

1 Problem 1: TSP (10 points)

- (a) Show that metric TSP is equivalent to the following problem: given a weighted graph G , find the cheapest walk that visits every vertex at least once and returns to the starting point.
- (b) In the metric path TSP problem, we are given special vertices s and t and need to compute the cheapest Hamiltonian path starting at s and ending at t . Give a 2-approximation for this problem.

2 Problem 2: Knapsack (15 points)

- (a) Modify the algorithm we went over in class so that it runs in time $O(n \cdot \min(W, V))$, where W is the capacity of the knapsack and V is the value of the optimal solution. **Hint:** What solutions do you really need to keep around in each subproblem?
- (b) Modify the algorithm so that it also returns an optimal solution, not just its value.
- (c) Show how to modify the FPTAS to improve the running time to $O(n^2/\epsilon)$. **Hint:** Start by running the greedy 2 approximation for knapsack.

3 Problem 3: Implementation of Knapsack (10 points)

Implement the dynamic program for knapsack you obtained in 2(a) and run it on the instance posted [here](#) for bounds $W = 10000000$ and $W = 20000000$. Turn in your code and write the answers you got here.