

1. An object is moving so that its position at time t is given by the vector function

$$\vec{r}(t) = \langle t, t + 1, t^2 \rangle.$$

Find the tangent component and the normal component of the acceleration \vec{a} at $t = 2$.
Then decompose $\vec{a}(1)$ as

$$\vec{a}(1) = \alpha_T \vec{T} + \alpha_N \vec{N}.$$

(Some fractions may appear.)

2. Reparametrize the curve

$$\vec{r}(t) = \left\langle \frac{2}{t^2 + 1} - 1, \frac{2t}{t^2 + 1}, 1 \right\rangle$$

with respect to arc length measured from point $(1, 0, 1)$ in the direction of increasing t .
Express the reparametrization in its simplest form.