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> with(LinearAlgebra):      -- This loads the LinearAlgebra package
> A:=Matrix([[0,2,1],[1,0,2],[1,2,0]]);

      A :=  $\begin{bmatrix} 0 & 2 & 1 \\ 1 & 0 & 2 \\ 1 & 2 & 0 \end{bmatrix}$ 
(1)

> B:=Matrix([[1,2,4,1],[3,4,5,1],[4,5,6,1]]);

      B :=  $\begin{bmatrix} 1 & 2 & 4 & 1 \\ 3 & 4 & 5 & 1 \\ 4 & 5 & 6 & 1 \end{bmatrix}$ 
(2)

> u:=<1,2,3>;      -- a column vector

      u :=  $\begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$ 
(3)

> v:=<5,2,1>;

      v :=  $\begin{bmatrix} 5 \\ 2 \\ 1 \end{bmatrix}$ 
(4)

> A.B;      -- matrix multiplication

       $\begin{bmatrix} 10 & 13 & 16 & 3 \\ 9 & 12 & 16 & 3 \\ 7 & 10 & 14 & 3 \end{bmatrix}$ 
(5)

> A.u;

       $\begin{bmatrix} 7 \\ 7 \\ 5 \end{bmatrix}$ 
(6)

> u.v;      -- dot product

      12
(7)

> ReducedRowEchelonForm(A);

       $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$ 
(8)

> ReducedRowEchelonForm(B);

(9)

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$$\begin{bmatrix} 1 & 0 & 0 & -1 \\ 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix} \quad (9)$$

**> MatrixInverse(A);**

$$\begin{bmatrix} -\frac{2}{3} & \frac{1}{3} & \frac{2}{3} \\ \frac{1}{3} & -\frac{1}{6} & \frac{1}{6} \\ \frac{1}{3} & \frac{1}{3} & -\frac{1}{3} \end{bmatrix} \quad (10)$$

**> Transpose(B);**

$$\begin{bmatrix} 1 & 3 & 4 \\ 2 & 4 & 5 \\ 4 & 5 & 6 \\ 1 & 1 & 1 \end{bmatrix} \quad (11)$$

**> Eigenvalues(A);**

$$\begin{bmatrix} 3 \\ -2 \\ -1 \end{bmatrix} \quad (12)$$

**> Eigenvectors(A);**

-- The columns of the matrix are eigenvectors.

$$\begin{bmatrix} -1 \\ 3 \\ -2 \end{bmatrix}, \begin{bmatrix} -3 & 1 & 1 \\ 1 & 1 & -\frac{3}{2} \\ 1 & 1 & 1 \end{bmatrix} \quad \begin{array}{l} \text{They are listed in the} \\ \text{same order as the} \\ \text{eigenvalues.} \end{array} \quad (13)$$