

# Projet CPS 2019: Spécification formelle.

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## Ecran

**Service:** Screen

**Observers:** **const** Height: [Screen]  $\rightarrow$  int  
**const** Width: [Screen]  $\rightarrow$  int  
**CellNature:** [Screen]  $\times$  int  $\times$  int  $\rightarrow$  Cell  
    **pre** CellNature(S,x,y) **requires**  $0 \leq y < \text{Height}(S)$  and  $0 \leq x < \text{Width}(S)$

**Constructors:** **init:** int  $\times$  int  $\rightarrow$  [Screen]  
    **pre** **init**(h,w) **requires**  $0 < h$  and  $0 < w$

**Operators:** **Dig:** [Screen]  $\times$  int  $\times$  int  $\rightarrow$  [Screen]  
    **pre** **Dig**(S,x,y) **requires** CellNature(S,x,y) = **PLT**  
**Fill:** [Screen]  $\times$  int  $\times$  int  $\rightarrow$  [Screen]  
    **pre** **Fill**(S,x,y) **requires** CellNature(S,x,y) = **HOL**  
**OpenDoor:** [Screen]  $\times$  int  $\times$  int  $\rightarrow$  [Screen]  
    **pre** **OpenDoor**(S,x,y) **requires** CellNature(S,x,y) = **DOR**  
**RevealTrap:** [Screen]  $\times$  int  $\times$  int  $\rightarrow$  [Screen]  
    **pre** **RevealTrap**(S,x,y) **requires** CellNature(S,x,y) = **TRP**

**Observations:**

[init]: Height(**init**(h,w)) = h  
    Width(**init**(h,w)) = w  
    **forall** (x,y) in [0;Width(S)]  $\times$  [0;Height(S)], CellNature(**init**(h,w),x,y) = **EMP**

[Dig]: CellNature(**Dig**(S,x,y),x,y) = **HOL**  
    **forall** (x,y) in [0;Width(S)]  $\times$  [0;Height(S)],  
        (x  $\neq$  u or y  $\neq$  v) **implies** CellNature(**Dig**(S,u,v),x,y) = CellNature(x,y)

[Fill]: CellNature(**Fill**(S,x,y),x,y) = **PLT**  
    **forall** (x,y) in [0;Width(S)]  $\times$  [0;Height(S)],  
        (x  $\neq$  u or y  $\neq$  v) **implies** CellNature(**Fill**(S,u,v),x,y) = CellNature(x,y)

[OpenDoor]: CellNature(**Fill**(S,x,y),x,y) = **EMP**  
    **forall** (x,y) in [0;Width(S)]  $\times$  [0;Height(S)],  
        (x  $\neq$  u or y  $\neq$  v) **implies** CellNature(**OpenDoor**(S,u,v),x,y) = CellNature(x,y)

[RevealTrap]: CellNature(**Fill**(S,x,y),x,y) = **EMP**  
    **forall** (x,y) in [0;Width(S)]  $\times$  [0;Height(S)],  
        (x  $\neq$  u or y  $\neq$  v) **implies** CellNature(**RevealTrap**(S,u,v),x,y) = CellNature(x,y)

# Ecran éditable

*Pas de changement par rapport à la spécification fournie*

**Service:** EditableScreen **includes** Screen  
**Observers:** Playable: [EditableScreen]  $\rightarrow$  bool  
**Operators:** SetNature: [EditableScreen]  $\times$  int  $\times$  int  $\times$  Cell  $\rightarrow$  [EditableScreen]  
pre SetNature(S,x,y,C) **requires**  $0 \leq y < \text{Height}(S)$  **and**  $0 \leq x < \text{Width}(S)$   
**Observations:**  
[invariant]: Playable(S) **min**  
forall (x,y) in  $[0;\text{Width}(S)[ \times [0;\text{Height}(S)[$ , CellNature(S,x,y)  $\neq$  HOL  
and forall x in  $[0;\text{Width}(S)[$ , CellNature(S,x,0) = MTL  
[SetNature]: CellNature(SetNature(S,x,y,C)),x,y = C  
forall (x,y) in  $[0;\text{Width}(S)[ \times [0;\text{Height}(S)[$ ,  
(x  $\neq$  u or y  $\neq$  v) **implies** CellNature(SetNature(S,u,v,C)),x,y) = CellNature(S,x,y)

## Environnement

**Service:** Environment **includes** Screen  
**Observers :** CellContent: int  $\times$  int  $\rightarrow$  Set{Character + Item}  
pre CellContent(E,x,y) **requires**  $0 \leq y < \text{Height}(S)$  **and**  $0 \leq x < \text{Width}(S)$   
**Constructors:** init: EditableScreen  $\rightarrow$  Environment  
**Operators:** AddToCellContent: [EditableScreen]  $\times$  int  $\times$  int  $\times$  {Character + Item}  
 $\rightarrow$  [EditableScreen]  
pre AddToCellContent(S,x,y,e) **requires**  $0 \leq y < \text{Height}(S)$   
and  $0 \leq x < \text{Width}(S)$   
and exists Guard g in CellContent(E,x,y) **implies not** e is Guard  
RemoveFromCellContent: [EditableScreen]  $\times$  int  $\times$  int  $\times$  {Character + Item}  
 $\rightarrow$  [EditableScreen]  
pre RemoveFromCellContent(S,x,y,e) **requires**  $0 \leq y < \text{Height}(S)$   
and  $0 \leq x < \text{Width}(S)$  **and** exists e in CellContent(E,x,y)  
**Observations:**  
[invariant]: forall (x,y) in  $[0;\text{Width}(E)[ \times [0;\text{Height}(E)[$ ,  
CellNature(E,x,y) in {MTL, PLT} **implies** CellContent(x,y) =  $\emptyset$   
[init]: forall (x,y) in  $[0;\text{Width}(E)[ \times [0;\text{Height}(E)[$ ,  
CellNature(init(S),x,y) = EditableScreen::CellNature(S,x,y)  
and CellContent(init(S),x,y) = {}  
[AddToCellContent]: CellContent(AddToCellContent(S, x, y, e), x, y) = CellContent(S, x, y) **union** {e}  
forall (x,y) in  $[0;\text{Width}(E)[ \times [0;\text{Height}(E)[$ ,  
(x  $\neq$  u or y  $\neq$  v)  
**implies** CellNature(AddToCellContent(S,u,v,e)),x,y) = CellNature(S,x,y)  
and CellContent(RemoveFromCellContent(S, u, v, e), x, y) = CellContent(S, x, y)  
[RemoveFromCellContent]: CellContent(RemoveFromCellContent(S, x, y, e), x, y) = CellContent(S, x, y) \ {e}  
forall (x,y) in  $[0;\text{Width}(E)[ \times [0;\text{Height}(E)[$ ,  
(x  $\neq$  u or y  $\neq$  v)  
**implies** CellNature(RemoveFromCellContent(S,u,v,e)),x,y)  
= CellNature(S,x,y)  
and CellContent(RemoveFromCellContent(S, u, v, e), x, y) = CellContent(S, x, y)

# Personnage

**Service:** Character

**Observers:** **const** Envi: [Character]  $\rightarrow$  Environment  
 Hgt: [Character]  $\rightarrow$  int  
 Col: [Character]  $\rightarrow$  int

**Constructors:** **init**: Environment  $\times$  int  $\times$  int  $\rightarrow$  [Character]  
     **pre** init(E,x,y) **requires** E  $\neq$  null **and not** Environment::CellNature(E,x,y) **in** {MTL, PLT, DOR}  
     **and**  $0 \leq y < \text{Environment::Height}(E)$  **and**  $0 \leq x < \text{Environment::Width}(E)$

**Operators:** GoLeft: [Character]  $\rightarrow$  [Character]  
 GoRight: [Character]  $\rightarrow$  [Character]  
 GoUp: [Character]  $\rightarrow$  [Character]  
 GoDown: [Character]  $\rightarrow$  [Character]

**Observations:**

[invariant]: Environment::CellNature(Envi(C),Col(C),Hgt(C)) **in** {EMP, HOL, LAD, HDR, NPL, NGU}

[init]: Hgt(init(E,x,y)) = y  
 Col(init(E,x,y)) = x  
 Envi(init(E,x,y)) = e  
**exists** init(E,x,y) **in** Environment::CellContent(Envi(init(E,x,y), x, y))

[GoLeft]: Hgt(GoLeft(C)) = Hgt(C)  
 Col(C) = 0 **implies** Col(GoLeft(C)) = Col(C)  
 Environment::CellNature(Envi(C),Col(C)-1,Hgt(C)) **in** {MTL, PLT, DOR}  
**implies** Col(GoLeft(C)) = Col(C)  
 Environment::CellNature(Envi(C),Col(C),Hgt(C)) **not in** {LAD, HDR}  
**and** Environment::CellNature(Envi(C),Col(C),Hgt(C)-1) **not in** {PLT, MTL, LAD,DOR}  
**and not exists** Guard g **in** Environment::CellContent(Envi(C),Col(C),Hgt(C)-1)  
**implies** Col(GoLeft(C)) = Col(C)  
**exists** Guard g **in** Environment::CellContent(Envi(C),Col(C)-1,Hgt(C))  
**implies** Col(GoLeft(C)) = Col(C)  
 (Col(C)  $\neq$  0) **and** Environment::CellNature(Envi(C),Col(C)-1,Hgt(C)) **not in** {MTL, PLT,DOR}  
**and** (Environment::CellNature(Envi(C),Col(C),Hgt(C)) **in** {LAD, HDR}  
     **or** Environment::CellNature(Envi(C),Col(C),Hgt(C)-1) **in** {PLT, MTL, LAD,DOR}  
     **or exists** Guard g **in** Environment::CellContent(Envi(C),Col(C),Hgt(C)-1) )  
**and not** (exists Guard g **in** Environment::CellContent(Envi(C),Col(C)-1,Hgt(C)))  
**implies** Col(GoLeft(C)) = Col(C)-1

[GoRight]: Hgt(GoRight(C)) = Hgt(C)  
 Col(C) = Environment::Width(Envi(GoRight(C))) - 1 **implies** Col(GoRight(C)) = Col(C)  
 Environment::CellNature(Envi(C),Col(C)+1,Hgt(C)) **in** {MTL, PLT, DOR}  
**implies** Col(GoRight(C)) = Col(C)  
 Environment::CellNature(Envi(C),Col(C),Hgt(C)) **not in** {LAD, HDR}  
**and** Environment::CellNature(Envi(C),Col(C),Hgt(C)-1) **not in** {PLT, MTL, LAD,DOR}  
**and not exists** Guard g **in** Environment::CellContent(Envi(C),Col(C),Hgt(C)-1)  
**implies** Col(GoRight(C)) = Col(C)  
**exists** Guard g **in** Environment::CellContent(Envi(C),Col(C)+1,Hgt(C))  
**implies** Col(GoRight(C)) = Col(C)  
 (Col(C)  $\neq$  Environment::Width(Envi(GoRight(C))) - 1)  
**and** Environment::CellNature(Envi(C),Col(C)+1,Hgt(C)) **not in** {MTL,PLT,DOR}  
**and** (Environment::CellNature(Envi(C),Col(C),Hgt(C)) **in** {LAD, HDR}  
     **or** Environment::CellNature(Envi(C),Col(C),Hgt(C)-1) **in** {PLT, MTL, LAD,DOR}  
     **or exists** Guard g **in** Environment::CellContent(Envi(C),Col(C),Hgt(C)-1) )  
**and not** (exists Guard g **in** Environment::CellContent(Envi(C),Col(C)+1,Hgt(C)))  
**implies** Col(GoRight(C)) = Col(C)+1

[GoUp]:  $\text{Col}(\text{GoUp}(C)) = \text{Col}(C)$   
 $\text{Hgt}(C) = \text{Environment::Height}(\text{Envi}(\text{GoUp}(C))) - 1$  **implies**  $\text{Hgt}(\text{GoUp}(C)) = \text{Hgt}(C)$   
 $\text{Environment::CellNature}(\text{Envi}(C), \text{Col}(C), \text{Hgt}(C)+1)$  **in** {MTL, PLT, DOR}  
**implies**  $\text{Hgt}(\text{GoUp}(C)) = \text{Hgt}(C)$   
 $\text{Environment::CellNature}(\text{Envi}(C), \text{Col}(C), \text{Hgt}(C)) \neq \text{LAD}$  **implies**  $\text{Hgt}(\text{GoUp}(C)) = \text{Hgt}(C)$   
**exists** Guard  $g$  **in**  $\text{Environment::CellContent}(\text{Envi}(C), \text{Col}(C), \text{Hgt}(C)+1)$   
**implies**  $\text{Hgt}(\text{GoUp}(C)) = \text{Hgt}(C)$   
 $(\text{Hgt}(C) \neq \text{Environment::Height}(\text{Envi}(\text{GoUp}(C))) - 1)$   
**and**  $\text{Environment::CellNature}(\text{Envi}(C), \text{Col}(C), \text{Hgt}(C)+1)$  **not in** {MTL, PLT, DOR}  
**and**  $\text{Environment::CellNature}(\text{Envi}(C), \text{Col}(C), \text{Hgt}(C)) = \text{LAD}$   
**and** **exists** Guard  $g$  **in**  $\text{Environment::CellContent}(\text{Envi}(C), \text{Col}(C), \text{Hgt}(C)+1)$   
**implies**  $\text{Hgt}(\text{GoUp}(C)) = \text{Hgt}(C)+1$

[GoDown]:  $\text{Col}(\text{GoDown}(C)) = \text{Col}(C)$   
 $\text{Hgt}(C) = 0$  **implies**  $\text{Hgt}(\text{GoDown}(C)) = \text{Hgt}(C)$   
 $\text{Environment::CellNature}(\text{Envi}(C), \text{Col}(C), \text{Hgt}(C)-1)$  **in** {MTL, PLT, DOR}  
**implies**  $\text{Hgt}(\text{GoDown}(C)) = \text{Hgt}(C)$   
**exists** Guard  $g$  **in**  $\text{Environment::CellContent}(\text{Envi}(C), \text{Col}(C), \text{Hgt}(C)-1)$   
**implies**  $\text{Hgt}(\text{GoDown}(C)) = \text{Hgt}(C)$   
 $(\text{Hgt}(C) \neq 0)$   
**and**  $\text{Environment::CellNature}(\text{Envi}(C), \text{Col}(C), \text{Hgt}(C)-1)$  **not in** {MTL, PLT, DOR}  
**and** **exists** Guard  $g$  **in**  $\text{Environment::CellContent}(\text{Envi}(C), \text{Col}(C), \text{Hgt}(C)-1)$   
**implies**  $\text{Hgt}(\text{GoDown}(C)) = \text{Hgt}(C)-1$

# Joueur

**Service:** Player **includes** Character

**Observers:** **const** Engine: [Player] → Engine  
FacingRight: [Player] → bool  
CurrentlyHeldItem: [Player] → Item  
NumberOfUsagesLeftForCurrentItem: [Player] → int

**Constructors:** **init**: int × int × Engine → [Player]  
**pre** init(x,y,E) **requires** E ≠ null  
**and not** Environment::CellNature(Engine::Environment(E),x,y) **in** {MTL, PLT, DOR, NPL}  
**and** 0 ≤ y < Environment::Height(Engine::Environment(E))  
**and** 0 ≤ x < Environment::Width(Engine::Environment(E))

**Operators:** DigLeft: [Player] → [Player]  
DigRight: [Player] → [Player]  
UseItem: [Player] → [Player]  
PickupItem: [Player] × ItemType → [Player]  
Step: [Player] → [Player]

**Observations:**

[invariants]: Environment::CellNature(Envi(C),Col(C),Hgt(C)) **in** {EMP, HOL, LAD, HDR, NGU}

[init]: Hgt(init(x,y,E)) = y  
Col(init(x,y,E)) = x  
Envi(init(x,y,E)) = Engine::Environment(E)  
**exists** init(x,y,E) Environment::CellContent(Envi(init(x,y,E)), x, y)  
Engine(init(x,y,E)) = E  
FacingRight(init(x,y,E))  
Item::Nature(CurrentlyHeldItem(init(x,y,E))) = Sword  
NumberOfUsagesLeftForCurrentItem(init(x,y,E)) = 3

[DigLeft]: **NoCellNatureChanged(C) defined by**  
( forall (i,j) in [0;Environment::Width(Environment(DigLeft(C)))[  
[0;Environment::Height(Environment(DigLeft(C)))[  
Environment::CellNature(Envi(DigLeft(C), i, j) ) = Environment::CellNature(Envi(C, i, j) )  
Hgt(DigLeft(C)) = Hgt(C)  
Col(DigLeft(C)) = Col(C)  
Col(C) = 0 **implies** NoCellNatureChanged  
Environment::CellNature(Envi(C), Col(C), Hgt(C)-1) **not in** {MTL, PLT, LAD, DOR, NPL}  
**and not exists** Guard g **in** Environment::CellContent(Envi(C), Col(C), Hgt(C)-1)  
**implies** NoCellNatureChanged  
Environment::CellNature(Envi(C), Col(C)-1, Hgt(C)) **not in** {EMP, HOL, LAD, HDR}  
**implies** NoCellNatureChanged  
Environment::CellNature(Envi(C), Col(C)-1, Hgt(C)-1) ≠ PLT  
**implies** NoCellNatureChanged  
Col(C) ≠ 0  
**and** (Environment::CellNature(Envi(C), Col(C), Hgt(C)-1) **in** {MTL, PLT, LAD, DOR, NPL}  
**or exists** Guard g **in** Environment::CellContent(Envi(C), Col(C), Hgt(C)-1))  
**and** Environment::CellNature(Envi(C), Col(C)-1, Hgt(C)) **in** {EMP, HOL, LAD, HDR}  
**and** Environment::CellNature(Envi(C), Col(C)-1, Hgt(C)-1) = PLT  
**implies** Environment::CellNature(Envi(DigLeft(C)), Col(C)-1, Hgt(C)-1) = HOL  
**and forall** (i,j) **in** [0;Environment::Width(Environment(DigLeft(C)))[  
[0;Environment::Height(Environment(DigLeft(C)))[  
((i ≠ Col(DigLeft(C))-1) **or** (j ≠ Hgt(DigLeft(C))-1) **implies**  
Environment::CellNature(Envi(DigLeft(C), i, j) ) = Environment::CellNature(Envi(C, i, j)  
FacingRight(DigLeft(C))  
CurrentlyHeldItem(DigLeft(C)) = CurrentlyHeldItem(C)  
NumberOfUsagesLeftForCurrentItem(DigLeft(C)) = NumberOfUsagesLeftForCurrentItem(C)

[DigRight]: **NoCellNatureChanged(C)** defined by

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    ( forall (i,j) in [0;Environment::Width(Environment(DigRight(C)))[
      [0;Environment::Height(Environment(DigRight(C)))[,
        Environment::CellNature(Envi(DigRight(C), i, j) ) = Environment::CellNature(Envi(C, i, j) )
    Hgt(DigRight(C)) = Hgt(C)
    Col(DigRight(C)) = Col(C)
    Col(C) = Environment::Width(Envi(DigRight(C))) - 1 implies NoCellNatureChanged
    Environment::CellNature(Envi(C), Col(C), Hgt(C)-1) not in {MTL, PLT, LAD, DOR, NPL}
    and not exists Guard g in Environment::CellContent(Envi(C), Col(C), Hgt(C)-1)
    implies NoCellNatureChanged
    Environment::CellNature(Envi(C), Col(C)+1, Hgt(C)) not in {EMP, HOL, LAD, HDR}
    implies NoCellNatureChanged
    Environment::CellNature(Envi(C), Col(C)+1, Hgt(C)-1)  $\neq$  PLT
    implies NoCellNatureChanged
    Col(C)  $\neq$  Environment::Width(Envi(DigRight(C))) - 1
    and (Environment::CellNature(Envi(C), Col(C), Hgt(C)-1) in {MTL, PLT, LAD, DOR, NPL}
    or exists Guard g in Environment::CellContent(Envi(C), Col(C), Hgt(C)-1))
    and Environment::CellNature(Envi(C), Col(C)+1, Hgt(C)) in {EMP, HOL, LAD, HDR}
    and Environment::CellNature(Envi(C), Col(C)+1, Hgt(C)-1) = PLT
    implies Environment::CellNature(Envi(DigRight(C)), Col(C)+1, Hgt(C)-1) = HOL
    and forall (i,j) in [0;Environment::Width(Environment(DigRight(C)))[
      [0;Environment::Height(Environment(DigRight(C)))[,
        ((i  $\neq$  Col(DigRight(C))+1) or (j  $\neq$  Hgt(DigRight(C))-1) implies
        Environment::CellNature(Envi(DigRight(C), i, j) ) = Environment::CellNature(Envi(C, i, j) )
    not FacingRight(DigLeft(C))
    CurrentlyHeldItem(DigLeft(C)) = CurrentlyHeldItem(C)
    NumberOfUsagesLeftForCurrentItem(DigLeft(C)) = NumberOfUsagesLeftForCurrentItem(C)

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[UseItem]: **CanUseItem(C)** defined by

CurrentlyHeldItem(C)  $\neq$  null  
**and** NumberOfUsagesLeftForCurrentItem(C)  $\geq 1$

CurrentlyHeldItem(C)  $\neq$  null **and** NumberOfUsagesLeftForCurrentItem(C) = 1  
**implies** CurrentlyHeldItem(UseItem('C')) = null  
**and** NumberOfUsagesLeftForCurrentItem(UseItem(C)) = 0

CurrentlyHeldItem(C)  $\neq$  null **and** NumberOfUsagesLeftForCurrentItem(C) > 1  
**implies** CurrentlyHeldItem(UseItem(C)) = CurrentlyHeldItem(C)  
**and** NumberOfUsagesLeftForCurrentItem(UseItem(C)) = NumberOfUsagesLeftForCurrentItem(C) - 1

CanUseItem **and** Item::Nature(CurrentlyHeldItem(C)) = Key **and** FacingRight(C)  
**and** Col(C) < Environment::Width(Envi(C)) - 1  
**and** Environment::CellNature(Envi(C), Col(C)+1, Hgt(C)) = DOR  
**implies** Environment::CellNature(Envi(UseItem(C), Col(C)+1, Hgt(C)) = EMP

CanUseItem **and** Item::Nature(CurrentlyHeldItem(C)) = Key **and not** FacingRight(C)  
**and** Col(C) > 0  
**and** Environment::CellNature(Envi(C), Col(C)-1, Hgt(C)) = DOR  
**implies** Environment::CellNature(Envi(UseItem(C), Col(C)-1, Hgt(C)+1) = EMP

**forall** Guard g **in** Engine::Guards(Engi(UseItem(C))),  
CanUseItem **and** Item::Nature(CurrentlyHeldItem(C)) = Flash  
**implies** Guard::TimeLeftParalyzed(g) = 10

CanUseItem **and** Item::Nature(CurrentlyHeldItem(C)) = Sword **and** Col(C) - 2  $\geq 0$   
**and exists** Guard g **in** Environment::CellContent(Envi(C), Col(C) - 2, Hgt(C))  
**implies exists** g **in** Environment::CellContent(Envi(UseItem(C)),  
Coord::X(Guard::InitCoords(g)), Coord::Y(Guard::InitCoords(g)))

CanUseItem **and** Item::Nature(CurrentlyHeldItem(C)) = Sword **and** Col(C) - 1  $\geq 0$   
**and exists** Guard g **in** Environment::CellContent(Envi(C), Col(C) - 1, Hgt(C))  
**implies exists** g **in** Environment::CellContent(Envi(UseItem(C)),  
Coord::X(Guard::InitCoords(g)), Coord::Y(Guard::InitCoords(g)))

CanUseItem **and** Item::Nature(CurrentlyHeldItem(C)) = Sword  
**and** Col(C) + 2 < Environment::Width(Envi(C))  
**and exists** Guard g **in** Environment::CellContent(Envi(C), Col(C) + 2, Hgt(C))  
**implies exists** g **in** Environment::CellContent(Envi(UseItem(C)),  
Coord::X(Guard::InitCoords(g)), Coord::Y(Guard::InitCoords(g)))

CanUseItem **and** Item::Nature(CurrentlyHeldItem(C)) = Sword  
**and** Col(C) + 1 < Environment::Width(Envi(C))  
**and exists** Guard g **in** Environment::CellContent(Envi(C), Col(C) + 1, Hgt(C))  
**implies exists** g **in** Environment::CellContent(Envi(UseItem(C)),  
Coord::X(Guard::InitCoords(g)), Coord::Y(Guard::InitCoords(g)))

**ExistsObstacleBetween(x1, x2, y)** defined by

**exists** Cell c **in** (union (forall i in [x1;x2], Environment::CellNature(Envi(C), i, y)))  
**with** (c in {MTL, PLT, DOR, NPL})

**forall** i in [0;Environment::Width(Envi(C))],  
CanUseItem **and** Item::Nature(CurrentlyHeldItem(C)) = Gun  
**and** FacingRight(C)  
**and** i > Col(C)  
**and not** ExistsObstacleBetween(Col(C), i, Hgt(C))  
**and exists** Guard g **in** Environment::CellContent(Envi(C), i, Hgt(C))  
**implies exists** g **in** Environment::CellContent(Envi(UseItem(C),  
Coord::X(Guard::InitCoords(g)), Coord::Y(Guard::InitCoords(g)))

CanUseItem **and** Item::Nature(CurrentlyHeldItem(C)) = Gun  
**and not** FacingRight(C)  
**and** i < Col(C)  
**and not** ExistsObstacleBetween(i, Col(C), Hgt(C))  
**and exists** Guard g **in** Environment::CellContent(Envi(C), i, Hgt(C))  
**implies exists** g **in** Environment::CellContent(Envi(UseItem(C),  
Coord::X(Guard::InitCoords(g)), Coord::Y(Guard::InitCoords(g)))

Col(UseItem(C)) = Col(C)  
Hgt(UseItem(C)) = Hgt(C)  
FacingRight(UseItem(C)) = FacingRight(C)

[PickupItem]: FacingRight(PickupItem(C, t)) = FacingRight(C)  
Col(PickupItem(C, t)) = Col(C)  
Hgt(PickupItem(C, t)) = Hgt(C)  
CurrentlyHeldItem(C)  $\neq$  null **and** Item::Nature(CurrentlyHeldItem(C)) = t **and** t = Key  
**implies** NumberOfUsagesLeftForCurrentItem(PickupItem(C, t)) =  
NumberOfUsagesLeftForCurrentItem(C)+1  
**and** CurrentlyHeldItem(PickupItem(C, t)) = CurrentlyHeldItem(C)  
CurrentlyHeldItem(C)  $\neq$  null **and** Item::Nature(CurrentlyHeldItem(C)) = t **and** t = Flash  
**implies** NumberOfUsagesLeftForCurrentItem(PickupItem(C, t)) =  
NumberOfUsagesLeftForCurrentItem(C)+1  
**and** CurrentlyHeldItem(PickupItem(C, t)) = CurrentlyHeldItem(C)  
CurrentlyHeldItem(C)  $\neq$  null **and** Item::Nature(CurrentlyHeldItem(C)) = t **and** t = Gun  
**implies** NumberOfUsagesLeftForCurrentItem(PickupItem(C, t)) =  
NumberOfUsagesLeftForCurrentItem(C)+1  
**and** CurrentlyHeldItem(PickupItem(C, t)) = CurrentlyHeldItem(C)  
CurrentlyHeldItem(C)  $\neq$  null **and** Item::Nature(CurrentlyHeldItem(C)) = t **and** t = Sword  
**implies** NumberOfUsagesLeftForCurrentItem(PickupItem(C, t)) =  
NumberOfUsagesLeftForCurrentItem(C)+3  
**and** CurrentlyHeldItem(PickupItem(C, t)) = CurrentlyHeldItem(C)  
**not** (CurrentlyHeldItem(C)  $\neq$  null **and** Item::Nature(CurrentlyHeldItem(C)) = t) **and** t = Key  
**implies** NumberOfUsagesLeftForCurrentItem(PickupItem(C, t)) = 1  
Item::Nature(CurrentlyHeldItem(PickupItem(C, t))) = t  
**not** (CurrentlyHeldItem(C)  $\neq$  null **and** Item::Nature(CurrentlyHeldItem(C)) = t) **and** t = Flash  
**implies** NumberOfUsagesLeftForCurrentItem(PickupItem(C, t)) = 1  
Item::Nature(CurrentlyHeldItem(PickupItem(C, t))) = t  
**not** (CurrentlyHeldItem(C)  $\neq$  null **and** Item::Nature(CurrentlyHeldItem(C)) = t) **and** t = Gun  
**implies** NumberOfUsagesLeftForCurrentItem(PickupItem(C, t)) = 1  
Item::Nature(CurrentlyHeldItem(PickupItem(C, t))) = t  
**not** (CurrentlyHeldItem(C)  $\neq$  null **and** Item::Nature(CurrentlyHeldItem(C)) = t) **and** t = Sword  
**implies** NumberOfUsagesLeftForCurrentItem(PickupItem(C, t)) = 3  
Item::Nature(CurrentlyHeldItem(PickupItem(C, t))) = t

[Step]: **Falling(C) defined by**  
(Environment::CellNature(Envi(C), Col(C), Hgt(C)) **not in** {LAD,HDR}  
**and** Environment::CellNature(Envi(C), Col(C), Hgt(C)-1) **in** {EMP,HDR,HOL,NGU}  
**and not exists** Guard g **in** Environment::CellContent(Envi(C), Col(C), Hgt(C)-1) )  
Falling **implies** Step(C) = GoDown(C)  
**not** Falling **and** NextCommand(C) = MOVEL **implies** Step(C) = GoLeft(C)  
**not** Falling **and** NextCommand(C) = MOVER **implies** Step(C) = GoRight(C)  
**not** Falling **and** NextCommand(C) = MOVED **implies** Step(C) = GoDown(C)  
**not** Falling **and** NextCommand(C) = MOVEU **implies** Step(C) = GoUp(C)  
**not** Falling **and** NextCommand(C) = DIGL **implies** Step(C) = DigLeft(C)  
**not** Falling **and** NextCommand(C) = DIGR **implies** Step(C) = DigRight(C)  
**not** Falling **and** NextCommand(C) = USEITEM **implies** Step(C) = UseItem(C)  
**not** Falling **and** NextCommand(C) = NONE **implies** Step(C) = C



*Les fonctions de déplacements de Player sont quasiment les mêmes que celles de Character, on change seulement le fait qu'on ne puisse pas aller dans une case NPL*

```
[GoLeft]:  Hgt(GoLeft(C)) = Hgt(C)
           Col(C) = 0 implies Col(GoLeft(C)) = Col(C)
           Environment::CellNature(Envi(C),Col(C)-1,Hgt(C)) in {MTL, PLT, DOR, NPL}
             implies Col(GoLeft(C)) = Col(C)
           Environment::CellNature(Envi(C),Col(C),Hgt(C)) not in {LAD, HDR}
             and Environment::CellNature(Envi(C),Col(C),Hgt(C)-1) not in {PLT, MTL, LAD,DOR, NPL}
             and not exists Guard g in Environment::CellContent(Envi(C),Col(C),Hgt(C)-1)
             implies Col(GoLeft(C)) = Col(C)
           exists Guard g in Environment::CellContent(Envi(C),Col(C)-1,Hgt(C))
             implies Col(GoLeft(C)) = Col(C)
           (Col(C) ≠ 0) and Environment::CellNature(Envi(C),Col(C)-1,Hgt(C)) not in {MTL, PLT,DOR, NPL}
             and (Environment::CellNature(Envi(C),Col(C),Hgt(C)) in {LAD, HDR}
                 or Environment::CellNature(Envi(C),Col(C),Hgt(C)-1) in {PLT, MTL, LAD,DOR, NPL}
                 or exists Guard g in Environment::CellContent(Envi(C),Col(C),Hgt(C)-1) )
             and not (exists Guard g in Environment::CellContent(Envi(C),Col(C)-1,Hgt(C)))
             implies Col(GoLeft(C)) = Col(C)-1

[GoRight]: Hgt(GoRight(C)) = Hgt(C)
           Col(C) = Environment::Width(Envi(GoRight(C))) - 1 implies Col(GoRight(C)) = Col(C)
           Environment::CellNature(Envi(C),Col(C)+1,Hgt(C)) in {MTL, PLT, DOR, NPL}
             implies Col(GoRight(C)) = Col(C)
           Environment::CellNature(Envi(C),Col(C),Hgt(C)) not in {LAD, HDR}
             and Environment::CellNature(Envi(C),Col(C),Hgt(C)-1) not in {PLT, MTL, LAD,DOR, NPL}
             and not exists Guard g in Environment::CellContent(Envi(C),Col(C),Hgt(C)-1)
             implies Col(GoRight(C)) = Col(C)
           exists Guard g in Environment::CellContent(Envi(C),Col(C)+1,Hgt(C))
             implies Col(GoRight(C)) = Col(C)
           (Col(C) ≠ Environment::Width(Envi(GoRight(C))) - 1)
             and Environment::CellNature(Envi(C),Col(C)+1,Hgt(C)) not in {MTL, PLT,DOR, NPL}
             and (Environment::CellNature(Envi(C),Col(C),Hgt(C)) in {LAD, HDR}
                 or Environment::CellNature(Envi(C),Col(C),Hgt(C)-1) in {PLT, MTL, LAD,DOR, NPL}
                 or exists Guard g in Environment::CellContent(Envi(C),Col(C),Hgt(C)-1) )
             and not (exists Guard g in Environment::CellContent(Envi(C),Col(C)+1,Hgt(C)))
             implies Col(GoRight(C)) = Col(C)+1

[GoUp]:    Col(GoUp(C)) = Col(C)
           Hgt(C) = Environment::Height(Envi(GoUp(C))) - 1 implies Hgt(GoUp(C)) = Hgt(C)
           Environment::CellNature(Envi(C),Col(C),Hgt(C)+1) in {MTL, PLT, DOR, NPL}
             implies Hgt(GoUp(C)) = Hgt(C)
           Environment::CellNature(Envi(C),Col(C),Hgt(C)) ≠ LAD implies Hgt(GoUp(C)) = Hgt(C)
           exists Guard g in Environment::CellContent(Envi(C),Col(C),Hgt(C)+1)
             implies Hgt(GoUp(C)) = Hgt(C)
           (Hgt(C) ≠ Environment::Height(Envi(GoUp(C))) - 1)
             and Environment::CellNature(Envi(C),Col(C),Hgt(C)+1) not in {MTL, PLT, DOR, NPL}
             and Environment::CellNature(Envi(C),Col(C),Hgt(C)) = LAD
             and exists Guard g in Environment::CellContent(Envi(C),Col(C),Hgt(C)+1)
             implies Hgt(GoUp(C)) = Hgt(C)+1

[GoDown]:  Col(GoDown(C)) = Col(C)
           Hgt(C) = 0 implies Hgt(GoDown(C)) = Hgt(C)
           Environment::CellNature(Envi(C),Col(C),Hgt(C)-1) in {MTL, PLT, DOR, NPL}
             implies Hgt(GoDown(C)) = Hgt(C)
           exists Guard g in Environment::CellContent(Envi(C),Col(C),Hgt(C)-1)
             implies Hgt(GoDown(C)) = Hgt(C)
           (Hgt(C) ≠ 0)
             and Environment::CellNature(Envi(C),Col(C),Hgt(C)-1) not in {MTL, PLT, DOR, NPL}
             and exists Guard g in Environment::CellContent(Envi(C),Col(C),Hgt(C)-1)
             implies Hgt(GoDown(C)) = Hgt(C)-1
```

## Garde

**Service:** Guard **includes** Character

**Observers:** **const** Id: [Guard]  $\rightarrow$  int  
**const** Engine: [Guard]  $\rightarrow$  Engine  
**const** Target: [Guard]  $\rightarrow$  Character  
**const** InitCoords: [Guard]  $\rightarrow$  Coord  
**const** Nature: [Guard]  $\rightarrow$  GuardType  
**Behaviour:** [Guard]  $\rightarrow$  Command  
**TimeInHole:** [Guard]  $\rightarrow$  int  
**IdCounter:** [Guard]  $\rightarrow$  int  
**CarryingTreasure:** [Guard]  $\rightarrow$  bool  
**TimeLeftParalyzed:** [Guard]  $\rightarrow$  int

**Constructors:** **init:** Engine  $\times$  int  $\times$  int  $\times$  Character  $\rightarrow$  [Guard]  
**pre** init(E,x,y,t) **requires** E  $\neq$  null  
**and not** Environment::CellNature(Engine::Environment(E),x,y) **in** {MTL, PLT, DOR, NGU}  
**and**  $0 \leq y < \text{Environment::Height}(\text{Engine::Environment}(E))$   
**and**  $0 \leq x < \text{Environment::Width}(\text{Engine::Environment}(E))$

**Operators:** **ClimbLeft:** [Guard]  $\rightarrow$  [Guard]  
**pre** ClimbLeft(G) **requires** Environment::CellNature(Envi(G),Hgt(G),Col(G)) = HOL  
**ClimbRight:** [Guard]  $\rightarrow$  [Guard]  
**pre** ClimbRight(G) **requires** Environment::CellNature(Envi(G),Hgt(G),Col(G)) = HOL  
**MoveToInitCoords:** [Guard]  $\rightarrow$  [Guard]  
**Paralyze:** [Guard]  $\rightarrow$  [Guard]  
**Step:** [Guard]  $\rightarrow$  [Guard]

**Observations:**  
[invariant]: Environment::CellNature(Envi(C),Col(C),Hgt(C)) **in** {EMP, HOL, LAD, HDR, NPL}  
Environment::CellNature(Envi(G),Col(G),Hgt(G)) = LAD  
**and** Hgt(G) < Character::Hgt(Target(G))  
**implies** Behaviour(G) = MOVEU  
Environment::CellNature(Envi(G),Col(G),Hgt(G)) = LAD  
**and** Hgt(G) > Character::Hgt(Target(G))  
**implies** Behaviour(G) = MOVED  
Environment::CellNature(Envi(G), Col(G), Hgt(G)) = HOL  
**and** Character::Col(Target(G)) = Col(G) **and** Character::Hgt(Target(G)) = Hgt(G)+1  
**and** Environment::CellNature(Envi(G),Col(G)+1,Hgt(G)+1) **in** {EMP,HDR,LAD,NPL}  
**implies** Behaviour(G) = MOVER  
Environment::CellNature(Envi(G), Col(G), Hgt(G)) = HOL  
**and** Character::Col(Target(G)) = Col(G) **and** Character::Hgt(Target(G)) = Hgt(G)+1  
**and** Environment::CellNature(Envi(G),Col(G)+1,Hgt(G)+1) **not in** {EMP,HDR,LAD,NPL}  
**implies** Behaviour(G) = MOVEL  
( Environment::CellNature(Envi(G),Col(G),Hgt(G))  $\neq$  LAD **or** Character::Hgt(Target(G)) = Hgt(G) )  
**and** ( Environment::CellNature(Envi(G),Col(G),Hgt(G)) **in** {HOL,HDR,LAD}  
**or** Environment::CellNature(Envi(G),Col(G),Hgt(G)-1) **in** {PLT,MTL,LAD,DOR,NGU,TRP}  
**or exists** Guard g **in** Environment::CellContent(Envi(G),Col(G),Hgt(G)-1) )  
**and** Character::Col(Target(G)) < Col(G)  
**implies** Behaviour(G) = MOVEU  
( Environment::CellNature(Envi(G),Col(G),Hgt(G))  $\neq$  LAD **or** Character::Hgt(Target(G)) = Hgt(G) )  
**and** ( Environment::CellNature(Envi(G),Col(G),Hgt(G)) **in** {HOL,HDR,LAD}  
**or** Environment::CellNature(Envi(G),Col(G),Hgt(G)-1) **in** {PLT,MTL,LAD,DOR,NGU,TRP}  
**or exists** Guard g **in** Environment::CellContent(Envi(G),Col(G),Hgt(G)-1) )  
**and** Character::Col(Target(G)) > Col(G)  
**implies** Behaviour(G) = MOVER

[init]: Engine(init(E,x,y,t)) = e  
Nature(init(E,x,y,t)) = NORMAL  
Coord::X(InitCoords(init(E,x,y,t))) = x  
Coord::Y(InitCoords(init(E,x,y,t))) = y  
Target(init(E,x,y,t)) = t  
Id(init(E,x,y,t)) = IdCounter(init(E,x,y,t)) - 1  
**not** CarryingTreasure(init(E,x,y,t))  
TimeInHole(init(E,x,y,t)) = 0  
TimeLeftParalyzed(init(E,x,y,t)) = 0

[ClimbLeft]: Col(C) = 0 **implies** Col(ClimbLeft(C)) = Col(C) **and** Hgt(ClimbLeft(C)) = Hgt(C)  
Screen::CellNature(Envi(C),Col(C)-1,Hgt(C)+1) **in** {MTL, PLT, DOR, NGU }  
**implies** Col(ClimbLeft(C)) = Col(C) **and** Hgt(ClimbLeft(C)) = Hgt(C)  
**exists** Guard g **in** Environment::CellContent(Envi(C),Col(C)-1,Hgt(C)+1)  
**implies** Col(ClimbLeft(C)) = Col(C) **and** Hgt(ClimbLeft(C)) = Hgt(C)  
Col(C) ≠ 0 **and**  
Screen::CellNature(Envi(C),Col(C)-1,Hgt(C)+1) **not in** {MTL, PLT, DOR, NGU }  
**and not exists** Guard g **in** Environment::CellContent(Envi(C),Col(C)-1,Hgt(C)+1)  
**and exists** Player p **in** Environment::CellContent(Envi(C),Col(C),Hgt(C)+1)  
**implies** Col(ClimbLeft(C)) = Col(C) **and** Hgt(ClimbLeft(C)) = Hgt(C)+1  
Col(C) ≠ 0 **and**  
Screen::CellNature(Envi(C),Col(C)-1,Hgt(C)+1) **not in** {MTL, PLT, DOR, NGU }  
**and not exists** Guard g **in** Environment::CellContent(Envi(C),Col(C)-1,Hgt(C)+1)  
**and not exists** Player p **in** Environment::CellContent(Envi(C),Col(C),Hgt(C)+1)  
**implies** Col(ClimbLeft(C)) = Col(C)-1 **and** Hgt(ClimbLeft(C)) = Hgt(C)+1

[ClimbRight]: Col(C) = Environment::Width(Envi(GoRight(C))) - 1  
**implies** Col(ClimbRight(C)) = Col(C) **and** Hgt(ClimbRight(C)) = Hgt(C)  
Screen::CellNature(Envi(C),Col(C)+1,Hgt(C)+1) **in** {MTL, PLT, DOR, NGU }  
**implies** Col(ClimbRight(C)) = Col(C) **and** Hgt(ClimbRight(C)) = Hgt(C)  
**exists** Guard g **in** Environment::CellContent(Envi(C),Col(C)+1,Hgt(C)+1)  
**implies** Col(ClimbRight(C)) = Col(C) **and** Hgt(ClimbRight(C)) = Hgt(C)  
Col(C) ≠ Environment::Width(Envi(GoRight(C))) - 1  
**and** Screen::CellNature(Envi(C),Col(C)+1,Hgt(C)+1) **not in** {MTL, PLT, DOR, NGU }  
**and not exists** Guard g **in** Environment::CellContent(Envi(C),Col(C)+1,Hgt(C)+1)  
**and exists** Player p **in** Environment::CellContent(Envi(C),Col(C),Hgt(C)+1)  
**implies** Col(ClimbRight(C)) = Col(C) **and** Hgt(ClimbRight(C)) = Hgt(C)+1  
Col(C) ≠ Environment::Width(Envi(GoRight(C))) - 1  
**and** Screen::CellNature(Envi(C),Col(C)+1,Hgt(C)+1) **not in** {MTL, PLT, DOR, NGU }  
**and not exists** Guard g **in** Environment::CellContent(Envi(C),Col(C)+1,Hgt(C)+1)  
**and not exists** Player p **in** Environment::CellContent(Envi(C),Col(C),Hgt(C)+1)  
**implies** Col(ClimbRight(C)) = Col(C)+1 **and** Hgt(ClimbRight(C)) = Hgt(C)+1

[MoveToInitCoords]: **exists** Guard g **in** Environment::CellContent(Envi(C),  
Coord::X(InitCoords(C)), Coord::Y(InitCoords(C))) **implies exists** g **in**  
Environment::CellContent(Envi(MoveToInitCoords(C)),  
Coord::X(InitCoords(g)), Coord::Y(InitCoords(g)))  
TimeInHole(MoveToInitCoords(C)) = 0  
Col(MoveToInitCoords(C)) = Coord::X(InitCoords(MoveToInitCoords(C)))  
Hgt(MoveToInitCoords(C)) = Coord::Y(InitCoords(MoveToInitCoords(C)))  
IdCounter(MoveToInitCoords(C)) = IdCounter(C)  
CarryingTreasure(MoveToInitCoords(C)) = CarryingTreasure(C)  
TimeLeftParalyzed(MoveToInitCoords(C)) = 0

[Paralyze]: CarryingTreasure(Paralyze(C)) = CarryingTreasure(C)  
TimeInHole(Paralyze(C)) = TimeInHole(C)  
Col(Paralyze(C)) = Col(C)  
Hgt(Paralyze(C)) = Hgt(C)  
IdCounter(Paralyze(C)) = IdCounter(C)  
TimeLeftParalyzed(Paralyze(C)) = 10

[Step]: **Falling(C) defined by**

(Environment::CellNature(Envi(C), Col(C), Hgt(C)) **not in** {LAD,HDR}  
**and** Environment::CellNature(Envi(C), Col(C), Hgt(C)-1) **in** {EMP,HDR,HOL,NPL}  
**and not exists** Guard g **in** Environment::CellContent(Envi(C), Col(C), Hgt(C)-1) )  
 TimeLeftParalyzed(C) = 0 **implies** TimeLeftParalyzed(Step(C))  
 TimeLeftParalyzed(C) > 0 **and** Falling **implies** TimeLeftParalyzed(Step(C)) = TimeLeftParalyzed(C)  
 TimeLeftParalyzed(C) > 0 **and not** Falling **implies** TimeLeftParalyzed(Step(C)) = TimeLeftParalyzed(C) - 1  
**exists** Treasure t **in** Environment::CellContent(Envi(C), Col(C), Hgt(C))  
**and not** CarryingTreasure(C)  
**implies** CarryingTreasure(Step(C))  
**and not exists** t **in** Environment::CellContent(Envi(Step(C)), Col(C), Hgt(C))  
**exists** Treasure t **in** Environment::CellContent(Envi(C), Col(C), Hgt(C))  
**and** CarryingTreasure(C)  
**implies** CarryingTreasure(Step(C))  
**and exists** t **in** Environment::CellContent(Envi(Step(C)), Col(C), Hgt(C))  
**not exists** Treasure t **in** Environment::CellContent(Envi(C), Col(C), Hgt(C))  
**and not** CarryingTreasure(C)  
**implies not** CarryingTreasure(Step(C))  
**and not exists** t **in** Environment::CellContent(Envi(Step(C)), Col(C), Hgt(C))  
**not exists** Treasure t **in** Environment::CellContent(Envi(C), Col(C), Hgt(C))  
**and** CarryingTreasure(C)  
**and** Environment::CellNature(Envi(C), Col(C), Hgt(C)-1) = HOL  
**and not** Environment::CellNature(Envi(C), Col(C), Hgt(C)) **in** {LAD, HDR, HOL}  
**and not exists** Guard g **in** Environment::CellContent(Envi(C), Col(C), Hgt(C)-1)  
**implies not** CarryingTreasure(Step(C))  
**and exists** Treasure t2 **in** Environment::CellContent(Envi(Step(C)), Col(C), Hgt(C))  
**not exists** Treasure t **in** Environment::CellContent(Envi(C), Col(C), Hgt(C))  
**and** CarryingTreasure(C)  
 (and Environment::CellNature(Envi(C), Col(C), Hgt(C)-1) ≠ HOL  
 or Environment::CellNature(Envi(C), Col(C), Hgt(C)) **in** {LAD, HDR, HOL}  
 or **exists** Guard g **in** Environment::CellContent(Envi(C), Col(C), Hgt(C)-1) )  
**implies** CarryingTreasure(Step(C))  
**and not exists** Treasure t2 **in** Environment::CellContent(Envi(Step(C)), Col(C), Hgt(C))  
 TimeLeftParalyzed(C) = 0 **and** Environment::CellNature(Envi(C), Col(C), Hgt(C)) = HOL  
**and** TimeInHole(C) < 5  
**implies** TimeInHole(Step(C)) = TimeInHole(C)+1  
 TimeLeftParalyzed(C) = 0 **and** Environment::CellNature(Envi(C), Col(C), Hgt(C)) = HOL  
**and** TimeInHole(C) ≥ 5  
**and** Behaviour(C) = MOVELEFT  
**implies** TimeInHole(Step(C)) = 0 **and** Step(C) = ClimbLeft(C)  
**and** TimeInHole(C) ≥ 5  
**and** Behaviour(C) = MOVER  
**implies** TimeInHole(Step(C)) = 0 **and** Step(C) = ClimbRight(C)  
 Falling **implies** Step(C) = GoDown(C)  
**not** Falling **and** TimeLeftParalyzed(C) = 0  
**and** Environment::CellNature(Envi(C), Col(C), Hgt(C)) ≠ HOL  
**and** Behaviour(C) = MOVELEFT  
**implies** Step(C) = GoLeft(C)  
**not** Falling **and** TimeLeftParalyzed(C) = 0  
**and** Environment::CellNature(Envi(C), Col(C), Hgt(C)) ≠ HOL  
**and** Behaviour(C) = MOVER  
**implies** Step(C) = GoRight(C)  
**not** Falling **and** TimeLeftParalyzed(C) = 0  
**and** Environment::CellNature(Envi(C), Col(C), Hgt(C)) ≠ HOL  
**and** Behaviour(C) = MOVEU  
**implies** Step(C) = GoUp(C)  
**not** Falling **and** TimeLeftParalyzed(C) = 0  
**and** Environment::CellNature(Envi(C), Col(C), Hgt(C)) ≠ HOL  
**and** Behaviour(C) = MOVED  
**implies** Step(C) = GoDown(C)  
 IdCounter(Step(C)) = IdCounter(C)

*Les fonctions de déplacements de Guard sont quasiment les mêmes que celles de Character, on change seulement le fait qu'on ne puisse pas aller dans une case NGU*

```
[GoLeft]:  Hgt(GoLeft(C)) = Hgt(C)
           Col(C) = 0 implies Col(GoLeft(C)) = Col(C)
           Environment::CellNature(Envi(C),Col(C)-1,Hgt(C)) in {MTL, PLT, DOR, NGU}
             implies Col(GoLeft(C)) = Col(C)
           Environment::CellNature(Envi(C),Col(C),Hgt(C)) not in {LAD, HDR}
             and Environment::CellNature(Envi(C),Col(C),Hgt(C)-1) not in {PLT, MTL, LAD,DOR, NGU}
             and not exists Guard g in Environment::CellContent(Envi(C),Col(C),Hgt(C)-1)
             implies Col(GoLeft(C)) = Col(C)
           exists Guard g in Environment::CellContent(Envi(C),Col(C)-1,Hgt(C))
             implies Col(GoLeft(C)) = Col(C)
           (Col(C) ≠ 0) and Environment::CellNature(Envi(C),Col(C)-1,Hgt(C)) not in {MTL, PLT,DOR, NGU}
             and (Environment::CellNature(Envi(C),Col(C),Hgt(C)) in {LAD, HDR}
                 or Environment::CellNature(Envi(C),Col(C),Hgt(C)-1) in {PLT, MTL, LAD,DOR, NGU}
                 or exists Guard g in Environment::CellContent(Envi(C),Col(C),Hgt(C)-1) )
             and not (exists Guard g in Environment::CellContent(Envi(C),Col(C)-1,Hgt(C)))
             implies Col(GoLeft(C)) = Col(C)-1

[GoRight]: Hgt(GoRight(C)) = Hgt(C)
           Col(C) = Environment::Width(Envi(GoRight(C))) - 1 implies Col(GoRight(C)) = Col(C)
           Environment::CellNature(Envi(C),Col(C)+1,Hgt(C)) in {MTL, PLT, DOR, NGU}
             implies Col(GoRight(C)) = Col(C)
           Environment::CellNature(Envi(C),Col(C),Hgt(C)) not in {LAD, HDR}
             and Environment::CellNature(Envi(C),Col(C),Hgt(C)-1) not in {PLT, MTL, LAD,DOR, NGU}
             and not exists Guard g in Environment::CellContent(Envi(C),Col(C),Hgt(C)-1)
             implies Col(GoRight(C)) = Col(C)
           exists Guard g in Environment::CellContent(Envi(C),Col(C)+1,Hgt(C))
             implies Col(GoRight(C)) = Col(C)
           (Col(C) ≠ Environment::Width(Envi(GoRight(C))) - 1)
             and Environment::CellNature(Envi(C),Col(C)+1,Hgt(C)) not in {MTL, PLT,DOR, NGU}
             and (Environment::CellNature(Envi(C),Col(C),Hgt(C)) in {LAD, HDR}
                 or Environment::CellNature(Envi(C),Col(C),Hgt(C)-1) in {PLT, MTL, LAD,DOR, NGU}
                 or exists Guard g in Environment::CellContent(Envi(C),Col(C),Hgt(C)-1) )
             and not (exists Guard g in Environment::CellContent(Envi(C),Col(C)+1,Hgt(C)))
             implies Col(GoRight(C)) = Col(C)+1

[GoUp]:    Col(GoUp(C)) = Col(C)
           Hgt(C) = Environment::Height(Envi(GoUp(C))) - 1 implies Hgt(GoUp(C)) = Hgt(C)
           Environment::CellNature(Envi(C),Col(C),Hgt(C)+1) in {MTL, PLT, DOR, NGU}
             implies Hgt(GoUp(C)) = Hgt(C)
           Environment::CellNature(Envi(C),Col(C),Hgt(C)) ≠ LAD implies Hgt(GoUp(C)) = Hgt(C)
           exists Guard g in Environment::CellContent(Envi(C),Col(C),Hgt(C)+1)
             implies Hgt(GoUp(C)) = Hgt(C)
           (Hgt(C) ≠ Environment::Height(Envi(GoUp(C))) - 1)
             and Environment::CellNature(Envi(C),Col(C),Hgt(C)+1) not in {MTL, PLT, DOR, NGU}
             and Environment::CellNature(Envi(C),Col(C),Hgt(C)) = LAD
             and exists Guard g in Environment::CellContent(Envi(C),Col(C),Hgt(C)+1)
             implies Hgt(GoUp(C)) = Hgt(C)+1

[GoDown]:  Col(GoDown(C)) = Col(C)
           Hgt(C) = 0 implies Hgt(GoDown(C)) = Hgt(C)
           Environment::CellNature(Envi(C),Col(C),Hgt(C)-1) in {MTL, PLT, DOR, NGU}
             implies Hgt(GoDown(C)) = Hgt(C)
           exists Guard g in Environment::CellContent(Envi(C),Col(C),Hgt(C)-1)
             implies Hgt(GoDown(C)) = Hgt(C)
           (Hgt(C) ≠ 0)
             and Environment::CellNature(Envi(C),Col(C),Hgt(C)-1) not in {MTL, PLT, DOR, NGU}
             and exists Guard g in Environment::CellContent(Envi(C),Col(C),Hgt(C)-1)
             implies Hgt(GoDown(C)) = Hgt(C)-1
```

# Moteur

**Service:** Engine

**Observers:** **const** **CommandManager:** [Engine] → CommandManager  
**Environment:** [Engine] → Environment  
**Player:** [Engine] → Player  
**Guards:** [Engine] → List{Guard}  
**Treasures:** [Engine] → List{Treasure}  
**Status:** [Engine] → Status  
**NextCommand:** [Engine] → Command  
**Holes:** [Engine] → Set{Hole}  
**NbLives:** [Engine] → int  
**Score:** [Engine] → int  
**ScoreAtStartOfLevel:** [Engine] → int  
**ScreenManager:** [Engine] → ScreenManager  
**NbTreasuresLeft:** [Engine] → int  
**CurrentLevel:** [Engine] → int

**Constructors:** **init:** ScreenManager × CommandManager × Engine → Engine  
**pre init(sm,cm,e) requires** sm ≠ null **and** ScreenManager::NbScreen(sm) ≥ 1

**Operators:** **Step:** [Engine] → [Engine]  
**pre Step(E) requires** Status(E) = **Playing**  
**AddHole:** [Engine] × int × int → [Engine]  
**pre AddHole(E,x,y) requires not exists** Hole h **in** Holes(E)  
**with** (Hole::X(h) = x **and** Hole::Y(h) = y)  
**and** Environment::CellNature(Environment(E), x, y) = **HOL**  
**Display:** [Engine] → [Engine]

**Observations:**  
**[invariants]:**  
**[init]:** Environment::Height(Environment(init(sm,cm,e))) = Screen::Width(ScreenManager::Screen(sm,0))  
Environment::Width(Environment(init(sm,cm,e))) = Screen::Height(ScreenManager::Screen(sm,0))  
**forall** (i,j) **in** [0;Environment::Width(Environment(init(sm,cm,e)))]  
[0;Environment::Height(Environment(init(sm,cm,e)))]  
Screen::CellNature(ScreenManager::Screen(sm, 0), i, j)  
= Screen::CellNature(Environment(init(sm,cm,e), i, j)  
Player::Col(Player(init(sm,cm,e))) = Coord::X(ScreenManager::PlayerFromScreen(sm, 0))  
Player::Hgt(Player(init(sm,cm,e))) = Coord::Y(ScreenManager::PlayerFromScreen(sm, 0))  
Player::Engine(Player(init(sm,cm,e))) = e  
**forall** CoordItem c **in** ScreenManager::ItemsFromScreen(sm, 0),  
**exists** Item i **in** Treasures(init(sm,cm,e))  
**with** (Item::Hgt(i) = CoordItem::Y(c) **and** Item::Col(i) = CoordItem::X(c)  
**and** Item::Nature(i) = CoordItem::ItemType(c))  
**forall** CoordGuard c **in** ScreenManager::GuardsFromScreen(sm, 0),  
**exists** Guard g **in** Guards(init(sm,cm,e))  
**with** (Guard::Hgt(g) = CoordGuard::Y(c) **and** Guard::Col(i) = CoordGuard::X(c)  
**and** Guard::Nature(i) = CoordGuard::Type(c))  
Status(init(sm,cm,e)) = **Playing**  
NextCommand(init(sm,cm,e)) = **NONE**  
Holes(init(sm,cm,e)) = {}  
NbLives(init(sm,cm,e)) = 3  
Score(init(sm,cm,e)) = 0  
ScoreAtStartOfLevel(init(sm,cm,e)) = 0  
ScreenManager(init(sm,cm,e)) = sm  
NbTreasuresLeft(init(sm,cm,e)) = **count** CoordItem c **in**  
ScreenManager::ItemsFromScreen(sm,0) **with** (CoordItem::ItemType(c) = Treasure)  
CurrentLevel(init(sm, cm, e)) = 0  
CommandManager(init(sm, cm, e)) = cm

```

[Step]:  loadlevel(E, no)(C) defined by
    CurrentLevel(Step(E)) = no
    and Status(Step(E)) = Playing
    and Status(Step(E)) = Playing
    and Environment::Height(Environment(Step(E)) = Screen::Width(ScreenManager::Screen(sm,no))
    and Environment::Width(Environment(Step(E)) = Screen::Height(ScreenManager::Screen(sm,no))
    and forall (i,j) in [0;Environment::Width(Environment(Step(E)))[
        [0;Environment::Height(Environment(Step(E)))[,
        Screen::CellNature(ScreenManager::Screen(sm, no), i, j) =
        Screen::CellNature(Environment(Step(E), i, j)
    and Player::Col(Player(Step(E)) = Coord::X(ScreenManager::PlayerFromScreen(sm, no))
    and Player::Hgt(Player(Step(E)) = Coord::Y(ScreenManager::PlayerFromScreen(sm, no))
    and forall CoordItem c in ScreenManager::ItemsFromScreen(sm, 0),
        exists Item i in Treasures(Step(E))
            with (Item::Hgt(i) = CoordItem::Y(c) and Item::Col(i) = CoordItem::X(c)
                and Item::Nature(i) = CoordItem::ItemType(c))
    and forall CoordGuard c in ScreenManager::GuardsFromScreen(sm, 0),
        exists Guard g in Guards(Step(E))
            with (Guard::Hgt(g) = CoordGuard::Y(c) and Guard::Col(i) = CoordGuard::X(c)
                and Guard::Nature(i) = CoordGuard::Type(c))
    and Status(Step(E)) = Playing
    and NextCommand(Step(E)) = NONE
    and Holes(Step(E)) = {}
    and NbLives(Step(E)) = NbLives(E) - 1
    and Score(Step(E)) = Score(E)
    and ScoreAtStartOfLevel(Step(E)) = Score(E)
    and ScreenManager(Step(E)) = ScreenManager(E)
    and NbTreasuresLeft(Step(E)) = count CoordItem c in
        ScreenManager::ItemsFromScreen(sm,no) with (CoordItem::ItemType(c) = Treasure)
    death(E) defined by
        (NbLives(E) = 1 implies NbLives(Step(E)) = 0 and Status(Step(E)) = Loss)
    and (NbLives(E) > 1
        implies NbLives(Step(E)) = NbLives(E) -1
            and NbLives(Step(E)) = NbLives(E) -1
            and Score(Step(E)) = ScoreAtStartOfLevel(E)
            and loadlevel(E, CurrentLevel(E)) )
    CommandManager(E) ≠ null
        implies NextCommand(Step(E)) = CommandManager::CurrentCommand(CommandManager(E))
    CommandManager(E) = null
        implies NextCommand(Step(E)) = NONE
    exists Guard g in Environment::CellContent(Envi(E), Player::Col(Player(E)), Player::Hgt(Player(E)))
        and NbLives(E) = 1
        implies NbLives(Step(E)) = 0 and Status(Step(E)) = Loss
    exists Guard g in Environment::CellContent(Envi(E), Player::Col(Player(E)), Player::Hgt(Player(E)))
        and NbLives(E) > 1
        implies death(E)
    not exists Guard g in Environment::CellContent(Envi(E), Player::Col(Player(E)), Player::Hgt(Player(E)))
        and exists Treasure t in Environment::CellContent(Envi(E), Player::Col(Player(E)), Player::Hgt(Player(E)))
        implies t not in Treasure(Step(E))
        and NbTreasuresLeft(Step(E)) = NbTreasuresLeft(E)-1
        and Score(Step(E)) = Score(E)+1
        and (NbTreasuresLeft(E) = 1
            and CurrentLevel(E) < ScreenManager::NbScreen(ScreenManager(E)) - 1
            implies CurrentLevel(Step(E)) = CurrentLevel(E)+1
            and loadlevel(E, CurrentLevel(E)) )
        and (NbTreasuresLeft(E) = 1
            and CurrentLevel(E) = ScreenManager::NbScreen(ScreenManager(E)) - 1
            implies CurrentLevel(Step(E)) = CurrentLevel(E)
            and Status(Step(E)) = Win

```

[Step]: **not exists** Guard g **in** Environment::CellContent(Envi(E), Player::Col(Player(E)), Player::Hgt(Player(E)))  
**and exists** Item i **in** Environment::CellContent(Envi(E), Player::Col(Player(E)), Player::Hgt(Player(E)))  
**implies** Item::Nature(Player::CurrentlyHeldItem(Player(Step(E))) = Item::Nature(i)  
**not exists** Guard g **in** Environment::CellContent(Envi(E), Player::Col(Player(E)), Player::Hgt(Player(E)))  
**and** Environment::CellNature(Envi(E), Player::Col(Player(E)), Player::Hgt(Player(E)) - 1) = **TRP**  
**implies** Environment::CellNature(Envi(Step(E)),  
Player::Col(Player(E)), Player::Hgt(Player(E)) - 1) = **EMP**  
**not** ( **exists** Treasure tin Environment::CellContent(Envi(E), Player::Col(Player(E)), Player::Hgt(Player(E)))  
**and** NbTreasuresLeft(E) = 1)  
**and not exists** Guard g  
**in** Environment::CellContent(Envi(E), Player::Col(Player(E)), Player::Hgt(Player(E)))  
**implies forall** Hole h **in** Holes(E),  
( Hole::Time(h) < 14 **implies exists** Hole o  
**with** (Hole::X(o) = Hole::X(h) **and** Hole::Y(o) == Hole::Y(h) **and** Hole::Time(o) = Hole::Time(h)) )  
**and** ( Hole::Time(h) = 14 **implies not exists** Hole o  
**with** (Hole::X(o) = Hole::X(h) **and** Hole::Y(o) == Hole::Y(h)) )  
**and** ( Hole::Time(h) = 14 **and** Player::X(Player(E)) = Hole::X(h)  
**and** Player::Y(Player(E)) = Hole::Y(h)  
**implies death(E)** )  
**not exists** Hole h **in** Holes(E) **with** (Hole::Time(h) = 14 **and** Hole::X(h) = Player::Col(Player(E))  
**and** Hole::Y(h) = Player::Hgt(Player(E)) )  
**and not exists** Guard g **in**  
Environment::CellContent(Envi(E), Player::Col(Player(E)), Player::Hgt(Player(E)))  
**and not (exists** Treasure tin  
Environment::CellContent(Envi(E), Player::Col(Player(E)), Player::Hgt(Player(E)))  
**and** NbTreasuresLeft(E) = 1)  
**implies** Status(Step(E)) = Playing

[AddHole]: Holes(AddHole(E,x,y)) = Holes(E) **union** Hole h **with** (Hole::X(h) = x **and** Hole::Y(h) = y)  
Environment(AddHole(E,x,y)) = Environment(E)  
Player(AddHole(E,x,y)) = Player(E)  
Guards(AddHole(E,x,y)) = Guards(E)  
Treasures(AddHole(E,x,y)) = Treasures(E)  
Status(AddHole(E,x,y)) = Status(E)  
NextCommand(AddHole(E,x,y)) = NextCommand(E)  
NbLives(AddHole(E,x,y)) = NbLives(E)  
Score(AddHole(E,x,y)) = Score(E)  
ScoreAtStartOfLevel(AddHole(E,x,y)) = ScoreAtStartOfLevel(E)  
ScreenManager(AddHole(E,x,y)) = ScreenManager(E)  
NbTreasuresLeft(AddHole(E,x,y)) = NbTreasuresLeft(E)  
CurrentLevel(AddHole(E,x,y)) = CurrentLevel(E)

[Display]: Environment(AddHole(E,x,y)) = Environment(E)  
Player(Display(E)) = Player(E)  
Guards(Display(E)) = Guards(E)  
Treasures(Display(E)) = Treasures(E)  
Status(Display(E)) = Status(E)  
NextCommand(Display(E)) = NextCommand(E)  
Holes(Display(E)) = Holes(E)  
NbLives(Display(E)) = NbLives(E)  
Score(Display(E)) = Score(E)  
ScoreAtStartOfLevel(Display(E)) = ScoreAtStartOfLevel(E)  
ScreenManager(Display(E)) = ScreenManager(E)  
NbTreasuresLeft(Display(E)) = NbTreasuresLeft(E)  
CurrentLevel(Display(E)) = CurrentLevel(E)



# Gestionnaire d'écran

**Service:** ScreenManager

**Observers:** NbScreen: [ScreenManager]  $\rightarrow$  int  
 LevelSetup: [ScreenManager]  $\times$  int  $\rightarrow$  LevelSetup  
     **pre** LevelSetup(S,i) **requires**  $0 \leq i < \text{NbScreen}(S)$   
 Screen: [ScreenManager]  $\times$  int  $\rightarrow$  EditableScreen  
     **pre** Screen(S,i) **requires**  $0 \leq i < \text{NbScreen}(S)$   
 GuardsFromScreen: [ScreenManager]  $\times$  int  $\rightarrow$  List{CoordGuard}  
     **pre** GuardsFromScreen(S,i) **requires**  $0 \leq i < \text{NbScreen}(S)$   
 ItemsFromScreen: [ScreenManager]  $\times$  int  $\rightarrow$  List{CoordItem}  
     **pre** ItemsFromScreen(S,i) **requires**  $0 \leq i < \text{NbScreen}(S)$   
 PlayerFromScreen: [ScreenManager]  $\times$  int  $\rightarrow$  Coord  
     **pre** PlayerFromScreen(S,i) **requires**  $0 \leq i < \text{NbScreen}(S)$

**Constructors:** init:  $\rightarrow$  [ScreenManager]

**Operators:** AddScreen: [ScreenManager]  $\times$  EditableScreen  $\times$  List{CoordGuard}  $\times$  List{CoordItem}  $\times$  Coord  
      $\rightarrow$  [ScreenManager]  
     **pre** AddScreen(S,es,g,i,p) **requires**  $p \neq \text{null}$  **and**  $es \neq \text{null}$   
 RemoveScreen: [ScreenManager]  $\times$  int  $\rightarrow$  [ScreenManager]  
     **pre** RemoveScreen(S,i) **requires**  $0 \leq i < \text{NbScreen}(S)$

**Observations:**

[invariants]: Screen(S, i) **min** LevelSetup::Screen(LevelSetup(S, i))  
 GuardsFromScreen(S, i) **min** LevelSetup::Guards(LevelSetup(S, i))  
 ItemsFromScreen(S, i) **min** LevelSetup::Items(LevelSetup(S, i))  
 PlayerFromScreen(S, i) **min** LevelSetup::Player(LevelSetup(S, i))

[init]: NbScreen(init()) = 0

[AddScreen]: NbScreen(AddScreen(S,es,g,i,p)) = NbScreen(S) + 1  
 Screen(AddScreen(S,es,g,i,p), NbScreen(S)) = es  
 PlayerFromScreen(AddScreen(S,es,g,i,p), NbScreen(S)) = p  
 $g = \text{null}$  **implies** GuardsFromScreen(AddScreen(S,es,g,i,p), NbScreen(S)) = {}  
 $g \neq \text{null}$  **implies** GuardsFromScreen(AddScreen(S,es,g,i,p), NbScreen(S)) = g  
 $i = \text{null}$  **implies** ItemsFromScreen(AddScreen(S,es,g,i,p), NbScreen(S)) = {}  
 $i \neq \text{null}$  **implies** ItemsFromScreen(AddScreen(S,es,g,i,p), NbScreen(S)) = i  
**forall** cpt in [0, NbScreen(S) [,  
     LevelSetup(AddScreen(S,es,g,i,p), cpt) = LevelSetup(S, cpt)

[RemoveScreen]: NbScreen(RemoveScreen(S,i)) = NbScreen(S) - 1  
**forall** cpt in [0, NbScreen(S) [,  
      $\text{cpt} < i$  **implies** LevelSetup(RemoveScreen(S,i), cpt) = LevelSetup(S, cpt)  
      $\text{cpt} \geq i$  **implies** LevelSetup(RemoveScreen(S,i), cpt) = LevelSetup(S, cpt + 1)