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Online Charge Scheduling for Electric Vehicles in Autonomous Mobility on Demand Fleets

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Motivation



System Description



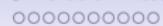
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Personal Urban Mobility

Personal Urban Mobility

- Three rapidly developing technologies:

Personal Urban Mobility

- Three rapidly developing technologies:
 - Autonomous Vehicles
 - Mobility-on-Demand
 - Plug-in Electric Vehicles

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- Three rapidly developing technologies:
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- Literature addressing the potential synergies is sparse

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- Specifically, let us consider a fleet of autonomous mobility-on-demand electric vehicles (AMoD EVs)

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- Three rapidly developing technologies:
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- Specifically, let us consider a fleet of autonomous mobility-on-demand electric vehicles (AMoD EVs)
 - Transport customers from origin to destination

Personal Urban Mobility

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- Literature addressing the potential synergies is sparse
- Specifically, let us consider a fleet of autonomous mobility-on-demand electric vehicles (AMoD EVs)
 - Transport customers from origin to destination
 - Must recharge periodically to remain in operation

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Benefits of AMoD EV Fleets

- How can we optimize this system?

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Benefits of AMoD EV Fleets

- How can we optimize this system?
 - Smart Charging

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 - Reduce electricity usage during peak hours - benefits the grid

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Benefits of AMoD EV Fleets

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 - Predict where are vehicles needed next - benefits customer
 - Limit out-of-service time of EVs - benefits fleet dispatcher

Managing such a system is possible...but it is a challenging problem

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Why is AMoD EV Fleet Smart Charging and Routing challenging?

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- AMoD EVs enter the “between-ride” state at random times throughout the day

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- Information is revealed in an online fashion
 - Do not know next customer’s trip length
 - Do not know traffic conditions

Why is AMoD EV Fleet Smart Charging and Routing challenging?

- AMoD EVs enter the “between-ride” state at random times throughout the day
- Information is revealed in an online fashion
 - Do not know next customer's trip length
 - Do not know traffic conditions
- Need to manage the fleet without knowledge of future
 - Mobility-on-Demand arrival distributions highly nonstationary
 - Tool of choice: Online Optimization (instead of MPC)
 - Accounts for adversarial input sequences

Why is AMoD EV Fleet Smart Charging and Routing challenging?

- Fleet charging facilities contain **shared resources**
 - Fleet vehicles need sufficient energy levels to serve customers
 - Which vehicle is granted charger usage?
 - Varying electricity prices

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- Fleet EVs need to be rebalanced throughout the service area
 - Route vehicles to serve future rides in the service area

Require **online** scheduling systems for **routing decisions** and **shared resource** allocation to enable **smart charging** for fleet EVs in the between-ride state

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- D regions within a service area \mathcal{D}



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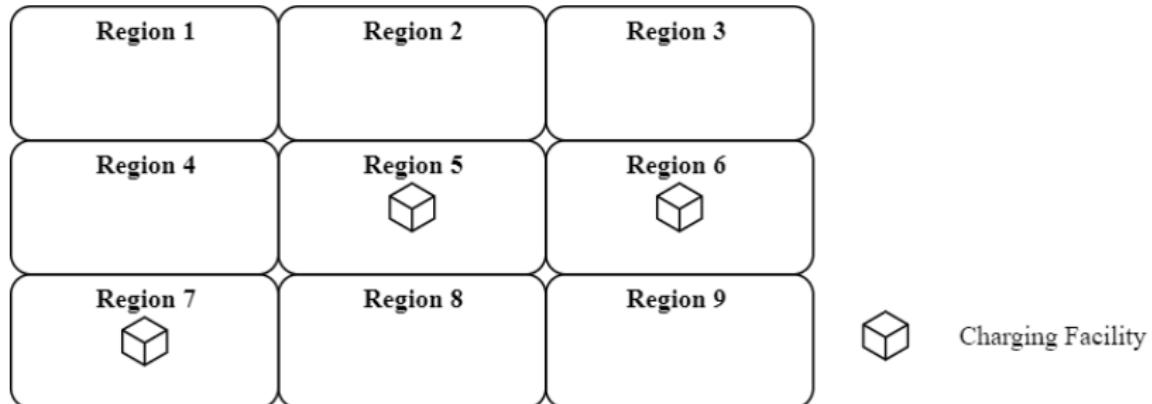
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System Description

- F charging facilities within service area \mathcal{D}



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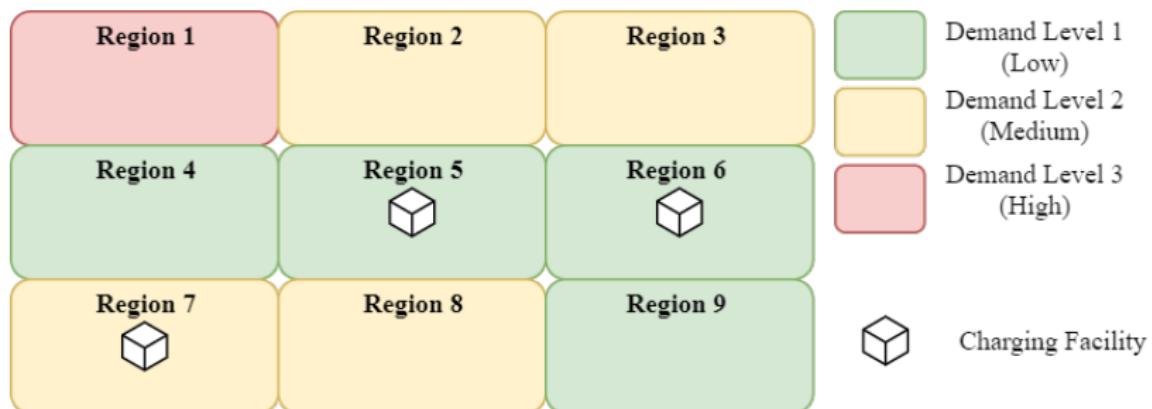
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System Description

- Varying customer demand across regions



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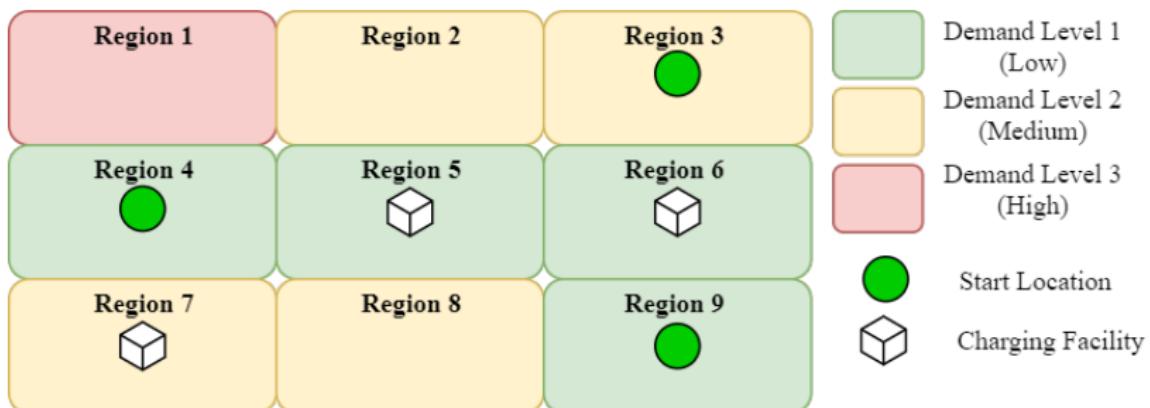
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System Description

- AMoD EVs enter the between-ride state



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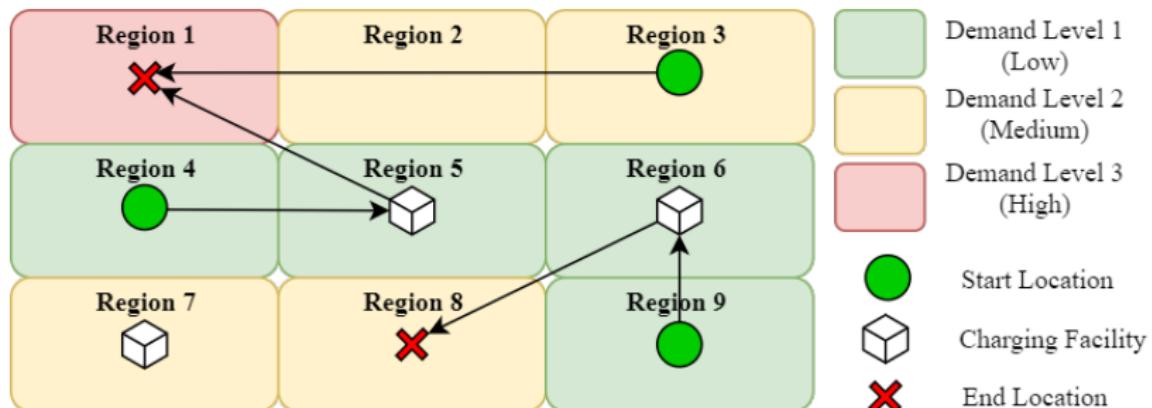
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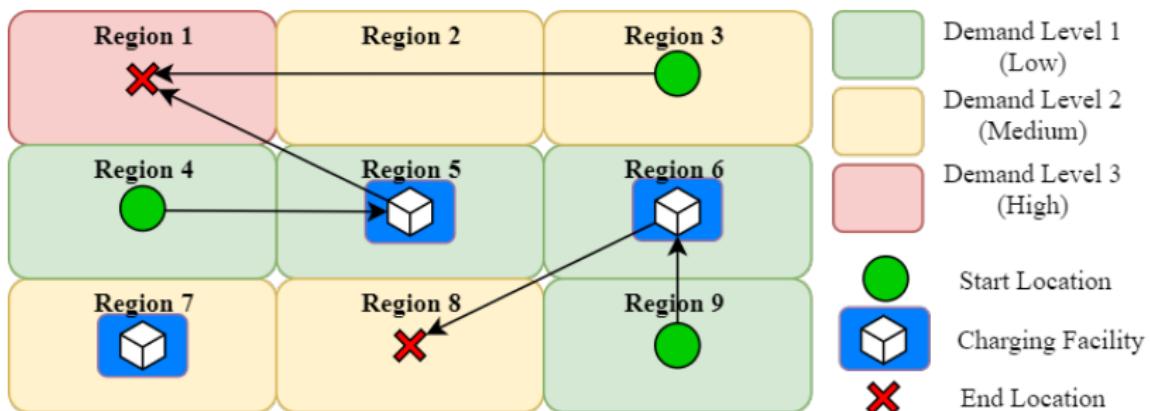
System Description

- EVs select between-ride charging schedules and next stops



System Description

- Now let's examine the charging facilities



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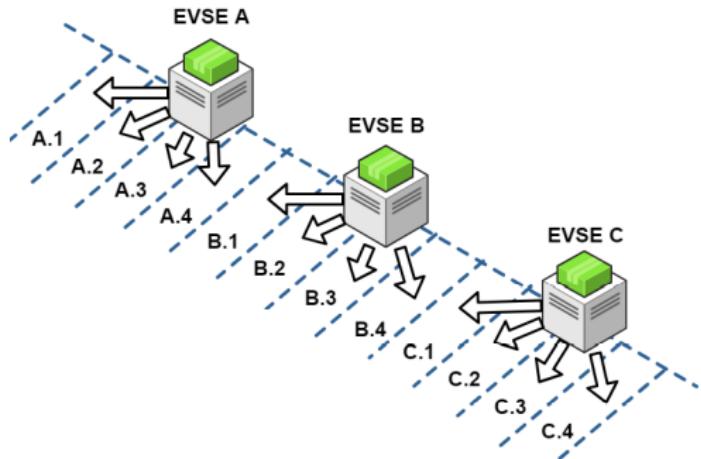
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- Charging facilities equipped with multiple-cable chargers



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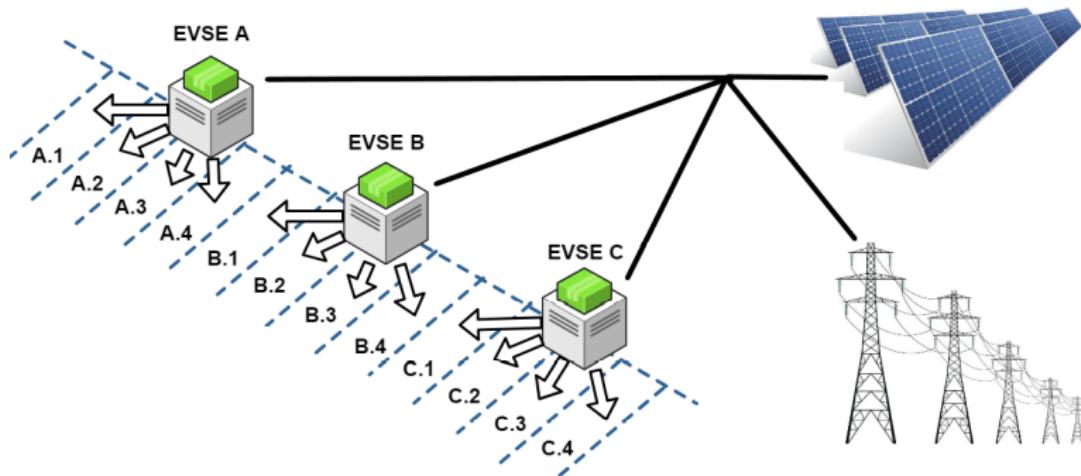
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- Energy procured from solar and distribution grid



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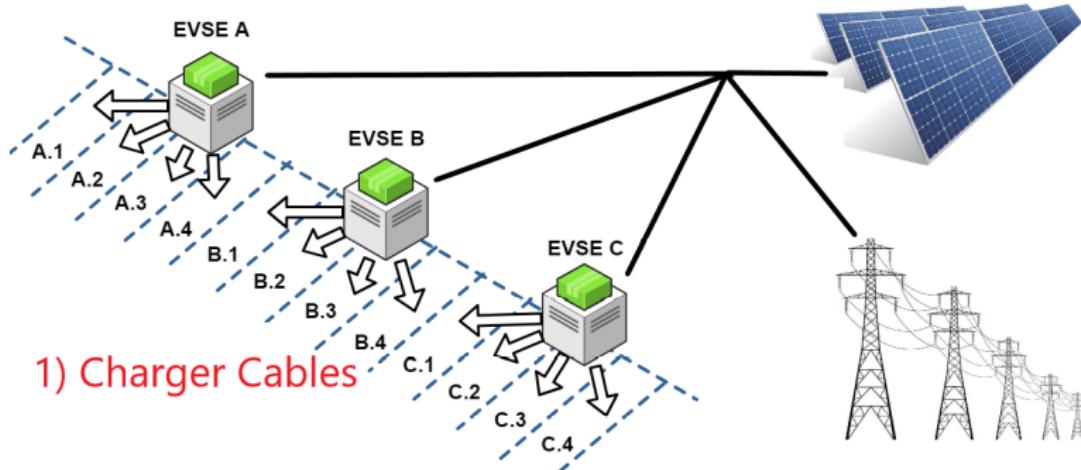
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- Limited shared charging resources



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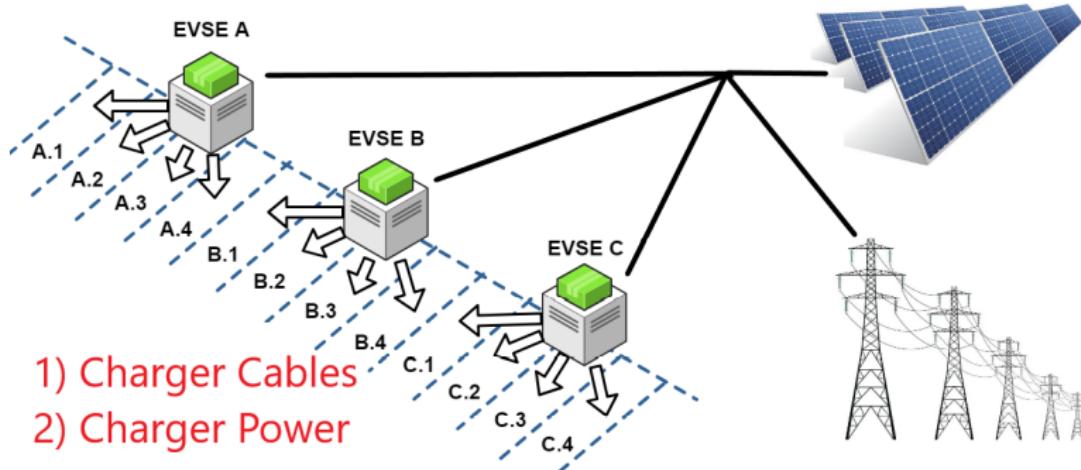
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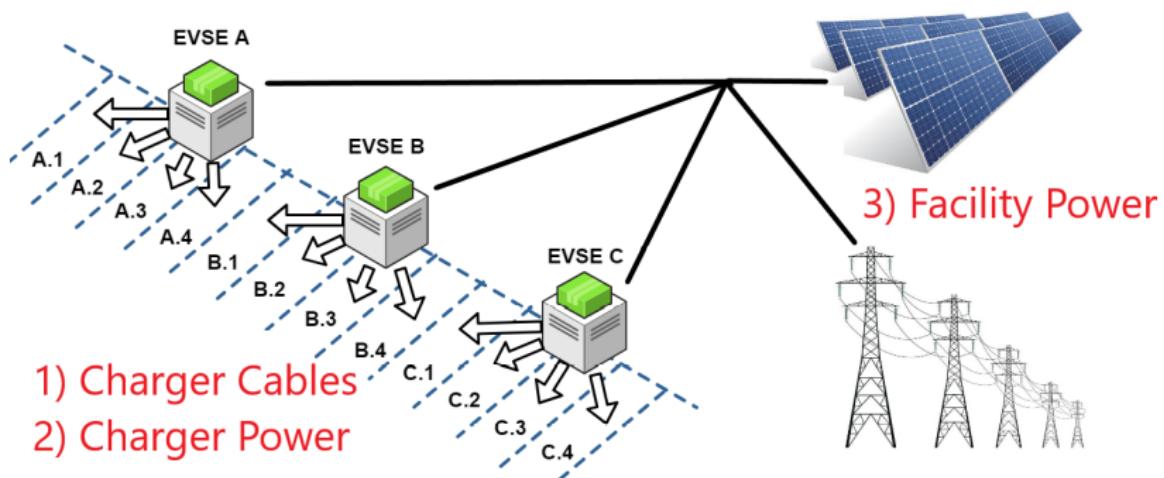
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- Limited shared charging resources



- Limited shared charging resources



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Between-Ride Schedules

- Each between-ride session $j \in \mathcal{J}$ begins at time t_j^- when an AMoD EV drops off a passenger

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Between-Ride Schedules

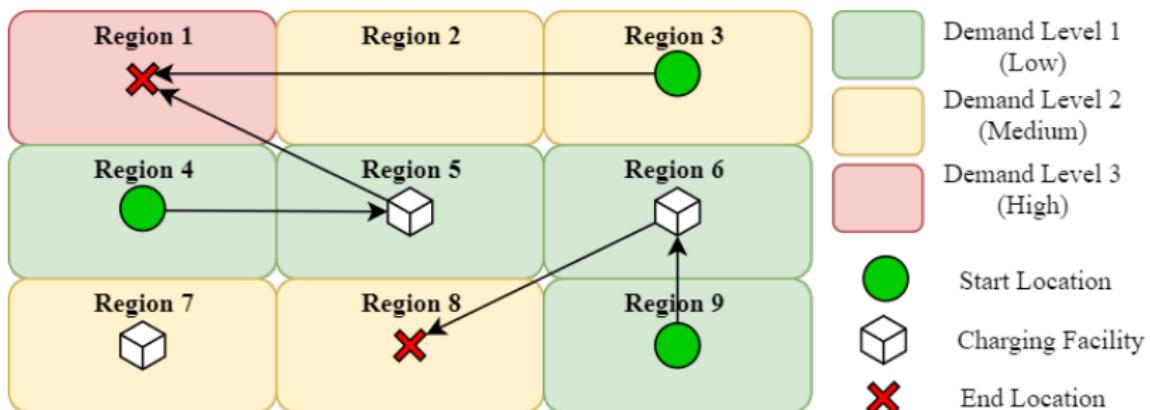
- Each between-ride session $j \in \mathcal{J}$ begins at time t_j^- when an AMoD EV drops off a passenger
- A set of feasible between-ride schedules is generated based on the vehicle's current battery level and location

Between-Ride Schedules

- Each between-ride session $j \in \mathcal{J}$ begins at time t_j^- when an AMoD EV drops off a passenger
- A set of feasible between-ride schedules is generated based on the vehicle's current battery level and location
- Schedules include:
 - Start/end time of the between-ride session
 - Start/end destination
 - Potential stop at a charging facility with charging schedule
 - Utility of the schedule to the fleet dispatcher

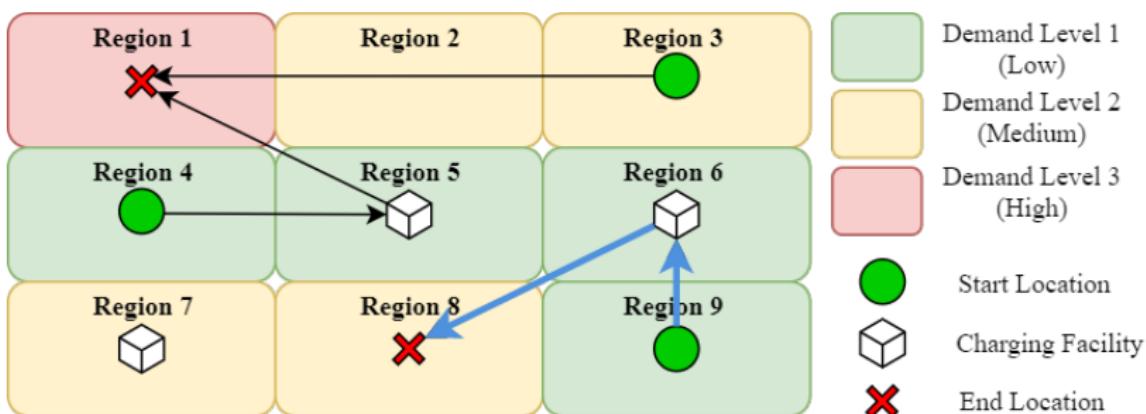
Example

- Recall the previous example:



Example

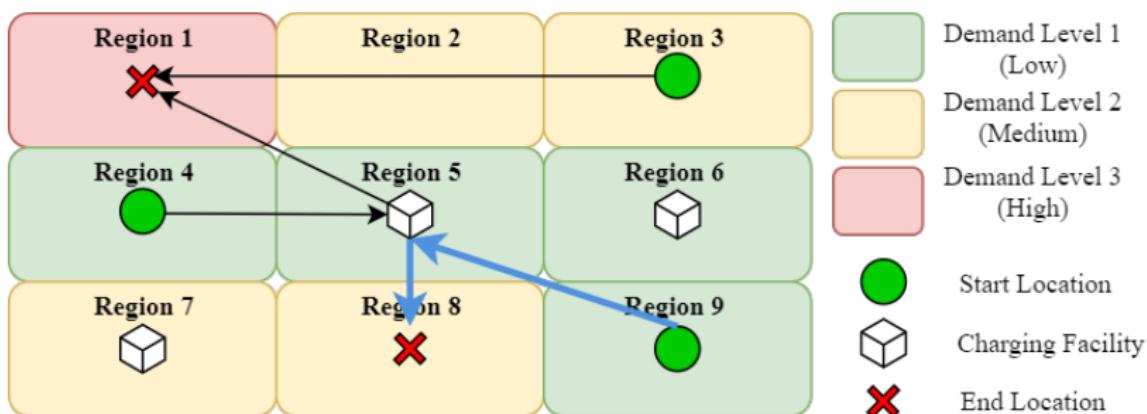
- Recall the previous example:



- Highlighted between-ride schedule was selected

Example

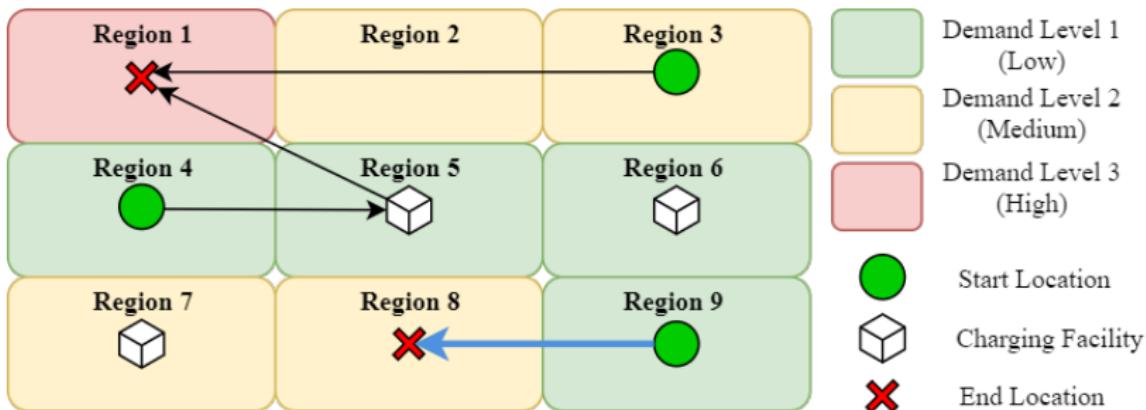
- Recall the previous example:



- Why not this schedule?

Example

- Recall the previous example:



- Or this one?

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Offline Welfare Maximization Problem

$$\max_x \sum_{\mathcal{J}, \mathcal{S}_j} v_{js} x_{js} - \sum_{\mathcal{T}, \mathcal{F}} G_f(y_g^f(t)) - \sum_{\mathcal{T}} O(y_o(t))$$

subject to:

$$\sum_{\mathcal{S}_j} x_{js} \leq 1, \quad \forall j$$

$$x_{js} \in \{0, 1\}, \quad \forall j, s$$

$$y_c^{mf}(t) \leq C_f, \quad \forall f, m, t$$

$$y_e^{mf}(t) \leq E_f, \quad \forall f, m, t$$

$$y_d(t) \leq \Omega_d(t), \quad \forall d, t$$

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Facilities' Electricity Costs

The energy procurement, $y_g^f(t)$, determines the operational cost of facility f (i.e., purchasing electricity from the distribution grid):

$$G_f(y_g^f(t)) = \begin{cases} 0 & y_g^f(t) \in [0, \delta_f(t)] \\ \pi_f(t)(y_g^f(t) - \delta_f(t)) & y_g^f(t) \in (\delta_f(t), \delta_f(t) + \mu_f(t)] \\ +\infty & y_g^f(t) > \delta_f(t) + \mu_f(t). \end{cases}$$

Fleet Out-Of-Service Penalty

The number of AMoD EVs in the between-ride state, $y_o(t)$, determines the out-of-service penalty:

$$O(y_o(t)) = \begin{cases} \phi(t)y_o(t), & y_o(t) \leq I(t) \\ +\infty & y_o(t) > I(t), \end{cases}$$

where $I(t)$ is the maximum number of out-of-service vehicles that the fleet dispatcher allows at time t

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where $I(t)$ is the maximum number of out-of-service vehicles that the fleet dispatcher allows at time t

Discourages excessively long recharging sessions

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Scheduling Decisions

- Can examine the following dual constraint:

$$u_j = \max_{s \in S_j} \left\{ v_{js} - p_d(t_{js}^+) d_{js}^+(t_{js}^+) - \sum_{t \in [t_j^-, t_{js}^+]} \left(o_{js}(t) p_o(t) + c_{js}^{mf}(t) p_c^{mf}(t) + e_{js}^{mf}(t) [p_e^{mf}(t) + p_g^f(t)] \right) \right\}$$

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- If $u_j \leq 0$, session j never yields positive utility

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Scheduling Decisions

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$$\begin{aligned} u_j = \max_{s \in S_j} \Big\{ & v_{js} - p_d(t_{js}^+) d_{js}^+(t_{js}^+) - \sum_{t \in [t_j^-, t_{js}^+]} \left(o_{js}(t) p_o(t) \right. \\ & \left. + c_{js}^{mf}(t) p_c^{mf}(t) + e_{js}^{mf}(t) [p_e^{mf}(t) + p_g^f(t)] \right) \Big\} \end{aligned}$$

- If $u_j \leq 0$, session j never yields positive utility
- if $u_j > 0$, session j is scheduled

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- If $u_j \leq 0$, session j never yields positive utility
- if $u_j > 0$, session j is scheduled
- Want to estimate the optimal **dual variables** in an online fashion

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Online Solution's Goals

- Design **online** scheduling mechanism for **fleet routing** and **smart charging** at facilities equipped with **shared** EV chargers

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Online Solution's Goals

- Design **online** scheduling mechanism for **fleet routing** and **smart charging** at facilities equipped with **shared** EV chargers
- Make irrevocable scheduling decisions in an online fashion

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Online Solution's Goals

- Design **online** scheduling mechanism for **fleet routing** and **smart charging** at facilities equipped with **shared** EV chargers
- Make irrevocable scheduling decisions in an online fashion
- Handle **adversarial** sequences (due to the nonstationary distributions of customer arrivals in Mobility-on-Demand)

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Online Solution's Goals

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- Make irrevocable scheduling decisions in an online fashion
- Handle **adversarial** sequences (due to the nonstationary distributions of customer arrivals in Mobility-on-Demand)
- Provide **performance guarantees**

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Proposed Solution: Update Heuristic for Dual Variables

- Fleet dispatcher does not know the future arrival sequence

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Proposed Solution: Update Heuristic for Dual Variables

- Fleet dispatcher does not know the future arrival sequence
 - Cannot accurately select dual variables beforehand

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Proposed Solution: Update Heuristic for Dual Variables

- Fleet dispatcher does not know the future arrival sequence
 - Cannot accurately select dual variables beforehand
- Proposed Solution: the dual variables $p_d(t)$, $p_o(t)$, $p_c^{mf}(t)$, $p_e^{mf}(t)$, and $p_g^f(t)$ have heuristic updating functions

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 - Dual variables increase as demand for shared resources increases

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Proposed Solution: Update Heuristic for Dual Variables

- Fleet dispatcher does not know the future arrival sequence
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 - Dual variables increase as demand for shared resources increases
- We are able to provide performance guarantees for pricing functions of the following form:

$$p_g^f(y_g^f(t)) = \begin{cases} \left(\frac{L_g}{2\Psi}\right) \left(\frac{2\Psi\pi_f(t)}{L_g}\right)^{\frac{y_g^f(t)}{\delta_f(t)}}, & y_g^f(t) < \delta_f(t), \\ \left(\frac{L_g - \pi_f(t)}{2\Psi}\right) \left(\frac{2\Psi(U_g - \pi_f(t))}{L_g - \pi_f(t)}\right)^{\frac{y_g^f(t)}{\delta_f(t) + \mu_f(t)}} + \pi_f(t), & y_g^f(t) \geq \delta_f(t). \end{cases}$$

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Performance Guarantee: Competitive Ratio

- Competitive ratio:

$$\frac{\text{Optimal Offline Solution's Welfare}}{\text{Worst Case[Online Mechanism's Welfare]}} \geq 1$$

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Performance Guarantee: Competitive Ratio

- Competitive ratio:

$$\frac{\text{Optimal Offline Solution's Welfare}}{\text{Worst Case[Online Mechanism's Welfare]}} \geq 1$$

- An online mechanism is “ α -competitive” when:

$$\alpha \geq \frac{\text{Optimal Offline Solution's Welfare}}{\text{Worst Case[Online Mechanism's Welfare]}} \geq 1$$

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Online Scheduling System Competitive Ratio

The proposed online fleet scheduling heuristic is α -competitive in welfare across all fleet resources for the fleet dispatcher over J between-ride sessions where $\alpha = \max\{\alpha_1, \alpha_2, \alpha_3, \alpha_4, \alpha_5\}$.

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Performance Guarantee: Competitive Ratio

$$\alpha_1 = \ln \left(\frac{2\Psi U_c}{L_c} \right)$$

$$\alpha_2 = \ln \left(\frac{2\Psi U_e}{L_e} \right)$$

$$\alpha_3 = \max_{\mathcal{F}, \mathcal{T}} \left\{ \ln \left(\frac{2\Psi(U_g - \pi_f(t))}{L_g - \pi_f(t)} \right) \right\}$$

$$\alpha_4 = \ln \left(\frac{2\Psi U_d}{L_d} \right)$$

$$\alpha_5 = \max_{\mathcal{T}} \left\{ \ln \left(\frac{2\Psi(U_o - \phi(t))}{L_o - \phi(t)} \right) \right\}$$

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Performance Guarantee: Competitive Ratio

$$\alpha_1 = \ln \left(\frac{2\Psi U_c}{L_c} \right) \text{(Charger Cables)}$$

$$\alpha_2 = \ln \left(\frac{2\Psi U_e}{L_e} \right) \text{(Charger Energy)}$$

$$\alpha_3 = \max_{\mathcal{F}, \mathcal{T}} \left\{ \ln \left(\frac{2\Psi(U_g - \pi_f(t))}{L_g - \pi_f(t)} \right) \right\} \text{(Facility Energy)}$$

$$\alpha_4 = \ln \left(\frac{2\Psi U_d}{L_d} \right) \text{(Regional AMoD EV Limit)}$$

$$\alpha_5 = \max_{\mathcal{T}} \left\{ \ln \left(\frac{2\Psi(U_o - \phi(t))}{L_o - \phi(t)} \right) \right\} \text{(Out-of-Service Penalty)}$$

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Proof Outline

- Ensure that the “welfare generated” by each between-ride session is above a “threshold value”

Proof Outline

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- Show the online dual variable update functions, fenchel conjugates, and facilities' operational cost functions satisfy the following *Differential Allocation-Payment Relationship*¹:

$$(p(t) - f'(y(t)))dy(t) \geq \frac{1}{\alpha(t)}f^{*\prime}(p(t))dp(t)$$

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- Resulting α is the maximum $\alpha(t)$ over all regions, facilities, resources, and time.

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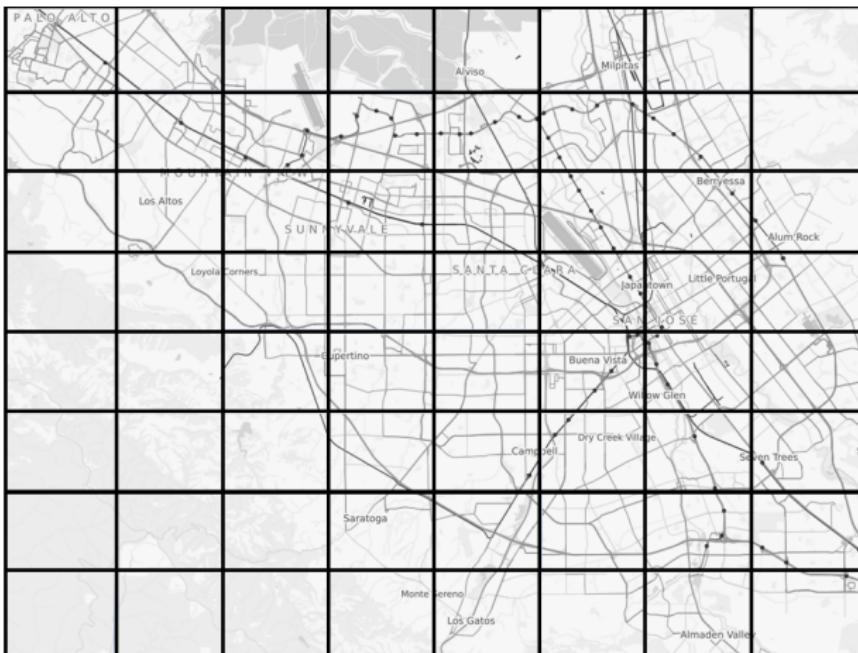
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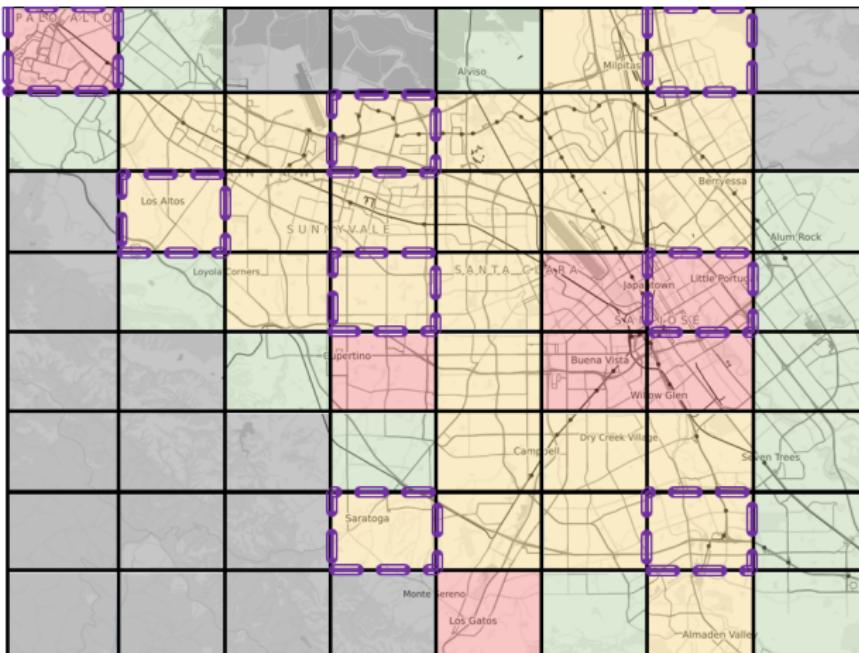
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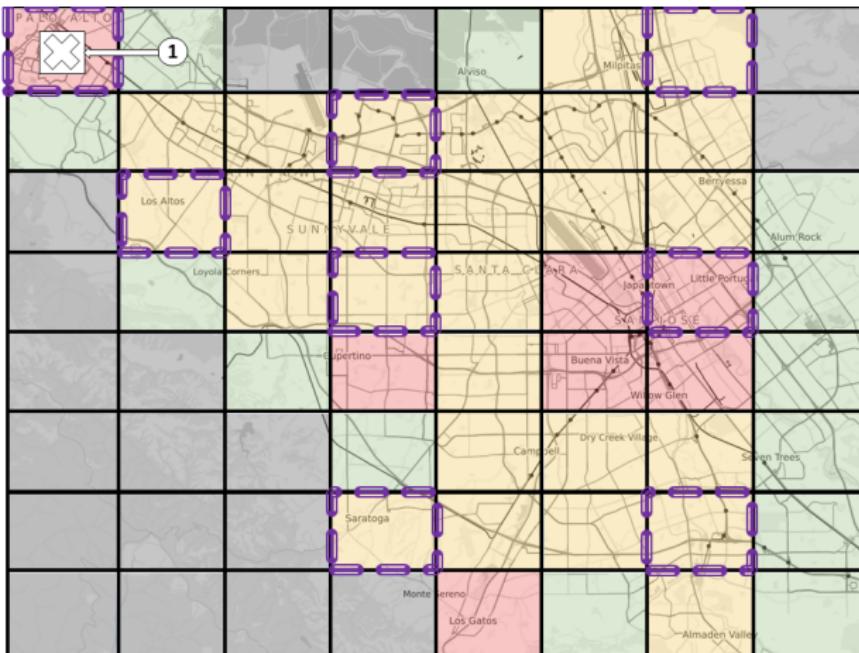
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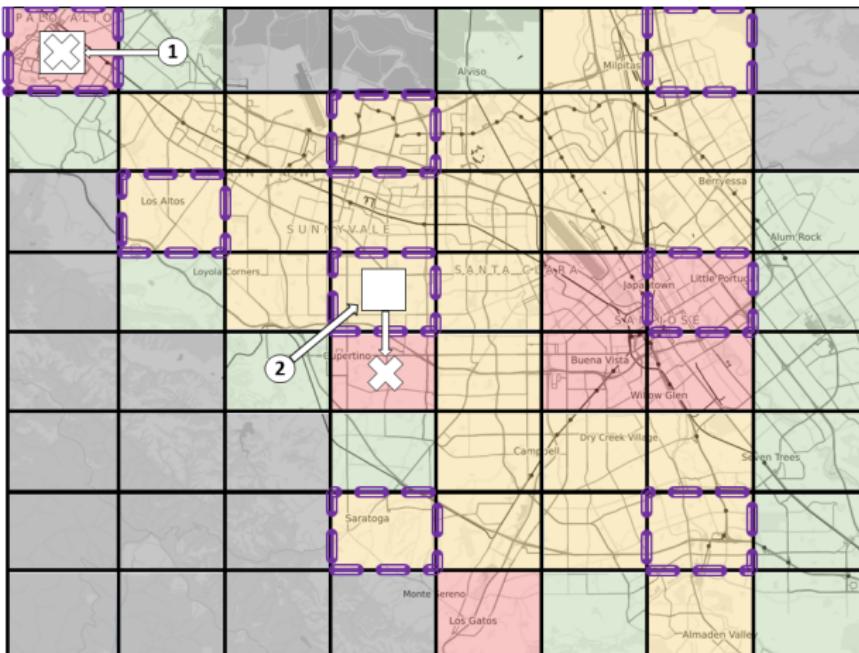
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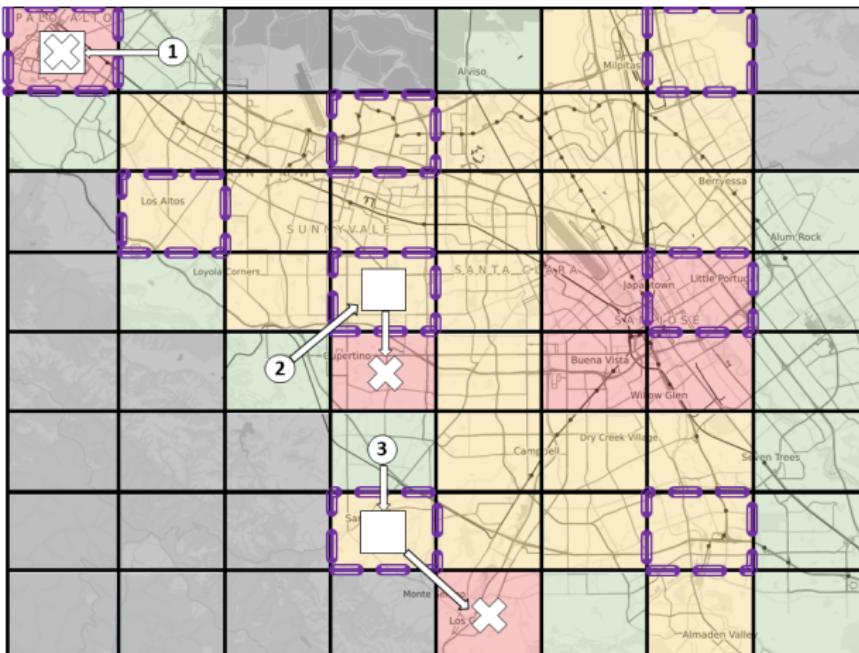
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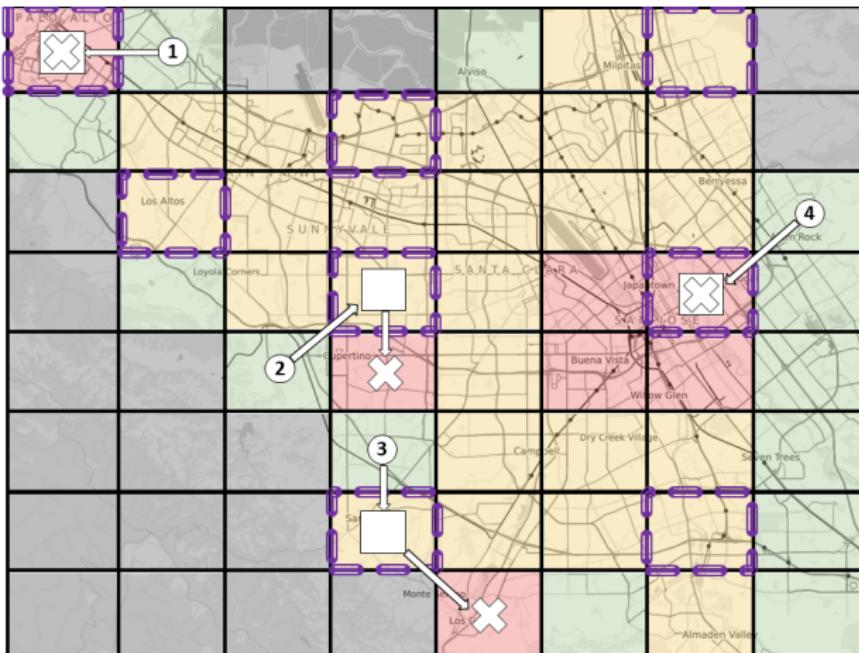
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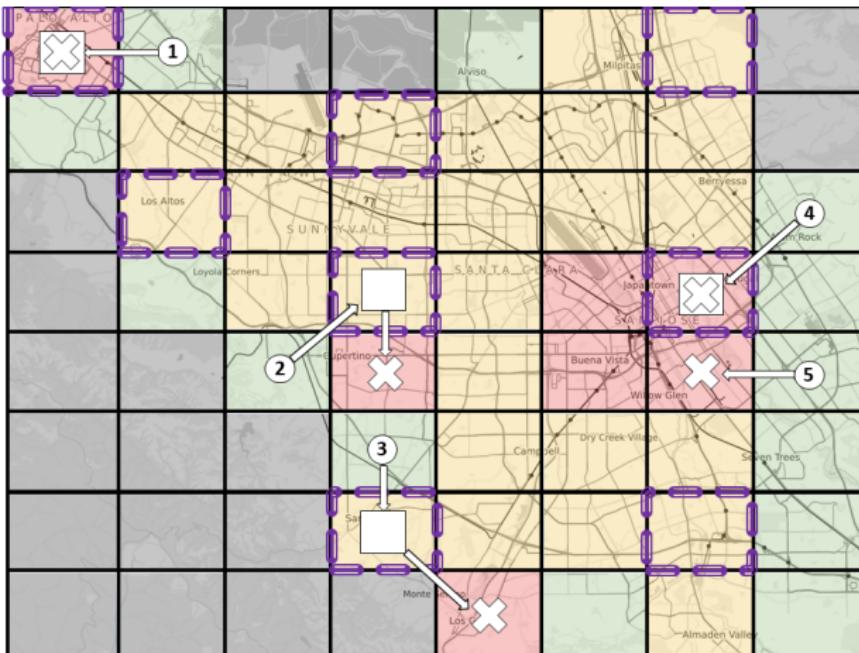
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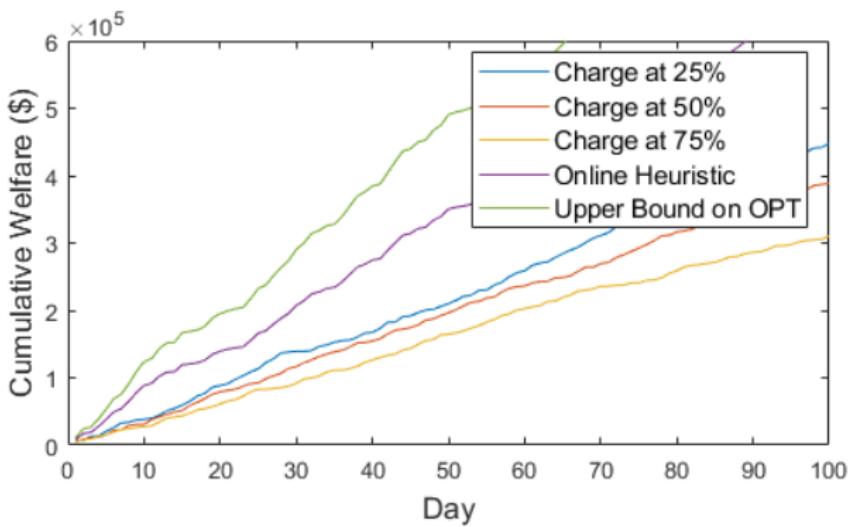
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Comparison with Threshold Strategies



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Conclusion

Online scheduling system for fleet **routing** and **smart charging** via heuristic dual variable update functions:

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1. Dispatcher for the AMoD EVs next customer pickup destination

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3. Does not rely on statistics and is robust to adversarially chosen arrival sequences

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Thank You!