# Package 'harmonious'

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<b>Description</b> A package for performing Bayesian inference on Explanatory Item Repsonse models in CmdStanR
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# Description

Creates an environment to estimate the  $p \times i$  interaction model with CmdStan.

# Usage

```
CreateMod(
  coef_hyper,
  sd_hyper,
  nWarmup_init,
  nSamples_init,
  nWarmup_run,
  nSamples_run,
  aux_envir
)
```

# Arguments

coef_hyper	Hyperparameter value for the standard deviation of normally distributed parameters
sd_hyper	Hyperparameter value for the shape parameter of gamma distributed parameters
nWarmup_init	Number of burn-in draws for the fixed $\theta$ model
nWarmup_run	Number of burn-in draws for the free $\theta$ model
nSamples_run	Number of sampled posterior values for the free $\boldsymbol{\theta}$ model (after burn-in has completed)
aux_envir	An environment object that contains objects to be loaded into the CreateMod environment (such as is returned by the genData function)
nSampels_init	Number of posterior draws for the fixed $\theta$ model (after burn-in has completed)

# **Details**

Creates an environment with methods for fitting the fixed  $\theta$  and free  $\theta$  models. Additionally, CreateMod includes a method for recursively checking  $\hat{R}$  convergence.

# Value

an environment object containing fixed  $\theta$  and free  $\theta$  model results

# See Also

```
initialize, sample, rhatCheck
```

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genData

Data Generating Function for the  $p \times i$  Interaction Model

# **Description**

Generates data for a  $p \times i$  Interaction Model under the Explanatory Item Response theoretical framework.

## Usage

genData(P, I, J, K, seed = NULL, isCorrI = TRUE)

# **Arguments**

Р	Number of examinees
I	Number of items
J	Number of potential item feature categories
K	Number of potential person feature categories
seed	Integer seed for replication (if NULL, a random seed will be generated)
isCorrI	Draw Cholesky-factorized lower triangular matrix for modeling structured item residuals?

## **Details**

Let a model of the log-odds transformed outcome  $(\eta_{pi})$  be defined as:

$$\eta_{pi} = \theta_p \lambda_i + \tau_i + \sum_{k=1}^{K} \sum_{j=1}^{J} \beta_{jk(\eta)} x_{ik} z_{pj}$$

where the linear predictor of latent trait measurements  $\theta_p$  is defined as:

$$\theta_p = \sum_{j=1}^{J} \beta_{j_{(\theta)}} z_{pj} + u_{p_{(\theta)}}$$

where the linear predictor of item slope/discrimination terms  $(\lambda_i)$  is defined as:

$$\lambda_i = \sum_{k=1}^K \beta_{k_{(\lambda)}} x_{ik} + u_{i_{(\lambda)}}$$

and where the linear predictor of item intercept/easiness terms  $(\tau_i)$  is defined as:

$$\tau_i = \sum_{k=1}^{K} \beta_{k_{(\tau)}} x_{ik} + u_{i_{(\tau)}}$$

For the linear predictor of latent trait measurements, the following assumption is made on its residual terms for the purposes of model identification:

$$u_{p_{(\theta)}} \sim \mathcal{N}(0,1)$$

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If an assumption is made that there is no structured dependency between the residual terms for the linear predictors of item intercepts and item slopes (isCorrI = FALSE), then:

$$u_{i_{(\lambda)}} \sim \mathcal{N}(0, \sigma_{\lambda}^2)$$
  
 $u_{i_{(\tau)}} \sim \mathcal{N}(0, \sigma_{\tau}^2)$ 

Whereas if it is assumed that the residuals of the linear predictors of item intercepts and item slopes is assumed to have a predictable underlying structure (isCorrI = TRUE), then:

$$\begin{bmatrix} u_{i_{(\lambda)}} \\ u_{i_{(\tau)}} \end{bmatrix} \sim \mathcal{MVN} \left( \mu = \begin{bmatrix} 0 \\ 0 \end{bmatrix}, \ \mathbf{\Sigma} = \begin{bmatrix} \sigma_{\lambda}^2 & \sigma_{\lambda} \sigma_{\tau} \\ \sigma_{\tau} \sigma_{\lambda} & \sigma_{\tau}^2 \end{bmatrix} \right)$$

## Value

an environment containing simulated data

genReport

Generate Text Report of Free  $\theta$  Model Results

# **Description**

Helper function that generates a text document in the user-specified save directory

# Usage

```
genReport(saveDir, fileDetails, ...)
```

# **Arguments**

saveDir Path to directory where report is saved
fileDetails string identifier for name of saved report
... additional arguments passed from parent frame

# **Details**

Model results include posterior descriptives and simulated data information

# Value

a . txt file of the free  $\theta$  results

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initialize

Run Fixed θ Model

# **Description**

Runs the first step in the two-step estimation framework

## Usage

```
initialize(...)
```

# **Arguments**

.. arguments passed from parent frame

## **Details**

The first step in the two-step estimation framework for the  $p \times i$  model

## Value

Model results for the standardized  $\theta$  model added to the environment rendered by CreateMod

#### See Also

CreateMod

rCorr

Generation of Data for the Person-by-Item Interaction Model

## **Description**

randomly samples a lower triangular, Cholesky-factorized matrix L from a Lewandowski-Kurowicka-Joe (LKJ) distribution given  $\eta$ .

## Usage

```
rCorr(nDim, eta = 1)
```

# **Arguments**

nDim desired dimension of the sampled  $n \times n$  matrix

eta concentration hyperparameter

# **Details**

Using the onion method, samples a Cholesky factorized lower-triangular matrix L from a Lewandowski-Kurowicka-Joe (LKJ) distribution given the concentration hyperparameter  $\eta$ , such that:

$$A = LL^{\top}$$

where A is a  $n \times n$  matrix and is a member of the set of all symmetric, positive-definite matrices.

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## Value

a Choleksy-factorized, lower triangular matrix

 ${\tt rhatCheck}$ 

Recursive Validation for Rhat Convergence

# **Description**

Helper function that validates  $\hat{R}$  convergence.

# Usage

```
rhatCheck(...)
```

# Arguments

... arguments passed from parent frame

## **Details**

```
\begin{array}{l} \textbf{Input:} \; \mathsf{CmdStan} \; \mathsf{model}, \; N_{\max}, \; \hat{R}_1 \\ \mathsf{Sample} \; \mathsf{CmdStan} \; \mathsf{model} \\ & \quad \textbf{while} \; \; \hat{R}_n \leq \hat{R}_{thresh} \; \; \textbf{or} \; \; n \leq N_{\max} \; \; \textbf{do} \\ & \quad \mathsf{Sample} \; \mathsf{free} \; \theta \; \mathsf{model} \\ & \quad n \mathrel{+}=1 \\ & \quad \textbf{end} \; \textbf{do} \\ & \quad \textbf{end} \; \textbf{while} \end{array}
```

## Value

modified free  $\theta$  model that is added to an environment created by CreateMod

# See Also

CreateMod

sample

Run Free  $\theta$  Model

# Description

Runs the second step of the two-step estiamtion framework

# Usage

```
sample(...)
```

# **Arguments**

... arguments passed from parent frame

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# **Details**

The second step treating latent trait measurements  $(\theta_p)$  as freely estimated parameters in the two-step estimation framework for the  $p \times i$  model

# Value

Model results for the full model added to the environment rendered by CreateMod

# See Also

CreateMod

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