

Notebook - Maratona de Programação

Lenhadoras de Segtree

Contents				4	Strings	7
					4.1 Kmp	7
1	Mat		2		4.2 Generate All Permutations	8
	1.1	Ceil	2		4.3 Generate All Sequences Length K	8
	1.2	To Decimal	2		4.4 Lcs	8
	1.3	Matrix Exponentiation	2		4.5 Trie	8
	1.4	Crt	3		4.6 Z-function	9
	1.5	Binary To Decimal	3			
	1.6	Fast Exponentiation	3	5	Misc	9
	1.7	Linear Diophantine Equation	3		5.1 Split	9
	1.8	Function Root	4		5.2 Int128	9
	1.9	Sieve Of Eratosthenes	4			
	1.10	Horner Algorithm	4	6	Graphs	9
		Multiplicative Inverse	4		6.1 Centroid Find	9
		Representation Arbitrary Base	4		6.2 Bipartite	9
		Set Operations	5		6.3 Prim	10
		Divisors	5		6.4 Ford Fulkerson Edmonds Karp	10
		Check If Bit Is On	5		6.5 Floyd Warshall	10
		Prime Factors	5		6.6 Lca	11
					6.7 Bellman Ford	12
2	\mathbf{DP}		5		6.8 Dinic	12
	2.1	Knapsack With Index	5		6.9 2sat	13
	2.2	Substr Palindrome	5		6.10 Find Cycle	15
	2.3	Edit Distance	6		6.11 Cycle Path Recovery	15
	2.4	Knapsack	6		6.12 Centroid Decomposition	16
	2.5	Digits	6		6.13 Tarjan Bridge	16
	2.6	Coins	6		6.14 Small To Large	17
	2.7	Minimum Coin Change	6		6.15 Tree Diameter	17
	2.8	Kadane	7		6.16 Dijkstra	17
					6.17 Kruskall	
3	Ten	plate	7			
	3.1	Template	7	7	Geometry	18
	3.2	Template Clean	7		7.1 2d	18

\mathbf{Alg}	orithms	21
8.1	Lis	21
8.2	Delta-encoding	21
8.3	Subsets	21
8.4	Binary Search Last True	21
8.5	Ternary Search	21
8.6	Binary Search First True	21
8.7	Biggest K	21
Data	a Structures	22
9.1	Ordered Set	22
9.2	Priority Queue	22
9.3	Dsu	23
9.4	Two Sets	23
9.5	Dynamic Implicit Sparse	24
9.6	Segtree2d	24
9.7	Minimum And Amount	26
9.8	Lazy Addition To Segment	26
9.9	Segment With Maximum Sum	28
9.10	Range Query Point Update	29
9.11	Lazy Assignment To Segment	29
9.12	Lazy Dynamic Implicit Sparse	30
9.13	Persistent	31
	8.1 8.2 8.3 8.4 8.5 8.6 8.7 Dat 9.1 9.2 9.3 9.4 9.5 9.6 9.7 9.8 9.9 9.10 9.11	8.2 Delta-encoding 8.3 Subsets 8.4 Binary Search Last True 8.5 Ternary Search 8.6 Binary Search First True 8.7 Biggest K Data Structures 9.1 Ordered Set 9.2 Priority Queue 9.3 Dsu 9.4 Two Sets 9.5 Dynamic Implicit Sparse 9.6 Segtree2d 9.7 Minimum And Amount 9.8 Lazy Addition To Segment 9.9 Segment With Maximum Sum

1 Math 38 // How to use: $39 // vector < vector < 11>> v = {{1, 1}, {1, 0}};$ 40 // Matriz transition = Matriz(v); 1.1 Ceil 41 // cout << fexp(transition, n)[0][1] << '\n'; 1 long long division_ceil(long long a, long long b) { 43 using ll = long long; return 1 + ((a - 1) / b); // if a != 0 45 const int MOD = 1e9+7; 3 } 46 1.2 To Decimal 47 struct Matriz{ vector < vector < 11 >> mat; 48 int rows, columns; const string digits { "0123456789 50 ABCDEFGHIJKLMNOPQRSTUVWXYZ" }; vector<ll> operator[](int i){ 51 52 return mat[i]; 3 long long to_decimal(const string& rep, long long 53 base) { long long n = 0; Matriz(vector < vector < 11 >> & matriz) { 55 mat = matriz; for (auto c : rep) { rows = mat.size(); 57 n *= base; columns = mat[0].size(); 58 n += digits.find(c); 59 60 Matriz(int row, int column, bool identity=false){ 61 return n; rows = row; columns = column; 62 12 } 63 mat.assign(rows, vector<11>(columns, 0)); 64 if(identity) { 1.3 Matrix Exponentiation for(int i = 0; i < min(rows, columns); i</pre> 65 ++) { mat[i][i] = 1; 1 // Description: 66 } $_{2}$ // Calculate the nth term of a linear recursion 67 } 68 4 // Example Fibonacci: 69 5 // Given a linear recurrence, for example fibonacci Matriz operator * (Matriz a) { 6 // F(n) = n, x <= 171 assert(columns == a.rows); 7 // F(n) = F(n - 1) + F(n - 2), x > 1vector < vector < 11 >> resp(rows, vector < 11 > (a. 73 $_{\rm 9}$ // The recurrence has two terms, so we can build a columns, 0)); matrix 2 x 1 so that for(int i = 0; i < rows; i++){</pre> $_{10}$ // n + 1 = transition * n 75 76 for (int j = 0; j < a.columns; j++) { for (int k = 0; k < a.rows; k++) { $_{12}$ // (2 x 1) = (2 x 2) * (2 x 1) 77 resp[i][j] = (resp[i][j] + (mat[i $_{13}$ // F(n) = a b * F(n - 1) 78 $_{14}$ // F(n - 1) c d F(n - 2)][k] * 1LL * a[k][j]) % MOD) % MOD; 79 } 16 // Another Example: } $_{\rm 17}$ // Given a grid 3 x n, you want to color it using 3 81 return Matriz(resp); distinct colors so that $_{18}$ // no adjacent place has the same color. In how many 83 different ways can you do that? Matriz operator + (Matriz a) { 19 // There are 6 ways for the first column to be assert(rows == a.rows && columns == a.columns colored using 3 distinct colors 86 20 // ans 6 ways using 2 equal colors and 1 distinct one vector < vector < ll >> resp(rows, vector < ll > (87 columns,0)); $_{22}$ // Adding another column, there are: for(int i = 0; i < rows; i++){</pre> 23 // 3 ways to go from 2 equal to 2 equal for(int j = 0; j < columns; j++){</pre> 89 24 // 2 ways to go from 2 equal to 3 distinct resp[i][j] = (resp[i][j] + mat[i][j] $_{25}$ // 2 ways to go from 3 distinct to 2 equal $_{26}$ // 2 ways to go from 3 distinct to 3 distinct + a[i][j]) % MOD; 91 $_{28}$ // So we star with matrix 6 6 and multiply it by the 92 return Matriz(resp); 93 transition 3 2 and get $18\ 12$ 6 6 2 2 95 }: 12 12 $_{ m 30}$ // the we can exponentiate this matrix to find the 97 Matriz fexp(Matriz base, 11 exponent){ nth column Matriz result = Matriz(base.rows, base.rows, 1); 98 while(exponent > 0){ 32 // Problem: 99 if(exponent & 1LL) result = result * base; 33 // https://cses.fi/problemset/task/1722/ 100 base = base * base; 101

9

10

35 // Complexity:

36 // O(log n)

102

103 104 exponent = exponent >> 1;

return result;

```
105
                                                           6 // }
                                                           7 // else if (a == 0) {
   1.4 Crt
                                                                if (c % b == 0 && y1 <= c / b && y2 >= c / b)
                                                           8 //
                                                                 ans = (x2 - x1 + 1);
                                                                   else ans = 0;
 1 ll crt(const vector < pair < ll, ll >> & vet) {
                                                          10 // }
       11 \text{ ans} = 0, 1cm = 1;
                                                          11 // else if (b == 0) {
       ll a, b, g, x, y;
                                                          12 //
                                                                if (c % a == 0 && x1 <= c / a && x2 >= c / a)
       for(const auto &p : vet) {
                                                               ans = (y2 - y1 + 1);
           tie(a, b) = p;
                                                          13 //
                                                                   else ans = 0;
           tie(g, x, y) = gcd(lcm, b);
                                                          14 // }
           if((a - ans) % g != 0) return -1; // no
       solution
                                                          16 // Careful when a or b are negative or zero
         ans = ans + x * ((a - ans) / g) % (b / g) *
                                                          _{18} // if (ans == -1) ans = find_all_solutions(a, b, c,
           lcm = lcm * (b / g);
 a
                                                                x1, x2, y1, y2);
           ans = (ans \% lcm + lcm) \% lcm;
10
                                                          19 // cout << ans << '\n';
11
       return ans:
12
                                                          21 // Problems:
13 }
                                                          22 // https://www.spoj.com/problems/CEQU/
                                                          23 // http://codeforces.com/problemsets/acmsguru/problem
         Binary To Decimal
                                                                /99999/106
                                                          _{25} // consider trivial case a or b is 0
 int binary_to_decimal(long long n) {
                                                          26 int gcd(int a, int b, int& x, int& y) {
    int dec = 0, i = 0, rem;
                                                          27
                                                                 if (b == 0) {
                                                                     x = 1;
     while (n!=0) {
                                                          28
                                                                     y = 0;
      rem = n \% 10;
                                                          29
       n /= 10;
                                                                     return a;
                                                          30
                                                                 }
      dec += rem * pow(2, i);
                                                          31
       ++i;
                                                          32
                                                                 int x1, y1;
                                                                int d = gcd(b, a % b, x1, y1);
                                                          33
                                                                 x = y1;
                                                          34
10
    return dec:
                                                          35
                                                                 y = x1 - y1 * (a / b);
                                                                 return d:
                                                          36
12 }
                                                          37 }
13
14 long long decimal_to_binary(int n) {
                                                          38
   long long bin = 0;
                                                          39 // x and y are one solution and g is the gcd, all
15
    int rem, i = 1;
                                                                passed as reference
                                                          _{40} // minx <= x <= maxx miny <= y <= maxy
17
    while (n!=0) {
                                                          41 bool find_any_solution(int a, int b, int c, int &x0,
18
      rem = n \% 2;
                                                                int &y0, int &g) {
19
      n /= 2;
                                                                 g = gcd(abs(a), abs(b), x0, y0);
20
      bin += rem * i;
                                                          43
                                                                 if (c % g) {
       i *= 10;
                                                                    return false;
                                                          44
22
                                                          45
                                                                 }
23
24
                                                          46
     return bin;
                                                          47
                                                                x0 *= c / g;
25
                                                                 y0 *= c / g;
26 }
                                                          48
                                                          49
                                                                 if (a < 0) x0 = -x0;
   1.6 Fast Exponentiation
                                                          50
                                                                 if (b < 0) y0 = -y0;
                                                                 return true;
                                                          51
                                                          52 }
 1 ll fexp(ll b, ll e, ll mod) {
                                                          53
      ll res = 1;
                                                          54 void shift_solution(int & x, int & y, int a, int b,
       b \% = mod;
 3
                                                                int cnt) {
       while(e){
                                                                x += cnt * b;
                                                          55
          if(e & 1LL)
                                                                 y -= cnt * a;
                                                          56
              res = (res * b) % mod;
                                                          57 }
           e = e >> 1LL;
           b = (b * b) \% mod;
                                                          59 // return number of solutions in the interval
       }
 9
                                                          60 int find_all_solutions(int a, int b, int c, int minx,
       return res;
10
                                                                 int maxx, int miny, int maxy) {
11 }
                                                                 int x, y, g;
                                                          61
                                                          62
                                                                 if (!find_any_solution(a, b, c, x, y, g))
   1.7 Linear Diophantine Equation
                                                                    return 0:
                                                          63
                                                                 a /= g;
 _1 // int a, b, c, x1, x2, y1, y2; cin >> a >> b >> c >> ^{65}
                                                                 b /= g;
                                                          66
        x1 >> x2 >> y1 >> y2;
                                                                 int sign_a = a > 0 ? +1 : -1;
 _2 // int ans = -1;
                                                          67
                                                                int sign_b = b > 0 ? +1 : -1;
 _3 // if (a == 0 && b == 0) {
                                                          68
 4 //
         if (c != 0) ans = 0;
          else ans = (x2 - x1 + 1) * (y2 - y1 + 1);
                                                          70
                                                                 shift_solution(x, y, a, b, (minx - x) / b);
```

```
if (x < minx)
                                                                 for (int i = 2; i < MAX; i++) {
71
                                                           6
72
           shift_solution(x, y, a, b, sign_b);
                                                           7
                                                                     if (is_prime[i]) {
       if (x > maxx)
73
                                                                         primes.push_back(i);
74
          return 0;
       int lx1 = x;
                                                                          for (int j = i + i; j < MAX; j += i)
                                                                              is_prime[j] = false;
76
                                                          11
       shift_solution(x, y, a, b, (maxx - x) / b);
                                                                     }
                                                          12
       if (x > maxx)
78
                                                          13
          shift_solution(x, y, a, b, -sign_b);
                                                          14 }
79
       int rx1 = x;
80
                                                                    Horner Algorithm
                                                             1.10
81
       shift_solution(x, y, a, b, -(miny - y) / a);
       if (y < miny)</pre>
83
                                                           1 // Description:
           shift_solution(x, y, a, b, -sign_a);
                                                           _2 // Evaluates y = f(x)
84
85
       if (y > maxy)
          return 0;
86
                                                           4 // Problem:
87
       int 1x2 = x;
                                                           5 // https://onlinejudge.org/index.php?option=
88
                                                                 com_onlinejudge&Itemid=8&page=show_problem&
       shift_solution(x, y, a, b, -(maxy - y) / a);
                                                                 problem=439
90
       if (y > maxy)
           shift_solution(x, y, a, b, sign_a);
                                                           7 // Complexity:
91
       int rx2 = x;
92
                                                           8 // O(n)
93
       if (1x2 > rx2)
                                                          10 using polynomial = std::vector<int>;
          swap(1x2, rx2);
95
                                                          11
       int 1x = max(1x1, 1x2);
96
                                                          12 polynomial p \{6, -5, 2\}; // p(x) = x^2 - 5x + 6;
       int rx = min(rx1, rx2);
97
                                                          13
98
                                                          14 int degree(const polynomial& p) {
       if (lx > rx)
99
                                                              return p.size() - 1;
                                                          15
          return 0:
100
                                                          16 }
       return (rx - lx) / abs(b) + 1;
101
                                                          17
102 }
                                                          18 int evaluate(const polynomial& p, int x) {
                                                              int y = 0, N = degree(p);
       Function Root
                                                               for (int i = N; i >= 0; --i) {
                                                              y *= x;
                                                          22
 const ld EPS1 = 1e-9; // iteration precision error
                                                                 y += p[i];
                                                          23
 2 const ld EPS2 = 1e-4; // output precision error
                                                          24
 4 ld f(ld x) {
                                                               return y;
    // \exp(-x) == e^{-x}
     return p * exp(-x) + q * sin(x) + r * cos(x) + s * 27 }
       tan(x) + t * x * x + u;
                                                             1.11 Multiplicative Inverse
                                                           1 ll extend_euclid(ll a, ll b, ll &x, ll &y) {
 9 ld root(ld a, ld b) {
                                                           2
                                                                 if (a == 0)
    while (b - a >= EPS1) {
                                                                 {
      1d c = (a + b) / 2.0;
                                                           3
11
                                                                     x = 0; y = 1;
                                                           4
       1d y = f(c);
                                                           5
                                                                     return b:
13
                                                           6
       if (y < 0) b = c;
14
                                                                 11 x1, y1;
                                                           7
      else a = c;
15
                                                                 11 d = extend_euclid(b%a, a, x1, y1);
                                                           8
16
                                                                 x = y1 - (b / a) * x1;
                                                           9
17
                                                                 y = x1;
                                                          10
     return (a + b) / 2;
18
                                                          11
                                                                 return d;
19 }
                                                          12 }
20
                                                          13
21 int main() {
                                                          14 // gcd(a, m) = 1 para existir solucao
   ld ans = root(0, 1);
                                                          _{15} // ax + my = 1, ou a*x = 1 (mod m)
    if (abs(f(ans)) <= EPS2) cout << fixed <<</pre>
                                                          16 ll inv_gcd(ll a, ll m) { // com gcd
      setprecision(4) << ans << '\n';</pre>
     else cout << "No solution\n";</pre>
                                                          17 11 x, y;
                                                               extend_euclid(a, m, x, y);
                                                          18
25
                                                               return (((x \% m) + m) \%m);
                                                          19
     return 0;
26
                                                          20 }
                                                          22 ll inv(ll a, ll phim) { // com phi(m), se m for primo
         Sieve Of Eratosthenes
                                                                  entao phi(m) = p-1
                                                              11 e = phim - 1;
 1 vector < bool > is_prime(MAX, true);
                                                               return fexp(a, e, MOD);
                                                          24
 vector < int > primes;
```

25 }

4 void sieve() {

is_prime[0] = is_prime[1] = false;

Representation Arbitrary Base

```
1 const string digits { "0123456789
                                                                     n /= p;
      ABCDEFGHIJKLMNOPQRSTUVWXYZ" };
                                                           8
                                                                     expoente++;
                                                           9
3 string representation(int n, int b) {
                                                                   ans.emplace_back(p, expoente);
                                                          10
   string rep;
                                                          11
                                                               }
                                                          12
                                                               if(n > 1) ans.emplace_back(n, 1);
                                                          13
     rep.push_back(digits[n % b]);
                                                          14
                                                               return ans:
      n /= b;
    } while (n);
10
                                                                  DP
    reverse(rep.begin(), rep.end());
                                                                  Knapsack With Index
    return rep;
13
14 }
                                                           void knapsack(int W, int wt[], int val[], int n) {
         Set Operations
                                                                 int i, w;
                                                                 int K[n + 1][W + 1];
1 // Complexity;
_{2} // O(n * m) being n and m the sizes of the two sets
                                                                 for (i = 0; i \le n; i++) {
_3 // 2*(count1+count2)-1 (where countX is the distance _6
                                                                     for (w = 0; w \le W; w++) {
                                                                          if (i == 0 || w == 0)
      between firstX and lastX):
                                                                             K[i][w] = 0;
5 vector<int> res;
                                                                          else if (wt[i - 1] <= w)
_{6} set_union(s1.begin(), s1.end(), s2.begin(), s2.end(), _{10}
                                                                             K[i][w] = max(val[i - 1] +
       inserter(res, res.begin()));
                                                                                  K[i - 1][w - wt[i - 1]], K[i -
7 set_intersection(s1.begin(), s1.end(), s2.begin(), s2
                                                                 1][w]);
      .end(), inserter(res, res.begin()));
                                                                          else
_{8} // present in the first set, but not in the second
                                                                              K[i][w] = K[i - 1][w];
9 set_difference(s1.begin(), s1.end(), s2.begin(), s2. 14
                                                                     }
      end(), inserter(res, res.begin()));
                                                          15
_{\rm 10} // present in one of the sets, but not in the other
set_symmetric_difference(s1.begin(), s1.end(), s2.
                                                                 int res = K[n][W];
                                                          17
      begin(), s2.end(), inserter(res, res.begin()));
                                                                 cout << res << endl;</pre>
                                                          19
  1.14 Divisors
                                                                 for (i = n; i > 0 && res > 0; i--) {
                                                          21
                                                                     if (res == K[i - 1][w])
                                                          22
1 vector < long long > all_divisors(long long n) {
                                                          23
                                                                         continue;
    vector <long long > ans;
                                                                     else {
                                                          24
    for(long long a = 1; a*a <= n; a++){
                                                                         cout << " " << wt[i - 1] ;</pre>
      if(n \% a == 0) {
                                                                         res = res - val[i - 1];
                                                          26
        long long b = n / a;
                                                                          w = w - wt[i - 1];
        ans.push_back(a);
                                                                     }
                                                          28
        if(a != b) ans.push_back(b);
                                                          29
                                                          30 }
    }
9
                                                          31
    sort(ans.begin(), ans.end());
10
                                                          32 int main()
    return ans;
                                                          33 {
12 }
                                                                 int val[] = { 60, 100, 120 };
                                                          34
                                                          35
                                                                 int wt[] = { 10, 20, 30 };
  1.15 Check If Bit Is On
                                                                 int W = 50;
                                                          36
                                                                 int n = sizeof(val) / sizeof(val[0]);
1 // msb de 0 é undefined
                                                          38
2 #define msb(n) (32 - __builtin_clz(n))
3 // #define msb(n) (64 - __builtin_clz11(n) )
                                                          39
                                                                 knapsack(W, wt, val, n);
                                                          40
4 // popcount
                                                                 return 0;
                                                          41
5 // turn bit off
                                                          42 }
                                                                   Substr Palindrome
7 bool bit_on(int n, int bit) {
      if(1 & (n >> bit)) return true;
      else return false;
                                                           1 // êvoc deve informar se a substring de S formada
10 }
                                                                 pelos elementos entre os indices i e j
                                                           _{2} // \acute{e} um palindromo ou \~{a}no.
  1.16 Prime Factors
                                                           4 char s[MAX];
1 vector < pair < long long, int >> fatora(long long n) {
                                                           5 int calculado[MAX][MAX]; // inciado com false, ou 0
    vector < pair < long long, int >> ans;
                                                           6 int tabela[MAX][MAX];
    for(long long p = 2; p*p <= n; p++) {
      if(n \% p == 0) {
                                                           8 int is_palin(int i, int j){
```

10

int expoente = 0;

while (n % p == 0) {

5

9 if(calculado[i][j]){

return tabela[i][j];

```
dp[i][j] = dp[i-1][j];
1.1
                                                           11
12
    if(i == j) return true;
                                                           12
                                                                     }
    if(i + 1 == j) return s[i] == s[j];
                                                                 }
13
                                                           13
                                                                 return dp[n][m];
14
                                                           14
    int ans = false;
                                                           15 }
    if(s[i] == s[j]){
16
                                                                  Digits
      if(is_palin(i+1, j-1)){
17
        ans = true;
18
19
                                                           _{\rm 1} // achar a quantidade de numeros menores que R que
20
                                                                 possuem no maximo 3 digitos nao nulos
    calculado[i][j] = true;
21
                                                           2 // a ideia eh utilizar da ordem lexicografica para
22
    tabela[i][j] = ans;
                                                                 checar isso pois se temos por exemplo
23
    return ans;
                                                           _{\rm 3} // o numero 8500, a gente sabe que se pegarmos o
                                                                 numero 7... qualquer digito depois do 7
                                                           _4 // sera necessariamente menor q 8500
       Edit Distance
  2.3
                                                           6 string r;
                                                           7 int tab[20][2][5];
1 // Description:
2 // Minimum number of operations required to transform
                                                           _{9} // i - digito de R
       a string into another
                                                           _{10} // menor - ja pegou um numero menor que um digito de
3 // Operations allowed: add character, remove
      character, replace character
                                                           _{11} // qt - quantidade de digitos nao nulos
                                                           12 int dp(int i, bool menor, int qt){
5 // Parameters:
                                                                 if(qt > 3) return 0;
_{6} // str1 - string to be transformed into str2
                                                                 if(i >= r.size()) return 1;
7 // str2 - string that str1 will be transformed into
                                                           14
                                                                 if(tab[i][menor][qt] != -1) return tab[i][menor][
8 // m - size of str1
                                                           15
9 // n - size of str2
                                                           16
11 // Problem:
                                                                 int dr = r[i] - '0';
                                                           17
                                                                 int res = 0;
12 // https://cses.fi/problemset/task/1639
                                                           18
                                                                 for(int d = 0; d <= 9; d++) {
14 // Complexity:
                                                           20
                                                                      int dnn = qt + (d > 0);
                                                           21
15 // 0(m \times n)
                                                                      if(menor == true) {
                                                           22
                                                                          res += dp(i+1, true, dnn);
17 // How to use:
                                                           23
                                                                      }
18 // memset(dp, -1, sizeof(dp));
                                                           25
                                                                      else if(d < dr) {
19 // string a, b;
                                                                          res += dp(i+1, true, dnn);
_{20} // edit_distance(a, b, (int)a.size(), (int)b.size()); ^{26}
                                                                      else if(d == dr) {
22 // Notes:
                                                           28
_{\rm 23} // Size of dp matriz is m x n
                                                                          res += dp(i+1, false, dnn);
                                                           30
25 int dp[MAX][MAX];
                                                           32
                                                                  return tab[i][menor][qt] = res;
27 int edit_distance(string &str1, string &str2, int m, 33
      int n) {
      if (m == 0) return n;
                                                             2.6 Coins
      if (n == 0) return m;
29
30
      if (dp[m][n] != -1) return dp[m][n];
31
                                                           1 int tb[1005];
32
      if (str1[m - 1] == str2[n - 1]) return dp[m][n] = 3 vector <int> moedas;
33
       edit_distance(str1, str2, m - 1, n - 1);
      return dp[m][n] = 1 + min({edit_distance(str1,
34
                                                           5 int dp(int i){
      str2, m, \hat{n} - 1), edit_distance(str1, str2, m - 1, \hat{i} if(\hat{i} >= n)
       n), edit_distance(str1, str2, m - 1, n - 1)}); 7
35 }
                                                               if(tb[i] != -1)
                                                                 return tb[i];
  2.4 Knapsack
                                                               tb[i] = max(dp(i+1), dp(i+2) + moedas[i]);
                                                           11
                                                           12
                                                               return tb[i];
int val[MAXN], peso[MAXN], dp[MAXN][MAXS];
                                                           13
                                                           14
3 int knapsack(int n, int m){ // n Objetos | Peso max
                                                           15 int main(){
      for(int i=0;i<=n;i++){</pre>
                                                              memset(tb,-1,sizeof(tb));
         for(int j=0; j \le m; j++){
                                                           16
               if(i==0 \text{ or } j==0)
                   dp[i][j] = 0;
                                                                   Minimum Coin Change
                                                             2.7
               else if(peso[i-1]<=j)</pre>
                  dp[i][j] = max(val[i-1]+dp[i-1][j-1]
      peso[i-1]], dp[i-1][j]);
                                                           1 int n;
              else
                                                           vector <int > valores;
```

```
4 int tabela[1005];
6 int dp(int k){
   if(k == 0) {
     return 0:
   if(tabela[k] != -1)
10
     return tabela[k];
11
   int melhor = 1e9;
    for(int i = 0; i < n; i++){
13
     if(valores[i] <= k)</pre>
15
        melhor = min(melhor,1 + dp(k - valores[i]));
16
   return tabela[k] = melhor;
```

2.8 Kadane

```
_{1} // achar uma subsequencia continua no array que a
      soma seja a maior possivel
2 // nesse caso vc precisa multiplicar exatamente 1
      elemento da subsequencia
3 // e achar a maior soma com isso
5 int n, x, arr[MAX], tab[MAX][2]; // tab[maior
      resposta no intervalo][foi multiplicado ou ano]
7 int dp(int i, bool mult) {
      if (i == n-1) {
          if (!mult) return arr[n-1]*x;
9
          return arr[n-1];
10
11
      if (tab[i][mult] != -1) return tab[i][mult];
12
      int res;
14
15
      if (mult) {
16
          res = max(arr[i], arr[i] + dp(i+1, 1));
19
      else {
          res = max({
              arr[i]*x,
21
              arr[i]*x + dp(i+1, 1),
22
              arr[i] + dp(i+1, 0)
          });
24
25
26
27
      return tab[i][mult] = res;
28 }
29
30 int main() {
31
      memset(tab, -1, sizeof(tab));
33
      int ans = -00;
34
      for (int i = 0; i < n; i++) {
35
          ans = max(ans, dp(i, 0));
36
38
      return 0;
39
40 }
41
44 int ans = a[0], ans_1 = 0, ans_r = 0;
45 int sum = 0, minus_pos = -1;
47 for (int r = 0; r < n; ++r) {
   sum += a[r];
48
      if (sum > ans) {
          ans = sum;
50
          ans_l = minus_pos + 1;
51
```

3 Template

3.1 Template

```
1 #include <bits/stdc++.h>
2 using namespace std;
 4 #define int long long
 5 #define optimize std::ios::sync_with_stdio(false);
       cin.tie(NULL);
6 #define vi vector<int>
7 #define ll long long
8 #define pb push_back
9 #define mp make_pair
10 #define ff first
11 #define ss second
12 #define pii pair <int, int>
13 #define MOD 100000007
_{14} #define sqr(x) ((x) * (x))
#define all(x) (x).begin(), (x).end()
16 #define FOR(i, j, n) for (int i = j; i < n; i++)
17 #define qle(i, n) (i == n ? "\n" : "
18 #define endl "\n"
19 const int 00 = 1e9;
20 const int MAX = 1e6;
22 int32_t main(){ optimize;
23
       return 0;
25 }
```

3.2 Template Clean

```
1 // Notes:
2 // Compile and execute
3 // g++ teste.cpp -o teste -std=c++17
4 // ./teste < teste.txt
6 // Print with precision
7 // cout << fixed << setprecision(12) << value << endl
9 // File as input and output
10 // freopen("input.txt", "r", stdin);
11 // freopen("output.txt", "w", stdout);
13 #include <bits/stdc++.h>
14 using namespace std;
15
16 int main() {
    ios::sync_with_stdio(false);
17
      cin.tie(NULL);
18
20
21
22
      return 0:
23 }
```

4 Strings

4.1 Kmp

```
vector <int > prefix_function(string s) {
                                                                     LCS_{table[i][j]} = LCS_{table[i - 1][j - 1]} +
                                                          18
      int n = (int)s.length();
                                                                 1;
      vector < int > pi(n);
                                                          19
                                                                   else
      for (int i = 1; i < n; i++) {
                                                                     LCS_table[i][j] = max(LCS_table[i - 1][j],
                                                          20
          int j = pi[i-1];
                                                                 LCS_table[i][j - 1]);
          while (j > 0 && s[i] != s[j])
                                                          21
              j = pi[j-1];
                                                          22
           if (s[i] == s[j])
                                                          23
               j++;
                                                               int index = LCS_table[m][n];
                                                          24
          pi[i] = j;
                                                               char lcsAlgo[index + 1];
10
                                                          25
      }
                                                               lcsAlgo[index] = '\0';
11
                                                          26
12
      return pi;
                                                          27
13 }
                                                               int i = m, j = n;
                                                          28
                                                               while (i > 0 \&\& j > 0) {
                                                          29
  4.2 Generate All Permutations
                                                                 if (s1[i - 1] == s2[j - 1]) {
                                                          30
                                                                   lcsAlgo[index - 1] = s1[i - 1];
                                                          31
vector < string > generate_permutations(string s) {
                                                                   j--;
                                                          33
      int n = s.size():
                                                                   index --;
      vector<string> ans;
3
                                                          35
                                                          36
      sort(s.begin(), s.end());
                                                                 else if (LCS_table[i - 1][j] > LCS_table[i][j -
                                                          37
                                                                 11)
                                                                   i - - ;
          ans.push_back(s);
                                                                 else
                                                          39
      } while (next_permutation(s.begin(), s.end()));
                                                          40
10
                                                          41
      return ans;
11
                                                          42
12 }
                                                               return lcsAlgo;
                                                          43
                                                          44 }
  4.3 Generate All Sequences Length K
                                                                   Trie
1 // gera todas as ípossveis êsequncias usando as letras
       em set (de comprimento n) e que tenham tamanho k
                                                           1 const int K = 26;
2 // sequence = ""
3 vector < string > generate_sequences(char set[], string
                                                           3 struct Vertex {
      sequence, int n, int k) {
                                                                 int next[K];
     if (k == 0){
                                                                 bool output = false;
         return { sequence };
                                                                 int p = -1;
6
                                                                 char pch;
                                                                 int link = -1;
     vector<string> ans;
                                                                 int go[K];
9
     for (int i = 0; i < n; i++) {
       auto aux = generate_sequences(set, sequence + 11
set[i], n, k - 1);
                                                                 Vertex(int p=-1, char ch='$') : p(p), pch(ch) {
                                                                     fill(begin(next), end(next), -1);
          ans.insert(ans.end(), aux.begin(), aux.end())
                                                                     fill(begin(go), end(go), -1);
           // for (auto e : aux) ans.push_back(e);
12
                                                          15 };
     }
13
                                                          16
14
                                                          17 vector < Vertex > t(1):
     return ans;
                                                          18
16 }
                                                             void add_string(string const& s) {
                                                          19
                                                                 int v = 0:
                                                          20
  4.4 Lcs
                                                                 for (char ch : s) {
                                                          21
                                                                     int c = ch - 'a';
                                                          22
1 // Description:
                                                                     if (t[v].next[c] == -1) {
                                                          23
2 // Finds the longest common subsquence between two
                                                                         t[v].next[c] = t.size();
                                                                         t.emplace_back(v, ch);
      string
                                                          25
                                                                     }
4 // Problem:
                                                          27
                                                                     v = t[v].next[c];
5 // https://codeforces.com/gym/103134/problem/B
                                                          28
                                                          29
                                                                 t[v].output = true;
7 // Complexity:
                                                          30 }
_8 // _0(mn) where m and n are the length of the strings _{31}
                                                          32 int go(int v, char ch);
10 string lcsAlgo(string s1, string s2, int m, int n) { 33
    int LCS_table[m + 1][n + 1];
11
                                                          34 int get_link(int v) {
                                                                 if (t[v].link == -1) {
12
                                                          35
                                                                     if (v == 0 || t[v].p == 0)
    for (int i = 0; i \le m; i++) {
     for (int j = 0; j <= n; j++) {
                                                                         t[v].link = 0;
14
                                                          37
        if (i == 0 || i == 0)
                                                                     else
15
          LCS_table[i][j] = 0;
                                                                         t[v].link = go(get_link(t[v].p), t[v].pch
16
                                                          39
        else if (s1[i - 1] == s2[j - 1])
                                                                 );
17
```

```
}
                                                                     ch = getchar();
40
                                                          10
41
      return t[v].link;
                                                          11
                                                                 }
42 }
                                                          12
                                                                 return x * f;
                                                          13 }
43
44 int go(int v, char ch) {
                                                          14 void print(__int128 x) {
      int c = ch - 'a';
                                                                 if (x < 0) {
45
                                                          15
      if (t[v].go[c] == -1) {
                                                                     putchar('-');
46
                                                          16
          if (t[v].next[c] != -1)
                                                                     x = -x;
47
                                                          17
              t[v].go[c] = t[v].next[c];
48
                                                          18
           else
                                                                 if (x > 9) print(x / 10);
              t[v].go[c] = v == 0 ? 0 : go(get_link(v), 20
                                                                 putchar(x % 10 + '0');
50
       ch);
      }
51
      return t[v].go[c];
52
                                                                  Graphs
53 }
                                                             6.1 Centroid Find
  4.6 Z-function
                                                           1 // Description:
1 vector<int> z_function(string s) {
                                                           2 // Indexed at zero
      int n = (int) s.length();
                                                           _{\rm 3} // Find a centroid, that is a node such that when it
      vector < int > z(n);
                                                                is appointed the root of the tree,
      for (int i = 1, l = 0, r = 0; i < n; ++i) {
                                                           _4 // each subtree has at most floor(n/2) nodes.
          if (i \le r)
              z[i] = min (r - i + 1, z[i - 1]);
                                                           6 // Problem:
           while (i + z[i] < n && s[z[i]] == s[i + z[i]]
                                                           7 // https://cses.fi/problemset/task/2079/
      ]])
               ++z[i];
                                                           9 // Complexity:
           if (i + z[i] - 1 > r)
9
                                                          10 // O(n)
              1 = i, r = i + z[i] - 1;
10
                                                          11
11
                                                          _{12} // How to use:
12
      return z;
                                                          13 // get_subtree_size(0);
13 }
                                                          14 // cout << get_centroid(0) + 1 << endl;</pre>
       Misc
                                                          16 int n;
                                                          17 vector < int > adj [MAX];
  5.1 Split
                                                          18 int subtree_size[MAX];
                                                          20 int get_subtree_size(int node, int par = -1) {
vector<string> split(string txt, char key = ' '){
                                                             int &res = subtree_size[node];
      vector<string> ans;
                                                          22
                                                              res = 1:
                                                          23
                                                               for (int i : adj[node]) {
      string palTemp = "";
                                                                if (i == par) continue;
                                                          24
      for(int i = 0; i < txt.size(); i++){</pre>
                                                                 res += get_subtree_size(i, node);
                                                          25
                                                               }
           if(txt[i] == key){
                                                          27
                                                              return res;
               if(palTemp.size() > 0){
                                                          28 }
                   ans.push_back(palTemp);
                   palTemp = "";
10
                                                          30 int get_centroid(int node, int par = -1) {
              }
11
                                                              for (int i : adj[node]) {
                                                          31
          } else{
                                                                 if (i == par) continue;
                                                          32
               palTemp += txt[i];
13
                                                          33
14
           }
                                                                 if (subtree_size[i] * 2 > n) { return
                                                          34
                                                                 get_centroid(i, node); }
16
                                                               }
                                                          35
17
                                                          36
                                                               return node;
      if(palTemp.size() > 0)
18
                                                          37 }
           ans.push_back(palTemp);
                                                          38
20
                                                          39 int main() {
      return ans;
                                                          40
                                                               cin >> n;
22 }
                                                               for (int i = 0; i < n - 1; i++) {
                                                          41
                                                          42
                                                                 int u, v; cin >> u >> v;
  5.2 Int128
                                                                 u--: v--:
                                                          43
                                                                 adj[u].push_back(v);
                                                          44
1 __int128 read() {
                                                          45
                                                                 adj[v].push_back(u);
      _{-int128} x = 0, f = 1;
                                                          46
      char ch = getchar();
                                                          47
      while (ch < '0' || ch > '9') {
                                                               get_subtree_size(0);
                                                          48
          if (ch == '-') f = -1;
                                                               cout << get_centroid(0) + 1 << endl;</pre>
          ch = getchar();
                                                          50 }
      while (ch >= '0' && ch <= '9') {
                                                             6.2
                                                                   Bipartite
```

x = x * 10 + ch - '0';

```
1 const int NONE = 0, BLUE = 1, RED = 2;
                                                                           if (adj[v][to] < min_e[to].w)</pre>
                                                           33
vector < vector < int >> graph (100005);
                                                            34
                                                                               min_e[to] = {adj[v][to], v};
3 vector < bool > visited(100005);
                                                                       }
                                                            35
4 int color [100005];
                                                            36
                                                            37
6 bool bfs(int s = 1){
                                                                   cout << total_weight << endl;</pre>
                                                            38
                                                            39 }
       queue <int> q;
       q.push(s);
9
                                                                    Ford Fulkerson Edmonds Karp
       color[s] = BLUE;
10
11
                                                            1 // Description:
12
       while (not q.empty()){
                                                            _{2} // Obtains the maximum possible flow rate given a
13
          auto u = q.front(); q.pop();
                                                                  network. A network is a graph with a single
14
                                                                  source vertex and a single sink vertex in which
           for (auto v : graph[u]){
                                                                  each edge has a capacity
               if (color[v] == NONE){
16
                    color[v] = 3 - color[u];
                                                            4 // Complexity:
18
                   q.push(v);
                                                            _{5} // O(V * E^2) where V is the number of vertex and E
               }
                                                                  is the number of edges
               else if (color[v] == color[u]){
20
                   return false;
21
                                                            7 int n;
22
                                                            8 vector < vector < int >> capacity;
           }
23
                                                            9 vector < vector < int >> adj;
25
                                                            int bfs(int s, int t, vector<int>& parent) {
26
       return true;
                                                                   fill(parent.begin(), parent.end(), -1);
27 }
                                                           12
                                                            13
                                                                   parent[s] = -2;
                                                                  queue <pair <int, int >> q;
29 bool is_bipartite(int n){
                                                            14
                                                                  q.push({s, INF});
30
                                                            16
31
       for (int i = 1; i <= n; i++)
           if (color[i] == NONE and not bfs(i))
                                                           17
                                                                   while (!q.empty()) {
32
                                                                      int cur = q.front().first;
               return false;
                                                           18
33
                                                                       int flow = q.front().second;
                                                            19
                                                                       q.pop();
                                                            20
      return true:
35
36 }
                                                           21
                                                            22
                                                                       for (int next : adj[cur]) {
  6.3 Prim
                                                                           if (parent[next] == -1 && capacity[cur][
                                                            23
                                                                   nextl) {
                                                                                parent[next] = cur;
1 int n;
                                                                                int new_flow = min(flow, capacity[cur
2 vector < vector < int >> adj; // adjacency matrix of graph 25
                                                                  ][next]);
_{3} const int INF = 1000000000; // weight INF means there
                                                                                if (next == t)
       is no edge
                                                                                    return new_flow;
                                                            27
                                                                                q.push({next, new_flow});
                                                            28
5 struct Edge {
                                                                           }
                                                            29
      int w = INF, to = -1;
6
                                                                       }
7 };
                                                                  }
                                                           31
                                                           32
9 void prim() {
                                                                  return 0;
                                                           33
       int total_weight = 0;
10
                                                           34 }
       vector < bool > selected(n, false);
11
                                                           35
       vector < Edge > min_e(n);
12
                                                           36 int maxflow(int s, int t) {
       min_e[0].w = 0;
13
                                                           37
                                                                   int flow = 0;
14
                                                                   vector < int > parent(n);
       for (int i=0; i < n; ++i) {
                                                           38
1.5
                                                                   int new_flow;
           int v = -1;
16
           for (int j = 0; j < n; ++ j) {
17
             if (!selected[j] && (v == -1 || min_e[j]. 41
                                                                   while (new_flow = bfs(s, t, parent)) {
18
                                                                      flow += new_flow;
       w < min_e[v].w)
                                                                       int cur = t;
                                                            43
19
                   v = j;
                                                                       while (cur != s) {
20
                                                                           int prev = parent[cur];
                                                            45
21
                                                                           capacity[prev][cur] -= new_flow;
                                                            46
           if (min_e[v].w == INF) {
22
                                                                           capacity[cur][prev] += new_flow;
                                                            47
               cout << "No MST!" << endl;</pre>
                                                                           cur = prev;
               exit(0);
                                                            48
24
                                                                       }
           }
                                                                  }
                                                            50
26
                                                            51
           selected[v] = true;
                                                            52
                                                                   return flow;
           total_weight += min_e[v].w;
                                                            53 }
           if (min_e[v].to != -1)
29
               cout << v << " " << min_e[v].to << endl;</pre>
                                                                     Floyd Warshall
                                                              6.5
31
           for (int to = 0; to < n; ++to) {
```

```
#include <bits/stdc++.h>
                                                                  auto [v, depth] = q.front();
                                                           35
                                                           36
                                                                  q.pop();
                                                                  level[v] = depth;
3 using namespace std;
                                                           37
4 using 11 = long long;
                                                           38
                                                                  for (auto [u,d] : adj[v]) {
6 const int MAX = 507;
                                                                    if (!visited[u]) {
                                                           40
7 const long long INF = 0x3f3f3f3f3f3f3f3f3fLL;
                                                                       visited[u] = true;
                                                           41
                                                                       up[u][0] = v;
                                                           42
                                                                       q.push(mp(u, depth + 1));
9 11 dist[MAX][MAX];
                                                           43
                                                                    }
                                                           44
                                                                  }
11
                                                           45
12 void floyd_warshall() {
                                                           46
                                                                }
      for (int i = 0; i < n; i++) {
                                                           47 }
13
           for (int j = 0; j < n; j++) {
                                                           48
14
               if (i == j) dist[i][j] = 0;
15
                                                           49 void find_level_peso() {
               else if (!dist[i][j]) dist[i][j] = INF;
                                                                queue <pii > q;
16
                                                           50
17
           }
      }
                                                                q.push(mp(1, 0));
18
                                                           52
                                                                visited[1] = true;
       for (int k = 0; k < n; k++) {
20
                                                           54
           for (int i = 0; i < n; i++) {
                                                                while (!q.empty()) {
                                                           55
21
               for (int j = 0; j < n; j++) {
                                                                  auto [v, depth] = q.front();
22
                                                           56
                   // trata o caso no qual o grafo tem
                                                           57
                                                                  q.pop();
23
       arestas com peso negativo
                                                                  level_peso[v] = depth;
                   if (dist[i][k] < INF && dist[k][j] < 59</pre>
24
                                                                  for (auto [u,d] : adj[v]) {
                                                           60
                        dist[i][j] = min(dist[i][j], dist 61
25
                                                                    if (!visited[u]) {
       [i][k] + dist[k][j]);
                                                                      visited[u] = true;
                                                           62
                   }
                                                                      up[u][0] = v;
26
               }
                                                                      q.push(mp(u, depth + d));
27
                                                           64
           }
                                                           65
28
       }
                                                                  }
29
                                                           66
30 }
                                                           67
                                                                }
                                                           68 }
  6.6 Lca
                                                           69
                                                           70 int lca(int a, int b) {
                                                                 // get the nodes to the same level
                                                           71
1 // Description:
                                                                  int mn = min(level[a], level[b]);
_{
m 2} // Find the lowest common ancestor between two nodes _{
m 72}
      in a tree
                                                                  for (int j = 0; j \le BITS; j++) {
                                                           74
                                                                    if (a != -1 && ((level[a] - mn) & (1 << j))) a
4 // Problem:
                                                                  = up[a][j];
5 // https://cses.fi/problemset/task/1135
                                                                    if (b != -1 && ((level[b] - mn) & (1 << j))) b
                                                            76
                                                                  = up[b][j];
7 // Complexity:
                                                           77
8 // O(log n)
                                                            78
                                                                  // special case
10 // How to use:
                                                           79
                                                                  if (a == b) return a;
11 // preprocess();
12 // lca(a, b);
                                                           81
                                                                  // binary search
                                                           82
                                                                  for (int j = BITS; j >= 0; j--) {
_{14} // Notes
                                                            83
                                                                    if (up[a][j] != up[b][j]) {
_{15} // To calculate the distance between two nodes use
                                                           84
                                                                      a = up[a][j];
      the following formula
                                                                       b = up[b][j];
16 // level_peso[a] + level_peso[b] - 2*level_peso[lca(a 86
                                                           87
      , b)]
                                                           88
17
                                                           89
                                                                  return up[a][0];
18 const int MAX = 2e5+10;
                                                           90 }
19 const int BITS = 30;
                                                           91
                                                           92 void preprocess() {
21 vector < pii > adj [MAX];
                                                                visited = vector < bool > (MAX, false);
22 vector < bool > visited(MAX);
                                                           93
                                                                find_level();
                                                           94
                                                                visited = vector < bool > (MAX, false);
24 int up[MAX][BITS + 1];
                                                           95
                                                                find_level_peso();
25 int level[MAX];
                                                           96
26 int level_peso[MAX];
                                                                for (int j = 1; j \le BITS; j++) {
                                                           98
                                                                   for (int i = 1; i <= n; i++) {
                                                           99
28 void find_level() {
                                                                    if (up[i][j - 1] != -1) up[i][j] = up[up[i][j -
   queue <pii > q;
29
                                                                   1]][j - 1];
    q.push(mp(1, 0));
                                                           101
31
                                                                }
    visited[1] = true;
                                                           102
                                                           103 }
33
    while (!q.empty()) {
34
```

6.7 Bellman Ford 11 capacity; 39 40 11 flow; Edge* residual; 41 1 struct edge 42 43 Edge() {} int a, b, cost; 44 Edge(int from, int to, ll capacity) : from(from), to(to), capacity(capacity) { 6 int n, m, v; flow = 0;46 7 vector<edge> e; 47 8 const int INF = 1000000000; 48 49 11 get_capacity() { 10 void solve() return capacity - flow; 50 11 { 51 vector < int > d (n, INF); 12 52 13 d[v] = 0;11 get_flow() { 53 for (int i=0; i < n-1; ++i) return flow; for (int j=0; j < m; ++j) 15 55 if (d[e[j].a] < INF)d[e[j].b] = min (d[e[j].b], d[e[j].a] 56 -void augment(ll bottleneck) { + e[j].cost); flow += bottleneck; 58 18 } residual ->flow -= bottleneck; 59 60 6.8 Dinic void reverse(ll bottleneck) { 62 flow -= bottleneck; 1 // Description: 63 residual ->flow += bottleneck; $_{2}$ // Obtains the maximum possible flow rate given a 64 network. A network is a graph with a single 65 source vertex and a single sink vertex in which bool operator < (const Edge& e) const { each edge has a capacity 67 return true; 68 69 70 }; 5 // https://codeforces.com/gym/103708/problem/J 72 struct Dinic { 7 // Complexity: $_8$ // O(V^2 * E) where V is the number of vertex and E 73 int source; int sink: is the number of edges 74 75 int nodes; 10 // Unit network 11 flow; 76 vector < vector < Edge *>> adj; 77 11 // A unit network is a network in which for any vertex except source and sink either incoming or 78 vector < int > level; vector < int > next; outgoing edge is unique and has unit capacity (79 vector < int > reach; 80 matching problem). 81 vector < bool > visited; 12 // Complexity on unit networks: O(E * sqrt(V)) vector < vector < int >> path; 82 $_{14}$ // Unity capacity networks Dinic(int source, int sink, int nodes) : source($_{\rm 15}$ // A more generic settings when all edges have unit 84 capacities, but the number of incoming and source), sink(sink), nodes(nodes) { adj.resize(nodes + 1); outgoing edges is unbounded $_{16}$ // Complexity on unity capacity networks: O(E * sqrt(86 void add_edge(int from, int to, ll capacity) { 88 Edge* e1 = new Edge(from, to, capacity); 18 // How to use: Edge* e2 = new Edge(to, from, 0); 19 // Dinic dinic = Dinic(num_vertex, source, sink); 90 20 // dinic.add_edge(vertex1, vertex2, capacity); 91 // Edge* e2 = new Edge(to, from, capacity); e1->residual = e2; 92 21 // cout << dinic.max_flow() << '\n';</pre> e2->residual = e1; 93 adj[from].pb(e1); 23 #include <bits/stdc++.h> 94 95 adj[to].pb(e2); 96 25 #define pb push_back 97 26 #define mp make_pair 98 bool bfs() { 27 #define pii pair<int, int> level.assign(nodes + 1, -1); 28 #define ff first 99 queue <int > q; 29 #define ss second 100 q.push(source); 101 30 #define ll long long level[source] = 0; 102 103 32 using namespace std; while (!q.empty()) { 104 int node = q.front(); 105 34 const 11 INF = 1e18+10; q.pop(); 106 36 struct Edge { 107 for (auto e : adj[node]) { int from; 37 if (level[e->to] == -1 && e-> 109 int to;

```
get_capacity() > 0) {
                                                                               }
                                                               176
110
                          level[e->to] = level[e->from] +
                                                              177
                                                                           }
                                                                      }
        1:
                                                               178
                          q.push(e->to);
111
                                                               179
112
                     }
                                                               180
                                                                      ll build_path(int v, int id, ll flow) {
                }
                                                                           visited[v] = true;
113
                                                              181
            }
                                                                           if (v == sink) {
114
                                                               182
                                                                                return flow:
115
                                                               183
            return level[sink] != -1;
116
                                                               184
        }
117
                                                               185
                                                                           for (auto e : adj[v]) {
118
                                                               186
        11 dfs(int v, 11 flow) {
119
                                                               187
                                                                                if (!visited[e->to] && e->get_flow() > 0)
            if (v == sink)
                                                                        ₹
120
                                                                                    visited[e->to] = true;
                 return flow;
121
                                                                                    11 bottleneck = build_path(e->to, id,
122
                                                               189
            int sz = adj[v].size();
                                                                       min(flow, e->get_flow()));
123
                                                                                    if (bottleneck > 0) {
124
            for (int i = next[v]; i < sz; i++) {</pre>
                 Edge* e = adj[v][i];
                                                                                         path[id].pb(e->to);
125
                                                               191
                 if (level[e->to] == level[e->from] + 1 &&192
                                                                                         e->reverse(bottleneck);
126
         e->get_capacity() > 0) {
                                                                                         return bottleneck;
                     11 bottleneck = dfs(e->to, min(flow, 194
                                                                                    }
127
        e->get_capacity()));
                                                                               }
                     if (bottleneck > 0) {
                                                                           }
128
                                                               196
                          e->augment(bottleneck);
                                                               197
                          return bottleneck;
130
                                                              198
                                                                           return 0;
                     }
                                                               199
131
                }
132
                                                              200
                                                                       void print_flow_path() {
133
                                                              201
                 next[v] = i + 1;
                                                                           path.clear();
134
                                                               202
            }
                                                                           11 \text{ sent = } -1;
135
                                                              203
                                                                           int id = -1;
136
                                                               204
                                                                           while (sent != 0) {
            return 0:
137
                                                              205
        }
                                                                                visited.assign(nodes + 1, false);
                                                              206
138
139
                                                               207
                                                                                path.pb(vector<int>{});
                                                                                sent = build_path(source, ++id, INF);
        11 max_flow() {
140
                                                              208
            flow = 0;
                                                                                path[id].pb(source);
141
            while(bfs()) {
                                                                           }
142
                                                              210
                next.assign(nodes + 1, 0);
                                                              211
                                                                           path.pop_back();
143
                 11 sent = -1;
                                                              212
144
                 while (sent != 0) {
                                                                           for (int i = 0; i < id; i++) {
                                                              213
145
                                                                                cout << path[i].size() << '\n';</pre>
146
                     sent = dfs(source, INF);
                                                               214
                                                                                reverse(path[i].begin(), path[i].end());
                     flow += sent;
147
                                                              215
                 }
                                                              216
                                                                                for (auto e : path[i]) {
148
149
            }
                                                              217
                                                                                    cout << e << ' ';
            return flow;
                                                              218
150
        }
                                                               219
                                                                                cout << '\n';
151
                                                                           }
152
                                                              220
153
        void reachable(int v) {
                                                               221
                                                                      }
            visited[v] = true;
                                                              222 };
154
155
                                                              223
            for (auto e : adj[v]) {
                                                               224 int main() {
156
                 if (!visited[e->to] && e->get_capacity() 225
                                                                      ios::sync_with_stdio(false);
157
       > 0) {
                                                                      cin.tie(NULL);
                     reach.pb(e->to);
158
                                                              227
                     visited[e->to] = true;
                                                                       int n, m; cin >> n >> m;
159
                                                              228
                     reachable(e->to);
160
                                                              229
                }
                                                                      Dinic dinic = Dinic(1, n, n);
161
                                                              230
            }
                                                               231
162
                                                                       for (int i = 1; i <= m; i++) {
163
        }
                                                               232
                                                                           int v, u; cin >> v >> u;
164
                                                               233
165
        void print_min_cut() {
                                                              234
                                                                           dinic.add_edge(v, u, 1);
            reach.clear();
166
                                                              235
            visited.assign(nodes + 1, false);
167
                                                               236
                                                                      cout << dinic.max_flow() << '\n';</pre>
            reach.pb(source):
                                                              237
168
169
            reachable(source);
                                                               238
                                                                       // dinic.print_min_cut();
                                                                      // dinic.print_flow_path();
170
                                                              239
            for (auto v : reach) {
171
                                                              240
                 for (auto e : adj[v]) {
                                                              241
                                                                      return 0;
172
                     if (!visited[e->to] && e->
                                                              242 }
173
        get_capacity() == 0) {
                                                                  6.9
                                                                        2sat
                          cout << e->from << ' ' ' << e->to
174
        << '\n';
                     }
175
                                                                1 // Description:
```

```
_2 // Solves expression of the type (a v b) ^ (c v d) ^ _{73}
                                                                       add_or(get_not(a), get_not(b));
      (e v f)
                                                            75
4 // Problem:
                                                                   void add_xnor(int a, int b) {
                                                            76
5 // https://cses.fi/problemset/task/1684
                                                            77
                                                                       add_or(get_not(a), b);
                                                                       add_or(a, get_not(b));
                                                            78
                                                            79
_{8} // O(n + m) where n is the number of variables and m _{80}
      is the number of clauses
                                                                   void departure_time(int v) {
                                                            81
                                                                       visited[v] = true;
10 #include <bits/stdc++.h>
                                                            83
11 #define pb push_back
                                                                       for (auto u : adj[v]) {
12 #define mp make_pair
                                                                            if (!visited[u]) departure_time(u);
                                                            85
13 #define pii pair<int, int>
                                                            86
14 #define ff first
                                                            87
15 #define ss second
                                                                       departure.pb(mp(++curr, v));
                                                            88
                                                            89
17 using namespace std;
                                                            90
                                                                   void find_component(int v, int component) {
                                                            91
19 struct SAT {
                                                                       scc[v] = component;
                                                            92
                                                                       visited[v] = true;
      int nodes;
                                                            93
20
       int curr = 0:
21
                                                            94
      int component = 0;
                                                                       for (auto u : rev[v]) {
22
                                                            95
       vector < vector < int >> adj;
                                                                           if (!visited[u]) find_component(u,
      vector < vector < int >> rev;
                                                                   component);
24
       vector < vector < int >> condensed;
                                                                       }
25
                                                            97
      vector < pii > departure;
26
                                                            98
       vector < bool > visited;
27
                                                            99
       vector < int > scc;
                                                                   void topological_order(int v) {
                                                           100
      vector<int> order;
                                                                       visited[v] = true;
29
                                                           101
                                                           102
30
       // 1 to nodes
                                                                       for (auto u : condensed[v]) {
31
                                                           103
       // nodes + 1 to 2 * nodes
                                                                            if (!visited[u]) topological_order(u);
                                                           104
32
       SAT(int nodes) : nodes(nodes) {
                                                           105
           adj.resize(2 * nodes + 1);
34
                                                           106
           rev.resize(2 * nodes + 1);
                                                                       order.pb(v);
                                                           107
           visited.resize(2 * nodes + 1);
36
                                                           108
           scc.resize(2 * nodes + 1);
                                                           109
37
      }
                                                           110
                                                                   bool is_possible() {
38
                                                                       component = 0;
39
                                                           111
                                                                       for (int i = 1; i <= 2 * nodes; i++) {
40
       void add_imp(int a, int b) {
                                                           112
                                                                            if (!visited[i]) departure_time(i);
           adj[a].pb(b);
41
                                                           113
           rev[b].pb(a);
                                                           114
42
       7
                                                           115
43
                                                                       sort(departure.begin(), departure.end(),
44
                                                           116
       int get_not(int a) {
                                                                   greater < pii > ());
45
           if (a > nodes) return a - nodes;
46
                                                           117
           return a + nodes;
                                                                       visited.assign(2 * nodes + 1, false);
48
                                                           119
                                                                       for (auto [_, node] : departure) {
49
                                                            120
       void add_or(int a, int b) {
                                                                           if (!visited[node]) find_component(node,
50
                                                           121
           add_imp(get_not(a), b);
                                                                   ++component);
51
           add_imp(get_not(b), a);
                                                                       }
                                                           122
53
                                                           123
                                                                       for (int i = 1; i <= nodes; i++) {
54
                                                           124
                                                                            if (scc[i] == scc[i + nodes]) return
       void add_nor(int a, int b) {
55
                                                           125
           add_or(get_not(a), get_not(b));
                                                                   false;
56
                                                           126
57
58
                                                           127
       void add_and(int a, int b) {
                                                           128
                                                                       return true;
59
60
           add_or(get_not(a), b);
                                                           129
           add_or(a, get_not(b));
61
                                                           130
           add_or(a, b);
                                                                   int find_value(int e, vector<int> &ans) {
                                                           131
       }
                                                                       if (e > nodes && ans[e - nodes] != 2) return
63
                                                           132
                                                                   !ans[e - nodes];
                                                                       if (e <= nodes && ans[e + nodes] != 2) return
       void add_nand(int a, int b) {
65
                                                           133
           add_or(get_not(a), b);
                                                                    !ans[e + nodes];
66
           add_or(a, get_not(b));
                                                           134
                                                                       return 0;
67
           add_or(get_not(a), get_not(b));
                                                           135
68
69
                                                            136
                                                                   vector < int > find_ans() {
70
                                                           137
       void add_xor(int a, int b) {
                                                                       condensed.resize(component + 1);
71
                                                           138
           add_or(a, b);
                                                           139
72
```

```
for (int i = 1; i <= 2 * nodes; i++) {
                                                         3 vector < int > adj[MAX];
140
141
                for (auto u : adj[i]) {
                    if (scc[i] != scc[u]) condensed[scc[i 5 bool dfs(int u, int p){
142
       ]].pb(scc[u]);
                                                                    if (visited[u]) return false;
           }
144
                                                                    path.pb(u);
145
                                                                    visited[u] = true;
            visited.assign(component + 1, false);
146
                                                             10
147
                                                             11
            for (int i = 1; i <= component; i++) {</pre>
                                                                    for (auto v : adj[u]){
                if (!visited[i]) topological_order(i);
                                                                        if (visited[v] and u != v and p != v){
149
                                                             13
                                                                             path.pb(v); return true;
151
                                                             15
            reverse(order.begin(), order.end());
152
                                                             16
                                                                         if (dfs(v, u)) return true;
153
                                                             17
            // 0 - false
154
                                                             18
            // 1 - true
155
            // 2 - no value yet
                                                                    path.pop_back();
156
                                                             20
            vector < int > ans(2 * nodes + 1, 2);
                                                                    return false;
                                                             22 }
158
            vector < vector < int >> belong (component + 1);
159
                                                             23
                                                             24 bool has_cycle(int N){
160
            for (int i = 1; i <= 2 * nodes; i++) {
                                                             25
161
                belong[scc[i]].pb(i);
                                                                    visited.reset();
163
                                                             27
                                                                    for (int u = 1; u \le N; ++u){
                                                             28
164
165
            for (auto p : order) {
                                                             29
                                                                         path.clear();
                for (auto e : belong[p]) {
                                                                         if (not visited[u] and dfs(u,-1))
166
                                                             30
                    ans[e] = find_value(e, ans);
                                                                             return true;
                                                             31
168
                                                             32
            }
169
                                                             33
170
                                                             34
            return ans;
                                                                    return false;
171
                                                             35
                                                             36 }
173 }:
                                                                6.11
                                                                       Cycle Path Recovery
174
175 int main() {
176
       ios::sync_with_stdio(false);
                                                             1 int n;
       cin.tie(NULL);
177
                                                             vector < vector < int >> adj;
178
                                                              3 vector < char > color;
179
       int n, m; cin >> n >> m;
                                                              4 vector <int> parent;
180
                                                              5 int cycle_start, cycle_end;
       SAT sat = SAT(m);
181
182
                                                              7 bool dfs(int v) {
       for (int i = 0; i < n; i++) {
183
                                                                    color[v] = 1;
            char op1, op2; int a, b; cin >> op1 >> a >>
                                                                    for (int u : adj[v]) {
                                                             9
       op2 >> b;
                                                                         if (color[u] == 0) {
           if (op1 == '+' && op2 == '+') sat.add_or(a, b<sub>11</sub>
                                                                             parent[u] = v;
                                                                             if (dfs(u))
           if (op1 == '-' && op2 == '-') sat.add_or(sat.<sub>13</sub>
186
                                                                                 return true;
       get_not(a), sat.get_not(b));
                                                                         } else if (color[u] == 1) {
                                                             14
           if (op1 == '+' && op2 == '-') sat.add_or(a,
187
                                                                             cycle_end = v;
       sat.get_not(b));
                                                                             cycle_start = u;
           if (op1 == '-' && op2 == '+') sat.add_or(sat.<sub>17</sub>
188
                                                                             return true;
       get_not(a), b);
                                                             18
189
                                                             19
190
                                                                    color[v] = 2;
       if (!sat.is_possible()) cout << "IMPOSSIBLE\n";</pre>
191
                                                             21
                                                                    return false:
192
       else {
193
            vector < int > ans = sat.find_ans();
                                                             23
            for (int i = 1; i <= m; i++) {
194
                                                             24 void find_cycle() {
                cout << (ans[i] == 1 ? '+' : '-') << ' '; 25
195
                                                                    color.assign(n, 0);
            }
                                                                    parent.assign(n, -1);
                                                             26
            cout << '\n';</pre>
197
                                                                    cycle_start = -1;
198
       }
                                                             28
199
                                                                    for (int v = 0; v < n; v++) {
                                                             29
       return 0;
                                                                         if (color[v] == 0 && dfs(v))
200
                                                             30
201 }
                                                             31
                                                                             break;
                                                             32
   6.10
          Find Cycle
                                                             33
                                                                    if (cycle_start == -1) {
                                                             34
                                                                        cout << "Acyclic" << endl;</pre>
 1 bitset < MAX > visited;
                                                             35
 vector < int > path;
                                                                    } else {
                                                             36
```

```
vector <int > cycle;
                                                         57 int32_t main(){
37
          cycle.push_back(cycle_start);
                                                         ios::sync_with_stdio(false);
38
          for (int v = cycle_end; v != cycle_start; v = 59
                                                                cin.tie(NULL);
39
       parent[v])
                                                        60
              cycle.push_back(v);
                                                                cin >> n;
                                                                adj.resize(n + 1);
           cycle.push_back(cycle_start);
                                                         62
41
          reverse(cycle.begin(), cycle.end());
                                                                ans.resize(n + 1);
                                                         63
                                                                removed.resize(n + 1);
43
                                                         64
          cout << "Cycle found: ";</pre>
                                                                subtree_size.resize(n + 1);
                                                         65
          for (int v : cycle)
                                                         66
            cout << v << " ";
                                                                for (int i = 1; i \le n - 1; i++) {
46
                                                         67
                                                                    int u, v; cin >> u >> v;
47
           cout << endl;</pre>
                                                         68
      }
                                                                     adj[u].insert(v);
48
                                                         69
49 }
                                                                     adj[v].insert(u);
                                                         70
                                                         71
         Centroid Decomposition
  6.12
                                                         72
                                                                solve(1, 'A');
                                                         73
                                                         74
1 int n;
vector < set < int >> adj;
                                                         75
                                                                if (!flag) cout << "Impossible!\n";</pre>
3 vector < char > ans;
                                                         76
                                                                else {
                                                         77
                                                                    for (int i = 1; i <= n; i++) {
                                                                         cout << ans[i] << ' ';
                                                         78
5 vector < bool > removed;
                                                         79
                                                                     cout << '\n';</pre>
7 vector<int> subtree_size;
                                                         81
9 int dfs(int u, int p = 0) {
                                                         82
   subtree_size[u] = 1;
                                                         83
                                                                return 0;
10
                                                         84 }
   for(int v : adj[u]) {
12
                                                                   Tarjan Bridge
                                                            6.13
     if(v != p && !removed[v]) {
        subtree_size[u] += dfs(v, u);
                                                          1 // Description:
15
                                                          2 // Find a bridge in a connected unidirected graph
16
                                                          3 // A bridge is an edge so that if you remove that
17
    return subtree_size[u];
                                                               edge the graph is no longer connected
19 }
                                                          5 // Problem:
20
                                                          6 // https://cses.fi/problemset/task/2177/
21 int get_centroid(int u, int sz, int p = 0) {
22 for(int v : adj[u]) {
     if(v != p && !removed[v]) {
                                                          8 // Complexity:
       if(subtree_size[v]*2 > sz) {
                                                          _{9} // O(V + E) where V is the number of vertices and E
24
          return get_centroid(v, sz, u);
                                                                is the number of edges
26
              }
                                                         11 int n;
28
      }
                                                         12 vector < vector < int >> adj;
29
                                                         13
30
    return u;
                                                         14 vector < bool > visited;
31 }
                                                         15 vector <int> tin, low;
                                                         16 int timer;
33 char get_next(char c) {
                                                         17
34    if (c != 'Z') return c + 1;
                                                         18 void dfs(int v, int p) {
      return '$';
                                                               visited[v] = true;
36 }
                                                                tin[v] = low[v] = timer++;
                                                         20
                                                                for (int to : adj[v]) {
                                                         21
                                                                    if (to == p) continue;
38 bool flag = true;
                                                         22
                                                         23
                                                                    if (visited[to]) {
39
40 void solve(int node, char c) {
                                                                         low[v] = min(low[v], tin[to]);
   int center = get_centroid(node, dfs(node));
                                                                    } else {
41
                                                         25
     ans[center] = c;
                                                                         dfs(to, v);
      removed[center] = true;
                                                                         low[v] = min(low[v], low[to]);
43
                                                         27
                                                                         if (low[to] > tin[v]) {
                                                         28
44
      for (auto u : adj[center]) {
                                                                             IS_BRIDGE(v, to);
45
                                                         29
          if (!removed[u]) {
46
                                                         30
               char next = get_next(c);
                                                         31
                                                                    }
               if (next == '$') {
48
                                                         32
                   flag = false;
49
                                                         33 }
50
                   return;
                                                         34
                                                         35 void find_bridges() {
51
               solve(u, next);
                                                                timer = 0;
                                                         36
          }
                                                                visited.assign(n, false);
53
                                                         37
      }
                                                                tin.assign(n, -1);
                                                          38
55 }
                                                                low.assign(n, -1);
                                                         39
                                                                for (int i = 0; i < n; ++i) {
56
                                                          40
```

Tree Diameter 6.15 if (!visited[i]) 41 42 dfs(i, -1); } 43 1 #include <bits/stdc++.h> 44 } 3 using namespace std; 6.14Small To Large 5 const int MAX = 3e5+17; 1 // Problem: 7 vector < int > adj[MAX]; 2 // https://codeforces.com/contest/600/problem/E 8 bool visited[MAX]; 4 void process_colors(int curr, int parent) { 10 int max_depth = 0, max_node = 1; 11 for (int n : adj[curr]) { 12 void dfs (int v, int depth) { if (n != parent) { visited[v] = true; 13 process_colors(n, curr); if (depth > max_depth) { if (colors[curr].size() < colors[n].size 16 10 max_depth = depth; ()) { max_node = v; 17 sum_num[curr] = sum_num[n]; 11 18 vmax[curr] = vmax[n]; 12 19 swap(colors[curr], colors[n]); 13 for (auto u : adi[v]) { 20 14 if (!visited[u]) dfs(u, depth + 1); 15 22 for (auto [item, vzs] : colors[n]) { 16 23 } if(colors[curr][item]+vzs > vmax[curr 17 1){ vmax[curr] = colors[curr][item] + 25 int tree_diameter() { dfs(1, 0); 18 vzs: max_depth = 0; 27 sum_num[curr] = item; 19 for (int i = 0; i < MAX; i++) visited[i] = false;</pre> 28 } 20 29 dfs(max_node, 0); else if(colors[curr][item]+vzs == 21 return max_depth; 30 vmax[curr]){ 31 } 22 sum_num[curr] += item; } 23 6.16 Dijkstra colors[curr][item] += vzs; 25 1 const int MAX = 2e5+7; 26 } 2 const int INF = 1000000000; 27 } 28 3 vector < vector < pair < int , int >>> adj(MAX); 30 } 5 void dijkstra(int s, vector<int> & d, vector<int> & p 31) { 32 int n = adj.size(); 6 33 int32_t main() { 7 d.assign(n, INF); p.assign(n, -1); 8 int n; cin >> n; 35 d[s] = 0;10 for (int i = 1; i <= n; i++) { 37 11 set < pair < int , int >> q; int a; cin >> a; q.insert({0, s}); 38 12 colors[i][a] = 1; 39 while (!q.empty()) { 13 vmax[i] = 1; 40 int v = q.begin()->second; 14 sum_num[i] = a; q.erase(q.begin()); 15 } 42 16 43 for (auto edge : adj[v]) { 17 for (int i = 1; i < n; i++) { 44 int to = edge.first; 18 int a, b; cin >> a >> b; 45 int len = edge.second; 19 20 47 adj[a].push_back(b); if (d[v] + len < d[to]) {</pre> adj[b].push_back(a); 48 q.erase({d[to], to}); 22 49 d[to] = d[v] + len;23 50 24 p[to] = v;process_colors(1, 0); 25 q.insert({d[to], to}); 52 } 53 for (int i = 1; $i \le n$; i++) { } 27 cout << sum_num[i] << (i < n ? " " : "\n");</pre> 54 28 55 29 } 56 30 return 0; 57 31 vector<int> restore_path(int s, int t) { vector < int > path; 32 59 } 33 60 for (int v = t; v != s; v = p[v]) 34 path.push_back(v); 35

```
path.push_back(s);
                                                                           swap(a, b);
36
                                                            32
37
                                                            33
                                                                       sizes[a] += sizes[b];
       reverse(path.begin(), path.end());
38
                                                            34
                                                                       link[b] = a;
       return path;
                                                            35
39
40 }
                                                            37 }:
41
42 int adj[MAX][MAX];
43 int dist[MAX]:
                                                            39 struct Edge {
44 int minDistance(int dist[], bool sptSet[], int V) {
                                                                   int u, v;
                                                           40
       int min = INT_MAX, min_index;
                                                                   long long weight;
                                                            41
46
                                                            42
47
       for (int v = 0; v < V; v++)
                                                            43
                                                                   Edge() {}
           if (sptSet[v] == false && dist[v] <= min)</pre>
48
                                                            44
               min = dist[v], min_index = v;
                                                                   Edge(int u, int v, long long weight) : u(u), v(v)
49
                                                            45
50
                                                                   , weight(weight) {}
       return min_index;
51
                                                            46
52 }
                                                            47
                                                                   bool operator < (const Edge& other) const {</pre>
                                                                       return weight < other.weight;</pre>
53
                                                            48
54 void dijkstra(int src, int V) {
55
                                                            50
       bool sptSet[V];
                                                                   bool operator > (const Edge& other) const {
                                                            51
56
       for (int i = 0; i < V; i++)
                                                            52
                                                                      return weight > other.weight;
57
           dist[i] = INT_MAX, sptSet[i] = false;
58
                                                            53
                                                            54 };
       dist[src] = 0:
60
                                                            55
                                                            56 vector < Edge > kruskal (vector < Edge > edges, int n) {
61
       for (int count = 0; count < V - 1; count++) {</pre>
                                                                   vector < Edge > result; // arestas da MST
62
                                                            57
           int u = minDistance(dist, sptSet, V);
                                                                   long long cost = 0;
63
                                                            58
                                                            59
           sptSet[u] = true;
                                                                   sort(edges.begin(), edges.end());
65
                                                            60
                                                            61
66
                                                                   DSU dsu(n);
67
                                                            62
           for (int v = 0; v < V; v++)
                                                            63
68
               if (!sptSet[v] && adj[u][v]
                                                            64
                                                                   for (auto e : edges) {
                   && dist[u] != INT_MAX
                                                                       if (!dsu.same(e.u, e.v)) {
70
                                                            65
                   && dist[u] + adj[u][v] < dist[v])
                                                                            cost += e.weight;
                   dist[v] = dist[u] + adj[u][v];
                                                                           result.push_back(e);
72
                                                            67
73
                                                            68
                                                                           dsu.unite(e.u, e.v);
74 }
                                                            69
                                                                       }
                                                                   }
                                                            70
         Kruskall
  6.17
                                                            71
                                                                   return result;
                                                            72
1 struct DSU {
                                                            73 }
      int n;
       vector<int> link, sizes;
                                                                   Geometry
       DSU(int n) {
          this ->n = n;
                                                              7.1 2d
           link.assign(n+1, 0);
           sizes.assign(n+1, 1);
9
                                                            1 #define vp vector<point>
           for (int i = 0; i \le n; i++)
                                                            2 #define ld long double
                                                            3 const ld EPS = 1e-6;
               link[i] = i;
11
       }
                                                            4 const ld PI = acos(-1);
12
13
       int find(int x) {
                                                            6 // typedef ll cod;
14
           while (x != link[x])
                                                            7 // bool eq(cod a, cod b){ return (a==b); }
15
               x = link[x];
                                                            8 typedef ld cod;
16
                                                            9 bool eq(cod a, cod b){ return abs(a - b) <= EPS; }</pre>
18
           return x;
                                                            10
                                                            11 struct point{
19
20
                                                            12
                                                                  cod x, y;
       bool same(int a, int b) {
                                                                   int id;
21
                                                            13
```

14

15

16

17

18

19

point(cod x=0, cod y=0): x(x), y(y){}

o.x, y+o.y}; }

o.x, y-o.y}; }

point operator+(const point &o) const{ return {x+

point operator-(const point &o) const{ return {x-

point operator*(cod t) const{ return {x*t, y*t};

point operator/(cod t) const{ return {x/t, y/t};

22

23

25

26

28

30

31

return find(a) == find(b);

void unite(int a, int b) {

if (a == b) return;

if (sizes[a] < sizes[b])</pre>

a = find(a);

b = find(b);

```
cod operator*(const point &o) const{ return x * o 87
                                                                  for(int i=0;i<len;i++)
20
      .x + y * o.y; }
                                                                    c=c+A[i];
      cod operator (const point &o) const{ return x * 089
                                                                  return c/len;
21
      .y - y * o.x; }
                                                          90 }
22
      bool operator < (const point &o) const{</pre>
          return (eq(x, o.x) ? y < o.y : x < o.x);
                                                           92 point forca_mod(point p, ld m){
23
                                                                  ld cm = norm(p);
24
                                                                  if(cm<EPS) return point();</pre>
      bool operator == (const point &o) const{
25
                                                           94
          return eq(x, o.x) and eq(y, o.y);
                                                                  return point(p.x*m/cm,p.y*m/cm);
26
                                                           95
27
    friend ostream& operator << (ostream& os, point p) { 97</pre>
28
      return os << "(" << p.x << "," << p.y << ")"; }
29
                                                           98 ld param(point a, point b, point v){
                                                                 // v = t*(b-a) + a // return t;
30 };
                                                           99
                                                                  // assert(line(a, b).inside_seg(v));
31
                                                           100
_{32} int ccw(point a, point b, point e){ // -1=dir; 0=
                                                                  return ((v-a) * (b-a)) / ((b-a) * (b-a));
                                                          101
      collinear; 1=esq;
cod tmp = (b-a) ^ (e-a); // vector from a to b
                                                          102 }
                                                          103
      return (tmp > EPS) - (tmp < -EPS);
                                                          104 bool simetric(vp &a){ //ordered
34
35 }
                                                                  int n = a.size();
                                                                  point c = center(a);
36
                                                          106
37 ld norm(point a){ // Modulo
                                                          107
                                                                  if(n&1) return false;
      return sqrt(a * a);
                                                                  for (int i=0; i < n/2; i++)
38
                                                          108
39 }
                                                                      if(ccw(a[i], a[i+n/2], c) != 0)
                                                          109
40 cod norm2(point a){
                                                                          return false;
                                                          110
      return a * a;
                                                                  return true;
41
                                                          111
42 }
                                                          112 }
43 bool nulo(point a){
                                                          113
      return (eq(a.x, 0) \text{ and } eq(a.y, 0));
                                                          114 point mirror(point m1, point m2, point p){
44
45 }
                                                                  // mirror point p around segment m1m2
                                                          115
46 point rotccw(point p, ld a){
                                                                  point seg = m2-m1;
                                                          116
      // a = PI*a/180; // graus
                                                                  1d \ t0 = ((p-m1)*seg) / (seg*seg);
                                                          117
      return point((p.x*cos(a)-p.y*sin(a)), (p.y*cos(a)118
                                                                  point ort = m1 + seg*t0;
48
      +p.x*sin(a)));
                                                                  point pm = ort-(p-ort);
                                                          119
49 }
                                                                  return pm;
50 point rot90cw(point a) { return point(a.y, -a.x); }; 121 }
51 point rot90ccw(point a) { return point(-a.y, a.x); };122
53 ld proj(point a, point b){ // a sobre b
                                                          124 ///////////
      return a*b/norm(b);
                                                          125 // Line //
54
55 }
                                                          126 //////////
56 ld angle(point a, point b){ // em radianos
                                                          127
      ld ang = a*b / norm(a) / norm(b);
                                                          128 struct line{
57
      return acos(max(min(ang, (ld)1), (ld)-1));
                                                          129
                                                                 point p1, p2;
58
                                                                  cod a, b, c; // ax+by+c = 0;
59 }
                                                          130
                                                                  // y-y1 = ((y2-y1)/(x2-x1))(x-x1)
60 ld angle_vec(point v){
                                                          131
      // return 180/PI*atan2(v.x, v.y); // graus
                                                          132
                                                                  line(point p1=0, point p2=0): p1(p1), p2(p2){
61
                                                                      a = p1.y - p2.y;
      return atan2(v.x, v.y);
62
                                                          133
63 }
                                                                      b = p2.x - p1.x;
64 ld order_angle(point a, point b){ // from a to b ccw 135
                                                                      c = p1 ^p2;
      (a in front of b)
                                                          136
                                                                  line(cod a=0, cod b=0, cod c=0): a(a), b(b), c(c)
      ld aux = angle(a,b)*180/PI;
                                                           137
      return ((a^b) \le 0 ? aux : 360 - aux);
66
67 }
                                                                      // Gera os pontos p1 p2 dados os coeficientes
                                                                      // isso aqui eh um lixo mas quebra um galho
68 bool angle_less(point a1, point b1, point a2, point 139
      b2){ // ang(a1,b1) <= ang(a2,b2)
                                                                  kkkkkk
      point p1((a1*b1), abs((a1^b1)));
                                                                      if(b==0){}
69
      point p2((a2*b2), abs((a2^b2)));
                                                                          p1 = point(1, -c/a);
70
                                                          141
                                                                          p2 = point(0, -c/a);
      return (p1^p2) <= 0;
71
                                                          142
72 }
                                                          143
                                                                      }else{
                                                                          p1 = point(1, (-c-a*1)/b);
73
                                                          144
                                                                          p2 = point(0, -c/b);
74 ld area(vp &p){ // (points sorted)
                                                          145
      ld ret = 0:
75
                                                          146
      for(int i=2;i<(int)p.size();i++)</pre>
                                                                  }
                                                          147
          ret += (p[i]-p[0])^(p[i-1]-p[0]);
77
                                                          148
      return abs(ret/2);
                                                          149
                                                                  cod eval(point p){
79 }
                                                                      return a*p.x+b*p.v+c:
                                                          150
80 ld areaT(point &a, point &b, point &c){
                                                          151
      return abs((b-a)^(c-a))/2.0;
                                                          152
                                                                  bool inside(point p){
81
82 }
                                                                      return eq(eval(p), 0);
                                                          153
                                                          154
84 point center(vp &A){
                                                                  point normal(){
                                                          155
     point c = point();
                                                          156
                                                                      return point(a, b);
      int len = A.size();
                                                          157
```

```
r = norm(a-c):
158
                                                           224
       bool inside_seg(point p){
                                                           225
                                                                   }
159
                                                                   bool inside(const point &a) const{
160
           return (
                                                           226
                ((p1-p) ^ (p2-p)) == 0 and
                                                           227
                                                                      return norm(a - c) <= r + EPS;
161
                ((p1-p) * (p2-p)) <= 0
                                                           228
           ):
                                                           229 }:
163
164
                                                           230
                                                           231 pair < point , point > tangent_points (circle cr, point p)
165
166 };
                                                                   1d d1 = norm(p-cr.c), theta = asin(cr.r/d1);
167
                                                           232
_{168} // be careful with precision error
                                                                   point p1 = rotccw(cr.c-p, -theta);
                                                           233
      inter_line(line 11, line 12){
                                                           234
                                                                   point p2 = rotccw(cr.c-p, theta);
                                                                   assert(d1 >= cr.r);
       ld det = l1.a*l2.b - l1.b*l2.a;
170
                                                           235
       if(det==0) return {};
                                                                   p1 = p1 * (sqrt(d1*d1-cr.r*cr.r) / d1) + p;
                                                           236
171
       1d x = (11.b*12.c - 11.c*12.b)/det;
                                                                   p2 = p2 * (sqrt(d1*d1-cr.r*cr.r) / d1) + p;
172
                                                           237
       1d y = (11.c*12.a - 11.a*12.c)/det;
                                                                   return {p1, p2};
173
                                                           238
174
       return {point(x, y)};
                                                           239 }
175
                                                           240
                                                           241
                                                           242 circle incircle(point p1, point p2, point p3){
177 // segments not collinear
178 vp inter_seg(line 11, line 12){
                                                                   1d m1 = norm(p2-p3);
                                                           243
                                                                   1d m2 = norm(p1-p3);
       vp ans = inter_line(l1, l2);
179
                                                           244
                                                                   1d m3 = norm(p1-p2);
       if(ans.empty() or !l1.inside_seg(ans[0]) or !l2. 245
180
       inside_seg(ans[0]))
                                                                   point c = (p1*m1 + p2*m2 + p3*m3)*(1/(m1+m2+m3));
                                                                   1d s = 0.5*(m1+m2+m3);
           return {};
181
                                                           247
       return ans;
                                                                   1d r = sqrt(s*(s-m1)*(s-m2)*(s-m3)) / s;
                                                           248
182
183 }
                                                           249
                                                                   return circle(c, r);
184 bool seg_has_inter(line 11, line 12){
                                                           250 }
       return ccw(l1.p1, l1.p2, l2.p1) * ccw(l1.p1, l1. 251
185
       p2, 12.p2) < 0 and
                                                           252 circle circumcircle(point a, point b, point c) {
              ccw(12.p1, 12.p2, 11.p1) * ccw(12.p1, 12.253
                                                                   circle ans;
186
       p2, 11.p2) < 0;
                                                                   point u = point((b-a).y, -(b-a).x);
                                                           254
187
                                                                   point v = point((c-a).y, -(c-a).x);
                                                           255
                                                           256
                                                                   point n = (c-b)*0.5;
189 ld dist_seg(point p, point a, point b){ // point -
                                                                   1d t = (u^n)/(v^u);
                                                           257
                                                                   ans.c = ((a+c)*0.5) + (v*t);
                                                           258
                                                                   ans.r = norm(ans.c-a);
       if((p-a)*(b-a) < EPS) return norm(p-a);
190
                                                           259
       if((p-b)*(a-b) < EPS) return norm(p-b);
                                                           260
                                                                   return ans;
191
       return abs((p-a)^(b-a)) / norm(b-a);
                                                           261 }
192
193
                                                           262
194
                                                           263 vp inter_circle_line(circle C, line L){
195 ld dist_line(point p, line l){ // point - line
                                                                   point ab = L.p2 - L.p1, p = L.p1 + ab * ((C.c-L.
                                                           264
                                                                   p1)*(ab) / (ab*ab));
       return abs(1.eval(p))/sqrt(1.a*1.a + 1.b*1.b);
196
197 }
                                                                   ld s = (L.p2-L.p1)^(C.c-L.p1), h2 = C.r*C.r - s*s
                                                           265
                                                                    / (ab*ab);
198
199 line bisector(point a, point b){
                                                                   if (h2 < -EPS) return {};
                                                           266
                                                                   if (eq(h2, 0)) return {p};
       point d = (b-a)*2:
200
                                                           267
201
       return line(d.x, d.y, a*a - b*b);
                                                                   point h = (ab/norm(ab)) * sqrt(h2);
202 }
                                                                   return \{p - h, p + h\};
                                                           269
                                                           270 }
203
204 line perpendicular(line 1, point p){ // passes
                                                           271
                                                           272 vp inter_circle(circle C1, circle C2){
       through p
       return line(1.b, -1.a, -1.b*p.x + 1.a*p.y);
                                                                   if(C1.c == C2.c) { assert(C1.r != C2.r); return
206 }
                                                                   {}; }
                                                                   point vec = C2.c - C1.c;
207
                                                           274
                                                           275
                                                                   1d d2 = vec*vec, sum = C1.r+C2.r, dif = C1.r-C2.r
208
209 ///////////
210 // Circle //
                                                                   1d p = (d2 + C1.r*C1.r - C2.r*C2.r)/(d2*2), h2 =
                                                           276
211 //////////
                                                                   C1.r*C1.r - p*p*d2;
                                                                   if (sum*sum < d2 or dif*dif > d2) return {};
212
                                                           277
                                                                   point mid = C1.c + vec*p, per = point(-vec.y, vec
213 struct circle{
                                                           278
       point c; cod r;
                                                                   .x) * sqrt(max((1d)0, h2) / d2);
214
       circle() : c(0, 0), r(0) {}
                                                                   if(eq(per.x, 0) and eq(per.y, 0)) return {mid};
                                                           279
       circle(const point o) : c(o), r(0){}
                                                                   return {mid + per, mid - per};
216
                                                           280
217
       circle(const point a, const point b){
                                                           281 }
           c = (a+b)/2;
218
                                                           282
           r = norm(a-c);
                                                           283 // minimum circle cover O(n) amortizado
219
       }
                                                           284 circle min_circle_cover(vp v){
220
       circle(const point a, const point b, const point 285
                                                                   random_shuffle(v.begin(), v.end());
221
                                                                   circle ans;
           assert(ccw(a, b, cc) != 0);
                                                                   int n = v.size();
222
                                                           287
            c = inter_line(bisector(a, b), bisector(b, cc288
                                                                   for(int i=0;i<n;i++) if(!ans.inside(v[i])){</pre>
223
       ))[0]:
                                                                       ans = circle(v[i]);
```

```
for(int j=0;j<i;j++) if(!ans.inside(v[j])){</pre>
                                                                 for(int j = 0; j < n; j++){
290
291
               ans = circle(v[i], v[j]);
                                                                  if((counter & (1LL << j)) != 0) {
                                                                      cout << nums[j] << '';</pre>
               for(int k=0; k < j; k++) if(!ans.inside(v[k]) 8
292
       ) {
                    ans = circle(v[i], v[j], v[k]);
                                                                  }
               }
                                                                  cout << '\n';</pre>
294
                                                           11
                                                                }
           }
                                                           12
       }
                                                           13 }
296
       return ans;
297
                                                                    Binary Search Last True
298 }
        Algorithms
                                                                 {
                                                                10--;
```

8.1 Lis

```
int lis(vector < int > const& a) {
      int n = a.size();
      vector < int > d(n, 1);
      for (int i = 0; i < n; i++) {
          for (int j = 0; j < i; j++) {
              if (a[j] < a[i])
                  d[i] = max(d[i], d[j] + 1);
9
      }
10
11
      int ans = d[0];
      for (int i = 1; i < n; i++) {
12
13
          ans = max(ans, d[i]);
14
      return ans;
15
16 }
```

Delta-encoding

```
1 #include <bits/stdc++.h>
2 using namespace std;
4 int main(){
      int n, q;
      cin >> n >> q;
       int [n];
      int delta[n+2];
9
       while(q--){
         int 1, r, x;
11
           cin >> 1 >> r >> x;
12
           delta[1] += x;
13
           delta[r+1] = x;
14
      }
16
17
       int curr = 0;
       for(int i=0; i < n; i++){
18
          curr += delta[i];
19
           v[i] = curr;
20
      }
21
22
       for(int i=0; i < n; i++){</pre>
23
         cout << v[i] << '';
25
       cout << '\n';
26
27
28
       return 0:
29 }
```

8.3 Subsets

```
void subsets(vector<int>& nums){
   int n = nums.size():
    int powSize = 1 << n;</pre>
```

```
int last_true(int lo, int hi, function < bool(int) > f)
   while (lo < hi) {
     int mid = lo + (hi - lo + 1) / 2;
4
      if (f(mid)) {
       lo = mid;
      } else {
        hi = mid - 1;
9
    }
10
    return lo:
11
12 }
```

Ternary Search

```
1 double ternary_search(double 1, double r) {
      double eps = 1e-9;
                                     //set the error
      limit here
      while (r - 1 > eps) {
3
          double m1 = 1 + (r - 1) / 3;
4
          double m2 = r - (r - 1) / 3;
5
          double f1 = f(m1);
                                 //evaluates the
      function at m1
          double f2 = f(m2); //evaluates the
      function at m2
         if (f1 < f2)
             1 = m1;
          else
10
             r = m2;
11
      }
12
      return f(1);
                                      //return the
13
      maximum of f(x) in [1, r]
```

Binary Search First True

```
int first_true(int lo, int hi, function < bool(int) > f)
      -{
    hi++;
2
   while (lo < hi) {
     int mid = lo + (hi - lo) / 2;
      if (f(mid)) {
       hi = mid;
6
      } else {
        lo = mid + 1;
      }
9
10
   }
   return lo;
11
```

Biggest K 8.7

```
_{\rm 1} // Description: Gets sum of k biggest or k smallest
                                                             elements in an array
                                                       3 // Problem: https://atcoder.jp/contests/abc306/tasks/
                                                             abc306_e
                                                       5 // Complexity: O(log n)
for(int counter = 0; counter < powSize; counter++){ 7 struct SetSum {</pre>
```

```
11 s = 0;
9
       multiset <11> mt;
      void add(ll x){
10
11
          mt.insert(x);
           s += x;
      }
13
      int pop(11 x){
14
          auto f = mt.find(x);
1.5
           if(f == mt.end()) return 0;
16
           mt.erase(f);
           s -= x;
18
19
           return 1;
      }
20
21 };
23 struct BigK {
24
      int k;
       SetSum gt, mt;
25
       BigK(int _k){
          k = _k;
27
28
       void balancear(){
29
         while((int)gt.mt.size() < k && (int)mt.mt.
30
       size()){
               auto p = (prev(mt.mt.end()));
31
               gt.add(*p);
32
33
               mt.pop(*p);
34
           while((int)mt.mt.size() && (int)gt.mt.size()
      &r. &r.
           *(gt.mt.begin()) < *(prev(mt.mt.end())) ){
36
               11 u = *(gt.mt.begin());
37
               11 v = *(prev(mt.mt.end()));
38
               gt.pop(u); mt.pop(v);
               gt.add(v); mt.add(u);
40
           }
41
      }
42
       void add(11 x){
43
           mt.add(x);
           balancear();
45
46
      void rem(ll x){
47
          //x = -x;
48
           if(mt.pop(x) == 0)
10
               gt.pop(x);
50
           balancear();
51
      }
52
53 };
54
55 int main() {
      ios::sync_with_stdio(false);
56
       cin.tie(NULL);
57
      int n, k, q; cin >> n >> k >> q;
59
60
      BigK big = BigK(k);
61
62
      int arr[n] = {};
64
       while (q--) {
65
66
         int pos, num; cin >> pos >> num;
           big.rem(arr[pos]);
           arr[pos] = num:
69
           big.add(arr[pos]);
           cout << big.gt.s << '\n';</pre>
      }
74
       return 0;
75
76 }
```

9 Data Structures

9.1 Ordered Set

```
1 // Description:
2 // insert(k) - add element k to the ordered set
3 // erase(k) - remove element k from the ordered set
4 // erase(it) - remove element it points to from the
       ordered set
5 // order_of_key(k) - returns number of elements
      strictly smaller than k
6 // find_by_order(n) - return an iterator pointing to
      the k-th element in the ordered set (counting
       from zero).
8 // Problem:
9 // https://cses.fi/problemset/task/2169/
10
11 // Complexity:
_{12} // O(log n) for all operations
_{14} // How to use:
15 // ordered_set <int> os;
16 // cout << os.order_of_key(1) << '\n;</pre>
17 // cout << os.find_by_order(1) << '\n;</pre>
_{19} // Notes
20 // The ordered set only contains different elements
21 // By using less_equal <T> instead of less <T> on using
       ordered_set declaration
22 // The ordered_set becomes an ordered_multiset
_{\rm 23} // So the set can contain elements that are equal
25 #include <ext/pb_ds/assoc_container.hpp>
26 #include <ext/pb_ds/tree_policy.hpp>
28 using namespace __gnu_pbds;
29 template <typename T>
30 using ordered_set = tree<T,null_type,less<T>,
       rb_tree_tag,tree_order_statistics_node_update>;
31
32 void Erase(ordered_set < int >& a, int x){
      int r = a.order_of_key(x);
       auto it = a.find_by_order(r);
34
       a.erase(it);
35
```

9.2 Priority Queue

```
1 // Description:
2 // Keeps the largest (by default) element at the top
      of the queue
4 // Problem:
5 // https://cses.fi/problemset/task/1164/
7 // Complexity:
8 // O(log n) for push and pop
_{9} // O (1) for looking at the element at the top
10
11 // How to use:
12 // prioriy_queue < int > pq;
13 // pq.push(1);
14 // pq.top();
15 // pq.pop()
17 // Notes
_{18} // To use the priority queue keeping the smallest
      element at the top
20 priority_queue <int, vector <int>, greater <int>> pq;
```

9.3 Dsu

```
#include <bits/stdc++.h>
3 using namespace std;
5 const int MAX = 1e6+17;
7 struct DSU {
      int n;
      vector <int > link, sizes;
10
11
      DSU(int n) {
         this ->n = n;
12
           link.assign(n+1, 0);
13
          sizes.assign(n+1, 1);
15
           for (int i = 0; i \le n; i++)
               link[i] = i;
17
      }
18
19
      int find(int x) {
20
           while (x != link[x])
21
             x = link[x];
22
23
24
           return x;
25
      bool same(int a, int b) {
27
          return find(a) == find(b);
29
30
      void unite(int a, int b) {
31
          a = find(a);
32
          b = find(b);
34
           if (a == b) return;
36
           if (sizes[a] < sizes[b])</pre>
               swap(a, b);
39
           sizes[a] += sizes[b];
           link[b] = a;
41
42
43
      int size(int x) {
44
45
           return sizes[x];
46
47 };
48
49 int main() {
       ios::sync_with_stdio(false);
       cin.tie(NULL);
51
      int cities, roads; cin >> cities >> roads;
53
       vector < int > final_roads;
54
       int ans = 0;
55
       DSU dsu = DSU(cities);
56
       for (int i = 0, a, b; i < roads; i++) {
           cin >> a >> b;
58
           dsu.unite(a, b);
59
60
61
       for (int i = 2; i <= cities; i++) {</pre>
           if (!dsu.same(1, i)) {
63
               ans++:
               final_roads.push_back(i);
65
               dsu.unite(1,i);
66
           }
      }
68
       cout << ans << '\n';</pre>
70
       for (auto e : final_roads) {
71
```

```
1 // Description
 _{2} // THe values are divided in two multisets so that
      one of them contain all values that are
 _{\mathrm{3}} // smaller than the median and the other one contains
       all values that are greater or equal to the
       median.
5 // Problem:
 6 // https://atcoder.jp/contests/abc306/tasks/abc306_e
7 // Problem I - Maratona Feminina de çãProgramao da
       Unicamp 2023
 8 // https://codeforces.com/group/WYIydkiPyE/contest
      /450037/attachments
9
10 // Complexity:
_{11} // Add and remove elements - O(log n)
12 // Return sum of biggest or smallest set or return
       the median - 0(1)
13
14 using ll = long long;
16 struct TwoSets {
17 multiset <int > small;
    multiset <int > big;
18
     11 \text{ sums} = 0:
19
     11 \text{ sumb} = 0;
20
21
    int n = 0;
22
     int size_small() {
23
      return small.size();
24
25
26
27
     int size_big() {
      return big.size();
28
29
30
     void balance() {
31
32
       while (size_small() > n / 2) {
         int v = *small.rbegin();
33
34
         small.erase(prev(small.end()));
        big.insert(v);
35
36
         sums -= v;
         sumb += v;
37
38
       while (size_big() > n - n / 2) {
39
        int v = *big.begin();
40
         big.erase(big.begin());
41
         small.insert(v);
42
43
         sumb -= v;
         sums += v;
44
45
     }
47
     void add(int x) {
48
49
      n++;
50
       small.insert(x);
51
       sums += x;
       while (!small.empty() && *small.rbegin() > *big.
52
       begin()) {
        int v = *small.rbegin();
53
         small.erase(prev(small.end()));
54
55
        big.insert(v);
56
        sums -= v;
         sumb += v;
57
       }
58
       balance();
59
```

```
}
                                                                      this -> n = n:
60
                                                           33
                                                           34
                                                                       create();
61
    bool rem(int x) {
                                                                       create();
62
                                                           35
      n - - ;
63
                                                           36
      auto it1 = small.find(x);
                                                           37
      auto it2 = big.find(x);
                                                                  ftype f(ftype a, ftype b) {
65
                                                           38
      bool flag = false;
66
                                                           39
                                                                      return a + b;
      if (it1 != small.end()) {
67
                                                           40
        sums -= *it1;
68
                                                           41
        small.erase(it1);
                                                                  ftype create() {
                                                           42
         flag = true;
                                                                      seg.push_back(0);
70
                                                           43
71
      } else if (it2 != big.end()) {
                                                           44
                                                                       e.push_back(0);
         sumb -= *it2;
72
                                                           45
                                                                      d.push_back(0);
         big.erase(it2);
                                                                      return seg.size() - 1;
73
                                                           46
                                                                  7
74
         flag = true;
                                                           47
75
                                                           48
76
      balance();
                                                            49
                                                                   ftype query(int pos, int ini, int fim, int p, int
77
      return flag;
                                                                      if (q < ini || p > fim) return NEUTRAL;
                                                                      if (pos == 0) return 0;
79
                                                           51
    11 sum_small() {
                                                                       if (p <= ini && fim <= q) return seg[pos];</pre>
                                                           52
80
                                                                       int m = (ini + fim) >> 1;
      return sums;
81
                                                           53
                                                                       return f(query(e[pos], ini, m, p, q), query(d
82
                                                           54
                                                                   [pos], m + 1, fim, p, q));
    11 sum_big() {
84
                                                           55
      return sumb;
85
                                                           56
                                                                  void update(int pos, int ini, int fim, int id,
86
                                                           57
                                                                  int val) {
87
    int median() {
                                                                      if (ini > id || fim < id) {</pre>
                                                           58
      return *big.begin();
                                                                           return:
89
                                                           59
90
                                                           60
91 };
                                                           61
                                                                       if (ini == fim) {
                                                           62
        Dynamic Implicit Sparse
                                                                           seg[pos] = val;
                                                           64
1 // Description:
                                                                           return;
                                                                      }
2 // Indexed at one
                                                           66
                                                           67
                                                                      int m = (ini + fim) >> 1;
_{4} // When the indexes of the nodes are too big to be
                                                           69
      stored in an array
_{5} // and the queries need to be answered online so we
                                                                       if (id <= m) {
                                                                           if (e[pos] == 0) e[pos] = create();
      can't sort the nodes and compress them
                                                           71
                                                                           update(e[pos], ini, m, id, val);
_{6} // we create nodes only when they are needed so there ^{72}
                                                           73
                                                                       } else {
      'll be (Q*log(MAX)) nodes
                                                                           if (d[pos] == 0) d[pos] = create();
_{7} // where Q is the number of queries and MAX is the
                                                           74
                                                                           update(d[pos], m + 1, fim, id, val);
      maximum index a node can assume
                                                           76
9 // Query - get sum of elements from range (1, r)
                                                                       seg[pos] = f(seg[e[pos]], seg[d[pos]]);
      inclusive
                                                            78
_{
m 10} // Update - update element at position id to a value ^{
m 79}
                                                                   ftype query(int p, int q) {
                                                           81
                                                                      return query(1, 1, n, p, q);
12 // Problem:
13 // https://cses.fi/problemset/task/1648
                                                           83
                                                           84
                                                                  void update(int id, int val) {
                                                           85
15 // Complexity:
                                                                      update(1, 1, n, id, val);
                                                           86
16 // O(log n) for both query and update
                                                           87
18 // How to use:
                                                           88 }:
_{\rm 19} // MAX is the maximum index a node can assume
                                                                   Segtree2d
21 // Segtree seg = Segtree(MAX);
                                                            1 // Description:
23 typedef long long ftype;
                                                            2 // Indexed at zero
                                                            _{\rm 3} // Given a N x M grid, where i represents the row and
24
25 const int MAX = 1e9+17;
                                                                   j the column, perform the following operations
                                                            _4 // update(j, i) - update the value of grid[i][j]
                                                            5 // query(j1, j2, i1, i2) - return the sum of values
27 struct Segtree {
      vector<ftype> seg, d, e;
                                                                  inside the rectangle
      const ftype NEUTRAL = 0;
                                                            6 // defined by grid[i1][j1] and grid[i2][j2] inclusive
29
      int n;
                                                            8 // Problem:
31
      Segtree(int n) {
                                                            9 // https://cses.fi/problemset/task/1739/
32
```

```
updateY(noX, lX, rX, 2*noY+1,lY, m, y
10
11 // Complexity:
                                                                   );
12 // Time complexity:
                                                                            else if(m < v)
_{13} // O(log N * log M) for both query and update
                                                                                updateY(noX, 1X, rX, 2*noY+2, m+1, rY
                                                            79
_{14} // O(N * M) for build
                                                                    , y);
15 // Memory complexity:
                                                            80
16 // 4 * M * N
                                                            81
                                                                            seg[noX][noY] = seg[noX][2*noY+1] + seg[
17
                                                            82
18 // How to use:
                                                                   noX][2*noY+2];
19 // Segtree2D seg = Segtree2D(n, n);
                                                            83
                                                                        }
20 // vector < vector < int >> v(n, vector < int >(n));
                                                                   }
                                                            84
21 // seg.build(v);
                                                                   void updateX(int noX, int lX, int rX, int x, int
22
                                                            86
23 // Notes
_{24} // Indexed at zero
                                                                        int m = (1X+rX)/2:
                                                            87
25
                                                            88
26 struct Segtree2D {
                                                                        if(1X != rX){
      const int MAXN = 1025;
                                                                            if(x \ll m){
27
                                                            90
      int N. M:
                                                                                updateX(2*noX+1, 1X, m, x, y);
29
                                                            92
                                                                            else if(m < x)
      vector < vector < int >> seg;
                                                                                updateX(2*noX+2, m+1, rX, x, y);
                                                            93
30
31
                                                            94
       Segtree2D(int N, int M) {
                                                                        }
32
                                                            95
           this ->N = N;
           this ->M = M;
                                                                        updateY(noX, 1X, rX, 0, 0, M - 1, y);
34
                                                            97
           seg.resize(2*MAXN, vector<int>(2*MAXN));
35
                                                            98
36
                                                            99
                                                                   int queryY(int noX, int noY, int lY, int rY, int
37
                                                            100
       void buildY(int noX, int 1X, int rX, int noY, int
                                                                   aY, int bY){
38
                                                                        if(aY <= 1Y && rY <= bY) return seg[noX][noY</pre>
       1Y, int rY, vector < vector < int >> &v) {
                                                            101
           if(1Y == rY){
39
               if(1X == rX){
40
                                                            102
                    seg[noX][noY] = v[rX][rY];
                                                                        int m = (1Y+rY)/2;
                                                            103
41
42
                    seg[noX][noY] = seg[2*noX+1][noY] +
                                                                        if(bY <= m) return queryY(noX, 2*noY+1, 1Y, m</pre>
43
                                                           105
       seg[2*noX+2][noY];
                                                                    , aY, bY);
               }
                                                                        if (m < aY) return queryY(noX, 2*noY+2, m+1,
44
                                                            106
           }else{
                                                                   rY, aY, bY);
45
               int m = (1Y+rY)/2;
46
                                                            107
                                                                        return queryY(noX, 2*noY+1, 1Y, m, aY, bY) +
47
                                                            108
               buildY(noX, 1X, rX, 2*noY+1, 1Y, m, v);
                                                                   queryY(noX, 2*noY+2, m+1, rY, aY, bY);
               buildY(noX, 1X, rX, 2*noY+2, m+1, rY, v);109
49
50
               seg[noX][noY] = seg[noX][2*noY+1] + seg[_{111}
                                                                   int queryX(int noX, int 1X, int rX, int aX, int
51
      noX][2*noY+2];
                                                                   bX, int aY, int bY){
          }
                                                                        if(aX <= 1X && rX <= bX) return queryY(noX,
52
      }
                                                                   0, 0, M - 1, aY, bY);
53
       void buildX(int noX, int 1X, int rX, vector<</pre>
                                                                        int m = (1X+rX)/2;
55
                                                            114
       vector <int>> &v){
                                                            115
          if(1X != rX){
                                                                        if(bX <= m) return queryX(2*noX+1, 1X, m, aX,</pre>
56
                                                            116
               int m = (1X+rX)/2;
                                                                    bX, aY, bY);
57
                                                                        if (m < aX) return queryX(2*noX+2, m+1, rX, aX
               buildX(2*noX+1, 1X, m, v);
                                                                    , bX, aY, bY);
59
               buildX(2*noX+2, m+1, rX, v);
60
                                                            118
                                                                        return queryX(2*noX+1, lX, m, aX, bX, aY, bY)
61
                                                            119
                                                                    + queryX(2*noX+2, m+1, rX, aX, bX, aY, bY);
62
           buildY(noX, 1X, rX, 0, 0, M - 1, v);
63
                                                            120
64
      }
                                                            121
                                                                   void build(vector<vector<int>> &v) {
65
                                                            122
      void updateY(int noX, int lX, int rX, int noY,
                                                                       buildX(0, 0, N - 1, v);
66
                                                            123
      int lY, int rY, int y){
                                                            124
           if(1Y == rY){
67
                                                            125
                                                                   int query(int aX, int bX, int aY, int bY) {
               if(1X == rX){
68
                                                            126
                    seg[noX][noY] = !seg[noX][noY];
                                                            127
                                                                        return queryX(0, 0, N - 1, aX, bX, aY, bY);
70
                                                            128
                    seg[noX][noY] = seg[2*noX+1][noY] +
                                                           129
71
      seg[2*noX+2][noY];
                                                                   void update(int x, int y) {
                                                            130
               }
                                                                        updateX(0, 0, N - 1, x, y);
72
                                                            131
           }else{
                                                            132
               int m = (1Y+rY)/2;
                                                            133 };
74
75
               if(y <= m){
76
```

```
9.7 Minimum And Amount
                                                                     if (ini == id && fim == id) {
                                                                          seg[pos] = mp(val, 1);
1 // Description:
                                                          67
_{2} // Query - get minimum element in a range (1, r)
                                                          68
      inclusive
                                                                          return;
_3 // and also the number of times it appears in that
                                                          70
                                                                     int e = 2*pos + 1:
_4 // Update - update element at position id to a value
                                                                     int d = 2*pos + 2;
      val
                                                           73
                                                                     int m = ini + (fim - ini) / 2;
                                                          74
6 // Problem:
                                                          75
7 // https://codeforces.com/edu/course/2/lesson/4/1/
                                                                      update(e, ini, m, id, val);
                                                                      update(d, m + 1, fim, id, val);
      practice/contest/273169/problem/C
                                                          77
                                                          78
                                                                     seg[pos] = f(seg[e], seg[d]);
9 // Complexity:
                                                          79
                                                          80
_{10} // O(log n) for both query and update
                                                          81
11
                                                                 void build(int pos, int ini, int fim, vector<int>
_{12} // How to use:
                                                          82
13 // Segtree seg = Segtree(n);
                                                                  &v) {
                                                                     if (ini == fim) {
14 // seg.build(v);
                                                          83
                                                                          if (ini < (int)v.size()) {</pre>
                                                          84
                                                                              seg[pos] = mp(v[ini], 1);
16 #define pii pair<int, int>
                                                          85
17 #define mp make_pair
                                                          86
                                                                          return;
18 #define ff first
                                                          87
                                                                     }
                                                          88
19 #define ss second
                                                          89
                                                                     int e = 2*pos + 1;
21 const int INF = 1e9+17;
                                                          90
                                                                      int d = 2*pos + 2;
                                                          91
                                                                     int m = ini + (fim - ini) / 2;
23 typedef pii ftype;
                                                          92
                                                          93
                                                          94
                                                                      build(e, ini, m, v);
25 struct Segtree {
                                                                     build(d, m + 1, fim, v);
      vector<ftype> seg;
                                                          95
26
                                                          96
      int n;
27
      const ftype NEUTRAL = mp(INF, 0);
                                                          97
                                                                      seg[pos] = f(seg[e], seg[d]);
28
                                                          98
      Segtree(int n) {
30
                                                                 ftype query(int p, int q) {
          int sz = 1;
                                                          100
31
          while (sz < n) sz *= 2;
                                                          101
                                                                     return query (0, 0, n - 1, p, q);
32
                                                          102
          this ->n = sz;
33
                                                          103
                                                                 void update(int id, int val) {
                                                          104
          seg.assign(2*sz, NEUTRAL);
35
                                                                     update(0, 0, n - 1, id, val);
                                                          105
                                                          106
37
                                                          107
      ftype f(ftype a, ftype b) {
38
                                                                 void build(vector<int> &v) {
                                                          108
39
          if (a.ff < b.ff) return a;
                                                          109
                                                                     build(0, 0, n - 1, v);
          if (b.ff < a.ff) return b;
40
                                                          110
          return mp(a.ff, a.ss + b.ss);
42
                                                                 void debug() {
43
                                                          112
                                                                     for (auto e : seg) {
                                                          113
44
                                                                          cout << e.ff << ' ' << e.ss << '\n';</pre>
      ftype query(int pos, int ini, int fim, int p, int114
45
                                                         115
                                                                      cout << '\n';</pre>
          if (ini >= p && fim <= q) {
46
                                                          117
              return seg[pos];
                                                          118 };
          }
48
49
                                                                  Lazy Addition To Segment
           if (q < ini || p > fim) {
              return NEUTRAL;
51
          }
                                                           1 // Description:
53
                                                           2 // Query - get sum of elements from range (1, r)
           int e = 2*pos + 1;
                                                                 inclusive
54
           int d = 2*pos + 2;
                                                           _{\rm 3} // Update - add a value val to elementos from range (
          int m = ini + (fim - ini) / 2;
                                                                 l, r) inclusive
56
          return f(query(e, ini, m, p, q), query(d, m + 5 // Problem:
58
                                                           6 // https://codeforces.com/edu/course/2/lesson/5/1/
       1, fim, p, q));
59
                                                                 practice/contest/279634/problem/A
60
                                                           8 // Complexity:
      void update(int pos, int ini, int fim, int id,
      int val) {
                                                           9 // O(log n) for both query and update
          if (ini > id || fim < id) {
                                                           11 // How to use:
63
               return;
                                                           12 // Segtree seg = Segtree(n);
64
```

65

```
return f(query(e, ini, m, p, q), query(d, m +
13 // seg.build(v);
                                                            81
                                                                   1, fim, p, q));
15 // Notes
                                                            82
16 // Change neutral element and f function to perform a 83
       different operation
                                                                   void update(int pos, int ini, int fim, int p, int
                                                                   q, int val) {
17
                                                                       propagate(pos, ini, fim);
18 const long long INF = 1e18+10;
19
                                                            86
20 typedef long long ftype;
                                                                       if (ini > q || fim < p) {
                                                            87
                                                                           return;
                                                            88
22 struct Segtree {
                                                            89
      vector<ftype> seg;
                                                            90
       vector<ftype> lazy;
                                                                       if (ini >= p && fim <= q) {
24
                                                            91
                                                                           lazy[pos] = apply_lazy(lazy[pos], val, 1)
       int n;
25
       const ftype NEUTRAL = 0;
26
       const ftype NEUTRAL_LAZY = -1; // change to -INF 93
                                                                           seg[pos] = apply_lazy(seg[pos], val, fim
27
       if there are negative numbers
                                                                   - ini + 1);
28
       Segtree(int n) {
                                                                           return;
                                                                       }
           int sz = 1;
30
                                                            96
           while (sz < n) sz *= 2;
                                                            97
31
                                                                       int e = 2*pos + 1;
           this->n = sz;
32
                                                            98
                                                                       int d = 2*pos + 2;
33
                                                           99
           seg.assign(2*sz, NEUTRAL);
                                                                       int m = ini + (fim - ini) / 2;
           lazy.assign(2*sz, NEUTRAL_LAZY);
35
                                                           101
       }
                                                                       update(e, ini, m, p, q, val);
36
                                                           102
                                                                       update(d, m + 1, fim, p, q, val);
37
                                                           103
       ftype apply_lazy(ftype a, ftype b, int len) {
38
                                                           104
           if (b == NEUTRAL_LAZY) return a;
                                                                       seg[pos] = f(seg[e], seg[d]);
39
                                                           105
           if (a == NEUTRAL_LAZY) return b * len;
                                                                   }
40
                                                           106
           else return a + b * len;
41
                                                           107
                                                                   void build(int pos, int ini, int fim, vector<int>
42
                                                           108
                                                                    &v) {
43
44
       void propagate(int pos, int ini, int fim) {
                                                           109
                                                                       if (ini == fim) {
           if (ini == fim) {
                                                                           if (ini < (int)v.size()) {</pre>
45
                                                           110
               return;
                                                                                seg[pos] = v[ini];
                                                           111
           }
47
                                                           112
                                                           113
                                                                           return;
48
           int e = 2*pos + 1;
                                                                       }
49
                                                           114
           int d = 2*pos + 2;
50
                                                           115
                                                                       int e = 2*pos + 1;
51
           int m = ini + (fim - ini) / 2;
                                                           116
                                                                       int d = 2*pos + 2;
52
                                                           117
           lazy[e] = apply_lazy(lazy[e], lazy[pos], 1); 118
                                                                       int m = ini + (fim - ini) / 2;
53
54
           lazy[d] = apply_lazy(lazy[d], lazy[pos], 1); 119
                                                                       build(e, ini, m, v);
55
           seg[e] = apply_lazy(seg[e], lazy[pos], m -
                                                                       build(d, m + 1, fim, v);
56
                                                           121
       ini + 1):
           seg[d] = apply_lazy(seg[d], lazy[pos], fim - 123
                                                                       seg[pos] = f(seg[e], seg[d]);
                                                                   }
      m):
                                                           124
58
                                                           125
           lazy[pos] = NEUTRAL_LAZY;
                                                                   ftype query(int p, int q) {
59
                                                           126
                                                                       return query(0, 0, n - 1, p, q);
60
                                                           127
                                                           128
       ftype f(ftype a, ftype b) {
62
                                                           129
                                                                   void update(int p, int q, int val) {
           return a + b;
                                                           130
63
                                                                       update(0, 0, n - 1, p, q, val);
64
                                                           131
65
                                                           132
       ftype query(int pos, int ini, int fim, int p, int133
66
                                                                   void build(vector<int> &v) {
       a) {
                                                           134
           propagate(pos, ini, fim);
                                                                       build(0, 0, n - 1, v);
67
                                                           135
                                                           136
68
           if (ini >= p && fim <= q) {
                                                           137
69
               return seg[pos];
                                                                   void debug() {
70
                                                           138
           }
                                                                       for (auto e : seg) {
71
                                                           139
                                                                            cout << e << ' ';
           if (q < ini || p > fim) {
                                                                       }
73
                                                           141
                                                                       cout << '\n';
               return NEUTRAL;
74
                                                           142
           }
                                                                       for (auto e : lazy) {
75
                                                           143
                                                                           cout << e << ' ';
76
                                                           144
           int e = 2*pos + 1;
                                                                       }
                                                           145
           int d = 2*pos + 2;
                                                                       cout << '\n';
78
                                                           146
           int m = ini + (fim - ini) / 2;
                                                                       cout << '\n';
                                                           147
80
                                                           148
                                                                   }
```

149 }; 61 62 Segment With Maximum Sum 9.9ftype query(int pos, int ini, int fim, int p, int 63 1 // Description: if (ini >= p && fim <= q) { return seg[pos]; 2 // Query - get sum of segment that is maximum among 65 all segments 3 // E.g 67 if (q < ini || p > fim) { 4 // Array: 5 -4 4 3 -5 68 return NEUTRAL; $_{5}$ // Maximum segment sum: 8 because 5 + (-4) + 4 = 8 $_{\rm 6}$ // Update - update element at position id to a value $^{\rm 70}$ val int e = 2*pos + 1;72 8 // Problem: int d = 2*pos + 2;73 int m = ini + (fim - ini) / 2; 9 // https://codeforces.com/edu/course/2/lesson/4/2/ 74 75 practice/contest/273278/problem/A return f(query(e, ini, m, p, q), query(d, m + 10 1, fim, p, q)); 11 // Complexity: $_{12}$ // O(log n) for both query and update 77 78 void update(int pos, int ini, int fim, int id, 14 // How to use: 79 int val) { 15 // Segtree seg = Segtree(n); if (ini > id || fim < id) { 16 // seg.build(v); 80 return; 82 19 // The maximum segment sum can be a negative number 83 if (ini == id && fim == id) { 20 // In that case, taking zero elements is the best 84 seg[pos] = Node(val, val, val, val); choice 85 $_{ m 21}$ // So we need to take the maximum between 0 and the return: 87 } 88 22 // max(OLL, seg.query(0, n).max_seg) 89 int e = 2*pos + 1;90 24 using ll = long long; 91 int d = 2*pos + 2;int m = ini + (fim - ini) / 2; 26 typedef ll ftype_node; 92 27 update(e, ini, m, id, val); 28 struct Node { 94 update(d, m + 1, fim, id, val); 95 29 ftype_node max_seg; 96 ftype_node pref; 30 seg[pos] = f(seg[e], seg[d]); 97 ftype_node suf; 98 ftype_node sum; 32 99 void build(int pos, int ini, int fim, vector<int> 34 Node(ftype_node max_seg, ftype_node pref, ftype_node suf, ftype_node sum) : max_seg(max_seg &v) { if (ini == fim) {), pref(pref), suf(suf), sum(sum) {}; // se a çãposio existir no array original 35 }; // seg tamanho potencia de dois 103 if (ini < (int)v.size()) {</pre> 37 typedef Node ftype; seg[pos] = Node(v[ini], v[ini], v[ini 38], v[ini]); 39 struct Segtree { } vector<ftype> seg; 106 40 int n; 107 return: 41 } const ftype NEUTRAL = Node(0, 0, 0, 0); 42 109 43 int e = 2*pos + 1;Segtree(int n) { 110 44 int d = 2*pos + 2;111 int sz = 1; 45 int m = ini + (fim - ini) / 2; 112 // potencia de dois mais proxima 46 while (sz < n) sz *= 2;113 47 build(e, ini, m, v); this->n = sz; 114 build(d, m + 1, fim, v); 115 49 // numero de nos da seg 116 50 seg[pos] = f(seg[e], seg[d]); 117 seg.assign(2*sz, NEUTRAL); 51 } 118 52 53 119 ftype query(int p, int q) { ftype f(ftype a, ftype b) { 54 return query(0, 0, n - 1, p, q); ftype_node max_seg = max({a.max_seg, b. 121 max_seg, a.suf + b.pref}); 122 ftype_node pref = max(a.pref, a.sum + b.pref)123 56 void update(int id, int val) { 124 ftype_node suf = max(b.suf, b.sum + a.suf); update(0, 0, n - 1, id, val); 125 57 ftype_node sum = a.sum + b.sum; 126 59 128 void build(vector<int> &v) { return Node(max_seg, pref, suf, sum); 60

```
build(0, 0, n - 1, v);
                                                                       int d = 2*pos + 2;
129
                                                            53
130
                                                            54
                                                                       int m = ini + (fim - ini) / 2;
131
                                                            55
       void debug() {
                                                                       return f(query(e, ini, m, p, q), query(d, m +
132
                                                            56
           for (auto e : seg) {
                                                                    1, fim, p, q));
               cout << e.max_seg << ', ' << e.pref << ', '57</pre>
134
        << e.suf << ' ' << e.sum << '\n';
                                                            58
                                                                   void update(int pos, int ini, int fim, int id,
135
                                                            59
           cout << '\n';</pre>
                                                                   int val) {
136
                                                                       if (ini > id || fim < id) {</pre>
137
                                                            60
138 };
                                                                           return;
                                                            61
           Range Query Point Update
                                                            63
                                                                       if (ini == id && fim == id) {
 1 // Description:
                                                            65
                                                                           seg[pos] = val;
                                                            66
 _2 // Indexed at zero
 3 // Query - get sum of elements from range (1, r)
                                                                           return;
       inclusive
 _4 // Update - update element at position id to a value ^{69}
                                                                       int e = 2*pos + 1;
                                                                       int d = 2*pos + 2;
                                                            71
 6 // Problem:
                                                                       int m = ini + (fim - ini) / 2;
                                                            72
 7 // https://codeforces.com/edu/course/2/lesson/4/1/
                                                            73
       practice/contest/273169/problem/B
                                                                       update(e, ini, m, id, val);
                                                                       update(d, m + 1, fim, id, val);
                                                            75
 9 // Complexity:
                                                            76
                                                                       seg[pos] = f(seg[e], seg[d]);
10 // O(\log n) for both query and update
                                                            77
                                                            78
12 // How to use:
                                                            79
                                                                   void build(int pos, int ini, int fim, vector<int>
13 // Segtree seg = Segtree(n);
                                                            80
                                                                    &v) {
14 // seg.build(v);
                                                                       if (ini == fim) {
                                                            81
                                                                           if (ini < (int)v.size()) {</pre>
16 // Notes
                                                            82
_{17} // Change neutral element and f function to perform a ^{83}
                                                                                seg[pos] = v[ini];
                                                                           }
       different operation
                                                                           return;
                                                                       }
19 // If you want to change the operations to point
                                                            86
       query and range update
                                                            87
                                                                       int e = 2*pos + 1;
20 // Use the same segtree, but perform the following
                                                                       int d = 2*pos + 2;
       operations
                                                            89
21 // Query - seg.query(0, id);
                                                                       int m = ini + (fim - ini) / 2;
22 // Update - seg.update(1, v); seg.update(r + 1, -v);
                                                            91
                                                                       build(e, ini, m, v);
24 typedef long long ftype;
                                                            93
                                                                       build(d, m + 1, fim, v);
                                                            94
25
                                                            95
                                                                       seg[pos] = f(seg[e], seg[d]);
26 struct Segtree {
       vector <ftype > seg;
27
                                                            96
       int n;
28
                                                                   ftype query(int p, int q) {
       const ftype NEUTRAL = 0;
                                                            98
                                                            99
                                                                       return query(0, 0, n - 1, p, q);
30
                                                           100
       Segtree(int n) {
31
           int sz = 1;
                                                           101
           while (sz < n) sz *= 2;
                                                                   void update(int id, int val) {
                                                           102
33
                                                                       update(0, 0, n - 1, id, val);
           this ->n = sz;
                                                           103
                                                           104
35
                                                           105
           seg.assign(2*sz, NEUTRAL);
36
                                                                   void build(vector<int> &v) {
       }
                                                           106
37
                                                                       build(0, 0, n - 1, v);
                                                           107
38
       ftype f(ftype a, ftype b) {
                                                           108
                                                                   }
                                                           109
40
           return a + b;
                                                                   void debug() {
                                                           110
41
                                                                       for (auto e : seg) {
                                                           111
42
                                                                           cout << e << ' ';
       ftype query(int pos, int ini, int fim, int p, int112
43
                                                                       cout << '\n';</pre>
           if (ini >= p && fim <= q) {
44
                                                                   }
                return seg[pos];
                                                           115
45
                                                           116 };
46
47
                                                                      Lazy Assignment To Segment
                                                              9.11
            if (q < ini || p > fim) {
                return NEUTRAL;
49
                                                             const long long INF = 1e18+10;
51
           int e = 2*pos + 1;
                                                             3 typedef long long ftype;
52
```

```
71
5 struct Segtree {
                                                           72
                                                                      if (ini > q || fim < p) {
      vector<ftype> seg;
                                                           73
                                                                          return;
      vector<ftype> lazy;
                                                           74
      int n;
      const ftype NEUTRAL = 0;
                                                                      if (ini >= p && fim <= q) {</pre>
9
                                                           76
      const ftype NEUTRAL_LAZY = -1; // Change to -INF
                                                                           lazy[pos] = apply_lazy(lazy[pos], val, 1)
10
      if there are negative numbers
                                                                          seg[pos] = apply_lazy(seg[pos], val, fim
11
      Segtree(int n) {
                                                                  - ini + 1);
12
          int sz = 1:
13
                                                           79
           // potencia de dois mais proxima
                                                                          return;
                                                                      }
15
           while (sz < n) sz *= 2;
                                                           81
          this ->n = sz;
16
                                                           82
                                                                      int e = 2*pos + 1;
17
                                                           83
                                                                      int d = 2*pos + 2;
           // numero de nos da seg
18
                                                           84
19
           seg.assign(2*sz, NEUTRAL);
                                                                      int m = ini + (fim - ini) / 2;
           lazy.assign(2*sz, NEUTRAL_LAZY);
20
                                                           86
                                                                      update(e, ini, m, p, q, val);
                                                                      update(d, m + 1, fim, p, q, val);
22
                                                           88
      ftype apply_lazy(ftype a, ftype b, int len) {
23
                                                           89
           if (b == NEUTRAL_LAZY) return a;
                                                                      seg[pos] = f(seg[e], seg[d]);
24
                                                           90
           if (a == NEUTRAL_LAZY) return b * len;
25
                                                           91
           else return b * len;
                                                           92
                                                                  void build(int pos, int ini, int fim, vector<int>
27
                                                           93
                                                                   &v) {
28
      void propagate(int pos, int ini, int fim) {
                                                                      if (ini == fim) {
29
          if (ini == fim) {
                                                                          // se a çãposio existir no array original
30
                                                           95
               return;
                                                                           // seg tamanho potencia de dois
31
                                                           96
          }
                                                                          if (ini < (int)v.size()) {</pre>
32
                                                           97
                                                           98
                                                                              seg[pos] = v[ini];
33
          int e = 2*pos + 1;
34
                                                           99
          int d = 2*pos + 2;
                                                                          return;
                                                          100
35
          int m = ini + (fim - ini) / 2;
                                                                      }
37
                                                          102
           lazy[e] = apply_lazy(lazy[e], lazy[pos], 1); 103
                                                                      int e = 2*pos + 1;
          lazy[d] = apply_lazy(lazy[d], lazy[pos], 1); 104
                                                                      int d = 2*pos + 2;
39
                                                                      int m = ini + (fim - ini) / 2;
40
          seg[e] = apply_lazy(seg[e], lazy[pos], m -
41
                                                                      build(e, ini, m, v);
      ini + 1);
                                                          107
                                                                      build(d, m + 1, fim, v);
42
           seg[d] = apply_lazy(seg[d], lazy[pos], fim - 108
      m):
                                                          109
                                                                      seg[pos] = f(seg[e], seg[d]);
43
                                                          110
44
           lazy[pos] = NEUTRAL_LAZY;
                                                          111
                                                                  7
                                                          112
45
                                                          113
                                                                  ftype query(int p, int q) {
46
      ftype f(ftype a, ftype b) {
                                                                      return query(0, 0, n - 1, p, q);
47
                                                          114
          return a + b;
49
                                                          116
                                                                  void update(int p, int q, int val) {
50
                                                          117
      ftype query(int pos, int ini, int fim, int p, int118
                                                                      update(0, 0, n - 1, p, q, val);
51
                                                          119
          propagate(pos, ini, fim);
52
                                                                  void build(vector<int> &v) {
53
                                                          121
           if (ini >= p && fim <= q) {
                                                          122
                                                                      build(0, 0, n - 1, v);
54
55
               return seg[pos];
                                                          123
                                                          124
56
                                                                  void debug() {
                                                          125
          if (q < ini || p > fim) {
58
                                                          126
                                                                      for (auto e : seg) {
               return NEUTRAL;
                                                                          cout << e << '';
                                                          127
59
          }
                                                                      }
60
                                                          128
                                                                      cout << '\n';
                                                          129
61
          int e = 2*pos + 1;
                                                                      for (auto e : lazy) {
                                                          130
          int d = 2*pos + 2;
                                                                          cout << e << ' ':
63
                                                          131
           int m = ini + (fim - ini) / 2;
                                                                      cout << '\n':
65
          return f(query(e, ini, m, p, q), query(d, m +134
                                                                      cout << '\n';
66
       1, fim, p, q));
                                                                  }
                                                          136 }:
67
                                                                     Lazy Dynamic Implicit Sparse
      void update(int pos, int ini, int fim, int p, int 9.12
69
       q, int val) {
70
          propagate(pos, ini, fim);
                                                            1 // Description:
```

```
2 // Indexed at one
                                                                  pos], fim - m);
                                                           64
_{\rm 4} // When the indexes of the nodes are too big to be
                                                                      lazy[pos] = NEUTRAL_LAZY;
                                                           65
      stored in an array
                                                           66
_{5} // and the queries need to be answered online so we
      can't sort the nodes and compress them
                                                                  ftype f(ftype a, ftype b) {
                                                           68
_{6} // we create nodes only when they are needed so there _{69}
                                                                      return a + b;
      'll be (Q*log(MAX)) nodes
                                                           70
_{7} // where Q is the number of queries and MAX is the
                                                           71
      maximum index a node can assume
                                                                  ftype create() {
                                                           72
                                                                      seg.push_back(0);
                                                           73
9 // Query - get sum of elements from range (1, r)
                                                           74
                                                                      e.push_back(0);
                                                                      d.push_back(0);
      inclusive
                                                           75
_{10} // Update - update element at position id to a value _{76}
                                                                      lazy.push_back(-1);
      val
                                                           77
                                                                      return seg.size() - 1;
11
                                                           78
12 // Problem:
13 // https://oj.uz/problem/view/IZhO12_apple
                                                                  ftype query(int pos, int ini, int fim, int p, int
                                                           80
                                                                   q) {
15 // Complexity:
                                                                      propagate(pos, ini, fim);
                                                           81
_{16} // O(log n) for both query and update
                                                                      if (q < ini || p > fim) return NEUTRAL;
                                                           82
                                                                      if (pos == 0) return 0;
18 // How to use:
                                                                      if (p <= ini && fim <= q) return seg[pos];</pre>
                                                           84
_{
m 19} // MAX is the maximum index a node can assume
                                                                      int m = (ini + fim) >> 1;
20 // Create a default null node
                                                                      return f(query(e[pos], ini, m, p, q), query(d
                                                           86
                                                                  [pos], m + 1, fim, p, q));
21 // Create a node to be the root of the segtree
                                                           87
23 // Segtree seg = Segtree(MAX);
                                                           88
                                                                  void update(int pos, int ini, int fim, int p, int
                                                           89
25 const int MAX = 1e9+10;
                                                                   q, int val) {
26 const long long INF = 1e18+10;
                                                                      propagate(pos, ini, fim);
                                                           90
                                                                      if (ini > q || fim < p) {
                                                           91
28 typedef long long ftype;
                                                                          return;
                                                           92
29
30 struct Segtree {
                                                           94
      vector<ftype> seg, d, e, lazy;
                                                                      if (ini >= p && fim <= q) {
31
      const ftype NEUTRAL = 0;
                                                                          lazy[pos] = apply_lazy(lazy[pos], val, 1)
32
      const ftype NEUTRAL_LAZY = -1; // change to -INF
33
      if the elements can be negative
                                                                          seg[pos] = apply_lazy(seg[pos], val, fim
                                                                  - ini + 1);
      int n:
34
35
      Segtree(int n) {
36
                                                           99
                                                                          return;
          this ->n = n;
37
                                                          100
           create();
                                                          101
38
           create();
                                                                      int m = (ini + fim) >> 1;
                                                          102
39
      }
40
                                                          103
                                                                      if (e[pos] == 0) e[pos] = create();
41
                                                          104
      ftype apply_lazy(ftype a, ftype b, int len) {
                                                                      update(e[pos], ini, m, p, q, val);
           if (b == NEUTRAL_LAZY) return a;
43
                                                          106
           else return b * len; // change to a + b * len107
                                                                      if (d[pos] == 0) d[pos] = create();
44
       to add to an element instead of updating it
                                                                      update(d[pos], m + 1, fim, p, q, val);
45
                                                          109
                                                                      seg[pos] = f(seg[e[pos]], seg[d[pos]]);
      void propagate(int pos, int ini, int fim) {
47
                                                          111
          if (seg[pos] == 0) return;
48
                                                          112
                                                                  ftype query(int p, int q) {
                                                          113
49
           if (ini == fim) {
                                                                      return query(1, 1, n, p, q);
                                                          114
50
               return;
                                                          115
52
          }
                                                          116
                                                                  void update(int p, int q, int val) {
                                                          117
53
          int m = (ini + fim) >> 1;
                                                          118
                                                                      update(1, 1, n, p, q, val);
54
                                                          119
55
           if (e[pos] == 0) e[pos] = create();
                                                          120 };
          if (d[pos] == 0) d[pos] = create();
57
                                                             9.13
                                                                     Persistent
          lazy[e[pos]] = apply_lazy(lazy[e[pos]], lazy[
59
      pos], 1);
                                                            _{1} // Description:
          lazy[d[pos]] = apply_lazy(lazy[d[pos]], lazy[ 2 // Persistent segtree allows for you to save the
60
      pos], 1);
                                                                  different versions of the segtree between each
                                                                  update
           seg[e[pos]] = apply_lazy(seg[e[pos]], lazy[
                                                            3 // Indexed at one
62
      pos], m - ini + 1);
                                                            _{\rm 4} // Query - get sum of elements from range (1, r)
63
           seg[d[pos]] = apply_lazy(seg[d[pos]], lazy[
                                                                  inclusive
```

```
5 // Update - update element at position id to a value 46
                                                                 ftype query(int pos, int ini, int fim, int p, int
                                                           48
7 // Problem:
8 // https://cses.fi/problemset/task/1737/
                                                           49
                                                                     if (q < ini || p > fim) return NEUTRAL;
                                                                     if (pos == 0) return 0;
                                                          50
                                                                      if (p <= ini && fim <= q) return seg[pos];</pre>
10 // Complexity:
                                                           51
                                                                     int m = (ini + fim) >> 1;
_{11} // O(log n) for both query and update
                                                          52
                                                                     return f(query(e[pos], ini, m, p, q), query(d
                                                          53
_{13} // How to use:
                                                                 [pos], m + 1, fim, p, q));
_{14} // vector<int> raiz(MAX); // vector to store the
                                                          54
      roots of each version
15 // Segtree seg = Segtree(INF);
                                                                 int update(int pos, int ini, int fim, int id, int
                                                          56
16 // raiz[0] = seg.create(); // null node
                                                                  val) {
_{17} // curr = 1; // keep track of the last version
                                                                     int novo = create();
                                                          57
                                                          58
19 // raiz[k] = seg.update(raiz[k], idx, val); //
                                                                      seg[novo] = seg[pos];
                                                                     e[novo] = e[pos];
      updating version k
                                                          60
20 // seg.query(raiz[k], l, r) // querying version k
                                                                     d[novo] = d[pos];
_{21} // raiz[++curr] = raiz[k]; // create a new version
                                                          62
      based on version k
                                                                      if (ini == fim) {
                                                          63
                                                                          seg[novo] = val;
                                                           64
23 const int MAX = 2e5+17;
                                                          65
                                                                          return novo;
                                                                      }
24 const int INF = 1e9+17;
                                                          66
25
                                                          67
26 typedef long long ftype;
                                                          68
                                                                      int m = (ini + fim) >> 1;
27
                                                          69
28 struct Segtree {
                                                                      if (id <= m) e[novo] = update(e[novo], ini, m</pre>
                                                           70
      vector<ftype> seg, d, e;
                                                                  , id, val);
      const ftype NEUTRAL = 0;
                                                                     else d[novo] = update(d[novo], m + 1, fim, id
30
                                                           71
                                                                  , val);
31
      int n;
32
                                                           72
      Segtree(int n) {
                                                                      seg[novo] = f(seg[e[novo]], seg[d[novo]]);
                                                           73
33
          this -> n = n;
                                                           74
                                                                      return novo:
                                                          75
35
                                                           76
      ftype f(ftype a, ftype b) {
37
                                                          77
                                                                 ftype query(int pos, int p, int q) {
          return a + b;
                                                          78
38
      7
39
                                                          79
                                                                      return query(pos, 1, n, p, q);
                                                          80
40
41
      ftype create() {
                                                           81
          seg.push_back(0);
                                                                 int update(int pos, int id, int val) {
42
                                                          82
          e.push_back(0);
                                                                      return update(pos, 1, n, id, val);
                                                          83
43
44
          d.push_back(0);
                                                          84
          return seg.size() - 1;
                                                          85 };
45
```