

# M 383: Assignment 5

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### Exercises 3.2.3 — Problem 1

*Problem.* Let  $A$  be an open set. Show that if a finite number of points are removed from  $A$ , the remaining set is still open. Is the same true if a countable number of points are removed?

*Proof.*

### Exercises 3.2.3 — Problem 4

*Problem.* Let  $A$  be a set and  $x$  a number. Show that  $x$  is a limit-point of  $A$  if and only if there exists a sequence  $x_1, x_2, \dots$  of distinct points in  $A$  that converges to  $x$ .

*Proof.*

### Exercises 3.2.3 — Problem 5

*Problem.* Let  $A$  be a closed set,  $x$  a point in  $A$ , and  $B$  be the set  $A$  with  $x$  removed. Under what conditions is  $B$  closed?

*Proof.*