1 // Description: Gets sum of k biggest or k smallest
                                                                     big.add(arr[pos]);
      elements in an array
                                                          71
                                                                     cout << big.gt.s << '\n';</pre>
3 // Problem: https://atcoder.jp/contests/abc306/tasks/73
      abc306_e
                                                                 return 0;
                                                          75
                                                          76 }
5 // Complexity: O(log n)
                                                                  Data Structures
7 struct SetSum {
      11 s = 0;
      multiset <11> mt;
                                                             9.1 Ordered Set
10
      void add(ll x){
          mt.insert(x);
11
          s += x;
                                                           1 // Description:
      }
                                                           2 // insert(k) - add element k to the ordered set
13
      int pop(11 x){
                                                           3 // erase(k) - remove element k from the ordered set
          auto f = mt.find(x);
                                                           4 // erase(it) - remove element it points to from the
15
          if(f == mt.end()) return 0;
                                                                 ordered set
16
          mt.erase(f);
                                                           5 // order_of_key(k) - returns number of elements
          s -= x;
                                                                 strictly smaller than k
18
19
           return 1;
                                                           6 // find_by_order(n) - return an iterator pointing to
                                                                 the k-th element in the ordered set (counting
      }
20
21 };
                                                                 from zero).
22
                                                           8 // Problem:
23 struct BigK {
                                                           9 // https://cses.fi/problemset/task/2169/
      int k;
      SetSum gt, mt;
25
                                                          11 // Complexity:
      BigK(int _k){
          k = _k;
                                                          _{\rm 12} // O(log n) for all operations
27
28
                                                          _{14} // How to use:
       void balancear(){
29
          while((int)gt.mt.size() < k && (int)mt.mt.
                                                          15 // ordered_set <int > os;
30
      size()){
                                                          16 // cout << os.order_of_key(1) << '\n;</pre>
31
               auto p = (prev(mt.mt.end()));
                                                          17 // cout << os.find_by_order(1) << '\n;</pre>
               gt.add(*p);
32
                                                          19 // Notes
33
               mt.pop(*p);
                                                          20 // The ordered set only contains different elements
34
           while((int)mt.mt.size() && (int)gt.mt.size() 21 // By using less_equal<T> instead of less<T> on using
                                                                  ordered_set declaration
           *(gt.mt.begin()) < *(prev(mt.mt.end())) ){
                                                          22 // The ordered_set becomes an ordered_multiset
                                                          _{\rm 23} // So the set can contain elements that are equal
37
               11 u = *(gt.mt.begin());
               11 v = *(prev(mt.mt.end()));
38
               gt.pop(u); mt.pop(v);
                                                          25 #include <ext/pb_ds/assoc_container.hpp>
               gt.add(v); mt.add(u);
                                                          26 #include <ext/pb_ds/tree_policy.hpp>
40
      }
42
                                                          28 using namespace __gnu_pbds;
      void add(11 x){
                                                          29 template <typename T>
43
```

```
30 using ordered_set = tree<T,null_type,less<T>,
                                                          37
                                                                      if (sizes[a] < sizes[b])</pre>
    rb_tree_tag,tree_order_statistics_node_update>; 38
                                                                          swap(a, b);
                                                           39
32 void Erase(ordered_set < int >& a, int x){
                                                                      sizes[a] += sizes[b];
                                                           40
      int r = a.order_of_key(x);
33
                                                           41
                                                                      link[b] = a;
      auto it = a.find_by_order(r);
34
                                                           42
      a.erase(it);
35
                                                           43
36 }
                                                                  int size(int x) {
                                                           44
                                                                      return sizes[x];
                                                           45
  9.2 Priority Queue
                                                           46
                                                           47 };
1 // Description:
                                                           49 int main() {
^{49} ^{2} // Keeps the largest (by default) element at the top ^{49} ^{50}
                                                                  ios::sync_with_stdio(false);
      of the queue
                                                                  cin.tie(NULL);
                                                           51
                                                           52
4 // Problem:
                                                           53
                                                                  int cities, roads; cin >> cities >> roads;
5 // https://cses.fi/problemset/task/1164/
                                                                  vector < int > final_roads;
                                                           54
                                                                  int ans = 0;
7 // Complexity:
                                                                  DSU dsu = DSU(cities);
                                                           56
_{8} // O(log n) for push and pop
                                                                  for (int i = 0, a, b; i < roads; i++) {
                                                           57
_{9} // _{0} (1) for looking at the element at the top
                                                                      cin >> a >> b;
                                                           58
                                                                      dsu.unite(a, b);
                                                           59
11 // How to use:
                                                           60
12 // prioriy_queue <int > pq;
                                                           61
13 // pq.push(1);
                                                           62
                                                                  for (int i = 2; i <= cities; i++) {
14 // pq.top();
                                                                      if (!dsu.same(1, i)) {
                                                           63
15 // pq.pop()
                                                                          ans++;
                                                           64
                                                                          final_roads.push_back(i);
17 // Notes
                                                                          dsu.unite(1,i);
                                                           66
_{18} // To use the priority queue keeping the smallest
                                                                      }
                                                           67
      element at the top
                                                                  }
                                                           68
                                                           69
20 priority_queue <int, vector <int>, greater <int>> pq;
                                                                  cout << ans << '\n';
                                                                  for (auto e : final_roads) {
                                                           71
  9.3 Dsu
                                                                      cout << "1 " << e << '\n';
                                                           73
1 #include <bits/stdc++.h>
                                                           74
                                                           75 }
3 using namespace std;
                                                                   Two Sets
                                                             9.4
5 const int MAX = 1e6+17;
                                                            1 // Description
                                                            _{2} // THe values are divided in two multisets so that
7 struct DSU {
      int n;
                                                                  one of them contain all values that are
      vector<int> link, sizes;
                                                           _3 // smaller than the median and the other one contains
9
                                                                  all values that are greater or equal to the
      DSU(int n) {
                                                                  median.
11
12
          this ->n = n;
                                                           5 // Problem:
           link.assign(n+1, 0);
13
                                                           6 // https://atcoder.jp/contests/abc306/tasks/abc306_e
           sizes.assign(n+1, 1);
14
                                                           7 // Problem I - Maratona Feminina de çãProgramao da
           for (int i = 0; i \le n; i++)
                                                                 Unicamp 2023
16
              link[i] = i;
                                                            8 // https://codeforces.com/group/WYIydkiPyE/contest
      }
                                                                 /450037/attachments
18
19
      int find(int x) {
                                                           10 // Complexity:
20
           while (x != link[x])
                                                           11 // Add and remove elements - O(log n)
21
              x = link[x];
                                                           12 // Return sum of biggest or smallest set or return
23
                                                                 the median - 0(1)
           return x;
24
                                                           13
      }
25
                                                           14 using ll = long long;
26
                                                           15
27
      bool same(int a, int b) {
                                                          16 struct TwoSets {
          return find(a) == find(b);
                                                          17 multiset <int > small;
28
                                                               multiset < int > big;
                                                           18
                                                              11 \text{ sums} = 0;
30
                                                           19
      void unite(int a, int b) {
31
                                                           20
                                                              11 \text{ sumb} = 0:
          a = find(a);
                                                               int n = 0;
                                                           21
          b = find(b);
33
                                                           22
                                                               int size_small() {
          if (a == b) return;
                                                                 return small.size();
35
                                                           24
                                                           25
36
```

```
4 // When the indexes of the nodes are too big to be
                                                                  stored in an array
27
    int size_big() {
                                                            _{5} // and the queries need to be answered online so we
28
      return big.size();
                                                                  can't sort the nodes and compress them
29
                                                            _{6} // we create nodes only when they are needed so there
    void balance() {
                                                                  'll be (Q*log(MAX)) nodes
31
      while (size_small() > n / 2) {
                                                            _{7} // where Q is the number of queries and MAX is the
32
        int v = *small.rbegin();
                                                                  maximum index a node can assume
33
         small.erase(prev(small.end()));
34
                                                            _{9} // Query - get sum of elements from range (1, r)
        big.insert(v);
         sums -= v;
                                                                  inclusive
36
         sumb += v;
37
                                                           _{10} // Update - update element at position id to a value
      }
38
                                                                  val
      while (size_big() > n - n / 2) {
39
                                                           12 // Problem:
        int v = *big.begin();
40
                                                           13 // https://cses.fi/problemset/task/1648
         big.erase(big.begin());
41
         small.insert(v);
        sumb -= v;
                                                           15 // Complexity:
43
         sums += v;
                                                           16 // O(log n) for both query and update
      }
45
                                                           18 // How to use:
46
                                                           _{19} // MAX is the maximum index a node can assume
    void add(int x) {
48
      n++;
                                                           21 // Segtree seg = Segtree(MAX);
      small.insert(x);
50
      sums += x;
                                                           23 typedef long long ftype;
51
      while (!small.empty() && *small.rbegin() > *big. 24
52
                                                           25 const int MAX = 1e9+17;
      begin()) {
         int v = *small.rbegin();
53
         small.erase(prev(small.end()));
                                                           27 struct Segtree {
54
         big.insert(v);
                                                                  vector < ftype > seg, d, e;
55
                                                           28
        sums -= v;
                                                                  const ftype NEUTRAL = 0;
56
                                                           29
         sumb += v;
                                                                  int n;
                                                           30
      }
                                                           31
      balance();
                                                                  Segtree(int n) {
59
                                                           32
                                                                      this ->n = n;
60
                                                           33
                                                                      create();
61
                                                           34
    bool rem(int x) {
                                                           35
                                                                      create();
62
      n--;
                                                           36
      auto it1 = small.find(x);
                                                           37
64
      auto it2 = big.find(x);
65
                                                           38
                                                                  ftype f(ftype a, ftype b) {
      bool flag = false;
                                                                      return a + b;
66
                                                           39
      if (it1 != small.end()) {
                                                           40
        sums -= *it1;
                                                           41
68
         small.erase(it1);
                                                                  ftype create() {
                                                           42
69
         flag = true;
                                                                      seg.push_back(0);
70
                                                           43
      } else if (it2 != big.end()) {
                                                                      e.push_back(0);
71
                                                           44
         sumb = *it2;
                                                                      d.push_back(0);
                                                                      return seg.size() - 1;
         big.erase(it2);
73
                                                           46
74
         flag = true;
                                                           47
75
                                                           48
                                                                  ftype query(int pos, int ini, int fim, int p, int
      balance();
76
                                                           49
      return flag;
                                                                      if (q < ini || p > fim) return NEUTRAL;
78
                                                           50
                                                           51
                                                                      if (pos == 0) return 0;
79
                                                                      if (p <= ini && fim <= q) return seg[pos];</pre>
80
    11 sum_small() {
                                                           52
                                                                      int m = (ini + fim) >> 1;
      return sums;
81
                                                           53
                                                                      return f(query(e[pos], ini, m, p, q), query(d
                                                           54
83
                                                                  [pos], m + 1, fim, p, q));
    11 sum_big() {
                                                           55
84
85
      return sumb;
                                                           56
                                                                  void update(int pos, int ini, int fim, int id,
86
                                                           57
                                                                  int val) {
                                                                      if (ini > id || fim < id) {</pre>
    int median() {
88
                                                           58
89
      return *big.begin();
                                                                          return;
90
                                                           60
91 }:
                                                           61
                                                                      if (ini == fim) {
                                                           62
  9.5 Dynamic Implicit Sparse
                                                                          seg[pos] = val;
                                                           63
                                                                           return:
1 // Description:
                                                           65
                                                                      }
2 // Indexed at one
                                                           67
```

```
int m = (ini + fim) >> 1;
                                                                           int m = (1Y+rY)/2;
68
                                                           46
                                                           47
69
           if (id <= m) {
                                                                           buildY(noX, 1X, rX, 2*noY+1, 1Y, m, v);
70
                                                           48
               if (e[pos] == 0) e[pos] = create();
71
                                                                           buildY(noX, 1X, rX, 2*noY+2, m+1, rY, v);
                                                            49
               update(e[pos], ini, m, id, val);
                                                                           seg[noX][noY] = seg[noX][2*noY+1] + seg[
           } else {
73
                                                           51
               if (d[pos] == 0) d[pos] = create();
                                                                  noX][2*noY+2];
               update(d[pos], m + 1, fim, id, val);
75
                                                           52
                                                                      }
76
                                                           53
          seg[pos] = f(seg[e[pos]], seg[d[pos]]);
                                                                  void buildX(int noX, int 1X, int rX, vector<</pre>
78
                                                           55
      }
79
                                                                  vector <int>> &v) {
                                                                      if(1X != rX){
80
                                                           56
                                                                           int m = (1X+rX)/2;
       ftype query(int p, int q) {
81
                                                           57
82
          return query(1, 1, n, p, q);
                                                           58
                                                                           buildX(2*noX+1, 1X, m, v);
83
                                                           59
                                                                           buildX(2*noX+2, m+1, rX, v);
      void update(int id, int val) {
85
                                                           61
86
          update(1, 1, n, id, val);
                                                                      buildY(noX, 1X, rX, 0, 0, M - 1, v);
87
                                                           63
88 };
                                                           64
                                                           65
        Segtree2d
  9.6
                                                                  void updateY(int noX, int 1X, int rX, int noY,
                                                           66
                                                                  int 1Y, int rY, int y) {
                                                                       if(1Y == rY){
                                                           67
1 // Description:
                                                                           if(1X == rX){
_2 // Indexed at zero
                                                           68
                                                                               seg[noX][noY] = !seg[noX][noY];
_3 // Given a N x M grid, where i represents the row and ^{69}
       j the column, perform the following operations
                                                                               seg[noX][noY] = seg[2*noX+1][noY] +
4 // update(j, i) - update the value of grid[i][j]
                                                                  seg[2*noX+2][noY];
_{5} // query(j1, j2, i1, i2) - return the sum of values
                                                                           }
      inside the rectangle
6 // defined by grid[i1][j1] and grid[i2][j2] inclusive 73
                                                                       }else{
                                                                           int m = (1Y+rY)/2;
8 // Problem:
                                                                           if(v \le m){
9 // https://cses.fi/problemset/task/1739/
                                                           76
                                                                               updateY(noX, 1X, rX, 2*noY+1,1Y, m, y
                                                                  );
11 // Complexity:
                                                                           else if(m < y)
12 // Time complexity:
                                                            78
_{13} // O(log N * log M) for both query and update
                                                                               updateY(noX, 1X, rX, 2*noY+2, m+1, rY
                                                                   , y);
_{14} // O(N * M) for build
                                                            80
15 // Memory complexity:
16 // 4 * M * N
                                                           81
                                                                           seg[noX][noY] = seg[noX][2*noY+1] + seg[
                                                           82
                                                                  noX][2*noY+2];
18 // How to use:
19 // Segtree2D seg = Segtree2D(n, n);
                                                           83
                                                                  }
20 // vector < vector < int >> v(n, vector < int >(n));
                                                           84
21 // seg.build(v);
                                                           85
                                                                  void updateX(int noX, int lX, int rX, int x, int
23 // Notes
                                                           87
                                                                       int m = (1X+rX)/2;
_{24} // Indexed at zero
                                                            88
25
                                                                       if(1X != rX){
26 struct Segtree2D {
                                                           89
                                                                           if(x \le m){
      const int MAXN = 1025;
27
                                                                               updateX(2*noX+1, 1X, m, x, y);
                                                           91
      int N, M;
                                                                           else if(m < x){
                                                           92
29
                                                           93
                                                                               updateX(2*noX+2, m+1, rX, x, y);
      vector < vector < int >> seg;
30
                                                           94
31
       Segtree2D(int N, int M) {
                                                                      }
                                                           95
32
           this ->N = N;
                                                           96
                                                           97
                                                                      updateY(noX, 1X, rX, 0, 0, M - 1, y);
34
           this ->M = M;
                                                           98
                                                                  }
           seg.resize(2*MAXN, vector<int>(2*MAXN));
35
36
                                                                  int queryY(int noX, int noY, int lY, int rY, int
37
                                                                  aY, int bY){
38
       void buildY(int noX, int 1X, int rX, int noY, int
       1Y, int rY, vector < vector < int >> &v) {
                                                                       if(aY <= 1Y && rY <= bY) return seg[noX][noY</pre>
           if(1Y == rY){
                                                                  1:
39
               if(1X == rX){
40
                   seg[noX][noY] = v[rX][rY];
                                                                      int m = (1Y+rY)/2;
                                                           103
41
                                                           104
42
                   seg[noX][noY] = seg[2*noX+1][noY] +
                                                                      if (bY <= m) return queryY(noX, 2*noY+1, 1Y, m
43
                                                                  , aY, bY);
       seg[2*noX+2][noY];
                                                                      if (m < aY) return queryY(noX, 2*noY+2, m+1,
               }
44
                                                                  rY, aY, bY);
          }else{
45
```

```
107
           return queryY(noX, 2*noY+1, 1Y, m, aY, bY) +
                                                           35
                                                                       seg.assign(2*sz, NEUTRAL);
108
       queryY(noX, 2*noY+2, m+1, rY, aY, bY);
                                                            36
                                                            37
109
                                                                   ftype f(ftype a, ftype b) {
                                                                       if (a.ff < b.ff) return a;
       int queryX(int noX, int 1X, int rX, int aX, int
111
                                                           39
       bX, int aY, int bY){
                                                                       if (b.ff < a.ff) return b;</pre>
                                                            40
           if (aX <= 1X && rX <= bX) return queryY(noX,
                                                           41
       0, 0, M - 1, aY, bY);
                                                                       return mp(a.ff, a.ss + b.ss);
                                                            42
                                                                  }
113
                                                            43
           int m = (1X+rX)/2;
114
                                                            44
                                                                   ftype query(int pos, int ini, int fim, int p, int
           if (bX <= m) return queryX(2*noX+1, lX, m, aX,
116
                                                                       if (ini >= p && fim <= q) {
        bX, aY, bY);
           if (m < aX) return queryX(2*noX+2, m+1, rX, aX 47
                                                                          return seg[pos];
       , bX, aY, bY);
                                                                       if (q < ini || p > fim) {
           return queryX(2*noX+1, 1X, m, aX, bX, aY, bY) 50
119
                                                                           return NEUTRAL;
        + queryX(2*noX+2, m+1, rX, aX, bX, aY, bY);
120
                                                            52
121
                                                            53
                                                                       int e = 2*pos + 1;
       void build(vector<vector<int>> &v) {
122
                                                            54
                                                                       int d = 2*pos + 2;
           buildX(0, 0, N - 1, v);
                                                            55
123
                                                                       int m = ini + (fim - ini) / 2;
125
                                                            57
       int query(int aX, int bX, int aY, int bY) {
                                                                       return f(query(e, ini, m, p, q), query(d, m +
126
           return queryX(0, 0, N - 1, aX, bX, aY, bY);
127
                                                                   1, fim, p, q));
128
                                                            59
129
       void update(int x, int y) {
                                                                  void update(int pos, int ini, int fim, int id,
130
                                                            61
           updateX(0, 0, N - 1, x, y);
131
                                                                  int val) {
                                                                       if (ini > id || fim < id) {
132
                                                            62
133 };
                                                           63
                                                                           return;
         Minimum And Amount
                                                            65
                                                                       if (ini == id && fim == id) {
                                                                           seg[pos] = mp(val, 1);
 1 // Description:
 2 // Query - get minimum element in a range (1, r)
                                                            68
                                                                           return;
       inclusive
 _{\rm 3} // and also the number of times it appears in that
                                                            70
                                                                       int e = 2*pos + 1;
 4 // Update - update element at position id to a value
                                                                       int d = 2*pos + 2;
                                                            73
       val
                                                            74
                                                                       int m = ini + (fim - ini) / 2;
 6 // Problem:
                                                            75
                                                                       update(e, ini, m, id, val);
 7 // https://codeforces.com/edu/course/2/lesson/4/1/
                                                            76
                                                                       update(d, m + 1, fim, id, val);
       practice/contest/273169/problem/C
                                                            77
                                                                       seg[pos] = f(seg[e], seg[d]);
 9 // Complexity:
                                                            79
                                                            80
_{10} // O(log n) for both query and update
                                                            81
                                                                  void build(int pos, int ini, int fim, vector<int>
12 // How to use:
                                                            82
13 // Segtree seg = Segtree(n);
                                                                   &v) {
                                                                       if (ini == fim) {
14 // seg.build(v);
                                                            83
                                                                           if (ini < (int)v.size()) {</pre>
                                                            84
1.5
                                                                               seg[pos] = mp(v[ini], 1);
                                                            85
16 #define pii pair <int, int>
17 #define mp make_pair
                                                            86
                                                                           return;
18 #define ff first
                                                            87
19 #define ss second
                                                            88
                                                                       }
                                                            89
                                                                       int e = 2*pos + 1;
21 const int INF = 1e9+17;
                                                           90
                                                                       int d = 2*pos + 2;
                                                           91
                                                                       int m = ini + (fim - ini) / 2;
23 typedef pii ftype;
                                                           92
                                                           93
                                                            94
                                                                       build(e, ini, m, v);
25 struct Segtree {
                                                                       build(d, m + 1, fim, v);
       vector<ftype> seg;
                                                           95
26
                                                           96
27
       int n;
                                                                       seg[pos] = f(seg[e], seg[d]);
       const ftype NEUTRAL = mp(INF, 0);
                                                           97
28
                                                           98
       Segtree(int n) {
                                                           99
30
                                                                  ftype query(int p, int q) {
           int sz = 1;
                                                           100
           while (sz < n) sz *= 2;
                                                           101
                                                                       return query(0, 0, n - 1, p, q);
32
                                                           102
           this->n = sz;
33
```

```
int d = 2*pos + 2;
                                                            50
                                                                       int m = ini + (fim - ini) / 2;
104
       void update(int id, int val) {
                                                            51
           update(0, 0, n - 1, id, val);
105
                                                            52
                                                            53
                                                                       lazy[e] = apply_lazy(lazy[e], lazy[pos], 1);
106
                                                                       lazy[d] = apply_lazy(lazy[d], lazy[pos], 1);
       void build(vector<int> &v) {
108
                                                            55
           build(0, 0, n - 1, v);
                                                                       seg[e] = apply_lazy(seg[e], lazy[pos], m -
109
                                                                   ini + 1);
110
                                                                       seg[d] = apply_lazy(seg[d], lazy[pos], fim -
111
                                                            57
       void debug() {
                                                                   m);
           for (auto e : seg) {
113
                                                            58
                cout << e.ff << ' ' << e.ss << '\n';
114
                                                                       lazy[pos] = NEUTRAL_LAZY;
115
                                                            60
           cout << '\n';</pre>
116
                                                            61
       }
                                                                   ftype f(ftype a, ftype b) {
117
                                                            62
118 };
                                                                       return a + b;
                                                            63
                                                            64
   9.8 Lazy Addition To Segment
                                                            65
                                                                   ftype query(int pos, int ini, int fim, int p, int
 1 // Description:
                                                                       propagate(pos, ini, fim);
 2 // Query - get sum of elements from range (1, r)
                                                            67
       inclusive
                                                                       if (ini >= p && fim <= q) {
 3 // Update - add a value val to elementos from range
                                                           (69
       l, r) inclusive
                                                                           return seg[pos];
                                                            71
 5 // Problem:
                                                            72
                                                                       if (q < ini || p > fim) {
 6 // https://codeforces.com/edu/course/2/lesson/5/1/
                                                            73
                                                                            return NEUTRAL;
                                                            74
       practice/contest/279634/problem/A
 8 // Complexity:
                                                            76
                                                                       int e = 2*pos + 1;
 _{9} // O(log n) for both query and update
                                                                       int d = 2*pos + 2;
                                                            78
10
                                                                       int m = ini + (fim - ini) / 2;
                                                            79
_{11} // How to use:
12 // Segtree seg = Segtree(n);
                                                            80
                                                                       return f(query(e, ini, m, p, q), query(d, m +
13 // seg.build(v);
                                                            81
                                                                    1, fim, p, q));
15 // Notes
                                                            82
_{16} // Change neutral element and f function to perform a ^{83}
                                                                   void update(int pos, int ini, int fim, int p, int
        different operation
                                                                    q, int val) {
18 const long long INF = 1e18+10;
                                                                       propagate(pos, ini, fim);
                                                            86
                                                                       if (ini > q || fim < p) {</pre>
20 typedef long long ftype;
                                                            87
                                                            88
                                                                            return;
21
                                                            89
22 struct Segtree {
       vector < ftvpe > seg;
                                                            90
23
                                                                       if (ini >= p && fim <= q) {</pre>
24
       vector<ftype> lazy;
                                                            91
                                                                            lazy[pos] = apply_lazy(lazy[pos], val, 1)
       int n;
25
       const ftype NEUTRAL = 0;
26
                                                                            seg[pos] = apply_lazy(seg[pos], val, fim
       const ftype NEUTRAL_LAZY = -1; // change to -INF 93
                                                                   - ini + 1);
       if there are negative numbers
                                                            94
                                                                            return;
       Segtree(int n) {
29
                                                                       }
                                                            96
30
           int sz = 1;
                                                            97
           while (sz < n) sz *= 2;
31
                                                                       int e = 2*pos + 1;
                                                            98
           this ->n = sz;
32
                                                                       int d = 2*pos + 2;
                                                            99
33
                                                                       int m = ini + (fim - ini) / 2;
           seg.assign(2*sz, NEUTRAL);
                                                            100
34
            lazy.assign(2*sz, NEUTRAL_LAZY);
                                                            101
                                                            102
                                                                       update(e, ini, m, p, q, val);
36
       }
                                                                       update(d, m + 1, fim, p, q, val);
                                                            103
37
                                                            104
       ftype apply_lazy(ftype a, ftype b, int len) {
38
            if (b == NEUTRAL_LAZY) return a;
                                                                       seg[pos] = f(seg[e], seg[d]);
                                                            105
39
40
            if (a == NEUTRAL_LAZY) return b * len;
                                                            106
                                                            107
            else return a + b * len;
41
                                                                   void build(int pos, int ini, int fim, vector<int>
                                                            108
42
43
                                                                       if (ini == fim) {
       void propagate(int pos, int ini, int fim) {
                                                            109
44
                                                                            if (ini < (int)v.size()) {</pre>
                                                            110
           if (ini == fim) {
45
                                                                                seg[pos] = v[ini];
                return:
                                                            111
46
                                                            112
                                                            113
                                                                            return;
                                                                       }
                                                            114
           int e = 2*pos + 1;
49
```

```
ftype_node suf;
115
                                                            31
           int e = 2*pos + 1;
                                                            32
                                                                   ftype_node sum;
116
           int d = 2*pos + 2;
117
                                                            33
           int m = ini + (fim - ini) / 2;
                                                                   Node (ftype_node max_seg, ftype_node pref,
118
                                                            34
                                                                   ftype_node suf, ftype_node sum) : max_seg(max_seg
            build(e, ini, m, v);
                                                                   ), pref(pref), suf(suf), sum(sum) {};
120
           build(d, m + 1, fim, v);
121
                                                            35 };
122
                                                            36
           seg[pos] = f(seg[e], seg[d]);
                                                            37 typedef Node ftype;
123
       }
124
                                                            38
                                                            39 struct Segtree {
125
126
       ftype query(int p, int q) {
                                                            40
                                                                   vector <ftype > seg;
                                                                   int n;
           return query(0, 0, n - 1, p, q);
127
                                                            41
                                                                   const ftype NEUTRAL = Node(0, 0, 0, 0);
128
                                                            42
129
                                                            43
       void update(int p, int q, int val) {
                                                                   Segtree(int n) {
130
                                                            44
           update(0, 0, n - 1, p, q, val);
131
                                                            45
                                                                       int sz = 1;
                                                                       // potencia de dois mais proxima
132
                                                            46
133
                                                                       while (sz < n) sz *= 2;
       void build(vector<int> &v) {
                                                                       this ->n = sz;
134
                                                            48
           build(0, 0, n - 1, v);
                                                            49
135
                                                                       // numero de nos da seg
136
                                                            50
                                                                       seg.assign(2*sz, NEUTRAL);
137
                                                            51
       void debug() {
                                                                   }
                                                            52
           for (auto e : seg) {
139
                                                            53
                cout << e << ' ';
                                                            54
                                                                   ftype f(ftype a, ftype b) {
140
141
                                                            55
                                                                       ftype_node max_seg = max({a.max_seg, b.
           cout << '\n';</pre>
                                                                   max_seg, a.suf + b.pref});
142
           for (auto e : lazy) {
                                                                       ftype_node pref = max(a.pref, a.sum + b.pref)
                                                            56
               cout << e << ' ';
144
                                                                       ftype_node suf = max(b.suf, b.sum + a.suf);
145
                                                            57
           cout << '\n';
                                                                       ftype_node sum = a.sum + b.sum;
146
                                                            58
           cout << '\n';</pre>
147
                                                            59
                                                            60
                                                                       return Node(max_seg, pref, suf, sum);
149 }:
                                                            61
         Segment With Maximum Sum
                                                                   ftype query(int pos, int ini, int fim, int p, int
                                                            63
                                                                       if (ini >= p && fim <= q) {
 1 // Description:
                                                                           return seg[pos];
 2 // Query - get sum of segment that is maximum among
                                                            65
       all segments
 3 // E.g
                                                            67
                                                                       if (q < ini || p > fim) {
 4 // Array: 5 -4 4 3 -5
 _{5} // Maximum segment sum: 8 because 5 + (-4) + 4 = 8
                                                            69
                                                                           return NEUTRAL;
 _{\rm 6} // Update - update element at position id to a value ^{\rm 70}
       val
                                                                       int e = 2*pos + 1;
                                                            72
 8 // Problem:
                                                                       int d = 2*pos + 2;
                                                                       int m = ini + (fim - ini) / 2;
 9 // https://codeforces.com/edu/course/2/lesson/4/2/
                                                            74
                                                            75
       practice/contest/273278/problem/A
                                                                       return f(query(e, ini, m, p, q), query(d, m +
                                                            76
                                                                    1, fim, p, q));
11 // Complexity:
_{12} // O(log n) for both query and update
                                                            77
                                                            78
                                                                   void update(int pos, int ini, int fim, int id,
14 // How to use:
                                                            79
15 // Segtree seg = Segtree(n);
                                                                   int val) {
                                                                       if (ini > id || fim < id) {
                                                            80
16 // seg.build(v);
                                                                           return;
                                                            81
18 // Notes
                                                            82
                                                            83
_{19} // The maximum segment sum can be a negative number
                                                                       if (ini == id && fim == id) {
                                                            84
20 // In that case, taking zero elements is the best
                                                                           seg[pos] = Node(val, val, val, val);
                                                            85
       choice
21 // So we need to take the maximum between 0 and the
                                                                           return:
       query
                                                            87
                                                                       7
22 // max(OLL, seg.query(0, n).max_seg)
                                                            89
                                                                       int e = 2*pos + 1;
                                                            90
24 using ll = long long;
                                                                       int d = 2*pos + 2;
                                                            91
                                                                       int m = ini + (fim - ini) / 2;
                                                            92
26 typedef ll ftype_node;
                                                            93
                                                                       update(e, ini, m, id, val);
28 struct Node {
                                                            94
```

ftype_node max_seg;

ftype_node pref;

29

update(d, m + 1, fim, id, val);

```
seg[pos] = f(seg[e], seg[d]);
                                                            20 // Use the same segtree, but perform the following
97
                                                                   operations
98
                                                            21 // Query - seg.query(0, id);
99
       void build(int pos, int ini, int fim, vector < int > 22 // Update - seg.update(1, v); seg.update(r + 1, -v);
100
           if (ini == fim) {
                                                            24 typedef long long ftype;
101
                // se a caposio existir no array original cap 25
102
                // seg tamanho potencia de dois
                                                            26 struct Segtree {
103
                if (ini < (int)v.size()) {</pre>
                                                                   vector<ftype> seg;
104
                                                            27
                    seg[pos] = Node(v[ini], v[ini], v[ini 28
                                                                   int n;
       ], v[ini]);
                                                                   const ftype NEUTRAL = 0;
                                                            29
                }
107
                return;
                                                            31
                                                                   Segtree(int n) {
           }
                                                                       int sz = 1;
108
                                                            32
109
                                                                        while (sz < n) sz *= 2;
                                                            33
            int e = 2*pos + 1;
                                                                        this ->n = sz;
110
                                                            34
            int d = 2*pos + 2;
                                                            35
           int m = ini + (fim - ini) / 2;
                                                                        seg.assign(2*sz, NEUTRAL);
112
                                                            36
                                                            37
           build(e, ini, m, v);
114
                                                            38
           build(d, m + 1, fim, v);
                                                                   ftype f(ftype a, ftype b) {
                                                            39
115
                                                            40
                                                                       return a + b;
116
           seg[pos] = f(seg[e], seg[d]);
117
                                                            41
       }
                                                            42
                                                                   ftype query(int pos, int ini, int fim, int p, int
119
                                                            43
       ftype query(int p, int q) {
120
           return query(0, 0, n - 1, p, q);
                                                                        if (ini >= p && fim <= q) {
121
                                                            44
                                                                            return seg[pos];
122
                                                            45
123
                                                            46
       void update(int id, int val) {
124
                                                            47
           update(0, 0, n - 1, id, val);
                                                                        if (q < ini || p > fim) {
125
                                                            48
                                                                            return NEUTRAL;
126
                                                            49
127
                                                            50
       void build(vector<int> &v) {
                                                            51
                                                                        int e = 2*pos + 1;
           build(0, 0, n - 1, v);
129
                                                            52
                                                                        int d = 2*pos + 2;
130
                                                                        int m = ini + (fim - ini) / 2;
131
                                                            54
       void debug() {
                                                            55
132
           for (auto e : seg) {
                                                                        return f(query(e, ini, m, p, q), query(d, m +
133
               cout << e.max_seg << ' ' ' << e.pref << '</pre>
                                                                    1, fim, p, q));
134
        << e.suf << ' ' ' << e.sum << '\n';
135
                                                            58
           cout << '\n';
                                                                    void update(int pos, int ini, int fim, int id,
136
                                                            59
137
       }
                                                                   int val) {
                                                                        if (ini > id || fim < id) {</pre>
138 };
                                                            60
                                                                            return;
                                                            61
           Range Query Point Update
                                                            62
   9.10
                                                                        if (ini == id && fim == id) {
                                                            64
                                                                            seg[pos] = val;
 1 // Description:
 2 // Indexed at zero
 _3 // Query - get sum of elements from range (1, r)
                                                            67
                                                                            return:
                                                                        }
       inclusive
 _{4} // Update - update element at position id to a value ^{69}
                                                                        int e = 2*pos + 1;
                                                             70
       val
                                                                        int d = 2*pos + 2;
                                                            71
                                                                        int m = ini + (fim - ini) / 2;
 6 // Problem:
                                                             72
 7 // https://codeforces.com/edu/course/2/lesson/4/1/
       practice/contest/273169/problem/B
                                                            74
                                                                        update(e, ini, m, id, val);
                                                                        update(d, m + 1, fim, id, val);
                                                            75
                                                            76
 9 // Complexity:
                                                            77
                                                                        seg[pos] = f(seg[e], seg[d]);
_{10} // O(log n) for both query and update
                                                            78
12 // How to use:
                                                            79
                                                                   void build(int pos, int ini, int fim, vector<int>
13 // Segtree seg = Segtree(n);
                                                                    &v) {
14 // seg.build(v);
                                                                        if (ini == fim) {
                                                                            if (ini < (int)v.size()) {</pre>
16 // Notes
                                                                                seg[pos] = v[ini];
_{
m 17} // Change neutral element and f function to perform a ^{
m 83}
        different operation
                                                                            return:
                                                            85
                                                                        }
_{19} // If you want to change the operations to point
                                                            87
       query and range update
```

```
int e = 2*pos + 1;
                                                                      seg[e] = apply_lazy(seg[e], lazy[pos], m -
88
                                                           41
           int d = 2*pos + 2;
                                                                  ini + 1);
89
                                                                       seg[d] = apply_lazy(seg[d], lazy[pos], fim -
           int m = ini + (fim - ini) / 2;
90
                                                            42
91
           build(e, ini, m, v);
                                                            43
           build(d, m + 1, fim, v);
                                                                       lazy[pos] = NEUTRAL_LAZY;
93
                                                           44
                                                            45
           seg[pos] = f(seg[e], seg[d]);
95
                                                           46
                                                                  ftype f(ftype a, ftype b) {
96
                                                           47
                                                                       return a + b;
97
                                                           48
       ftype query(int p, int q) {
98
                                                           49
           return query(0, 0, n - 1, p, q);
99
                                                            50
100
                                                           51
                                                                   ftype query(int pos, int ini, int fim, int p, int
101
       void update(int id, int val) {
102
                                                           52
                                                                      propagate(pos, ini, fim);
           update(0, 0, n - 1, id, val);
103
                                                           53
104
                                                           54
                                                                       if (ini >= p && fim <= q) {
                                                                          return seg[pos];
105
                                                           55
106
       void build(vector<int> &v) {
           build(0, 0, n - 1, v);
107
                                                           57
                                                                       if (q < ini || p > fim) {
                                                           58
108
                                                           59
                                                                           return NEUTRAL;
109
       void debug() {
                                                           60
110
           for (auto e : seg) {
                                                           61
               cout << e << ' ';
                                                                       int e = 2*pos + 1;
112
                                                           62
                                                           63
                                                                       int d = 2*pos + 2;
113
           cout << '\n';</pre>
                                                                       int m = ini + (fim - ini) / 2;
114
                                                           64
115
                                                           65
116 };
                                                                       return f(query(e, ini, m, p, q), query(d, m +
                                                            66
                                                                   1, fim, p, q));
           Lazy Assignment To Segment
   9.11
                                                           67
                                                            68
                                                                  void update(int pos, int ini, int fim, int p, int
                                                           69
 const long long INF = 1e18+10;
                                                                   q, int val) {
                                                                      propagate(pos, ini, fim);
 3 typedef long long ftype;
                                                           70
                                                            71
                                                                       if (ini > q || fim < p) {
                                                            72
 5 struct Segtree {
       vector < ftype > seg;
                                                            73
                                                                           return;
       vector <ftype > lazy;
                                                                       7
                                                            74
                                                            75
       int n;
       const ftype NEUTRAL = 0;
                                                                       if (ini >= p && fim <= q) {
 9
       const ftype NEUTRAL_LAZY = -1; // Change to -INF 77
                                                                           lazy[pos] = apply_lazy(lazy[pos], val, 1)
10
       if there are negative numbers
                                                                           seg[pos] = apply_lazy(seg[pos], val, fim
11
                                                                   - ini + 1);
12
       Segtree(int n) {
           int sz = 1;
13
                                                                           return;
           // potencia de dois mais proxima
                                                            80
                                                                       }
           while (sz < n) sz *= 2;
15
           this ->n = sz;
                                                           82
16
                                                                       int e = 2*pos + 1;
                                                           83
17
                                                                       int d = 2*pos + 2;
           // numero de nos da seg
                                                           84
18
                                                                       int m = ini + (fim - ini) / 2;
           seg.assign(2*sz, NEUTRAL);
                                                           85
           lazy.assign(2*sz, NEUTRAL_LAZY);
20
                                                                       update(e, ini, m, p, q, val);
                                                           87
21
                                                                       update(d, m + 1, fim, p, q, val);
                                                            88
22
                                                            89
       ftype apply_lazy(ftype a, ftype b, int len) {
23
                                                                       seg[pos] = f(seg[e], seg[d]);
                                                            90
           if (b == NEUTRAL_LAZY) return a;
24
           if (a == NEUTRAL_LAZY) return b * len;
                                                            91
25
           else return b * len;
                                                            92
                                                                   void build(int pos, int ini, int fim, vector<int>
                                                            93
27
                                                                   &v) {
28
                                                                       if (ini == fim) {
       void propagate(int pos, int ini, int fim) {
29
           if (ini == fim) {
                                                                           // se a çãposio existir no array original
30
                                                                           // seg tamanho potencia de dois
               return;
                                                           96
           }
                                                                           if (ini < (int)v.size()) {</pre>
32
                                                                               seg[pos] = v[ini];
                                                           98
33
           int e = 2*pos + 1;
                                                           99
34
           int d = 2*pos + 2;
                                                                           return;
35
                                                           101
           int m = ini + (fim - ini) / 2;
37
                                                                       int e = 2*pos + 1;
           lazy[e] = apply_lazy(lazy[e], lazy[pos], 1); 103
                                                                       int d = 2*pos + 2;
           lazy[d] = apply_lazy(lazy[d], lazy[pos], 1); 104
```

int m = ini + (fim - ini) / 2;

39

```
106
                                                                  33
107
             build(e, ini, m, v);
             build(d, m + 1, fim, v);
108
                                                                  34
109
                                                                  35
             seg[pos] = f(seg[e], seg[d]);
111
                                                                  37
112
                                                                  38
        ftype query(int p, int q) {
113
                                                                  39
            return query (0, 0, n - 1, p, q);
114
                                                                 40
115
                                                                  41
116
                                                                  42
117
        void update(int p, int q, int val) {
                                                                  43
            update(0, 0, n - 1, p, q, val);
118
                                                                  44
119
120
                                                                  45
        void build(vector<int> &v) {
121
                                                                  46
122
            build(0, 0, n - 1, v);
                                                                  47
123
                                                                  48
        void debug() {
125
                                                                  50
            for (auto e : seg) {
                                                                  51
126
                 cout << e << '';
127
                                                                  52
                                                                  53
128
             cout << '\n';</pre>
             for (auto e : lazy) {
130
                                                                  55
                 cout << e << ' ';
                                                                  56
131
132
                                                                  57
            cout << '\n';</pre>
133
                                                                  58
             cout << '\n';</pre>
134
                                                                  59
        }
135
136 };
                                                                  60
```

9.12 Lazy Dynamic Implicit Sparse

```
1 // Description:
2 // Indexed at one
                                                            64
_{4} // When the indexes of the nodes are too big to be
       stored in an array
                                                            66
_{5} // and the queries need to be answered online so we
                                                            67
       can't sort the nodes and compress them
                                                            68
_{6} // we create nodes only when they are needed so there ^{69}
                                                            70
      'll be (Q*log(MAX)) nodes
_{7} // where Q is the number of queries and MAX is the
                                                            71
      maximum index a node can assume
                                                            72
                                                            73
_{9} // Query - get sum of elements from range (1, r)
      inclusive
                                                            76
10 // Update - update element at position id to a value
                                                            77
                                                            78
12 // Problem:
                                                            79
13 // https://oj.uz/problem/view/IZhO12_apple
                                                            80
                                                            81
15 // Complexity:
                                                            82
16 // O(log n) for both query and update
                                                            83
18 // How to use:
                                                            84
_{
m 19} // MAX is the maximum index a node can assume
                                                            85
                                                            86
20 // Create a default null node
_{21} // Create a node to be the root of the segtree
                                                            87
23 // Segtree seg = Segtree(MAX);
                                                            88
24
25 const int MAX = 1e9+10;
26 const long long INF = 1e18+10;
                                                            91
                                                            92
28 typedef long long ftype;
                                                            93
29
30 struct Segtree {
                                                            94
   vector<ftype> seg, d, e, lazy;
31
      const ftype NEUTRAL = 0;
```

```
const ftype NEUTRAL_LAZY = -1; // change to -INF
if the elements can be negative
int n:
Segtree(int n) {
    this ->n = n;
    create();
    create();
ftype apply_lazy(ftype a, ftype b, int len) {
    if (b == NEUTRAL_LAZY) return a;
    else return b * len; // change to a + b * len
 to add to an element instead of updating it
void propagate(int pos, int ini, int fim) {
    if (seg[pos] == 0) return;
    if (ini == fim) {
        return;
    int m = (ini + fim) >> 1;
    if (e[pos] == 0) e[pos] = create();
    if (d[pos] == 0) d[pos] = create();
   lazy[e[pos]] = apply_lazy(lazy[e[pos]], lazy[
pos], 1);
   lazy[d[pos]] = apply_lazy(lazy[d[pos]], lazy[
pos], 1);
    seg[e[pos]] = apply_lazy(seg[e[pos]], lazy[
pos], m - ini + 1);
    seg[d[pos]] = apply_lazy(seg[d[pos]], lazy[
pos], fim - m);
    lazy[pos] = NEUTRAL_LAZY;
ftype f(ftype a, ftype b) {
   return a + b;
ftype create() {
   seg.push_back(0);
    e.push_back(0);
    d.push_back(0);
    lazy.push_back(-1);
    return seg.size() - 1;
ftype query(int pos, int ini, int fim, int p, int
    propagate(pos, ini, fim);
    if (q < ini || p > fim) return NEUTRAL;
    if (pos == 0) return 0;
    if (p <= ini && fim <= q) return seg[pos];</pre>
    int m = (ini + fim) >> 1;
    return f(query(e[pos], ini, m, p, q), query(d
[pos], m + 1, fim, p, q));
void update(int pos, int ini, int fim, int p, int
 q, int val) {
    propagate(pos, ini, fim);
    if (ini > q || fim < p) {</pre>
        return:
    }
    if (ini >= p && fim <= q) {</pre>
        lazy[pos] = apply_lazy(lazy[pos], val, 1)
```

```
28 struct Segtree {
                                                                  vector<ftype> seg, d, e;
               seg[pos] = apply_lazy(seg[pos], val, fim 29
97
       - ini + 1);
                                                                  const ftype NEUTRAL = 0;
                                                           30
                                                                  int n;
                                                           31
98
99
                return;
                                                           32
           }
                                                                   Segtree(int n) {
100
                                                           33
                                                                       this ->n = n;
101
                                                           34
           int m = (ini + fim) >> 1:
102
                                                           35
103
                                                           36
           if (e[pos] == 0) e[pos] = create();
                                                                  ftype f(ftype a, ftype b) {
104
                                                           37
           update(e[pos], ini, m, p, q, val);
                                                                      return a + b;
105
                                                           38
106
                                                           39
           if (d[pos] == 0) d[pos] = create();
107
                                                           40
           update(d[pos], m + 1, fim, p, q, val);
                                                                   ftype create() {
                                                           41
108
                                                                       seg.push_back(0);
109
                                                           42
           seg[pos] = f(seg[e[pos]], seg[d[pos]]);
                                                                       e.push_back(0);
110
                                                           43
111
       }
                                                            44
                                                                       d.push_back(0);
                                                                       return seg.size() - 1;
112
                                                           45
       ftype query(int p, int q) {
113
           return query (1, 1, n, p, q);
114
                                                           47
                                                                   ftype query(int pos, int ini, int fim, int p, int
115
                                                           48
116
       void update(int p, int q, int val) {
                                                                       if (q < ini || p > fim) return NEUTRAL;
117
                                                           49
           update(1, 1, n, p, q, val);
                                                                       if (pos == 0) return 0;
                                                                       if (p <= ini && fim <= q) return seg[pos];</pre>
119
                                                           51
120 };
                                                                       int m = (ini + fim) >> 1;
                                                            52
                                                                       return f(query(e[pos], ini, m, p, q), query(d
                                                            53
                                                                   [pos], m + 1, fim, p, q));
   9.13 Persistent
                                                            54
                                                            55
 1 // Description:
                                                                   int update(int pos, int ini, int fim, int id, int
                                                            56
 _{2} // Persistent segtree allows for you to save the
                                                                   val) {
       different versions of the segtree between each
                                                                      int novo = create();
       update
 _{\rm 3} // Indexed at one
                                                                       seg[novo] = seg[pos];
                                                            59
 4 // Query - get sum of elements from range (1, r)
                                                                       e[novo] = e[pos];
                                                                       d[novo] = d[pos];
       inclusive
                                                            61
 _{5} // Update - update element at position id to a value _{62}
       val
                                                                       if (ini == fim) {
                                                                           seg[novo] = val;
                                                            64
 7 // Problem:
                                                                           return novo;
 8 // https://cses.fi/problemset/task/1737/
                                                                       }
                                                           66
                                                            67
10 // Complexity:
                                                            68
                                                                       int m = (ini + fim) >> 1;
_{11} // O(log n) for both query and update
                                                            69
12
                                                                       if (id <= m) e[novo] = update(e[novo], ini, m</pre>
13 // How to use:
                                                                   , id, val);
_{14} // vector<int> raiz(MAX); // vector to store the
                                                                       else d[novo] = update(d[novo], m + 1, fim, id
       roots of each version
                                                                   , val);
15 // Segtree seg = Segtree(INF);
                                                            72
16 // raiz[0] = seg.create(); // null node
                                                                       seg[novo] = f(seg[e[novo]], seg[d[novo]]);
                                                            73
17 // curr = 1; // keep track of the last version
                                                            74
                                                                       return novo;
19 // raiz[k] = seg.update(raiz[k], idx, val); //
                                                            76
       updating version k
                                                            77
20 // seg.query(raiz[k], l, r) // querying version k
                                                                  ftype query(int pos, int p, int q) {
                                                            78
21 // raiz[++curr] = raiz[k]; // create a new version
                                                                       return query(pos, 1, n, p, q);
                                                            79
       based on version k
                                                            80
                                                            81
23 const int MAX = 2e5+17;
                                                                   int update(int pos, int id, int val) {
                                                            82
24 const int INF = 1e9+17;
                                                           83
                                                                       return update(pos, 1, n, id, val);
                                                           84
26 typedef long long ftype;
                                                           85 };
```