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Bulk RNA-seq: Pathway Analysis

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# Section 1

Overview

# WHAT IS PATHWAY ANALYSIS?

#### Many names for the same thing:

- ► Pathway analysis
- ► Gene set enrichment analysis
- ► Go-term analysis
- ► Gene list enrichment analysis

- ▶ Gene expression  $X_1, X_2, \ldots, X_m$
- ightharpoonup Phenotype expression Y
- ► Study the relationship between the genes and the phenotype.

$$Y = \beta_{i0} + \beta_{i1}X_i + \epsilon$$

or

$$logit{P(Y = 1)} = \beta_{i0} + \beta_{i1}X_i$$

or other GLMs.

► For each gene, test the significance level

$$H_{0,i}: \beta_{i1} = 0.$$

- ▶ For each  $H_{0,i}$ , use Wald/score/likelihood ratio test to obtain test statistic and the corresponding P-value  $P_i$ .
- ▶ If  $P_i$  is large, then the chance that SNP/Gene i is associated with phenotype Y is small.
- ightharpoonup If  $P_i$  is small, we think SNP/Gene *i* could be important.
- ▶ Thresholding P-values: Claim SNP/Gene i is significantly associated with the phenotype (Reject  $H_{0,i}$ ) if  $P_i < c$ .

- ► How to decide the threshold?
- ▶ The threshold c depends on the desired type I error  $\alpha$  and the number of genes m.
- ▶ Different type I error measures:
  - ► Family-wise error rate (FWER):

P(falsely reject any one gene)

► False discovery rate (FDR):

 $\mathsf{E}\left(\frac{\text{number of the falsely rejected genes}}{\text{total number of the rejected genes}}\right)$ 

### Type I Error Rate

 $H_l$ : Gene set  $S_l$  is not associated with the phenotype,  $l = 1, \ldots, m$ .

	Claim significant	Claim non-significant	Total
True nulls	$N_{00}$	$N_{01}$	$m_0$
False nulls	$N_{10}$	$N_{11}$	$m_1$
Total	R	m-R	m

- ► FDR =  $E(N_{00}/(R \vee 1))$ .
- ► FWER =  $P(N_{00} \ge 1)$ .

- ▶ Typically,  $\alpha = 0.05$ .
- ightharpoonup Assume all P-values are i.i.d Unif(0,1),

$$FWER = \alpha = (1 - c)^m.$$

• With  $\alpha = 0.05$ ,

with $\alpha = 0.00$ ,						
m	1	10	100	1000	10000	
c	5E-2	5E-3	5E-4	5E-5	5E-6	

- ► FWER is more conservative than FDR. This means, controlling FWER at level  $\alpha$  will require  $c(\alpha)$  to be smaller (than those for controlling FDR at level  $\alpha$ ).
- ightharpoonup If the threshold c is smaller, fewer genes will be rejected (identified).
- ▶ Because m is very large (too many candidate genes), to control type I error (no matter which one is used) usually requires c to be very small. Thus, the power of the test will be very small.

# Manhattan plot for single gene/SNP analysis

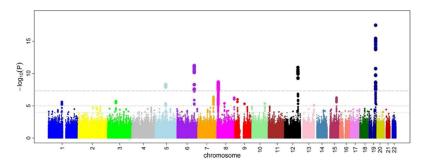


Figure: An example from Gibson (2010).

#### PATHWAY ANALYSIS

- ► An analysis to investigate the relationship between a disease phenotype and a set of genes on the basis of shared biological or functional properties.
- ► A set of genes:
  - ► Genes involved in a pathway
  - ► Genes corresponding to a Gene Ontology term
  - ▶ Genes mentioned in a paper to have certain similarities
- ► Are many genes in the pathway differentially expressed (up-regulated/down-regulated)?
- ► What is the probability of observing these changes just by chance?
- ► The trick is to reduce the number of candidate features.

Numer of genes >> number of gene sets

#### WHY PATHWAY ANALYSIS?

Single gene approach: List top 10-50 most-significant genes.

Pathway analysis: List the pathways whose genes have consistent trend to affect the phenotype.

#### Why pathway analysis?

Single gene approach: List top 10-50 most-significant genes.

► Assumption 1: Single gene work solely to largely increase the disease susceptibility

Pathway analysis: List the pathways whose genes have consistent trend to affect the phenotype.

► Assumption 1: Multiple Genes in the same pathway work together to confer disease susceptibility.

### WHY PATHWAY ANALYSIS?

Single gene approach: List top 10-50 most-significant genes.

- ► Assumption 1: Single gene work solely to largely increase the disease susceptibility
- ► Assumption 2: The most associated gene is the best candidate for therapeutic intervention.

Pathway analysis: List the pathways whose genes have consistent trend to affect the phenotype.

- ► Assumption 1: Multiple Genes in the same pathway work together to confer disease susceptibility.
- ► Assumption 2: Targeting susceptibility pathways have clinical implications for finding additional drug targets.

# Section 2

Statistical Issues

#### TWO TYPES OF NULLS

- ► Self-contained analysis: None of those genes in the gene set are associated with the phenotype.
- ► Competitive analysis: None of those genes in the gene set are associated with the phenotype.

#### TWO TYPES OF NULLS

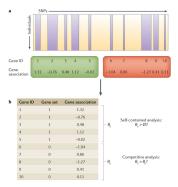
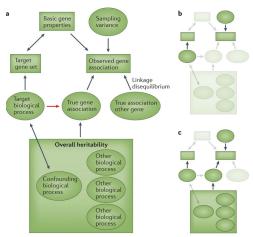


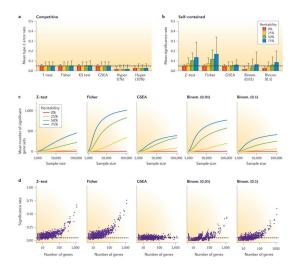
Figure: Schematic of the two-tier structures of GSA Leeuw et al. (2016).

#### Underlying Mechanism



Leeuw et al., 2016

# Self-contained Tests Inflate Type I Error



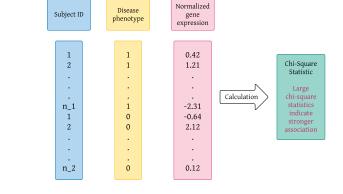
### Section 3

Gene Set Enrichment Analysis (GSEA)

### **GSEA**

- ► Gen-Gen: Kai Wang, Mingyao Li, and Maja Bucan (Dec. 2007). "Pathway-based approaches for analysis of genomewide association studies". In: Am J Hum Genet 81.6, pp. 1278–83. DOI: 10.1086/522374
- ► GSEA: Aravind Subramanian et al. (Oct. 2005). "Gene set enrichment analysis: a knowledge-based approach for interpreting genome-wide expression profiles". In: *Proc Natl Acad Sci U S A* 102.43, pp. 15545–50. DOI: 10.1073/pnas.0506580102

#### NORMALIZED GENE EXPRESSION DATA



- ► Chi-square statistics cannot differentiate the over-expressed or under-expressed genes.
- ► Wald statistics can differentiate the over-expressed or under-expressed genes.

# SUMMARIZE GENE-PHENOTYPE ASSOCIATION

- ightharpoonup In total N genes.
- ▶ For gene j, get the test statistics  $r_j$ .
- ightharpoonup Examples of  $r_i$ :
  - ► Score statistics
  - ► Wald statistics
  - ► Chi-square statistics

### ENRICHMENT SCORE

- ▶ A given gene set S,  $Card(S) = N_H$ .
- ▶ For gene j, the larger the  $r_j$  is, the more associated gene j with the phenotype.
- ► Rank the association statistics from the largest to the smallest, denoted by

$$r_{(1)} \ge r_{(2)} \ge \ldots \ge r_{(N)}$$
.

► Calculate a weighted Kolmogrov-Smirnov like running sum statistic

$$\mathrm{ES}(\mathcal{S}) = \max_{1 \leq j \leq N} \left\{ \sum_{j^* \in \mathcal{S}, \ j^* \leq j} \frac{|r_{(j^*)}|^p}{N_R} - \sum_{j^* \not\in \mathcal{S}, \ j^* \leq j} \frac{1}{N - N_H} \right\},$$

where 
$$N_R = \sum_{j^* \in \mathcal{S}} |r_{(j^*)}|^p$$
.

### ENRICHMENT SCORE

Weighted Kolmogrov-Smirnov like running sum statistic

$$\mathrm{ES}(\mathcal{S}) = \max_{1 \leq j \leq N} \left\{ \sum_{j^* \in \mathcal{S}, \ j^* \leq j} \frac{|r_{(j^*)}|^p}{N_R} - \sum_{j^* \notin \mathcal{S}, \ j^* \leq j} \frac{1}{N - N_H} \right\},$$

where  $N_R = \sum_{j^* \in \mathcal{S}} |r_{(j^*)}|^p$ .

- ightharpoonup p is a parameter that gives higher weight to genes with extreme statistics.
- ▶ Common choice p = 1.
- ▶ p = 0 leads to regular KS statistic, usually not as powerful as p = 1.

### NORMALIZED ENRICHMENT SCORE

- ▶ The enrichment score ES(S) relies on the maximum statistic, so that a larger gene set S tends to produce larger ES(S).
- ► Two-step normalization procedure:
  - 1. Permute the phenotype label of all samples
  - 2. During each permutation  $\pi$ , repeat the calculation of the enrichment score  $ES(S, \pi)$ .
- ► Then

$$NES(S) = \frac{ES(S) - mean\{ES(S, \pi)\}}{sd\{ES(S, \pi)\}}$$

- ► The NES adjusts for different sizes of genes.
- ► THE NES preserves correlations between SNPs on the same gene.

### CONTROL FDR

► NES\*: the normalized enrichment score in the observed data

FDR = 
$$\frac{\% \text{ of all } (\mathcal{S}, \pi) \text{ with } \text{NES}(\mathcal{S}, \pi) \geq \text{NES}^*}{\% \text{ of observed } \mathcal{S} \text{ with } \text{NES}(\mathcal{S}) \geq \text{NES}^*}.$$

- ► Rationale
  - ► FDR =  $E\{N_{00}/(R \vee 1)\}$ .
  - ▶  $N_{00}/m$ : Estimated by % of all  $(S, \pi)$  with NES $(S, \pi) \geq$  NES\*.
  - ▶ R/m: Estimated by % of observed S with NES(S) ≥ NES\*.
- ▶ Larger NES\* corresponds to smaller  $\widehat{FDR}$ .
- ▶ If  $\widehat{\text{FDR}} \leq \alpha$ , claim the corresponding gene set significant.

#### Control fwer

- ► NES\*: the normalized enrichment score in the observed data
- ▶  $\widehat{\text{FWER}} = \%$  of all  $\pi$  with the highest NES( $\mathcal{S}, \pi$ )  $\geq$  NES\*.
- ► Rationale:
  - FWER =  $P(N_{00} \ge 1) = E\{I(N_{00} \ge 1)\}.$
  - ▶ Each permutation  $\pi$  can be viewed as a realization of the event. If the highest NES( $\mathcal{S}, \pi$ ) ≥ NES\*, then there is a false rejection.
- ► Larger NES\* corresponds to smaller FWER.
- ▶ If  $\widehat{\text{FWER}} \leq \alpha$ , claim the corresponding gene set significant.

# Section 4

References



- Gibson, Greg (July 2010). "Hints of hidden heritability in GWAS". In: *Nat Genet* 42.7, pp. 558–60. DOI: 10.1038/ng0710-558.
- Leeuw, Christiaan A. de et al. (June 2016). "The statistical properties of gene-set analysis". In: *Nature Reviews Genetics* 17.6, pp. 353–364. ISSN: 1471-0064. DOI: 10.1038/nrg.2016.29.
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