

USN 15CS54

Fifth Semester B.E. Degree Examination, Dec.2018/Jan.2019 **Automata Theory and Computability**

Time: 3 hrs. Max. Marks: 80

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- 1 a. Define the following with example:
 - i) String ii) Language iii) Alphabet
- iv) DFSM.
- (08 Marks)

- b. Design a DFSM to accept each of the following languages:
 - i) $L = \{W \in \{0, 1\}^* : W \text{ has } 001 \text{ as a substring}\}\$
 - ii) $L = \{W \in \{a, b\}^* : W \text{ has even number of a's and even number of b's} \}.$

(08 Marks)

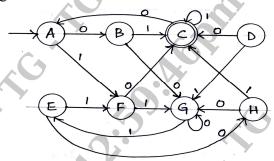
OR

2 a. Define NDFSM. Convert the following NDFSM to its equivalent DFSM. (08 Marks)



b. Minimize the following DFSM.

(08 Marks)



Module-2

- 3 a. Define Regular expression and write Regular expression for the following language.
 - i) $L = \{a^{2n} b^{2m} \mid n \ge 0, m \ge 0\}$

(08 Marks)

- ii) $L = \{a^n b^m \mid m \ge 1, n \ge 1, nm \ge 3\}.$
- b. Obtain the Regular expression for the following FSM.

(08 Marks)



OR

- 4 a. Define a Regular grammar. Design regular grammars for the following languages.
 - i) Strings of a's and b's with at least one a.
 - ii) Strings of a's and b's having strings without ending with ab.
 - iii) Strings of 0's and 1's with three consecutive 0's.

(08 Marks)

b. State and prove pumping theorem for regular languages.

(08 Marks)

Module-3

- Define context free grammar. Design a context free grammar for the languages. 5 (08 Marks)
 - i) $L = \{0^m \ 1^m \ 2^n \mid m \ge 0 , n \ge 0\}$
- $L = \{a^1 b^j \mid i \neq j, i \geq 0, j \geq 0\}$ ii)
- iii) $L = \{a^n b^{n-3} \mid n \ge 3\}.$
- b. Consider the grammar G with production

 $S \rightarrow AbB$

 $A \rightarrow aA \in$

(08 Marks)

 $B \rightarrow aB \mid bB \mid \in$

Obtain leftmost derivation, rightmost derivation and parse tree for the string aaabab.

OR

- Define a PDA. Obtain a PDA to accept
 - $L = \{a^n b^n \mid W \in \{a, b\}^*\}$. Draw the transition diagram.

(08 Marks)

b. Convert the following grammar into equivalent PDA.

 $S \rightarrow aABC$

 $A \rightarrow aB|a$

(08 Marks)

 $B \rightarrow bA|b$ $C \rightarrow a$.

Module-4

- State and prove pumping lemma for context free languages. Show that 7 (10 Marks) $L = \{a^n b^n c^n \mid n \ge 0\}$ is not context free.
 - Explain Turing machine model.

(06 Marks)

(08 Marks)

OR

- Design a Turing machine to accept the language $L = \{0^n \ 1^n \ 2^n \mid n \ge 1\}$. 8 (08 Marks)
 - Design a Turing machine to accept strings of a's and b's ending with ab or ba.

<u> Module-5</u>

- Explain the following: 9
 - i) Non deterministic Turing machine
- ii) Multi tape Turing machine.

(06 Marks)

- Define the following:
 - i) Recursively enumerable language ii) Decidable language.
- (06 Marks)

What is Post correspondence problem?

(04 Marks)

10 What is Halting problem of Turing machine?

(06 Marks)

- Define the following: i) Quantum computer
- Class NP. (06 Marks)

Explain Church Turing Thesis.

(04 Marks)