

Information Security 2020

2nd Project

Prof. Junbeom Hur

TA. Dohyun Ryu

Information System Security Lab.,
Department of Computer Science and Engineering,
Korea University, Seoul, Korea

Hash Function

- Consider the following structure of a hash function that takes a 768-bit input and returns a 256-bit output

input : $X = (A_0, B_0, C_0, D_0, E_0, F_0, G_0, H_0, W_0, W_1, \dots, W_{15})$.

Where $A_0, B_0, C_0, D_0, E_0, F_0, G_0, H_0, W_0, W_1, \dots, W_{15}$ are each 32-bit.

Intermediate variable : $A_i, B_i, C_i, D_i, E_i, F_i, G_i, H_i, W_i$ each are 32-bit.

number of Round: R

#output : $Y = (A_0 \oplus A_i, B_0 \oplus B_i, C_0 \oplus C_i, D_0 \oplus D_i, E_0 \oplus E_i, F_0 \oplus F_i, G_0 \oplus G_i, H_0 \oplus H_i)$

For ($i = 16; i < R; i++$):

$$W_i = (W_{i-3} \lll 1) \oplus (W_{i-8} \lll 6) \oplus (W_{i-14} \lll 11) \oplus W_{i-16}$$

For ($i = 0; i < R; i++$):

$$(A_{i+1}, B_{i+1}, C_{i+1}, D_{i+1}, E_{i+1}, F_{i+1}, G_{i+1}, H_{i+1}) = \text{Round}(A_i, B_i, C_i, D_i, E_i, F_i, G_i, H_i, W_i)$$

Hash Function

- i-th *Round()* function structure

input : $(A_i, B_i, C_i, D_i, E_i, F_i, G_i, H_i, W_i)$

Intermediate variable : T which is 32-bit

output : $(A_{i+1}, B_{i+1}, C_{i+1}, D_{i+1}, E_{i+1}, F_{i+1}, G_{i+1}, H_{i+1})$

$T = (W_i[0], W_i[1], W_i[2], W_i[3])$

$T = \text{MDS}(S(T[0] \oplus A_i[0]), S(T[1] \oplus A_i[1]), S(T[2] \oplus A_i[2]), S(T[3] \oplus A_i[3]))$

$T = \text{MDS}(S(T[0] \oplus B_i[0]), S(T[1] \oplus B_i[1]), S(T[2] \oplus B_i[2]), S(T[3] \oplus B_i[3]))$

$T = \text{MDS}(S(T[0] \oplus C_i[0]), S(T[1] \oplus C_i[1]), S(T[2] \oplus C_i[2]), S(T[3] \oplus C_i[3]))$

$T = \text{MDS}(S(T[0] \oplus D_i[0]), S(T[1] \oplus D_i[1]), S(T[2] \oplus D_i[2]), S(T[3] \oplus D_i[3]))$

$T = \text{MDS}(S(T[0] \oplus E_i[0]), S(T[1] \oplus E_i[1]), S(T[2] \oplus E_i[2]), S(T[3] \oplus E_i[3]))$

$T = \text{MDS}(S(T[0] \oplus F_i[0]), S(T[1] \oplus F_i[1]), S(T[2] \oplus F_i[2]), S(T[3] \oplus F_i[3]))$

$T = \text{MDS}(S(T[0] \oplus G_i[0]), S(T[1] \oplus G_i[1]), S(T[2] \oplus G_i[2]), S(T[3] \oplus G_i[3]))$

$(A_{i+1}, B_{i+1}, C_{i+1}, D_{i+1}, E_{i+1}, F_{i+1}, G_{i+1}, H_{i+1}) = (H_i \oplus T, A_i, B_i, C_i, D_i, E_i, F_i, G_i)$

Definitions

- \oplus : Bitwise exclusive OR
- $\lll n$: n-bit left rotation
- $S()$: S-box of AES (reference: FIPS 197)
- $MDS()$: Matrix multiplication of AES (reference: FIPS 197)
- $T = (T[0], T[1], T[2], T[3])$: Concatenates four 8-bit $T[0]$, $T[1]$, $T[2]$, $T[3]$, and assigns the 32-bit result to T
- $(T[0], T[1], T[2], T[3]) = T$: Separates 32-bit T into four 8-bit $T[0]$, $T[1]$, $T[2]$, $T[3]$

Goals

1. Given an arbitrary 256-bit output Y , find the maximum number of rounds (R in the previous algorithm) to determine 768-bit input X with less than 2^{253} hash operations
2. Describe the algorithm (for each round) to solve it

1. Source code and exe file for solution (**20 points**)

- You don't need to implement an algorithm that requires more than 2^{32} hash operations
- However, it must be described in the report!
- Your program has to print X for each round given a value Y

2. Report (**30 points**)

- You need to show your solutions step by step
- Appendix: Source code with comments

Submission Guideline

- **Please upload the followings on Blackboard**

1. Source code and exe file for solution (**C is encourage, but if you want you can use Python, Java...etc**)
2. Report (**.doc, .hwp, or pdf file**)

→ Compress all of the files (**.zip**)

– **Late submission and any kind of plagiarism will result in 0 point**

ASSIGNMENT SUBMISSION

Text Submission

Write Submission

Attach Files

Browse My Computer

Browse Content Collection

Browse Cloud Storage

Browse Dropbox

Attached files

File Name

Link Title

hash_function_2020xxxxxx.zip

hash_function_2020xxxxxx

[Do not attach](#)

Submission Guideline

- **Deadline: 2020 Oct. 31, 23:59:00**
- **Late submission is not accepted**