

```

1) public static void two(int n)
{
    if(n > 0)    //exit condition
    {
        System.out.println("n: " +n);    //potentially n operations
        two(n - 1);    //n-1 times
        two(n - 1);    //n-1 times
    }
    else if (n < 0)    //exit condition
    {
        two(n + 1);    //potentially n times
        two(n + 1);    //potentially n times
        System.out.println("n: " + n);    //potentially n times
    }
}

```

GRF is $5n$.

$O(n)$

```

2) public void three(int n)
{
    int i, j, k;    //3
    for (i = n/2; i > 0; i = i/2)    //log n
        for (j = 0; j < n; j++)    // n^2
            for (k = 0; k < n; k++)    // (n-1)^3
                System.out.println("i: " + i + " j: " + j+" k: " + k);
    //n-1 times
} // end three

```

GRF = $n^3 + n^2 + n - 1 + \log N$

$O(n^3)$

```

3) public static void four(int n)
{
    if (n > 1)    //termination condition    //exit condition
    {
        System.out.println(n);    //1
        four(n-1);    //n-1 times
    }
    for (int i = 0; i < n; i++)    //n times
        System.out.println(i);    //n times
}

```

GRF = $2n + n - 1 + 1$

$O(N)$

Explanation:

In order to get your growth rate function, we count how many times a particular line of code is executed, given an arbitrary input size n .

Once we have the GRF, we can then approximate the time complexity by dropping the constant terms (terms that are added or subtracted) and lower order terms (if you have n^3 and n^2 , n^2 is dropped because it's a lower order than n^3). Whatever you have left, is your big-oh notation time complexity.

For all of my examples, I first looked for the GRF, then dropped the constant terms and lower order terms, in order to get the big-oh notation time complexity.