

Alden Harcourt and Nathan Parker

Id_rsa_homework:

-----BEGIN RSA PRIVATE KEY-----

MIIG5QIBAAKCAyEayjbZdj5OkIQysjVwxB/1hCXn5rkoGs0FfHByycvH5g8CDe9F
9078KkjjgzlfZfstj+1YABA8fXMHcYr7rXE5gk/g+kepLy1ITb1IMpfJ2RWbfDy
Yiq4Wmy5WmrMi+s91pvn92uGCqOufxG5hPzVj/2o02u+kni3MoIM+BhrfKOfwEJs
6H6wolns+atpQlrUalzFAkljXBQmZBc0t2QcxSI1sLhBMZB9Vg64ynjbp9fPgokh
Hq9eYP1Aa3J5EVMvYXcGOjn55Xq5GCvh//nUQ3BQtebPuKKU4Q4jO8TBvh6gsUO
K0Q2C7ScT8UxL2QYwhckKqaDKA3xHxIxO1MnUUpuqutv81c9XhnafRhDNeqL2s7/
jLZImapp9b1+Y1I0xNYOSw8aE9iHRkjaO6ZUvhYcPTm88zO3F8cyJ8ietZN8kVcx
H7Y0WDZCDXHX7jskXsi45zbJFgdVN8vgfWxfEeYLi5kFEF38QGyHPUsk+12GeLrW
TC1/g2YHVtDth9C5AgMBAAECggGAJhIGhgr7+pxQ+RkzllEYBZ2nV9pjMQyJbGC1
U8WwaGFJ9zqlwaBViqr4NoKQw7/y14aNS1HDObEW5SsP8BsBg0WrqyMjuJSY3nZ
06cWHBH5bbBvyciWNbwDd4Dk6rDKzyVCGmRdc5JWb2j0XxPE11uf1dISqnvcrb8r
VuguEGSz1lwLKgh0E310Jps9cR/SFwZJNwF/Gd5XTf/Kdn58JiiElIVSPNUhq7qQ
0tnHLQXI9QMBP8gvgh4b6z69iWOrQKWgzJfQKwZR+squQRaErwykol0qO7idQ5BQ
/ZYdQ4q8XS/972cH3Ev4/jD6iuNNZeiko9gAaFzx3Jd9A7ZTowpgSezRx4vLqZYq
qpGx7kbgm8ptrat7gpoiO0ieY8eti2tBTD6x3ITwAB3/AVfDrar3NSRfzUYidWL
kv56gTxyBYdyJqcAtbvHvgBkNFk4qFulw0N/wZcHsYt/jMOFq0nEaqTwJnks0/Aj
Dr/g728WmNR7CK7xSTFqEE+wP4LJAoHBAO+5GaAiDsXkHqEx6aJOSXt50CIW9eEU
/RWcBbzDNsPywPVTe3xpcBv1TsPqA1omL3EQ87IzV06hdHHGxzwlfBTKtg1rkHF
yJVLiaEUAVL2F0YdEow3VCE1sLWP70UCXnhRRhm+rcPhcexp3tRt2KEDnDAAo27w
OTb/q9wFC9MdtI9dnxsPrwctIMc961U7yIDAMIM61bccMHEF4QwKiqKFp+w2TtT+
IHwJ0d7057Pg1C6eyKikuZybjTbU+aop7QKBwQDX8cQofWJc2PW0UY5j/fQSfMiD
ceJg4x6hVICUNQ4NzbelMVsryw9CYs6FrCkVNz6Nt52cTVtQ/kFVO3dADRWOn4B
OZNAerOcqv9V3M4PoSTXsJPrB3ZYit2CeJyQtA1fT2naHVog1BqVXLnZk5vTQZtr
FradgxmiRa9i/YXsSQk47RjY8QUBb5hE10+aOSG4HskuYscVCgLKIXFlbgVM+kCn
UHqCrVGF2gUy9Di/6zMy7AjhlCq+o6bvos6ruH0CgcEAlriFcRYyvbK4vNa5809P
ii/Debt/6n2cxhprzQvcAgU95sEPUECIGR7539nhM6vwhiEhwBbiMOybuJJ77I0j
al+Rz5CouDfXbm6o4LrIPIX1uiKLR9d9sMemC/GsWXJuQLWw4nztmcvE6Sdzb5KE
8m9noxKzrwugnYDQmCwgDCORR5KAd647uMJZ6ot2zAcjgDfXLFdAibIsh61PmpeC
JL7uHmji1a4ew4IVDx5iE8mW/pzcwwxOWzW96qyrMJ7dAoHBALgv68tJXwuotrlt
2hDpvDPEoVaUXa2cKzUaGW3QbwNREzHgjhhe20HYkRtj3RjdlXoKMOe/mf1vu8hT
b2tQUFO4II+zFykP2gC5jT7V/s2zHD4mMlgJE5Ta6psa8Z0/O7tknDLFmPn5iC9
7Xtqjr+7NvA5eFuTRd2VOYpqib9HcllQmh/4O/fEkpEtQSVfU6ZzA8//yqTkXArC
SbFIDTpiPaE4YLZzVJShqEuUyY7Q82OctdqKgYcHmUzOhg8sFQKBwQC6yccGR+0e
pniKwxh/dnwgekHEvGSvJq4ZJTavIP5DPmdQCEhu58T9AQ4whnX9vxiqu6GZXF1
0BIKBHYC+QF+D4RN5R0Sula1E486pzRZ5EDjfd5tasqg1vlbDJfKYyM4YG919GNQ
EDdzyZdhVD1leK3YFPL8d2UWACUDJnYMB6S3NRb/OnmJDR6fZ8RMlw1SVy8DOIQ
JHnOGmpB8PWL6a/VZNFQK9dju459ws+Ki/Jr2/R0HPAto0SR/zTL2vE=

-----END RSA PRIVATE KEY-----

Id_rsa_homework.pub:

ssh-rsa

```
AAAAB3NzaC1yc2EAAAADAQABAAQgQDKNtI2Pk6QhDKyNXDEH/WEJefmuSgazQV8cHLJy8fmDwIN70X3TvwqSOOoDMh9I+y2P7VgAEDx9cwxivutCTmCT+D6R6kvLWVNvUgyl8nZFZt8PJiKrhABLLaasyL6z3Wm+f3a4YKo65/EbmE/NWP/ajTa76SeLcyggz4GGt8o5/AQmzofrCgiez5q2IAitRqXMUCSWNcFCZkFzS3ZBzFKXWwuEEExkH1WDrjKeNun18+CiSEer15g/UBrcnkRUyy/JdwY6OfnlerkYK+H/+dRDcFC15s+4opThDiM7xMG+HqCxQ4rRDYLtJxPxTEvZBjCFyQqpoMoDfEfEjE7UydRSm6q62/zVz1eGdp9GEM16ovazv+MtmWZqmn1vX5jUjTE1g5LDxoT2ldGSNo7plS+Fhw9ObzzM7cXxzInyJ61k3yRVzEftjRYNkINcdfuOyReyLjnNskWB1U3y+B9bF8R5guLmQUQXfxAbIc9SyT7XYZ4utZMLX+DZgdW0O2H0Lk= kali@kali
```

=====Private Key=====

We expect these to be in the file:

- Version
- Modulus-n
- Public exponent-e
- Private exponent-d
- Prime1-p
- Prime2-q
- Exponent1-d mod(p-1)
- Exponent2-d mod(q-1)
- coefficient-(inverse of q) mod p
- otherPrimeInfos

To decode the private key we used cat id_rsa_homework and copy/pasted the key into [Lapo Luchini's ASN.1 decoder](#)

Integers in decoded file:

- Version, 0
 - This integer clarifies that the RSA key is using the two prime method and not the multi prime method
 - Found at offset 4. The DER encoding is 02 01 and then the version number
- Modulus
 - This is n, the product of primes p and q
 - Value:
4589004501146546129500770666748560868636636402140150924853872310
2394067268335754186932714591283946019247060478827951321787610552
9722795880064859389499931776582097107566868824025233250316245931
6735645827023666060961521225146455142403255653848248736421407991
9217302060318249295216693749360254102062555631197189734037542654
192620412501400035325122562024138062876618427072452222644840424
14287696326601114949013024515746284054102930410499001229283609803

44980640170003608880839703805395497486399341133805501781104179687
1289783711967924212255577146560703364917519017161459481420161581
7190351756470729197392929812451040208824419804193906140401065331
4577566572678623747907902103653311318947020458098233632624045818
52409741800349519444735639113304093722576176471394467110492402890
4106292689398567052999892765323159496452483293998248779469408965
0980311910849101241063827745815498556166099807917162722451706057
57765231246887281899327673

- publicExponent

- This is the public exponent, e
- Value: 65537

- privateExponent

- This is the private exponent, d
- Value:

8639613048720060335206869229851399709732386018250187250913148831
9405709597686910147774432608230002587619185455241875182549770787
1657951533664993450622535090919359317898867965460021126848497860
4382679408079634968517590008158679337556276589561105487638363444
8214395146441966969655488628787020345499312244308791298567560315
3570726398291841762453308408280555241776639856010277318095635072
2930386516407035061086061354464432699109648089933044336291191533
9406050976910045612517484103469199324325450992248712683718352572
6831766988656132930032691779379252173668927947228304485017524872
7807080220394474522747428777609640167839665571715616217538429022
40403476367985883842110081188264538205143728125521423044769634985
11423252972235264286806089967282214352821056498311380815562260387
9422892455246166015485999682886304854508200876941572873334662473
1421994133500860410133205021959460559001554699628471880361635912
40940909239785514107634377

- prime1

- This is the prime p which is a factor of n
- Value:

22570603118779684791870013569951114152995419941853244630184103571
4620370902759620086877651572798434523136318609142035072323139379
4036545747467443965956124073211685379193996454023979126105812728
8536342150880874370325050713788225594679410913052675948716392521
7080941359835024205601396644520241447594076340792691715025534159
3719087935014891725676013546703896346781450015619664648718121553
6841906241171446743920503824832325646862973580839076145367999286
43786539411949

- prime2

- This is the prime q which is a factor of n
- Value:

2033177614703748282427826439532326232741321778331230245202726527
7781755703842218569076258883689449268256734518093601472927276833
12033259374927100668547923824407975668024405441114148895345289779
9059194740361392220704132998414846048999797308547447589897451642
73677440119658441112992278375945749780385316185746559169993433271
6403501274088767729293434314542469346167074386517632835049929640
1039918798465957723790690544100563634908480109137625178746451937
6271785572477

- exponent1

- This is equal to $d \bmod (p-1)$

- Value:

1419078843263068055982122936890360649212164546293029807569366903
6759284653017700147519406797774020010872990842256584151174260277
5963617296373645465335950825391286595434164859374182614234997045
1690098689789045010344147145370773510579924510844767860089505094
6137022122971759727164510961346196116465681852422849477573930962
7186467214493017095009658876957953597157528797310844685979569096
2655554490848634302887291697975519139232782743180911748432013077
494655299395293

- exponent2

- This is equal to $d \bmod (q-1)$

- Value: (1536 bit)

1734174519497761954917574349503601081587609229701350984582559625
49814968962429799318368829110175400864593008960879232911967567586
9498865767414590235609814209691951597828650071758545693286332200
2374382818735393193846839655132085376093499393479923902950663737
69539271331443111521356720157117223354345770930421699361329675243
7771630036777515408086633272023582006826575692081559391587286829
6103428916725644609948209572068868068842777814374843368887009122
5021232917525

- Coefficient

- This is the modular inverse of $q \bmod p$

- Value: (1536 bit)

- 1758663683935358677868069683325075125561170933141242867495737232
96123435649471184384830312412135551664015699847085916032011154769
0896712003078656055430258767789083425195803455174792184456755061
1014513398655046177685268212177264089715025562509531013397052326
2523304850777186352561933598630187313688965910724512655858430715
7775659564778694639435861985724764545765308025748849452354658237
05700439134499311568383776180051001501220595611217505519130635528
9916057574129

====Public Key====

What we expect to find

- Modulus
- publicExponent

What we found:

- Sequence, contains the modulus and the publicExponent

- Modulus

- This is n

- Value: (3072 bit)

4589004501146546129500770666748560868636636402140150924853872310
2394067268335754186932714591283946019247060478827951321787610552
9722795880064859389499931776582097107566868824025233250316245931
6735645827023666060961521225146455142403255653848248736421407991
9217302060318249295216693749360254102062555631197189734037542654
1926204125014000353251225620241380628766184270724525222644840424
14287696326601114949013024515746284054102930410499001229283609803
44980640170003608880839703805395497486399341133805501781104179687
1289783711967924212255577146560703364917519017161459481420161581
7190351756470729197392929812451040208824419804193906140401065331
4577566572678623747907902103653311318947020458098233632624045818
52409741800349519444735639113304093722576176471394467110492402890
4106292689398567052999892765323159496452483293998248779469408965
0980311910849101241063827745815498556166099807917162722451706057
57765231246887281899327673

- publicExponent

- This is e

- 65537

====Sanity Check=====

The following relationships were confirmed through the following python code:

```
1  import math
2
3  q = 20331776147037482824278264395323262
4  p = 22570603118779684791870013569951114
5  m = 22570603118779684791870013569951114
6  n = 45890045011465461295007706667485608
7  e = 65537
8  d = 86396130487200603352068692298513997
9  exp1 = 14190788432630680559821229368903
10 exp2 = 17341745194977619549175743495036
11 coeff = 1758663683935358677868069683325
12
13
14 def lcm(a, b):
15     return abs(a * b) // math.gcd(a, b)
16
17 ln = lcm(p-1, q - 1)
18
19 if m == n:
20     print("Sane")
21 else:
22     print("Insane")
23
24 if d % (p - 1) == exp1:
25     print("Sane")
26 else:
27     print("Insane")
28
29 if d % (q - 1) == exp2:
30     print("Sane")
31 else:
32     print("Insane")
33
34 if (e * d) % ln == 1:
35     print("Sane")
36 else:
37     print("Insane")
38
39
```

PROBLEMS 186 OUTPUT DEBUG CONSOLE TERMINAL

```
PS C:\Users\alden\OneDrive\Documents\GitHub\Stock-
Sane
Sane
Sane
Sane
```