Brussels
Faculty of
Engineering

CSD Labs Report
Control of a Rolling Mill

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Contents

Chapter 1

Introduction

1.1 Description of the plant

The goal of this project is to control the rolling of a metallic strip using a rolling mill. The plant is composed of two DC motor driven single rolls which unwind and wind up the sheet of metal. Between those two, the strip passes through a pair of rolls driven by a third DC motor, in order to have its thickness reduced and made uniform.

The actuators of the plant are the three DC motors, which are controlled through their armature current. The speed of those motors are measured using three velocity sensors. There are also two traction sensors to measure the tension in the strip left and right of the middle pair of rolls. Finally, a thickness sensor measures the thickness of the metallic strip on both sides as well.

The first requirement is to control the traction of the metallic strip. When this is achieved, a more advanced requirement is to control the thickness of the metallic strip.

1.2 Broad design of the controller

The plant will be controlled using a numerical controller implemented in matlab. To set this up, eight ADC and two DAC ports are available, along with second order Butterworth filters with various ω_c and an analog computer.

Intuitively, we know that the traction of the strip between two rolls will probably mostly depend on the difference of speed between the rolls. Similarly, we also know that the thickness reduction at the middle pair of

rolls probably mostly depends on the difference between the traction of the strip that is fed into the pair of rolls and the traction of the sheet that is pulled out of it. With this in mind, we propose to control this process using a cascade controller.

First, we will control the speed of the DC motors using the current as input. Then, we will control the traction of the metallic strip using the speed of the motors as input. Finally, we will control the thickness of the metallic sheet using the tractions of the strips as input.

Moreover, since we know that the traction will depend on a *difference* of speeds, we also propose to simplify this scheme by modulating the speed of only one motor during the operation. One motor is designated as "master": it will be controlled with a constant reference with the only goal of spinning at the setpoint speed as steadily as possible. The other is designated as "slave": its reference will vary during operation in order to control the traction of the strip and it should have adequate transient response properties.

1.3   Structure of this report

First, in chapter 2, we will describe the experimental setup which was used throughout this project. This report will then follow the chronological order of the work that was done during the labs. We used a bottom up approach where the inner loops are first implemented in order to then design the outer loops.

As stated before, to simplify the controller, only one motor – the slave – is controlled with a dynamic reference while the other – the master – is kept at a speed which should be as steady as possible. In chapter 3, the dynamics of the master motor are identified and a controller is designed to achieve zero steady state error and perturbation rejection. Then, in chapter 4, the dynamics of the slave motor are identified and a controller is designed to achieve reasonably fast reference tracking.

In chapter 5, the relation between both motors' speeds and the traction of the metallic strip is modelled and identified, and a controller is designed to stabilize the system and reduce the steady state error.

Finally, chapter 6 describes some considerations in controlling the thickness when rolling the metal strip. Since this objective is not attainable in the course of the lab sessions due to other constraints and complexity this will be done theoretically.

In appendix A the matlab code for the controller can be found.

Chapter 2

Description of the Experimental Setup

2.1 General Wiring

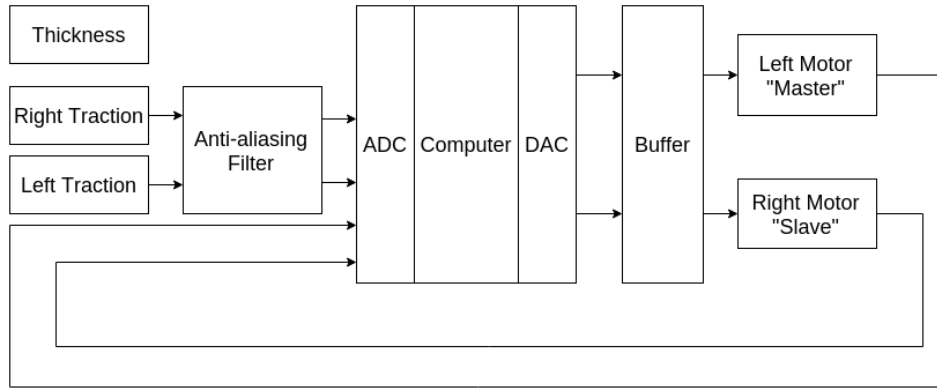The setup is wired as described in figure 2.1. We use the maximum recom-

Figure 2.1: Wiring for the control of the rolling mill

mended sampling frequency $f_s = 100\,\text{Hz}$, which is a common value for the control of a DC motor.

2.1.1 Anti-aliasing filtering

To be perfectly rigorous, we should filter every input before sampling it. However, we only have a limited amount of single signal, second order But-

terworth filters at our disposition, each with a different f_c. With the chosen f_s, those constraints on the available f_c, and the fact that second order Butterworth filters have a large transition band, only two of the available f_c values seem actually useful:

- $f_c = 40\,\text{Hz}$, which provides $37.1\,\%$ attenuation at $50\,\text{Hz}$ and $62.9\,\%$ rejection at $100\,\text{Hz}$.

- $f_c = 20\,\text{Hz}$, which provides $62.9\,\%$ attenuation at $50\,\text{Hz}$ and $80.4\,\%$ rejection at $100\,\text{Hz}$.

The other available filters either do not actually prevent aliasing, or have a too high passband attenuation. Even the two most adequate filters have a non ideal passband gain, and thus introduce a significant delay in the feedback loop. For this reason we choose not to use them in the inner loop, which should be fast, but rather in the outer loop. This is why only the two traction measurements are filtered in figure 2.1.

Chapter 3

Control of the Master Motor

This chapter describes all the steps that were taken in the design of a controller for the master motor of the rolling mill plant. Along the way all the design choices will be explained and substantiated.

3.1 Master motor

The master motor is the one that pulls the strip and winds it up on a spool. The left motor was chosen as master since its RPM at working current is higher than the right motor. This is necessary since when the strip is compressed to reduce its thickness it extends. The speed of the winding motor needs to be higher than the feeding motor. Figure 3.1 shows a plot of the motor characteristics and table 3.1 shows the currents for different operating points.

Armature current [A]	Angular velocity [RPM]
5.4	530.7
5.7	649.8

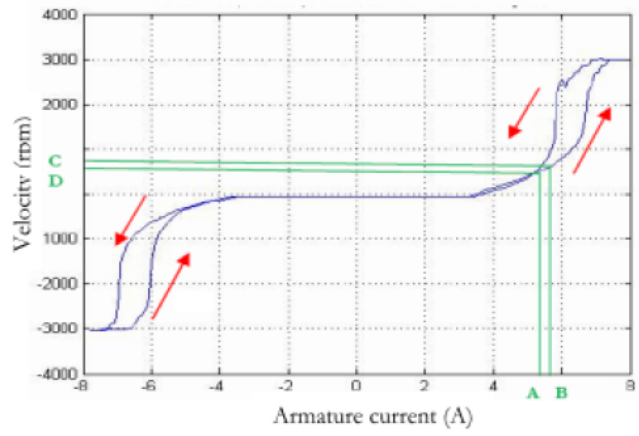Table 3.1: Operating points of the left motor

Figure 3.1: Rotational Velocity of the Left motor in function of the Current

3.2 Identifying the transfer function

The transfer function of the left motor was identified using matlab. To do this, velocity was sampled for a step input. Since the motor works around a given operating region, it was started from the lower setpoint current and an the step increased the current to the higher setpoint. The transient from stopped to the operating is not very interesting. The behaviour of the change in velocity was used to calculate a transfer function using the least squares method.

Figure 3.2 shows the sampled data points and the curve that corresponds to the transfer function of the left motor (equation 3.1).

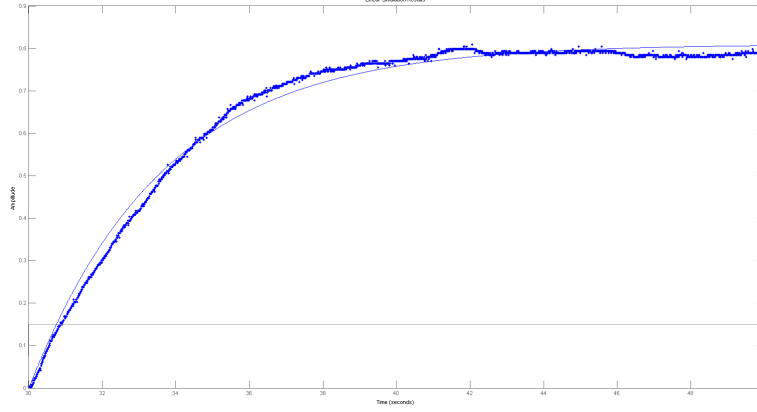$$G(s) = \frac{5.398}{3.642S + 1} \tag{3.1}$$

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Figure 3.2: Sampled data with the fitted curve from the calculated transfer function

3.3   Controller design

This controller needs to be able to keep the master velocity stable and constant. A PI controller has been chosen to control this motor.

To design this PI controller the root locus method has been used. The zero of the PI controller was used to cancel the pole of the transfer function of the left motor. This was done as follows:

The transfer function for the left motor was transformed to make the pole location visible.

$$G(s) = \frac{5.398}{3.642S + 1} \tag{3.2}$$

$$= \frac{1.482}{s + 0.274}$$

The same was done for the PI controller so that the zero location becomes easily visible.

$$C(s) = K_p + \frac{K_i}{s} \tag{3.3}$$

$$= K_p \left(\frac{s + \frac{K_i}{K_p}}{s} \right)$$

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To use the zero to compensate the pole of the left motor the nominator of the controller $C(s)$ needs to be the same of the denominator of the left motor $G(s)$. This means that $\frac{K_i}{K_p} = 0.294$

Using these previous equations K_p can be chosen using the root locus tool from matlab. The total system, without K_p equates to:

$$Sys(s) = \frac{1.482}{s + 0.274} \cdot \frac{s + 0.274}{s} \tag{3.4}$$

$$= \frac{1.482}{s} \tag{3.5}$$

Entering this system in the matlab root locus tool provides us with the root locus plot seen on figure 3.3. The gain can be chosen arbitrarily, but larger than 0.
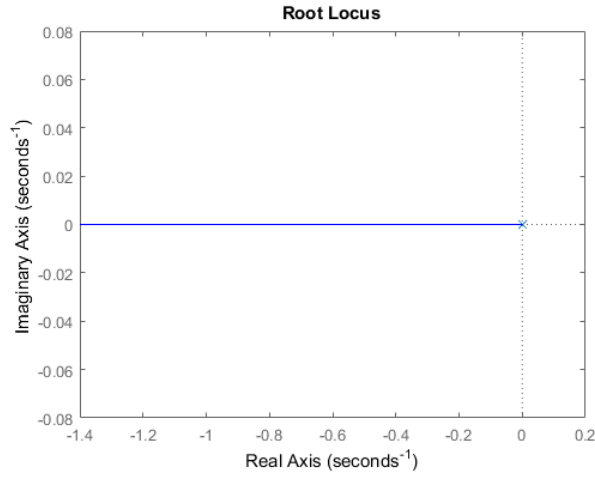

Figure 3.3: Root locus plot for the left motor with a PI controller

Several different values were used in simulation in simulink (figure 3.4, figure 3.5 and figure 3.6)
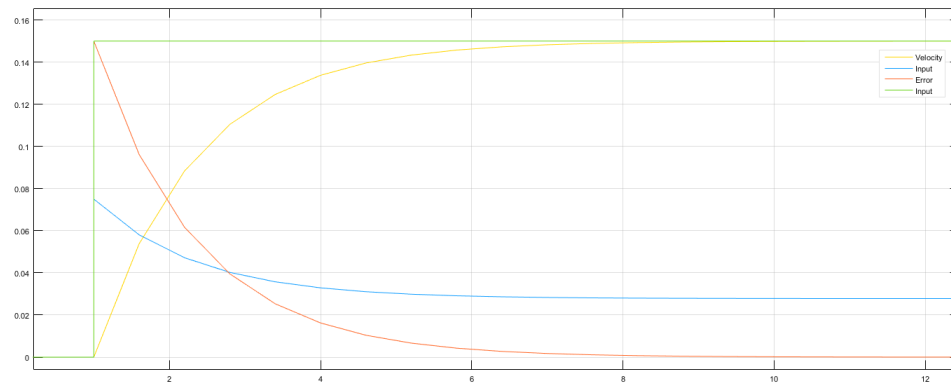
8

Figure 3.4: Simulink simulation of the left motor behaviour for $K_p = 0.5$
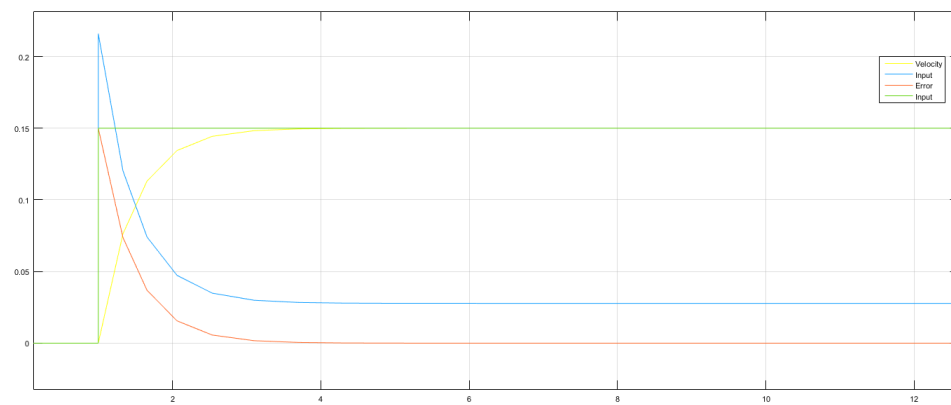

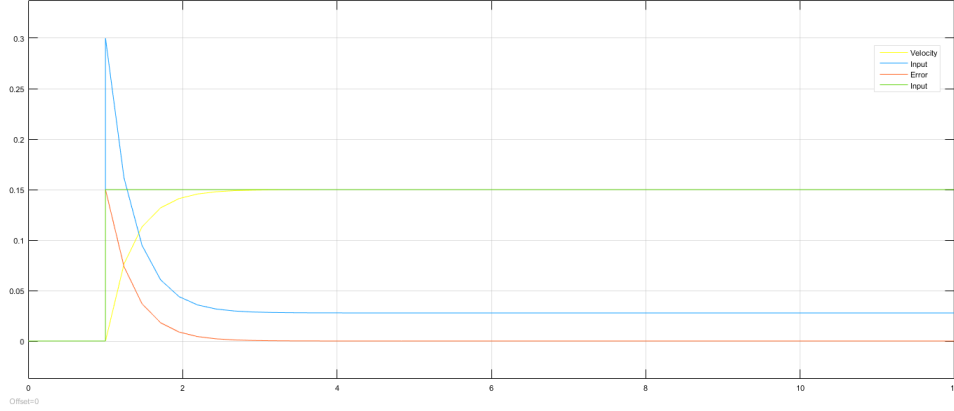Figure 3.5: Simulink simulation of the left motor behaviour for $K_p = 1.44$

Figure 3.6: Simulink simulation of the left motor behaviour for $K_p = 2$

Using the previous equations and calculated values, a discrete time PI controller could be implemented in matlab using the DAQ system.

The controller was tested in practice for different values of the K_p (see figure 3.7, figure 3.8 and figure 3.9). Based on these measurements $K_p = 1.44$ was chosen. $K_p = 0.5$ has a quite long settling time with a larger overshoot than $K_p = 1.44$. Since $\frac{K_i}{K_p} = 0.294$, $K_i = 0.3954$. In none of the simulations is there overshoot present while all of the practical experiments do. This is because the transfer function of the motor was reduced to a first order system while in practice it behaves as a non linear system of higher order.

3.4   Conclusions

For the controller of the whole plant cascade control was chosen with a grey box approach. The left motor was designated as the master motor. So first this motor was identified using the step response around the operating point.

After the system had been identified a controller could be devised to control the velocity of the motor. A PI controller was chosen to keep the velocity stable and to reject disturbances. The PI controller was designed to cancel the pole of the transfer function of the motor. Multiple values of the feedback gain were simulated and tested in practice. Finally $K_p = 1.44$ was chosen to be used in the final plant controller.
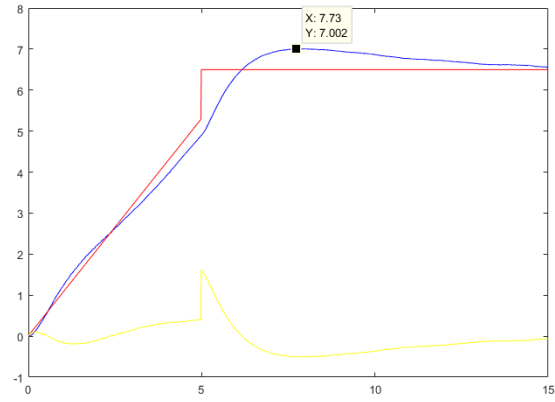
Figure 3.7: Response of the left motor behaviour for $K_p = 0.5$ to the red curve as input.
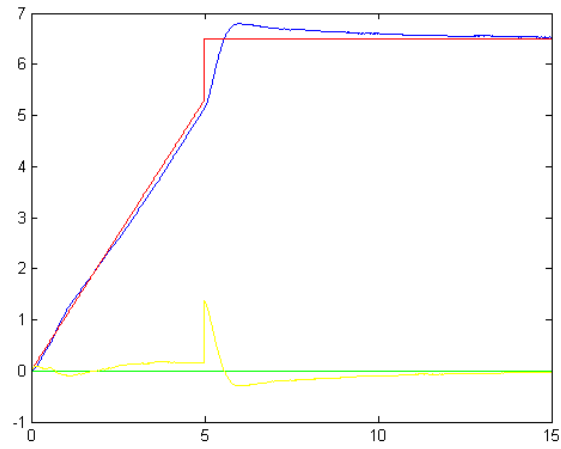

Figure 3.8: Response of the left motor behaviour for $K_p = 1.44$ to the red curve as input.
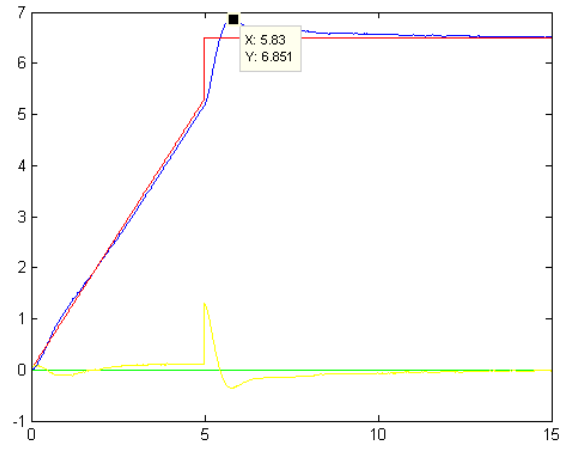
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Figure 3.9: Response of the left motor behaviour for $K_p = 2$ to the red curve as input.

Chapter 4

Control of the Slave Motor

In this chapter the properties of the design of the controller for the slave motor will be explained. The process is analogous to the master motor, first the motor is identified around the operating point, then a controller is designed which is then simulated and tested in practice.

4.1 Slave motor

Now that the master motor has a controller to keep the speed constant the slave motor can be controlled. The slave motor feeds the metal strip to the master motor. The right motor will be the slave. The speed of the feeding motor has to be lower than the winding motor. Figure 4.1 shows a plot of the motor characteristics and table 4.1 shows the currents for different operating points.

Armature current [A]	Angular velocity [RPM]
5.4	244
5.7	370

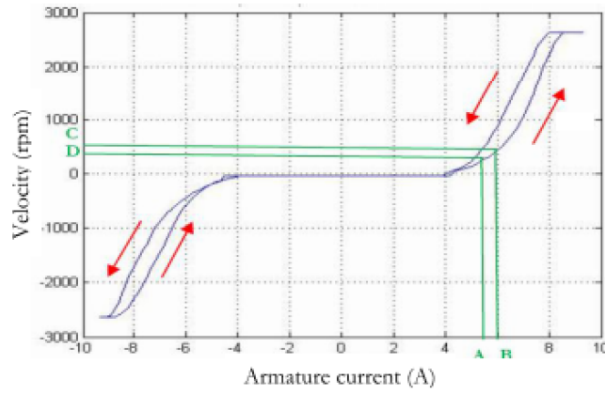Table 4.1: Operating points of the right motor

Figure 4.1: Rotational Velocity of the Right motor in function of the Current

4.2 Identifying the transfer function

The transfer function was identified the same way the master motor was done: stepping from one operating point to another and measuring the step response. Using the least squares method a best fitting curve (figure 4.2) to the sampled data points was generated with a corresponding first order transfer function (equation 4.1).

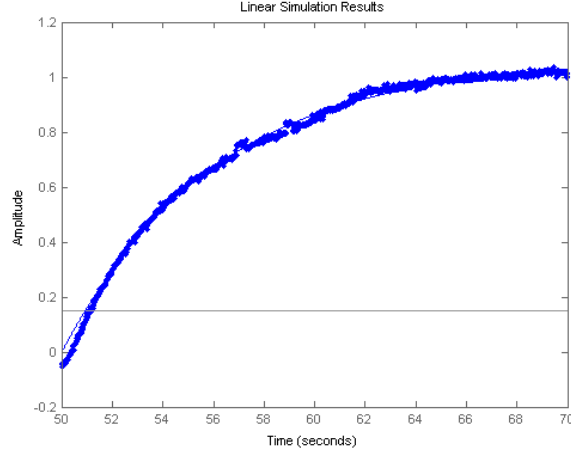$$G(s) = \frac{7.128}{6.0665S + 1} \tag{4.1}$$

Figure 4.2: Sampled data with the fitted curve from the calculated transfer function

4.3 Controller Design

The controller for this motor needs to be fast enough to be able to keep the tension of the strip constant despite disturbances. To do this a proportional controller with gain K was chosen. A proportional controller has a steady state error, but in this case this is negligible because this controller is part of a larger cascade controller.

Figure 4.3 shows a root locus plot for the right motor. The gain can again be chosen arbitrarily.K was chosen based on a couple simulations (figures 4.4, 4.5 and 4.6) and practical experiments for different gains (figures 4.7, 4.8 and 4.9). None of the simulations have overshoot while some of the practical experiments do (depending on K). This is because the transfer function of the motor was reduced to a first order system while in practice it probably as a non-linear system.

A gain of $K = 3$ was used since using a higher gain has the risk of putting current output of the controller in saturation. Saturation will occur is a too large step is applied to the input of the controller, but in practice it should not occur. The system is started up using a ramp instead of using a step, but this will be explained in a later chapter.
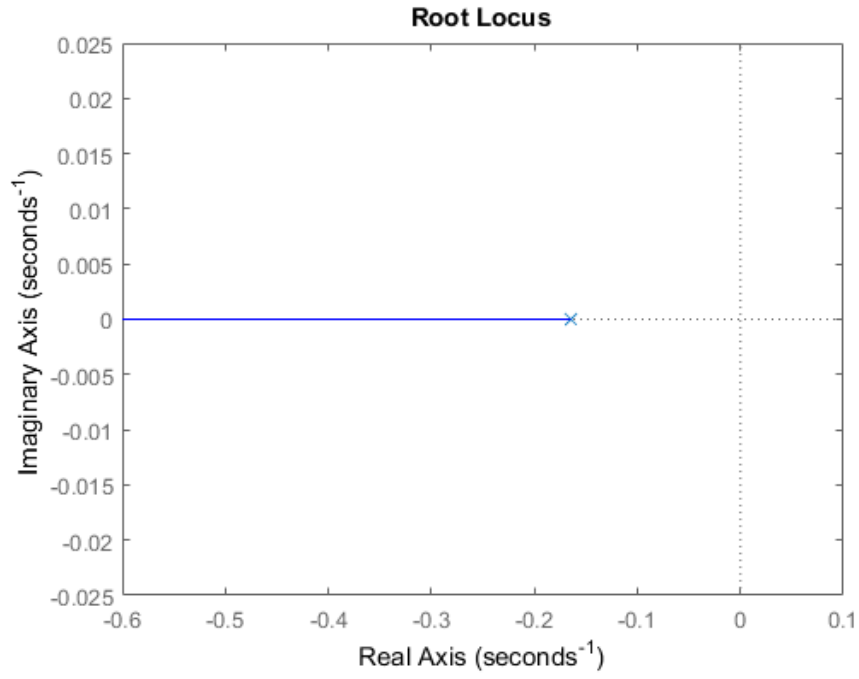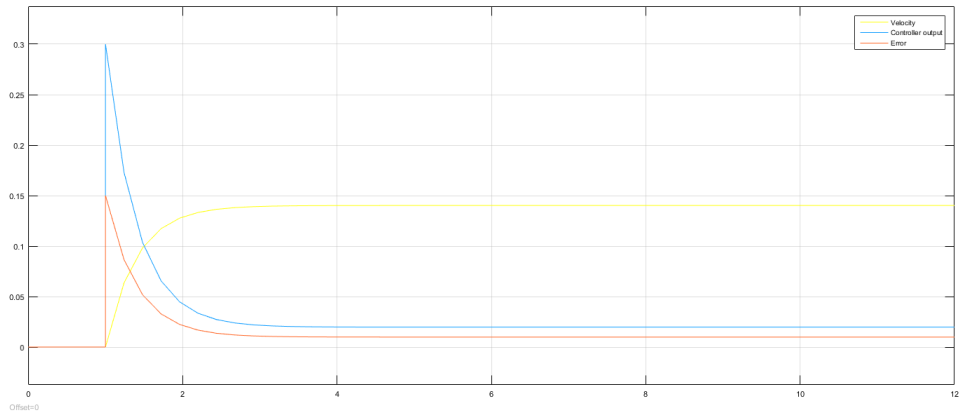
Figure 4.3: Root locus plot for the right motor

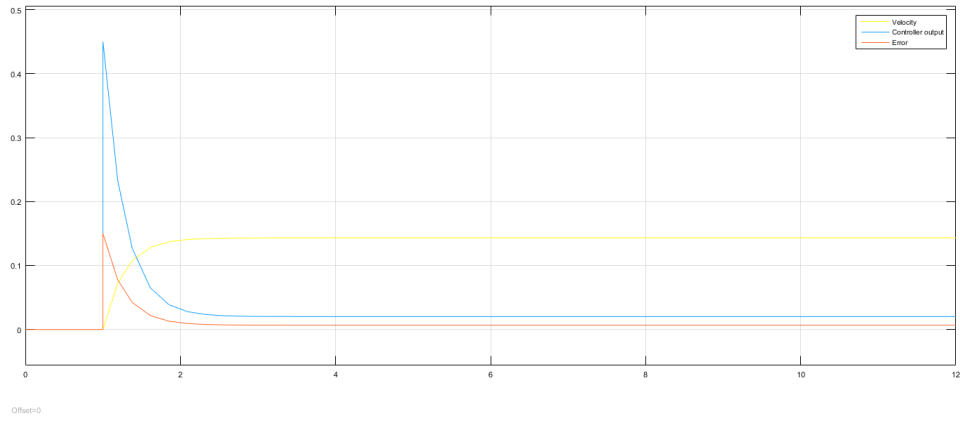Figure 4.4: Simulink simulation of the right motor behaviour for $K = 2$

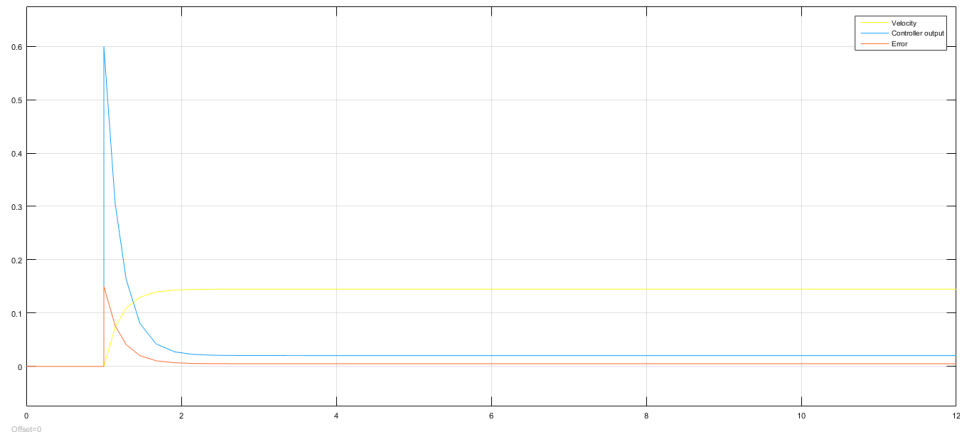Figure 4.5: Simulink simulation of the right motor behaviour for $K = 3$

Figure 4.6: Simulink simulation of the right motor behaviour for $K = 4$
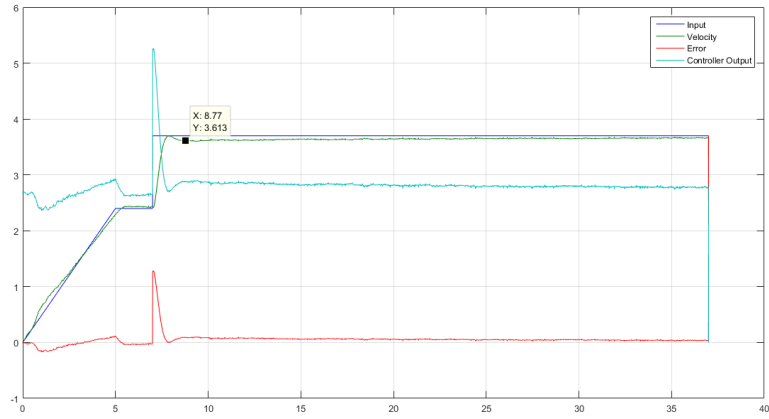
Figure 4.7: Response of the left motor behaviour for $K = 2$ to the blue curve as input.
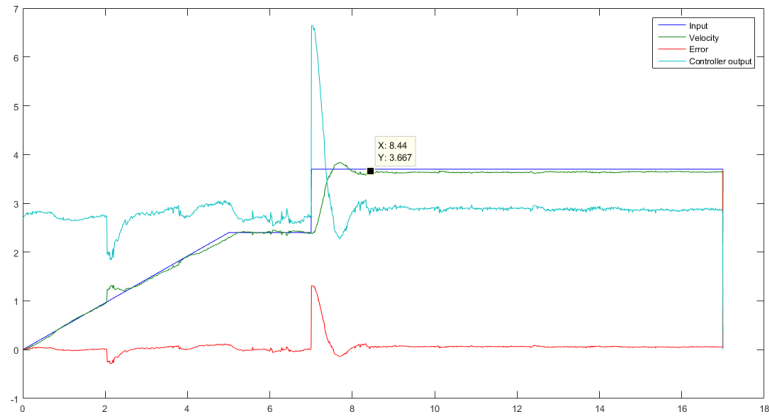

Figure 4.8: Response of the left motor behaviour for $K = 3$ to the blue curve as input.

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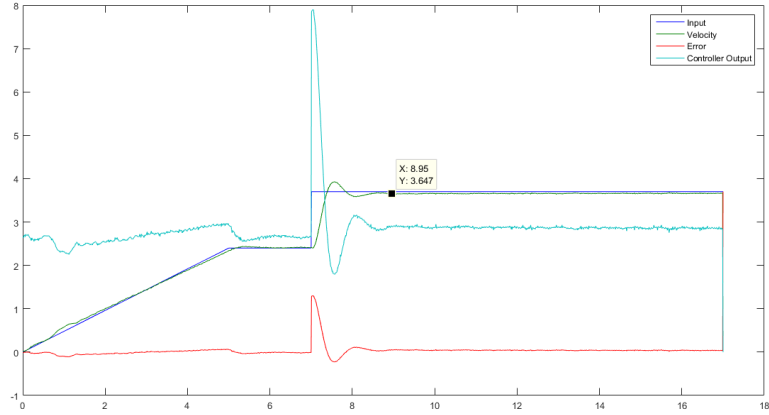
Figure 4.9: Response of the left motor behaviour for $K = 4$ to the blue curve as input.

4.4 Conclusions

A proportional controller was chosen to have a fast response to disturbances. The fact that there can be a steady state error is less important since this loop is controlled by another feedback loop. The outer loop will be able to compensate for the steady state error.

As we did for the other motor, the behaviour was identified using a step between two operating points. Starting from the obtained transfer function some simulations and experiments were done with proportional control. Finally a gain of $K = 3$ was selected.

Chapter 5

Modelling and Control of the Traction

5.1 Modelling of the Traction of the Metallic Strip

As presented in the introduction, we know from a physical intuition that the traction in the metallic strip depends mainly on the difference of speed between the rolls, rather than on each of the speeds individually. For this reason, we only have to determine $Trac(s)$ as described in figure 5.1, where ω_i is the speed of a motor, and f is the traction of the metallic strip[1].
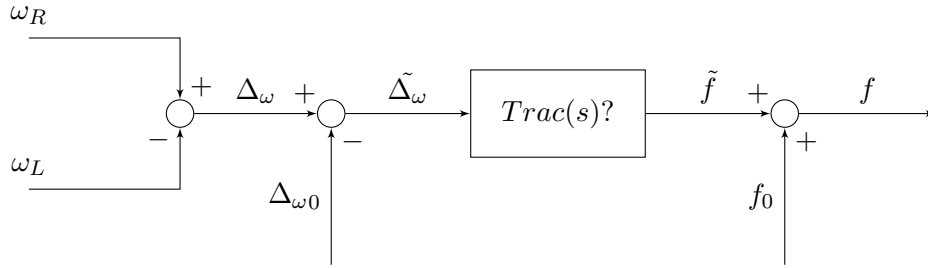
Figure 5.1: Simple gray-box model of the traction of the metallic strip

Furthermore, we also know that $Trac(s)$ should contain a close-to-perfect integrator. Indeed, if we increase Δ_ω slightly from the setpoint $\Delta_{\omega 0}$, we ex-

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[1]Since we do not control the middle pair of rolls, we are not able to control the left and right traction separately. For this reason, in the following, we only care about controlling the right traction, which is denoted f but sometimes f_R in the matlab figures. With this setup, the left traction has roughly the same evolution as the right traction, multiplied by a coefficient slightly lower than 1.

pect the tension in the metallic strip to rise indefinitely until breakage. This is also confirmed by the experience: we observe that the system's response to a real world pulse is really close to a step, as showed in figure 5.2. Fi-
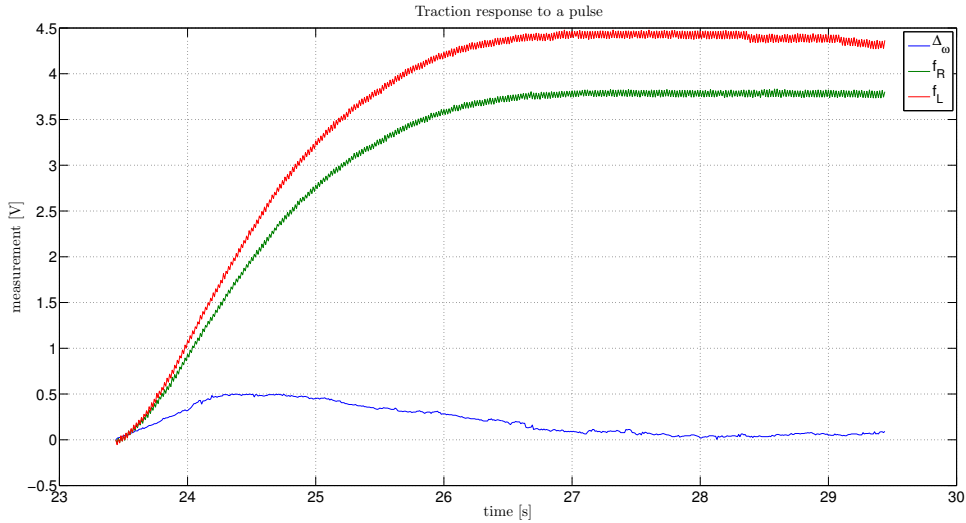

Figure 5.2: Traction response to a real world pulse

nally, this is supported by a second order numerical approximation of the dynamics, which always yields a pole that is very close to zero.

However, this leads the rest of the optimisation problem to be badly conditioned. This means that the second pole is not reliably placed, and that the final result does not fit the real response accurately. Moreover, the obtained transfer function, with a very large K and p_2, takes a long time to simulate with simulink.

To solve this, we refine our gray-box approximation by artificially introducing an integrator in the system we want to identify. We then compute its response to $\tilde{\Delta}_\omega(t)$ and try to determine the rest of the dynamics based on this new input and the observed response, as shown in figure 5.3, where $\frac{1}{s} \cdot H(s) = Trac(s)$. In the figure, we also use the fact that only ω_L is supposed to contribute to $\tilde{\Delta}_\omega$, since the master velocity is chosen steady. $\tilde{\omega_R}$ is thus considered as a disturbance.

Fitting a simple first order transfer function to $H(s)$ is not easy because the dynamics between $\int_0^t \tilde{\omega}_L(t)$ and $f(t)$ is very fast, as shown in figure 5.4. This leads to very large poles which are not well approximated and difficult to simulate, as experienced previously.

To solve this, we try to fit $H(s)$ with a transfer function of the form
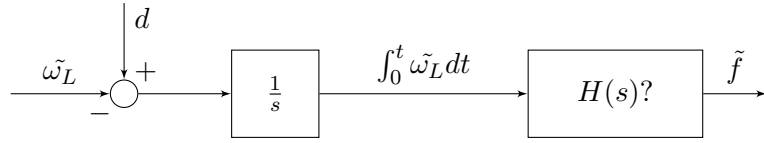
21

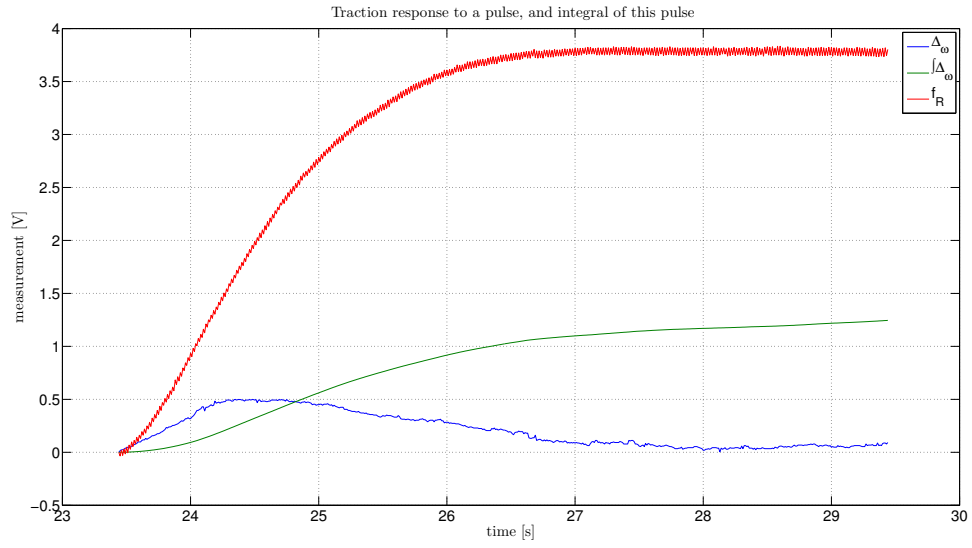Figure 5.3: Gray-box model of the traction of the metallic strip

Figure 5.4: Right traction response to a pulse and output of the intermediate integrator

$K\frac{s-z_1}{s-p_2}$, because the introduction of a zero speeds up a step response, which would bring p_2 reasonably closer to the origin. The result is shown in figure 5.5, where we see that $Trac(s)$ as given in equation 5.1 seems to fit the experience very well.

$$H(s) = 13.096 \cdot \frac{s + 0.9221}{s + 4.063}$$

$$Trac(s) = 13.096 \cdot \frac{s + 0.9221}{s(s + 4.063)} \tag{5.1}$$
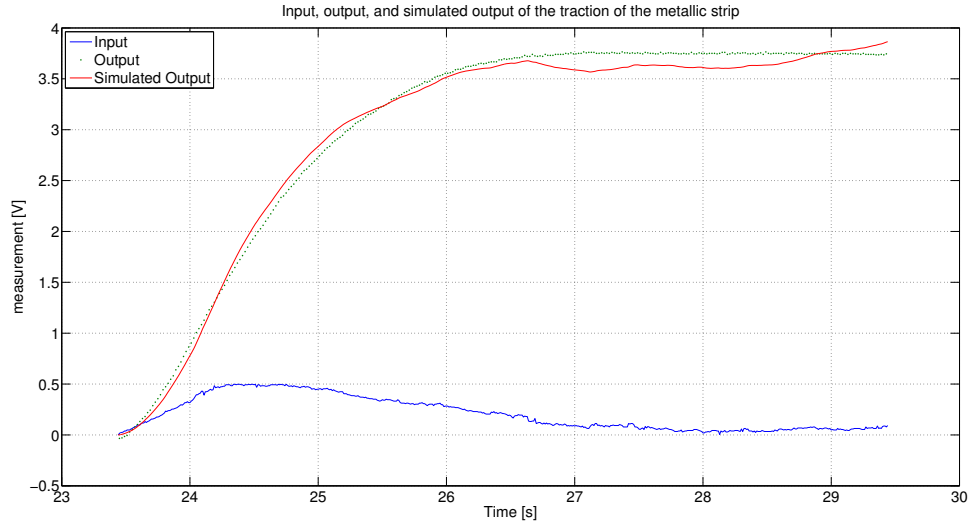
Figure 5.5: Input, output, and simulated output of the traction of the metallic strip

5.2 Control of the Traction

5.2.1 Simple P Controller

Since there already is an integrator in the system, and since we do not have specifications on the transient response, we first try to control the traction with a simple P controller, which should provide asymptotic stability and zero steady-state error. Figure 5.6 shows the root locus of the traction for this controller, with the approximation that the inner slave speed loop is fast enough to be considered perfectly transparent. The root locus shows

Figure 5.6: Root locus of the traction

that $k_P < 0$[1] can be theoretically chosen as high as desired while keeping the closed-loop poles on the real axis.

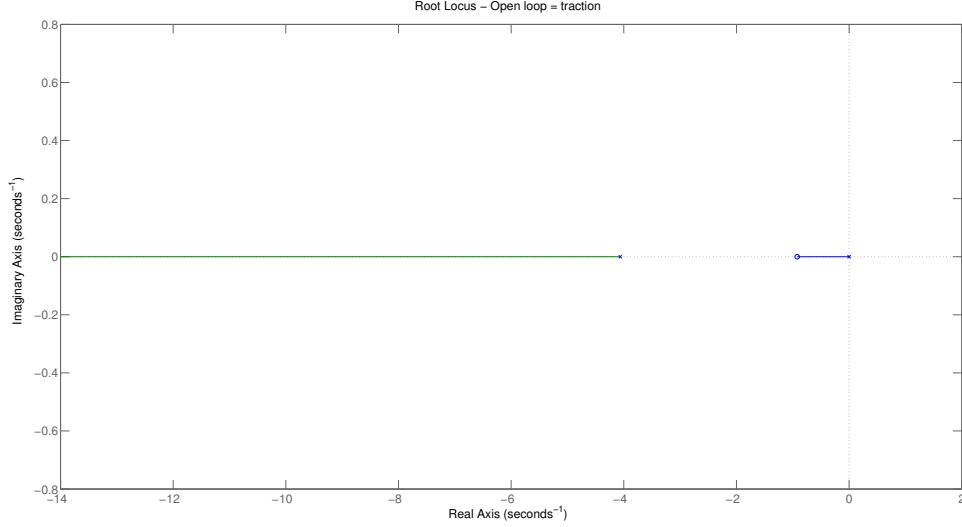Figure 5.7 shows the closed-loop traction response to a constant reference, with an arbitrary gain of -1, as simulated by simulink. First, we observe that the closed-loop poles are not real, which is due to non linearities and higher order effects. More importantly, we see that the steady-state error is not cancelled.

Comparing the measured traction and the master speed, we observe that the initial ramp on the master motor is not compensated. In steady state, the master speed also creates an offset on the traction. This is because the right velocity is actually a disturbance, as was shown in figure 5.3. This disturbance is not rejected because the integrator is in the plant, and not in the controller.

To achieve perturbation rejection, an integrator should be added to the controller. However, this is not a good solution as is, because the open loop would then contain two integrators. This would greatly reduce the phase margin and thus make the closed loop system nearly unstable and slow its response down.

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[1]The $\tilde{\omega}_L$ input is inverting, as shown in figure 5.3
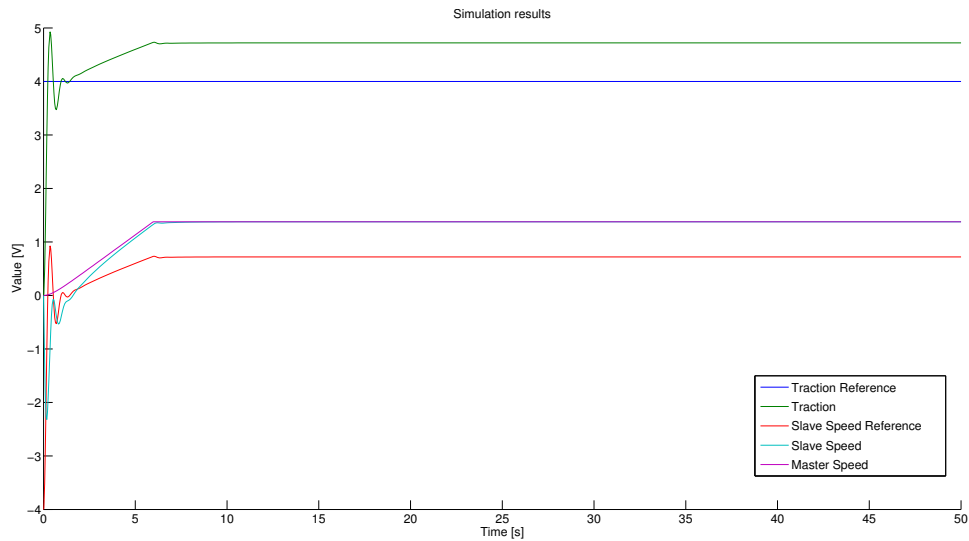
Figure 5.7: Simulation of the rolling mill operation with a P controller on the traction

5.2.2 Second Loop: PI Controller

Rather then adding an integrator to the existing controller, we can add a second external loop with a PI, as shown in figure 5.8 ,to achieve pertur-

Figure 5.8: Final controller architecture

bation rejection while preserving the phase margin. In this subsection, the reasoning behind this second loop will be explained. In the following, we do not neglect the effect of the inner slave speed loop anymore. However, we do make the approximation that the traction is a essentially an integra-

tor[1]. The plant that is controlled using an inner P and an outer PI is thus approximated by the series of the closed loop transfer function of the slave motor and an integrator – the transfer function of the traction.
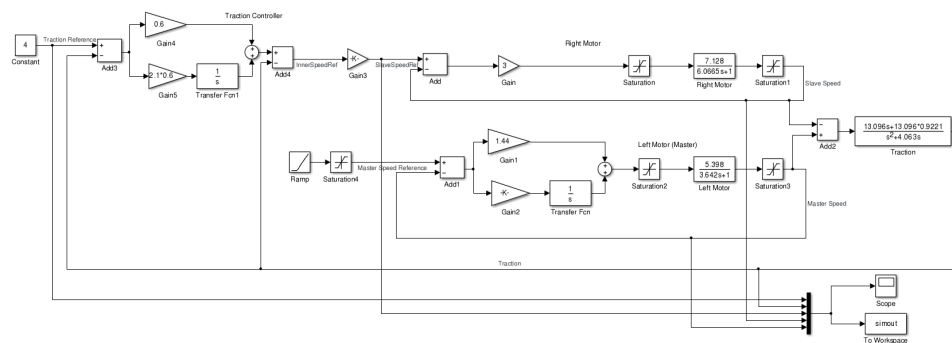
With that in mind, the closed loop poles of the inner traction loop are given by figure 5.9 ,which shows the root locus of $Slave(s) \cdot Trac_{approx}(s)$.
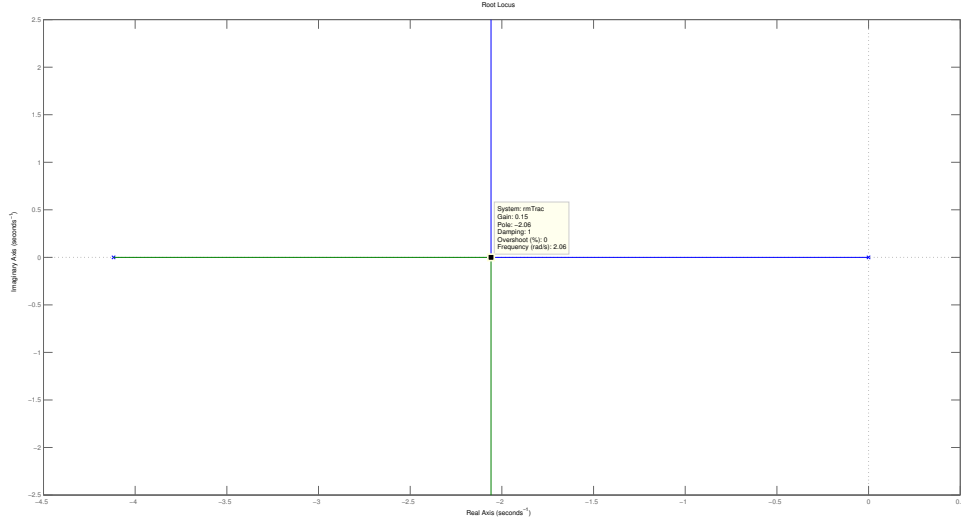

Figure 5.9: Root locus of the inner traction loop

We observe that using a P controller, it is possible to move the integrator pole into the LHP, which is the essence of feedback control. This is the reason why we can now afford to add a PI outer loop: for an adequate choice of $K_{p_{inner}}$, the plant, which is given by closed loop transfer function of the inner traction loop, can have two real, negative poles. This means that adding a PI to it will ensure a reasonable phase margin, as well as zero steady state error and perturbation rejection.

On figure 5.9 we choose $K_{p_{inner}} \lessapprox 0.15$ to obtain the fastest possible real poles for the inner loop. This yields a pair of real poles around -2. There is now left to determine the gains of the outer PI, given those inner loop poles to complete the controller design of our rolling mill.

To do so, we use the classical approach of cancelling the slowest pole in the plant with the zero from the PI, and then determining a first $K_{p_{outer}}$ with a root locus. The resulting plot is shown in figure 5.10. From the root locus, we can extract two reasonable first values: $K_{p_{outer}} \lessapprox 0.52$ would

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[1]Neglecting the higher order zeroes and poles in $Trac(s)$ given in equation 5.1, we obtain $Trac_{approx}(s) = \frac{7.16}{s}$.
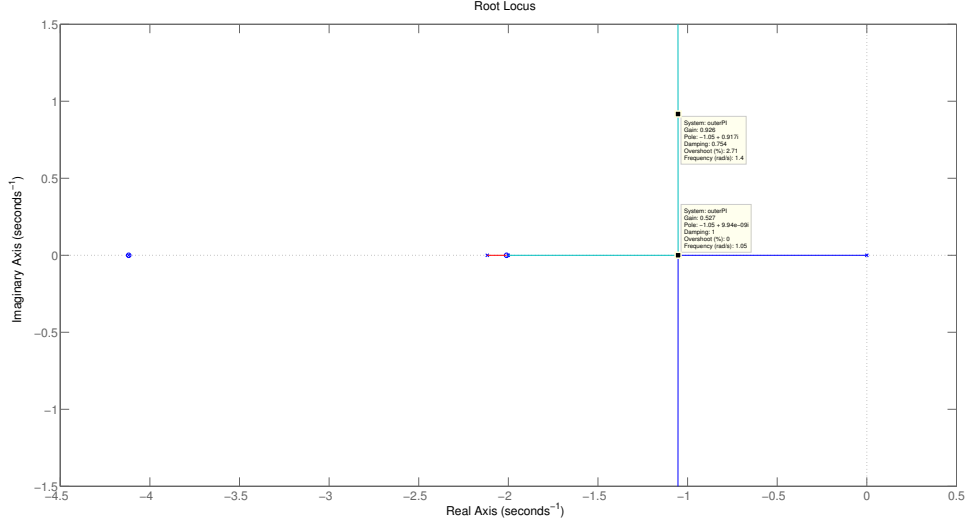
Figure 5.10: Root locus of the outer traction loop

provide the fastest real poles and $K_{p_{outer}} \approx 0.93$ would provide a damping of 0.7 – any value inbetween could also be a good first choice. K_i is then determined accordingly using $K_i = |z_{PI}| \cdot K_{Pouter}$. The root locus also shows us that if the poles of the inner loop are not perfectly known and z_{PI} cannot be placed perfectly, $p_{inner\,fast} < z_{PI} < p_{inner\,slow}$ is better than $p_{inner\,fast} < p_{inner\,slow} < z_{PI}$, because the latter pole-zero configuration would make the closed loop poles leave the real axis, as shown in figure 5.11.

With this controller, we should be able to move the integrating pole from the plant to the controller. The total closed loop should thus be stable and have zero steady-state error, perturbation rejection and a reasonable phase margin. In the following section, we will verify this design using simulink simulations and real world experiences and tune the gains if necessary.

5.3 Tuning of the PI Controller

Figure 5.12 shows the the simulated output of the rolling mill with the following gains:

$$K_{p_{inner}} = -0.14$$
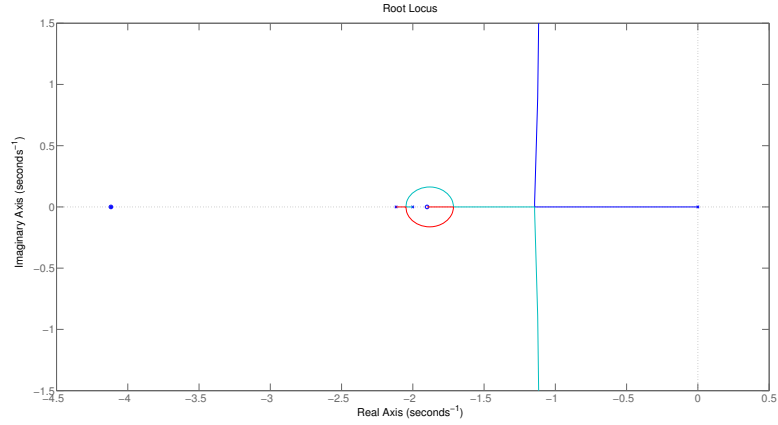$$K_{p_{outer}} = 0.6$$
$$K_i = 1.26$$

Figure 5.11: Root locus of the outer traction loop with a bad pole-zero configuration
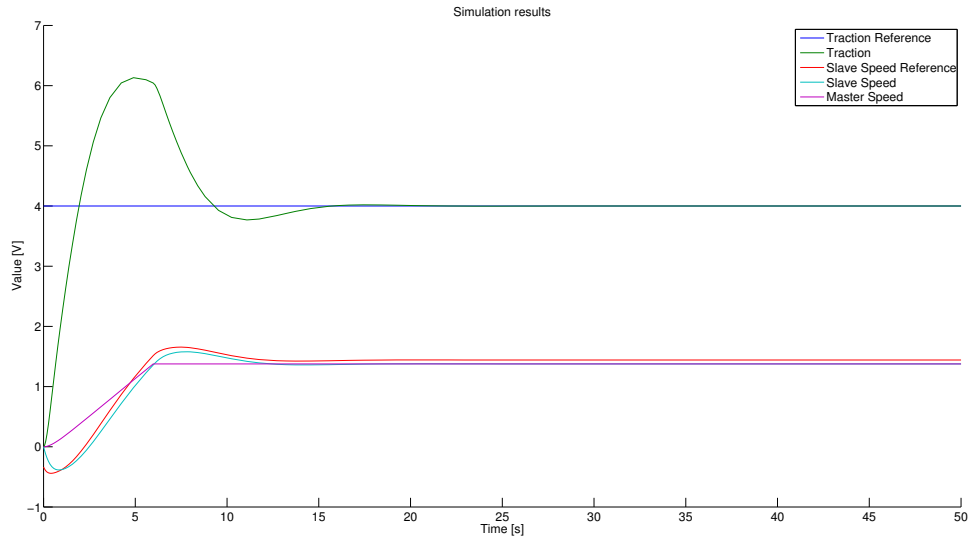

Figure 5.12: Simulation of the rolling mill operation with a P - PI controller on the traction. $K_{p_{outer}} = 0.6$.

We see that all the desired properties are achieved. However, the effect of the master speed ramp is still present, which is normal since a single integrator in the controller is able to reject perturbation of order ≤ 1. This is supported by the experience, as shown in figure 5.13.
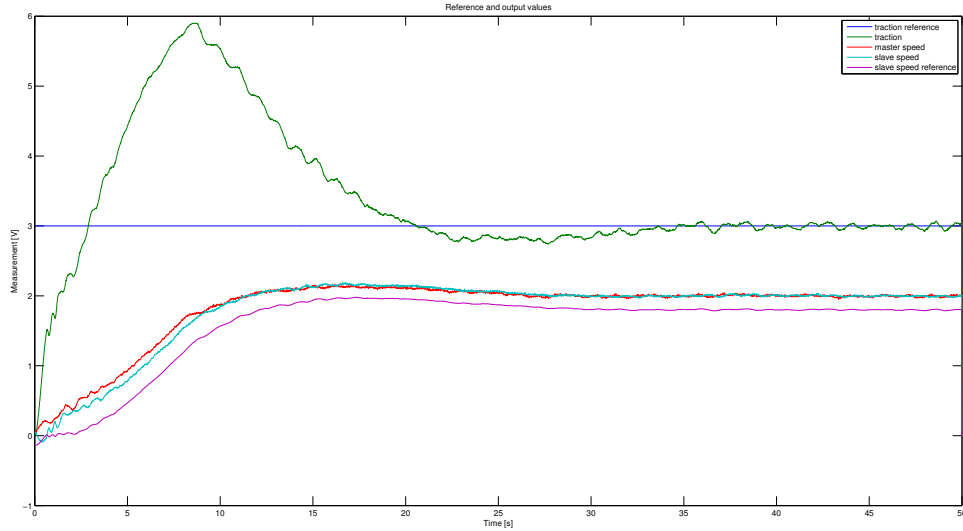
Figure 5.13: Operation of the rolling mill. $K_{p_{outer}} = 0.327$.

As a result, the controller should be tuned first and foremost to limit the overshoot induced by the initial ramp, because a measured traction $> 6\,\mathrm{V}$ is dangerous for the plant. We should thus increase $K_{P_{outer}}$ until the traction overshoot is low enough, and then check if the resulting lower damping is still satisfying.

Fortunately, figure 5.14 shows that values 5.2 - 5.4 along with an initial ramp on the traction provide an acceptable overshoot and sufficient damping. Figure 5.15 finishes the validation this design by showing that the actuators do not go into saturation and are reasonably sollicitated during normal operation.

Figure 5.14: Operation of the rolling mill. $K_{p_{outer}} = 2$.

$$K_{p_{inner}} = -0.14 \qquad (5.2)$$
$$K_{p_{outer}} = 2 \qquad (5.3)$$
$$K_i = 4.2 \qquad (5.4)$$

Figure 5.15: Actuators values during operation with the final controller

Chapter 6

Thickness control

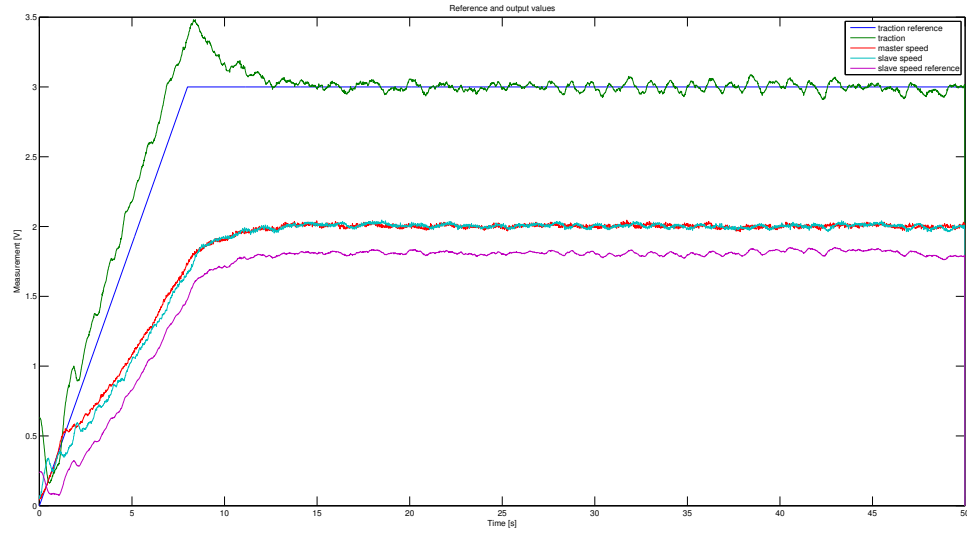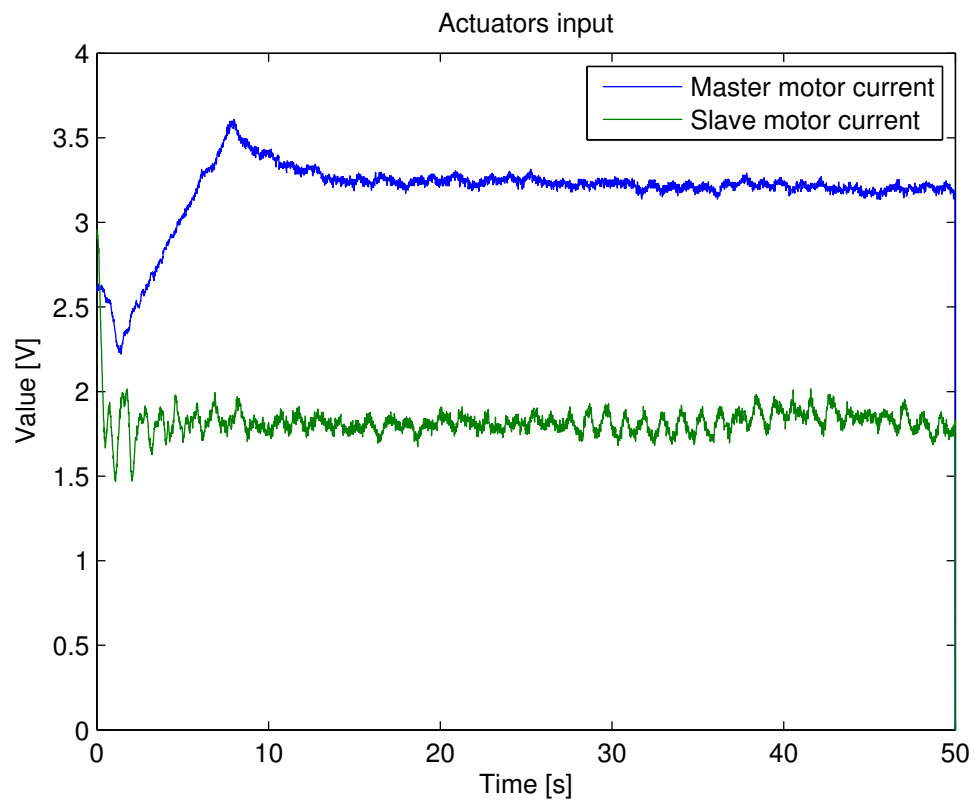In this section some considerations will be made about the more advanced objectives. Since the more advanced objectives are not attainable in the course of the lab sessions only some theoretical reflections will be made. The more advanced objective was to design a controller to control the thickness of the rolled metal strip.

6.1 Workings

The full workings of the mill are as follows: One motor unwinds the metal strip from a spool. The metal strip passes between two cylinders driven by a second motor. The metal is compressed between these too cylinders and is subsequently wound up by the third motor. The thickness is controlled by the distance between the two rolls. This distance can be controlled manually by a crank.

We have three motors as actuators, one manual setting, and multiple sensors:

- Thickness sensor before the rolls

- Thickness sensor after the rolls

- Traction sensor before the rolls

- Traction sensor after the rolls

- Velocity sensors for each of the motors

- Rolling force sensor

The reasons the objective is not attainable are that de DAQ has not enough outputs, and the complex relation between the thickness and the parameters of the actuators.

6.2 Controller considerations

The broad design of the controller will again be a gray-box approach using a cascade controller since it is almost impossible to model the behaviour of the motors and rolling using the physical relations.

Instead of designating one of the winding motors as master now the central rolling motor is designated as master. This motor should be controlled using a PI controller to keep its velocity constant and disturbance free. The two other motors should use a proportional controller to have a fast response to their reference inputs.

Both the slave motors will be controlled so they match the speed of the master motor while keeping the tension at a certain value.

The most outer loop sets the speed and the tension using a lookup table with the relation of all the parameters such as the speed, thickness of the metal strip, rolling force and tension.

Appendix A

Controller code

```matlab
%controller.m
function [time, reference, output, input, innerTractionRefArray, rSpeedRefArray] = controller()

    %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
    %Control System Design Lab: Overall Controller Loop
    %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
    %%
    %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
    %Setup
    %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

    T_S = 0.01;%Set the sampling time.


    function [nSamples, time, reference, output, input] = referenceGenerator()
        %REF(1,:) = traction
        %REF(2,:) = master speed

        %traction
        EXP_LENGTH = 50;%sec
        TRACTION_REF = 3;
        TRAC_SETUP_TIME = 8;

        tracRamp = 0:T_S*TRACTION_REF/TRAC_SETUP_TIME:TRACTION_REF;
        reference(1,:) = [tracRamp TRACTION_REF*ones(1, EXP_LENGTH/T_S - length(tracRamp))];

        %master
        SETUP_TIME = 8;%seconds
        SETUP_POINT = 2;%V Left Motor

        ramp = 0:T_S*SETUP_POINT/SETUP_TIME:SETUP_POINT;
        rampLength = length(ramp);

        reference(2,:) = [ramp ones(1,length(reference(1,:))-rampLength)*SETUP_POINT];

        nSamples = length(reference);
        time=0:T_S:(nSamples-1)*T_S;
        output = zeros(2, nSamples);
        input = zeros(8, nSamples);
    end
```

```matlab
%%
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%Controllers
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
function current = lmController(speedRef, measuredSpeed)
  if speedRef < 0
    FRICTION_COMPENSATOR  = -2.7;
  else
    FRICTION_COMPENSATOR  = 2.7;
  end
  KP = 2;
  KI = KP/3.642;

  persistent errorIntegral;
  if isempty(errorIntegral)
    errorIntegral = 0;
  end

  error = speedRef - measuredSpeed;
  errorIntegral = errorIntegral + error*T_S;

  current = FRICTION_COMPENSATOR + KP*error + KI*errorIntegral;
end

function current = rmController(speedRef, measuredSpeed)
  if speedRef < 0
    FRICTION_COMPENSATOR  = -2.1;
  else
    FRICTION_COMPENSATOR  = 2.1;
  end
  KP = 3;

  error = speedRef - measuredSpeed;
  current = FRICTION_COMPENSATOR + KP*error;
end

function speedRef = innerLoopSpeed(traction, innerTractionRef)
  K = -0.123;
  speedRef = K*(innerTractionRef-traction);
end

function innerTractionRef = outerLoopTraction(traction, tractionRef)
  persistent errorIntegral;
  if isempty(errorIntegral)
    errorIntegral = 0;
  end
  K = 2;
  ZERO = 1.9;
  KI = ZERO*K;
  error = tractionRef - traction;
  errorIntegral = errorIntegral + error*T_S;
  innerTractionRef = K*(error) + KI*errorIntegral;
end
```

```matlab
%%
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%Main Loop
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
[nSamples, time, reference, output, input] = referenceGenerator();
%precompute the reference and generate arrays of according size
innerTractionRefArray = zeros(1,nSamples);
rSpeedRefArray = zeros(1,nSamples);
i=1;
while i < nSamples
  tic %Begins the first strike of the clock.
  [input(1,i), input(2,i), input(3,i), input(4,i), input(5,i), ...
    input(6,i), input(7,i), input(8,i)]  = anain; %Acquisition of the measurements.

  rmVelocity = input(5,i); %saving the inputs in a variable for ease of working
  lmVelocity = input(4,i);
  lTraction = input(3,i);
  rTraction = input(2,i);

  if(lTraction > 6 || rTraction > 6) % safety measures if traction is to high
    lmCurrent = 0;
    rmCurrent = 0;
    i = nSamples + 1;
  else
    lmCurrent = lmController(reference(2,i), lmVelocity);

    %Cascade loops
    innerTractionRef = outerLoopTraction(rTraction, reference(1,i));
    rSpeedRef = innerLoopSpeed(rTraction, innerTractionRef);
    rmCurrent = rmController(rSpeedRef, rmVelocity);
    innerTractionRefArray(i) = innerTractionRef;
    rSpeedRefArray(i) = rSpeedRef;
  end

  output(2,i) = rmCurrent;
  output(1,i) = lmCurrent;
  anaout(lmCurrent, rmCurrent);

  if toc > T_S
    disp('Sampling time too small');%Test if the sampling time is too small.
  else
    while toc <= T_S
      %Does nothing until the second strike of the clock reaches the sampling time set.
    end
  end
  i=i+1;
  end
end
```

```matlab
%main.m
openinout;
[time, reference, output, input, innerTractionRef, rSpeedRef] = controller();
anaout(0,0);
closeinout;
%%
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%Plots
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
figure %Open a new window for plot.
plot(time,reference(1,:), time, input(2,:), time,...
  input(4,:), time, input(5,:), time, rSpeedRef); %Plot the experiment (input and output).
legend('traction reference','traction','master speed',...
  'slave speed', 'slave speed reference');
title('Reference and output values')
xlabel('Time [s]');ylabel('Measurement [V]');

figure;
plot(time, output(1,:), time, output(2,:));
legend('Master motor current', 'Slave motor current');
title('Actuators input')
xlabel('Time [s]');ylabel('Value [V]');
```