

# Package ‘makehams’

March 7, 2015

**Title** Ultimate Select Survival Model (AMLCR)

**Version** 1.0

**Description** Implements Makeham's Law (with variable select period), De Moivre's Law, CFM as well as provides various actuarial functions such as moments of insurances and annuities.

**Depends** R (>= 2.1.1)

**License** GPL-2

**LazyData** true

## R topics documented:

annx . . . . .	1
Ax . . . . .	2
cfm . . . . .	3
createInsuranceTable . . . . .	3
createLifeTable . . . . .	4
demoivres . . . . .	4
makehams . . . . .	5
tEx . . . . .	5
thV . . . . .	6
tpx . . . . .	6
tqx . . . . .	7
udeferredtx . . . . .	7
uxt . . . . .	8
v . . . . .	8
<b>Index</b>	<b>9</b>

---

annx	<i>EPV of Annuity</i>
------	-----------------------

---

## Description

Calculates the Expected Presented Value of various annuities

## Usage

```
annx(x = gl.g(x), s = 0, i = gl.g(i), m = 1, n = gl.g(w) - x, c = 0,  
     e = 1, mt = 1)
```

**Arguments**

x	the current age
s	the select used so far
i	the interest rate
m	the compounding frequency
n	the length of the term
c	indicator of continuous (1 if continuous)
e	indicator of endowment (NOTE of an annuity should always be 1)
mt	the moment of the insurance

**Details**

By default calculates the first moment of discrete, whole life annuity due

---

Ax	<i>EPV of Insurance</i>
----	-------------------------

---

**Description**

Calculates the Expected Presented Value of various insurances

**Usage**

$Ax(x = gl.g(x), s = 0, i = gl.g(i), m = 1, n = gl.g(w) - x, c = 0, e = 0, mt = 1)$

**Arguments**

x	the current age
s	the select used so far
i	the interest rate
m	the compounding frequency
n	the length of the term
c	indicator of continuous (1 if continuous)
e	indicator of endowment (1 if endowment)
mt	the moment of the insurance

**Details**

By default calculates first moment of discrete, whole life insurance

cfm

*Change Survival Model to CFM***Description**

Changes parameters and force of mortality function to use constant force of mortality

**Usage**

```
cfm(mu = 0.04, delta = log(1 + gl.g(i)), w = 1000)
```

**Arguments**

mu	the force of mortality
delta	the force of interest
w	the arbitrarily large limiting age

**Details**

To revert to makehams use makehams()

createInsuranceTable *Create Insurance Table***Description**

Creates a table containing EPV's of whole life insurances (discrete)

**Usage**

```
createInsuranceTable(x = gl.g(x), w = gl.g(w), d = gl.g(d), n = 5,  
  i = gl.g(i), mt = 1)
```

**Arguments**

x	the starting age
w	the limiting age
d	the select period
n	pure endowment period
i	the interest rate
mt	the moment t calculate

**Details**

Computes life table using recursion

---

createLifeTable	<i>Create Ultimate Select Life Table</i>
-----------------	--

---

### Description

Creates a life table based on the select period, radix and Makeham model parameters

### Usage

```
createLifeTable(x = gl.g(x), w = gl.g(w), radix = gl.g(radix),
  d = gl.g(d))
```

### Arguments

x	the starting age for the life table
w	the limiting age
radix	the number of individuals aged x
d	the select period

### Details

See Appendix Tables of DHW 2nd edition

---

demoivres	<i>Change Survival Model to DeMoivre's</i>
-----------	--

---

### Description

Change Survival Model to DeMoivre's

### Usage

```
demoivres(w = 100, delta = log(1 + gl.g(i)))
```

### Arguments

w	the limiting age
delta	the force of interest

### Details

Changes parameters and force of interest function to Uniform model

---

makehams	<i>Change Survival to Makeham's</i>
----------	-------------------------------------

---

**Description**

Change Survival to Makeham's

**Usage**

```
makehams(A = 0.00022, B = 2.7e-06, c = 1.124, d = 2, x = 20,
w = 131, radix = 1e+05, i = 0.05)
```

**Arguments**

A	model parameter
B	model parameter
c	model parameter
d	select period
x	the default age
w	the limiting age
radix	the number of starting individuals in life table
i	the effective annual interest rate

**Details**

Reverts the survival model back to Makeham's law with default parameters

---

tEx	<i>Actuarial Present Value Factor</i>
-----	---------------------------------------

---

**Description**

Calculates the Expected Present value of a pure endowment insurance

**Usage**

```
tEx(t, x = gl.g(x), s = 0, i = gl.g(i), mt = 1)
```

**Arguments**

t	the years from x
x	the current age
s	the select used so far
i	the interest rate
mt	the moment of the insurance

**Details**

Alternative actuarial "A" notation is also used for tEx

---

thV	<i>Benefit Reserve</i>
-----	------------------------

---

### Description

Uses Euler's method to solve Thiele's differential equation to approximate the value of  $t+hV$

### Usage

```
thV(t = 0, h = 1, x = gl.g(x), tV = 0, Pt = function(t) t^0 *
  gl.g(pi), deltat = function(t) t^0 * log(1 + gl.g(i)), bt = function(t)
  t^0, ut = function(t) uxt(t, x), s = 0.01)
```

### Arguments

t	the time for which the reserve is known
h	the the time from t for which the reserve should be calculated
x	the age of the person for which the reserve is being calculated
tV	the value of the reserve at time t
Pt	the premium as a function of t
deltat	the force of interest as a function of t
bt	the death benefit payable immediately at the time of death as a function of t
ut	the force of mortality as a function of t
s	the step to use in Euler's method

### Details

This function does not take into account expenses

---

tpx	<i>Survival Function</i>
-----	--------------------------

---

### Description

Probability that x survives t years given survival to age x

### Usage

```
tpx(t, x = gl.g(x), s = 0, uxt = gl.g(uxt))
```

### Arguments

t	the number of years to survive
x	the current age
s	select already used
uxt	the force of mortality (can be used to override the default force of mortality)

### Details

Uses a default select period of 2 (for makeham's law)

---

$tqx$	<i>CDF of Future Lifetime</i>
-------	-------------------------------

---

### Description

Probability that  $x$  dies in the next  $t$  years, given survival to age  $x$

### Usage

$tqx(t, x = gl.g(x), s = 0, uxt = gl.g(uxt))$

### Arguments

$t$	the number of years before death
$x$	the current age
$s$	select already used
$uxt$	the force of mortality (can be used to override the default force of mortality)

### Details

Calculated as  $1 - tpx(t, x)$

---

$udeferredtqx$	<i>Deferred CDF of Future Lifetime</i>
----------------	--

---

### Description

Probability of surviving  $u$  years and dying in the next  $t$  years

### Usage

$udeferredtqx(u, t = 1, x = gl.g(x), s = 0)$

### Arguments

$u$	the number of years to survive
$t$	the number of years to death within
$x$	the current age
$s$	the select used

### Details

Can be calculated by splitting the CDF. Use  $tpx(u, x) - tpx(u+t, x)$

---

uxt	<i>Force of Mortality</i>
-----	---------------------------

---

### Description

The select force of mortality,  $u[x]+s = 0.9^{(2-s)} u_{x+s}$  where the force of mortality is  $u_{x+s} = A + Bc^{(x+t)}$

### Usage

```
uxt(t, x = gl.g(x), s = 0, d = gl.g(d), A = gl.g(A), B = gl.g(B),
    c = gl.g(c))
```

### Arguments

t	the years after age x
x	the current age
s	select already used
d	the select period
A	Makeham model parameter
B	Makeham model parameter
c	Makeham model parameter

---

v	<i>Present Value Factor</i>
---	-----------------------------

---

### Description

Calculates the present value of a cash flow

### Usage

```
v(i = gl.g(i), n = 1, delta = log(1 + i))
```

### Arguments

i	the effective annual interest rate
n	the number of years to apply discounting
delta	the force of interest

### Details

The force of interest is internally derived from the effective annual interest rate



# Index

annx, [1](#)  
Ax, [2](#)  
  
cfm, [3](#)  
createInsuranceTable, [3](#)  
createLifeTable, [4](#)  
  
demoivres, [4](#)  
  
makehams, [5](#)  
  
tEx, [5](#)  
thV, [6](#)  
tpx, [6](#)  
tqx, [7](#)  
  
udeferredtx, [7](#)  
uxt, [8](#)  
  
v, [8](#)