Bentley University MA255 in pure R $\,$

Content extracted from the How to Data Website

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Contents

MA255 is an undergraduate statistics course at Bentley University on the Design of Experiments. The description from the course catalog can be found here.

The course covers various experimental designs including factorial and fractional factorial designs, interaction among factors, and applications in management (including cost savings and policy making) as well as in marketing.

The sequence of topics below is not necessarily the final version; this topic page is under construction.

Summarizing data and exploratory analysis

- How to summarize a column
- How to compute summary statistics
- How to summarize and compare data by groups
- How to create bivariate plots to compare groups

Experiments with one treatment factor

- How to check the assumptions of a linear model
- How to compute the power of a test comparing two population means
- How to perform an analysis of covariance (ANCOVA)
- How to perform pairwise comparisons
- How to perform post-hoc analysis with Tukey's HSD test
- How to test for a treatment effect in a single factor design

Analyzing data from a larger design

- How to plot interaction effects of treatments
- How to analyze the sample means of different treatment conditions
- How to compare two nested linear models
- How to conduct a mixed designs ANOVA
- How to conduct a repeated measures ANOVA
- How to perform a planned comparison test

Content last modified on 07 December 2021.

How to summarize a column

Description

When provided with a dataset in which you want to focus on one column, how would you compute descriptive statistics for that column?

Related task:

- How to compute summary statistics
- How to summarize and compare data by groups

Solution in pure R

The solution below uses an example dataset about the teeth of 10 guinea pigs at three Vitamin C dosage levels (in mg) with two delivery methods (orange juice vs. ascorbic acid). (See how to quickly load some sample data (on website).)

```
df <- ToothGrowth
```

Let us consider qualitative and quantitative variables separately.

Consider the qualitative column "supp" in the dataset (which type of supplement the animal received). To count the distribution of each categorical value, use table():

```
table(df$supp) # OR summary(df$supp)

OJ VC
30 30
```

The output says that there are 30 observations under each of the two levels, Orange Juice and Ascorbic Acid. If you wish to jointly summarize two categorical columns, provide both to table():

```
table(df$supp, df$dose)

0.5 1 2
0J 10 10 10
VC 10 10 10
```

This informs us that there are 10 observations for each of the combinations.

Note: If there are more than 2 categorical variables of interest, you can use ftable() instead.

Now consider the quantitative column len in the dataset (the length of the animal's tooth). We can compute summary statistics for it just as we can for a whole dataframe (as we cover in how to compute summary statistics).

```
Min. 1st Qu. Median Mean 3rd Qu. Max.
4.20 13.07 19.25 18.81 25.27 33.90
```

The individual functions for mean, standard deviation, etc. covered under "how to compute summary statistics" apply to individual columns as well. For example, we can compute quantiles:

```
quantile(df$len) # quantiles
```

```
0% 25% 50% 75% 100%
4.200 13.075 19.250 25.275 33.900
```

Content last modified on 24 October 2021.

How to compute summary statistics

Description

The phrase "summary statistics" usually refers to a common set of simple computations that can be done about any dataset, including mean, median, variance, and some of the others shown below.

Related tasks:

- How to summarize a column
- How to summarize and compare data by groups

Solution in pure R

We first load a famous dataset, Fisher's irises, just to have some example data to use in the code that follows. (See how to quickly load some sample data (on website).)

```
library(datasets)
data(iris)
```

How big is the dataset? The output shows number of rows then number of columns.

```
dim(iris) # Short for "dimensions."
```

```
[1] 150 5
```

What are the columns and their data types? Can I see a sample of each column?

```
str(iris) # Short for "structure."
```

```
'data.frame': 150 obs. of 5 variables:

$ Sepal.Length: num 5.1 4.9 4.7 4.6 5 5.4 4.6 5 4.4 4.9 ...

$ Sepal.Width : num 3.5 3 3.2 3.1 3.6 3.9 3.4 3.4 2.9 3.1 ...

$ Petal.Length: num 1.4 1.4 1.3 1.5 1.4 1.7 1.4 1.5 1.4 1.5 ...

$ Petal.Width : num 0.2 0.2 0.2 0.2 0.4 0.3 0.2 0.2 0.1 ...

$ Species : Factor w/ 3 levels "setosa", "versicolor", ..: 1 1 1 1 1 1 1 1 1 ...
```

What do the first few rows look like?

```
head(iris) # Gives 5 rows by default. You can do head(iris,10), etc.
```

```
Sepal.Length Sepal.Width Petal.Length Petal.Width Species
1 5.1
               3.5
                            1.4
                                          0.2
                                                      setosa
2 4.9
               3.0
                            1.4
                                          0.2
                                                       setosa
3 4.7
               3.2
                            1.3
                                          0.2
                                                      setosa
4 4.6
               3.1
                            1.5
                                          0.2
                                                      setosa
5 5.0
               3.6
                            1.4
                                          0.2
                                                       setosa
6 5.4
                            1.7
               3.9
                                          0.4
                                                       setosa
```

The easiest way to get summary statistics for an R data.frame is with the summary function.

```
summary(iris)
```

```
Sepal.Length
                Sepal.Width
                               Petal.Length
                                              Petal.Width
Min. :4.300
               Min.
                     :2.000
                              Min.
                                     :1.000
                                             Min.
                                                    :0.100
1st Qu.:5.100
               1st Qu.:2.800
                              1st Qu.:1.600
                                             1st Qu.:0.300
Median :5.800
               Median :3.000
                              Median :4.350
                                           Median :1.300
Mean
     :5.843
               Mean :3.057
                              Mean :3.758
                                             Mean :1.199
3rd Qu.:6.400
               3rd Qu.:3.300
                              3rd Qu.:5.100
                                             3rd Qu.:1.800
Max.
     :7.900
              Max. :4.400
                              Max.
                                     :6.900
                                             Max. :2.500
     Species
         :50
setosa
versicolor:50
virginica:50
```

The columns from the original dataset are the column headings in the summary output, and the statistics computed for each are listed below those headings.

We can also compute these statistics (and others) one at a time for any given set of data points. Here, we let xs be one column from the above data.frame but you could use any vector or list.

Content last modified on 26 July 2021.

How to summarize and compare data by groups

Description

When given a set of data that has different treatment conditions and an outcome variable, we need to perform some exploratory data analysis. How would you quantitatively compare the treatment conditions with regards to the outcome variable?

Related tasks:

• How to compute summary statistics

Solution in pure R

The solution below uses an example dataset about the teeth of 10 guinea pigs at three Vitamin C dosage levels (in mg) with two delivery methods (orange juice vs. ascorbic acid). (See how to quickly load some sample data (on website).)

```
df <- ToothGrowth
```

To obtain the descriptive statistics of the quantitative column (len for length of teeth) based on the treatment levels (supp), we can use either the tapply or favstats functions.

```
attach(df)
tapply(len, supp, summary)
```

```
$0J
  Min. 1st Qu.
                 Median
                            Mean 3rd Ou.
                                            Max
  8.20
          15.53
                  22.70
                           20.66
                                   25.73
                                           30.90
   Min. 1st Qu.
                 Median
                            Mean 3rd Qu.
                                            Max.
   4.20
          11.20
                  16.50
                           16.96
                                   23.10
                                            33.90
```

You can replace summary in the call to tapply with mean, median, max, min, or quantile to get just one value. An example is shown below for quantiles.

```
tapply(len, supp, quantile, prob = 0.25, data=df) # 1st quartile
```

```
0J VC
15.525 11.200
```

Content last modified on 24 October 2021.

How to create bivariate plots to compare groups

Description

Suppose we have a dataset with different treatment conditions and an outcome variable, and we want to perform exploratory data analysis. How would we visually compare the treatment conditions with regards to the outcome variable?

Related tasks:

- How to create basic plots (on website)
- How to add details to a plot (on website)
- How to create a histogram (on website)
- How to create a box (and whisker) plot (on website)
- How to change axes, ticks, and scale in a plot (on website)
- How to plot interaction effects of treatments

Solution in pure R

How to check the assumptions of a linear model

Description

If you plan to use a linear model to describe some data, it's important to check if it satisfies the assumptions for linear regression. How can we do that?

Solution in pure R

When performing a linear regression, the following assumptions should be checked.

1. We have two or more columns of numerical data of the same length.

The solution below uses an example dataset about car design and fuel consumption from a 1974 Motor Trend magazine. (See how to quickly load some sample data (on website).) We can see that our columns all have the same length.

```
df <- mtcars
head(df)</pre>
```

```
qsec vs am gear carb
                  mpg cyl disp hp drat wt
Mazda RX4
                               110 3.90 2.620 16.46 0
                  21.0 6
                  21.0 6
                               110 3.90 2.875 17.02 0
                                                                4
Mazda RX4 Wag
                           160
Datsun 710
                  22.8 4
                           108
                                 93 3.85 2.320 18.61 1
                                                                1
                  21.4 6
Hornet 4 Drive
                           258
                               110 3.08 3.215 19.44 1
                                                                1
Hornet Sportabout 18.7 8
                           360
                               175 3.15 3.440 17.02 0
                                                                2
                              105 2.76 3.460 20.22 1 0 3
Valiant
                  18.1 6
                           225
                                                                1
```

2. Scatter plots we've made suggest a linear relationship.

Scatterplots are covered in how to create basic plots (on website), but after making the model, we can also examine the residuals.

So let's make the model. Our predictors will be the number of cylinders and the weight of the car and the response will be miles per gallon. (See also how to fit a linear model to two columns of data (on website).)

```
model = lm(mpg~ cyl + wt, data=df)
```

We test for linearity with residual plots. We show just one residual plot here; you should make one for each predictor. R's plot function knows how to create residual plots. (See also how to compute the residuals of a linear model (on website).)

```
plot(model, which = 1)
```

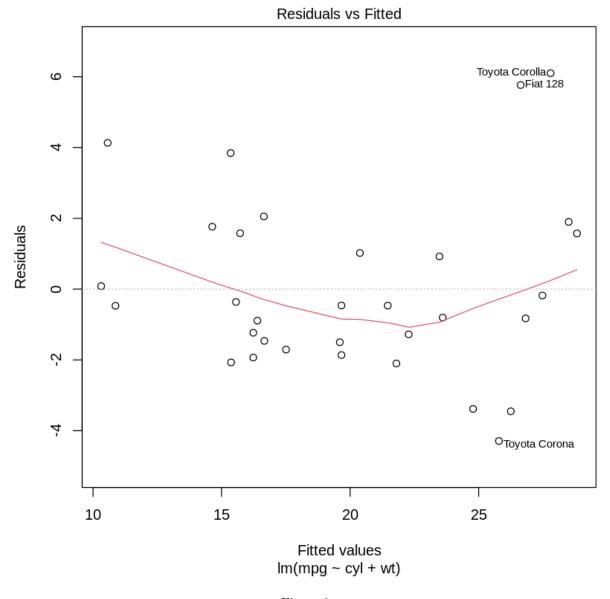


Figure 1: png

3. After making the model, the residuals seem normally distributed.

We can check this by constructing a QQ-plot, which compares the distribution of the residuals to a normal distribution. Here we use SciPy, but there are other methods; see how to create a QQ-plot (on website).

```
plot(model, which = 2)
```

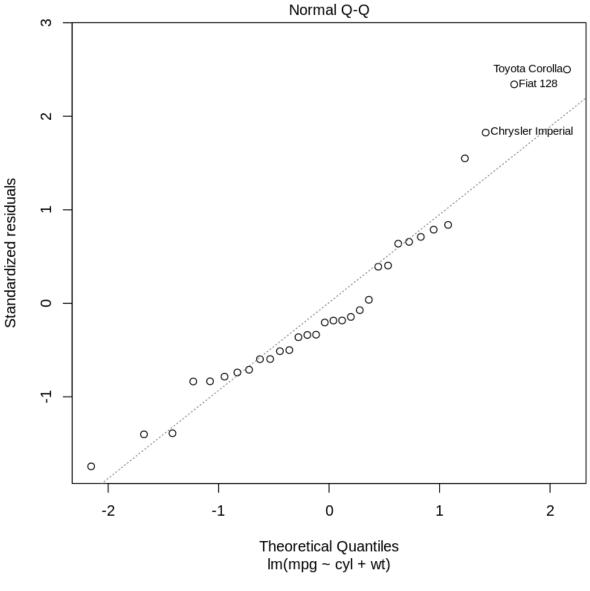


Figure 2: png

4. After making the model, the residuals seem homoscedastic.

This assumption is sometimes called "equal variance," and can be checked by the regplot function in Seaborn. We must first standardize the residuals, which we can do with NumPy. We want to see a plot with no clear pattern; a cone shape to the data would indicate heteroscedasticity, the opposite of homoscedasticity.

```
plot(model, which = 3) # assumption of equal variance
```

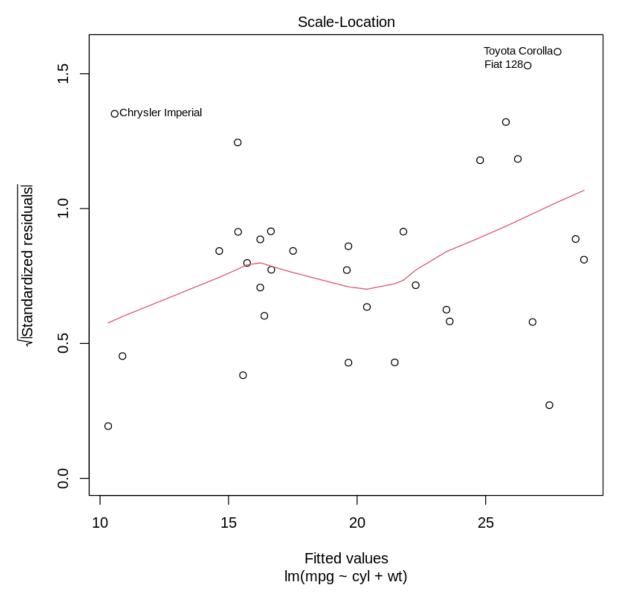


Figure 3: png

Content last modified on 24 October 2021.

How to compute the power of a test comparing two population means

Description

When creating a factorial design, it is important that it has adequate power to detect significant main effects and interaction effects of interest. How can we calculate the power of a two-sample t test that we aim to perform in such a situation?

Related tasks:

• How to choose the sample size in a study with two population means (on website)

Solution in pure R

We use the power.t.test function in R. It embodies a relationship among five variables; you provide any four of them and it will compute the fifth to be consistent with the first four, regarding the two-sample t-test you plan

For this example, let's say that:

- You plan to create a balanced 4×2 factorial experiment with 32 subjects.
- You wish to be able to detect a difference
- You want to know the expected power for the test of a main effect of factor A.
- Your significance level is $\alpha = 0.05$.

We proceed as follows.

```
# install.packages('pwr') # if you have not already installed it
library(pwr)

obs <- 32  # number of subjects (or observations)
effect <- 0.25  # effect size
alpha <- 0.05  # significance level
ratio <- 1  # ratio of the number of observations in one sample to the other

# We leave power unspecified, so that power.t2n.test will compute it for us:
pwr.t2n.test(n1=obs, n2=obs, d=effect, sig.level=alpha, power=NULL)</pre>
```

```
t test power calculation

n1 = 32
n2 = 32
d = 0.25
sig.level = 0.05
power = 0.1662985
alternative = two.sided
```

The power is 0.1663, which means that the probability of rejecting the null hypothesis when in fact it is false OR the probability of avoiding a Type II error is 0.1663.

Content last modified on 30 November 2021.

How to perform an analysis of covariance (ANCOVA)

Description

Recall that covariates are variables that may be related to the outcome but are unaffected by treatment assignment. In a randomized experiment with one or more observed covariates, an analysis of covariance (ANCOVA) addresses this question: How would the mean outcome in each treatment group change if all groups were equal with respect to the covariate? The goal is to remove any variability in the outcome associated with the covariate from the unexplained variability used to determine statistical significance.

Related tasks:

- How to do a one-way analysis of variance (ANOVA) (on website)
- How to compare two nested linear models
- How to conduct a mixed designs ANOVA
- How to conduct a repeated measures ANOVA

Solution in pure R

The solution below uses an example dataset about car design and fuel consumption from a 1974 Motor Trend magazine. (See how to quickly load some sample data (on website).)

```
df <- mtcars
df$vs <- as.factor(df$vs)</pre>
```

Let's use ANCOVA to check the effect of the engine type (0 = V-shaped, 1 = straight, in the variable vs) on the miles per gallon when considering the weight of the car as a covariate. We will use the ancova function from the pingouin package to conduct the test.

```
cov.model <- lm(mpg ~ wt + vs, data = df)
anova(cov.model)</pre>
```

```
Df Sum Sq Mean Sq F value Pr(>F)
wt 1 847.72525 847.725250 109.704168 2.284396e-11
vs 1 54.22806 54.228061 7.017656 1.292580e-02
Residuals 29 224.09388 7.727375 NA NA
```

The p-value for each variable can be found in the final column of the output, called Pr(>F).

The p-value for the wt variable tests the null hypothesis, "The quantities wt and mpg are not related." Since it is below 0.05, we reject the null hypothesis, and conclude that wt is significant in predicting mpg.

The p-value for the vs variable tests the null hypothesis, "The quantities vs and mpg are not related if we hold wt constant." Since it is below 0.05, we reject the null hypothesis, and conclude that vs is significant in predicting mpg even among cars with equal weight (wt).

If we wish to create a 2-factor ANCOVA model, we can test to see if the engine type (0 = V-shaped, 1 = straight) and transmission type (0 = automatic, 1 = manual) have an effect on the Miles/gallon per car when considering the weight of the car as a covariate.

```
cov.model.2 <- lm(mpg ~ wt + vs + am, data = df)
anova(cov.model.2)</pre>
```

```
Df Sum Sq
                        Mean Sq
                                   F value
                                              Pr(>F)
           1 847.725250 847.725250 109.729918 3.420018e-11
wt
٧s
              54.228061 54.228061
                                     7.019303 1.310627e-02
                                     1.006807 3.242621e-01
           1
               7.778149
                          7.778149
Residuals 28 216.315728
                          7.725562
                                           NA
```

The p-values are again in the final column of output. They show that at the 5% significance level, we would conclude that engine type (vs) significantly impacts the Miles/gallon per car while accounting for the weight of the car (wt) but the transmission type (am) does not.

Content last modified on 07 December 2021.

How to perform pairwise comparisons

Description

When analyzing data from a completely randomized single-factor design, suppose that you have performed an ANOVA and noticed that there's a significant difference between at least one pair of treatment levels. How can pairwise comparisons help us explore which pairs of treatment levels are different?

Related tasks:

- How to do a one-way analysis of variance (ANOVA) (on website)
- How to perform post-hoc analysis with Tukey's HSD test

Solution in pure R

The solution below uses an example dataset that details the counts of insects in an agricultural experiment with six types of insecticides, labeled A through F. (This is one of the datasets built into R for use in examples like this one.)

```
df <- InsectSprays
head( df, 10 )</pre>
```

```
count spray
   10
          Α
2
    7
          Α
3
   20
          Α
   14
          Α
5
   14
6
   12
   10
          Α
8
   23
          Α
   17
          Α
10 20
```

Before we perform any post hoc analysis, we need to see if the count of insects depends on the type of insecticide given by conducting a one way ANOVA. (See also how to do a one-way analysis of variance (ANOVA) (on website).)

```
aov1 = aov(count ~ spray, data = df)
summary(aov1)
```

```
Df Sum Sq Mean Sq F value Pr(>F)
spray 5 2669 533.8 34.7 <2e-16 ***
Residuals 66 1015 15.4
---
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

At the 5% significance level, we see that the count differs according to the type of insecticide used. We assume that the model assumptions are met, but do not verify that here.

If we would like to compare the pairs without any corrections, we can use the pairwise.t.test function built into R.

```
pairwise.t.test(df$count, df$spray, p.adj="none")
```

```
Pairwise comparisons using t tests with pooled SD

data: df$count and df$spray

A B C D E
B 0.604 - - - - -
C 7.3e-11 8.5e-12 - - -
D 9.8e-08 1.2e-08 0.081 - -
E 2.8e-09 3.3e-10 0.379 0.379 -
F 0.181 0.408 2.8e-13 4.0e-10 1.1e-11

P value adjustment method: none
```

Techniques to adjust the above table for multiple comparisons include the Bonferroni correction, Fisher's Least Significant Difference (LSD) method, Dunnett's procedure, and Scheffe's method. These can be used in place of "none" for the p.adj argument; see details here.

You can also determine the magnitude of these differences; see how to perform post-hoc analysis with Tukey's HSD test.

Content last modified on 10 September 2021.

How to perform post-hoc analysis with Tukey's HSD test

Description

If we run a one-way ANOVA test and find that there is a significant difference between population means, we might want to know which means are actually different from each other. One way to do so is with Tukey's Honestly Significant Differences (HSD) method. It creates confidence intervals for each pair of samples, while controlling for Type I error rate across all pairs. Thus the resulting intervals are a little wider than those produced using Fisher's LSD method. How do we make these confidence intervals, with an appropriate visualization?

Solution in pure R

We load here the same data that appears in the solution for how to perform pairwise comparisons. That solution used ANOVA to determine which pairs of groups have significant differences in their means; follow its link for more details.

```
# Load an inbuilt data set called InsectSprays and assign it to the variable df
df <- InsectSprays
head( df, 10 )</pre>
```

```
count spray
   10
           Α
2
    7
           Α
3
   20
           Α
   14
           Α
5
   14
           Α
6
   12
   10
           Α
   23
8
           Α
9
   17
           Α
10 20
           Α
```

We now want to perform an unplanned comparison test on the data to determine the magnitudes of the differences between pairs of groups. We do this by applying Tukey's HSD approach to perform pairwise comparisons and generate confidence intervals that maintain a specified experiment-wide error rate. We use R's built-in TukeyHSD function, and we give it the same ANOVA results that we computed in the solution for how to perform pairwise comparisons.

```
aov1 <- aov(count ~ spray, data = df)
TukeyHSD(aov1, "spray", ordered=TRUE, conf.level = 0.95)</pre>
```

```
Tukey multiple comparisons of means
    95% family-wise confidence level
    factor levels have been ordered
Fit: aov(formula = count ~ spray, data = df)
$spray
          diff
                    lwr
                              upr
                                      p adj
E-C 1.4166667 -3.282742 6.116075 0.9488669
D-C 2.8333333 -1.866075 7.532742 0.4920707
A-C 12.4166667 7.717258 17.116075 0.0000000
B-C 13.2500000 8.550591 17.949409 0.0000000
F-C 14.5833333 9.883925 19.282742 0.0000000
D-E 1.4166667 -3.282742 6.116075 0.9488669
A-E 11.0000000 6.300591 15.699409 0.0000000
B-E 11.8333333 7.133925 16.532742 0.0000000
F-E 13.1666667 8.467258 17.866075 0.0000000
A-D 9.5833333 4.883925 14.282742 0.0000014
B-D 10.4166667 5.717258 15.116075 0.0000002
F-D 11.7500000 7.050591 16.449409 0.0000000
B-A 0.8333333 -3.866075 5.532742 0.9951810
F-A 2.1666667 -2.532742 6.866075 0.7542147
F-B 1.3333333 -3.366075 6.032742 0.9603075
```

Because the above table contains a lot of information, it's often helpful to visualize these intervals. R lets us do so by simply calling plot on the above table. We add a few plotting parameters to improve its appearance.

```
plot( TukeyHSD(aov1, "spray", ordered=TRUE, conf.level = 0.95),
    las=1, cex.axis=0.9 )
```

95% family-wise confidence level

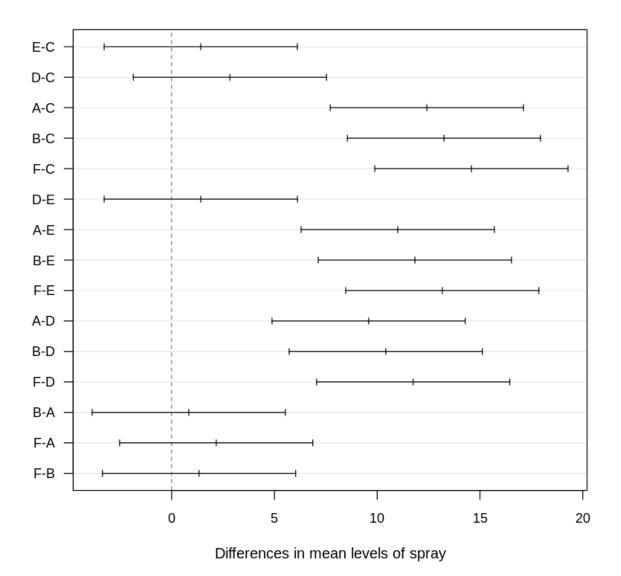


Figure 4: png

Confidence intervals that cross the vertical, dashed line at x=0 are those in which the means across those groups may be equal. Other intervals have mean differences whose 95% confidence intervals do not include zero.

Content last modified on 14 September 2021.

How to test for a treatment effect in a single factor design

Description

Suppose you are given a dataset that has more than one treatment level and you wish to see if there is a unit-level treatment effect. How would you check that?

Solution in pure R

How to plot interaction effects of treatments

Description

When there are multiple treatment conditions with multiple levels and you wish to undertsand the interaction effects of each of them, a plot can be useful. How can we create the right kind of plot for that situation?

- How to create basic plots (on website)
- How to add details to a plot (on website)
- How to create a histogram (on website)
- How to create a box (and whisker) plot (on website)
- How to change axes, ticks, and scale in a plot (on website)
- How to create bivariate plots to compare groups

Solution in pure R

How to analyze the sample means of different treatment conditions

Description

In a single-factor experiment with three or more treatment levels, how can we compare them to see which one impacts the outcome variable the most?

Solution in pure R

How to compare two nested linear models

Description

Model A is said to be "nested" in model B if the predictors included in A are a subset of those included in B. In such a situation, how can we determine if the larger model (in this case B) is significantly better than the smaller (reduced) model? We can use an Extra Sums of Squares test, also called a partial F-test, to compare two nested linear.

This technique will also help us with another question. If we have a multivarate linear model,

$$\hat{y} = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_k x_k,$$

how can we test the influence of only some of the coefficients? If we remove some of the coefficients, we have a smaller model nested in the larger one, so the question is the same.

Related tasks:

- How to do a one-way analysis of variance (ANOVA) (on website)
- How to conduct a mixed designs ANOVA
- How to conduct a repeated measures ANOVA
- How to perform an analysis of covariance (ANCOVA)

Solution in pure R

The solution below uses an example dataset about car design and fuel consumption from a 1974 Motor Trend magazine. (See how to quickly load some sample data (on website).)

We will create two models, one nested inside the other, in a natural way in this example. But this is not the only way to create nested models; it is just an example.

```
# install.packages("datasets") # if you have not done so already
library(datasets)
data(mtcars)
df <- mtcars</pre>
```

Consider a model using number of cylinders (cyl) and weight of car (wt) to predict its fuel efficiency (mpg). We create this model and perform an ANOVA to see if the predictors are significant.

```
# Build the model
add_model <- lm(mpg ~ cyl + wt, data = df)
# Perform an ANOVA
anova(add_model)</pre>
```

```
Df Sum Sq Mean Sq F value Pr(>F)

cyl 1 817.7130 817.712952 124.04369 5.424327e-12

wt 1 117.1623 117.162269 17.77303 2.220200e-04

Residuals 29 191.1720 6.592137 NA NA
```

The final column of output suggests that both predictors are significant. A natural question to ask is whether the two predictors have an interaction effect. Let's create a model containing the interaction term.

```
# Build the model with interaction
int_model <- lm(mpg ~ cyl * wt, data = df)
# Perform an ANOVA
anova(int_model)</pre>
```

```
Df Sum Sq Mean Sq F value Pr(>F)

cyl 1 817.71295 817.712952 145.856269 1.280635e-12

wt 1 117.16227 117.162269 20.898350 8.942713e-05

cyl:wt 1 34.19577 34.195767 6.099533 1.988242e-02

Residuals 28 156.97620 5.606293 NA NA
```

As seen in the final column of output, there is a significant interaction between the two predictors.

We now have one model (add_model) nested inside a larger model (int_model). To check which model is better, we can conduct an ANOVA comparing the two models.

```
# Use ANOVA to compare the models
anova(add_model, int_model)
```

```
Res.Df RSS Df Sum of Sq F Pr(>F)
1 29 191.1720 NA NA NA NA
2 28 156.9762 1 34.19577 6.099533 0.01988242
```

We have just performed this hypothesis test:

 H_0 = the two models are equally useful for predicting the outcome

 $H_a =$ the larger model is significantly better than the smaller model

In the final column of the output, called Pr(>F), the only number in that column is our test statistic, 0.01988. Since is below our chosen threshold of 0.05, we reject the null hypothesis, and prefer to use the second model.

This method can be used to check if covariates should be included in the model, or if additional variables should be added as well.

Content last modified on 30 November 2021.

How to conduct a mixed designs ANOVA

Description

When you have a dataset that includes the responses of a mixed design test, where one factor is a withinsubjects factor and the other is a between-subjects factor, and you wish check if there is a significant difference for both factors, this requires a Mixed Design ANOVA. How can we conduct one?

Related tasks:

- How to do a one-way analysis of variance (ANOVA) (on website)
- How to do a two-way ANOVA test with interaction (on website)
- How to do a two-way ANOVA test without interaction (on website)
- How to compare two nested linear models using ANOVA
- How to conduct a repeated measures ANOVA
- How to perform an analysis of covariance (ANCOVA)

Solution in pure R

We create the data for a hypothetical 2×2 mixed design with the following attributes.

- Between-subjects treatment factor: Type of music played (classical vs. rock)
- Within-subjects treatment factor: Type of room (light vs. no light)
- Outcome variable: Heart rate of subject

```
room.type heart.rate
  subject music
1 1
                                78
          Classical Light
2 2
          Rock
                     Light
                                60
3 3
                                85
          Classical Light
                                75
4 4
          Rock
                     Light
5 5
          Classical Light
                                99
6 6
          Rock
                     Light
                                94
```

We conduct a two-way mixed-design ANOVA as shown below. The specific parameters have these meanings:

- The dependent variable is heart.rate.
- The within-group factor is room.type.
- The between-group factor is music.
- The Error() term is critical in differentiating between a between subjects and within subjects model. It tells R that there is one observation per subject for each level of room.type.

```
aov_mixed <- aov(heart.rate ~ room.type*music + Error(subject/room.type), data=df)
summary(aov_mixed)</pre>
```

```
Error: subject
         Df Sum Sq Mean Sq F value Pr(>F)
music
          1 162.4
                     162.4
                             1.587 0.243
Residuals 8 819.0
                     102.4
Error: subject:room.type
               Df Sum Sq Mean Sq F value Pr(>F)
room.type
                1 832.1
                           832.1
                                   6.416 0.0351 *
                    76.0
                            76.0
                                   0.586 0.4658
room.type:music 1
Residuals
                8 1037.4
                           129.7
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

The output informs us that, on average, the subjects that listened to classical music did not significantly differ (p = 0.243 > 0.05) from those that listened to rock music. However, there is, on average, a significant difference (p = 0.0351 < 0.05) between each of the subject's heart rate when put in a room with or without light. Additionally, since the interaction term is not significant (p = 0.4658 > 0.05), we can use the additive (no interaction) model.

Content last modified on 24 October 2021.

How to conduct a repeated measures ANOVA

Description

In a repeated measures test, the same subject receives multiple treatments. When you have a dataset that includes the responses of a repeated measures test where the measurements are dependent (within subjects design), you may wish to check if there is a difference in the treatment effects. How would you conduct a repeated measures ANOVA to answer that question?

Related tasks:

- How to do a one-way analysis of variance (ANOVA) (on website)
- How to do a two-way ANOVA test with interaction (on website)
- How to do a two-way ANOVA test without interaction (on website)
- How to compare two nested linear models using ANOVA
- How to conduct a mixed designs ANOVA
- How to perform an analysis of covariance (ANCOVA)

Solution in pure R

How to perform a planned comparison test

Description

Suppose that ANOVA reveals a significant difference between treatment levels, and you wish to explore further through post hoc analysis by comparing two specific treatment levels. How can we perform planned comparisons, also called a contrast test?

Solution in pure R