## PHYSICS 180E, WINTER 2025

## HOMEWORK 6

## (DUE WEDNESDAY MARCH. 12 BY MIDNIGHT ON GRADESCOPE)

- 1. Assuming a plasma density of  $n_e \sim 5 \times 10^{10} \ {\rm cm}^{-3}$  and a magnetic field strength of  $B = 60 \ {\rm G} \ (0.006 \ {\rm T})$ :
  - (a) Make a plot of the dispersion relation  $\omega$  (y-axis) versus  $k_{||}$  (x-axis) for the frequency range you will use in the lab (say 20 MHz to 140MHz). Recall for pure parallel propagation ( $\theta = 0$ ) the dispersion relation is given by:

$$\omega=|\omega_{ce}|rac{k_{||}^2\delta_e^2}{1+k_{||}^2\delta_e^2}$$

where  $\delta_e = c/\omega_{pe}$  is the electron skin depth (inertial length). Note that  $\omega$  and  $\omega_{ce}$  are in rad/s not Hz in the expression above.

- (b) What is the parallel wavelength you should measure for 70 MHz waves? How does this compare to the mean free path for electron-neutral collisions in this plasma (assume 1 mTorr neutral gas pressure and recall  $\lambda_{mfp} = 1/(n_g \sigma)$ )?
- 2. We can extend the dispersion relation for parallel propagating whistler waves to include the presence of electron neutral collisions as follows:

$$k_{||}^2 \delta_e^2 = \frac{\omega}{|\omega_{ce}| - (\omega + i\nu)}$$

where  $\nu$  is the collision frequency and i indicates an imaginary number.

- (a) Assuming a real frequency, find an expression for the imaginary part of  $k_{||}$ . (If you like, you can find an approximate answer by assuming  $v \ll \omega$ ).
- (b) For the parameters in the first problem and again assuming f=70 Mhz, compute the damping length (inverse of the imaginary part of k). How does this compare to your wavelength? You can assume an electron temperature of 3 eV when doing this calculation; you will need it for the collision frequency, which is  $v=v_{th,e}/\lambda_{mfp}$ .

A useful resource for equations in this lab is the Naval Research Laboratory's "Plasma Formulary", a copy of which you can find on the course website.