

<b>Code</b>	<b>MONTE_CARLO_SIMULATION.PY</b>
<b>Author</b>	Nathaniel Heatwole, PhD ( <a href="mailto:heatwolen@gmail.com">heatwolen@gmail.com</a> ) ( <a href="#">GitHub</a> ) ( <a href="#">LinkedIn</a> )
<b>Summary</b>	Uses Monte Carlo simulation to test the central limit theorem, by generating and averaging random draws from several constituent distributions
<b>Methods/ Process</b>	<p><a href="#">Monte Carlo simulation</a></p> <ul style="list-style-type: none"> <li>- Method for evaluating complex probability spaces, where the output depends on several constituent probability distributions</li> <li>- Constituent distributions can be of any type/family (discrete or continuous)</li> <li>- Especially useful in cases where closed-form analytic solutions do not exist</li> <li>- Number of observations chosen should adequately cover the sample space and generate stable output distribution</li> </ul> <p><a href="#">Central limit theorem</a></p> <ul style="list-style-type: none"> <li>- Average value of sequence of random variables (independently sampled) is normally distributed</li> <li>- Asymptotically correct, as number of distributions (and observations sampled from each) increases</li> <li>- Holds regardless of types or parameters of constituent distributions</li> </ul> <p>Steps</p> <ol style="list-style-type: none"> <li>1. Define constituent distributions</li> <li>2. Generate one random sample from each distribution (sampling independently)</li> <li>3. Compute average value of those random samples (rowwise)</li> <li>4. Repeat for many sets of random draws (sampling with replacement)</li> <li>5. Assess distribution of average value (columnwise, across all trials)</li> </ol>
<b>Training Data</b>	<p>Constituent distributions</p> <ul style="list-style-type: none"> <li>- 10 <a href="#">triangular</a> (three-parameter: minimum, mode, maximum)</li> <li>- Fixed-width, non-overlapping, and abutting (no gaps)</li> <li>- Mode value alternating between minimum and maximum values</li> <li>- Each is highly non-normal (skewed, with linear density segments)</li> <li>- Resembles sawtooth wave when all are viewed together</li> <li>- 1 million random draws from each</li> </ul>
<b>Results</b>	Average value distribution is smooth bell-shaped curve (as the central limit theorem predicts), even though all constituent distributions are highly non-normal