# ncaa\_region\_optimizer

June 19, 2020

## 1 Genetic Algorithms for Region Paritioning

We will be using some Python modules installed by pip rather than Anaconda, so I must adjust the import path.

```
[1]: import sys
sys.path.insert( 1, '/usr/local/lib/python3.7/site-packages' )
```

Import other packages.

```
[3]: %matplotlib inline
```

## 1.1 Import the data

```
[4]: data_filename = 'wrestling-schools-data.csv'
df = pd.read_csv( data_filename )
len( df )
```

[4]: 106

```
[5]: df.head()
```

```
[5]:
        UniqueID
                            College/University Name
                                                                       Street \
     0
               1
                                     Adrian College
                                                             10 S Madison St
     1
               2
                  Alfred State College (add 2018)
                                                      10 Upper College Drive
     2
               3
                                       Alma College
                                                           614 W Superior St
     3
               4
                                           Augsburg
                                                          2211 Riverside Ave
     4
               5
                                     Augustana (IL)
                                                                 639 38th St
              City State
                            Latitude Longitude Power-1 Power-2
                                                                    NCAA Asgt \
                       MI 41.899337 -84.044547
     0
             Adrian
                                                    2.4514
                                                              2.927
                                                                            3.0
     1
             Alfred
                       NY 42.254334 -77.789646
                                                    0.0000
                                                              0.000
                                                                            NaN
     2
                           43.380011 -84.655654
                                                                            3.0
               Alma
                       ΜI
                                                    5.1091
                                                              5.941
     3 Minneapolis
                       MN 44.963541 -93.267835
                                                    9.6340
                                                              8.890
                                                                            2.0
     4 Rock Island
                       IL 41.470591 -90.583733
                                                    0.0000
                                                              0.301
                                                                            1.0
        ND Asgt
                 ND Asgt2
                           ND Asgt3 Purdue Asgt1 Purdue Asgt2 WSU Asgt1 \
     0
            2.0
                      1.0
                                 5.0
                                                4.0
                                                              2.0
                                                                          2.0
     1
            NaN
                      NaN
                                 {\tt NaN}
                                               5.0
                                                              7.0
                                                                          4.0
     2
            6.0
                      1.0
                                 5.0
                                                4.0
                                                              2.0
                                                                          5.0
     3
            6.0
                      5.0
                                 3.0
                                                5.0
                                                              4.0
                                                                          6.0
     4
            2.0
                      4.0
                                 3.0
                                                3.0
                                                              2.0
                                                                          5.0
        WSU Asgt2
              6.0
     0
              4.0
     1
     2
              6.0
     3
              5.0
              5.0
     4
```

#### 1.1.1 Drop schools we don't want in this analysis

Some schools were dropped for various domain-specific reasons. See paper.

```
[6]: df = df.drop( [ 31, 61, 85 ] )
num_schools = len( df )
num_schools
```

[6]: 103

#### 1.1.2 Make it easy to fetch desired rows/columns

```
[7]: def school ( key ):
    if type( key ) == int or type( key ) == np.int64:
        column = 'UniqueID'
    else:
        column = 'College/University Name'
    return df[df[column] == key].iloc[0]
```

```
(SCH_ID, SCH_NAME, SCH_ADDR, SCH_CITY, SCH_STATE, SCH_LAT, SCH_LNG, SCH_POW1, SCH_POW2,

SCH_NCAA, SCH_ND1, SCH_ND2, SCH_ND3, SCH_PUR1, SCH_PUR2, SCH_WSU1, SCH_WSU2)

⇒= \
list(df.columns.values)

def all_ids():
    return list(df['UniqueID'])

def index_to_id(index):
    return df['UniqueID'].iloc[index]

# print(school(2)[SCH_NAME])

# print(school('Augsburg')[SCH_ID])

# print(school(50)[SCH_LAT], get_school(50)[SCH_LNG])
```

### 1.2 Map distance tools

Define measure for computing distance on the (curved) surface of the earth.

```
[8]: def school_latlng ( school ): return ( school[SCH_LAT], school[SCH_LNG] )
```

Now pre-compute the distance between any two pair of schools and cache it in a matrix, because we'll be asking these distance questions a million times below, and this cache will speed it up a lot.

### 1.3 Utilities for partitions

```
return [ random.randint( 0, num_parts_in_partition - 1 ) for i in range(⊔
→num_schools ) ]
```

```
[11]: def print partition ( partition ):
         for part_index in range( num_parts_in_partition ):
             schools = schools_in_part_in_partition( part_index, partition )
             powers = [ school[SCH_POW2] for school in schools ]
             print( 'Region {:1d}, {:2d} schools, mean power {:7.5f} (stdev {:7.5f}):
      →'.format(
                 part_index + 1, size of_part_in_partition( part_index, partition ),
                 statistics.mean( powers ), statistics.stdev( powers ) )
             print( '----')
             centroid = (
                 statistics.mean( [ school[SCH_LAT] for school in schools ] ),
                 statistics.mean([school[SCH LNG] for school in schools]),
             print( ' Centroid: {:7.3f} lat, {:7.3f} lon'.format(
                 centroid[0], centroid[1] ) )
             latlngs = [ school_latlng( school ) for school in schools ]
             print( ' Mean distance to centroid: {:8.3f} miles'.format(
                 statistics mean( [ great_circle( centroid, latlng ).miles for_
      →latlng in latlngs ] )
             ) )
             for s in schools:
                 print( '
                               {:30.30s} {:30.30s} {:>7.1f} miles'.format(
                     s[SCH_NAME],
                     '{}, {}, {}'.format(s[SCH ADDR], s[SCH CITY], s[SCH STATE]),
                     great_circle( school_latlng( s ), centroid ).miles
                 ) )
             print()
     # print_partition( random_partition() )
```

#### 1.4 Test map-drawing tools

#### All Schools



#### Plotting a random partition as an example



We will also want to be able to alter a partition so that its parts are numbered from west to easy, so that we can easily name them, as follows.

Schools labeled with this index:	Fall into the region with this name:
0	West
1	Central
2	Midwest
3	Mideast
4	East
5	Northeast

```
[14]: def resequence partition (partition):
          part_indices = range( max( partition ) + 1 )
          def average_longitude ( part_index ):
              lngs = [ school_latlng( s )[1] for s in \
                       schools_in_part_in_partition( part_index, partition ) ]
              return sum( lngs ) / len( lngs ) if len( lngs ) > 0 else 0
          result = [ ]
          new_indices = sorted( part_indices, key=average_longitude )
          permutation = dict( zip( new_indices, part_indices ) )
          convert = lambda i: permutation[i] if i in permutation else len(⊔
       →permutation )
          return [ convert( partition[i] ) for i in range( len( partition ) ) ]
      region_names = [ 'West', 'Central', 'Midwest', 'Mideast', 'East', 'Northeast' ]
      def region name ( index ):
          if 0 <= index < len( region_names ):</pre>
              return region_names[index]
          return 'Other'
      # resequence_partition( random_partition() )
```

## 1.5 Components of the Objective Function

First, we will want to experiment with the range of the various components of the objective function, to see how we should rescale them to match each other.

#### 1.5.1 Component 1: Variance of size of parts in the partition

```
[16]: def part_size_variance ( partition ):
    return statistics.variance( (
        size_of_part_in_partition( part, partition )
        for part in range( num_parts_in_partition )
        ) )
    obj_fn_mean1, obj_fn_std1 = how_to_standardize( part_size_variance )
    # plus we want size variance to be bad, so we need a -1 multiplier:
    def obj_fn_component_1 ( partition ):
        return ( part_size_variance( partition ) - obj_fn_mean1 ) / -obj_fn_std1
```

HBox(children=(FloatProgress(value=0.0, max=2500.0), HTML(value='')))

#### 1.5.2 Component 2: Total distance between schools in each part of the partition

```
[17]: # from itertools import combinations
      def total_distance_in_one_part ( part_index, partition ):
          # # Formerly, we used total travel distance among all pairs of schools,_{\sqcup}
       → like so:
          # indices = indices_for_part_in_partition( part_index, partition )
          # return sum( ( distance_lookup( i, j )
                          for i, j in combinations (indices, 2)))
          # To be consistent with other clustering techniques, we now use total \Box
       \rightarrow distance to centroid:
          indices = indices_for_part_in_partition( part_index, partition )
          centroid = ( df.iloc[indices][SCH_LAT].mean(), df.iloc[indices][SCH_LNG].
       →mean() )
          return sum( [geodesic( school locations[i], centroid ).miles for i in___
       →indices ] )
      def total_distance_of_all_parts ( partition ):
          return sum( ( total_distance_in_one_part( part, partition )
                        for part in range( num_parts_in_partition ) )
      obj_fn_mean2, obj_fn_std2 = how_to_standardize( total_distance_of_all_parts )
      \# plus we want travel distance to be bad, so we need a -1 multiplier:
      def obj_fn_component_2 ( partition ):
          return ( total_distance_of_all_parts( partition ) - obj_fn_mean2 ) / _ _
       \rightarrow-obj_fn_std2
```

HBox(children=(FloatProgress(value=0.0, max=2500.0), HTML(value='')))

#### 1.5.3 Component 3: Variance of mean powers of each part in partition

HBox(children=(FloatProgress(value=0.0, max=2500.0), HTML(value='')))

### 1.5.4 Objective function: sum of 3 components

### 1.6 Solving the problem with Genetic Algorithms

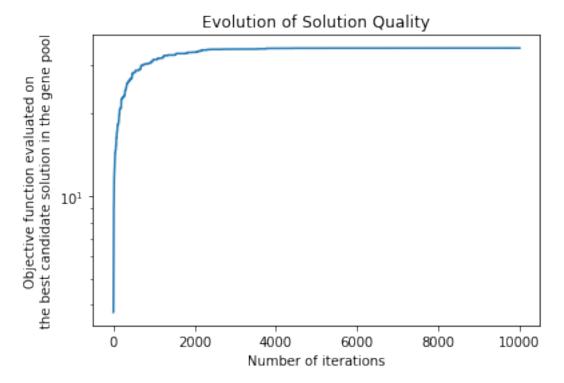
```
[20]: num_generations = 10000
def progress_bar ( name="Progress", size=num_generations ):
    bar = tqdm( range( size ), desc=name )
    def step ( *args ):
        bar.update( 1 )
        bar.display()
    return step
best, fitness_curve = optimize_partition(
    objective_function = objective_function,
    initial_pool = [ random_partition() for i in range( 10 ) ],
    size_of_partition = num_parts_in_partition,
    prob_mutate = 0.1,
    num_generations = num_generations,
    progress_callback = progress_bar()
)
```

HBox(children=(FloatProgress(value=0.0, description='Progress', max=10000.0, style=ProgressSty

```
After 10000 generations: max score = 34.6383 100% done, 10:55/10:55 (00:00)
```

```
[21]: # print_partition( best )

[22]: plt.plot( range( len( fitness_curve ) ), fitness_curve )
    plt.xlabel( 'Number of iterations' )
    plt.ylabel( 'Objective function evaluated on\nthe best candidate solution in_\( \text{\text{\text{othe gene pool'}}} \)
    plt.yscale( 'log' )
    plt.title( 'Evolution of Solution Quality' )
    # plt.savefig( 'evolution.pdf' )
    plt.show()
```



### 1.7 Viewing All Solutions

```
[23]: from itertools import combinations
   def robustness_check ( partition ):
        num_alternatives = 0
        num_better = 0
        best_obj_fun = objective_function( partition )
        for i, j in tqdm( list( combinations( range( len( partition ) ), 2 ) ) ):
        if partition[i] != partition[j]:
```

```
num_alternatives += 1
            partition[i], partition[j] = partition[j], partition[i] # try this_
→swap
            value obj fun = objective function( partition )
            if value_obj_fun > best_obj_fun:
                num better += 1
                best_obj_fun = value_obj_fun
            partition[i], partition[j] = partition[j], partition[i] # unswap, __
\rightarrow back to original
   print(f"{num_better} of {num_alternatives} neighboring partitions had_
⇔better objective functions." )
   print(f"Best objective function value among neighboring partitions:
→{best_obj_fun}" )
def partition_report ( name ):
   partition = list( ( df[name] - df[name].min() ).fillna( -1 ).astype( int ) )
   print( 'Region'.ljust( 20 ), 'N'.rjust( 6 ), 'Power'.rjust( 7 ), 'Distance'.
→rjust( 10 ) )
   for i in sorted( list( pd.Series( partition ).unique() ) ):
        if i == -1:
            continue
        s = size_of_part_in_partition( i, partition )
        print( region_name( i ).ljust( 20 ),
               str(s).rjust(6),
               str( round( mean_power_of_part( i, partition ), 2 ) ).rjust( 7 ),
               str( round( total_distance_in_one_part( i, partition ) / s, 2 )__
 →).rjust( 10 ) )
   print( 'Components'.ljust( 20 ),
           str( round( obj_fn_component_1( partition ), 2 ) ).rjust( 6 ),
           str( round( obj_fn_component_2( partition ), 2 ) ).rjust( 7 ),
           str( round( obj_fn_component_3( partition ), 2 ) ).rjust( 10 ) )
   print( 'Objective function'.ljust( 20 ), str( objective_function( partition⊔
→) ).rjust( 25 ) )
     robustness_check( partition )
   partition map( resequence partition( partition ), name+' Six-Part__
 →Partition')
```

```
[24]: GA = 'GA Best'
df[GA] = best
partition_report( GA )
```

Region	N	Power	Distance
West	18	2.06	75.4
Central	19	1.51	77.48
Midwest	17	1.78	110.72
Mideast	16	3.04	262.69
East	17	2.71	102.86
Northeast	16	1.78	134.48

Components 1.46 32.31 0.87 Objective function 34.638341667027454

### GA Best Six-Part Partition



## [25]: partition\_report( SCH\_NCAA )

Region	N	Power	Distance
West	15	3.65	125.72
Central	17	2.34	250.28
Midwest	17	2.07	143.35
Mideast	18	2.24	141.95
East	17	1.74	82.86
Northeast	17	1.16	72.53
Components	1.49	31.13	0.14
Objective function		32.75780	2125126304

## NCAA Asgt Six-Part Partition



[26]: # Don't waste time computing this; ND's third result is better (below). # partition\_report( SCH\_ND1 )

[27]: # Don't waste time computing this; ND's third result is better (below).
# partition\_report( SCH\_ND2 )

## [28]: partition\_report( SCH\_ND3 )

Region	N	Power	Distance
West	17	2.52	144.36
Central	16	1.53	66.24
Midwest	16	3.12	264.48
Mideast	18	1.22	74.93
East	16	1.58	109.68
Northeast	18	3.04	138.58
Components	1.49	31.66	0.14
Objective function		33.2893	0979190577

#### ND Asgt3 Six-Part Partition



## [29]: partition\_report( SCH\_PUR1 )

Region	N	Power	Distance
West	16	2.66	67.8
Central	18	1.01	110.32
Midwest	18	3.32	146.96
Mideast	15	2.21	176.04
East	18	2.68	292.02
Northeast	17	1.01	181.03

Components 1.43 27.53 -0.34 Objective function 28.61507038148471

## Purdue Asgt1 Six-Part Partition



[30]: # Don't waste time computing this; it's an 8-school solution. # partition\_report( SCH\_PUR2 )

## [31]: partition\_report( SCH\_WSU1 )

Region	N	Power	Distance
West	17	2.14	76.04
Central	17	2.16	173.55
Midwest	18	2.01	94.59
Mideast	16	2.25	187.51
East	17	2.18	141.75
Northeast	17	2.16	225.0
Components	1.54	29.39	1.67
Objective function		32.6071	7496050781



```
[32]: # Can't evaluate this one, because it's 8 regions, and the code herein assumes

→6.

# partition_report( SCH_WSU2 )
```

## 1.8 Exporting Partitions

The following function is useful for making spreadsheets that can easily beloaded into batchgeo.com for visualizing any region partition with high-quality graphics.

```
[33]: def export_partition ( colname ):
    cols = ['College/University Name', 'Street', 'City_
    ', 'State', 'Latitude', 'Longitude', colname]
    new_df = df[cols]
    cols[3] = 'City'
    cols[6] = 'Group'
    new_df.columns = cols
    new_df.to_csv( 'partition_'+colname+'.csv', index=False )
    for col in df.columns[9:]:
        export_partition( col )
```

```
[]:
```