

List of publications

Modeling of neutron star atmospheres and emergent radiation

Paper I. Nättilä, J., Suleimanov, V. F., Kajava, J. J. E., Poutanen, J.: Models of neutron star atmospheres enriched with nuclear burning ashes, 2015, A&A, 581:A83, <http://dx.doi.org/10.1051/0004-6361/201526512>

Paper II. Nättilä, J. Pihajoki, P.: Radiation from rapidly rotating oblate neutron stars, 2017, A&A, submitted

Understanding the astrophysical environments of X-ray bursts

Paper III. Poutanen, J., Nättilä, J., Kajava, J. J. E., Latvala, O.-M., Galloway, D. K., Kuulkers, E., Suleimanov, V. F.: The effect of accretion on the measurement of neutron star mass and radius in the low-mass X-ray binary 4U 1608-52, 2014, MNRAS, 442, 3777–3790, <http://dx.doi.org/10.1093/mnras/stu1139>

Paper IV. Kajava, J. J. E., Nättilä, J., Latvala, O.-M., Pursiainen, M., Poutanen, J., Suleimanov, V. F., Revnivtsev, M. G., Kuulkers, E., Galloway, D. K.: The influence of accretion geometry on the spectral evolution during thermonuclear (type I) X-ray bursts, 2014, MNRAS, 445:4218–4234, <http://dx.doi.org/10.1093/mnras/stu2073>

Constraining the mass, radius, and composition of neutron stars

Paper V. Nättilä, J., Steiner, A. W., Kajava, J. J. E., Suleimanov, V. F., Poutanen, J.: Equation of state constraints for the cold dense matter inside neutron stars using the cooling tail method, 2016, A&A, 591:A25, <http://dx.doi.org/10.1051/0004-6361/201527416>

Paper VI. Kajava, J. J. E., Nättilä, J., Poutanen, J., Cumming, A., Suleimanov, V., Kuulkers, E.: Detection of burning ashes from thermonuclear X-ray bursts, 2017, MNRAS, 464:L6–L10, <http://dx.doi.org/10.1093/mnrasl/slz167>

Paper VII. Nättilä, J., Miller, M. C., Steiner, A. W., Kajava, J. J. E., Suleimanov, V. F., Poutanen, J.: Atmosphere model fits of thermonuclear X-ray burst cooling tail spectra: new neutron star mass and radius constraints using Bayesian hierarchical modeling, 2017, A&A, submitted

Additional publications not included in the thesis

Kuuttila, J., Kajava, J. J. E., Nättilä, J., Motta, S. E., Sanchez-Fernandez, C., Kuulkers, E., Cumming, A., Poutanen, J.: Flux decay during thermonuclear X-ray bursts analysed with the dynamic power-law index method, 2017, A&A, in press, <https://arxiv.org/abs/1705.05653>

Kajava, J. J. E., Koljonen, K. I. I., Nättilä, J., Suleimanov, V., Poutanen, J.: Variable spreading layer in 4U 1608-52 during thermonuclear X-ray bursts in the soft state, 2017, MNRAS, in press, <https://arxiv.org/abs/1707.09479>

Suleimanov, V. F., Poutanen, J., Nättilä, J., Kajava, J. J. E.; Revnivtsev, M. G., Werner, K.: The direct cooling tail method for X-ray burst analysis to constrain neutron star masses and radii, 2017, MNRAS, 466, 906-913, <http://dx.doi.org/10.1093/mnras/stw3132>

Suleimanov, Valery V. F., Kajava, J. J. E., Molkov, S. V., Nättilä, J., Lutovinov, A. A., Werner, K. Poutanen, J.: Basic parameters of the helium accreting X-ray bursting neutron star in 4U 1820-30, 2017, MNRAS,

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it is possible to set constraints on the size of the emitting area, and in the end, the radius of the neutron star. We will also summarize the content of the articles in this thesis, and discuss our work where we try to understand not only the complex role of the astrophysical surroundings but in the end, the composition of the core.

1.1 Measuring the sizes of the bursting sources

Even though the bursts characteristics change from one burst to another as we saw in Sect. ??, the cooling appears to obey some common trends. This means that as long as we have some kind of an energy injection deep below the neutron star's atmosphere, the energy will radiate out and the uppermost layers of the star will then shape it into a similar cooling curve, independent of the actual details of the injection. If we are then able to model the atmosphere and the processes therein, we can use the bursts as probes for the neutron star interiors. Note, however, that not every burst is powerful enough to be of practical use. As we shall see, we additionally require that the bursts reach the Eddington limit, which in practice means using the PRE-bursts only.

To begin, let us define three different families of quantities: Observed quantities (obs), theoretical quantities predicted by our model at infinity (∞), and the same theoretical model quantities in the local frame of the star (*). This is done, because general relativistic effects change the local physical quantities as they travel from the star to a distant observer.* More specifically, we can connect the temperatures T , radii R , and luminosities L as

$$R_{\infty} = R_*(1 + z) \quad (1.1)$$

$$T_{\infty} = \frac{T_*}{1 + z} \quad (1.2)$$

$$L_{\infty} = \frac{L_*}{1 + z}, \quad (1.3)$$

where $(1 + z)$ is the redshift factor that is related to the previously defined compactness $u = 2GM/Rc^2$ as

$$1 + z = (1 - u)^{-1/2}. \quad (1.4)$$

From the observations, we see that the detected burst spectra are reasonably well-described by the Planck function (blackbody) as

$$F_{E,\text{obs}} \approx \pi B_E(T_{\text{obs}}) K_{\text{obs}}, \quad (1.5)$$

where $B_E(T_{\text{obs}})$ is a blackbody function with a measured temperature T_{obs} and normalization K_{obs} , together with E which is energy that we observe at. The normalization for a

*see, e.g. [1] W. H. G. Lewin, J. van Paradijs, and R. E. Taam. *SSRv.* (1993).

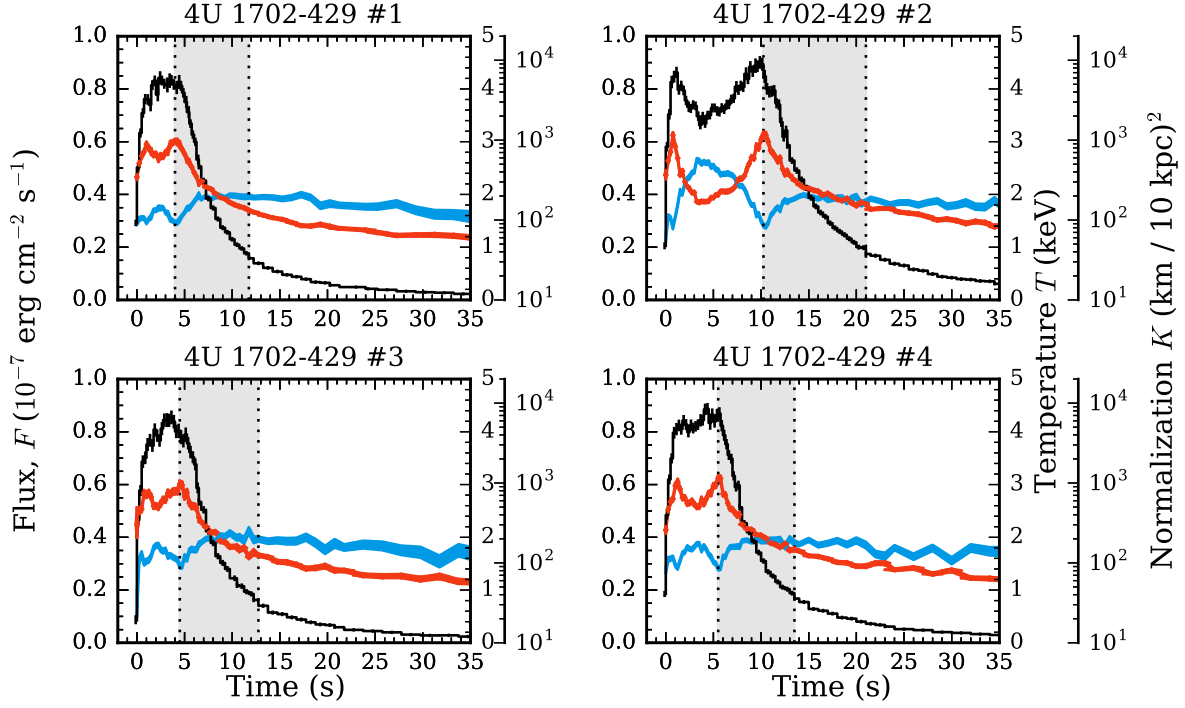


Figure 1.1: Examples of bolometric flux, temperature and blackbody normalization evolution during the hard-state PRE bursts. The black line shows the estimated bolometric flux (left-hand vertical axis) in units of $10^{-7} \text{ erg cm}^{-2} \text{ s}^{-1}$. The blue ribbon shows the blackbody normalization (outer right-hand vertical axis) in $(\text{km}/10 \text{ kpc})^2$. The red ribbon shows the blackbody temperature (inner right-hand vertical axis) in keV. Highlighted gray area marks a typical region of the cooling tail used in the fitting procedures.

circular object at a distance D in the sky is

$$K_{\text{obs}} = \frac{R_{\text{obs}}^2}{D^2}. \quad (1.6)$$

Observed bolometric flux is then

$$F_{\text{obs}} = \int_0^\infty F_{E,\text{obs}} dE = \sigma_{\text{SB}} T_{\text{obs}}^4 \frac{R_{\text{obs}}}{D^2}. \quad (1.7)$$

Some examples of Planck function fit results for X-ray bursts are shown in Fig. 1.1. Here the time-dependent spectral fits are shown for one particular source, 4U 1702–429.*

*NMS17, see [2] J. Nättilä *et al.* *A&A.* (2016), for more detailed description of the data.

All of the bursts shown here are exhibiting the photospheric radius expansion, that can be seen from the characteristic dip in the normalization and of the simultaneous maximum in the temperature.* The flux corresponding to the exact moment when the photosphere collapses back to the neutron star's surface is dubbed the touchdown flux, and it is visualized by the first vertical dotted line in the Figures.

From the atmosphere models of neutron stars, we obtain a similar result. The local detailed model spectra is well approximated by a so-called diluted blackbody model given as

$$F_{E,*} \approx \pi w B_E(f_c T_{\text{eff},*}), \quad (1.8)$$

where w is the dilution factor, f_c is the color-correction factor, and $T_{\text{eff},*}$ is the effective temperature of the atmosphere. This allows us to connect the observed values to the theoretical model values by first redshifting these quantities to infinity. From (1.2) we simply obtain that the temperature of the model as seen by a distant observer must be

$$f_c T_{\text{eff},\infty} = f_c \frac{T_{\text{eff},*}}{1+z}. \quad (1.9)$$

Similarly, the area of the star on the sky must be related not to R_* but to R_∞ as given by (1.1)

$$w \frac{R_\infty^2}{D^2} = w \frac{R_*^2(1+z)^2}{D^2}. \quad (1.10)$$

The latter (1.10) gives immediate constraints for the radius as it can be equated with the observed size (1.6) as[†]

$$R_{\text{obs}}^2 = w R_\infty^2 = w R_*^2(1+z)^2. \quad (1.11)$$

Additional constraints can be obtained by measuring Eddington limit of the source. As we have seen, there exists a flux for which the radiation forces equal to the gravitational forces (see Sect. ??), given as

$$F_{\text{Edd},*} = \frac{GMc}{\kappa_T R_*^2}(1+z), \quad (1.12)$$

where $\kappa_T = 0.2(1+X) \text{ cm}^2 \text{ g}^{-1}$, is the Thomson electron scattering opacity and X is the hydrogen mass fraction. One should note here that even though we use the Thomson electron scattering opacity in the notation, one is not restricted to assuming this. It is, for example, possible to take the Klein-Nishina reduction in the cross-section into account which formally allows for super-Eddington fluxes.[‡] In reality the Eddington limit is, of

*see, e.g. [3] D. K. Galloway *et al.* *ApJS*. Paradijs *et al.* *PASJ*. (1990). (2008), for more thorough discussion.

[‡] [6] V. Suleimanov, J. Poutanen, and K. [†] [4] W. Penninx *et al.* *A&A*. (1989); [5] J. van Werner. *A&A*. (2012).

1.1 Measuring the sizes of the bursting sources

course, still respected. Using this characteristic flux we can also define the Eddington luminosity $L_{\text{Edd},*}$ and the corresponding Eddington temperature $T_{\text{Edd},*}$ as

$$L_{\text{Edd},*} = 4\pi R_*^2 F_{\text{Edd},*} = 4\pi R_*^2 \sigma_{\text{SB}} T_{\text{Edd},*}^4. \quad (1.13)$$

These are again quantities defined near the star whereas what one observes at infinity are given by

$$L_{\text{Edd},\infty} = \frac{L_{\text{Edd},*}}{1+z}, \quad (1.14)$$

$$F_{\text{Edd},\infty} = \frac{L_{\text{Edd},\infty}}{4\pi D^2} = \frac{GMc}{\kappa_{\text{T}} D^2} \frac{1}{1+z}, \quad (1.15)$$

and

$$T_{\text{Edd},\infty} = \frac{T_{\text{Edd},*}}{1+z}. \quad (1.16)$$

As the simplest case, we can obtain additional constraints for the radius and mass by just measuring the $F_{\text{Edd},\infty}$ somehow. This can be done, for example, by equation it with the touchdown flux obtained from the time-dependent burst spectra. This is the basis of the so-called “touchdown method”.*

A more sophisticated version of this is the so-called “cooling tail method”.† Here we can compute the varying color-correction factor f_c from the atmosphere models as a function of $\ell \equiv L_*/L_{\text{Edd},*}$. In this case, the dilution factor was fully omitted as $f_c \approx w^{-4}$. The color-correction factor can then be related to multiple K_{obs} measurements, each representing an one time snapshot from the cooling tail. As the time time passes and the surface cools down, the flux decreases. This allows us to compare the model dependency of ℓ vs. f_c to the observations of $F_{\text{obs}}/F_{\text{Edd},\infty}$ vs. $K_{\text{obs}}^{-1/4}$. Hence, extra information from the observations is used because not only are the individual color-correction factor values compared against the model but also the mutual dependency of them. The fitting procedure is two dimensional in this case as we fit $F_{\text{Edd},\infty}$ and R_∞^2/D^2 simultaneously. Interestingly, the combination of these two fit parameters then yield a distance-independent quantity, physically corresponding to the Eddington temperature of the source at infinity, and given as **check**

$$T_{\text{Edd},\infty} = 1.14 \times 10^8 \left(\frac{F_{\text{Edd},\infty}}{10^{-7} \text{ erg cm}^{-2} \text{ s}^{-1}} \right)^{1/4} \left(\frac{(\text{km}/10 \text{ kpc})^2}{R_\infty^2/D^2} \right)^{1/4} \text{ K}. \quad (1.17)$$

* [7] T. Ebisuzaki. *PASJ.* (1987); [5] J. van Suleimanov, J. Poutanen, and K. Werner. *A&A.* Paradijs *et al.* *PASJ.* (1990); [8] F. Özel. *Nature.* (2011); [6] V. Suleimanov, J. Poutanen, and K. Werner. *A&A.* (2012); [12] J. Poutanen *et al.* *MN-* (2006); [9] F. Özel *et al.* *ApJ.* (2016).

† [10] V. Suleimanov *et al.* *ApJ.* (2011); [11] V. RAS. (2014).

This corresponds to a parametric relation for the M and R via the compactness u , given as

$$R = \frac{c^3 u(1-u)^{3/2}}{2\kappa_T \sigma_{\text{SB}} T_{\text{Edd},\infty}^4} \approx 1188 \frac{u(1-u)^{3/2}}{(1+X) T_{\text{Edd},\infty,7}^4} \text{ km},$$

$$M \approx u \frac{R}{2.95 \text{ km}} M_{\odot},$$
(1.18)

where $T_{\text{Edd},\infty,7} = T_{\text{Edd},\infty}/10^7 \text{ K}$. Later on, another variant of this was introduced, called “direct cooling tail method” where the assumption of $f \approx w^{-4}$ was relaxed, i.e., both f_c and w are considered, and the fitting is done directly via the M , R and D parameters.*

The usage of these methods on X-ray burst data span almost a three decades of scientific work as of now. Starting from the early work in the late 80s they have since improved and been applied to various sources to estimate the radius and mass. Latest in the family, is the method of fitting the observed data directly with the atmosphere models.† Although computationally more demanding exercise, it allows us to finally extract every piece of information possible from the data. This is based on the additional model dependency on the surface gravity, composition, and detailed spectral shape that slightly deviates from the assumed Planck function.

The big caveat here for any of the aforementioned methods are the surroundings. We have seen that the astrophysical environment of neutron stars can be very active and lively. In the general picture, we have the accretion as an energy source and the disk to dissipate this energy. The disk is, however, not a simple geometrically thin steady layer but can have complex inner flow. On the other hand, if the disk does extend all the way down to the star, an additional complication originates from the boundary or spreading layer that can not only cover the star but also radiate on its own. These are some of the complications that we face when trying to analyze our neutron star observations, as after all when trying to constrain the mass and radius of the star we must make sure that it is actually the star that we are looking.

1.2 Scientific summary of the results

In this thesis, we have focused on constraining the cool ultra-dense matter inside neutron stars with astrophysical measurements. The main results are two-folded as we have both

- improved our understanding of ultra-dense matter and have been able to put stringent constraints on the equation of state of the neutron star interiors, and
- progressed our understanding of neutron star environments and astrophysics of X-ray burst.

* [2] J. Nättilä *et al.* *A&A.* (2016); [13] V. F. Suleimanov *et al.* *MNRAS.* (2017).
 †NMS17.

To be able to do this, we had to develop our observational and statistical methods, do theoretical research in order to understand the astrophysical scenarios better, develop and improve our physical models, and finally apply these new methods and information to real-world observations. Because of this, the results and work in this thesis can be divided into three categories that we now discuss in more detail. In short, these include 1) theoretical work on the models, 2) understanding the astrophysical environment better, and 3) applying the models and the new insights to astronomical observations.

1.2.1 Modeling of neutron star atmospheres and emergent radiation

Computing hot neutron star atmosphere models for the X-ray bursters, is of paramount importance for obtaining the mass and radius measurements from the burst observations. More specifically, we are interested in the color correction factor f_c and the dilution factor w , in order to compare our knowledge to observations. Previous models for hot atmospheres have all assumed simple hydrogen, helium, or solar composition for the plasma. In some cases, however, the burning ashes may rise from the burning depths up to the photosphere, leading to the appearance of the metal absorption edges in the spectra. These effects may have a substantial impact on the color correction factor and the dilution factor w . In paper I, we have developed a new atmosphere modeling code to compute the emergent spectra for a composition consisting of any atomic species. We find that the metals may change f_c by up to about 40%. The presented models also made possible to determine the NS mass and radii more accurately for cases when we do see signs of burning ashes, and provided a new tool to probe the nuclear burning mechanisms in X-ray bursts.

The radiative process that we consider all occur at or near the neutron star. Because of this, many general relativistic effects play an important role in shaping the observations. In paper II, a theoretical framework for emission originating from rapidly rotating oblate compact objects was described in detail. In order to solve the geodesic equation, a new splitted Hamilton-Jacobi formalism was constructed for a Butterworth-Ipser metric that is expanded up to second order in rotation and hence includes effects of light bending, frame-dragging, and quadrupole deviations. We also gave detailed descriptions of the numerical algorithms used and provide an open source implementation of the numerical framework called BENDER. As an application, we study spectral line profiles from rapidly rotating oblate neutron stars. The Full Width at Tenth Maximum and Full Width at Half Maximum for the so-called smearing kernels are also reported for all of the possible viewing angles. These can be then used to quantitatively estimate the effects of rotational smearing on the observed spectra.

1.2.2 Understanding the astrophysical environments of X-ray bursts

As we have seen, the neutron star environment is an important factor that needs to be understood before reliable mass and radius estimates can be obtained from X-ray burst observa-

tions. In paper III, we study the effects of accretion for an one particular source, LMXB system 4U 1608–52. We found a strong dependence of the burst properties on the flux and spectral hardness of the persistent emission before burst. Bursts occurring during the low accretion rate (hard) state exhibit evolution of the blackbody normalization consistent with the theoretical predictions of neutron star atmosphere models. However, bursts occurring during the high accretion rate (soft) state show roughly constant normalization, which is inconsistent with the models and therefore these bursts cannot be easily used to determine neutron star parameters.

In the next paper IV, we continue our analysis further by studying 246 X-ray bursts in total, from 11 different LMXB systems. Again, we found a dependence between the persistent spectral properties and the time evolution of the blackbody normalization during the bursts. The neutron star atmosphere model predictions agree with the observations for most bursts occurring in hard, low-luminosity, spectral states, but rarely during soft, high-luminosity, states. We attributed the observed phenomena to the accretion flow, which can influence the cooling of the neutron star especially during the soft state when the accretion rate is high. The results had the important implication that only the bursts occurring in the hard, low-luminosity spectral states could be reliably used for mass and radius determination.

1.2.3 Constraining the mass, radius and composition of neutron stars

By now applying the atmosphere model results to the X-ray burst data, we can try and set constraints for the size of the emitting source. However, here it is crucial to take into account also the accretion rate, i.e., consider bursts that occur during the hard-state only. In paper V. we did this analysis for three different LMXB systems: 4U 1702–429, 4U 1724–307, and SAX J1810.8–260. This allows us to set constraints for the masses, radii, compositions, and distances of the neutron stars in those systems. We then obtained a parameterized equation of state by comparing the resulting neutron star structures to the radius and mass measurements we had. This was done by solving the TOV-equations (see Sect. ??) and then using Monte Carlo algorithm within a Bayesian framework to obtain constraints for the underlying equation of state parameters. This allows us to set limits on various nuclear parameters and to constrain an empirical pressure-density relationship for the dense matter. Our predicted equation of state leads to a neutron star radius between 10.5 to 12.8 km for a mass of $1.4 M_{\odot}$.

The bursts that we considered in the aforementioned publication, were constrained to have an atmosphere consisting of almost fully of hydrogen and helium. This is always not the case as explosive nuclear burning can fuse H and He into heavier elements too. In paper VI, we presented our analysis of one particularly interesting long burst observed from the neutron star in LMXB system HETE J1900.1-2455. New atmosphere model fits

to this bursts indicated that sometimes the photosphere can consist entirely of metals, i.e., nuclear burning ashes. These heavy metals like iron and nickel were detected already early on during the burst, which makes it possible that a radiatively driven wind might eject some of these ashes also into the interstellar space. Hence, neutron star X-ray bursts might be one possible source of interstellar pollution.

Most previous works on X-ray bursts have used the Planck functions as a proxy to simplify the model vs. data comparison. In paper VII, we, for the first time, fitted neutron star atmosphere models directly to the observed spectra. This was done using a new nested hierarchical Bayesian model that allowed us to set new limits on mass, radius, composition, and distance of the neutron star in 4U 1702–429. We then find a radius of $R = 12.4 \pm 0.4$ km, gravitational mass $M = 1.9 \pm 0.3 M_{\odot}$, distance $D = 5.9 \pm 0.3$ kpc, and hydrogen mass fraction $X < 0.09$ with a 68% confidence for this source.

1.3 The author's contribution to the publications

Paper I.: Models of neutron star atmospheres enriched with nuclear burning ashes

The author contributed to the main idea of the paper, independently redesigned the neutron star atmosphere code used for the calculations, and implemented new physical processes to this numerical framework. The author also prepared most of the manuscript.

Paper II.: Radiation from rapidly rotating oblate neutron stars

The author independently proposed the idea of applying the split-Hamilton method to the ray tracing problem, derived the theoretical framework and all the related formulae, designed the numerical code, and prepared most of the manuscript.

Paper III.: The effect of accretion on the measurement of neutron star mass and radius in the low-mass X-ray binary 4U 1608-52

The author of the thesis made contributions to the manuscript, reduced and analyzed the observational X-ray data, and contributed to the scientific discussions related to the manuscript.

Paper IV.: The influence of accretion geometry on the spectral evolution during thermonuclear (type I) X-ray bursts

The author participated in the reduction and analysis of the observational data, made significant contributions to the development of the data reduction software, and helped in the preparation of the manuscript.

Paper V.: Equation of state constraints for the cold dense matter inside neutron stars using the cooling tail method

The author independently designed the Bayesian fitting framework for the cooling tail method, reduced and analyzed the X-ray observations, and finally led the equation of state

modeling from the observations. The author also prepared the manuscript.

Paper VI.: Detection of burning ashes from thermonuclear X-ray bursts

The author contributed to the main idea of this research and was responsible of the atmosphere modeling of the observations. The Bayesian atmosphere spectral model fitting framework was also independently designed by the author. Author also contributed to the manuscript.

Paper VII.: Atmosphere model fits of thermonuclear X-ray burst cooling tail spectra: new neutron star mass and radius constraints using Bayesian hierarchical modeling

The author independently designed the hierarchical Bayesian fitting framework, implemented it into a code together with M.C. Miller and A.W. Steiner, analyzed the data, and, finally, prepared the manuscript together with M.C. Miller, with the help from the other co-authors.

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