

Notebook - Maratona de Programação

Lenhadoras de Segtree

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1 Misc

1.1 Split

```
vector < string > split(string txt, char key = ' '){
       vector<string> ans;
       string palTemp = "";
      for(int i = 0; i < txt.size(); i++){</pre>
           if(txt[i] == key){
               if(palTemp.size() > 0){
                    ans.push_back(palTemp);
                    palTemp = "";
1.0
               }
11
12
           } else{
               palTemp += txt[i];
13
           }
15
16
17
18
      if(palTemp.size() > 0)
          ans.push_back(palTemp);
2.0
       return ans;
22 }
```

1.2 Int128

```
1 __int128 read() {
       _{-}int128 x = 0, f = 1;
      char ch = getchar();
      while (ch < '0' || ch > '9') {
          if (ch == '-') f = -1;
          ch = getchar();
      while (ch >= '0' && ch <= '9') {
         x = x * 10 + ch - '0';
          ch = getchar();
10
      return x * f;
12
13 }
_{14} void print(__int128 x) {
15
      if (x < 0) {
          putchar('-');
16
          x = -x;
1.7
      if (x > 9) print(x / 10);
1.9
      putchar(x % 10 + '0');
20
21 }
```

2 Template

2.1 Template

```
15 #define all(x) (x).begin(), (x).end()
16 #define FOR(i, j, n) for (int i = j; i < n; i++)
17 #define qle(i, n) (i == n ? "\n" : " ")
18 #define endl "\n"
19 const int oo = 1e9;
20 const int MAX = 1e6;
21
22 int32_t main(){ optimize;
23
24     return 0;
25 }</pre>
```

2.2 Template Clean

```
1 #include <bits/stdc++.h>
2 using namespace std;
_4 // g++ teste.cpp -o teste -std=c++17
5 // ./teste < teste.txt
7 // cout << fixed << setprecision(12) << value << endl
9 // freopen("input.txt", "r", stdin);
10 // freopen("output.txt", "w", stdout);
12 int main() {
   ios::sync_with_stdio(false);
13
      cin.tie(NULL);
14
15
16
17
18
      return 0;
19 }
```

3 Strings

3.1 Kmp

```
vector < int > prefix_function(string s) {
     int n = (int)s.length();
      vector < int > pi(n);
      for (int i = 1; i < n; i++) {
4
          int j = pi[i-1];
           while (j > 0 && s[i] != s[j])
7
              j = pi[j-1];
           if (s[i] == s[j])
               j++:
          pi[i] = j;
      }
12
      return pi;
13 }
```

3.2 Generate All Permutations

```
vector<string> generate_permutations(string s) {
int n = s.size();
vector<string> ans;

sort(s.begin(), s.end());

do {
   ans.push_back(s);
   } while (next_permutation(s.begin(), s.end()));

return ans;
}
```

3.3 Generate All Sequences Length K

```
1 // gera todas as ípossveis êsequncias usando as letras30
                                                                     int m = (1x + rx) / 2;
       em set (de comprimento n) e que tenham tamanho k 31
                                                                     apply_mod_op(lazy[2 * x + 1], lazy[x], 1);
2 // sequence = ""
                                                                     apply_mod_op(tree[2 * x + 1], lazy[x], m - lx
3 vector < string > generate_sequences(char set[], string
      sequence, int n, int k) {
     if (k == 0){
                                                                     apply_mod_op(lazy[2 * x + 2], lazy[x], 1);
                                                          34
         return { sequence };
                                                                     apply_mod_op(tree[2 * x + 2], lazy[x], rx - m
                                                                 ):
6
     vector < string > ans;
                                                                     lazy[x] = -1;
                                                          37
     for (int i = 0; i < n; i++) {
9
                                                          38
10
           auto aux = generate_sequences(set, sequence + 39
       set[i], n, k - 1);
                                                                 void build(vector<int> &arr, int x, int lx, int
          ans.insert(ans.end(), aux.begin(), aux.end())
                                                                 rx) {
                                                                     if (rx - lx == 1) {
                                                                          if (lx < (int)arr.size())</pre>
          // for (auto e : aux) ans.push_back(e);
12
                                                          42
13
                                                                              tree[x] = arr[lx];
14
                                                          44
                                                                          return;
     return ans;
16 }
                                                                     }
                                                          46
                                                          47
  3.4 Z-function
                                                                     int m = (1x + rx) / 2;
                                                          48
                                                                     build(arr, 2 * x + 1, 1x, m);
                                                          49
                                                                     build(arr, 2 * x + 2, m, rx);
vector < int > z_function(string s) {
                                                          5.1
      int n = (int) s.length();
                                                                     tree[x] = merge(tree[2 * x + 1], tree[2 * x +
      vector < int > z(n);
                                                                  2]);
      for (int i = 1, l = 0, r = 0; i < n; ++i) {
                                                          5.3
          if (i <= r)</pre>
                                                          54
               z[i] = min (r - i + 1, z[i - 1]);
                                                                 void build(vector<int> &arr) {
                                                          5.5
          while (i + z[i] < n && s[z[i]] == s[i + z[i]
                                                                     build(arr, 0, 0, size);
                                                          56
      ]])
                                                          5.7
               ++z[i];
                                                          5.8
          if (i + z[i] - 1 > r)
                                                                 void update(int 1, int r, int v, int x, int lx,
               l = i, r = i + z[i] - 1;
10
                                                                 int rx) {
11
                                                                     propagate(x, lx, rx);
12
      return z;
                                                          6.1
13 }
                                                                     if (1x >= r \mid \mid 1 >= rx) return;
                                                          62
                                                                     if (lx >= l && rx <= r) {
                                                          63
       ED
                                                                         apply_mod_op(lazy[x], v, 1);
                                                          64
                                                                          apply_mod_op(tree[x], v, rx - lx);
                                                          65
                                                          66
                                                                          return:
      Seg Lazy
  4.1
                                                          67
                                                          68
                                                                     int m = (1x + rx) / 2;
                                                          69
using ll = long long;
                                                          70
                                                                     update(1, r, v, 2 * x + 1, lx, m);
                                                                     update(1, r, v, 2 * x + 2, m, rx);
3 struct segTree {
      int size:
      vector<ll> tree, lazy;
                                                                     tree[x] = merge(tree[2 * x + 1], tree[2 * x +
                                                          73
                                                                  2]);
                                                                 }
      ll modify_op(ll a, ll b, ll len) {
                                                          7.4
          if (b == -1) return a;
                                                          75
                                                                 void update(int 1, int r, int v) {
          return b * len;
                                                          76
9
                                                                     update(1, r, v, 0, 0, size);
                                                          7.7
                                                          78
                                                          79
12
      void apply_mod_op(ll &a, ll b, ll len) {
                                                                 11 query(int 1, int r, int x, int lx, int rx) {
                                                          80
          a = modify_op(a, b, len);
13
                                                                     propagate(x, lx, rx);
                                                          81
14
                                                          82
                                                                     if (lx >= r || l >= rx) return 0;
                                                          83
16
      ll merge(ll a, ll b) {
                                                                     if (lx >= l && rx <= r) return tree[x];</pre>
                                                          8.4
          return a + b;
17
                                                          8.5
18
                                                                     int m = (1x + rx) / 2;
                                                          86
19
                                                                     ll s1 = query(1, r, 2 * x + 1, lx, m);
                                                          87
20
      void init(int n) {
                                                          88
                                                                     11 s2 = query(1, r, 2 * x + 2, m, rx);
           size = 1:
21
           while (size < n) size *= 2;
                                                          89
                                                          90
                                                                     return merge(s1, s2);
23
           tree.assign(2 * size, 0LL);
                                                                 }
          lazy.assign(2 * size, -1);
                                                          91
24
                                                          92
                                                                 11 query(int 1, int r) {
                                                          93
26
                                                                     return query(1, r, 0, 0, size);
       void propagate(int x, int lx, int rx) {
                                                          94
         if (rx - lx == 1) return;
                                                          95
28
                                                          96
29
```

```
void debug() {
97
                                                            5.5
98
          for (auto e : tree)
                                                            56
                                                                      int query(int p, int q){ return query(1,1,
               cout << e << ' ';
99
                                                                   size,p,q); }
100
           cout << endl;
                                                            58
                                                                       void build(){ return build(1,1,size); }
           for (auto e : lazy)
                                                           59 }:
102
               cout << e << ' ';
                                                              4.3
                                                                    Dsu
            cout << endl:
104
105
106 };
                                                            # # include <bits/stdc++.h>
  4.2 Seg Tree
                                                            3 using namespace std;
 1 class SegTree{
                                                            5 const int MAX = 1e6+17;
      vector < int > seg;
                                                            7 struct DSU {
       vector < int > v;
       int size;
                                                                  int n;
                                                            8
                                                                   vector < int > link, sizes;
       int el_neutro = INT_MAX;
                                                            9
                                                            1.0
       int f(int a, int b){
                                                                   DSU(int n) {
                                                                       this -> n = n;
           return min(a,b);
                                                            1.2
                                                                       link.assign(n+1, 0);
 9
                                                            13
                                                                       sizes.assign(n+1, 1);
10
       void update(int pos, int ini, int fim, int i, int 15
11
                                                                       for (int i = 0; i <= n; i++)</pre>
        val){
                                                            16
                                                                           link[i] = i;
12
           if(i < ini or i > fim) return;
                                                            1.7
           if(ini == fim){
13
                                                            18
                seg[pos] = val; return;
14
                                                            19
                                                                   int find(int x) {
                                                            20
15
                                                           21
                                                                       while (x != link[x])
           int m = (ini+fim)/2;
                                                                           x = link[x];
1.7
                                                           22
            int e = 2*pos, d = 2*pos+1;
                                                            23
18
            update(e, ini, m, i, val);
                                                            24
                                                                       return x;
19
           update(d, m+1, fim, i, val);
                                                           25
2.0
                                                           26
            seg[pos] = f(seg[e], seg[d]);
                                                                   bool same(int a, int b) {
22
                                                            27
                                                                       return find(a) == find(b);
24
                                                            29
       int query(int pos, int ini, int fim, int p, int q30
25
                                                                   void unite(int a, int b) {
            if(q < ini or p > fim) return el_neutro;
                                                                       a = find(a);
26
                                                            32
           if(p <= ini and fim <= q) return seg[pos];</pre>
                                                                       b = find(b);
                                                            33
28
                                                            3.4
                                                                       if (a == b) return;
           int m = (ini + fim)/2;
                                                            3.5
29
           int e = 2*pos, d = 2*pos+1;
3.0
           return f(query(e,ini,m,p,q), query(d,m+1,fim, 37
                                                                       if (sizes[a] < sizes[b])</pre>
31
       p,q));
                                                                            swap(a, b);
32
                                                            3.9
33
                                                            40
                                                                       sizes[a] += sizes[b];
       void build(int pos, int ini, int fim){
                                                                       link[b] = a;
34
                                                            41
          if(ini == fim){
3.5
                                                            42
                seg[pos] = v[ini]; return;
36
                                                            43
                                                                   int size(int x) {
37
                                                           44
                                                                       return sizes[x];
                                                           45
           int m = (ini+fim)/2;
3.9
                                                           46
40
           int e = 2*pos, d=2*pos+1;
                                                           47 };
41
           build(e,ini,m);
                                                           49 int main() {
42
           build(d,m+1,fim);
                                                           50
                                                                   ios::sync_with_stdio(false);
                                                                   cin.tie(NULL);
44
                                                           51
            seg[pos] = f(seg[e], seg[d]);
                                                            52
45
                                                                   int cities, roads; cin >> cities >> roads;
46
                                                            53
                                                                   vector < int > final_roads;
47
                                                            54
       public:
                                                                   int ans = 0;
           SegTree(int n, vector<int> source): seg(4*
                                                                   DSU dsu = DSU(cities);
49
                                                            56
       size), v(size){
                                                                   for (int i = 0, a, b; i < roads; i++) {</pre>
5.0
               size = n;
                                                                       cin >> a >> b;
                for(int i=0; i<size; i++) v[i] = source[i59</pre>
51
                                                                       dsu.unite(a, b);
       ];
                                                            60
           }
52
                                                            6.1
                                                                   for (int i = 2; i <= cities; i++) {</pre>
                                                            62
                                                                    if (!dsu.same(1, i)) {
           void update(int i, int val){ return update
54
                                                            63
       (1,1,size,i,val); }
                                                                           ans++;
                                                            64
```

```
final_roads.push_back(i);
                                                                 void update(int 1, int r, int val){ return
                                                          5.6
               dsu.unite(1,i);
                                                                 update_range(1,1,size,1, r,val); }
          }
67
                                                           5.7
                                                           5.8
                                                                  int query(int i){ return query_point(1,1,size,i);
68
      cout << ans << '\n';
70
                                                          59
      for (auto e : final_roads) {
                                                                  void build(){ return build(1,1,size); }
                                                          60
           cout << "1 " << e << '\n';
                                                          61 }:
7.2
73
                                                                  DP
                                                             5
74
75 }
                                                                  Knapsack
  4.4 Seg Pqru
                                                             5.1
                                                           int val[MAXN], peso[MAXN], dp[MAXN][MAXS];
#include <bits/stdc++.h>
2 using namespace std;
                                                           3 int knapsack(int n, int m){ // n Objetos | Peso max
                                                                 for(int i=0;i<=n;i++){</pre>
4 class SegTree {
      vector<int> seg;
                                                                     for(int j=0;j<=m;j++){
                                                                          if(i==0 or j==0)
      vector < int > v;
                                                                             dp[i][j] = 0;
      int size;
                                                                          else if(peso[i-1]<=j)</pre>
      int el_neutro = INT_MAX;
                                                                              dp[i][j] = max(val[i-1]+dp[i-1][j-1]
      int f(int a, int b){
                                                                 peso[i-1]], dp[i-1][j]);
10
                                                           1.0
          return min(a,b);
                                                                              dp[i][j] = dp[i-1][j];
                                                                    }
                                                           12
13
      void update_range(int pos, int ini, int fim, int 13
14
                                                                 return dp[n][m];
      1, int r, int val){
                                                           14
                                                           15
           if(r < ini or l > fim) return;
16
          if(1 <= ini and fim <= r){
                                                                   Minimum Coin Change
               seg[pos] += val;
18
19
           int mid = (ini+fim)/2;
                                                           vector < int > valores;
21
           update_range(2*pos, ini, mid, 1, r, val);
                                                           4 int tabela[1005];
23
           update_range(2*pos+1, mid+1, fim, 1, r, val); 5
                                                           6 int dp(int k){
      }
24
                                                                 if(k == 0){
                                                                      return 0;
      int query_point(int pos, int ini, int fim, int i) 8
26
                                                                 if(tabela[k] != -1)
           if(ini == fim) return seg[pos];
                                                           10
                                                                     return tabela[k];
28
                                                                 int melhor = 1e9;
29
           int mid = (ini + fim)/2;
                                                           12
                                                                 for(int i = 0; i < n; i++){</pre>
           if(i<=mid)
                                                           13
30
31
               return query_point(2*pos, ini, mid, i);
                                                          14
                                                                      if(valores[i] <= k)</pre>
                                                                          melhor = min(melhor,1 + dp(k - valores[i
32
           else
               return query_point(2*pos+1, mid+1, fim, i
                                                                 ]));
      );
                                                           16
                                                                 return tabela[k] = melhor;
                                                           17
34
                                                           18 }
      void build(int pos, int ini, int fim){
36
                                                             5.3 Digits
          if(ini == fim){
               seg[pos] = v[ini]; return;
38
39
                                                           1 // achar a quantidade de numeros menores que R que
                                                                 possuem no maximo 3 digitos nao nulos
40
                                                           2 // a ideia eh utilizar da ordem lexicografica para
           int m = (ini+fim)/2;
41
           int e = 2*pos, d=2*pos+1;
                                                                 checar isso pois se temos por exemplo
                                                           _{\rm 3} // o numero 8500, a gente sabe que se pegarmos o
43
           build(e,ini,m);
                                                                 numero 7... qualquer digito depois do 7
44
                                                           _4 // sera necessariamente menor q 8500
45
          build(d,m+1,fim);
46
           seg[pos] = f(seg[e], seg[d]);
                                                           6 string r;
      }
                                                           7 int tab[20][2][5];
48
49
                                                           _{9} // i - digito de R
50 public:
      SegTree(int n, vector<int> source): seg(4*size), 10 // menor - ja pegou um numero menor que um digito de
51
      v(size){
                                                                 R.
                                                           _{11} // qt - quantidade de digitos nao nulos
           size = n:
52
           for(int i=0; i<size; i++) v[i] = source[i];</pre>
                                                           int dp(int i, bool menor, int qt){
53
                                                                 if(qt > 3) return 0;
      }
54
                                                           13
                                                                 if(i >= r.size()) return 1;
55
                                                           14
```

```
if(tab[i][menor][qt] != -1) return tab[i][menor][ 1 // achar uma subsequencia continua no array que a
1.5
                                                                 soma seja a maior possivel
                                                            _{2} // nesse caso vc precisa multiplicar exatamente 1
16
      int dr = r[i]-'0';
                                                                 elemento da subsequencia
      int res = 0;
                                                            3 // e achar a maior soma com isso
19
      for(int d = 0; d <= 9; d++) {</pre>
                                                           5 int n, x, arr[MAX], tab[MAX][2]; // tab[maior
20
          int dnn = qt + (d > 0);
                                                                  resposta no intervalo][foi multiplicado ou ano]
           if(menor == true) {
               res += dp(i+1, true, dnn);
                                                           7 int dp(int i, bool mult) {
                                                                  if (i == n-1) {
24
                                                           8
           else if(d < dr) {</pre>
                                                           9
                                                                      if (!mult) return arr[n-1]*x;
                                                                      return arr[n-1];
26
              res += dp(i+1, true, dnn);
                                                           10
                                                           11
                                                                  if (tab[i][mult] != -1) return tab[i][mult];
           else if(d == dr) {
                                                           12
               res += dp(i+1, false, dnn);
29
                                                           13
30
                                                           14
                                                                  int res;
      }
3.1
                                                           1.5
                                                           16
                                                                  if (mult) {
                                                                     res = max(arr[i], arr[i] + dp(i+1, 1));
      return tab[i][menor][qt] = res;
33
                                                           17
34 }
                                                           18
                                                           19
                                                                  else {
  5.4 Coins
                                                           2.0
                                                                      res = max({
                                                                          arr[i]*x,
                                                           21
                                                                          arr[i]*x + dp(i+1, 1),
                                                           22
1 int tb[1005];
                                                           23
                                                                          arr[i] + dp(i+1, 0)
2 int n;
                                                           24
                                                                      });
3 vector < int > moedas;
                                                           25
                                                           26
5 int dp(int i){
                                                                  return tab[i][mult] = res;
                                                          27
      if(i >= n)
                                                           28 }
          return 0;
                                                           29
      if(tb[i] != -1)
                                                           30 int main() {
          return tb[i];
                                                           31
                                                                  memset(tab, -1, sizeof(tab));
                                                           32
      tb[i] = max(dp(i+1), dp(i+2) + moedas[i]);
      return tb[i];
12
                                                                  int ans = -00:
                                                           3.4
13 }
                                                                  for (int i = 0; i < n; i++) {</pre>
                                                           35
14
                                                           36
                                                                      ans = max(ans, dp(i, 0));
15 int main(){
                                                           37
      memset(tb,-1,sizeof(tb));
16
                                                           38
                                                                  return 0;
                                                           3.9
  5.5 Substr Palindromo
                                                                   Algoritmos
_{\rm 1} // \mathbf{\hat{e}}\,\mathrm{voc} deve informar se a substring de S formada
      pelos elementos entre os indices i e j
                                                             6.1 Lis
2 // é um palindromo ou ãno.
4 char s[MAX];
                                                            int lis(vector<int> const& a) {
5 int calculado[MAX][MAX]; // inciado com false, ou 0
                                                                  int n = a.size();
6 int tabela[MAX][MAX];
                                                                  vector < int > d(n, 1);
                                                                  for (int i = 0; i < n; i++) {
8 int is_palin(int i, int j){
                                                                      for (int j = 0; j < i; j++) {
      if(calculado[i][j]){
                                                                          if (a[j] < a[i])</pre>
                                                            6
1.0
          return tabela[i][j];
                                                                               d[i] = max(d[i], d[j] + 1);
                                                                      }
      if(i == j) return true;
                                                                  }
      if(i + 1 == j) return s[i] == s[j];
13
                                                           10
                                                           11
                                                                  int ans = d[0];
      int ans = false;
15
                                                                  for (int i = 1; i < n; i++) {</pre>
                                                           12
16
      if(s[i] == s[j]){
                                                           13
                                                                      ans = max(ans, d[i]);
          if(is_palin(i+1, j-1)){
1.7
                                                           14
               ans = true;
18
                                                                  return ans;
                                                           15
19
                                                           16 }
      }
20
      calculado[i][j] = true;
21
                                                                   Binary Exponentiation
      tabela[i][j] = ans;
22
      return ans;
23
24 }
                                                            1 long long power(long long a, long long b) {
                                                                  long long res = 1;
                                                                  while (b > 0) {
  5.6 Kadane
                                                            3
```

4

if (b & 1)

```
res = res * a;
                                                              cin >> n >> q;
                                                        6
          a = a * a;
                                                        7
                                                              int [n];
          b >>= 1;
                                                              int delta[n+2];
      }
      return res;
                                                              while(q--){
10 }
                                                                 int 1, r, x;
                                                       11
                                                                  cin >> 1 >> r >> x;
                                                        12
        Ternary Search
                                                                  delta[1] += x;
                                                       1.3
                                                                  delta[r+1] -= x;
                                                       14
double ternary_search(double 1, double r) {
                                                       16
      double eps = 1e-9;
                                   //set the error
                                                       17
                                                              int curr = 0;
      limit here
                                                              for(int i=0; i < n; i++){
                                                       18
      while (r - l > eps) {
                                                                  curr += delta[i];
                                                       19
         double m1 = 1 + (r - 1) / 3;
                                                                  v[i] = curr;
                                                       20
          double m2 = r - (r - 1) / 3;
                                                       21
         double f1 = f(m1);
                                //evaluates the
      function at m1
                                                              for(int i=0; i < n; i++){</pre>
                                                       23
         double f2 = f(m2);
                                //evaluates the
                                                                  cout << v[i] << ' ';
      function at m2
                                                       2.5
         if (f1 < f2)
                                                              cout << '\n';
                                                       26
             1 = m1;
                                                       27
         else
1.0
                                                       28
                                                              return 0:
             r = m2;
                                                       29 }
      }
12
      return f(1);
                                      //return the
                                                                Binary Search Last True
      maximum of f(x) in [1, r]
14 }
                                                        int last_true(int lo, int hi, function < bool(int) > f)
  6.4 Binary Search First True
                                                              lo--;
                                                              while (lo < hi) {
int first_true(int lo, int hi, function < bool(int) > f)
                                                                 int mid = lo + (hi - lo + 1) / 2;
      ſ
                                                                  if (f(mid)) {
      hi++;
                                                                     lo = mid;
      while (lo < hi) {
                                                                  } else {
         int mid = lo + (hi - lo) / 2;
                                                                     hi = mid - 1;
         if (f(mid)) {
             hi = mid;
                                                              }
                                                       1.0
          } else {
                                                              return lo;
             lo = mid + 1:
                                                       12 }
9
      }
                                                          6.9 Kadane
     return lo:
                                                        int ans = a[0], ans_1 = 0, ans_r = 0;
  6.5 Edit Distance
                                                        1 int sum = 0, minus_pos = -1;
                                                        4 for (int r = 0; r < n; ++r) {
int editDist(string str1, string str2, int m, int n)
                                                              sum += a[r];
                                                              if (sum > ans) {
      if (m == 0) return n;
                                                                 ans = sum;
      if (n == 0) return m;
                                                                  ans_l = minus_pos + 1;
                                                                  ans_r = r;
      if (str1[m - 1] == str2[n - 1]) return editDist(
      str1, str2, m - 1, n - 1);
                                                              if (sum < 0) {
                                                        11
      return 1 + min({editDist(str1, str2, m, n - 1),
                                                                  sum = 0;
      editDist(str1, str2, m - 1, n), editDist(str1,
                                                                  minus_pos = r;
      str2, m - 1, n - 1)});
                                                        14
7 }
                                                       15 }
  6.6 Ceil
                                                              Grafos
1 long long division_ceil(long long a, long long b) {
                                                          7.1 Floyd Warshall
      return 1 + ((a - 1) / b); // if a != 0
3 }
                                                        # # include <bits/stdc++.h>
  6.7 Delta-encoding
                                                        3 using namespace std;
#include <bits/stdc++.h>
                                                        4 using ll = long long;
2 using namespace std;
                                                        6 const int MAX = 507;
                                                        7 const long long INF = 0x3f3f3f3f3f3f3f3f3fLL;
4 int main(){
```

int n, q;

```
9 ll dist[MAX][MAX]:
                                                                          parent[u] = v;
10 int n;
                                                           12
                                                                          if (dfs(u))
                                                                              return true;
11
                                                           1.3
void floyd_warshall() {
                                                                      } else if (color[u] == 1) {
                                                           14
      for (int i = 0; i < n; i++) {
                                                                          cycle_end = v;
          for (int j = 0; j < n; j++) {
                                                                          cycle_start = u;
14
                                                           16
               if (i == j) dist[i][j] = 0;
                                                                          return true;
15
               else if (!dist[i][j]) dist[i][j] = INF;
16
17
                                                           19
      }
                                                                  color[v] = 2;
                                                           20
                                                                  return false;
19
                                                           21
20
      for (int k = 0; k < n; k++) {
                                                           22 }
          for (int i = 0; i < n; i++) {
21
                                                           23
               for (int j = 0; j < n; j++) {
                                                           24 void find_cycle() {
                   // trata o caso no qual o grafo tem _{25}
                                                                color.assign(n, 0);
      arestas com peso negativo
                                                                  parent assign(n, -1);
                                                           26
                   if (dist[i][k] < INF && dist[k][j] < 27</pre>
                                                                  cycle_start = -1;
                       dist[i][j] = min(dist[i][j], dist 29
                                                                  for (int v = 0; v < n; v++) {
                                                                      if (color[v] == 0 && dfs(v))
      [i][k] + dist[k][j]);
                   }
                                                                          break;
                                                           31
26
               }
                                                           32
27
           }
                                                           33
28
      }
                                                                  if (cycle_start == -1) {
                                                           34
30
                                                                      cout << "Acyclic" << endl;</pre>
                                                           3.5
                                                           36
                                                                  } else {
       Tree Diameter
                                                                      vector < int > cycle;
                                                           3.7
                                                                      cycle.push_back(cycle_start);
                                                           38
                                                           39
                                                                      for (int v = cycle_end; v != cycle_start; v =
#include <bits/stdc++.h>
                                                                   parent[v])
                                                           40
                                                                          cycle.push_back(v);
3 using namespace std;
                                                                      cycle.push_back(cycle_start);
                                                           41
                                                                      reverse(cycle.begin(), cycle.end());
                                                           42
5 const int MAX = 3e5+17;
                                                           43
                                                                      cout << "Cycle found: ";</pre>
                                                           44
vector < int > adj[MAX];
                                                                      for (int v : cycle)
                                                           45
8 bool visited[MAX];
                                                                          cout << v << " ":
                                                           46
                                                           47
                                                                      cout << endl;</pre>
int max_depth = 0, max_node = 1;
                                                           48
                                                           49 }
12 void dfs (int v, int depth) {
13
      visited[v] = true;
                                                             7.4 Bfs
14
      if (depth > max_depth) {
           max_depth = depth;
                                                           void bfs(int start){
16
           max_node = v;
17
                                                           2
                                                                  queue < int > q;
18
                                                                  q.push(start);
19
      for (auto u : adj[v]) {
          if (!visited[u]) dfs(u, depth + 1);
                                                                  vector < bool > visited(GRAPH_MAX_SIZE, false);
21
                                                                  visited[start] = true;
22
23 }
                                                                  while(q.size()){
                                                                     int u = q.front();
24
25 int tree_diameter() {
                                                                      q.pop();
      dfs(1, 0);
                                                                      for(int w: graph[u]){
26
                                                                          if(not visited[w]){
27
      max_depth = 0;
      for (int i = 0; i < MAX; i++) visited[i] = false; 13</pre>
28
                                                                              q.push(w);
      dfs(max_node, 0);
                                                                               visited[w] = true;
29
                                                           14
      return max_depth;
                                                                          }
31 }
                                                                      }
                                                           16
                                                                  }
                                                           17
  7.3 Cycle Path Recovery
                                                           18
                                                           19 }
1 int n;
                                                                   Bipartite
                                                             7.5
vector < vector < int >> adj;
3 vector < char > color;
                                                           1 const int NONE = 0, BLUE = 1, RED = 2;
4 vector < int > parent;
                                                           vector < vector < int >> graph (100005);
5 int cycle_start, cycle_end;
                                                           3 vector < bool > visited(100005);
                                                           4 int color[100005];
7 bool dfs(int v) {
      color[v] = 1;
      for (int u : adj[v]) {
                                                           6 bool bfs(int s = 1){
          if (color[u] == 0) {
```

```
queue < int > q;
                                                                   visited.reset();
                                                            26
9
       q.push(s);
                                                            27
       color[s] = BLUE;
                                                                   for (int u = 1; u <= N; ++u){</pre>
1.0
                                                            28
                                                                       path.clear();
                                                            29
                                                                        if (not visited[u] and dfs(u,-1))
       while (not q.empty()){
                                                            30
          auto u = q.front(); q.pop();
                                                                            return true;
                                                            31
13
14
                                                            32
           for (auto v : graph[u]){
1.5
                                                            3.3
               if (color[v] == NONE){
                                                            34
16
                    color[v] = 3 - color[u];
                                                                   return false;
                                                            35
                    q.push(v);
                                                            36 }
18
19
                                                             7.8 Dinic
               else if (color[v] == color[u]){
20
21
                   return false;
                                                            1 const int N = 300;
           }
23
       }
24
                                                             3 struct Dinic {
2.5
                                                                   struct Edge {
                                                             4
       return true;
                                                                       int from, to; ll flow, cap;
                                                             5
27 }
28
                                                                   vector < Edge > edge;
29 bool is_bipartite(int n){
3.0
                                                                   vector < int > g[N];
       for (int i = 1; i <= n; i++)</pre>
                                                                   int ne = 0;
                                                            10
           if (color[i] == NONE and not bfs(i))
32
                                                                   int lvl[N], vis[N], pass;
33
               return false;
                                                                   int qu[N], px[N], qt;
                                                            12
3.4
                                                            13
       return true;
35
                                                            14
                                                                   ll run(int s, int sink, ll minE) {
36 }
                                                                       if(s == sink) return minE;
                                                            15
                                                            16
  7.6 Dfs
                                                                       11 \text{ ans} = 0;
                                                            1.7
                                                            18
                                                                        for(; px[s] < (int)g[s].size(); px[s]++) {</pre>
                                                            19
vector < vector < int >> graph;
                                                            20
                                                                            int e = g[s][ px[s] ];
vector < bool > visited;
                                                            21
                                                                            auto &v = edge[e], &rev = edge[e^1];
                                                                            if(lvl[v.to] != lvl[s]+1 || v.flow >= v.
                                                            22
4 void dfs(int vertex){
                                                                   cap)
      visited[vertex] = true;
                                                                                                     // v.cap - v.flow
                                                            23
                                                                                continue:
                                                                    < lim
      for(int w: graph[vertex]){
                                                                            11 tmp = run(v.to, sink,min(minE, v.cap-v
                                                            24
          if(!visited[w]){
                                                                   .flow));
               dfs(w);
                                                                            v.flow += tmp, rev.flow -= tmp;
                                                            25
           }
1.0
                                                                            ans += tmp, minE -= tmp;
                                                            26
       }
11
                                                                            if(minE == 0) break;
                                                            27
12 }
                                                                        }
                                                            28
                                                                       return ans;
                                                            29
  7.7 Find Cycle
                                                            30
                                                                   bool bfs(int source, int sink) {
                                                            3.1
1 bitset < MAX > visited;
                                                            32
                                                                       qt = 0;
vector < int > path;
                                                                        qu[qt++] = source;
                                                            3.3
                                                                        lvl[source] = 1;
s vector < int > adj[MAX];
                                                            34
                                                            35
                                                                        vis[source] = ++pass;
                                                                        for(int i = 0; i < qt; i++) {
5 bool dfs(int u, int p){
                                                            36
                                                                            int u = qu[i];
                                                            37
                                                                            px[u] = 0;
      if (visited[u]) return false;
                                                            3.8
                                                                            if(u == sink) return true;
                                                            3.9
9
       path.pb(u);
                                                            40
                                                                            for(auto& ed : g[u]) {
       visited[u] = true;
                                                                                auto v = edge[ed];
10
                                                            41
                                                                                if(v.flow >= v.cap || vis[v.to] ==
12
       for (auto v : adj[u]){
                                                                   pass)
           if (visited[v] and u != v and p != v){
                                                                                     continue; // v.cap - v.flow < lim</pre>
13
                                                            43
               path.pb(v); return true;
                                                                                vis[v.to] = pass;
14
                                                            44
                                                                                lvl[v.to] = lvl[u]+1;
1.5
                                                            45
16
                                                            46
                                                                                qu[qt++] = v.to;
           if (dfs(v, u)) return true;
1.7
                                                            47
                                                                        }
                                                            48
19
                                                            49
                                                                       return false;
      path.pop_back();
20
                                                            50
                                                                   11 flow(int source, int sink) {
21
       return false;
                                                            51
22 }
                                                            52
                                                                       reset_flow();
                                                                       11 \text{ ans} = 0;
                                                            53
                                                                        //for(lim = (1LL << 62); lim >= 1; lim /= 2)
24 bool has_cycle(int N){
                                                            5.4
                                                            55
                                                                        while(bfs(source, sink))
```

```
ans += run(source, sink, LLINF);
                                                                               q.insert({d[to], to});
56
                                                           2.5
57
          return ans;
                                                           26
                                                                          }
                                                                      }
5.8
                                                           2.7
      void addEdge(int u, int v, ll c, ll rc) {
59
                                                           28
          Edge e = \{u, v, 0, c\};
                                                           29 }
           edge.pb(e);
61
                                                           30
           g[u].push_back(ne++);
                                                           31 vector<int> restore_path(int s, int t) {
                                                                 vector < int > path;
63
                                                           3.2
           e = \{v, u, 0, rc\};
64
                                                           33
           edge.pb(e);
                                                           34
                                                                  for (int v = t; v != s; v = p[v])
           g[v].push_back(ne++);
                                                                     path.push_back(v);
66
                                                           35
                                                           36
                                                                  path.push_back(s);
68
      void reset_flow() {
                                                           3.7
          for(int i = 0; i < ne; i++)
                                                          38
                                                                  reverse(path.begin(), path.end());
69
               edge[i].flow = 0;
7.0
                                                          39
                                                                  return path;
           memset(lvl, 0, sizeof(lvl));
                                                           40 }
71
           memset(vis, 0, sizeof(vis));
          memset(qu, 0, sizeof(qu));
                                                           42 int adj[MAX][MAX];
7.3
           memset(px, 0, sizeof(px));
                                                           43 int dist[MAX]:
                                                           44 int minDistance(int dist[], bool sptSet[], int V) {
           qt = 0; pass = 0;
7.5
76
                                                                  int min = INT_MAX, min_index;
                                                           45
77 };
                                                           46
                                                           47
                                                                  for (int v = 0; v < V; v++)
  7.9 Bellman Ford
                                                                      if (sptSet[v] == false && dist[v] <= min)</pre>
                                                                          min = dist[v], min_index = v;
                                                           49
                                                           5.0
1 struct edge
                                                           51
                                                                  return min_index;
                                                           52 }
      int a, b, cost;
3
                                                           53
                                                           54 void dijkstra(int src, int V) {
                                                           55
6 int n, m, v;
                                                                  bool sptSet[V];
                                                           56
7 vector < edge > e;
                                                           5.7
                                                                  for (int i = 0; i < V; i++)</pre>
8 const int INF = 1000000000;
                                                           58
                                                                      dist[i] = INT_MAX, sptSet[i] = false;
10 void solve()
                                                                  dist[src] = 0;
11 {
                                                           6.1
      vector < int > d (n, INF);
12
                                                           62
                                                                  for (int count = 0; count < V - 1; count++) {</pre>
      d[v] = 0;
13
                                                           63
                                                                      int u = minDistance(dist, sptSet, V);
      for (int i=0; i<n-1; ++i)
                                                           64
           for (int j=0; j<m; ++j)</pre>
1.5
                                                                      sptSet[u] = true;
               if (d[e[j].a] < INF)</pre>
                   d[e[j].b] = min (d[e[j].b], d[e[j].a]_{67}
1.7
        + e[j].cost);
                                                                      for (int v = 0; v < V; v++)
18
                                                                           if (!sptSet[v] && adj[u][v]
                                                           69
                                                           7.0
                                                                               && dist[u] ! = INT_MAX
  7.10 Dijkstra
                                                                               && dist[u] + adj[u][v] < dist[v])
                                                                               dist[v] = dist[u] + adj[u][v];
                                                                  }
1 const int MAX = 2e5+7;
                                                           7.3
2 const int INF = 1000000000;
3 vector < vector < pair < int , int >>> adj(MAX);
                                                              7.11 Kruskall
5 void dijkstra(int s, vector<int> & d, vector<int> & p
      ) {
                                                            vector < int > parent, rank;
      int n = adj.size();
7
      d.assign(n, INF);
                                                            3 void make_set(int v) {
      p.assign(n, -1);
                                                                 parent[v] = v;
                                                            4
                                                                  rank[v] = 0;
                                                            5
      d[s] = 0;
                                                            6 }
      set <pair < int , int >> q;
                                                           8 int find_set(int v) {
      q.insert({0, s});
12
                                                                if (v == parent[v])
13
      while (!q.empty()) {
                                                           9
          int v = q.begin()->second;
                                                                      return v;
14
                                                           10
           q.erase(q.begin());
                                                                  return parent[v] = find_set(parent[v]);
                                                          12 }
16
           for (auto edge : adj[v]) {
                                                           13
               int to = edge.first;
                                                           14 void union_sets(int a, int b) {
18
               int len = edge.second;
                                                          15
                                                               a = find_set(a);
19
                                                                  b = find_set(b);
                                                          16
                                                                  if (a != b) {
               if (d[v] + len < d[to]) {</pre>
21
                                                           1.7
                   q.erase({d[to], to});
                                                                      if (rank[a] < rank[b])</pre>
                                                           18
                   d[to] = d[v] + len;
                                                                          swap(a, b);
23
                                                           19
                   p[to] = v;
                                                                      parent[b] = a;
                                                           20
24
```

```
if (rank[a] == rank[b])
                                                         40 {
22
             rank[a]++;
                                                         41
                                                                if (is_ancestor(u, v))
      }
23
                                                         42
                                                                    return u;
24 }
                                                         43
                                                                if (is_ancestor(v, u))
                                                                   return v;
                                                         44
                                                                for (int i = 1; i >= 0; --i) {
26 struct Edge {
                                                         45
      int u, v, weight;
                                                                    if (!is_ancestor(up[u][i], v))
      bool operator < (Edge const& other) {</pre>
                                                                        u = up[u][i];
28
                                                         4.7
          return weight < other.weight;</pre>
                                                         48
                                                         49
                                                                return up[u][0];
30
31 };
                                                         50 }
                                                         51
33 int n;
                                                         52 void preprocess(int root) {
34 vector < Edge > edges;
                                                         53
                                                             tin.resize(MAX);
                                                         5.4
                                                                tout.resize(MAX);
36 int cost = 0;
                                                         5.5
                                                                timer = 0;
37 vector < Edge > result;
                                                         56
                                                                up.assign(MAX, vector < int > (32));
38 parent.resize(n);
                                                         5.7
                                                                dfs(root, root);
39 rank.resize(n);
                                                         58 }
40 for (int i = 0; i < n; i++)
                                                         5.9
     make_set(i);
                                                         60 //distance between a and b
41
                                                         61 // dist[a] + dist[b] - 2*dist[lca(a, b)]
43 sort(edges.begin(), edges.end());
                                                                 Math
_{45} for (Edge e : edges) {
   if (find_set(e.u) != find_set(e.v)) {
46
                                                            8.1 Log
          cost += e.weight;
47
          result.push_back(e);
          union_sets(e.u, e.v);
                                                          int intlog(double base, double x) {
      }
5.0
                                                                return (int)(log(x) / log(base));
                                                          2
51
  7.12 Lca
                                                            8.2 Multiplicative Inverse
1 const int MAX = 2e5+17;
                                                         1 ll extend_euclid(ll a, ll b, ll &x, ll &y) {
                                                              if (a == 0)
                                                          2
3 int n, 1;
                                                          3
                                                                {
4 vector < vector < int >> adj;
                                                                    x = 0; y = 1;
                                                          4
5 // vector < pair < int , int >> adj [MAX];
                                                                    return b;
                                                          5
6 // int dist[MAX];
                                                          7
                                                                ll x1, y1;
8 int timer;
                                                                ll d = extend_euclid(b%a, a, x1, y1);
                                                          8
9 vector < int > tin, tout;
                                                                x = y1 - (b / a) * x1;
                                                          9
10 vector < vector < int >> up;
                                                                y = x1;
                                                         10
                                                                return d;
                                                         11
void dfs(int v, int p)
                                                         12 }
13 {
                                                         13
      tin[v] = ++timer;
1.4
                                                         14 // gcd(a, m) = 1 para existir solucao
      up[v][0] = p;
1.5
                                                        _{15} // ax + my = 1, ou a*x = 1 \pmod{m}
      for (int i = 1; i <= 1; ++i)
                                                        16 ll inv_gcd(ll a, ll m) { // com gcd
          up[v][i] = up[up[v][i-1]][i-1];
                                                         17 11 x, y;
                                                         18
                                                                extend_euclid(a, m, x, y);
      for (int u : adj[v]) {
19
                                                                return (((x % m) +m) %m);
                                                         19
          if (u != p)
                                                         20 }
              dfs(u, v);
                                                         21
22
                                                         22 ll inv(ll a, ll phim) { // com phi(m), se m for primo
                                                                 entao phi(m) = p-1
      /*for (auto [u, peso] : adj[v]) {
24
                                                                11 e = phim - 1;
         if (u != p) {
                                                                return fexp(a, e, MOD);
              dist[u] = dist[v] + peso;
26
                                                         25 }
              dfs(u, v);
27
28
                                                            8.3 Divisors
29
      tout[v] = ++timer;
                                                          vector<long long> all_divisors(long long n) {
3.1
                                                              vector < long long > ans;
                                                              for(long long a = 1; a*a <= n; a++){
34 bool is_ancestor(int u, int v)
                                                               if(n % a == 0) {
35
                                                                  long long b = n / a;
3.6
      return tin[u] <= tin[v] && tout[u] >= tout[v];
                                                                  ans.push_back(a);
37 }
                                                                  if(a != b) ans.push_back(b);
```

39 int lca(int u, int v)

}

```
sort(ans.begin(), ans.end());
                                                                   for (int j = i * i; j <= n; j += i)
   return ans;
                                                                       is_prime[j] = false;
12 }
                                                               }
                                                         9 }
  8.4 Prime Factors
                                                                 Check If Bit Is On
                                                          8.9
vector<pair<long long, int>> fatora(long long n) {
    vector<pair<long long, int>> ans;
                                                         1 // msb de 0 é undefined
                                                         2 #define msb(n) (32 - __builtin_clz(n))
    for(long long p = 2; p*p <= n; p++) {
      if(n % p == 0) {
                                                         3 // #define msb(n) (64 - __builtin_clzll(n) )
        int expoente = 0;
        while(n % p == 0) {
                                                         5 bool bit_on(int n, int bit) {
          n /= p;
                                                              if(1 & (n >> bit)) return true;
                                                               else return false;
          expoente++;
        }
9
        ans.emplace_back(p, expoente);
10
                                                          8.10 Crt
11
   }
    if(n > 1) ans.emplace_back(n, 1);
                                                        1 ll crt(const vector < pair < ll, ll >> & vet) {
    return ans;
14
                                                              ll ans = 0, lcm = 1;
15 }
                                                              ll a, b, g, x, y;
                                                              for(const auto &p : vet) {
                                                         4
  8.5 Binary To Decimal
                                                                   tie(a, b) = p;
                                                         5
                                                                   tie(g, x, y) = gcd(lcm, b);
                                                                  if((a - ans) % g != 0) return -1; // no
int binary_to_decimal(long long n) {
    int dec = 0, i = 0, rem;
                                                              solution
                                                                  ans = ans + x * ((a - ans) / g) % (b / g) *
                                                         8
    while (n!=0) {
                                                                  lcm = lcm * (b / g);
      rem = n % 10;
                                                         9
                                                                  ans = (ans % lcm + lcm) % lcm;
      n /= 10;
                                                        10
      dec += rem * pow(2, i);
                                                        11
                                                               }
                                                              return ans;
      ++i;
                                                        12
                                                        13 }
9
                                                          8.11 Matrix Exponentiation
    return dec;
11
                                                        1 #include <bits/stdc++.h>
14 long long decimal_to_binary(int n) {
                                                         2 #define debug(x) cout << "[" << #x << " = " << x << "
   long long bin = 0;
                                                              1 0
   int rem, i = 1;
16
                                                         3 #define ff first
                                                         4 #define ss second
    while (n!=0) {
1.8
     rem = n % 2;
19
                                                        6 using namespace std;
      n /= 2;
20
                                                        7 using ll = long long;
     bin += rem * i;
21
                                                        8 using ld = long double;
      i *= 10;
                                                        9 using pii = pair<int,int>;
23
                                                        10 using vi = vector<int>;
24
25
    return bin;
                                                        12 using tii = tuple <int, int, int>;
                                                        13
                                                        14 const int oo = (int)1e9;
  8.6 Mmc
                                                        15 const 11 00 = 0x3f3f3f3f3f3f3f3f3f1LL;
                                                        17 const int MOD = 1e9+7;
1 long long lcm(long long a, long long b){
      return (a/__gcd(a,b)*b);
                                                        18
                                                        19 struct Mat{
                                                              vector < vector < ll >> matriz;
                                                        20
  8.7 Combinatory
                                                              int 1, c;
                                                        22
                                                               Mat(vector < vector < 11 >> & mat) {
                                                        23
int comb(int k){
                                                        24
                                                                  matriz = mat;
      if(k==1 or k==0)return 0;
                                                                   1 = mat.size();
                                                        25
      return (k*(k-1))/2;
                                                        26
                                                                   c = mat[0].size();
4 }
                                                        27
  8.8 Sieve Of Eratosthenes
                                                               Mat(int r, int col, bool identidade=false){
                                                        29
                                                                  1 = r; c = col;
                                                        30
1 int n;
                                                                   matriz.assign(1, vector<11>(col, 0));
                                                        31
vector < bool > is_prime(n+1, true);
                                                                  if(identidade){
                                                        32
3 is_prime[0] = is_prime[1] = false;
                                                                      for(int i = 0; i < min(1,col); i++)
4 for (int i = 2; i <= n; i++) {
                                                                          matriz[i][i] = 1;
                                                        3.4
     if (is_prime[i] && (long long)i * i <= n) {
                                                        3.5
```

```
}
                                                           8 // number of elements
36
                                                          9 long long sum_of_n_first_squares(int n) {
      Mat operator * (const Mat& a) const{
                                                          10 return (n * (n - 1) * (2 * n - 1)) / 6;
38
          assert(c == a.1);
39
                                                          11 }
           vector<vector<ll>> resp(1, vector<ll>(a.c, 0) 12
      ):
                                                          13 // first element, last element, number of elements
                                                          14 long long sum_pa(int a1, int an, int n) {
41
          for(int i = 0; i < 1; i++){
                                                          15 return ((a1 + an) * n) / 2;
42
               for(int j = 0; j < a.c; j++){
43
                   for(int k = 0; k < a.1; k++){
                                                          17
                      resp[i][j] = (resp[i][j] + (
                                                          18 // first element, number of elements, ratio
45
      matriz[i][k]*a.matriz[k][j]) % MOD) % MOD;
                                                          19 long long general_term_pa(int a1, int n, int r) {
                                                          20 return a1 + (n - 1) * r;
46
                                                          21 }
47
          }
48
                                                          22
          return Mat(resp);
                                                          23 // first term, numbers of elements, ratio
49
50
                                                          24 long long sum_pg(int a1, int n, int q) {
                                                          25 return (a1 * (fexp(q, n) - 1)) / (q - 1);
5.1
      Mat operator + (const Mat& a) const{
           assert(1 == a.1 && c == a.c);
53
                                                          27
           vector<vector<ll>> resp(1, vector<ll>(c,0)); 28 // -1 < q < 1
54
                                                          29 // first term, ratio
           for(int i = 0; i < 1; i++){</pre>
55
              for(int j = 0; j < c; j++){
                                                          30 long long sum_infinite_pg(int a1, double q) {
56
                   resp[i][j] = (resp[i][j] + matriz[i][31 return a1 * (1 - q);
      j] + a.matriz[i][j]) % MOD;
                                                          32 }
58
          }
                                                          34 // first term, number of elements, ratio
59
          return Mat(resp);
                                                          35 long long general_term_pg(int a1, int n, int q) {
60
                                                          36  return a1 * fexp(q, n -1);
61
62 }:
                                                          37 }
63
_{\rm 64} Mat fexp(Mat& base, ll expoente, ll sz){
                                                          _{
m 39} // first element of original pa, first element of
      Mat result = Mat(sz, sz, 1);
                                                                derived pa, number of elements of original pa,
6.5
      while (expoente > 0) {
                                                                ratio of derived pa
          if(expoente & 1) result = result * base;
                                                          40 long long sum_second_order_pa(int a1, int b1, int n,
67
           base = base * base;
                                                                 int r) {
           expoente /= 2;
                                                          41 return a1 * n + (b1 * n * (n - 1)) / 2 + (r * n * (n
69
                                                                 - 1) * (n - 2)) / 6
70
71
      return result;
                                                          42 }
72 }
                                                          43
                                                          44 // GEOMETRIA
73
                                                          45 // seno
74 int main() {
      ios::sync_with_stdio(false);
                                                          46 a / sen(a) = b / sen(b) = c / sen(c)
7.6
      cin.tie(NULL);
                                                          47
                                                          48 //cosseno
      11 n, a, b;
                                                          49 a^2 = b^2 + c^2 - 2*b*c*cos(a)
78
      cin >> a >> b >> n;
7.9
                                                          51 // area losango
      Mat X(2,2);
                                                          52 A = (1/2) * diagonal_maior * diagonal_menor
8.1
82
      X.matriz[0][1] = 1;
                                                          54 // volume prisma
83
      X. matriz[1][0] = -1;
                                                          55 V = B * H
84
      X.matriz[1][1] = 1;
                                                          57 //volume esfera
86
87
      Mat y = fexp(X, n-1, 2);
                                                          58 V = (4/3) * PI * R^3
      11 ans = y.matriz[0][0] * a + y.matriz[0][1] * b; 60 //volume piramide
89
                                                          _{61} V = (1/3) * B * H
90
      while(ans < 0)
91
          ans += MOD;
92
                                                          63 //volume cone
                                                          _{64} V = (1/3) * PI * R^2 * H
93
      cout << ans % MOD << endl;</pre>
94
95 }
                                                          66 //condicao de existencia
                                                          67 a - b | < c < a + b
  8.12 Formulas
                                                            8.13 Mdc
#define lcm(a,b) (a*b)/gcd(a,b)
                                                          1 long long gcd(long long a, long long b){
3 int gcd(int a, int b) {
                                                                return b ? gcd(b, a % b) : a;
                                                          2
4 if (b == 0) return a;
                                                          3 }
   return gcd(b, a % b);
6 }
                                                           5 // or just use __gcd(a,b)
```

8.14 Fast Exponentiation

```
1 ll fexp(ll b, ll e, ll mod) {
2     ll res = 1;
3     b %= mod;
4     while(e){
5         if(e & 1LL)
```

```
res = (res * b) % mod;
res = (res * b) % mod;
return res;
return res;
return res;
return res;
```