

Transform

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	Level	Completed	Goal
	Beginner	10	15
	Intermediate	4	
	Advanced	2	Total Completed
	Expert	0	16

Transform

CSCI 5722: Computer Vision

Fall 2024

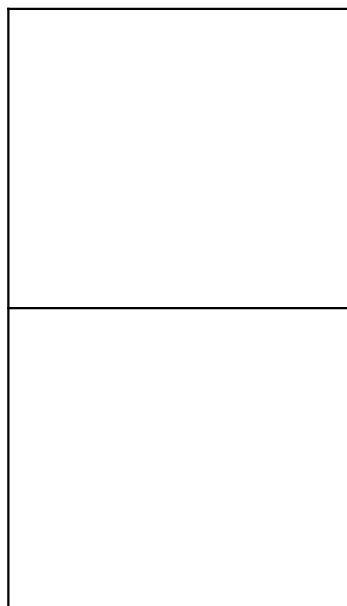
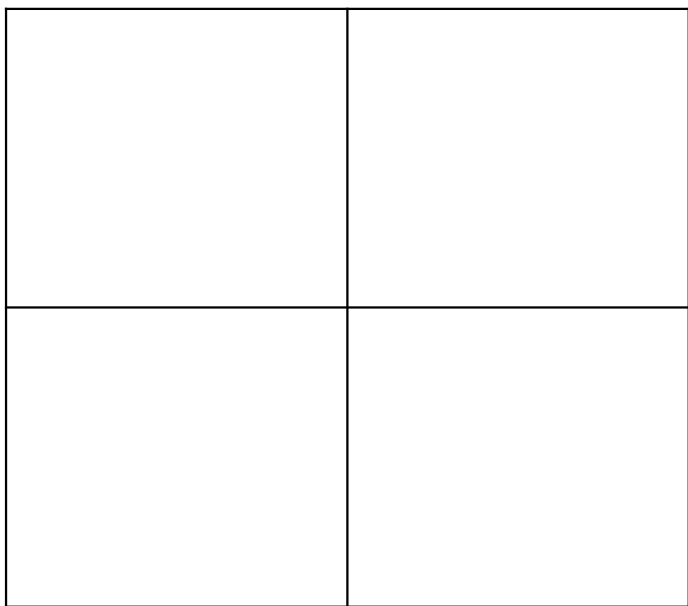
Dr. Tom Yeh

Linear Transform

CSCI 5722 Computer Vision



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2	7
3	5

1
-1

2	7
3	5

1	1	0	1
-1	0	1	1

1	1	0	1
-1	0	1	1

2	7
3	5

1	0	0	0
0	0	1	0
0	1	0	1
0	0	0	1
1	0	1	0

4	5	1
2	2	4
7	4	2
9	3	8

4	5	1
2	2	4
7	4	2
9	3	8

1	0	0	0
0	0	1	0
0	1	0	1
0	0	0	1
1	0	1	0

4	5	1
7	4	2
11	5	12
9	3	8
2	0	2



Linear Transform (i.e., Multiply Matrices)

$$a+b+c+d=15$$

1	1	0	1
-1	0	1	1

4	2
5	1

2	<div>b</div> 4	2	<div>d</div> 6
<div>a</div> 4	5	<div>c</div> 1	6



Linear Transform (i.e., Multiply Matrices)

$$a+b+c+d = 24$$

1	0	0	0
0	0	1	0
0	1	0	1
0	0	0	1
1	0	1	0

4	5	-1
-2	2	4
7	-4	2
9	3	8

4	^b 5	-1
7	-4	^c 2
7	5	12
^a 9	3	^d 8
11	8	7

What are the missing values?

$$a+b+c+d=135$$

0	1	0	99	53	^c 24
1	0	0	17 3	21	74
0	0	1	21	54	^d 36

173	21	74
99	53	24
^a 21	^b 54	36



What are the values of A and B?

$$a+b = 4$$

A	1	0
0	2	B

3	7
2	8
1	-1

-1	1
9	11

$$A = \boxed{ - 1 }$$

$$B = \boxed{ 5 }$$

Homogeneous Coordinate

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Convert to Homogeneous Coordinates

4
2

3
5
2

Convert to Homogeneous Coordinates

2	1	2	0
4	2	3	1

Equality in Homogeneous Coordinates

P_0

4
2
1

p_1 p_2 p_3

8	1	-8
	2	

q_1 q_2

8	1
	6

Which point is not equivalent to the rest in the homogenous coordinate? Cross it out!

A	B	C	D
3	9	-6	3
2	6	-4	2
1	3	-2	2



Which point is not equivalent to the rest in the homogenous coordinate? Cross it out!

A	B	C	D
2	2	-2	4
5	5	-5	1
1	2	-1	0
			2



Suppose these points are all equivalent in the homogenous coordinates. Fill in the missing values.

A	B	C	D
4	8	2	^c 12
2	4	^b 1	6
^a 1	2	1/2	^d 3

$$a+b+c+d = 17$$

Homogenous Transformation

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Translation Matrix

x
y

Translate by [-3, 2]

A	B
5	4
3	2

to H. C. 

A^H	B^H

A'	B'
H	H

Scaling Matrix

x
y

Scale by [3, -2]

A	B
2	1
3	4

to H. C.



A^H	B^H

A'	B'
H	H



Translate by [2, 3]

A	B
4	-2
1	5

to H. C.



A^H	B^H
4	-2
1	^c 5
1	1

A'^H	B'^H
6	0
4	^d 8
1	1

^a 1	0	2
0	1	^b 3
0	0	1

$$a+b+c+d = 17$$



Scale by [2, 3]

A	B
3	1
2	-1

to H. C.



A^H	B^H
3	1
2	^c -1
1	1

A'^H	B'^H
6	2
6	^d -3
1	1

^a 2	0	0
0	3	^b 0
0	0	1

$$a+b+c+d = -2$$



Suppose P is translated to P' . What are the values of the transformation matrix M ?

P

5
8
1

M

a 1	0	c -3
0	b 1	d 6
0	0	1

P'

2
1
4
1

$$a+b+c+d = 5$$



Suppose P is scaled to P' . What are the values of the transformation matrix M ?

P

5
8
1

M

a 3	b 0	0
0	c -2	d 0
0	0	1

P'

15
-16
1

$$a+b+c+d = 1$$



Suppose a group of points are scaled by a common matrix M . Which point does not belong to this group? Cross it out!

P1 P2 P3 P4

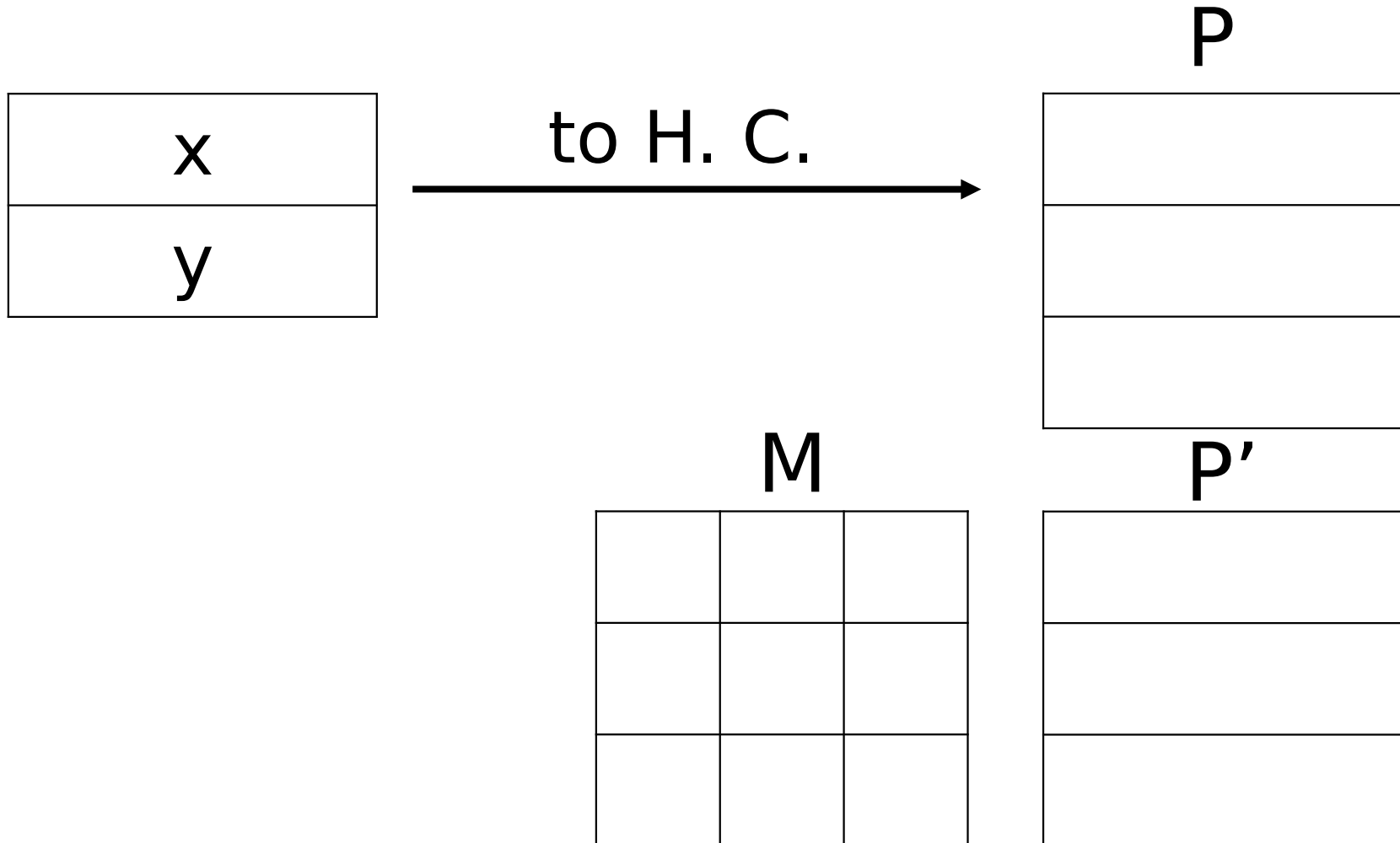
2	4	3	5
3	-1	2	-2
1	1	1	1

M

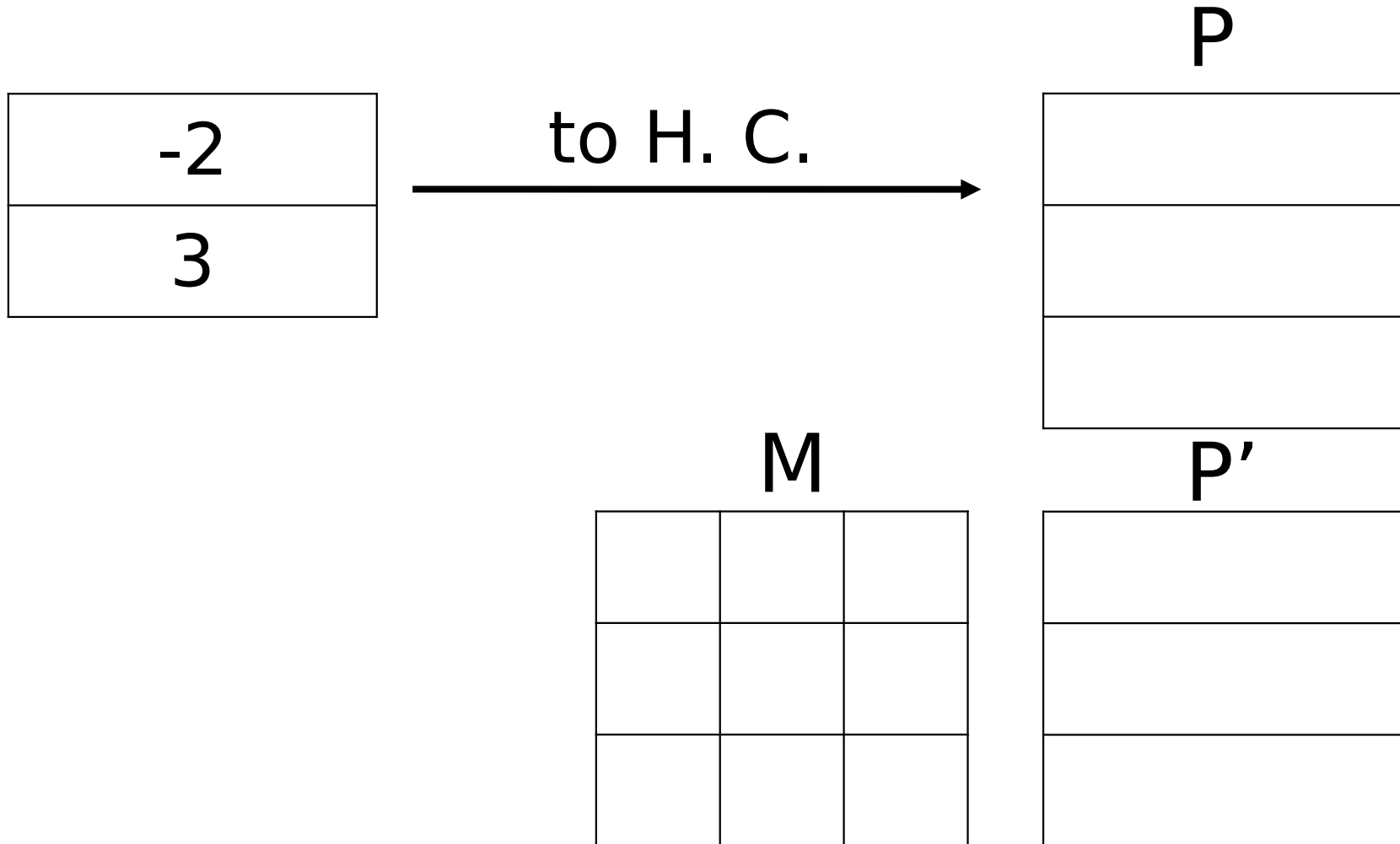
2	0	0
0	-2	0
0	0	1

4	8	6	1
0			0
-6	3	-4	4
1	1	1	1

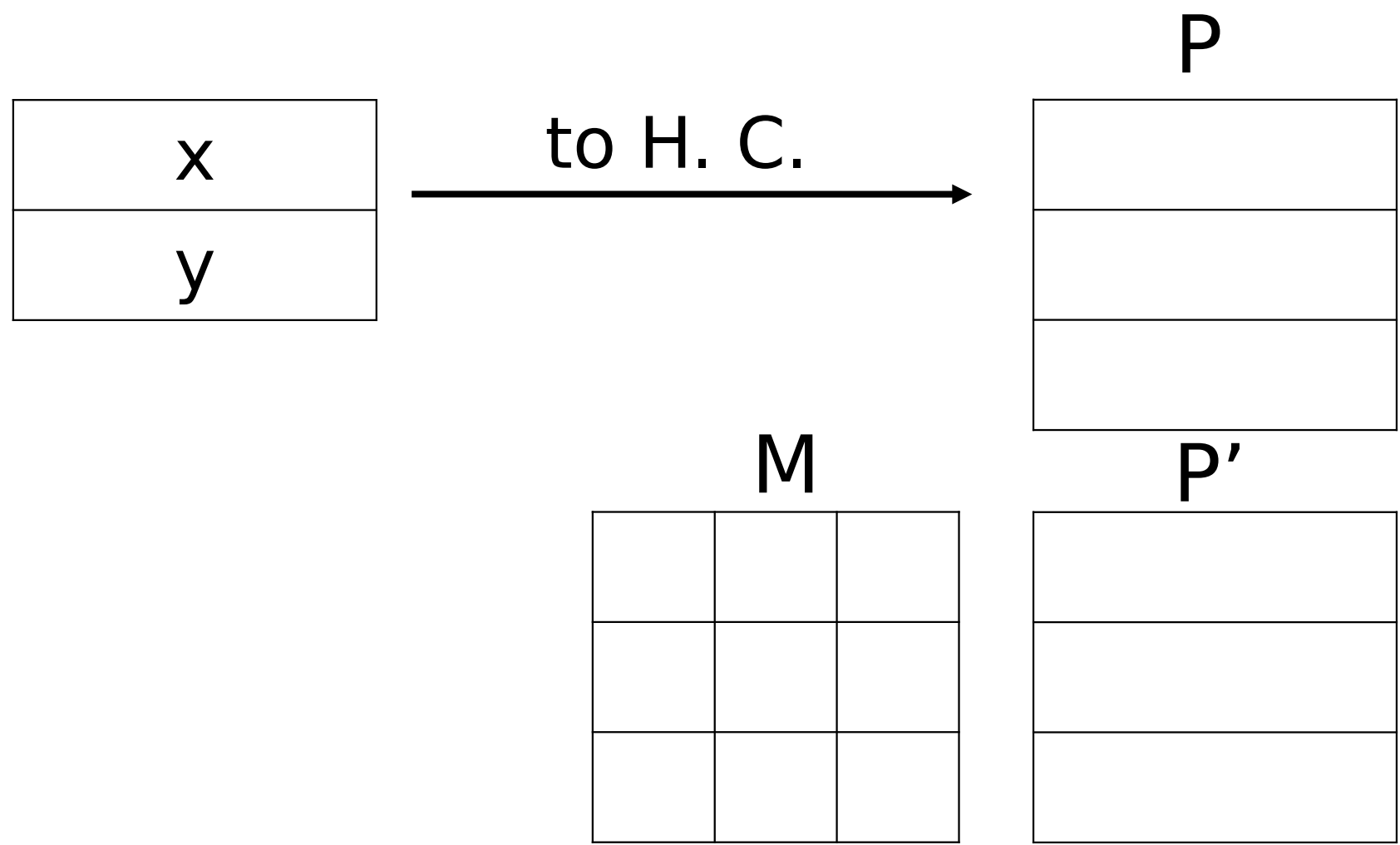
Scale by $[s_x, s_y]$ then Translate by $[t_x, t_y]$



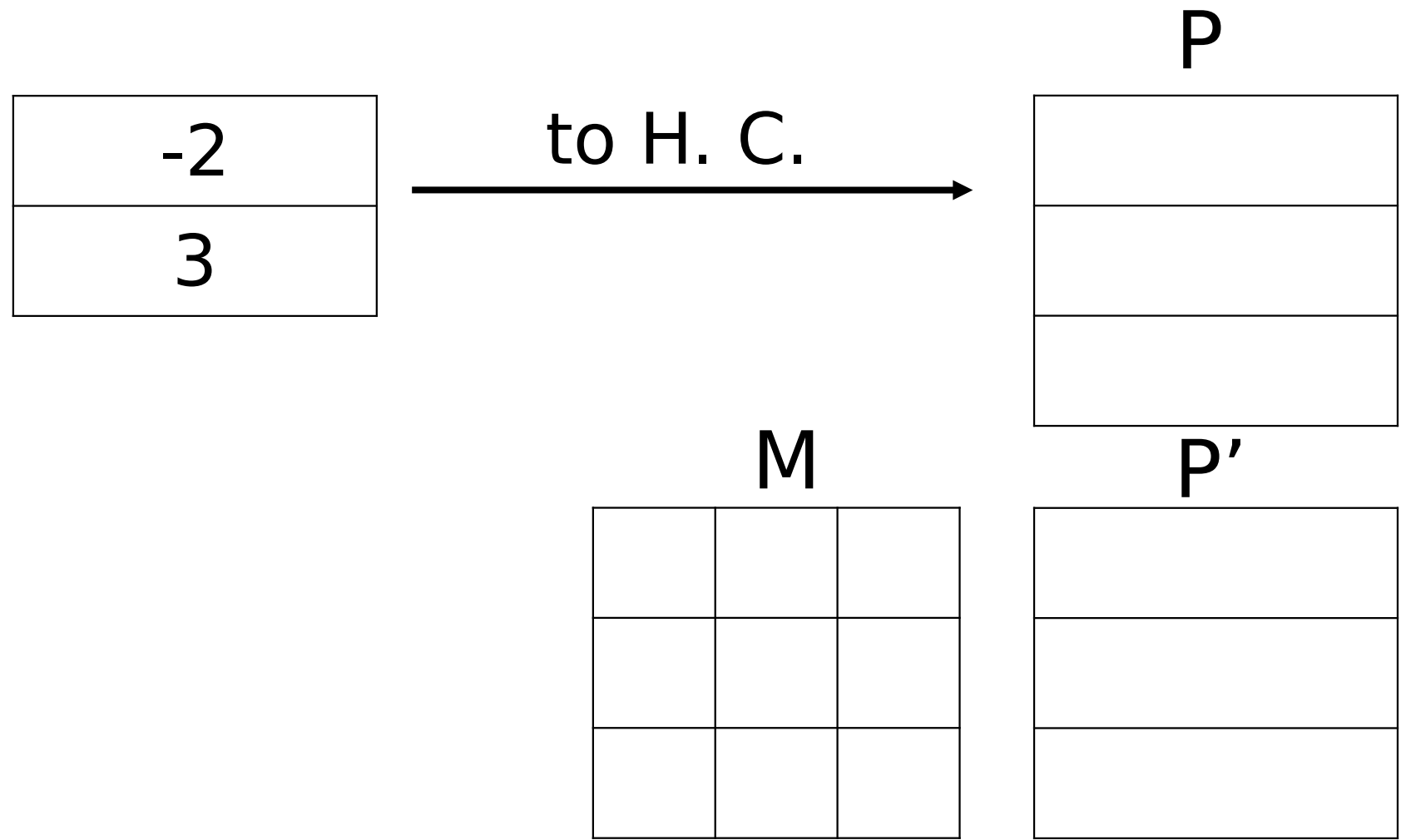
Scale by [2, 5] then Translate by [-3, 10]



Translate by $[t_x, t_y]$ then Scale by $[s_x, s_y]$



Translate by [-3, 10] then Scale by [2, 5]





Scale by $[3, 2]$ then Translate by $[4, -3]$

4
-2

to H. C.



P

4
-2
1

M

^a 3	0	4
0	^b 2	^c -3
0	0	1

P'

16
^d -7
1

$$a+b+c+d = -5$$



Translate by $[4, -3]$ then Scale by $[3, 2]$

4
-2

to H. C.



P

4
-2
1

M

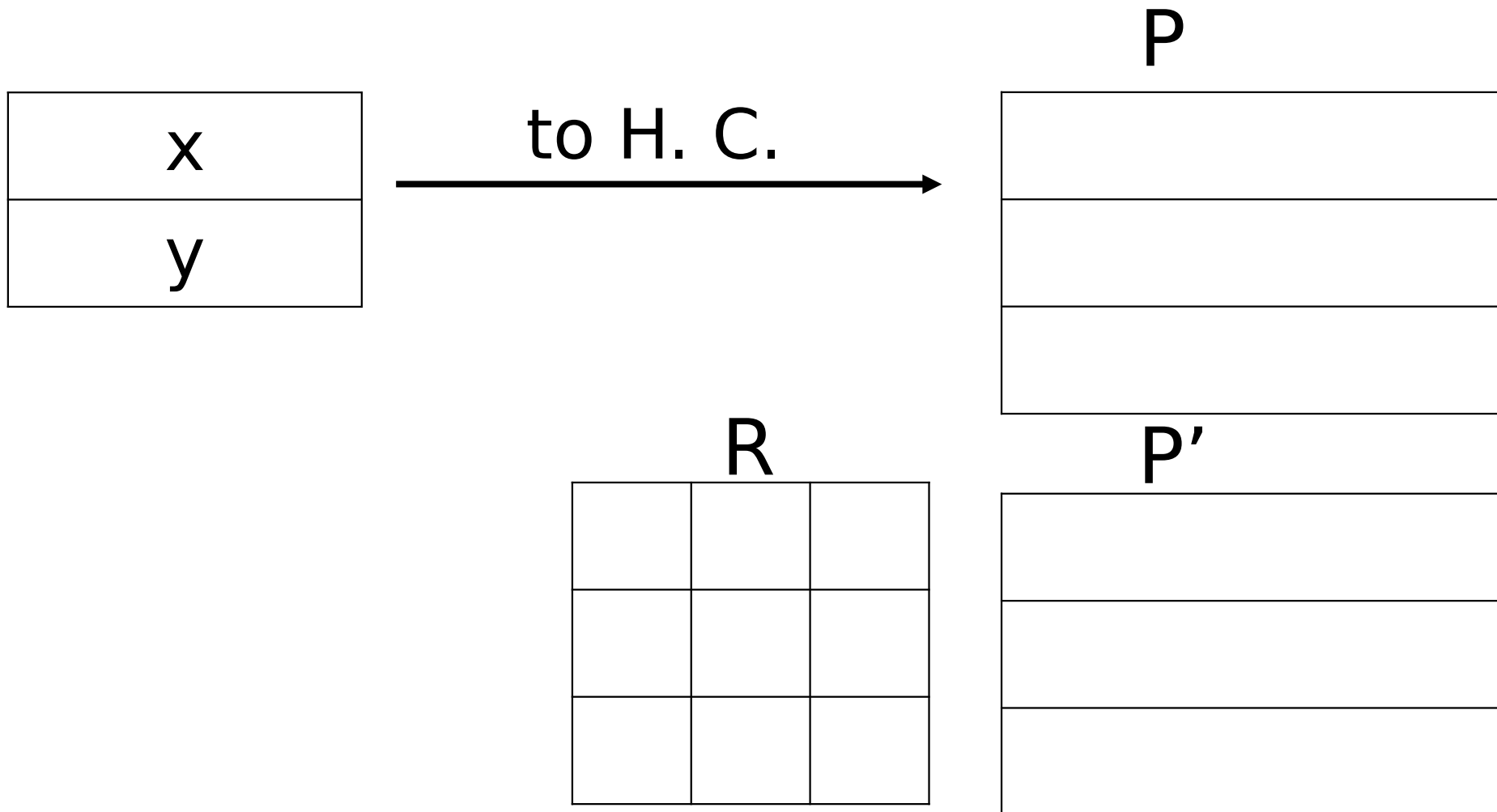
^a 3	0	4
0	^b 2	^c -3
0	0	1

P'

28
^d -13
1

$$a+b+c+d = -11$$

Rotation Matrix



Rotate by 45° (CCW)

2
4

to H. C.



P

R

P'

$$\cos(45^\circ) = \underline{\hspace{2cm}}$$

$$\sin(45^\circ) = \underline{\hspace{2cm}}$$



Rotate by 37° (CCW)

10
25

to H. C.



P

10
25
1

$$\cos(37^\circ) = 0.8$$

$$\sin(37^\circ) = 0.6$$

R

<small>a</small> 0.8	-0.6 <small>b</small>	0 <small>c</small>
0.6	0.8	0 <small>d</small>
0	0	1

P'

-7
26
1

$$a+b+c+d = 20.4$$



Rotate by 90° (CCW)

8
5

to H. C.



P

8
5
1

$$\cos(90^\circ) = \underline{\underline{0}}$$

$$\sin(90^\circ) = \underline{\underline{1}}$$

$$a+b+c+d = 4$$

R

0	-1	0
a 1	b 0	0
0	0	1

P'

c -5	
d 8	
	1

Scale, Translate, Rotate

$$P = (3, 2)$$

Scale by [4, 2]

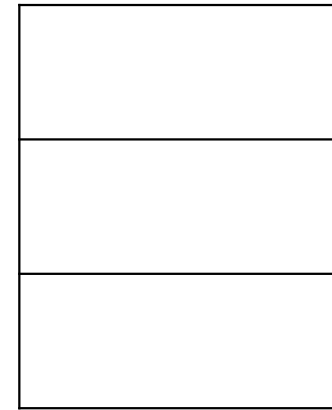
Translate by [3, 6]

Rotate CCW by 37°

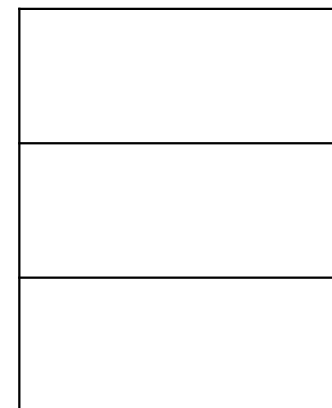
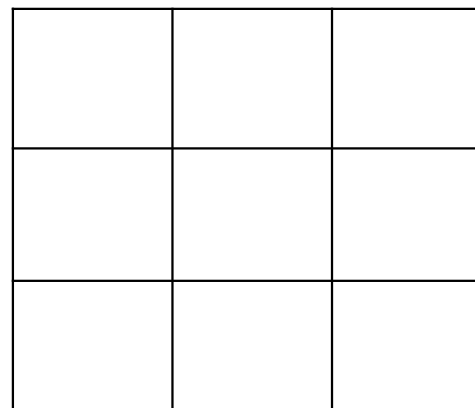
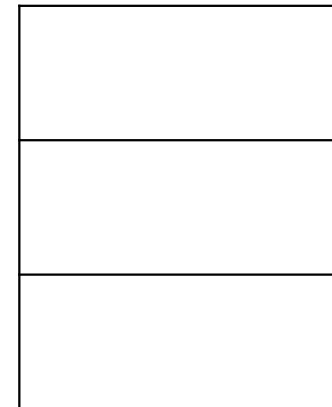
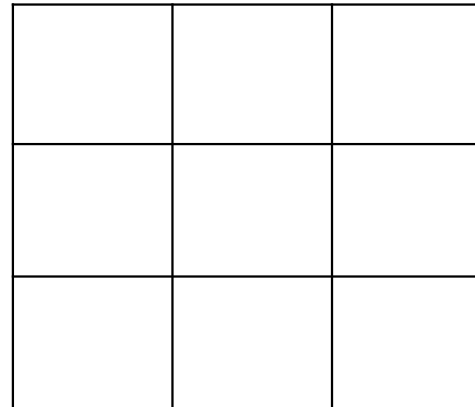
$$P' = ?$$

$$\cos(37^\circ) =$$

$$\sin(37^\circ) =$$



P



P'

Scale, Translate, Rotate

$$P = (2, 3)$$

Scale by $[3, -4]$

Translate by $[-1, 2]$

Rotate CCW by 53°

$$P' = ?$$

$$\cos(53^\circ) = 0.6$$

$$\sin(53^\circ) = 0.8$$

$$a+b+c+d = 4$$

2
3
1

P

3	0	-1
0	-4	2
0	0	1

a 5
b -10
1

0.6	-0.8	0
0.8	0.6	0
0	0	1

c 11
d -2
1

P'