# An analysis of the North Sea International Bottom Trawl Survey Data

## Abstract

In this research we present non-parametric estimation procedures for calculating abundance at age indices, and investigate the sensitivity of these estimates with respect to the number of otholits collected at sea. The procedures presented are applied to the North Sea International Bottom Trawls Survey data for cod (*Gadus morhua*) and saithe (*Pollachius virens*). We demonstrate how much information would be lost if the survey design was defined such that fewer otholits were collected. The abundance at age indices introduced differ from non-parametric indices provided by IBTS by how the age given length relation (ALK) is included. We use ALK's without the assumption of constant ALK over pre defined areas. All abundance at age indices are presented with variance estimates. Currently, such variance estimates are *only* utilized for assessment of Herring (*Clupea harengus*) in the North Sea, even thou they may include valuable information from the survey.

## 1    Introduction

Fish stock assessments are used by fishery managers for making management decisions regarding catch quotas. The assessments provide fundamental information about the status of the stock, for instance, whether the stock is increasing and support for increased levels of harvest should be given, or whether the stock is decreasing and stricter control on harvest should be implemented. Associated with the parameters used in fish stock assessment is their uncertainty, which should not be ignored when formulating management policies (Walters and Ludwig, 1981; Ludwig and Walters, 1981). This uncertainty can arise from many sources

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including natural variability, estimation procedures and lack of knowledge regarding the parameter (Ehrhardt and Legault, 1997). The North Sea International Bottom Trawl Survey (IBTS) data, coordinated by the International Council for the Exploration of the Sea (ICES), provides information on seasonal distribution of stocks and estimates of abundance indices and catch in numbers of fish per age-class without an assessment of the accuracy of these estimates. As pointed out by Ludwig and Walters (1981) estimates of parameters relating to stock size are of little value unless they are accompanied by uncertainty estimates. The indices of abundance at age from IBTS are based on data obtained from a stratified semi-random sampling approach of trawl stations, and it is essential to account for the sampling approach so as to produce reliable variance estimates (Lehtonen and Pahkinen, 2004). If the sampling approach is ignored, the effect on the variance of the parameters could be substantial. In particular, the variance could be greatly inflated due to the clustering effect, which involves intra-cluster correlation of the variables (Aanes and Vølstad, 2015; Lehtonen and Pahkinen, 2004).

There are two separate **cost full aspects?** of the North Sea International Bottom Trawl Survey (IBTS) for generating abundance indices per age. The first consist of calculating indices per *length* class, which are obtained by trawling in a **stratified procedure** and counting the number of fish caught. Then that knowledge is transformed to indices with respect to age. The latter part is achieved with an age-length key (ALK), which is constructed by sampling otoliths in a stratified procedure from each haul and/or sub-area. To our best knowledge, there has been no research on how much the uncertainty of the abundance indices is related to these two distinct parts. The main contribution of this article is to shed light on how the indices estimates and their associated uncertainty estimates change if less effort was spent on collection of otoliths. We achieve the reduction of otoliths by mimicking a defined sampling procedure with less effort. We also focus on the spatial distribution of the ALK, and such spatial structures in the ALK has also been investigated in Berg and Kristensen (2012); Hirst et al. (2012).

Currently, abundance indices from IBTS are reported in DATRAS (ICES, 2018b) using an age-length key (ALK) (Fridriksson, 1934) which is assumed to be constant over relatively large areas. In this paper we propose two ALKs which accounts for spatial variation: i) a nonparametric haul based ALK, and ii) a spatial model-based ALK. These ALKs are described in section 2, and the results from the model based

ALK gives a strong case for assuming variation in the ALK within RFAs. A spatial model based ALK (Berg and Kristensen, 2012) is currently used for assessment in the North Sea with use of IBTS data. The model introduced in Berg and Kristensen (2012) is similar to the model used in this paper; the main difference is that we include the spatial structure through a spatial random field (Lindgren et al., 2011) and not through two dimensional splines (Wood, 2017).An overview of the North Sea International Bottom Trawl Survey is given in Section 1.1. The current estimators for ALK and catch per unit effort (CPUE) used by ICES in their database for trawl surveys (DATRAS) and our proposed ALK estimators are given in Section 2. Two case studies, in which the methods described in Section 2 are applied to, are given in Section 3, and a discussion is given in Section 4.

## 1.1   Overview of the North Sea International Bottom Trawl Surveys

The North Sea International Bottom Trawl Survey was formed in 1991, which is a combination of the International Young Herring Survey (IYHS) and eight national surveys in the North Sea, Skagerrak and Kattegat areas. These surveys began in the 1960's, and the 1970's and 1980's, respectively. The IYHS was developed with the aim of obtaining annual recruitment indices for the combined North Sea herring *Clupea harengus* stock (ICES, 2012), but yielded valuable information on other fish species such as cod *Gadus morhua* and haddock *Melanogrammus aeglefinus*.

The North Sea IBTS began with quarterly surveys providing information on seasonal distribution of stocks sampled, hydrography and the environment, which allows changes in fish stock to be monitored and abundance of all fish species to be determined. These quarterly surveys, however became difficult to sustain as countries experienced budget cuts making it impossible to maintain high levels of research vessel effort. As such, in 1997 countries carried out a survey only twice a year; a first quarter survey (January-February) and a third quarter survey (August-September). The target species of IBTS fished from 1991-2018 includes standard pelagic species: Herring (Clupea harengus), Sprat (Sprattus sprattus) and Mackerel (Scomber scombrus); and standard roundfish species: Cod (Gadus morhua), Haddock (Melanogrammus aeglefinus), Saithe (Pollachius virens), Norway Pout (Trisopterus esmarkii) and Whiting (Merlangius merlangus).

Research vessels from seven nations in the first quarter (Q1) and six nations in the third quarter (Q3) are

used for conducting surveys on all finfish species in the North Sea during January-February and July-August, respectively, between 1997-2017 (Table 4 in Web appendix A gives details of the different research vessels). The sampling frame is defined by the ICES index or roundfish areas (RFA) as shown in Figure 1 numbered 1 to 10, and which we refer to as superstrata (Nottestad et al., 2015; Fuller, 2011). These roundfish areas were substratified into small strata defined by non-overlapping statistical rectangles of roughly $30 \times 30$ nautical miles ($1^o$ Longitude $\times$ $0.5^o$ Latitude), and were convenient to use for North Sea IBTS as they were already being used for fisheries management purposes. Most statistical rectangles contain a number of possible tows that are deemed free of obstructions, and vessels are free to choose any position in the rectangles as long as the hauls are separated by at least 10 nautical miles within and between rectangles. However, all countries select tows based on a semi-random approach from datababes of national safe tows or DATRAS or commercial fishing data, except Sweden who uses fixed stations and in some cases depth-stratified semi-random sampling design (ICES, 2018a), and England who also uses fixed stations and only conduct surveys during the third quarter. In some rectangles, sampling may be further stratified due to significant changes in seabed depth which may, in turn, cause variations in the fish population. In particular, the North Sea IBTS herring, saithe and sprat data are weighted by depth strata in the statistical rectangle (see Table 6 in appendix C). It is also a requirement that countries avoid clustering their stations between adjacent rectangles in order to reduce positive serial correlation, and thereby maximize survey precision. The latest major reallocation of rectangles occurred in 1991, but since then the survey has tried to keep at least one vessel in every subarea in which it had fished in the most recent years. Minor reallocation of rectangles between Norway, Scotland and Germany was done in 2013. Each rectangle was typically sampled twice by two different countries before 1997, but after that target coverage of two trawl hauls per rectangle per survey was introduced because of national financial constraints (ICES, 2015). But in some rectangles in the Eastern English Channel, Southern North Sea and Central North Sea intensified sampling is carried out.

The recommended standard trawling gear of the North Sea IBTS is the mulitpurpose chalut à Grande Ouverture Verticale (GOV) trawl (ICES, 2012), which has been used on all participating vessels since 1992, while different pelagic and bottom trawls suitable for fishing finfish species were used before 1992. Standardized trawling protocols were adopted with a towing speed of 4 knots but depending on vessel performance,

tide and weather conditions the average towing speed can be at minimum 3.5 and maximum 4.5 knots. From 2000-2018 trawling is done during the daylight hours, which are considered 15 minutes before sunrise to 15 minutes after sunset (ICES, 2012). After each trawl the total catch of the different species is weighed on board and biological parameters such as length for all fish species caught (to 0.1cm below for shellfish, to 0.5cm below for herring and sprat and to 1cm below for all other species) are collected. Where the numbers of individuals are too large for all of them to be measured to obtain the length distribution, a representative subsample of 100 fish is selected. Otoliths are collected on board from a small fraction of all the target species from all round fish areas (RFAs) (Figure 1) to retrieve age reading. Table 5 in Web appendix B gives the minimum sampling levels of otoliths for the target species.
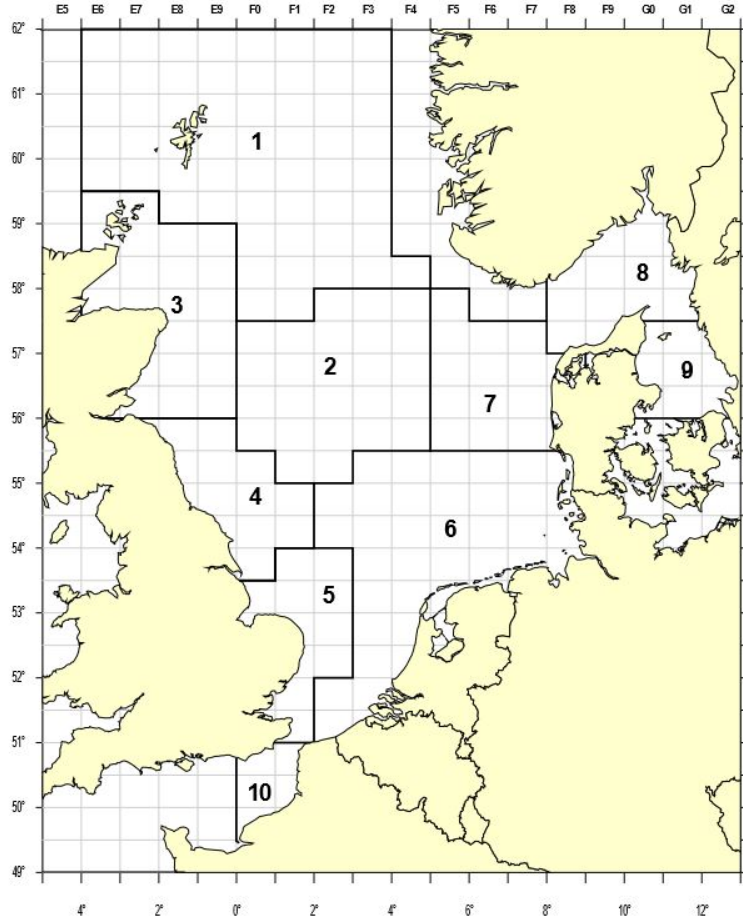


Figure 1: Standard roundfish areas used for roundfish since 1980, for all standard species since 1991. Additional RFA 10 added in 2009. For example, the number 1 indicates ICES Index Area 1, and an ICES Statitical rectangle (ST) in IA 1 is 43F1 (ICES, 2015).

# 2   METHODS

This section gives the estimators of abundance indices. The estimators are haul time-based and utilizes an ALK approach. We consider the ALK approach used in DATRAS and we propose two ALK estimators. The ALK used in DATRAS for computing abundance indices does not account explicitly for the spatial distribution in the age-length composition, which may be different and would result in a biased ALK. This difference may be caused either by variation in length-at-age distributions or by variations in the relative abundance of age classes, that is age-at-length distributions (Gerritsen et al., 2006). To account for the spatial distribution we propose a design-based ALK estimator that is haul dependent (Section 2.2.2) and a model-based ALK estimator (2.2.3).

## 2.1   Catch per unit effort

In this paper, the catch per unit effort (CPUE) is defined as the number of fish of a certain species and age or length which are caught per hour trawl. In this section we define the CPUE matematically, which explains how the index is calculated.

For a given species of interest, let $n_{h,l}$ be the number of fish with length $l$ caught by trawl haul $h$. The CPUE for a given length $l$ by trawl haul $h$ is defined as

$$\text{CPUE}_{h,l} = \frac{n_{h,l}}{d_h}, \tag{2.1}$$

were $d_h$ is the duration of the trawl in hours. The CPUE per age class is further defined as

$$\text{CPUE}_{h,a} = \sum_{l \in \mathbf{L}} \text{CPUE}_{h,l} \times ALK_{a,l,h}, \tag{2.2}$$

where $\mathbf{L}$ is the set of all length classes and $ALK_{a,l,h}$ is the age length key, which represents the estimated proportion of fish with age $a$ in $l$th length class in haul $h$. For a given number of trawl hauls in a statistical rectangle, the mean CPUE defined as mCPUE in a statistical rectangle can be expressed as the average CPUE of the trawl hauls in the statistical rectangle:

$$\text{mCPUE}_{s,a} = \sum_{h \in H_s} \frac{\text{CPUE}_{h,a}}{|H_s|}. \tag{2.3}$$

Here $H_s$ represents the set of trawl hauls taken in statistical rectangle $s$, and $|H_s|$ is the number of hauls taken in the rectangle. The mCPUE in $p$th RFA is further defined as

$$\text{mCPUE}_{p,a} = \sum_{s \in S_p} \frac{\text{mCPUE}_{s,a}}{|S_p|} \omega_s, \tag{2.4}$$

where $S_p$ is the set of all statistical rectangles in RFA $p$, $|S_p|$ is the number of statistical rectangles in RFA $p$, and $\omega_s$ is a weight variable for each statistical rectangle. The weight variable $\omega_s$ varies between species. For some species $\omega$ equals 1 (e.g. Gadus morhua) for all $s$, and for other species it is the proportion of the statistical rectangle which has depth between 10 to 200 meters, for example Pollachius virens (see Table 6 in Web appendix C for weightings of statistical rectangles). The index for abundance at age in the whole study area, $mCPUE_{N,a}$, is further defined by

$$mCPUE_{N,a} = \frac{\sum_{p \in \mathbf{P}} A_p \text{mCPUE}_{p,a}}{A_{\text{total}}}. \tag{2.5}$$

Here $\mathbf{P}$ is the set of RFAs, $A_p$ is the area of RFA $p$, and $A_{\text{total}} = \sum_{p \in \mathbf{P}} A_p$.

## 2.2 ALK Estimators

The definition of the CPUE of age includes an ALK, see (2.2), which we described in this section. Three ALK estimators are included in this paper, which are named as follows: $i$) DATRAS ALK, $ii$) haul based ALK and $iii$) model based ALK.

### 2.2.1 DATRAS ALK

Let $\text{ALK}^{\text{D}}$ denote the DATRAS ALK. The $\text{ALK}^{\text{D}}$ is defined as constant within each RFA, and is calculated for each RFA by aggregating the age observation from each RFA. $ALK^{\text{D}}_{a,l,h}$ used in equation (2.2) is defined as the proportion of observed fish with age $a$ in length class $l$ in the RFA $h$. If there are no observed fish in length class $l$ in the RFA, ages from length classes close to $l$ is used. The details of the procedure for borrowing strength from neighbouring length classes are given in Web appendix D.1. The underlying assumption of this ALK is that age-length compositions are homogeneous within the RFAs. This is a rather strong assumption, and any violation would have an unknown impact on the estimates of abundance indices. Aanes and Vølstad (2015) illustrated that violation of the assumption of constant ALK leads to biased estimates of CPUEs.

*2.2.2   Haul based ALK*

We define a haul dependent ALK by $ALK^H$. The $ALK^H_{a,l,h}$ is defined as the average proportion of observed

fish with age $a$ in **length class $l$ in haul $h$?**. If there are no observed ages of fish in a length class $l$ in the

haul, ages from the same length class in the haul close by is used (Web appendix D.2 describes the procedure

in detail).

*2.2.3   Spatial Model-Based ALK Estimator*

In this section we introduce a spatial model based ALK. Using such a model enables us to obtain smooth

structures in the distribution of age given length. It further enables us to utilize spatial latent effects. Spatial

model-based approach of age-lengths are widely used (Berg and Kristensen, 2012; Hirst et al., 2012; Rindorf

and Lewy, 2001), and are used for stock assessment in the North Sea (Berg et al., 2014).

Let the response variable of the age group of a fish be $a = M, ..., A$ where $M$ is the youngest age, and

$A$ is the oldest age which is typically defined as a "plus group". Suppose $y(l, \mathbf{s}, h)$ is the age of a fish with

length $l$ caught at location $\mathbf{s}$. As in Berg and Kristensen (2012) we use a continuous ratio model for the

spatial age given length model. **That is, let**

$$\pi_a(y(l, \mathbf{s})) = P(y = a | y \geq a, l, \mathbf{s}) = \frac{p_a(l, \mathbf{s})}{p_a(l, \mathbf{s}) + \cdots p_{A-1}(l, \mathbf{s})} \quad \textbf{for } a = M, ..., A - 1, \tag{2.6}$$

**were $p_a(l, s)$ is the probability of a fish with length $l$ at location s to be of age $a$. Further is it**

**assumed a logit link**

$$\log \left( \frac{\pi_a(y(l, \mathbf{s}))}{1 - \pi_a(y(l, \mathbf{s}))} \right) = \beta_a + f_a(l) + \gamma_a(\mathbf{s}). \tag{2.7}$$

**Here $\beta_a$ is an intercept, $f_a(l)$ is a continuous function of length and $\boldsymbol{\gamma}$ is a mean zero Gaussian**

**spatial random field with Matérn covariance function. The spatial random field is intended to**

**capture any spatial variation in the ALK.**

*these equations and definitions above are not quite clear. these definitions of the equations need restructuring*

*i think. we need to explain what is on the left hand side of (2.6), for example, Let the probability of a fish of*

*age a given length l at location s be defined as ....I do not understand the meaning of the word logit attached*

*to the left side of (2.7) and a definition of the left hand side of (2.7) is needed also, again for example,*

*Further, let the probability of......be...... Also, where in equation (2.6) is equation (2.7) used or called? Also, are we including haul effect in the model or has it been include already and our results are reflecting that, and if not should we state that it's possible to include random effects and how it can be done?*

The continuous function $f_a(l)$ in (2.7) is modelled with usage of P-splines (Wood, 2017), and these spline regression coefficients are included as a Gaussian random effect. The precision matrix for the spline regression coefficients is constructed such that the variability (or wryggliness) in the spline is penalized, see Wood (2017, page 239) for details. The R package mgcv (Wood, 2015) is used for extracting the precision matrix needed for the spline regression coefficients.

We assume that the spatially Gaussian random field in (2.7), $\boldsymbol{\gamma}$, follows a stationary Matérn covariance structure:

$$\text{Cov}(\gamma(\mathbf{s}_1), \gamma(\mathbf{s}_2)) = \frac{\sigma_\gamma^2}{2^{\nu-1}\Gamma(\nu)} (\kappa_\gamma ||\mathbf{s}_1 - \mathbf{s}_2||)^\nu K_\nu(\kappa_\gamma ||\mathbf{s}_1 - \mathbf{s}_2||), \tag{2.8}$$

where $\sigma_\gamma^2$ is the marginal variance, $|| \cdot ||$ is the Euclidean distance measure in kilometres, $\nu$ is a smoothing parameter, $\kappa_\gamma$ is a spatial scale parameter and $K_\nu(\cdot)$ is the modified Bessel function of the second kind with $\nu = 1$. The spatial field is estimated with the stochastic partial differential equation (SPDE) procedure described in Lindgren et al. (2011). The main concept behind the SPDE procedure is that the precision matrix of a spatial field with Matérn covariance function can be approximated by a sparse matrix on a grid covering the area of interest. Such a grid and sparse precision matrix are constructed with use of the R-INLA package (Rue et al., 2009).

The model based ALK estimate is obtained by maximizing the likelihood. We maximize the likelihood with use of an R-Package called Template Model Building (TMB), (Kristensen et al., 2015) combined with the optimizing function nlminb in R. In this application TMB is advantageous as it **it Laplace approximate the latent fields for computational efficiency,** utilizes sparse structures in the latent fields, and uses automatic derivation. The time needed for estimating the model varies slighlty between species and year. A laptop with processor intel(R) Core(TM) i5-6300 CPU @ 2,40 GHz, used e.g. approximately 2 minutes to estimate the **model** for cod in year 2018.

## 2.3 Uncertainty estimation

In this section we describe how the uncertainty of the CPUE estimates are calculated. We use nonparametric bootstrapping to quantify the uncertainty of the CPUEs. Nonparametric resampling allows us to estimate the sampling distribution of the CPUE empirically without making assumptions concerning the data. The percentile method is used to estimate 95% confidence intervals of the estimated CPUEs (Carpenter and Bithell, 2000).

A bootstrap procedure for estimating the uncertainty of CPUEs in the North Sea is suggested in ICES (2013). In the rest of this paper, we refer to this procedure as DATRAS bootstrap procedure. The DATRAS procedure is divided into two parts; one part which samples CPUE per length (2.1), and another part which samples the ALK used in (2.2). The DATRAS bootstrap procedure is based on the assumption of homogeneous CPUE within RFAs. This assumption is likely to be wrong, and will typically cause an overestimation of the uncertainty. Therefore, we have included a bootstrap procedure, defined as the stratified bootstrap procedure, which instead assumes constant CPUE within each statistical rectangle.

### 2.3.1 DATRAS and stratified bootstrap procedure

In this section we describe the bootstrap procedure for catch at length proposed by *DATRAS* (ICES, 2013) and the stratified procedure, and elaborate how the ALK is simulated. Assume there are $N_\mathrm{s}$ trawl hauls in a statistical rectangle. The DATRAS bootstrap procedure consists of sampling with replacement $N_\mathrm{s}$ of all trawl hauls in the corresponding RFA, and place them in the statistical rectangle. This procedure is performed independently across all statistical rectangles. It is worth reiterating that this procedure is based on the assumption that ALK is homogeneous in the whole RFA. The stratified bootstrap procedure is a modification of the DATRAS bootstrap procedure. Rather than sampling hauls from the whole RFA, we sample the $N_\mathrm{s}$ trawl hauls from the list of hauls within the same statistical rectangle. If there is only one trawl haul within a statistical rectangle, we sample either that haul or the closest haul.

For simulating the DATRAS ALK we sample with replacement age observations within each RFA stratified with respect to length. If there is only one observed age from a given length class, we sample either that age or, at random, an age of the closest length class with observed ages. For the haul based ALK,

<sup>218</sup> we use the observed ages in the sampled hauls when simulating the CPUE per length (**is this from the**

<sup>219</sup> **stratified bootstrap procedure? what about explanations for the model based ALK? We also**

<sup>220</sup> **have codes for stratified procedure where DATRAS ALK is used, should we mention that this**

<sup>221</sup> **is done INSTEAD or AS WELL and include this results below in results section? Jon Helge**

<sup>222</sup> **mentioned that it's not plausible to show results of DATRAS bootstrap as it does not account**

<sup>223</sup> **for the survey design. Better off using our proposed stratified procedure with DATRAS ALK**).

## *2.4 Reducing sampling effort*

<sup>225</sup> The current sampling procedure for the North Sea IBTS data is the sampling of one otolith from every

<sup>226</sup> observed length group in every trawl (see Table 5 in Web appendix B). We investigate the effect on the

<sup>227</sup> estimated mCPUE and its variance if the sampling procedure of otoliths changes such that fewer otoliths

<sup>228</sup> were collected. To determine this effect we remove otholits in a stratified manner, mimicking a sampling

<sup>229</sup> procedure where fewer otoliths are collected. For sampling fewer otoliths, we define wider length groups, for

<sup>230</sup> example 2 cm, or 3 cm, or 5 cm and so on, and simulate the otolith collection such that only one otolith is

<sup>231</sup> sampled from every wider length group. This removal procedure is flexible as pooling can be adjusted such

<sup>232</sup> that information on age-length distribution is not lost due to pooling. Estimated mCPUE's with summary

<sup>233</sup> statistics, based on the simulated reduced data sets are then compared with the parameters estimated from

<sup>234</sup> using all of data. In principle, we are free to define any length class to reduce the number of observed

<sup>235</sup> otoliths. For simplicity we propose two procedures: i) sample at random one otolith from every 2 cm length

<sup>236</sup> group, and ii) sample at random one otolith from every 5 cm length group. These are reasonable grouping

<sup>237</sup> procedures for the species of interest as indicated in Figure 2, since the likelihood of overlapping in these

<sup>238</sup> groups is small. The species and data used in this research are discussed in detail in Section 3. Figure 3.1

<sup>239</sup> gives predicted probabilities of age given length of two target species of IBTS.

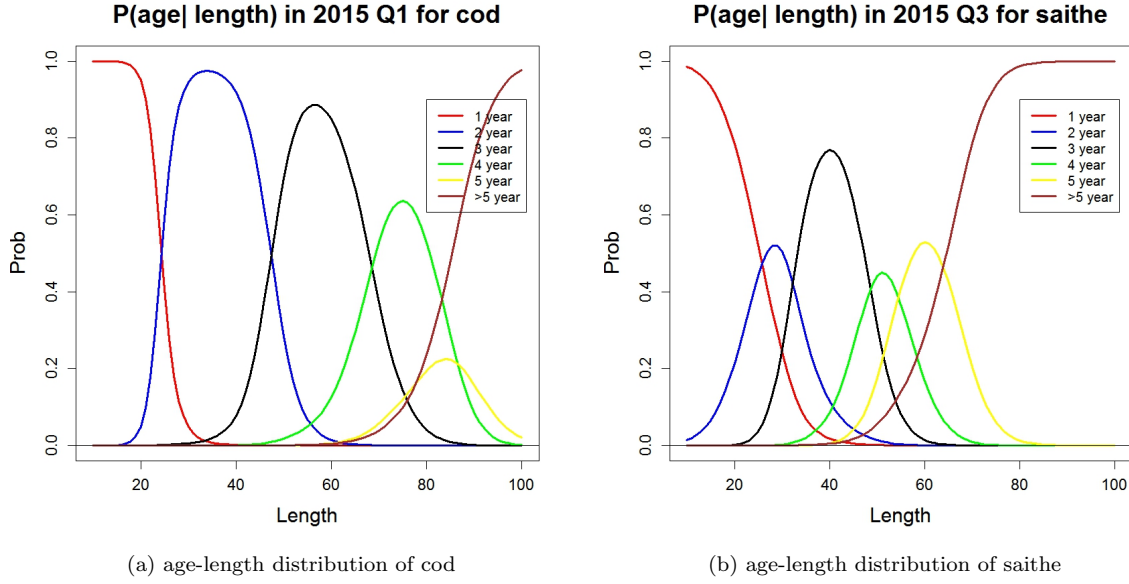| P(age\| length) in 2015 Q1 for cod | P(age\| length) in 2015 Q3 for saithe |
|---|---|
| (a) age-length distribution of cod | (b) age-length distribution of saithe |

Figure 2: Predicted probabilities of age given length using the model described in (2.6) and (2.7) for cod (left panel) and saithe (right panel) in Q1 and Q3, respectively in year 2015.

- *I thought to include this plot here to show that it's reasonable to group at 2cm and 5 cm*

- *If 2018 data would be used these plots need updating with that data*

- *include (cm) on the x-axis to demonstrate the unit used for length; write out the word "probability" on y- axis; remove bold titles on the plots*

# 3   Case studies

In this section we apply the methods described in Section 2 to data from the International Bottom Trawl Survey for the year 2018, which is obtained from the DATRAS database (ICES, 2018b). We choose year 2018 because in that year new sampling procedures proposed by ICES for the collection of otoliths were introduced in the surveys. For instance, one otolith per length group is sampled for most target species (see Table 5 in Web appendix B for details of the sampling procedures for each target species). In this paper the focal species are cod and saithe and the samples are collected in the first and third quarters. All samples are caught using the standard GOV gear described in Section 1.1. Table 1 gives a brief description of the data for year 2018 in the first quarter. The data (Table 1) shows that cod can be as old as 8 years, and saithe as

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old as ..... years but for simplicity, in our analyses we consider the age groups 1 to 6+ for all ALK methods, where the last group consists of fish of age 6 or older . Note that age 0 for the target species are included in IBTS and are required in the calculation of the ALKs but the results of these estimation are not included in any further analyses.

- *logical reasons for using 2018 data but we do not have Q3 data and it was recommended by J Devine etc to use Q3 data for saithe (I am not sure of the reasons, we could clarify this) but Q1 is not recommended for saithe. Should we consider 2017 as most countries were adopting the sampling strategy of one otolith per cm at that time?*

- *possibly explain the data in Table 1 a bit more, here in this paragraph?*

- *I am unable to extract year and haul.ID from the data, subsetting etc doesnt seem to work to filter on 2018 only to fill this Table with relevant information. This is strange and I do not know why*

Table 1: Summary of North Sea IBTS cod and saithe (in parentheses) data for first quarter in year 2018.

| Data | Description |
|---|---|
| Trawl hauls | Total of 357 trawl hauls in Q1 of 2018, 238 (83) with length and 231 (82) with age information |
| Age | The age of cod varied between 1 to 8 years, while saithe age ranged from 1 to .... |
| Length | Length information in cm of each cod varied between 8 to 112 cm while saithe varied between ... to ... cm |
| Date | Date of catch in Q1 varied between 13.01.2015 to 19.02.2015 and in Q3 between 26.07.2015 to 06.09.2015 |
| Duration of haul | Mean duration is 25.9 minutes, with 15 to 30 minutes as 90% coverage interval. |
| Total count for all ages | ..... cod in year 2018 Q1 and ....saithe in Q1 of 2018. |

## 3.1 Cod and Saithe using ALK methods

Recall that the main assumption of DATRAS ALK is that the age-length compositions of species across large areas are the same. To illustrate that this assumption may not be valid, we used the spatial ALK model (2.7) to predict probabilities of age given length of a .....cm long cod and a .....cm long saithe in the North Sea (Figure 3). These plots provide strong evidence against a null hypothesis of no spatial effect in

the ALKs, as the likelihood of age given length changes in some areas. The plots also suggest that cod is distributed in all areas of the North Sea (Figure 3 (a)), whereas saithe is more likely to inhabit areas in the northern North Sea, specifically RFA 1 (Figure 3 (b)).

Table 2 shows abundance indices, defined in (2.5), of cod and saithe estimated from each of the three ALK methods. Estimates of the standard error (SE), relative standard error (RSE in parentheses), the lower bound (LB) and upper bound (UB) of approximate 95% confidence intervals are also given. The estimated indices of abundance of cod are similar for all ALKs, but the the spatial ALKs generally gave higher estimates. Also, the spatial ALKs provide a better fit to the data in terms of precision. Uncertainty estimates (RSE) for older fishes ($\geq 4$) are higher, as expected, for the spatial ALKs as fewer samples are generally collected for these, and given that spatial variation in the data is accounted for, variability would be higher.

Abundance indices of saithe ......

- *generate plots for year 2018 Q1. Possibly show same age given length group for both species?*

- *discuss differences in estimates from ALK methods (Table 2 - in terms of relative standard error estimates; overestimation and underestimation from DATRAS (bootstrap) method not knowing the strength in either direction) - Issues:*

    − *Ignores fine scale stratification at the first stage, hence overestimation of the uncertainty*

    − *Ignores age-length data collected at the haul level, hence underestimates the uncertainty*

    − *Biases in both direction*

- *test for significant differences between estimates from ALK methods for age groups?*

- *As discussed in Section 2.2.1 and shown in the results in Table 2 the assumption of no difference in regional compositions of age-length structures is invalid and DATRAS ALK have introduced bias in both direction, and the extent of this bias in either direction is unknown. Hence, this ALK is not appropriate to perform further analyses.*

- *codes do not run for saithe Q1 2018*
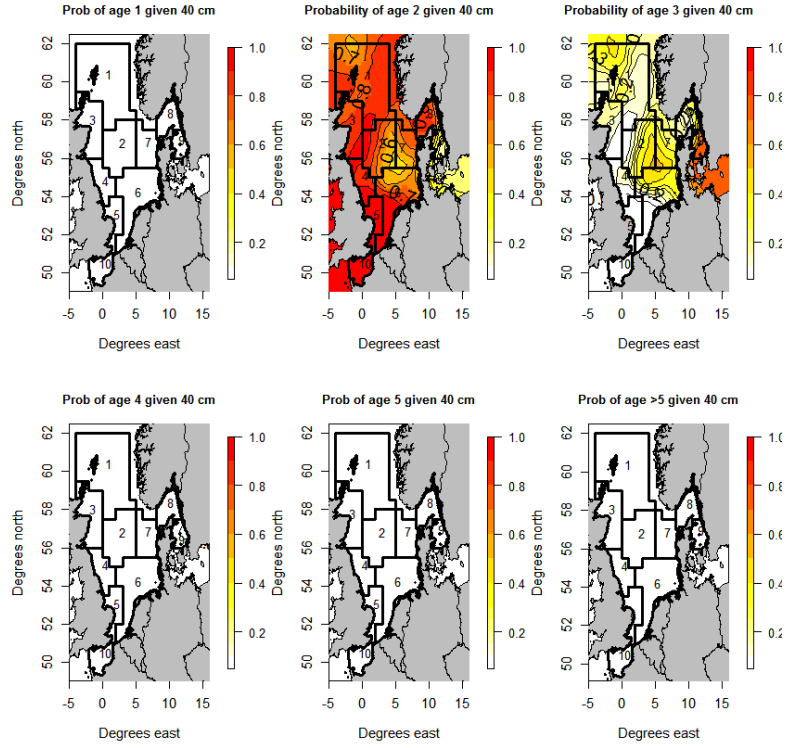
**(a) cod**
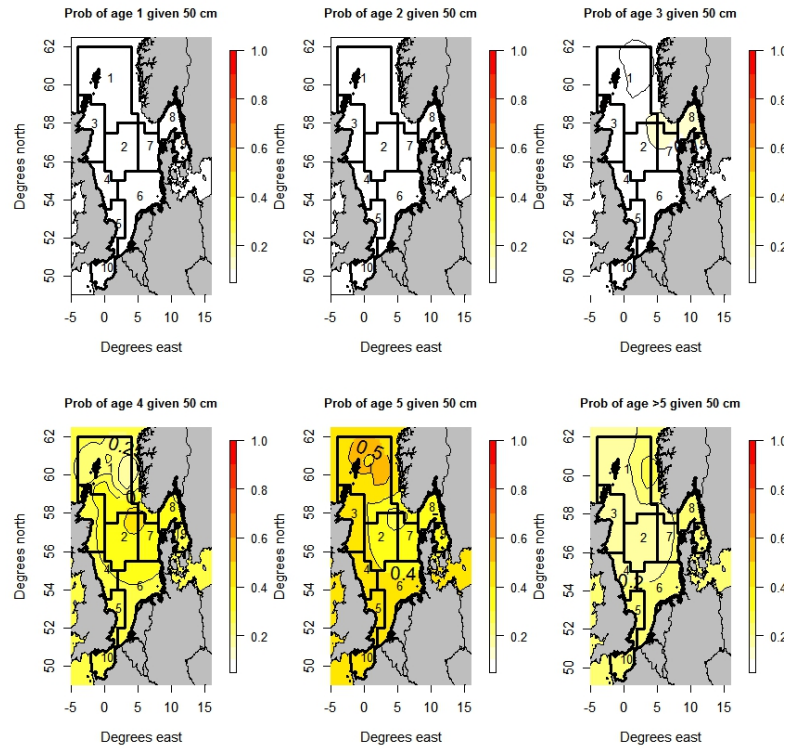


**(b) saithe**

Figure 3: Predicted probabilities of age given length using model (2.6) and (2.7) for the year 2018 Q1. Graph (a) gives probabilities of predicted age of a ....cm long cod, and graph (b) gives probabilities of predicted age of a ....cm saithe in RFAs 1 to 10 in the North Sea.

Table 2: Average estimates of abundance indices for the North Sea cod and saithe species from 200 bootstrap samples and 100 simulation runs, in year 2018 Q1. Standard error estimates (SE) (relative standard error, RSE in parentheses) and the lower bounds (LB) and upper bounds (UP) of approximate 95% confidence intervals from the three ALK methods are also given.

| Species | $a$ | DATRAS ALK | | | | Haul based ALK | | | | Model based ALK | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| | | $m\widehat{CPUE}_{N,a}$ | SE(RSE) | LB | UB | $m\widehat{CPUE}_{N,a}$ | SE (RSE) | LB | UB | $m\widehat{CPUE}_{N,a}$ | SE (RSE) | LB | UB |
| **cod 2018 Q1** | 1 | 0.895 | 0.13 (14.5%) | 0.671 | 1.180 | 0.905 | 0.13 (14.4%) | 0.712 | 1.206 | | (%) | | |
| | 2 | 6.758 | 0.99 (14.6%) | 5.399 | 8.722 | 6.811 | 1.07 (15.7%) | 5.283 | 9.276 | | (%) | | |
| | 3 | 1.771 | 0.21 (11.9%) | 1.321 | 2.108 | 1.652 | 0.17 (10.3%) | 1.260 | 1.948 | | (%) | | |
| | 4 | 1.655 | 0.29 (17.5%) | 1.009 | 2.126 | 1.667 | 0.32 (19.2%) | 0.917 | 2.048 | | (%) | | |
| | 5 | 0.821 | 0.16 (19.5%) | 0.468 | 1.045 | 0.782 | 0.12 (15.3%) | 0.497 | 0.954 | | (%) | | |
| | 6+ | 1.049 | 0.23 (21.9%) | 0.529 | 1.365 | 1.131 | 0.30 (26.5%) | 0.361 | 1.438 | | (%) | | |
| **saithe 2018 Q1** | 1 | 0.059 | 0.03 (50.1%) | 0.030 | 0.079 | 0.059 | 0.01 (16.9%) | 0.031 | 0.041 | | (%) | | |
| | 2 | 0.06 | 0.02 (33.3%) | 0.058 | 0.085 | 0.059 | 0.01 (16.9%) | 0.057 | 0.067 | | (%) | | |
| | 3 | 2.805 | 2.63 (93.8%) | 0.469 | 5.442 | 0.372 | 0.07 (18.8%) | 0.305 | 0.427 | | (%) | | |
| | 4 | 16.752 | 14.06 (83.9%) | 2.644 | 29.272 | 15.017 | 11.68 (69.7%) | 3.081 | 24.999 | | (%) | | |
| | 5 | 12.117 | 10.35 (85.4%) | 3.112 | 22.655 | 16.119 | 12.45 (77.8%) | 3.457 | 26.877 | | (%) | | |
| | 6+ | 3.983 | 1.74 (43.7%) | 2.126 | 5.408 | 4.150 | 2.03 (48.9%) | 1.968 | 5.829 | | (%) | | |
| **saithe 2017 Q3** | 1 | 0.130 | 0.05 (38.4%) | 0.046 | 0.213 | 0.132 | 0.05 (37.9%) | 0.053 | 0.213 | | (%) | | |
| | 2 | 1.293 | 0.30 (23.2%) | 0.658 | 1.812 | 1.190 | 0.29 (24.4%) | 0.500 | 1.562 | | (%) | | |
| | 3 | 14.812 | 2.31 (15.6%) | 9.282 | 18.088 | 14.979 | 2.16 (14.4%) | 9.554 | 17.404 | | (%) | | |
| | 4 | 16.391 | 2.39 (14.6%) | 10.705 | 20.116 | 16.256 | 2.31 (14.2%) | 10.841 | 19.738 | | (%) | | |
| | 5 | 3.832 | 0.59 (15.4%) | 2.782 | 4.979 | 3.913 | 0.74 (18.9%) | 2.618 | 5.204 | | (%) | | |
| | 6+ | 3.190 | 0.54 (16.9%) | 2.104 | 4.149 | 3.178 | 0.56 (17.6%) | 2.183 | 4.300 | | (%) | | |

## 3.2   Optimum sampling effort for North Sea Cod and Saithe

In order to determine optimum sampling levels of otoliths for saithe and cod in the North Sea, ALKs are estimated using the haul-based method. The haul based ALK and spatial ALK model gave similar estimates of abundance indices and precision (Table 2) as both approaches account for spatial variation in the data. The spatial ALK model is quite complex, and model fitting would be computer-intensive since the model must be fitted for each bootstrap run and each simulated sampling procedure that mimics the real data collection procedure. Also, the assumption of no difference in regional compositions of age-length structures is invalid, as shown in Figure 3 and Table 2, so DATRAS ALK method is not use for further analyses.

In the year 2018 Q1, **x** otoliths for cod and **y** otoliths for saithe were sampled (Table 1). Sampling at random, one otolith per 2 cm length group removes **x** percent of otoliths for cod and **y** percent of otoliths for saithe; while **x**% of otoliths for cod and **y**% of otoliths for saithe are removed when one otolith per

$_{305}$ 5 cm length group is sampled. Table 3 gives estimates of abundance $\left(m\widehat{CPUE}_{N,a}\right)$, its standard error

$_{306}$ $\left(\widehat{SE}_{mCPUE_{N,a}}\right)$ and the upper bound (UP) and lower bound (LB) of the parameter estimates when all the

$_{307}$ otolith data is used and when either one otolith is sampled per 2 cm or 5 cm length group for $n = 100$

$_{308}$ simulations and $B = 200$ bootstrap runs. The coefficient of variation ($Cv\%$) is also given.

$_{309}$ Sampling one otolith per 2 cm or 5 cm length group provide .........

$_{310}$ • discuss effects of this reduction on estimate and variance

$_{311}$ • make reference to plot in Figure 2

$_{312}$ • fill **x** and **y** in text with values

Table 3: Estimates of abundance indices and standard error estimates for the North Sea cod and saithe species when all the otolith data is used and when one otolith per 2 cm or 5 cm length group is used. The lower bounds (LB) and upper bounds (UP) of approximate 95% confidence intervals are given.

| Species | $a$ | No. otoliths | All data | | Reduced data by 2 cm | | | | | | Reduced data by 5 cm | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| | | | | | $m\widehat{CPUE}_{N,a}$ | | | $\widehat{SE}_{mCPUE_{N,a}}$ | | | $m\widehat{CPUE}_{N,a}$ | | | $\widehat{SE}_{mCPUE_{N,a}}$ | | |
| | | | $m\widehat{CPUE}_{N,a}$ | $\widehat{SE}_{mCPUE_{N,a}}$ | LB | UB | $Cv\%$ | LB | UB | $Cv\%$ | LB | UB | $Cv\%$ | LB | UB | $Cv\%$ |
| cod | 1 | | 0.764 | 0.26 | 0.60 | 0.24 | | | 0.70 | 0.36 | | | | | | |
| | 2 | | 21.989 | 6.76 | 22.21 | 4.15 | | | 22.11 | 4.28 | | | | | | |
| | 3 | | 11.285 | 2.19 | 10.58 | 1.20 | | | 10.99 | 1.77 | | | | | | |
| | 4 | | 3.265 | 0.71 | 3.67 | 1.28 | | | 3.50 | 0.87 | | | | | | |
| | 5 | | 1.147 | 0.34 | 1.27 | 0.42 | | | 1.20 | 0.48 | | | | | | |
| | 6+ | | 1.276 | 0.38 | 1.40 | 0.70 | | | 1.21 | 0.42 | | | | | | |
| saithe | 1 | | 0.764 | 0.26 | 0.60 | 0.24 | | | 0.70 | 0.36 | | | | | | |
| | 2 | | 21.989 | 6.76 | 22.21 | 4.15 | | | 22.11 | 4.28 | | | | | | |
| | 3 | | 11.285 | 2.19 | 10.58 | 1.20 | | | 10.99 | 1.77 | | | | | | |
| | 4 | | 3.265 | 0.71 | 3.67 | 1.28 | | | 3.50 | 0.87 | | | | | | |
| | 5 | | 1.147 | 0.34 | 1.27 | 0.42 | | | 1.20 | 0.48 | | | | | | |
| | 6+ | | 1.276 | 0.38 | 1.40 | 0.70 | | | 1.21 | 0.42 | | | | | | |

# 4 DISCUSSION

In this paper we have determined minimum sampling efforts of otoliths for target species of the North Sea International Bottom Trawl Survey. This was achieved by testing sampling procedures that mimic the real data collection procedure but with a reduced number of otoliths. Two sampling procedures, 1) sampling at random, one otlotih per 2 cm and 2) sampling at random, one otolith per 5 cm length group, were tested and the effect on estimated abundance indices and their variance were investigated. Abundance indices were estimated using age-length keys (ALKs). The database for trawl surveys (DATRAS) manned by ICES includes an ALK that uses the raw proportions of age given length assuming constant age-length compositions over relatively large areas. We have developed two spatial ALK methods to estimate abundance indices and their variance that accounts for spatial variation in the data: 1) a haul based ALK that produces an ALK for each trawl haul, and which uses the raw proportions of age given length, and 2) a spatial ALK model that uses logits for modelling the age distribution in catch data from the length-stratified subsamples. Several studies have used spatial ALK modelling for estimating abundance indices of the North Sea stocks used in assessments (Berg and Kristensen, 2012; Berg et al., 2014; Gerritsen et al., 2006). These studies used continuous ratio logits with Generalized Linear Model (GLM) or General Additive Models (GAMs) to model the spatial effects and found regional effects...... We propose to use Gaussian Random Field Theory to model the spatial effects as a smooth surface.........

- discuss positives of using GRT to model spatial effects: what problems are eliminated when using this in terms of missing data

- compare the effects of our method with GAMs (Berg and Kristensen, 2012)

- what does our model allows in terms of the age groups (samller or higher age groups (6+) possible with our model); covariates such as haul effect (included as a random effect)

Also, both spatial ALK methods proposed in this paper provided a much better fit to the data compared with DATRAS ALK....

Reducing the number of otoliths by ....... percent had **no** significant effect on estimated abundance

- discuss sampling procedure: limitation and advantages; and possibly more advanced selection procedures?

- new approach adopted in surveys from 2018

- IBTS has a standardized survey indices? so changes in catch rates are due to changes in population size? Berg et al. (2014) developed a standardized index for IBTS data but only applied to some species e.g., haddock? cod- last year 2017

- how does changes in survey design or other factors affect changes in catch rates? If so are these changes significant?

# 5   General comments

- Decide on whether we say, "in this research or paper"

- Decide on whether to say, "In this subsection or section"

- Decide on year of data for case studies

- Decide on writing "haul(model)-based or haul (model) based

- Decide on calling the survey "The North Sea IBTS or IBTS"

- Decide on writing "Cod or cod, and Saithe or saithe"

- Decide on a title for the paper

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# A  Areas fished by different countries in the North Sea IBTS

Typically, two different countries fish each rectangle so that at least two trawl hauls are made per rectangle, but intensified sampling is carried out in the following areas: at least 3 hauls per rectangle are taken in statistical rectangles 31F1, 31F2, 32F1, 33F4, 34F2, 34F3, 34F4, 35F3, 35F4; while six or more hauls per rectangle are taken in statistical rectangles 30F1, 32F2, 32F3, 33F2, 33F3 (ICES 1999). The Skagerrak and Kattegat is fished solely by Sweden, who sample more than once in every rectangle while the west of Shetland (in Q1 and Q3) and inshore areas (Q3) is fished solely by Scotland. The edge of the Norwegian Trench is fished solely by Norway, but inshore areas near Denmark is fished by Denmark. The southern North Sea is fished by Denmark, Germany and England. France, typically, is the only country that surveys the western English Channel. Areas are surveyed by a single country because of the large proportion of untrawalable area (and subsequent gear damage issues experienced by other nations) for efficient logistical purposes. Table 4 gives the countries and research vessels participating the North Sea IBTS.

Table 4: Survey countries, vessel name, and period research vessels participating in first quarter (Q1) and third quarter (Q3) during 1997-2017.

|  | **First Quarter (Q1)** | | **Third Quarter (Q3)** | |
| **Country** | Vessel name | Period | Vessel name | Period |
| Denmark | Dana | January-February | Dana | July-August |
| France | Thalassa II | January-February | - | - |
| Germany | Walther Herwig III | January-February | Walther Herwig III | July-August |
| Netherlands | Tridens 2 | January-February | - | - |
| Norway | G.O. Sars | January-February | Johan Hjort | July |
| UK England | - | - | Endeavour | August-September |
| UK Scotland | Scotia III | January-February | Scotia III | July-August |
| Sweden | Dana | January-February | Dana | August |

# B  Otolith sampling per fish species

From 1991-2017, most countries conducted quota sampling of otoliths per length group in a RFA. But from 2013 Norway has been sampling one otolith per length class from each trawl haul (to 0.1cm below for shellfish,

to 0.5cm below for herring and sprat and to 1cm below for all other species). From the first quarter in 2018 all countries are required to sample one otolith per length class per trawl haul. Table 5 gives the minimum sampling levels of otoliths for the target species. However, for the smallest size groups, that presumably contain only one age group, the number of otoliths per length class may be reduced, and more otoliths per length are required for the larger length classes.

Table 5: Minimum sampling levels of otoliths by species for RFA or per trawl haul.

| Period | Species | Minimum sampling levels of otoliths per length class |
|---|---|---|
| **1991-2017** | | **Number of otoliths per length class in a RFA** |
| | herring | 8 otoliths per $\frac{1}{2}$ cm group |
| | sprat | 16 otoliths per $\frac{1}{2}$ cm length class $8.0 - 11.0$ cm |
| | | 12 otoliths per $\frac{1}{2}$ cm length class $\geq 11.0$ cm |
| | mackerel | 8 otoliths per $\frac{1}{2}$ cm length class |
| | cod | 8 otoliths per 1 cm length class |
| | haddock | 8 otoliths per 1 cm length class |
| | whiting | 8 otoliths per 1 cm length class |
| | Norway pout | 8 otoliths per 1 cm length class |
| | saithe | 8 otoliths per 1 cm length class |
| | All target species | From 2013 Norway and Scotland, and Netherlands from 2016 have been sampling 1 otolith per length class from each trawl haul (to 0.1cm below for shellfish, to 0.5cm below for herring and sprat, and to 1cm below for all other species). |
| **2018** | | **Number of otoliths per length class per trawl haul** |
| | herring | 1 otolith per $\frac{1}{2}$ cm group |
| | sprat | 1 otolith per $\frac{1}{2}$ cm length class $8.0 - 11.0$ cm |
| | | 1 otolith per $\frac{1}{2}$ cm length class $\geq 11.0$ cm |
| | mackerel | 1 otolith per 1 cm length class |
| | cod | 1 otolith per 1 cm length class |
| | haddock | 2 otoliths per 5 cm length class $11 - 15, 16 - 20, 21 - 25, 26 - 30$ cm |
| | Norway pout | 2 otoliths per 5 cm length class $5 - 10, 11 - 15$ cm |
| | | 2 otoliths per 1 cm length class $> 15$ cm |
| | saithe | 1 otolith per 1 cm length class |
| | plaice | 1 otolith per 1 cm length class |

# C    Weightings of Statistical Rectangles

Table 6: Weights used for Pollachius virens in equation (2.3).

| StatRec | Weight | StatRec | Weight | StatRec | Weight | StatRec | Weight | StatRec | Weight |
|---------|--------|---------|--------|---------|--------|---------|--------|---------|--------|
| 31F1 | 0.6  | 38F0 | 1    | 41F7 | 1    | 44F3 | 1    | 48E7 | 1    |
| 31F2 | 0.8  | 38F1 | 1    | 41F8 | 0.1  | 44F4 | 1    | 48E8 | 0.9  |
| 31F3 | 0.05 | 38F2 | 1    | 41G0 | 0.2  | 44F5 | 0.9  | 48E9 | 1    |
| 32F1 | 0.8  | 38F3 | 1    | 41G1 | 0.97 | 44F8 | 0.25 | 48F0 | 1    |
| 32F2 | 1    | 38F4 | 1    | 41G2 | 0.53 | 44F9 | 0.8  | 48F1 | 1    |
| 32F3 | 0.8  | 38F5 | 1    | 42E7 | 0.4  | 44G0 | 0.94 | 48F2 | 1    |
| 32F4 | 0.01 | 38F6 | 1    | 42E8 | 1    | 44G1 | 0.6  | 48F3 | 0.5  |
| 33F1 | 0.3  | 38F7 | 1    | 42E9 | 1    | 45E6 | 0.4  | 48G0 | 0.02 |
| 33F2 | 1    | 38F8 | 0.3  | 42F0 | 1    | 45E7 | 1    | 49E6 | 0.8  |
| 33F3 | 1    | 39E8 | 0.5  | 42F1 | 1    | 45E8 | 1    | 49E7 | 1    |
| 33F4 | 0.4  | 39E9 | 1    | 42F2 | 1    | 45E9 | 1    | 49E8 | 0.4  |
| 34F1 | 0.4  | 39F0 | 1    | 42F3 | 1    | 45F0 | 1    | 49E9 | 1    |
| 34F2 | 1    | 39F1 | 1    | 42F4 | 1    | 45F1 | 1    | 49F0 | 1    |
| 34F3 | 1    | 39F2 | 1    | 42F5 | 1    | 45F2 | 1    | 49F1 | 1    |
| 34F4 | 0.6  | 39F3 | 1    | 42F6 | 1    | 45F3 | 1    | 49F2 | 1    |
| 35F0 | 0.8  | 39F4 | 1    | 42F7 | 1    | 45F4 | 0.6  | 49F3 | 0.5  |
| 35F1 | 1    | 39F5 | 1    | 42F8 | 0.2  | 45F8 | 0.3  | 50E6 | 0.1  |
| 35F2 | 1    | 39F6 | 1    | 42G0 | 0.32 | 45F9 | 0.02 | 50E7 | 0.6  |
| 35F3 | 1    | 39F7 | 1    | 42G1 | 0.89 | 45G0 | 0.24 | 50E8 | 0.7  |
| 35F4 | 0.9  | 39F8 | 0.4  | 42G2 | 0.64 | 45G1 | 0.55 | 50E9 | 0.9  |
| 35F5 | 0.1  | 40E7 | 0.04 | 43E7 | 0.03 | 46E6 | 0.4  | 50F0 | 1    |
| 36F0 | 0.9  | 40E8 | 0.8  | 43E8 | 0.9  | 46E7 | 0.9  | 50F1 | 1    |
| 36F1 | 1    | 40E9 | 1    | 43E9 | 1    | 46E8 | 1    | 50F2 | 1    |
| 36F2 | 1    | 40F0 | 1    | 43F0 | 1    | 46E9 | 1    | 50F3 | 0.2  |
| 36F3 | 1    | 40F1 | 1    | 43F1 | 1    | 46F0 | 1    | 51E6 | 0    |
| 36F4 | 1    | 40F2 | 1    | 43F2 | 1    | 46F1 | 1    | 51E7 | 0    |
| 36F5 | 1    | 40F3 | 1    | 43F3 | 1    | 46F2 | 1    | 51E8 | 0.5  |
| 36F6 | 0.9  | 40F4 | 1    | 43F4 | 1    | 46F3 | 0.8  | 51E9 | 1    |
| 36F7 | 0.4  | 40F5 | 1    | 43F5 | 1    | 46F9 | 0.3  | 51F0 | 1    |
| 36F8 | 0.5  | 40F6 | 1    | 43F6 | 1    | 46G0 | 0.52 | 51F1 | 1    |
| 37E9 | 0.2  | 40F7 | 1    | 43F7 | 1    | 46G1 | 0.2  | 51F2 | 0.5  |
| 37F0 | 1    | 40F8 | 0.1  | 43F8 | 0.94 | 47E6 | 0.8  | 51F3 | 0    |
| 37F1 | 1    | 41E6 | 0.03 | 43F9 | 0.41 | 47E7 | 0.6  | 52E6 | 0    |
| 37F2 | 1    | 41E7 | 0.8  | 43G0 | 0.21 | 47E8 | 1    | 52E7 | 0    |
| 37F3 | 1    | 41E8 | 1    | 43G1 | 0.7  | 47E9 | 1    | 52E8 | 0    |
| 37F4 | 1    | 41E9 | 1    | 43G2 | 0.3  | 47F0 | 1    | 52E9 | 0.1  |
| 37F5 | 1    | 41F0 | 1    | 44E6 | 0.5  | 47F1 | 1    | 52F0 | 0.2  |
| 37F6 | 1    | 41F1 | 1    | 44E7 | 0.5  | 47F2 | 1    | 52F1 | 0.5  |
| 37F7 | 1    | 41F2 | 1    | 44E8 | 0.9  | 47F3 | 0.6  | 52F2 | 0.1  |
| 37F8 | 0.8  | 41F3 | 1    | 44E9 | 1    | 47F9 | 0.01 |      |      |
| 38E8 | 0.2  | 41F4 | 1    | 44F0 | 1    | 47G0 | 0.3  |      |      |
| 38E9 | 0.9  | 41F5 | 1    | 44F1 | 1    | 47G1 | 0.02 |      |      |
| 52F3 | 0    | 41F6 | 1    | 44F2 | 1    | 48E6 | 1    |      |      |

# D    Imputation for missing age samples

Catches of the target species are sampled (or subsampled with a size of 100 if the catches are too large) for length, and otoliths are typically collected from a subsample of the individuals sampled for length in the RFA, or per trawl haul as in the case of Norway for determining age of the fish (see Table **??**). In the case of

Norway where all trawl hauls are sampled for otoliths, missing age samples would still occur for the following two reasons: 1) the fish is below minimum length for otolith sampling (unreadable otoliths) or 2) otoliths are misplaced. Abundance indices by age group are estimated based on three age-length-keys (ALK): 1) DATRAS ALK estimator, 2) Haul dependent ALK estimator, and 3) Spatial model-based ALK estimator.

## D.1 DATRAS ALK Borrowing Approach

The ALK proposed in DATRAS (ICES 2013), which is an aggregation of individual samples from a haul combined over a round fish area (RFA), and missing age samples are imputed as follows:

1. If there is no ALK for a length in the CPUE dataframe, age information is obtained accordingly

   - If length class (CPUE) < minimum length class (ALK), then age=1 for the first quarter and age=0 for all other quarters

   - If minimum length class (ALK) < length class (CPUE) < maximum length (ALK) then age is set to the nearest ALK. If the ALK file contains values at equal distance, a mean is taken from both values.

2. If length class (CPUE) > maximum length (ALK) age is set to the plus group.

The underlying assumption of this ALK approach is that age-length compositions are homogeneous within the superstrata.

## D.2 Haul-based ALK Borrowing Approach

The second is an a haul dependent ALK estimator which we propose, and is denoted by $\text{ALK}^H$. Since the age-length composition of fish may be space-variant, that is, there may be variation in age-length compositions between trawl stations within a superstrata, the spatial dependence of the age-length composition must be accounted for to produce reliable estimates of the CPUE per age estimates. If this spatial dependence is ignored not only will estimates of abundance be biased but the impact on the variance may be substantial. So for each trawl haul an $\text{ALK}^H$ is produced. Since there are few or none observations of ages for each length class in a trawl haul, length classes are therefore pooled in increasing order such that there are five length

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classes in each pooled length group. To replace missing values for the age distribution in the pooled length groups the method of "borrowing" ages from length groups in trawl hauls closest in air distance within the RFA is used. If there are no observed ages in the pooled length group in the RFA, missing values for the age distribution are replaced following the procedure outlined in the DATRAS ALK procedure (D.1) in step 1.