



# 1 Introduction

Neutrons stars are curious objects encompassing many still unsolved problems of modern physics and astrophysics. Their unique nature makes them ideal laboratories for many of the most energetic phenomena in space. Born from the ashes of a supernova, they begin their life only when some other normal star fades away and dies in a spectacular supernova explosion.<sup>1</sup> From there on, they continue their life by slowly collecting the surrounding interstellar matter or by devouring an unlucky companion star floating next to them. It is not the impressive  $\sim 10^{30}$  kilograms they weight but the mere  $\sim 10$  km in radius sphere that they encapsulate this material into that is then able to bend the spacetime itself. Such an impressive feat rewards them with a categorization into a special stellar group called *compact objects*. Along with white dwarfs and black holes, these strange compact objects have been under a scientific scrutiny for almost nine decades now. Still, some of the most fundamental questions remain: What are neutron stars made of? How big are they? How do we see them?

In the next few sections, we will start our journey by building our intuition of these peculiar objects habiting the Space around us. A short history of their discovery is given, followed by simple physical arguments why we actually expect them to exists in a first place. Next, some actual observable phenomena is reviewed. These are also closely connected to the surroundings and environments of the neutron stars, and hence those will be discussed and described also.

## 1.1 Short history

### 1.1.1 From imagination into a reality

In 1908, Lev Landau was born in Baku, Azerbaijan. Lev turned out to become a brilliant Soviet scientist who already at an age of 14 matriculated from the Baku State University studying in both, Department of Physics and Mathematics, and the Department of Chemistry simultaneously. Soon after that he became disinterested in chemistry but continued to be fascinated by physics through his whole career. In 1931, at an age of 23, Landau published an exceptional paper where he speculated on the existence of stars containing matter on nuclear densities:<sup>2</sup>

*...the density of matter becomes so great that atomic nuclei come in close contact, forming one gigantic nucleus.*

What made this paper exceptional was that it was done before the existence of neutrons were confirmed, hence proposing that quantum mechanics might be violated as the atoms consisting of protons and electrons only would live together. Nevertheless, it marked the first theoretical speculation on the existence of what we now know as neutron stars.

Lev needed not to wait for long. It was already next year in 1932, that James Chadwick then confirmed that neutrons really were a fundamental part of our nuclear physics with his works dubbed as *Possible*

<sup>1</sup> For the pedantic ones, we specify that a supernova is actually an implosion followed by a subsequent explosion.

<sup>2</sup> [1] L. D. Landau. *Phys. Z. Sowjetunion*. (1932).

*Existence of a Neutron*<sup>3</sup> and a later follow-up of *Existence of a Neutron*<sup>4</sup>. His findings then became to confirm the theoretical predictions of his supervisor Ernest Rutherford made already in 1920<sup>5</sup>. Later on Chadwick was awarded the Nobel Prize in physics (1935) of his findings. Chadwick himself continued his career as part of the Manhattan project, as it was basically his work that inspired the U.S. government to begin a serious atomic bomb research.

Now that the existence of the neutron was confirmed, it did not take long for others, independent of Landau, to propose similar stars. One year after the discovery, in December 1933 at the Meeting of the American Physical Society at Stanford, Wilhelm Baade and Frank Zwicky made their famous propose that Supernovae should be considered as a new category of astronomical objects.<sup>6</sup> At the same time they also stated:

*...we advance the view that a super-nova represents the transition of an ordinary star into a neutron star, consisting mainly of neutrons. Such a star may possess a very small radius and an extremely high density.*

Such a statements were, however, deemed as a work of imagination from a bunch of weird theorists. Zwicky, on the other hand, kept on insisting that neutron stars are really out there. A.G.W. Cameron, a former post-doc during the 1959–1969 at Caltech where Zwicky was also situated, recalls:

*For years Fritz [Zwicky] had been pushing his ideas about neutron stars to anyone who would listen and had been universally ignored. I believe that the part of the problem was his personality, which implied strongly that people were idiots if they did not believe in neutron stars.* (Cameron, 1999)

Progress on the theoretical understanding of neutron stars was also tightly connected to understanding the interiors of white dwarfs. Unlike the mysterious nuclear forces related to neutrons, white dwarfs physics was more related to understanding the behavior of electrons. A breakthrough came in 1925 when a young Paul Dirac formulated the quantum wave equations for the motion of the electrons<sup>7</sup>. What soon followed, was a description of a pressure of degenerate electron gas by Ralph Fowler, Dirac's supervisor<sup>8</sup>. Implications of this were severely against the previously known physics: Even in zero temperature, there would be a degeneracy pressure preventing matter from collapsing caused by the exclusion principle of quantum mechanics.

Using a simplified uniform density approximation, Edmund Stoner was then able to show that this implied a maximum mass limit for white dwarfs.<sup>9</sup> Thus, a surprising result was obtained: when the density of a white dwarf approaches infinity, the mass reaches a maximum value. It was later on realized by German-Estonian Wilhelm Anderson that the electrons in this problem must actually be treated relativistically<sup>10</sup>, something omitted by Stoner. Anderson also tried to correct the crude mistake by deriving the equation of state of relativistic degenerate electron gas but ended up making severe mistakes. It was then Stoner who corrected his equations, based on the communications with Anderson, and re-derived his maximum mass limit. Regardless of Stoner's efforts, the maximum mass limit was later named Chandrasekhar's mass limit for its importance in astrophysics.

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<sup>3</sup> [2] J. Chadwick. *Nature*. (1932).

<sup>4</sup> [3] J. Chadwick. *Proceedings of the Royal Society of London Series A*. (1932).

<sup>5</sup> [4] E. Rutherford. *Proceedings of the Royal Society of London Series A*. (1920).

<sup>6</sup> [5] W. Baade and F. Zwicky. *Proceedings of the National Academy of Science*. (1934); [6] W. Baade and F. Zwicky. *Phys-*

*ical Review*. (1934).

<sup>7</sup> [7] P. A. M. Dirac. *Proceedings of the Royal Society of London Series A*. (1925).

<sup>8</sup> [8] R. H. Fowler. *MNRAS*. (1926).

<sup>9</sup> [9] E. C. Stoner. *Philos. Mag.* (1930).

<sup>10</sup> [10] W. Anderson. *Zeitschrift für Physik*. (1929).

This was to honor Subrahmanyan Chandrasekhar, a young prolific Indian physicist and astrophysicist who was working on the same topic after reading Fowler's paper on the degenerate electron gas. Unlike Stoner's limit computed using the uniform density approximation, Chandrasekhar realized that a polytropic density profile is a more physical, albeit mathematically more challenging, formulation. 19 years old Chandrasekhar, already known for his mathematical skills, was still able to numerically integrate the equations by hand and obtained a similar limiting mass<sup>11</sup>. Later on, it has been, however, found that Chandrasekhar was not even the second person to derive the mass limit, but third:<sup>12</sup> A soviet physicist Yakov Frenkel published a similar derivation, independently and unknowingly of the progress in the west, where he applied the relativistic degenerate electron gas results to white dwarfs, and concluded that a similar upper limit on the mass exists<sup>13</sup>. It was, however, due to the slow publishing speed in the Soviet journals, that his work never became available to his western peers.

Nevertheless, a maximum mass for a white dwarf was laid out, and in the end after all the relevant physical inclusions, it turned out to be  $1.44 M_{\odot}$ , or 1.44 times the mass of our Sun. What makes this limit even more important is that a maximum mass for a white dwarf is just an minimum mass for a neutron star. An important connection first made by George Gamow in 1939<sup>14</sup>. Idea behind this is simple: If it is the degenerate electron gas pressure, quantum mechanical in nature, that keeps the white dwarfs from collapsing, what happens when the maximum mass is attained and even this pressure is not able to resist the forces of gravity? At a conference in Paris in 1939, Chandrasekhar then laid out the answer:

*If the degenerate core attain sufficiently high densities, the protons and electrons will combine to form neutrons. This would cause a sudden diminution of pressure resulting in the collapse of the star to a neutron core.*

A neutron star should thus have a mass close to the Chandrasekhar limit, i.e.  $M \sim 1.44 M_{\odot}$ , and consists of neutron only. Exactly like proposed by Landau eight years ago without knowing anything about neutrons yet, or later on by Baade and Zwicky when they presented their theory of supernovae!

It was then before the second World War, that a solid basis for a theory of neutron stars was laid out. This was, however, just the beginning. Next question would be the critical one that we are still trying to find the answer to: If they exists, how big are they? The problem was that because of the extremely dense nature of these objects, the standard stellar equilibrium equations were not valid anymore, and because of this, it was not possible to estimate even the size of the star. The problem was unwieldy because it was general relativistic in nature: The immense mass of the neutron star was bending the spacetime itself, and more compact it was, the more it could bend it. On the other hand, the more curved the spacetime was, the more the star would gain weight.

It was already during the same year in 1939 as Gamow's remark, that a theoretical framework for studying this was published. This was done independently by Richard Tolman<sup>15</sup>, and Robert Oppenheimer together with his student George Volkoff<sup>16</sup>. Both papers were even submitted on the same day, 3rd of January, to Physical Review and were published on the same February issue. More importantly, they both described a hydrostatic equilibrium for a spherically symmetric object in general relativity, exactly what is needed to study neutron stars. Because of the utter importance, the solution is now known as Tolman-Oppenheimer-Volkoff equation. In addition, Oppenheimer and Volkoff applied their equation and numerically calculated a structure of a neutron star consisting of non-interacting strongly degenerate neutron gas. This marked the first try in characterizing neutron stars. Similar to white dwarfs, they also obtained an upper limit for the

<sup>11</sup> [11] S. Chandrasekhar. *MNRAS*. (1931).

<sup>12</sup> [12] D. G. Yakovlev. *Physics Uspekhi*. (1994).

<sup>13</sup> [13] J. Frenkel. *Zeitschrift für Physik*. (1928).

<sup>14</sup> [14] G. Gamow. *Physical Review*. (1939).

<sup>15</sup> [15] R. C. Tolman. *Physical Review*. (1939).

<sup>16</sup> [16] J. R. Oppenheimer and G. M. Volkoff. *Physical Review*. (1939).

mass. As a disappointment for everybody, it was, however, calculated to be of around  $0.7 M_{\odot}$ , i.e. less than the Chandrasekhar limit of  $1.44 M_{\odot}$  for white dwarfs, indicating that neutron stars could not exist in nature. It took almost two decades then to show that it was actually the assumption of no interaction between the neutrons that was causing this hiccup.

More over, it was not actually Tolman, or Oppenheimer and Volkoff who first discovered general relativistic hydrostatic equation. It was now Chandrasekhar's turn to avoid having an important result credited to him: Together with John Von Neumann, Chandrasekhar extended his work on white dwarfs to cover also neutron stars and in the process derived exactly the same equilibrium equation in 1934, i.e., five years before the groundbreaking publication of Tolman, Oppenheimer and Volkoff.<sup>17</sup> It is, however, worth mentioning that later on, in 1983, Chandrasekhar received a Noble prize in physics for his work on "theoretical studies of the physical processes of importance to the structure and evolution of the stars". So he certainly received at least some credit from his important work.

Around the same time, in 1937, Gamow and Landau also independently proposed that a accretion of matter onto a dense neutron star core could be the missing source of energy for stars. This increased the interest towards neutron stars and the field flourished on the 1930s. Soon it was, however, shown that stars are powered not by accretion but by thermonuclear reactions (as suggested in the 1920s by Eddington and others). The interest in neutron stars then faded away and the research focused on weaponing the nuclear forces.

Next big breakthrough came almost 20 years later in the 1950s, when John Wheeler and his collaborators constructed the first realistic equation of state of dense matter<sup>18</sup>. For the outer layers, known as the crust, they applied a semi-empirical mass formula together with the equation of state of degenerate electrons. For the dense core, they assumed a mixture of three ideal Fermi gases compose of neutrons, protons, and electrons. This marked the first consistent formulation for the neutron star structure. It was followed by Cameron who applied the Skyrme equation of state for the high-density matter. This had important conclusions, as he was then able to show that nuclear forces stiffen the matter considerably in comparison to the non-interacting neutrons. Similar to Tolman and Volkoff, he then went on and calculated the maximum possible mass of approximately  $2 M_{\odot}$ . This marked an important theoretical breakthrough as it implied that neutron stars can, after all, exists. A new wave of interest towards neutron stars was thus launched as everybody wanted to observe them.

### 1.1.2 Many observational faces of neutron stars

After Wheeler and Cameron laying the modern foundation for the neutron star structure studies, everybody was eager to find these strange objects from the night sky. It did not take long, when researchers realized that as neutron stars are born in the supernova explosions, we expect them to be hot. Most of the theoretical effort in the 60s was then focused on developing models for the cooling of neutron stars. It was the possible thermal radiation from this cooling that could then be used to detect them. First calculations predicted surface temperatures of  $T \sim 10^6$  K for a neutron star of around 1000 years old<sup>19</sup>. This had important implications for the observers as it means that neutron stars would radiate mainly in the X-rays. Atmosphere of Earth, on the other hand, was impenetrable in the X-ray wavelengths. Luckily, 60s also marked the beginning of golden era for spaceborn observatories.

X-ray observations in space started in the 60's with pioneer experiments by Riccardo Giacconi (Nobel Prize 2002). Several X-ray sources were discovered but their nature remained elusive. The activity was also focused on supernova remnant and a natural target was the Crab nebula.

During the 1920s and 1930s, the Crab nebula was identified as the remnant of a supernova that exploded

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<sup>17</sup> [17] G. Baym. 1982.

<sup>18</sup> [18] J. A. Wheeler. *ARA&A*. (1966).

<sup>19</sup> [19] H.-Y. Chiu and E. E. Salpeter. *Physical Review Letters*. (1964).

on July 4, 1054. A bright star was observed by Chinese, Japanese and Arab astronomers. The "star" remained visible in daytime for 23 days and disappeared from the night sky after two years. Native Americans (Anasazi) might have also observed this event as suggested by the interpretation of a petroglyph in Chaco Canyon.

Already in 1942, Baade and Minkowski found that the central region of the Crab nebula contains an unusual star.

Subsequent theoretical efforts were focused on understanding the origin of the energy powering the Crab nebula.

A radio emission was detected in 1949. In 1953, Shklovsky predicted that this is due to synchrotron radiation by relativistic electrons spiraling along a strong magnetic field. Later the polarization of radio emission was confirmed.

In 1964, Lodewijk Woltjer (who did his PhD with Jan Oort on the Crab nebula) argued that neutron stars could have very strong magnetic fields.<sup>20</sup> This was also independently shown by Ginzburg.<sup>21</sup>

The Crab nebula was observed during a lunar occultation on 7 July 1964. The size of the X-ray source was estimated as 1 light-year  $10^{13}$  km (size of the nebula 11 ly). This was much larger than the typical size of a neutron star (10-20 km).

In 1967, Franco Pacini (who was a young postdoc at Cornell) showed that a rapidly rotating neutron star with a strong dipole magnetic field could power the Crab nebula.

In 1967, Iosif Shklovsky correctly proposed that Scorpius X-1 (found in 1962) is a neutron star accreting matter from a normal star.<sup>22</sup> But his work attracted little attention among astrophysicists

On July 1967 everything changed because of Jocelyn Bell, a graduate student of Anthony Hewish in Mullard Radio Astronomy Observatory. Primitive antenna of wires strung on stakes in a pasture.

She discovered that the signal was pulsing with great regularity, at a rate of about one pulse per second. (1.3s) Temporarily (jokingly) dubbed "Little Green Man 1" (LGM-1) the source (now known as PSR B1919+21) was identified after several years as a rapidly rotating neutron star. Duppied as pulsar, short of pulsating radio source. Later published in Nature 1968 by Hewish.<sup>23</sup>

The other possibility was that pulsars are strongly magnetised rotating neutrons stars as proposed by Timothy Gold (and earlier by Pacini).<sup>24</sup>

The discovery of the Crab and Vela pulsars definitely established the nature of pulsars and confirmed the predictions of Baade and Zwicky 35 years earlier that neutron stars are the compact remnants of supernova explosions.

### X-ray bursts here

Real kick off for X-ray bursts reserach when first long-duration observation were performed with dutch astronomy satellite ANS Hunting for a black hole in the globular cluster NGC 6624 Grindlay and Heise stumbled upon X-ray burst 1975<sup>25,26</sup> Competing group in Los Alamos (Belian et al) 1976<sup>27</sup> Vela(-5) to monitor compliance with the 1963 Partial Test Ban Treaty by the Soviet Union. Could not make an association to a known X-ray source since their positional accuracy was insufficient.

Subsequently Clark et al found using exisiting SAS-3 data from May 1975 a series of ten bursts from NGC6624.1820-303<sup>28</sup> Even more retrospectively 1969<sup>29</sup> 5 second exponential-like decay Cen X-4, Vela

<sup>20</sup> [20] L. Woltjer. *ApJ*. (1964).

<sup>21</sup> [21] V. L. Ginzburg. *Soviet Physics Doklady*. (1964).

<sup>22</sup> [22] I. S. Shklovsky. *ApJ*. (1967).

<sup>23</sup> [23] A. Hewish *et al.* *Nature*. (1968).

<sup>24</sup> [24] T. Gold. *Nature*. (1968).

<sup>25</sup> [25] J. Grindlay and J. Heise. *IAU Circ.* (1975).

<sup>26</sup> [26] J. Grindlay *et al.* *ApJ*. (1976).

<sup>27</sup> [27] R. D. Belian, J. P. Conner, and W. D. Evans. *ApJ*. (1976).

<sup>28</sup> [28] G. W. Clark *et al.* *ApJ*. (1976).

<sup>29</sup> [29] R. D. Belian, J. P. Conner, and W. D. Evans. *ApJ*. (1972).

satellite and later 1971<sup>30</sup> 3U 1735-44 Kosmos 428 belian<sup>31</sup> babushkina 75<sup>32</sup>

Accretion onto a massive black hole.

Pioneering work on thermonuclear instabilities on surface layers of accreting neutron stars.<sup>33</sup> computed stationary burning shells, found that mostly unstable

X-ray bursts were due to thermonuclear flashes on the surface of accreting neutron stars. Laura Maraschi suggested this in early February 1976 when visiting MIT X-ray bursts of nuclear origin?<sup>34</sup> Gamma-ray bursts from thermonuclear explosions on neutron stars?<sup>35</sup>

What are they? Answer came when optical counter part of Cen X-4<sup>36</sup> and Aql X-1<sup>37</sup> was observed.

The first millisecond pulsar was found in 1982 at Arecibo by Backer's team

The theory of magnetars was proposed in 1992 by Robert Duncan, Christopher Thompson and Bohdan Paczynski to explain Soft Gamma Repeaters (SGR). SGRs are repeated sources of X and  $\gamma$ -ray bursts.<sup>38</sup>

The first such object called SGR 0525-66 was discovered. A very intense gamma-ray burst was detected on March 5, 1979 by two Soviet satellites Venera 11 and Venera 12.<sup>39</sup>

## 1.2 From first principles to a neutrons star

### 1.2.1 Background: Sun and stars

Let us first see, what can we learn from neutron stars using simple estimates and conservation laws. Neutrons star are born from a death of a normal star. Most familiar such a star is our Sun  $1.496 \times 10^{13}$  cm from us.<sup>40</sup> With a mass of  $M_{\odot} = 1.99 \times 10^{33}$  g and radius of  $R_{\odot} = 6.96 \times 10^{10}$  cm, our Sun gives us an idea of the typical stellar size scales. Curiously, these numbers also means that the mean density of the Sun is  $\rho_{\odot} \approx 1.41 \text{ g cm}^{-3}$ , a mere  $1.4\times$  the density of the water.

Like all stars, our Sun is held together by the inward pulling gravity. Gravity does not prefer any direction more than some other and, just like we easily observe, a spherical object is expected to form. In addition to the inward-facing force, an outward-facing force is needed to balance the system. For normal stars this force is originating from the thermal pressure.

We observe stars in the night sky because they shine on us. This radiation, and also the origin of the thermal pressure, is from the thermonuclear fusion burning inside the star. *Thermo* here refers to the temperature and heat, *nuclear* to the atomic nuclei, and *fusion* to the process where elements are fused together. During the thermonuclear fusion process, the star's core fuses light elements such as protons into heavier ones like helium. Mass of two protons is less than a mass of one helium atom. This mass difference between the start and end results is then transferred into energy in accordance to the Einstein's famous formula  $E = mc^2$ . A whole sequence of such a fusions takes place inside the star where lighter elements are merged together building heavier and heavier elements. This energy release from the mass-to-energy conversion will then give the star a sufficient thermal pressure support to keep it from not collapsing under the relentless gravity.

The fusion of elements does not continue forever. In the beginning, two protons collide two form a helium. In the next stage three helium nuclei collide to form a carbon, and so on, until iron is created. Production of iron marks the end of the possible fusion chain because fusion of two iron cores does not

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<sup>30</sup> [30] O. P. Babushkina *et al. Soviet Astronomy Letters*. (1975).

<sup>31</sup> [29] R. D. Belian, J. P. Conner, and W. D. Evans. *ApJ*. (1972).

<sup>32</sup> [30] O. P. Babushkina *et al. Soviet Astronomy Letters*. (1975).

<sup>33</sup> [31] C. J. Hansen and H. M. van Horn. *ApJ*. (1975).

<sup>34</sup> [32] L. Maraschi and A. Cavaliere. 1977.

<sup>35</sup> [33] S. E. Woosley and R. E. Taam. *Nature*. (1976).

<sup>36</sup> [34] J. van Paradijs *et al. ApJ*. (1980).

<sup>37</sup> [35] J. Thorstensen, P. Charles, and S. Bowyer. *ApJ*. (1978).

<sup>38</sup> [36] R. C. Duncan and C. Thompson. *ApJ*. (1992).

<sup>39</sup> [37] E. P. Mazets *et al. Nature*. (1979).

<sup>40</sup> Throughout this thesis we will typically present our quantities only up to some fixed precision instead of the full litany of numbers. We will also adopt the centimeter-gram-second (cgs) unit system instead of the (maybe) more common SI-system. Such a selection is sure to disappoint some, but try to endure.



release energy anymore, it requires it to take place.<sup>41</sup> This iron produced, will then sink to the center of star forming a dead core without any energy input.

Like all big furnaces, at some point the stars will run out of fuel to burn. What is then left behind is a inner core of iron with a subsequent onion-like layers of lighter and lighter elements. Crucial question to ask next is: What is supporting this iron core now that the thermal pressure from the fusion processes are lost? To answer this, we need to look inside the iron atom: Iron nucleus, consisting of 26 protons and 32 neutrons, and surrounded by 26 electrons, repulses its neighbors because of the negatively charged electron cloud does not want to get in touch with its neighbors flying next to it in the iron-atom lattice.<sup>42</sup> It is this antisocial behavior originating from the electric charge repulsion that also gives internal support to our everyday materials and prevents us from not falling through the floor. Electrons and protons inside the atom itself, on the other hand, are repulsing each other because of the quantum effects. **explain quantum repulsion**

### 1.2.2 Neutron stars at last

From this setup it only takes a short step into realizing the existence of neutron stars. What if at some point even these quantum effects are not enough to support the core? Let us consider the consequences of this thought play. More detailed calculations show that the resulting iron-core sitting at the center of the star is weighting at a maximum of around  $\sim M_{\odot}$ . Hence, there are  $M_{\text{core}}/m_{\text{atom}} \sim M_{\odot}/m_p \approx 1.99 \times 10^{33} \text{ g}/1.67 \times 10^{-24} \text{ g} \sim 10^{57}$  atoms trapped inside the core.<sup>43</sup> Here we are already considering not iron atoms but pure hydrogen atoms only to simplify the presentation. Working backwards from these numbers, we can estimate the size of the core.

### 1.2.3 Neutron star dimensions

It turns out that Sun is also not as stable as one would think: With a rotation period of about 25.5 days it then takes Sun about a month to revolve around itself. Similar to a bicycle dynamo hub, this rotation also gives rise to a detectable surface magnetic field of  $B_{\odot} \approx 1 \text{ Gauss}$ .<sup>44</sup>

A typical neutron star, on the other hand, weights about  $M \sim 1.5 M_{\odot}$  but extends only up to  $R \sim 10 \text{ km}$ . Such dimensions give us an impressive mean density of  $\rho \sim 7 \times 10^{14} \text{ g cm}^{-3}$ . In comparison, a typical nucleon (such as a neutron) weights about  $1.67 \times 10^{-24} \text{ g}$  and has a radius of about  $1.25 \times 10^{-13} \text{ cm}$ , yielding us a nuclear density of  $\rho_n \approx 2 \times 10^{14} \text{ g cm}^{-3}$ . Hence, even the mean density inside the star is already on the same order of magnitude as the internal density inside nuclei. This suggests us that the composition inside a neutron star is not our typical every-day matter.

Suppose a neutron star is, like any normal star, a blob of gas held together by the inwards pulling gravity. Gravity does not prefer any direction more than some other and so a stable end-result is an isotropic configuration. A pure inward pulling force is, of course, not enough so we also need a countering outward-facing force to resist the compression of the material. As an first approximation, there is no need to assume that this force would have any preferred direction either. Hence, our expected outcome is a sphere held together by the gravity originating from the mass  $M$  of the matter itself. Let us, for a while forget the exact origin and nature of the compression-resisting force and see what can we learn solely from the current information only.

<sup>41</sup>This opens up another possibility of creating energy by splitting heavy elements. Such a process is called fission and is familiarly taken advantage of in earthly nuclear power plants.

<sup>42</sup>More precise consideration shows that nickel ( $^{56}\text{Ni}$ ) is actually thermodynamically more favored in the core because of the lack of neutrons needed to synthesize iron-58 ( $^{58}\text{Fe}$ ).

<sup>43</sup> The mass of the atom,  $m_{\text{atom}} = m_p + m_e$ , is also approximated (to an excellent accuracy) by just considering the central nuclei alone as the electron mass  $m_e \approx 9.11 \times 10^{-28} \text{ g}$  is negligible in comparison to the proton mass.

<sup>44</sup>A typical refrigerator magnet is about 50× stronger with a magnetic field of 50 Gauss.

### **1.3 What do we actually know?**

### **1.4 Connection to this thesis**

In this thesis we study many aspects of the neutron stars, their environment and the internal processes that will in the end help us in constraining the behavior of the ultra-dense matter inside the star.





## 2.0.2 Tolman-Volkoff-Oppenheimer equations

Newtonian pressure gradient needed to oppose the gravity is

$$\frac{dP}{dr} = -\frac{GM\rho}{r^2}. \quad (2.6)$$

Taking into account the general relativistic corrections we get

$$\frac{dP}{dr} = -\frac{GM\rho}{r^2} \times \frac{(1 + P/\rho c^2)(1 + 4\pi r^3 P/mc^2)}{1 - 2Gm/rc^2}. \quad (2.7)$$

Difference originates from the source of gravity: in the Newtonian case it is the mass  $m$ , whereas in the General relativity it is the energy momentum tensor that depend both on the energy density and the pressure. As a result, energy and pressure give rise to a gravitational fields.

It has an important consequence to the stability of neutron stars: Successive increase in the pressure to counter the gravity is ultimately self-defeating.

**Solution for a constant density  $\rho_0$  gives**

$$P(r) = G \frac{2\pi}{3} \rho_0^2 (R^2 - r^2) \quad (2.8)$$

**whereas the GR gives**

$$P(r) = \rho_0^2 c^2 \left[ \frac{(1 - u(\frac{r}{R})^2)^{1/2} - (1 - u)^{1/2}}{3(1 - u)^{1/2} - (1 - u(\frac{r}{R})^2)^{1/2}} \right], \quad (2.9)$$

**where  $u = 2GM/Rc^2$ .**

## 2.1 Equation of state

Often means dependency between  $P$  and  $\rho$ . Or sometimes the associated energy density  $\epsilon = \rho c^2$ . Also depends on  $T$  but composed mainly on strongly degenerate fermions so so temperature dependency is negligible.

Bulk property of the sea of fermions.

Eos for  $\rho > \rho_n$  can not be produced in laboratory. Can not be calculated because of the lack of precise many-body theory of strongly interacting particles.

Baryon mass  $M_b$  that is sum of baryon masses. Gravitational mass  $M$  that is  $M_b$  from where the gravitational binding energy is subtracted.<sup>2</sup>

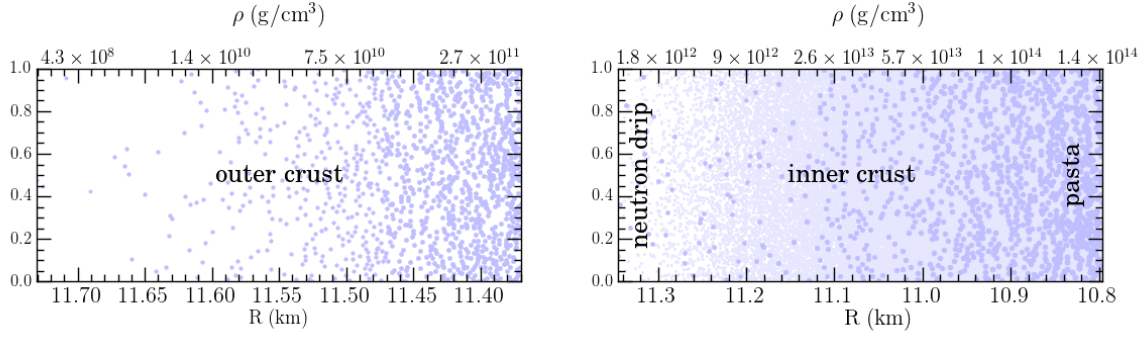
## 2.2 Atmosphere

Thin layer of plasma From centimeters in hot to millimeters in cold Zavlin & Pavlov 2002

Where spectrum or thermal electromagnetic radiation is formed. Spectrum, beaming and polarization of emerging radiation can be determined from radiation transfer problem in atmospheric layers.

Contains information on the parameters of the surface: effective temperature surface gravity chemical composition geometry of the system mass and radii.

Eddington limit of where radiation force exceeds the gravitational one.



**Figure 2.1:** Molecular simulation of the crust. Figure adapted from <https://github.com/awsteiner/nstar-plot>.

## 2.3 Crust

### Outer crust

From atmosphere to  $\rho_N D \sim 4 \times 10^{11} \text{ g cm}^{-3}$ . In thickness some hundred meters. Non degenerate electron gas Ultra-relativistic electron gas  $\rho > 10^6 \text{ g cm}^{-3}$ . Pressure provided by electrons here.

In deeper layers ions form a strongly coupled Coulomb system (liquid or solid). Hence, crust. Fermi energy grows with increasing  $\rho$ . Induces  $\beta$  captures and enriches nuclei with neutrons. At the base neutrons start to drip out from nuclei.

Inner crust About one kilometer thick. Density from  $\rho \sim \rho_{ND}$  (at upper boundary) to  $\sim 0.5 \rho_n$  at the base. Matter consists of electrons, free neutrons  $n$  and neutron-rich atomic nuclei. Fraction of free  $n$  grow with  $\rho$ .

Finally, nuclei disappear at the crust-core interface.

## 2.4 Core

Outer core. Density ranges  $0.5 \rho_n < \rho < 2 \rho_n$ . Several kilometers. Neutrons with several per cent admixture of protons  $p$  and electrons  $e^-$ . Strongly degenerate. Electrons form almost ideal Fermi gas. Neutrons and protons, interacting via nuclear forces, constitute a strongly interacting Fermi liquid.

Inner core. Where  $\rho > 2 \rho_n$ . Central density can be around  $(10 - 15) \rho_n$ . Very model dependent. Main problem.

## 2.5 LMXB

### LMXB<sup>3</sup>

infalling matter leads to X-rays<sup>4</sup>

Roche Lobe<sup>5,6</sup>

Hard and soft state<sup>7</sup>

alterate between these two states<sup>8,9</sup>

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