# Model Creation and Validation for the Social Vulnerability Index Training Random Forest and Geographically Weighted Random Forest Models

Thesis for a Master of Public Health, Epidemiology

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## Statement of Purpose

The purpose of the file is to build two final models: a traditional random forest model (RF) and a geographically weighted random forest model (GWFRF). The following two sentence provide a overarching description of the two models. In a RF model, each tree in the forest is built from a different bootstrap sample of the training data, and at each node, a random subset of predictors (features) is considered for splitting, rather than the full set of predictors. A GWRF model expands on this concept by incorporating spatial information by weighting the training samples based on their geographic proximity to the prediction location. The splitting process in a RF model is determined by the mean squared error and in a GWRF is influenced by the spatial weights (i.e., weighted mean squared error), which adjust the contribution of each sample based on its geographic distance.

#### Overview of Hyperparameters Definitions

In James et al 2021, Ch 8.2.2 Random Forests, James et al 2023, Ch 15.2 Definition of Random Forests and Garson 2021, Ch 5 Random Forest, the hyperparameters that are shared between the traditional RF and the geographically-weighted RF models include:

- Number of randomly selected predictors: This is the number of predictors (p) considered for splitting at each node. It controls the diversity among the trees. A smaller m leads to greater diversity, while a larger m can make the trees more similar to each other.
  - for regression this defaults to p/3, where p is the total of predictor variables
- Number of trees: This is the total number of decision trees in the forest (m). More trees generally lead to a more stable and accurate model, but at the cost of increased computational resources and time.
  - for the randomForest::randomForest(), this defaults to 500

Additionally, GWRF involves an extra tuning spatial parameters:

• Bandwidth parameter: This controls the influence of spatial weights, determining how quickly the weight decreases with distance. A smaller bandwidth means only very close samples have significant influence, while a larger bandwidth allows more distant samples to also contribute to the model.

#### Outline of Hyper-parameter Tuning Process

4 RF models will be built, and they differ based on the different hyperparameters: (1) default settings, (2) first tune p, and subsequently tune, then m while keeping p constant, (3) simultaneously tune m and p with a grid search, (4) tuned with Out of Bag MSE Error Rates as described by Garson 2021. Two metrics will be implemented in the tuning process: Root Mean Squared Error and Out of Bag Error Rate.

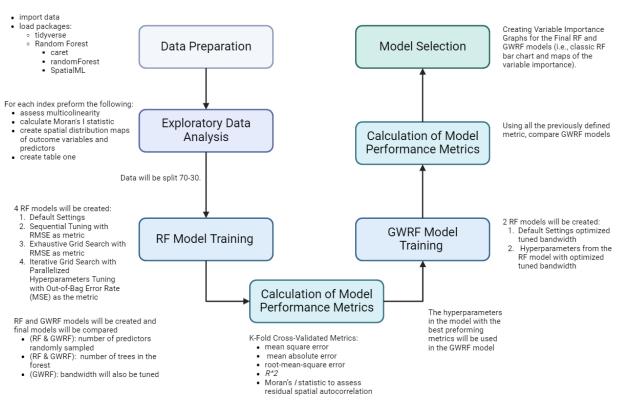
In Garson 2021, Ch 5 Random Forest, Garson teaches Random Forest Models by using randomForest::randomForest(), and in chapter 5.5.9 (pg. 267), he provides methods for tuning both of these parameters simultaneously using the Out of Bag MSE Error Rates. This value is a measure of the prediction error for data points that were not used in training each tree, and it can be written as OOB Error Rate =  $\frac{1}{n}\sum_{i=1}^{N}(y_i - \hat{y}_i^{\text{OOB}})^2$ .  $\hat{y}_i^{\text{OOB}}$  is the OOB prediction for the i-th observation, which is obtained by averaging the predictions from only those trees that did not include i in their bootstrap sample. To provide a high-level summary, since each tree in a Random Forest is trained on a bootstrap sample (a random sample with replacement) of the

data, approximately one-third of the data is not used for training each tree. This subset of data is referred to as the "out-of-bag" data for that tree, and this value is calculated using the data points that were not included in the bootstrap sample used to build each tree.

Georganos et al (2019) created the package(SpatialML), and subsequently the tuning is made possible by the SpatialML::grf.bw() function. The function uses an exhaustive approach (i.e., it tests sequential nearest neighbor bandwidths within a range and with a user defined step, and returns a list of goodness of fit statistics).

4 RF models will be built, and they differ based on the different hyperparameters: (1) default settings; (2) tuned by first tuning mtry, with ntrees set to default, and subsequently tuning then ntrees while keeping the newly defined mtry constant and both methods use RMSE as the metric; (3) tuned both mtry and ntrees with an Exhaustive Grid Search and both methods use RMSE as the metric, (4) tune tuned with Out of Bag MSE Error Rates as described by Garson 2021. For each model, MAE, MSE, RMSE, and  $R^2$  will be calculated and the hyperparameters of the best model will continue onto the GWRF. To provide points of comparison in the GWRF, two additional models will be created. Thus, two GWRF models will be created: (1) default mtry and ntrees with optimized bandwidth parameter, and (2) using the previously defined best hyperparameters. The same model evaluation metrics will be compared in addition to calculating the residual autocorrelation.

Lastly, the feature importance plots will be generated for the final, and local feature importance plots will also be created.



### Traditional Random Forest Model

#### Model Training and Hyperparameter Tuning

Models will be created and compared at the end of the section.

#### RF Model 1 - Default Settings

**Background**: The default settings for the RF model is mtry = p/3, and ntrees = 500, where p is the number of predictors.

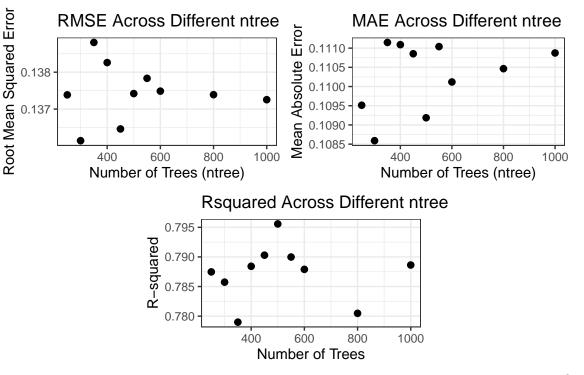
```
##
## Call:
## randomForest(x = x, y = y, ntree = 500, mtry = param$mtry, importance = TRUE)
## Type of random forest: regression
## Number of trees: 500
## No. of variables tried at each split: 5
##
## Mean of squared residuals: 0.01921465
## % Var explained: 77.13
```

#### RF Model 2 - Sequential Processing With RMSE Metric

**Background**: This model training process uses a combination of sequential processing and cross-validation. First, tuning the mtry parameter by using cross-validation to find the best value for each iteration. The model runs 10 times (i.e., the for loop) because given the nature of the building random forest models, the value of m within the loop changes. Therefore, preforming the function 10 times and taking the average of the most optimal mtry value it calculates and prints the average of the best *mtry* values. During the second step, the *ntree* is changing and cross-validated while *mtry* is held constant.

```
##
## Call:
## randomForest(x = x, y = y, ntree = 300, mtry = param$mtry, importance = TRUE)
## Type of random forest: regression
## Number of trees: 300
## No. of variables tried at each split: 6
##
## Mean of squared residuals: 0.01867418
## % Var explained: 77.78
```

The following graph illustrates preformance metrics across different values of *ntree*, and the selection for the final *ntree* value stems from having the lowest RMSE/MAE and the highest R-Squared Value.



mtry = 6

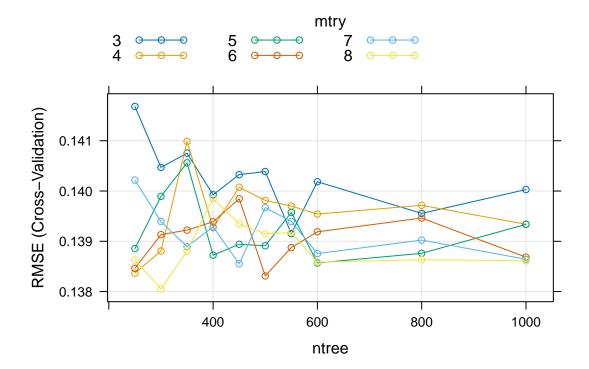
The second model hyperparameters have been set to mtry = 6, and ntrees = 300.

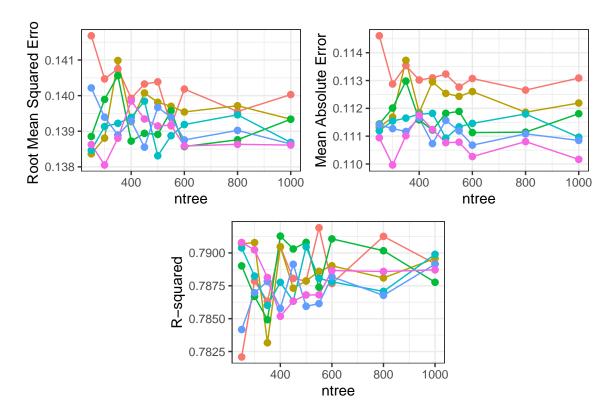
#### Model 3 - Exhaustive Grid Search with RMSE as Metric

**Background**: To preform an exhaustive Grid Search, Brownlee (2020) created a custom function that preforms the grid search. This function checks every combination of *mtry* and *ntree* values determines the final values with RMSE.

```
##
## Call:
## randomForest(x = x, y = y, ntree = param$ntree, mtry = param$mtry, importance = TRUE)
## Type of random forest: regression
## Number of trees: 300
## No. of variables tried at each split: 8
##
## Mean of squared residuals: 0.01880437
## % Var explained: 77.62
```

The following graph illustrates preformance metrics across different values of *ntree*, and the selection for the final *ntree* value stems from having the lowest RMSE/MAE and the highest R-Squared Value.





The final values used for the model were mtry = 8 and ntree = 300. Note that the variation between each of the combinations is minimal.

#### Model 4

This code snippet is designed to optimize the hyperparameters *mtry* and *ntree* in a Random Forest model and by examining the OOB MSE across these combinations, the code identifies which parameters yield the lowest error, helping to optimize the Random Forest model. Here's how the code meets this objective:

- Iterative Search for *mtry*: The mtry\_iter function generates an iterable sequence of *mtry* values, starting from 1 up to the number of predictors, incremented by a step factor. This allows the code to explore different numbers of predictors used at each split in the trees.
- Specification of *ntree* Values: A predefined vector *vntree* contains different values for the number of trees to be grown in the forest. This allows the code to assess how the number of trees impacts the model performance.
- Error Calculation Across Hyperparameter Combinations: The tune function performs a grid search over the specified *mtry* values and the maximum number of trees specified in *vntree*. For each combination, the function trains a Random Forest model and calculates the OOB error rate (MSE if y is continuous).
- Parallel Processing: The foreach loop with the .dopar argument allows for parallel execution of the grid search, which speeds up the computation.
- Result Aggregation: The results are combined into a data frame, which can then be analyzed to identify the optimal combination of *mtry* and *ntree* that minimizes the OOB error rate.

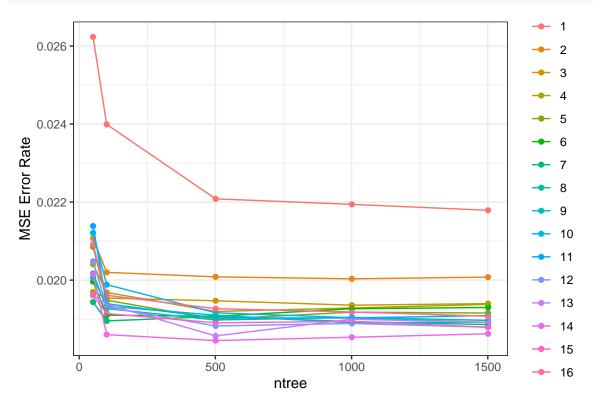
```
#####################
##### RF Mod 4 #####
####################
# create an interaction function to search over different values of mtry
mtry_iter = function(from, to, stepFactor = 1.05){
 nextEl = function(){
    if (from > to) stop('StopIteration')
    i = from
    from <<- ceiling(from * stepFactor)</pre>
    i
  obj = list(nextElem = nextEl)
  class(obj) = c('abstractiter', 'iter')
  obj
}
# create a vector of ntree values of interest
vntree = c(51, 101, 501, 1001, 1501)
# specify the predictor (x) and outcome (y) object
x = df %>% select(starts_with("e_")) %>% st_drop_geometry()
y = df %>% pull(rpl_themes)
# Create a function to get random forest error information for different mtry values
tune = function(x, y, ntree = vntree, mtry = NULL, keep.forest = FALSE, ...) {
```

```
# Define the combination function to aggregate results
  comb = function(a, b) {
    if (is.null(a)) return(b)
   rbind(a, b)
 results = foreach(mtry = mtry_iter(1, ncol(x)), .combine = comb, .packages = 'randomForest')
    model = randomForest::randomForest(x, y, ntree = max(ntree), mtry = mtry, keep.forest = FA
    if (is.factor(y)) {
     errors = data.frame(ntree = ntree, mtry = mtry, error = model$err.rate[ntree, 1])
     errors = data.frame(ntree = ntree, mtry = mtry, error = model$mse[ntree])
   return(errors)
 return(results)
}
# running the tuning
results = tune(x,y) %>%
 mutate(MSE = error) %>%
  select(-error)
# examinations of other hyperparameters
# table
temp = results %>%
  arrange(MSE) %>%
 head()
kable(temp, caption = "Model 4 Preformance Metrics", digits = 4, align = c("l", "l", "c"))
```

Table 1: Model 4 Preformance Metrics

ntree	mtry	MSE
501	14	0.0184
1001	14	0.0185
501	13	0.0186
101	14	0.0186
1501	14	0.0186
1501	12	0.0188

## labs(color = "mtry", y = "MSE Error Rate")



```
best_mtry = temp$mtry[[1]]
best_ntree = temp$ntree[[1]]
# creating the first model
rf_mod4 = train(rpl_themes ~.,
                 data = df,
                 method = "rf",
                 trControl = trainControl(method = "cv", number = 10),
                 tuneGrid = expand.grid(mtry = best_mtry),
                 ntree = best_ntree,
                 importance = TRUE)
# Print the results
rf_mod4$finalModel
##
## Call:
##
    randomForest(x = x, y = y, ntree = ..1, mtry = param$mtry, importance = TRUE)
##
                  Type of random forest: regression
##
                        Number of trees: 501
## No. of variables tried at each split: 14
             Mean of squared residuals: 0.01908644
##
```

% Var explained: 77.29

##

The final model hyperparameters have been set to mtry = 14, and ntrees = 501. The graph below illustrates that the errors across the hyperparameters used with this method are very similar.

### **RF** Model Evaluation

Despite variations in the m and ntrees parameters across different models, the overall prediction performance remains consistent. The relatively low MSE and RMSE values across the models indicate that the predictions are generally close to the actual values. The high R-Squared values suggest that each model explains a significant portion of the variance in the target variable. However, since model 4 produced code that is lowest MSE and RMSE, and highest R-squared value, these are the parameters that will be head contains for the GWRF.

• Mean Absolute Error (MAE):  $\frac{1}{n}\sum_{i=1}^{n}|y_i-\hat{y}_i|$ • Mean Squared Error (MSE):  $\frac{1}{n}\sum_{i=1}^{n}(y_i-\hat{y}_i)^2$ • Root Mean Squared Error (RMSE):  $\sqrt{\frac{1}{n}\sum_{i=1}^{n}(y_i-\hat{y}_i)^2}$ 

• R-Squared Value:  $\frac{\Sigma(y-\hat{y})^2}{\Sigma(y-\bar{y})^2}$ 

Table 2: Performance Metrics for Each Model

Model	$\operatorname{mtry}$	ntree	MAE	RMSE	$R\_Squared$
Model 1	5	500	0.111	0.139	0.790
Model 2	6	550	0.112	0.138	0.789
Model 3	8	540	0.112	0.139	0.788
Model 4	14	501	0.108	0.138	0.789

## Training a Geographically Weighted Random Forest Model

#### GWRF Model 1

This model has hyperparameters defined with mtry and trees by the default, and optimized bandwith.

```
## Ranger result
##
## Call:
## ranger(rpl_themes ~ e_pov150 + e_unemp + e_hburd + e_nohsdp +
                                                                         e_uninsur + e_age65 + e
##
## Type:
                                      Regression
## Number of trees:
                                      500
## Sample size:
                                      246
## Number of independent variables:
                                      16
## Mtry:
                                      5
## Target node size:
                                      5
## Variable importance mode:
                                      impurity
## Splitrule:
                                      variance
## 00B prediction error (MSE):
                                      0.01898519
## R squared (00B):
                                      0.774974
     e pov150
                 e_unemp
                             e hburd
                                       e_nohsdp e_uninsur
                                                               e_age65
                                                                          e_age17
## 3.11886904 0.35103129 0.72168143 1.52655612 0.44640200 1.05723955 0.50747560
##
     e_disabl
                e_sngpnt
                            e_limeng
                                       e_minrty
                                                   e_{munit}
                                                              e_mobile
## 0.28549567 0.48836060 3.30680893 2.50852329 0.96675258 0.09114209 1.31459441
##
      e_noveh
                e_groupq
## 3.25499941 0.30207710
                                              3rd Qu.
##
        Min.
               1st Qu.
                          Median
                                       Mean
                                                            Max.
## -0.407359 -0.109665 -0.005041 -0.006256
                                            0.096517
                                                       0.501859
                 1st Qu.
                              Median
                                           Mean
                                                   3rd Qu.
                                                             0.0614741
## -0.0457386 -0.0068265 0.0000491 0.0009267
                                                 0.0079773
##
                     Min
                                 Max
                                           Mean
                                                        StD
## e pov150 0.046156835 0.88564486 0.33982742 0.16187352
## e_unemp
             0.014877945 \ 0.31376208 \ 0.08115051 \ 0.04731030
## e hburd
             0.021651832 0.66255123 0.16761710 0.12182127
## e_nohsdp
             0.038328814\ 1.14256174\ 0.25038711\ 0.20982340
## e uninsur 0.020891089 0.22493313 0.07990350 0.04257707
## e_age65
             0.014934781 \ 0.79831976 \ 0.14149547 \ 0.18942335
## e_age17
             0.015950759\ 0.24873496\ 0.07811220\ 0.04815336
## e_disabl
             0.021494108 0.49258775 0.07935985 0.05388009
             0.020125384 0.52719856 0.11282993 0.08591079
## e_sngpnt
## e_limeng
             0.017820815 1.13352793 0.28145306 0.19524155
## e_minrty
             0.028178321 0.89391507 0.22791211 0.18023411
## e_munit
             0.016766064 \ 0.94984198 \ 0.20420939 \ 0.18799483
## e_mobile
             0.001055735 0.07820255 0.01465081 0.01209504
## e_crowd
             0.019229361 \ 0.91334070 \ 0.20558264 \ 0.14672485
## e_noveh
             0.054622095 \ 0.88894292 \ 0.35680150 \ 0.20188076
## e groupq
             0.021167695 0.18541030 0.06335931 0.02737005
```

The final model hyperparameters have been set to  $bandwidth=49,\ mtry=5,\ and\ ntrees=500.$ 

#### GWRF Model 2

This model has hyperparameters defined with mtry and trees by the default, and optimized bandwith.

```
## Ranger result
##
## Call:
   ranger(rpl_themes ~ e_pov150 + e_unemp + e_hburd + e_nohsdp +
                                                                        e_uninsur + e_age65 + e
##
                                      Regression
## Type:
## Number of trees:
                                      501
## Sample size:
                                      246
## Number of independent variables:
                                      16
## Mtry:
                                      14
## Target node size:
                                      5
## Variable importance mode:
                                      impurity
## Splitrule:
                                      variance
## 00B prediction error (MSE):
                                      0.01883109
## R squared (00B):
                                      0.7768005
     e_pov150
##
                                       e_nohsdp e_uninsur
                                                              e_age65
                 e_unemp
                            e_hburd
                                                                          e_age17
## 4.10081279 0.31785849 0.31273405 0.88710876 0.30684484 1.15957328 0.47339192
     e_disabl
                e_sngpnt
                           e_limeng
                                       e_minrty
                                                   e_munit
                                                             e_mobile
                                                                          e_crowd
## 0.25058089 0.30080880 5.31853956 1.33509068 1.08804794 0.09666911 0.84673178
##
      e_noveh
                e_groupq
## 3.32078161 0.24738591
##
         Min.
                 1st Qu.
                             Median
                                           Mean
                                                   3rd Qu.
                                                                 Max.
## -0.4601121 -0.1193271 -0.0009903 -0.0062199
                                                 0.1036436
                                                            0.4871807
##
         Min.
                 1st Qu.
                                                   3rd Qu.
                             Median
                                           Mean
                                                                 Max.
## -0.0546891 -0.0064796 -0.0001545
                                     0.0005713
                                                 0.0066960
                                                            0.0579278
##
                                 Max
                                             Mean
             0.0134565521 1.08182924 0.319395820 0.22224044
## e_pov150
## e_unemp
             0.0047098959 0.31425217 0.053719871 0.04439710
## e_hburd
             0.0077887639 1.12829917 0.134592860 0.18749551
## e nohsdp
             0.0192541366 2.37289162 0.304738276 0.43303174
## e_uninsur 0.0100748366 0.20525875 0.052836979 0.04051624
## e age65
             0.0043546796 1.50395820 0.160254345 0.29791113
## e_age17
             0.0067403201 0.34369630 0.057245864 0.06093593
## e_disabl
             0.0077638674 0.38294912 0.037217133 0.03840158
## e_sngpnt
             0.0064697490 0.75923053 0.086742849 0.11356979
## e_limeng
             0.0080110778 2.47321868 0.261771262 0.29669757
## e_minrty
             0.0091052206 1.30925511 0.207884201 0.24281671
## e_munit
             0.0119653092 1.67699261 0.245406399 0.33357410
## e_mobile
             0.0002019652 0.07982328 0.009813122 0.01180187
## e_crowd
             0.0093362544 1.62490074 0.192861641 0.24326663
## e noveh
             0.0152481131 1.60799589 0.398805303 0.36846838
## e_groupq 0.0071932965 0.24371320 0.045329541 0.03001460
```

The final model hyperparameters have been set to bandwidth = 47, mtry = 14, and ntrees = 501.

## **GWRF** Model Evaluation

The models both preform nearly identically because the hyperparameters preform nearly identically. Therefore, the model define by the previous traditional random forest model.

Table 3: Performance Metrics for Each Model

Model	bw	mtry	ntree	MAE	RMSE	R_Squared
Model 5	49	5	500	0.110	0.138	0.774
Model 6	47	9	501	0.108	0.137	0.776

## Random Forest Model Comparisons

Model 4 shows a lower MAE and MSE, indicating that it generally makes smaller errors in prediction. The RMSE is also relatively low, and the high  $R^2$  value (0.791) suggests that this model explains a significant portion of the variance in the SVI. Overall, Model 4 performs well and is effective in predicting SVI using the selected predictors.

Model 6 has higher MAE and MSE values, indicating that it makes larger errors on average compared to Model 4. The RMSE is also higher, and the  $R^2$  is lower (0.638), suggesting that Model 6 explains less variance in the SVI. This could mean that while the Geographically Weighted Random Forest accounts for spatial autocorrelation, it may not perform as well in terms of overall prediction accuracy as the traditional Random Forest.

Model 4 (Traditional Random Forest) outperforms Model 6 (Geographically Weighted Random Forest) in terms of accuracy and explained variance. However, Model 6 is still valuable because it accounts for spatial dependencies. Model 6 might be more appropriate despite its lower overall performance metrics, particularly if the goal is to understand regional variations in the SVI. However, if the focus is purely on predictive accuracy, Model 4 appears to be the better choice.

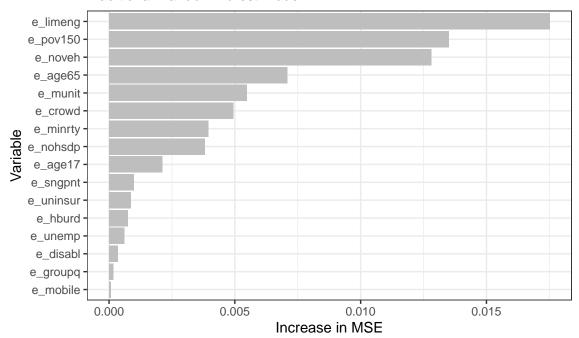
Table 4: Performance Metrics for Each Model

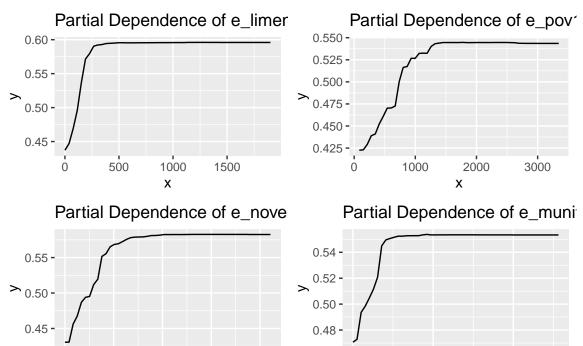
	Model	bw	mtry	ntree	MAE	RMSE	R_Squared
4	Model 4	-	14	501	0.108	0.138	0.789
2	Model 6	47	9	501	0.108	0.137	0.776

## Graphs for the Final Models

#### **Traditional Random Forest**

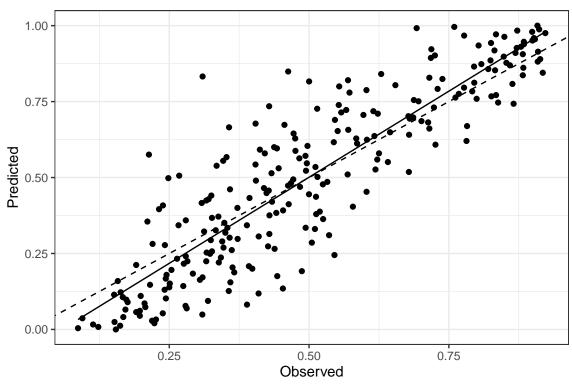
# Variable Importance (Increase in %IncMSE) Traditional Random Forest Model

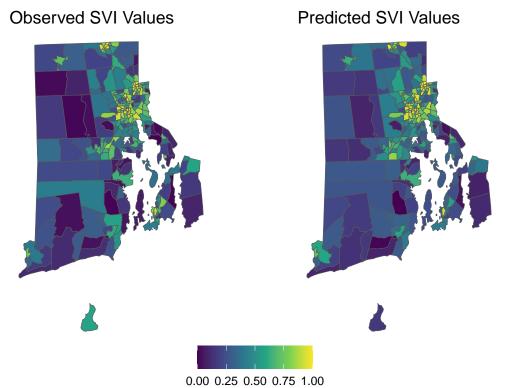




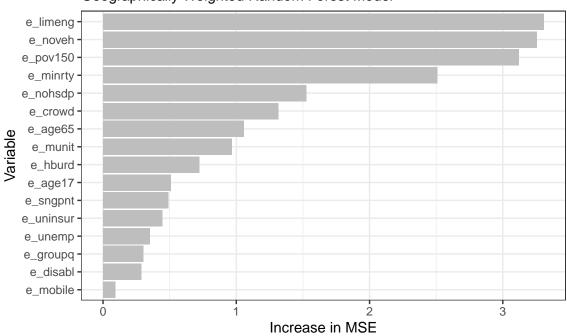
Χ

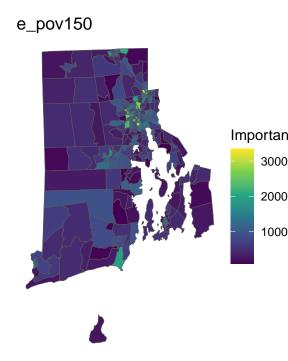
## Geographically Weighted Random Forest



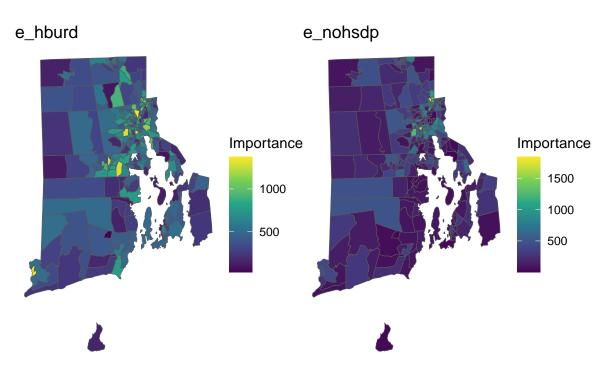


## Variable Importance (Increase in %IncMSE) Geographically Weighted Random Forest Model

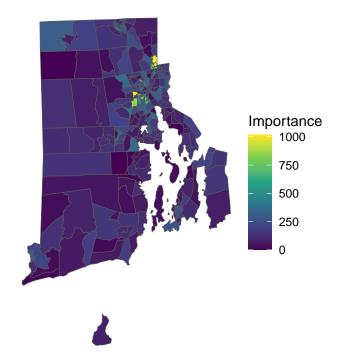


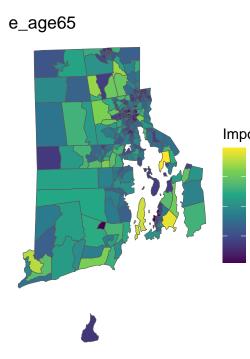


## ${\bf Local\ Variable\ Importance\ of\ SocioEconomic\ Status\ Variables}$

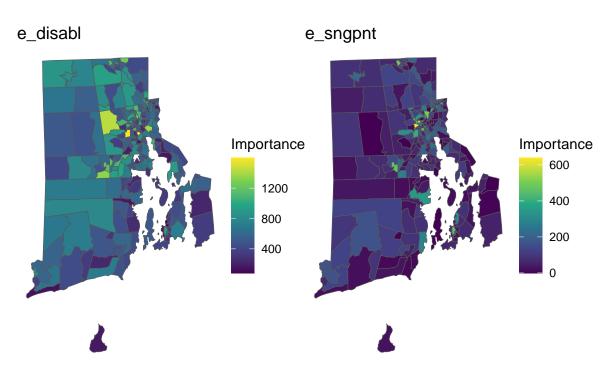


# e\_uninsur

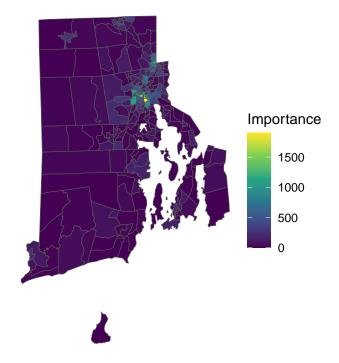




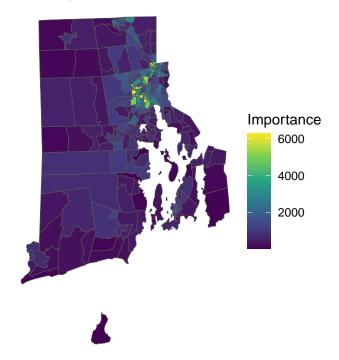
## ${\bf Local\ Variable\ Importance\ of\ Household\ Characteristics\ Variables}$

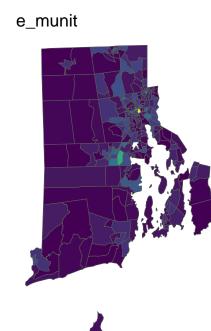


# e\_limeng

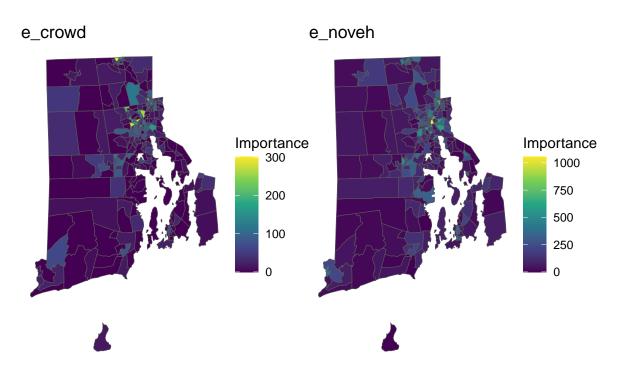


Local Variable Importance of Racial & Ethnic Minority Status Variables e\_minrty

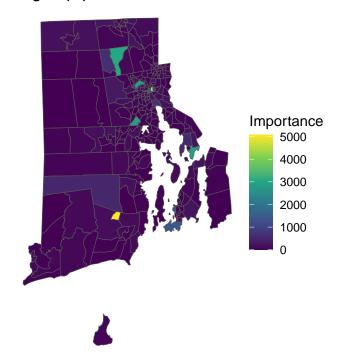




## Local Variable Importance of Housing Type & Transportation Variables



### e\_groupq



## Code Appendix

```
knitr::opts_chunk$set(warning = FALSE, message = FALSE, echo = FALSE)
knitr::opts_chunk$set(fig.width=6, fig.height=4)
options(tigris_use_cache = TRUE)
options(repos = c(CRAN = "https://cran.r-project.org"))
#####################
#### Preparation ####
#############################
### importing packages
# define desired packages
library(tidyverse)
                      # general data manipulation
library(knitr)
                      # Rmarkdown interactions
library(here)
                      # define top level of project folder
                          # this allows for specification of where
                          # things live in relation to the top level
library(foreach)
                      # parallel execution
# spatial tasks
library(tigris)
                      # obtain shp files
library(spdep)
                      # exploratory spatial data analysis
# random forest
library(caret)
                      # machine learning model training
library(rsample)
                      # splitting testing/training data
```

```
library(randomForest) # traditional RF model
library(SpatialML)
                     # spatial RF model
# others
library(foreach)
                     # parrallel processing
library(ggpubr)
                      # arrange multiple graphs
### setting seed
set.seed(926)
### loading data
svi_df = read_csv(here::here("01_Data", "svi_df.csv")) %>%
 mutate(fips = as.character(fips)) %>%
  select(-...1)
### obtaining SPH files for RI tracts
tracts = tracts(state = "RI", year = 2022, cb = TRUE)
### joining data
svi_df = inner_join(tracts, svi_df, by = c("GEOID" = "fips"))
### defining analytical coordinates and df
df_coords = svi_df %>%
 mutate(
    # redefines geometry to be the centroid of the polygon
    geometry = st_centroid(geometry),
    # pulls the lon and lat for the centroid
   lon = map_dbl(geometry, ~st_point_on_surface(.x)[[1]]),
   lat = map_dbl(geometry, ~st_point_on_surface(.x)[[2]])) %>%
  # removes geometry, coerce to data.frame
  st_drop_geometry() %>%
  # only select the lon and lat
  select(lon, lat)
# only obtain response and predictor variables
df = svi_df %>%
 st_drop_geometry() %>%
  select(rpl_themes, starts_with("e_"))
####################
##### RF Mod 1 #####
#####################
### setting seed
set.seed(926)
# obtain the number of predictors
pred_num = svi_df %>%
  st_drop_geometry() %>%
```

```
select(starts_with("e_")) %>%
  colnames() %>%
  length()
# determine the default number of predictors
mtry = round(pred_num / 3)
# creating the first model
rf_mod1 = train(rpl_themes ~.,
                 data = df,
                 method = "rf",
                 trControl = trainControl(method = "cv", number = 10),
                 tuneGrid = expand.grid(mtry = mtry),
                 ntree = 500,
                 importance = TRUE)
# Print the results
rf mod1$finalModel
####################
##### RF Mod 2 #####
####################
### setting seed
set.seed(926)
### Step 1: Find the best `mtry` value
# Create an empty list to store the results
results_list = vector("list", 10)
# Loop to repeat the code 10 times
for (i in 1:10) {
  # Train the random forest model with 10-fold cross-validation
  rf_mod2 = train(rpl_themes ~ ., data = df, method = "rf",
                  ntree = 500, # Start with a default number of trees
                  trControl = trainControl(method = "cv", number = 10),
                  tuneGrid = expand.grid(mtry = c(3:8)))
  # print model results
  # print(rf_mod2)
  plot(rf_mod2)
  # Extract the best number of predictors (mtry) from the model
  m = rf_mod2$bestTune$mtry
  # Store the result in the list
  results_list[[i]] = m
}
mean_mtry = round(mean(unlist(results_list)))
```

```
# Step 2: Find the best `ntree` value using cross-validation with the optimal `mtry`
store_maxtrees = list()
ntree_values = c(250, 300, 350, 400, 450, 500, 550, 600, 800, 1000) # List of `ntree` values t
for (ntree in ntree_values) {
    rf_maxtrees = train(rpl_themes ~ ., data = df, method = "rf",
                        tuneGrid = expand.grid(mtry = mean_mtry), # Use the fixed best `mtry`
                        trControl = trainControl(method = "cv", number = 10),
                        ntree = ntree)
    # print model results
    # print(rf_maxtrees)
    store_maxtrees[[as.character(ntree)]] <- rf_maxtrees</pre>
}
# 500 subjectively made
# summary(resamples(store_maxtrees))
# creating the first model
rf_mod2 = train(rpl_themes ~.,
                 data = df,
                 method = "rf",
                 trControl = trainControl(method = "cv", number = 10),
                 tuneGrid = expand.grid(mtry = mean_mtry),
                 ntree = 300,
                 importance = TRUE)
# Print the results
rf_mod2$finalModel
# Initialize an empty data frame to store all metrics
metrics_df <- data.frame()</pre>
# Loop through each model in store_maxtrees
for (ntree in names(store_maxtrees)) {
 model <- store_maxtrees[[ntree]]</pre>
  # Extract metrics for the current model
 model_metrics <- data.frame(</pre>
   ntree = as.numeric(ntree),
                                                 # Capture the ntree value
   RMSE = model$results$RMSE,
                                                # Extract RMSE
    MAE = model$results$MAE,
                                                # Extract MAE
   Rsquared = model$results$Rsquared,
                                                # Extract Rsquared
                                                 # Capture the mtry value
   mtry = model$bestTune$mtry
  )
  # Append the metrics to the main data frame
 metrics_df <- rbind(metrics_df, model_metrics)</pre>
```

```
}
# Create the line graph
a=ggplot(metrics_df, aes(x = ntree, y = RMSE)) +
  geom_point(size = 2) +
  labs(title = "RMSE Across Different ntree",
       x = "Number of Trees (ntree)",
       y = "Root Mean Squared Error",
       shape = "ntree") +
  theme_bw()
b=ggplot(metrics_df, aes(x = ntree, y = MAE)) +
  geom_point(size = 2) +
  labs(title = "MAE Across Different ntree",
       x = "Number of Trees (ntree)",
       y = "Mean Absolute Error",
       shape = "ntree") +
  theme_bw()
c=ggplot(metrics_df, aes(x = ntree, y = Rsquared)) +
  geom_point(size = 2) +
  labs(title = "Rsquared Across Different ntree",
       x = "Number of Trees",
       y = "R-squared",
       shape = "ntree") +
  theme_bw()
blank = ggplot() + theme_void()
fig = ggarrange(
    ggarrange(a, b, blank, nrow = 1,
        widths = c(1, 1, 0), legend = "none"),
    ggarrange(blank, c, blank, nrow = 1,
        widths = c(0.5, 1, 0.5), legend = "none"),
    nrow = 2,
    legend = "none"
)
annotate_figure(fig, bottom = text_grob("mtry = 6", hjust = 1, x = 1))
#####################
##### RF Mod 3 #####
#####################
### setting seed
set.seed(926)
```

```
# Define the tuned parameter
grid = expand.grid(.mtry = c(3:8),
                    .ntree = c(250, 300, 350, 400, 450, 500, 550, 600, 800, 1000))
ctrl = trainControl(method = "cv", number = 10)
# create custom
customRF <- list(type = "Regression", library = "randomForest", loop = NULL)</pre>
customRF$parameters <- data.frame(parameter = c("mtry", "ntree"), class = rep("numeric", 2), 1</pre>
customRF$grid <- function(x, y, len = NULL, search = "grid") {}</pre>
customRF$fit <- function(x, y, wts, param, lev, last, weights, classProbs, ...) {</pre>
  randomForest(x, y, mtry = param$mtry, ntree=param$ntree, ...)
customRF$predict <- function(modelFit, newdata, preProc = NULL, submodels = NULL)</pre>
   predict(modelFit, newdata)
customRF$prob <- function(modelFit, newdata, preProc = NULL, submodels = NULL)</pre>
   predict(modelFit, newdata, type = "prob")
customRF$sort <- function(x) x[order(x[,1]),]</pre>
customRF$levels <- function(x) x$classes</pre>
# creating the first model
rf_mod3 = train(rpl_themes ~.,
                 data = df,
                 method = customRF,
                 trControl = ctrl,
                 tuneGrid = grid,
                 importance = TRUE)
# Print the results
rf_mod3$finalModel
plot(rf_mod3)
metrics_df = as.data.frame(rf_mod3$results)
# Create the line graph
a = ggplot(metrics_df, aes(x = ntree, y = RMSE, color = as.factor(mtry))) +
  geom_line() +
  geom point(size = 2) +
  labs(y = "Root Mean Squared Error") +
  theme bw()
b = ggplot(metrics_df, aes(x = ntree, y = MAE, color = as.factor(mtry))) +
  geom_line() +
  geom_point(size = 2) +
  labs(y = "Mean Absolute Error") +
  theme_bw()
```

```
c = ggplot(metrics_df, aes(x = ntree, y = Rsquared, color = as.factor(mtry))) +
  geom line() +
  geom point(size = 2) +
  labs(y = "R-squared") +
  theme bw()
fig = ggarrange(
    ggarrange(a, b, blank, nrow = 1,
        widths = c(1, 1, 0), legend = "none"),
    ggarrange(blank, c, blank, nrow = 1,
        widths = c(0.5, 1, 0.5), legend = "none"),
    nrow = 2,
    legend = "none"
annotate_figure(fig)
####################
##### RF Mod 4 #####
####################
# create an interaction function to search over different values of mtry
mtry_iter = function(from, to, stepFactor = 1.05){
  nextEl = function(){
    if (from > to) stop('StopIteration')
    i = from
    from <<- ceiling(from * stepFactor)</pre>
    i
  obj = list(nextElem = nextEl)
  class(obj) = c('abstractiter', 'iter')
  obj
}
# create a vector of ntree values of interest
vntree = c(51, 101, 501, 1001, 1501)
# specify the predictor (x) and outcome (y) object
x = df %>% select(starts_with("e_")) %>% st_drop_geometry()
y = df %>% pull(rpl_themes)
# Create a function to get random forest error information for different mtry values
tune = function(x, y, ntree = vntree, mtry = NULL, keep.forest = FALSE, ...) {
  # Define the combination function to aggregate results
  comb = function(a, b) {
    if (is.null(a)) return(b)
    rbind(a, b)
```

```
results = foreach(mtry = mtry_iter(1, ncol(x)), .combine = comb, .packages = 'randomForest')
    model = randomForest::randomForest(x, y, ntree = max(ntree), mtry = mtry, keep.forest = FA
    if (is.factor(y)) {
      errors = data.frame(ntree = ntree, mtry = mtry, error = model$err.rate[ntree, 1])
    } else {
      errors = data.frame(ntree = ntree, mtry = mtry, error = model$mse[ntree])
    return(errors)
  }
  return(results)
}
# running the tuning
results = tune(x,y) %>%
  mutate(MSE = error) %>%
  select(-error)
# examinations of other hyperparameters
# table
temp = results %>%
  arrange(MSE) %>%
 head()
kable(temp, caption = "Model 4 Preformance Metrics", digits = 4, align = c("l", "l", "c"))
# plot
ggplot(results, aes(y = MSE, x = ntree,
                    color = as.factor(mtry))) +
  geom_point() +
  geom_line() +
  theme_bw() +
  labs(color = "mtry", y = "MSE Error Rate")
best_mtry = temp$mtry[[1]]
best_ntree = temp$ntree[[1]]
# creating the first model
rf_mod4 = train(rpl_themes ~.,
                 data = df,
                 method = "rf",
                 trControl = trainControl(method = "cv", number = 10),
                 tuneGrid = expand.grid(mtry = best_mtry),
                 ntree = best_ntree,
                 importance = TRUE)
# Print the results
rf_mod4$finalModel
```

```
#####################
##### RF Models ####
####################
# Create a data frame with the results
results_rf = data.frame(
 Model = c("Model 1", "Model 2", "Model 3", "Model 4"),
 mtry = c(rf_mod1$results$mtry,
           rf_mod2$results$mtry,
           rf mod3$bestTune[[1]],
           rf mod4$results$mtry),
 ntree = c(500, 550, 540, 501),
 MAE = c(rf_mod1$results$MAE,
           rf_mod2$results$MAE,
           mean(rf_mod3$results$MAE),
           rf_mod4$results$MAE),
 RMSE = c(rf_mod1$results$RMSE,
           rf_mod2$results$RMSE,
           mean(rf_mod3$results$RMSE),
           rf_mod4$results$RMSE),
  R_Squared = c(rf_mod1$results$Rsquared,
           rf_mod2$results$Rsquared,
           mean(rf mod3$results$Rsquared),
           rf_mod4$results$Rsquared))
# Print the results using kable
kable(results rf, caption = "Performance Metrics for Each Model",
      digits = 3, align = c("l", "c", "c", "c", "c", "c", "c"))
####################
#### GWRF Mod 1 ####
####################
# testing for optimal bandwidth
temp = SpatialML::grf.bw(rpl_themes ~ e_pov150 + e_unemp + e_hburd + e_nohsdp +
                               e_uninsur + e_age65 + e_age17 + e_disabl +
                               e_sngpnt + e_limeng + e_minrty + e_munit +
                               e_mobile + e_crowd + e_noveh + e_groupq,
                             dataset = df,
                             kernel = "adaptive",
                             bw.min = 20,
                             bw.max = 50,
                             coords = df_coords,
                             trees = 500,
                             mtry = mtry,
                             step = 1, importance = "impurity")
best.bw_gwrf_mod1 = temp$Best.BW
```

```
# defining the spatial model with prior model hyparameters
gwrf_mod1 = SpatialML::grf(rpl_themes ~ e_pov150 + e_unemp + e_hburd + e_nohsdp +
                           e_uninsur + e_age65 + e_age17 + e_disabl +
                           e_sngpnt + e_limeng + e_minrty + e_munit +
                           e_mobile + e_crowd + e_noveh + e_groupq,
                         dframe = df,
                         kernel = "adaptive",
                         coords = df_coords,
                         bw = best.bw_gwrf_mod1,
                         ntree = 500,
                         mtry = mtry,
                         importance = "impurity")
####################
#### GWRF Mod 2 ####
####################
# testing for optimal bandwidth
temp = SpatialML::grf.bw(rpl_themes ~ e_pov150 + e_unemp + e_hburd + e_nohsdp +
                               e_uninsur + e_age65 + e_age17 + e_disabl +
                               e_sngpnt + e_limeng + e_minrty + e_munit +
                               e_mobile + e_crowd + e_noveh + e_groupq,
                             dataset = df,
                             kernel = "adaptive",
                             bw.min = 20,
                             bw.max = 50,
                             coords = df coords,
                             trees = best_ntree,
                             mtry = rf_mod4$results$mtry,
                             step = 1)
best.bw_gwrf_mod2 = temp$Best.BW
# defining the spatial model with prior model hyparameters
gwrf_mod2 = SpatialML::grf(rpl_themes ~ e_pov150 + e_unemp + e_hburd + e_nohsdp +
                           e_uninsur + e_age65 + e_age17 + e_disabl +
                           e_sngpnt + e_limeng + e_minrty + e_munit +
                           e_mobile + e_crowd + e_noveh + e_groupq,
                         dframe = df,
                         kernel = "adaptive",
                         coords = df_coords,
                         bw = best.bw_gwrf_mod2,
                         ntree = best_ntree,
                         mtry = rf_mod4$results$mtry,
                         importance.mode = "impurity") # this is a ranger argument
                                                        # specification of this value
                                                        # corrected errors that previously appe
```

```
# no importance value specified
####################
#### GWRF Models ###
#####################
# Model 5
predictions5 = gwrf_mod1$Global.Model$predictions
mse5 = mean((df$rpl_themes - predictions5)^2)
rmse5 = sqrt(mse5)
mae5 = sum(abs(df$rpl_themes - predictions5))/length(predictions5)
r_squared5 = 1 - sum((df$rpl_themes - predictions5)^2) / sum((df$rpl_themes - mean(df$rpl_themes
# Model 6
predictions6 = gwrf_mod2$Global.Model$predictions
mse6 = mean((df$rpl_themes - predictions6)^2)
rmse6 = sqrt(mse6)
mae6 = sum(abs(df$rpl_themes - predictions6))/length(predictions6)
r_squared6 = 1 - sum((df$rpl_themes - predictions6)^2) / sum((df$rpl_themes - mean(df$rpl_themes
# Create a data frame with the results
results_grf = data.frame(
  Model = c("Model 5", "Model 6"),
  bw = c(best.bw_gwrf_mod1, best.bw_gwrf_mod2),
 mtry = c(5, 9),
 ntree = c(500, 501),
 MAE = c(mae5, mae6),
 RMSE = c(rmse5, rmse6),
  R_Squared = c(r_squared5, r_squared6)
# Print the results using kable
kable(results_grf, caption = "Performance Metrics for Each Model",
      digits = 3, align = c("l", "c", "c", "c", "c", "c", "c"))
#####################
#### All Models ####
#####################
final_results = results_rf[4,] %>%
  mutate(bw = "-") %>%
  select(Model, bw, mtry, ntree, MAE, RMSE, R_Squared)
final_results = rbind(final_results, results_grf[2,])
# Print the results using kable
kable(final_results, caption = "Performance Metrics for Each Model",
      digits = 3, align = c("l", "r", "r", "r", "r", "r", "r"))
###################
#### RF Results ####
```

```
#####################
df = df \%
  mutate(rf_pred = as.data.frame(rf_mod4$finalModel$predicted)[[1]])
# Predicted 1:1 Plot
\#ggplot(df, aes(x = rf_pred, y = rpl_themes)) +
# geom point() +
# theme_bw() +
# geom abline(slope=1, intercept=0, linetype="dashed", size=0.5) +
# geom smooth(method = "lm", se = FALSE, colour="black", size=0.5) +
# labs(x="Observed", y = "Predicted")
# Variable Importance
temp = as.data.frame(rf_mod4$finalModel$importance)
colnames(temp) = c("IncMSE", "IncNodePurity")
temp = tibble::rownames_to_column(temp, "Variable")
ggplot(temp, aes(x = fct_reorder(Variable, IncMSE), y = IncMSE)) +
  geom_bar(stat = "identity", fill = "grey") +
  coord_flip() + # Flip coordinates for better readability
  labs(title = "Variable Importance (Increase in %IncMSE)",
       subtitle = "Traditional Random Forest Model",
       x = "Variable",
       y = "Increase in MSE") +
  theme bw()
# Generate Partial Dependence Plots and store them as ggplot objects
a = as.data.frame(randomForest::partialPlot(rf_mod4\finalModel, df, e_limeng, plot = FALSE))
b = as.data.frame(randomForest::partialPlot(rf_mod4\finalModel, df, e_pov150, plot = FALSE))
c = as.data.frame(randomForest::partialPlot(rf mod4$finalModel, df, e noveh, plot = FALSE))
d = as.data.frame(randomForest::partialPlot(rf_mod4$finalModel, df, e_munit, plot = FALSE))
# Convert the base R plots to applot objects
plot_a <- ggplot(a, aes(x, y)) + geom_line() + labs(title = "Partial Dependence of e_limeng")</pre>
plot_b <- ggplot(b, aes(x, y)) + geom_line() + labs(title = "Partial Dependence of e_pov150")</pre>
plot_c <- ggplot(c, aes(x, y)) + geom_line() + labs(title = "Partial Dependence of e_noveh")</pre>
plot_d <- ggplot(d, aes(x, y)) + geom_line() + labs(title = "Partial Dependence of e_munit")</pre>
# Arrange the plots in a grid
gridExtra::grid.arrange(plot_a, plot_b, plot_c, plot_d, nrow = 2, ncol = 2)
#####################
### GWRF Results ###
####################
# Spatial Distribution of Prediction and Observation Summary Index Values
svi_df = svi_df %>%
```

```
mutate(grf_pred = gwrf_mod1$Global.Model$predictions)
# Predicted 1:1 Plot
ggplot(svi_df, aes(x = grf_pred, y = rpl_themes)) +
  geom point() +
  theme_bw() +
  geom_abline(slope=1, intercept=0,linetype="dashed",size=0.5) +
  geom_smooth(method = "lm", se = FALSE, colour="black", size=0.5) +
  labs(x="Observed", y = "Predicted")
a = ggplot(svi_df, aes(fill = rpl_themes)) +
  geom_sf() +
  theme_void() +
  scale_fill_viridis_c() +
  labs(title = "Observed SVI Values") +
  theme(legend.title=element_blank())
b = ggplot(svi_df, aes(fill = grf_pred)) +
  geom_sf() +
  theme_void() +
  scale_fill_viridis_c() +
  labs(title = "Predicted SVI Values") +
  theme(legend.title=element_blank())
ggarrange(a,b, ncol = 2, common.legend = TRUE, legend="bottom")
# Global Variable Importance
temp = as.data.frame(gwrf_mod1$Global.Model$variable.importance)
colnames(temp) = c("IncMSE")
temp = tibble::rownames_to_column(temp, "Variable")
ggplot(temp, aes(x = reorder(Variable, IncMSE), y = IncMSE)) +
  geom_bar(stat = "identity", fill = "grey") +
  coord_flip() + # Flip coordinates for better readability
  labs(title = "Variable Importance (Increase in %IncMSE)",
       subtitle = "Geographically Weighted Random Forest Model",
       x = "Variable",
       y = "Increase in MSE") +
  theme_bw()
# Local Variable Importance
variable_names = colnames(gwrf_mod1$Local.Variable.Importance)
plot_lst = list()
# Loop through the names and create maps
for (var_name in variable_names) {
  # Generate the map using ggplot2
  p <- ggplot(svi_df, aes_string(fill = var_name)) +</pre>
```

```
geom_sf() +
    scale_fill_viridis_c() +
    labs(title = paste(var_name),
        fill = "Importance") +
    theme void()
  # Save the plot or print it
 plot_lst[[var_name]] = p
######### SES Variable
ggarrange(plot_lst[["e_pov150"]], plot_lst[["e_unemp"]])
ggarrange(plot_lst[["e_hburd"]], plot_lst[["e_nohsdp"]])
plot_lst[["e_uninsur"]]
############ Household Characteristics
ggarrange(plot_lst[["e_age65"]], plot_lst[["e_age17"]])
ggarrange(plot_lst[["e_disabl"]], plot_lst[["e_sngpnt"]])
plot_lst[["e_limeng"]]
############ Racial & Ethnic Minority Status
plot_lst[["e_minrty"]]
############ Housing Type & Transportation
ggarrange(plot_lst[["e_munit"]], plot_lst[["e_mobile"]])
ggarrange(plot_lst[["e_crowd"]], plot_lst[["e_noveh"]])
plot_lst[["e_groupq"]]
```