An analysis of the North Sea International Bottom Trawl Survey Data

Abstract

In this research we present estimation procedures for calculating abundance at age indices, and investigate the sensitivity of these of the resulting estimates with respect to the number of otholits collected at sea. The procedures presented are applied to the North Sea International Bottom Trawls Survey data for cod (*Gadus morhua*) and saithe (*Pollachius virens*). We demonstrate how much information would be lost if the survey design was defined such that fewer otholits were collected. Age length keys (ALKs) are used to map lengths to age, and we use ALKs with and without the assumption of constant age length structures over relatively large areas. All abundance at age indices are presented with variance estimates.

1 Introduction

Fish stock assessments are used by fishery managers for making management decisions regarding catch quotas. The assessments provide fundamental information about the status of the stock, for instance, whether the stock is increasing and support for increased levels of harvest should be given, or whether the stock is decreasing and stricter control on harvest should be implemented. Associated with the parameters used in fish stock assessment is their uncertainty, which should not be ignored when formulating management policies (Walters and Ludwig, 1981; Ludwig and Walters, 1981; Berg et al., 2014). This uncertainty can arise from many sources including natural variability, estimation procedures and lack of knowledge regarding the parameter (Ehrhardt and Legault, 1997). The North Sea International Bottom Trawl Survey (IBTS) data, coordinated by the International Council for the Exploration of the Sea (ICES), provides information on seasonal distribution of stocks and estimates of abundance indices and catch in numbers of fish per age-class without an assessment of the accuracy of these estimates. As stated by Ludwig and Walters (1981) it is relevant for managers to take into account the uncertainty related to stock size when making management polices. The indices of abundance at age from IBTS are based on data obtained from a stratified semi-random sampling approach of trawl stations, and it is essential to account for the sampling approach so as to produce reliable variance estimates (Lehtonen and Pahkinen, 2004). If the sampling approach is ignored, the effect on the variance of the parameters could be substantial. In particular, the variance could be greatly inflated due to the clustering effect, which involves intra-cluster correlation of the variables (Aanes and Vølstad, 2015; Lehtonen and Pahkinen, 2004).

There are two separate stages for generating abundance indices per age from the North Sea International Bottom Trawl Survey (IBTS) data. The first consist of calculating indices per *length* class, which are obtained by trawling in a stratified manner, sorting the catch by taxa and take biological measurement of the sorted catch. Then that knowledge is transformed to indices with respect to age. The latter part is achieved with an age-length key (ALK), which is constructed by sampling pairs of otoliths (each fish has a pair of otoliths) in a stratified procedure from each haul and/or sub-area. To our best knowledge, there has been no research on how much the uncertainty of the abundance indices is related to these two distinct parts. The main contribution of this research is to shed light on how the indices estimates and their associated uncertainty estimates change if less effort was spent on collection of otoliths. We achieve the reduction of otoliths by mimicking a defined sampling procedure with less effort. We also focus on the spatial distribution of the ALK, and such spatial structures in the ALK has also been investigated in Berg and Kristensen (2012) and Hirst et al. (2012).

Currently, abundance indices from IBTS are reported in DATRAS (ICES, 2018c) using an age-length key (ALK) (Fridriksson, 1934) which is assumed to be constant over relatively large areas. In this research we propose two ALKs which accounts for spatial variation: i) a nonparametric haul based ALK, and ii) a spatial model based ALK. These ALKs are described in Section 2. A spatial model based ALK (Berg and Kristensen, 2012; Berg et al., 2014) known as the NS-IBTS Delta-GAM index (ICES, 2016b) is currently being used to calculate standardized age-based survey indices used in assessment for the North Sea stock (haddock and cod). And, as far as we are aware the variance estimates of parameters estimated from NS-IBTS Delta-GAM index are *only* utilized for assessment of Herring (*Clupea harengus*) in the North Sea.

The spatial ALK model introduced in Berg and Kristensen (2012) is similar to the model used in this paper; the main difference is that we include the spatial structure through a spatial random field (Lindgren et al., 2011) and not through two dimensional splines (Wood, 2017).

An overview of the North Sea International Bottom Trawl Survey is given in Section 1.1. The current estimators for ALK and catch per unit effort (CPUE) used by ICES in their database for trawl surveys (DATRAS) and our proposed ALK estimators are given in Section 2. We apply these ALK methods to two case studies in Section 3, and a discussion is given in Section 4. R-code for reproducing the results can be fund at github (https://github.com/natoyaj/TestPackage.git).

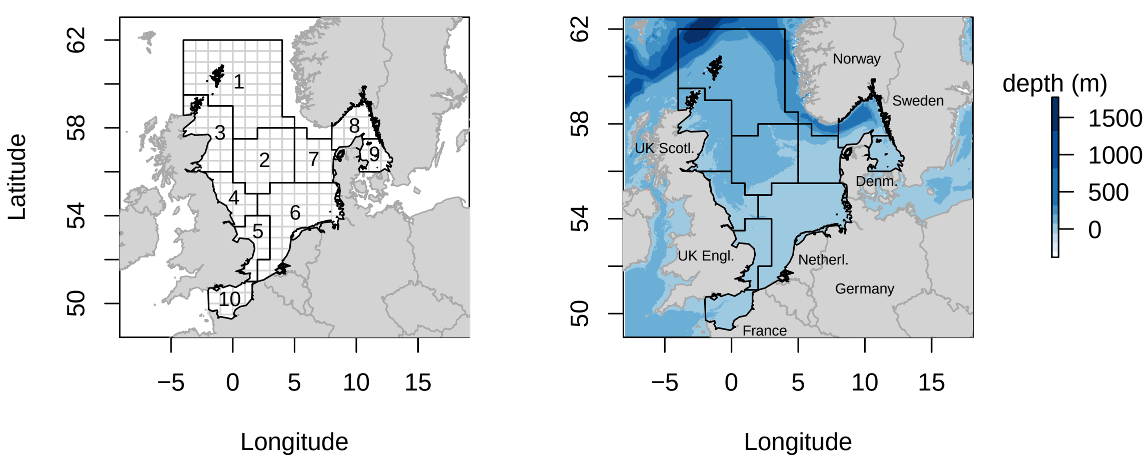
1.1 Overview of the North Sea International Bottom Trawl Survey

The North Sea International Bottom Trawl Survey was formed in 1991, to combine the International Young Herring Survey (IYHS) and eight national surveys in the North Sea, Skagerrak and Kattegat areas. These surveys began in the 1960's, and the 1970's and 1980's, respectively. The IYHS was developed with the aim of obtaining annual recruitment indices for the combined North Sea herring (*Clupea harengus*) stock (ICES, 2012), but yielded valuable information on other fish species such as cod (*Gadus morhua*) and haddock (*Melanogrammus aeglefinus*).

The North Sea IBTS began with quarterly surveys providing information on seasonal distribution of stocks sampled, hydrography and the environment, which allows changes in fish stock to be monitored and abundance of all fish species to be determined. These quarterly surveys, however became difficult to sustain as countries experienced budget cuts making it impossible to maintain high levels of research vessel effort. As such, in 1997 countries carried out a survey only twice a year; a first quarter survey (January-February) and a third quarter survey (July-September). The target species of IBTS fished from 1991-2018 includes standard pelagic species: Herring (*Clupea harengus*), Sprat (*Sprattus sprattus*) and Mackerel (*Scomber scombrus*); and standard roundfish species: Cod (*Gadus morhua*), Haddock (*Melanogrammus aeglefinus*), Saithe (*Pollachius* *virens*), Norway Pout (*Trisopterus esmarkii*) and Whiting (*Merlangius merlangus*). There are also several by-catch species (see for example, ICES, 2006)

Research vessels from seven nations in the first quarter (Q1) and six nations in the third quarter (Q3) are used for conducting surveys on all finfish species in the North Sea during January-February and July-August, respectively, between 1997-2018 (Table S1.1 in Supplementary Materials S1 gives details of the research vessels). The sampling frame is defined by the ICES index or roundfish areas (RFA) as shown in Figure 1 numbered 1 to 10. These roundfish areas were substratified into small strata defined by non-overlapping statistical rectangles of roughly 30×30 nautical miles (1^o Longitude $\times$ 0.5^o Latitude), and were convenient to use for IBTS as they were already being used for fisheries management purposes. Most statistical rectangles contain a number of possible tows that are deemed free of obstructions (found in databases of national safe tows or DATRAS or commercial fishing data), and vessels are free to choose any position in the rectangles as long as the hauls are separated by at least 10 nautical miles within and between rectangles (ICES, 2018b). However, all countries select tows based on a semi-random approach from datababes of national safe tows or DATRAS or commercial fishing data, except Sweden who uses fixed stations and in some cases depth-stratified semi-random sampling design (ICES, 2018b); and England who also uses fixed stations and only conduct surveys during the third quarter. In some rectangles, sampling may be further stratified due to significant changes in seabed depth which may, in turn, cause variations in the fish population. In particular, the North Sea IBTS herring, saithe and sprat data are weighted by depth strata in the statistical rectangle (see Table S3.1 in Supplementary Materials S3). But this weighting is not included in the current estimation procedure in DATRAS. It is also a requirement that countries avoid clustering their stations between adjacent rectangles in order to reduce positive serial correlation, and thereby maximize survey precision. The latest major reallocation of rectangles occurred in 1991, but since then the survey has tried to keep at least one vessel in every subarea in which it had fished in the most recent years. Minor reallocation of rectangles between Norway, Scotland and Germany was done in 2013. Each rectangle was typically sampled twice by two different countries before 1997, but after that target coverage of two trawl hauls per rectangle per survey was introduced because of national financial constraints (ICES, 2015). But in some rectangles in the Eastern English Channel, Southern North Sea and Central North Sea intensified sampling is carried out.

The recommended standard trawling gear of the North Sea IBTS is the mulitpurpose chalut à Grande Ouverture Verticale (GOV) trawl (ICES, 2012), which has been used on all participating vessels since 1992, while different pelagic and bottom trawls suitable for fishing finfish species were used before 1992. Standardized trawling protocols were adopted with a towing speed of 4 knots but depending on vessel performance, tide and weather conditions the average towing speed can be at minimum 3.5 and maximum 4.5 knots. From 2000-2018 trawling is done during the daylight hours, which are considered 15 minutes before sunrise to 15 minutes after sunset (ICES, 2012). After each trawl the total catch of the different species is weighed on board and biological parameters such as length for all fish species caught (to 0.1 cm below for shellfish, to 0.5 cm below for herring and sprat and to 1 cm below for all other species) are collected. Where the numbers of individuals are too large for all of them to be measured to obtain the length distribution, a representative subsample of 100 fish is selected. A pair of otoliths are collected on board from a small fraction of all the target species from all RFAs (Figure 1) to retrieve age reading. Table S2.1 in Supplementary Materials S2 gives the minimum sampling levels of otoliths for the target species.



(a)

Figure 1: Standard roundfish areas (RFAs) used for roundfish since 1980 and for all standard species since 1991 (left panel). RFA 10 was added in 2009. The number 1, for example, indicates ICES RFA 1. The small grey rectangles in the left panel indicates the statistical rectangles of approximately 30 × 30 nautical miles (these vary from 28 nm wide in the north, to 40 nm wide in the south of North sea) (1^o Longitude $\times$ 0.5^o Latitude). The map in the right panel shows the Norwegian trench and shelf edge (depths 1000-1500).

2 METHODS

This section gives the estimators of abundance indices. The estimators are haul-duration based and utilizes an ALK approach. We consider the ALK approach used in DATRAS and we propose two ALK estimators. The ALK used in DATRAS for computing abundance indices does not account explicitly for the spatial distribution in age-length structures over large areas. As differences in age-length structures may exist over large areas, these differences do have the potential to result in a biased ALK (Gerritsen et al., 2006; Kimura, 1977). These differences may be caused either by variation in length-at-age distributions or by variations in the relative abundance of age classes, that is age-at-length distributions (Gerritsen et al., 2006). To account for the spatial distribution we propose a design-based ALK estimator that is haul dependent (Section 2.2.2) and a model based ALK estimator (2.2.3).

2.1 Catch per unit effort

In this research, the catch per unit effort (CPUE) is defined as the number of fish of a certain species and age or length which are caught per hour trawl. In this section we define the CPUE mathematically, which explains how the index is calculated. For a given species of interest, let $n_{h,l}$ be the number of fish with length l caught by trawl haul h. The CPUE for a given length l by trawl haul h is defined as

$$\mathrm{CPUE}_{h,l} = \frac{n_{h,l}}{d_h}, \tag{2.1}$$

were d_h is the duration of the trawl in hours. The CPUE per age class is further defined as

$$\mathrm{CPUE}_{h,a} = \sum_{l \in \mathbf{L}} \mathrm{CPUE}_{h,l} \times ALK_{a,l,h}, \tag{2.2}$$

where $\mathbf{L}$ is the set of all length classes and $ALK_{a,l,h}$ is the age length key, which represents the estimated proportion of fish with age a in lth length class in haul h. For a given number of trawl hauls in a statistical rectangle, the mean CPUE defined as mCPUE in a statistical rectangle can be expressed as the average CPUE of the trawl hauls in the statistical rectangle:

$$\mathrm{mCPUE}_{s,a} = \frac{\sum_{h \in H_s} \mathrm{CPUE}_{h,a}}{|H_s|}. \tag{2.3}$$

Here H_s represents the set of trawl hauls taken in statistical rectangle s, and $|H_s|$ is the number of hauls taken in the rectangle. The mCPUE in pth RFA is further defined as

$$\text{mCPUE}_{p,a} = \frac{\sum_{s \in S_p} \text{mCPUE}_{s,a}}{|S_p|} \omega_s, \tag{2.4}$$

where S_p is the set of all statistical rectangles in RFA p, $|S_p|$ is the number of statistical rectangles in RFA p, and ω_s is a weight factor for each statistical rectangle (see Table S3.1 in Supplementary Materials S3). For species such as saithe, herring, and sprat the indices at age are calculated using the mean over rectangles, weighted for the percentage of area with water depths between 10m-200m, and for RFAs 8 and 9 water depths between 10m-250m (ICES, 2013a).

The mean catch per unit at age in the whole study area is defined as

$$\text{mCPUE}_a = \frac{\sum_{p \in \mathbf{P}} A_p \text{mCPUE}_{p,a}}{A_{\text{total}}}. \tag{2.5}$$

We refer to (2.5) as the index of abundance at age, where $\mathbf{P}$ is the set of RFAs, A_p is the area of RFA p, and $A_{\text{total}} = \sum_{p \in \mathbf{P}} A_p$.

2.2 ALK estimators

The definition of the CPUE of age includes an ALK, see (2.2), which we described in this section. Three ALK estimators are included in this research, which are named as follows: *i*) DATRAS ALK, *ii*) haul based ALK and *iii*) model based ALK.

2.2.1 Area based ALK

We refer to the ALK used in DATRAS to estimate abundance at age for the IBTS data as an area based ALK, defined as $ALK^{\text{A}}_{a,l,h}$. The area based ALK is defined as constant within each RFA, and is calculated for each RFA by aggregating the age observation from each RFA. $ALK^{\text{A}}_{a,l,h}$ used in equation (2.2) is defined as the proportion of observed fish with age a in length class l in the RFA h. If there are no observed fish in length class l in the RFA, ages from length classes close to l is used. The details of the procedure for borrowing age data from neighbouring length classes are given in Supplementary Materials S4.1. We want to highlight that missing ages occur seldom, in e.g. quarter 1 year 2018, 99.1% of the cod had an observed age in the corresponding RFA within the same cm group. The underlying assumption of this ALK is that age-length compositions are homogeneous within the RFAs. This is a rather strong assumption, and any violation would have an unknown impact on the estimates of abundance indices. Aanes and Vølstad (2015) illustrated that violation of the assumption of constant ALK leads to biased estimates of CPUEs.

2.2.2 Haul based ALK

We define a haul dependent ALK by ALK^H. The $ALK^H_{a,l,h}$ used in equation (2.2) is defined as the average proportion of observed fish with age a in length class l in haul h. If there are no observed ages of fish in a length class l in the haul, ages from the same length class in the haul close by is used (see Supplementary Materials S4.2 for the procedure). We want to highlight that missing ages occur seldom, in e.g. quarter 1 year 2018, 98.6% of the cod had an observed age in the corresponding haul within the same cm group.

2.2.3 Model based ALK

In this section we introduce a spatial model based ALK, which we define as $\mathrm{ALK}^{\mathrm{M}}$. Using such a model enables us to obtain smooth structures in the distribution of age given length. It further enables us to utilize spatial latent effects. Spatial model based approach of age-lengths are widely used (Berg and Kristensen, 2012; Hirst et al., 2012; Rindorf and Lewy, 2001), and are used for stock assessment in the North Sea (Berg et al., 2014).

Let the response variable of the age group of a fish be $a = M, ..., A$ where M is the youngest age, and A is the oldest age which is typically defined as a "plus group". Suppose $y(l, \mathbf{s})$ is the age of a fish with length l caught at location $\mathbf{s}$. As in Berg and Kristensen (2012) we use a continuous ratio model for the spatial age given length model. However, in our application we assume for each species we know a length l^* such that all fish above length l^* are above age M, and all fish with length below l^* are of age below A. By including such a variable we reduce the number of parameters in the model by removing one linear predictor. Define the continuous ratio we are modelling as

$$\pi_a[y(l, \mathbf{s})] = \frac{p_a(l, \mathbf{s})}{p_a(l, \mathbf{s}) + \cdots + p_A(l, \mathbf{s}) + p_M(l, \mathbf{s})} \quad \text{for } a = M+1, ..., A-1, \tag{2.6}$$

where $p_a(l, s)$ is the probability of a fish with length l at location $\mathbf{s}$ to be of age a. Note that either $p_A(l, \mathbf{s})$

or $p_M(l, \mathbf{s})$ is known to be equal to zero, and the other is selected such that $\sum_a p_a = 1$. We assume the logit link

$$\log\left[\frac{\pi_a[y(l,\mathbf{s})]}{1-\pi_a[y(l,\mathbf{s})]}\right] = f_a(l) + \gamma_a(\mathbf{s}), \tag{2.7}$$

where $f_a(l)$ is a continuous function of length and $\boldsymbol{\gamma}$ is a mean zero Gaussian spatial random field with Matérn covariance function (Stein, 2012). The spline $f_a(l)$ is intended to account for the fact that longer fish are typically older, and the spatial random field, $\boldsymbol{\gamma}$, is intended to account for spatial variation in the ALK. The continuous function $f_a(l)$ in (2.7) is modelled with usage of P-splines (Wood, 2017), and these spline regression coefficients are included as a mean zero Gaussian random effect. The precision matrix for the spline regression coefficients is constructed such that wiggliness is penalized, see Wood (2017, page 239) for details. The R package mgcv (Wood, 2015) is used for extracting the precision matrix needed for the spline regression coefficients. The marginal variance of the P-splines regression coefficients, σ_f^2, is estimated in our inference procedure.

We assume that the spatially Gaussian random field in (2.7), $\boldsymbol{\gamma}$, follows a stationary Matérn covariance structure defined as

$$\text{Cov}(\gamma(\mathbf{s}_1), \gamma(\mathbf{s}_2)) = \frac{\sigma_\gamma^2}{2^{\nu-1}\Gamma(\nu)}(\kappa||\mathbf{s}_1 - \mathbf{s}_2||)^\nu K_\nu(\kappa||\mathbf{s}_1 - \mathbf{s}_2||), \tag{2.8}$$

where σ_γ^2 is the marginal variance of the spatial field; $||\mathbf{s}_1 - \mathbf{s}_2||$ is the distance between $\mathbf{s}_1$ and $\mathbf{s}_2$ in kilometres; κ is a spatial scale parameter of the spatial field; ν is a smoothing parameter and $K_\nu(\cdot)$ is the modified Bessel function of the second kind with $\nu = 1$. The spatial field is estimated with the stochastic partial differential equation (SPDE) procedure described in Lindgren et al. (2011). The main concept behind the SPDE procedure is that the precision matrix of a spatial field with Matérn covariance function can be approximated by a sparse matrix on a grid covering the area of interest. Such a grid and sparse precision matrix are constructed with use of the R-INLA package (Rue et al., 2009). Figure 2 gives an illustration of the mesh used for approximating (2.8) for one of our focal species (cod), which we describe in Section 3. Detail regarding the construction of the mesh can be found at github (https://github.com/OlavNikolaiBreivik/IBTSspatialALK).

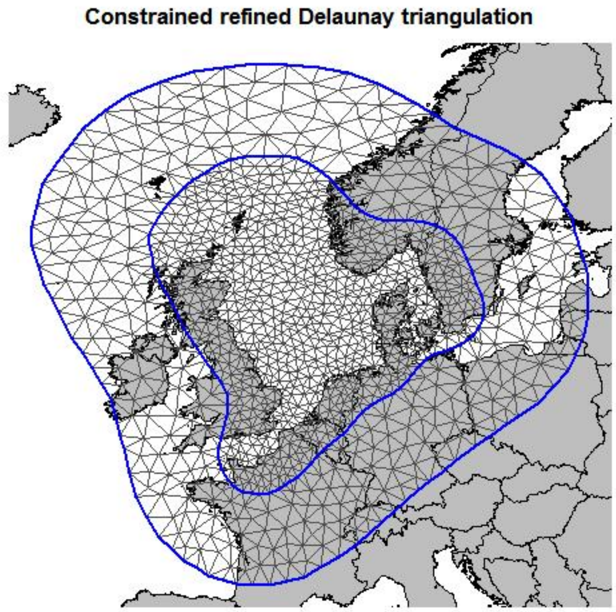


Figure 2: Mesh used in the case study for cod in Section 3 for approximating (2.8) with the SPDE-procedure. The species specific constant l^* is selected as the mid point between the shortest fish of age A and the longest fish of age M in the corresponding year and quarter. A sensitivity analysis of this constant were performed by adjusting it up and down 5 cm for cod in year 2018 in Q1. The point estimate of the mCPUE_a then changed in the forth decimal, which we will consider negligible.

The model based ALK estimate is obtained by maximizing the likelihood. We maximize the likelihood with use of an R-Package called Template Model Building `TMB` (Kristensen et al., 2015), combined with the optimizing function `nlminb` in R. In this application `TMB` is advantageous as it uses Laplace approximation for the latent fields gaining computational efficiency, it also utilizes sparse structures in the latent fields, and uses automatic derivation.

2.3 Uncertainty estimation

In this section we describe how the uncertainty of the CPUE estimates are calculated. We use nonparametric bootstrapping to quantify the uncertainty of the CPUEs. In nonparametric bootstrapping independent samples of lengths and age are drawn with replacement from the original data and approximate 95% confidence intervals are obtained using bias-corrected percentile method (Carpenter and Bithell, 2000). Nonparametric resampling allows us to estimate the sampling distribution of the CPUE empirically without making assumptions concerning the data. The bias-Corrected method adjusts for the bias and skew of the sampling distribution of the data (Puth et al., 2015; Karlsson, 2009). The bootstrap procedure is given in Supplementary Materials S5. (The procedure in S5 is a general description of a bootstrap procedure, this should be just included with a reference.)

A bootstrap procedure for estimating the uncertainty of CPUEs in the North Sea is suggested in ICES (2006). This procedure is given in Supplementary Materials S5 (The procedure in S5 is just a general description of a bootstrap procedure and not what is written in ICES (2006).). In the rest of this research, we refer to this procedure as DATRAS bootstrap procedure, as it is the current procedure outlined in DATRAS for uncertainty estimation of IBTS indices (The procedure for sampling CA data is the exact same, but not sampling the HL-data, we have however implemented that procedure also but i thought we agreed not to use it). However, this bootstrap procedure has never been implemented in DATRAS. The DATRAS procedure is divided into two parts; one part which samples CPUE per length (2.1), and another part which samples the ALK used in (2.2). The DATRAS bootstrap procedure is based on the assumption of homogeneous CPUE within RFAs (It assumes constant ALK in the RFA. We have also implemented the procedure from DATRAS for sampling HL-data which assumes constant CPUE in the RFA, but that procedure is not used in the manuscript). This assumption is likely to be wrong, and would typically cause an overestimation of the uncertainty. Therefore, we have included a bootstrap procedure, defined as the stratified bootstrap procedure, which instead assumes constant CPUE within each statistical rectangle.

2.3.1 Bootstrap procedures and reducing effort

In this section we describe the two bootstrap procedures used in this research. The two procedures differ by how the ages are sampled. The DATRAS and stratified bootstrap procedure are constructed as follows:

1. For each statistical rectangle, sample $|H_s|$ hauls with replacement from the corresponding statistical rectangle. If there is only one haul within a statistical rectangle, sample either that haul or the closest haul.

2. Sample age observations from the sampled hauls obtained by step 1. For the DATRAS procedure this is achieved by (a), and for the stratified procedure this is achieved by (b):

   (a) For each RFA and length group, sample with replacement $n_{l,a,RFA}$ age observations stratified with respect to RFA and length group. Here $n_{l,a,RFA}$ is the total number of age observations in length group l in the corresponding RFA. If there is only one observed age from a given length group, i.e. $n_{l,a,RFA} = 1$, we sample either that age or an age in the closest length class with observed ages within the RFA.

(b) For each *haul* and length group, sample without replacement $n_{l,a,h}$ age observations stratified with respect to *haul* and length group using a pseudo-population bootstrap procedure (Mashreghi et al., 2016) (TODO). Here $n_{l,a,h}$ is the total number of age observations in length group l in the corresponding haul. Ages are sampled with probability proportional to the number of fish in the corresponding cm group and haul. If there is only one observed age within a length group in a haul, that age is sampled.

3. Calulate mCPUE_a, see equation (2.5), with use of the sampled data.

4. Repeat 1-3 B times.

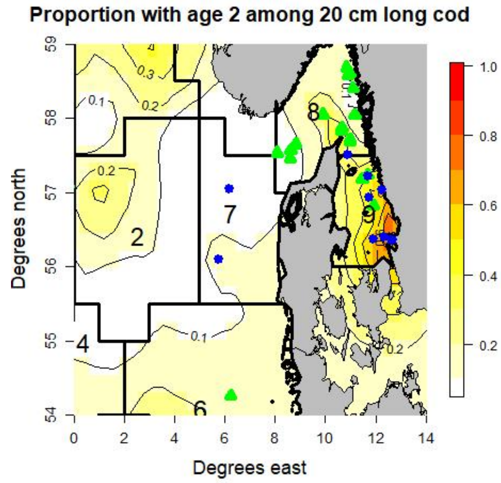
In this research we investigate how mCPUE_a is affected by reducing the number of age readings. We sample realisations of data obtained with a sampling procedure with fewer age reading by choosing $n_{l,a,h}$ in step 2b equal a pre defined number. In our case study we have chosen $n_{l,a,h}$ equal *one* or *two* when sampling the reduced effort. By doing that, the sampled data sets in the bootstrap procedure are possible realisations of data obtained by collecting only *one* or *two* otoliths per length group at sea. In our case study we have chosen the length groups to have width $1\text{cm}, 2\text{cm}, ...$ or 5cm.

3 Case studies

In this section we apply the methods described in Section 2 to data for cod and saithe from the International Bottom Trawl Survey for the years 2014-2018, which is obtained from the DATRAS database (ICES, 2018c). These years are chosen for several reasons. The first is that in year 2018 new sampling procedures proposed by ICES for the collection of otoliths were introduced in the surveys. For instance, *one* pair of otoliths per length group is sampled for most target species (see Table S2.1 in Supplementary Materials S2 for the sampling procedures for each target species), and this data is appropriate for the application of our proposed sample optimization procedure described in Section **??**. The second is that IBTS included age 0 in Q3 surveys. Also, some species such as saithe that occupies the deeper waters in the northern part of the North Sea and in the Skagerrak and Kattegat, along the shelf edge (ICES, 2018a), the IBTS Q3 data is relevant for analyses compared with data from IBTS Q1 surveys, which do not adequately cover these areas where saithe is distributed (ICES, 2016a); see Figure 1. In the third quarter of 2015, an experiment on tow duration of the North Sea IBTS hauls was conducted to investigate the effect on the composition of catches, and which continued into the first quarter of 2016 (**?**). A mix of of 15 minutes and 30-minutes hauls were used in all rectangles to which two hauls have been allocated: one 15-minutes haul and one 30-minutes haul maintaining a full North Sea-wide set of regular 30-minutes hauls in case there were significant differences in the 15-minutes haul. Four nations (Denmark, Germany, Norway and Scotland) participated in the experiment, while two nations (England and Sweden) retained haul duration for all of their hauls at 30-minutes. France conducted some additional 15-minutes hauls, paired with 30-minutes hauls during the first quarter of 2016 (**?**). These years provide extensive sample data for cod and saithe with yearly sampling effort varying between 333 and 389 trawl hauls. For each of these trawl hauls sampled in the years 2014-2018, concurrent length measurements and otoliths for age determination were obtained from a subsample of cod and saithe. The subsample of otoliths taken for age determination varied between 1600 and 2895 for cod, and between 581 and 1631 for saithe. Table S6.1 in Supplementary Materials S6 briefly describes the data for the years 2014-2018.

3.1 Estimated indices of abundance and variability for cod and saithe

In this section we apply the three ALK methods given in section 2.2 for abundance estimation, and the bias-corrected bootstrap method, given in Section 2.3.1 for estimating variability of estimated indices of abundance. In this section we apply the three ALK methods, given in section 2.2, for estimating abundance at age and the bias-corrected bootstrap method, given in Section 2.3.1, for estimating variability of estimated indices of abundance. The main assumption of the area based ALK is that the age-length compositions of species over large areas are the same. Figure 3 illustrates the predicted probability of age of cod given length using the spatial model based ALK (2.7). Figure 3 illustrates that the main assumption of the area based ALK of constant age-length compositions over large areas is not valid as a fish of length 20 cm could be of age 1 or age 2 in Skagerak area. see Figure 3. This trend can be seen over several years of IBTS time series, which further discredit the assumption of constant ALK over large areas in the North sea. Figure S2 in Supplementary Materials S7.1 illustrates that age given length of 20 cm long cod varies over large areas in years 2014-2018, while FigureS3 provides more illustrative examples of different length groups further discrediting the assumption of constant ALK over large areas in the North Sea.

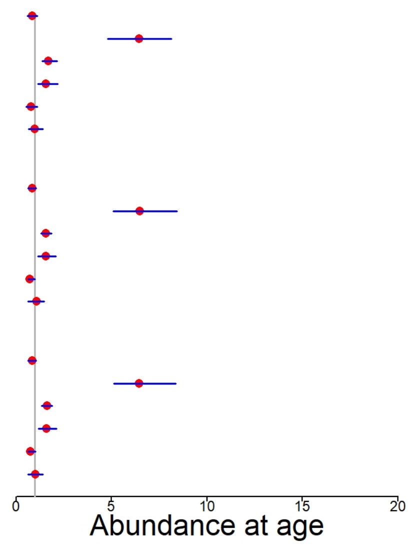


(a) (b)

Figure 3: Estimated proportion of age 1 and 2 year-old cod of length 20 cm long in Skagerak. The green triangles (▲) and blue circles (●) are observations of one and two year old cod, respectively, which are in the length interval 19 cm to 21 cm.

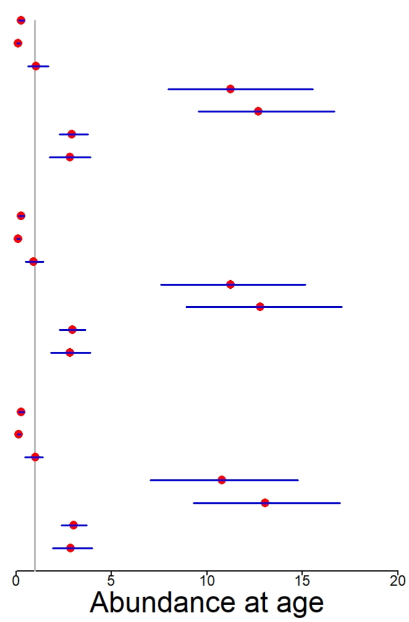
Figures 4 gives estimates of indices of abundance for cod in 2018 Q1 and for saithe in 2017 Q3. Approximate 95% confidence intervals from the bias-corrected bootstrap method for 200 bootstrap replication are estimated from the three ALK methods I think we need to run 'production' run on larger number of iterations before interpreting too much. The stratified procedure described in 2.3.1 is used in the sampling process to estimate bootstrap confidence intervals. Figures 4 shows that the resulting indices of abundance for cod and saithe turned out to be similar for all ALKs. IBTS is a complex multistage survey design, and since the ALKs are estimated from cluster-correlated data the resulting effective sample for estimating age-composition of fish would be lower than the number of fish measured (ICES, 2013b). Hence, the ALKs are subject to large sampling errors. For example, the estimated percentage relative standard errors from the spatial ALKs for the plus group (6+) for cod are $> 25\%$, suggesting high sampling error in the ALKs. (Which parameter is tested here (age, length or something else)? Could the observation also be explained by high natural variation and the collapsing of potentially hetergenous length and ages into one group? Also, it should be remembered that DATRAS ALK is constant. Aanes and Vølstad (2015) showed that in such cases, and where only the variability of length compositions are allowed for, the estimated age-distributions may appear to be more precise than they truly are since the ALK itself is subject to sampling errors, see for example the estimated relative standard standard errors for ages 2, and the older fish (4, 5 and 6+) for both species.

Age	Species	Mean	Median	SE	RSE%	Width CI-95	Estimate (CI_{95})
Area based							
1	cod	0.903	0.909	0.141	16.52	0.504	0.85 (0.60-1.10)
2	cod	6.581	6.542	0.955	14.82	3.314	6.45 (4.80-8.12)
3	cod	1.593	1.580	0.208	12.33	0.790	1.68 (1.38-2.17)
4	cod	1.437	1.376	0.290	18.48	1.013	1.57 (1.16-2.17)
5	cod	0.708	0.686	0.169	21.67	0.580	0.78 (0.52-1.10)
6+	cod	0.851	0.804	0.227	22.77	0.736	1.00 (0.67-1.41)
Haul based							
1	cod	0.914	0.917	0.120	13.90	0.409	0.86 (0.63-1.04)
2	cod	6.506	6.387	0.903	13.90	3.349	6.50 (5.09-8.44)
3	cod	1.555	1.559	0.140	8.93	0.519	1.57 (1.32-1.84)
4	cod	1.403	1.347	0.304	19.22	0.938	1.58 (1.16-2.10)
5	cod	0.649	0.642	0.113	15.27	0.377	0.74 (0.62-0.99)
6+	cod	0.807	0.776	0.290	26.97	0.820	1.07 (0.64-1.46)
Model based							
1	cod	0.907	0.904	0.116	13.40	0.420	0.87 (0.64-1.06)
2	cod	6.466	6.342	0.880	13.63	3.234	6.46 (5.12-8.36)
3	cod	1.616	1.619	0.143	8.76	0.525	1.63 (1.35-1.88)
4	cod	1.405	1.336	0.309	19.32	0.949	1.60 (1.18-2.13)
5	cod	0.658	0.652	0.114	15.13	0.400	0.75 (0.63-1.03)
6+	cod	0.782	0.738	0.275	26.87	0.770	1.02 (0.63-1.40)



(a) Cod in year 2018 Q1

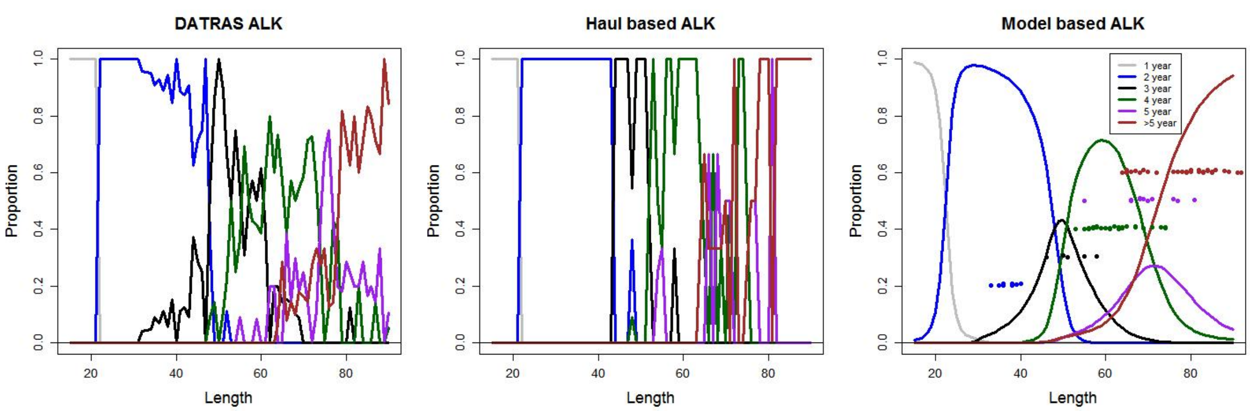
Age	Species	Mean	Median	SE	RSE%	Width CI-95	Estimate (CI_{95})
Area based							
0	saithe	0.282	0.282	0.0905	32.1	0.299	0.28 (0.13-0.43)
1	saithe	0.123	0.123	0.0500	40.3	0.175	0.12 (0.04-0.22)
2	saithe	0.968	0.965	0.2545	24.4	1.049	1.04 (0.64-1.69)
3	saithe	10.854	10.802	2.0127	17.9	7.565	11.24 (7.97-15.54)
4	saithe	12.357	12.335	1.8752	14.8	7.126	12.70 (9.55-16.67)
5	saithe	2.898	2.872	0.3684	12.7	1.496	2.91 (2.27-3.76)
6+	saithe	2.827	2.836	0.5635	19.8	2.144	2.84 (1.75-3.89)
Haul based							
0	saithe	0.278	0.280	0.0903	32.0	0.298	0.28 (0.13-0.43)
1	saithe	0.121	0.122	0.0495	40.2	0.169	0.12 (0.04-0.21)
2	saithe	0.878	0.861	0.2487	26.8	0.936	0.93 (0.51-1.45)
3	saithe	10.889	10.879	2.0360	18.1	7.585	11.24 (7.57-15.16)
4	saithe	12.531	12.476	2.1241	16.6	8.140	12.79 (8.92-17.06)
5	saithe	2.967	2.976	0.3463	11.7	1.350	2.97 (2.28-3.63)
6+	saithe	2.812	2.808	0.5532	19.6	2.071	2.82 (1.82-3.89)
Model based							
0	saithe	0.288	0.284	0.0897	31.8	0.300	0.28 (0.13-0.43)
1	saithe	0.138	0.137	0.0480	32.8	0.169	0.15 (0.07-0.24)
2	saithe	1.161	1.154	0.2554	25.1	0.949	1.02 (0.46-1.41)
3	saithe	10.686	10.621	2.0077	18.6	7.726	10.79 (7.03-14.75)
4	saithe	12.663	12.749	2.0426	15.6	7.694	13.06 (9.28-16.98)
5	saithe	2.925	2.920	0.3650	12.1	1.354	3.01 (2.36-3.72)
6+	saithe	2.672	2.680	0.5589	19.6	2.069	2.85 (1.93-3.99)



(b) Saithe in year 2017 Q3

Figure 4: Estimated confidence intervals (CI_{95}) from bias-corrected bootstrap method for cod in year 2018 Q1 and saithe in year 2017 Q3. Estimated indices of abundance (Estimate), and its standard error (SE), percentage relative standard error (RSE%), bootstrap mean (Mean) and Median estimates and the width of the confidence interval (Width CI-95) are also given.

As regards to which spatial ALK method to adopt, it is difficult to identify a method that gives the best performance over all age groups. While both methods seem to give reasonable estimates, the spatial model based ALK generally gave shorter interval widths for both species (Figure 4). Furthermore, compared with DATRAS ALK and the haul based ALK, the spatial model based ALK allows smooth functions of the spatial effects predicting numbers-at-age. Figure 5 illustrates the estimated age compositions as a function of length for a given haul in RFA 1. The haul selected is the haul with the most number of observed ages of cod in 2018 Q1. Notice that the the model based ALK is smooth, while the DATRAS ALK and the haul based ALK are not. This is an important advantage of the model based ALK, and it is surprising that it did not result in a larger difference in the estimated index of abundance as shown Figure 4. An intuitive reason for this is presumably because there are enough observed ages per length group for the haul based ALK to be representative. But, there are some limitations of the spatial model based ALK. For instance, the uncertainty of relative abundance from the spatial model based ALK is calculated using bootstrapping, as approximation of the joint distribution of the regression coefficient and spatial effect, in some cases, fails to account for the negative correlations between ages. Also, estimating relative abundance at age and its precision from the spatial ALK model can be computationally intensive.



(a) (b) (c)

Figure 5: Estimated age compositions of cod as a function of length in a given haul in RFA 1 using a) DATRAS ALK, b) haul based ALK and c) model based ALK. Note that explanation of the colours are only given in c). Each coloured point in c) defines an observed cod with the corresponding length and age in the haul. The haul selected is the haul with most observed ages of cod in 2018 Q1.

We also demonstrate the implications of using DATRAS bootstrap procedure for estimating the uncertainty around indices of abundance (see Figure S4 in Supplementary Materials S7.2). Compared with the stratified bootstrap procedure, DATRAS bootstrap procedure gives an overestimation of the uncertainty for all age groups, suggesting that it is highly relevant to account for the variation in the data over large areas.

3.2 Alternative sampling procedure for North Sea Cod and Saithe

Table 1: Comparison of estimated uncertainty from proposed sampling procedures with estimated uncertainty from original data

age	mCPUE	SE.resampled	SE	RSE.resampled	RSE
1 cm (85.9% of otoliths)					
1	0.86	0.122	0.119	14.179	13.895
2	6.50	1.002	0.902	15.426	13.897
3	1.57	0.180	0.140	11.518	8.934
4	1.58	0.294	0.304	18.611	19.223
5	0.74	0.122	0.113	16.560	15.269
6+	1.07	0.275	0.289	25.623	26.968
3 cm (62.1% of otoliths)					
1	0.86	0.133	0.119	15.478	13.895
2	6.50	1.059	0.902	16.311	13.897
3	1.57	0.192	0.140	12.279	8.934
4	1.58	0.298	0.304	18.714	19.223
5	0.74	0.132	0.113	17.767	15.269
6+	1.07	0.311	0.289	29.178	26.968
5 cm (51.0% of otoliths)					
1	0.86	0.129	0.119	15.126	13.895
2	6.50	0.995	0.902	15.338	13.897
3	1.57	0.163	0.140	10.381	8.934
4	1.58	0.320	0.304	20.095	19.223
5	0.74	0.208	0.113	27.857	15.269
6+	1.07	0.289	0.289	27.193	26.968

In this section we investigate the effect of sampling fewer otoliths on the estimated indices of abundance for the North Sea IBTS saithe and cod. **We use the spatial ALK model based approach, although the haul based could also be used (see Supplementary Materials.....)**. The removal procedure for otolith sampling described in Section **??** is applied to data in year 2018 Q1 for cod and year 2017 Q3 for saithe. We sample one pair of otoliths per length group described in Section **??**: 1 cm, 2 cm, 3 cm, 4 cm, 5 cm, 6 cm or 7 cm. Recall that prior to 2018 the standardized IBTS sampling procedure was 8 pairs of otoliths per length group but some nations such as Norway and Netherlands sampled one pair of otoliths per length group from every haul. Although the revised standardized IBTS sampling procedure is one pair of otolith per 1 cm length group for standard round fish as of year 2018 Q1, except for haddock and Norway Pout where 2 otoliths per cm is to be sampled, some nations (Sctoland and Sweden) continue to sample more than one pair of otoliths, particularly for older age groups (see Table S2.1 in Supplementary Materials S2).

Figure 6 gives the percentage relative standard error of estimated indices of abundance and mean square error for cod and saithe from the seven different sampling procedures described above. Estimates are computed from 1000 simulations and 1000 bootstrap replication A total of 1600 pairs of otoliths were sampled for cod in year 2018 Q1, while 2163 pairs of otoliths were sampled for saithe in year 2017 Q3 (see Table S6.2 in Supplementary Materials S6). The proportion of otoliths removed for cod from each of the sampling procedures stated above is: 14.4%, 28.6%, 38.4%, 44.5%, 49.3%, 52.6% or 55.6%, respectively, while for saithe the following proportions of otoliths are removed: 27.1%, 48.9%, 59.5%, 65.6%, 69.8%, 73.1% or 75.2%, respectively. Notice that 14% of the cod data in year 2018 Q1 is removed for the sampling procedure of a pair of otoliths per 1 cm length group. This should be 0% if all nations followed the revised standardized IBTS sampling procedure of year 2018 Q1.

Tables S7.2 and S7.3 in Supplementary Materials S7.3 give results of the estimated indices of abundance and approximate 95% bias-corrected boostrap confidence intervals

discuss graph

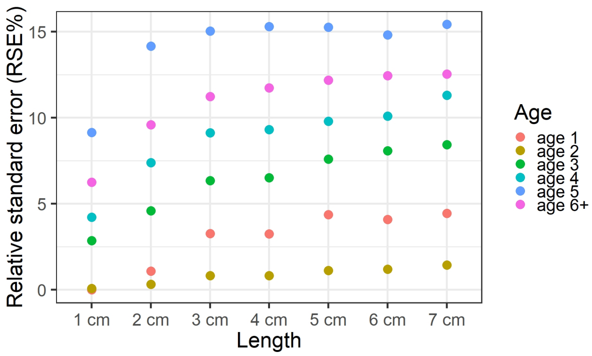
- **We discuss and include these in explanations below**
- Accuracy of estimates of reduced data compared with estimates from full data
- Precision in estimates is measured by standard error (SE) and relative standard error (RSE)
- accuracy is measured by root mean square error (RMSE) = $\sqrt{\mathrm{SE}^2 + (\mathrm{bias})^2}$. Measures how close, on average, a fitted line is to the data points (measure of goodness of fit). One can compare the RMSE to observed variation in measurements of a typical point (**the two should be similar for a reasonable fit**). Can we use this even though we do not have a "true value", which we would never know from large survey data and since we did not simulate synthetic data? Can we consider $\hat{\lambda}_a$ as a "true value"?

The nonparametric bias-corrected bootstrap method is adopted for estimating confidence intervals of indices of abundance, and although this method has the advantage of correcting for the bias and skew of the sampling distribution of the data; accounting for some of the variability in the sampling distribution of the CPUE; and does not assume any distribution for the data, there are some limitations of the bootstrap approach. The most important limitation is the assumption that the distribution of the data represented by the sample is a reasonable estimate of the population function from which the data are sampled. If this assumption is violated the random sampling performed in the bootstrap procedure may add another level of sampling error, resulting in invalid statistical estimations (Haukoos and Lewis, 2005). As discussed in Section 1.1 the selection of the trawling locations for IBTS surveys is semi-random where cruise leaders selects "clear" tow locations or "blind" tow locations if no clear tow exists by checking the proposed trawl track for hazardous seabed obstructions with acoustic methods. More recently, selection of tow locations is based on pre-proposed valid tow locations with start and end positions executed in the period 2000-2018. Hence, the lack of a fully randomized sampling process has the potential to result in biased estimates of parameters and their uncertainty. Additionally, prior to 2013, all nations were sampling 8 pairs of otoliths per 1 cm length group for our focal species (Table S2.1 in Supplementary Materials S2), and these samples could be acquired from, for example the first haul (or first few trawl hauls), resulting in an unrepresentative sample of the population. From 2013, some nations adopted the current sampling procedure outlined by ICES for IBTS 2018 surveys of 1 pair of otolith per 1 cm length group from each haul, while other nations continued with sampling 8 pairs of otoliths per 1 cm length group. So, bias was still introduced via the sampling procedure. Another limitation of the bootstrap is the smaller the original sample the less likely it is to represent the entire population, thus the more difficult it becomes to compute valid confidence intervals. Note that the bootstrap relies heavily on the tails of the estimated sampling distribution when computing

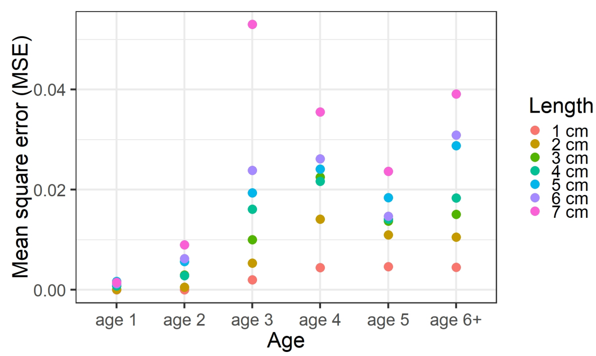
these results in the graph are from the haul based ALK procedure. The model based ALK procedure gave an error, when it's working those will be here and haul based will go in supplementary materials

4 DISCUSSION

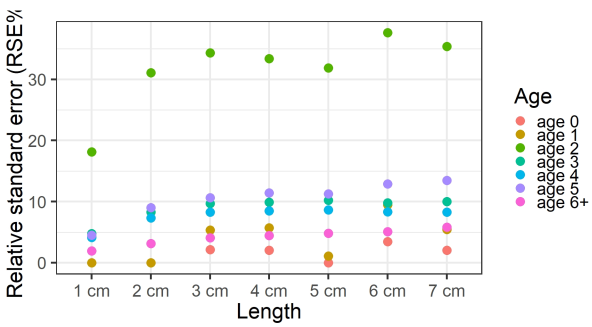
In this research we have determined optimal sampling efforts of otoliths for target species of the North Sea International Bottom Trawl Survey (IBTS). This was achieved by testing different sampling procedures that mimic the real data collection procedure but with a reduced number of otoliths. The estimated indices of



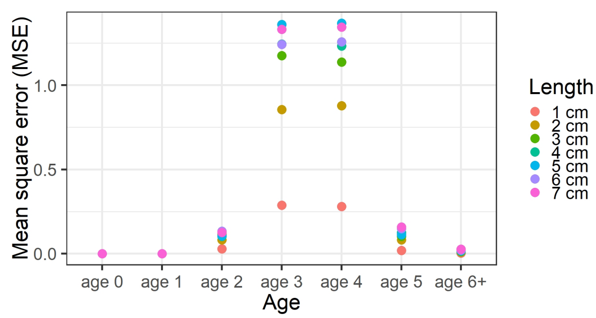
(a) Percentage relative standard error (RSE%) for cod



(b) Mean square error (MSE) for cod



(c) Percentage relative standard error (RSE%) for saithe



(d) Mean square error (MSE) for saithe

Figure 6: Percentage relative standard error (RSE%) and mean square errror (MSE) for age given seven length group sampling procedures of otolith collection for cod in year 2018 Q1 and saithe in year 2017 Q3.

abundance and their estimated uncertainty were investigated to determine if there is any real change in the precision of the estimates. Abundance indices were estimated using age-length keys (ALKs). The database for trawl surveys (DATRAS) manned by ICES includes an ALK that uses the raw proportions of age given length assuming constant age-length compositions over relatively large areas. We have developed two spatial ALK methods to estimate abundance indices and their variance that accounts for spatial variation in the data: 1) a haul based ALK that produces an ALK for each trawl haul, and which uses the raw proportions of age given length, and 2) a spatial ALK model that uses logits for modelling the age distribution in catch data from the length-stratified subsamples. Several studies have used spatial ALK modelling for estimating abundance indices of the North Sea stocks used in assessments (Berg and Kristensen, 2012; Berg et al., 2014; Gerritsen et al., 2006). These studies used continuous ratio logits with General Linear Model (GLM) or General Additive Models (GAMs) to model the spatial effects and found large spatio-temporal variability of the ALK and relative abundance at age. We proposed to use Gaussian Random Field Theory to model the spatial effects as a smooth surface to estimate age-at-length and relative abundance for the IBTS data. The spatial model based ALK and the design based spatial ALK (haul based) gave similar estimates as DATRAS estimator for relative abundance at age but the spatial ALK estimators gained better precision.

The spatial ALK model based estimator appears to be a useful tool to detect significant differences between ALKs over large areas, although estimation of the uncertainty in the ALK from the joint precision matrix is problematic. Including the uncertainty of the ALK in the model requires an approximation of the joint distribution of the regression coefficient and the spatial effect, but this approximation is only as good as the quality of the data in a given year and quarter. For instance, the approximation of the ALK can predict juvenile ages given longer lengths, which goes against the natural biology. This occurs presumably because the approximation fails to account for the negative correlation structures between ages. So the uncertainty in the relative abundance was, therefore, calculated using bootstrapping as done by Berg and Kristensen (2012); Berg et al. (2014). In future, the model might be expanded to include the probability of recording inaccurate age-at-length data, so that uncertainty in the ALK could be estimated using the joint precision matrix. The model might also be expanded to include covariates such as trawl hauls to capture any haul variation, for example a trawl haul may "hit" a school of fish of a certain age.

With regards to how many otoliths to sample per length group, the evidence is clear that .....

discuss DATRAS and Haul based ALK and recommended optimum sampling level of otoliths per length group

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Supplemental Materials: Optimizing sampling effort of the North Sea International Bottom Trawl Survey.

S1 Areas fished by different countries in the North Sea IBTS

Typically, two different countries fish each rectangle so that at least two trawl hauls are made per rectangle, but intensified sampling is carried out in the following areas: at least 3 hauls per rectangle are taken in statistical rectangles 31F1, 31F2, 32F1, 33F4, 34F2, 34F3, 34F4, 35F3, 35F4; while six or more hauls per rectangle are taken in statistical rectangles 30F1, 32F2, 32F3, 33F2, 33F3 (ICES 1999). The Skagerrak and Kattegat is fished solely by Sweden, who sample more than once in every rectangle while the west of Shetland (in Q1 and Q3) and inshore areas (Q3) is fished solely by Scotland. The edge of the Norwegian Trench is fished solely by Norway, but inshore areas near Denmark is fished by Denmark. The southern North Sea is fished by Denmark, Germany and England. France, typically, is the only country that surveys the western English Channel. Areas are surveyed by a single country because of the large proportion of untrawalable area (and subsequent gear damage issues experienced by other nations) for efficient logistical purposes. Table S1.1 gives the countries and research vessels participating the North Sea IBTS.

Table S1.1: Survey countries, vessel name, and period research vessels participating in first quarter (Q1) and third quarter (Q3) during 1997-2017.

	First Quarter (Q1)		**Third Quarter (Q3)**	
Country	Vessel name	Period	Vessel name	Period
Denmark	Dana	January-February	Dana	July-August
France	Thalassa II	January-February	-	-
Germany	Walther Herwig III	January-February	Walther Herwig III	July-August
Netherlands	Tridens 2	January-February	-	-
Norway	G.O. Sars	January-February	Johan Hjort	July
UK England	-	-	Endeavour	August-September
UK Scotland	Scotia III	January-February	Scotia III	July-August
Sweden	Dana	January-February	Dana	August

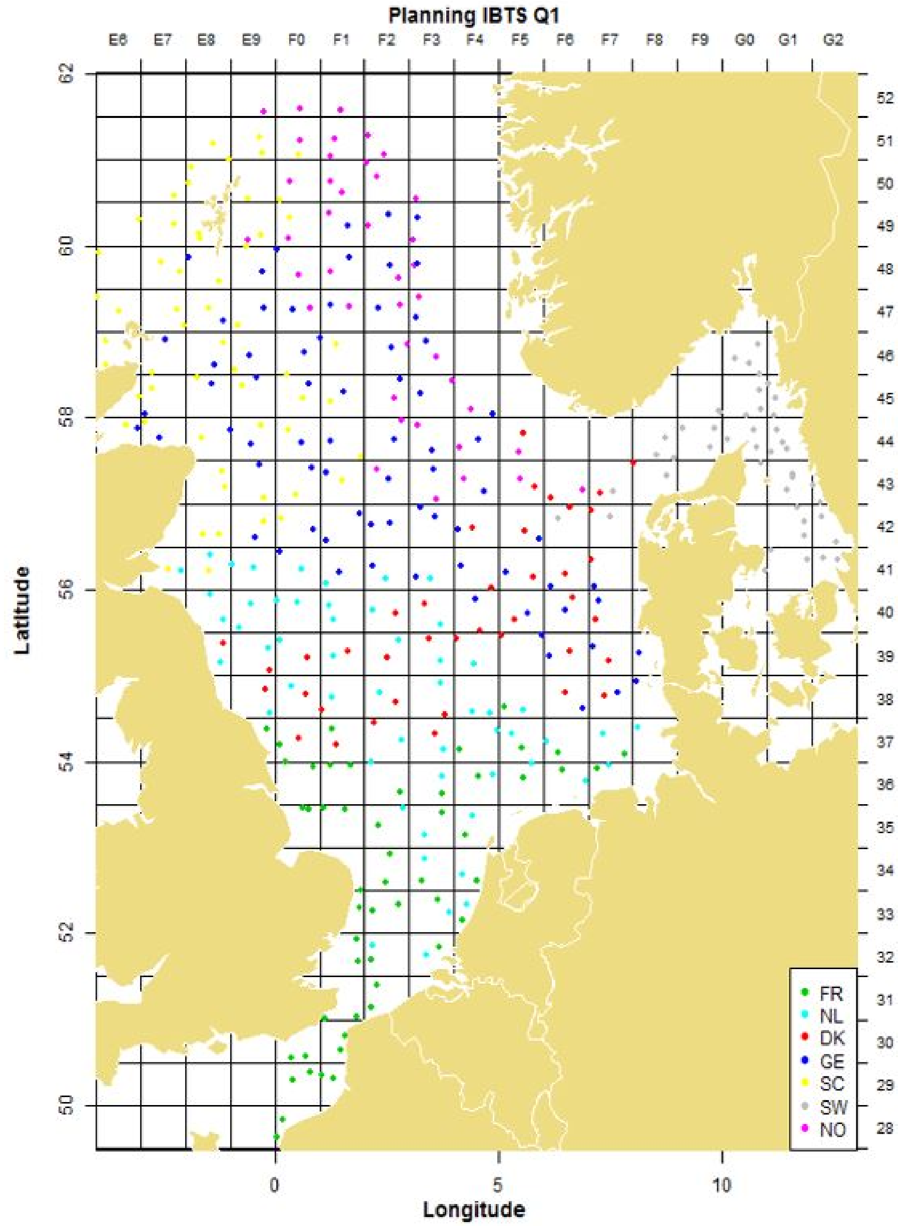


Figure S1: North Sea IBTS 2018 sampling program for nations. Seven nations carry out sampling: France (FR), Netherlands (NL), Denmark (DN), Germany (GE), Scotland (SC), Sweden (SW) and Norway (NO).

S2 Otolith sampling per fish species

From 1991-2017, most countries conducted quota sampling of otoliths per length group in a RFA. But from 2013 Norway has been sampling one otolith per length class from each trawl haul (to 0.1cm below for shellfish, to 0.5cm below for herring and sprat and to 1cm below for all other species). From the first quarter in 2018 all countries are required to sample one otolith per length class per trawl haul. Table S2.1 gives the minimum sampling levels of otoliths for the target species. However, for the smallest size groups, that presumably contain only one age group, the number of otoliths per length class may be reduced, and more otoliths per length are required for the larger length classes.

Table S2.1: Minimum sampling levels of otoliths by species for RFA or per trawl haul.

Period	Species	Minimum sampling levels of otoliths per length class
1991-2017		**Number of otoliths per length class in a RFA**
	herring	8 otoliths per $\frac{1}{2}$ cm group
	sprat	16 otoliths per $\frac{1}{2}$ cm length class $8.0 - 11.0$ cm
		12 otoliths per $\frac{1}{2}$ cm length class ≥ 11.0 cm
	mackerel	8 otoliths per $\frac{1}{2}$ cm length class
	cod	8 otoliths per 1 cm length class
	haddock	8 otoliths per 1 cm length class
	whiting	8 otoliths per 1 cm length class
	Norway pout	8 otoliths per 1 cm length class
	saithe	8 otoliths per 1 cm length class
	All target species	From 2013 Norway and Scotland, and Netherlands from 2016 have been sampling 1 otolith per length class from each trawl haul (to 0.1cm below for shellfish, to 0.5cm below for herring and sprat, and to 1cm below for all other species).
2018		**Number of otoliths per length class per trawl haul**
	herring	1 otolith per $\frac{1}{2}$ cm group
	sprat	1 otolith per $\frac{1}{2}$ cm length class $8.0 - 11.0$ cm
		1 otolith per $\frac{1}{2}$ cm length class ≥ 11.0 cm
	mackerel	1 otolith per 1 cm length class
	cod	1 otolith per 1 cm length class
	haddock	2 otoliths per 5 cm length class $11 - 15,\ 16 - 20,\ 21 - 25,\ 26 - 30$ cm
	Norway pout	2 otoliths per 5 cm length class $5 - 10,\ 11 - 15$ cm
		2 otoliths per 1 cm length class > 15 cm
	saithe	1 otolith per 1 cm length class
	plaice	1 otolith per 1 cm length class

S3 Weightings of Statistical Rectangles

The weightings of the some statistical rectangles are alloted to species such as sprat, saithe and herring by depth strata between 10m -200m and for RFA 8 and 9 water depths between 10m-250m. Table S3.1 gives these weights, which are used in the analysis of the saithe data (ICES, 2013a).

Table S3.1: Weights used for Pollachius virens in equation (2.3).

StatRec	Weight	StatRec	Weight	StatRec	Weight	StatRec	Weight	StatRec	Weight
31F1	0.6	38F0	1	41F7	1	44F3	1	48E7	1
31F2	0.8	38F1	1	41F8	0.1	44F4	1	48E8	0.9
31F3	0.05	38F2	1	41G0	0.2	44F5	0.9	48E9	1
32F1	0.8	38F3	1	41G1	0.97	44F8	0.25	48F0	1
32F2	1	38F4	1	41G2	0.53	44F9	0.8	48F1	1
32F3	0.8	38F5	1	42E7	0.4	44G0	0.94	48F2	1
32F4	0.01	38F6	1	42E8	1	44G1	0.6	48F3	0.5
33F1	0.3	38F7	1	42E9	1	45E6	0.4	48G0	0.02
33F2	1	38F8	0.3	42F0	1	45E7	1	49E6	0.8
33F3	1	39E8	0.5	42F1	1	45E8	1	49E7	1
33F4	0.4	39E9	1	42F2	1	45E9	1	49E8	0.4
34F1	0.4	39F0	1	42F3	1	45F0	1	49E9	1
34F2	1	39F1	1	42F4	1	45F1	1	49F0	1
34F3	1	39F2	1	42F5	1	45F2	1	49F1	1
34F4	0.6	39F3	1	42F6	1	45F3	1	49F2	1
35F0	0.8	39F4	1	42F7	1	45F4	0.6	49F3	0.5
35F1	1	39F5	1	42F8	0.2	45F8	0.3	50E6	0.1
35F2	1	39F6	1	42G0	0.32	45F9	0.02	50E7	0.6
35F3	1	39F7	1	42G1	0.89	45G0	0.24	50E8	0.7
35F4	0.9	39F8	0.4	42G2	0.64	45G1	0.55	50E9	0.9
35F5	0.1	40E7	0.04	43E7	0.03	46E6	0.4	50F0	1
36F0	0.9	40E8	0.8	43E8	0.9	46E7	0.9	50F1	1
36F1	1	40E9	1	43E9	1	46E8	1	50F2	1
36F2	1	40F0	1	43F0	1	46E9	1	50F3	0.2
36F3	1	40F1	1	43F1	1	46F0	1	51E6	0
36F4	1	40F2	1	43F2	1	46F1	1	51E7	0
36F5	1	40F3	1	43F3	1	46F2	1	51E8	0.5
36F6	0.9	40F4	1	43F4	1	46F3	0.8	51E9	1
36F7	0.4	40F5	1	43F5	1	46F9	0.3	51F0	1
36F8	0.5	40F6	1	43F6	1	46G0	0.52	51F1	1
37E9	0.2	40F7	1	43F7	1	46G1	0.2	51F2	0.5
37F0	1	40F8	0.1	43F8	0.94	47E6	0.8	51F3	0
37F1	1	41E6	0.03	43F9	0.41	47E7	0.6	52E6	0
37F2	1	41E7	0.8	43G0	0.21	47E8	1	52E7	0
37F3	1	41E8	1	43G1	0.7	47E9	1	52E8	0
37F4	1	41E9	1	43G2	0.3	47F0	1	52E9	0.1
37F5	1	41F0	1	44E6	0.5	47F1	1	52F0	0.2
37F6	1	41F1	1	44E7	0.5	47F2	1	52F1	0.5
37F7	1	41F2	1	44E8	0.9	47F3	0.6	52F2	0.1
37F8	0.8	41F3	1	44E9	1	47F9	0.01		
38E8	0.2	41F4	1	44F0	1	47G0	0.3		
38E9	0.9	41F5	1	44F1	1	47G1	0.02		
52F3	0	41F6	1	44F2	1	48E6	1		

S4 Imputing missing ages

With the current IBTS sampling procedure, *one* age reading is collected from every cm group in every haul for cod and saithe. However, missing ages do occur, and in this section we describe how missing ages are accounted for. Note that missing ages are automatically accounted for with the model based approach. However, for the area based ALK and the haul based ALK, some adhoc procedure needs to be followed when age is missing. We want to highlight that missing ages occur relatively seldom. E.g. in 1st. quarter in year 2018 and with length group width equal 1cm, 0.9% of the cod miss age with respect to the area based ALK. In the same example, 1.4% of the cod miss age with respect to the haul based ALK.

S4.1 Area based ALK

Assume there do not exist an age reading of a fish of length l in a RFA. Just as in (ICES, 2013a), the following procedure is done for the area based ALK:

- If l is between the minumum length and maximum length, the age is set to be equal the ALK to the closest length group with observed ages in the RFA. In cases where there are two equally close length groups with observed ages, the average of those two ALKs is used.
- If l is smaller then the smallest measured fish in the RFA, the age is set to the minimum age.
- If l is larger or equal the maximum length, the age is set to the maximum age.

S4.2 Haul based ALK

Assume there do not exist an age reading of a fish of length l in a haul. For the haul based procedure, the following is done in sequential order:

- If there exist an age reading of that length group closer than 60 nautical mile in the same RFA, the ALK from the closest haul with such an age reading is used.
- If there exist a fish with length in the interval $l \pm 1cm$ with age information in the same haul, that observed age is used.

- If the two first step did not produce an ALK for l, there exist little information close in space and length, and the area based ALK is used.

S5 Nonparametric Bootstrap Sampling procedure

Nonparametric bootstrapping is attractive as it makes no distributional assumption, and is suitable for estimating confidence interval for indices of abundance. Suppose we have a vector $\mathbf{x}$ of m independent observations, and we are interested in estimating a parameter $\hat{\theta}(\mathbf{x})$ and its variance. The general nonparametric bootstrap algorithm is as follows:

1. Sample m observations randomly with replacement from $\mathbf{x}$ to obtain a bootstrap data set, denoted by $\mathbf{x}^*$.
2. Calculate the bootstrap version of the statistic of interest, $\theta^* = \hat{\theta}(\mathbf{x}^*)$.
3. Repeat steps 1 and 2 a large number of times, say B, to obtain an estimate of the bootstrap distribution
4. calculate the average of the bootstrapped statistics, $\sum_{b=1}^{B} {\theta^*}_{(b)}/B$
5. compute the variance of the estimator $\hat{\theta}(\mathbf{x})$ through the variance of the set ${\theta^*}_{(b)},\ b = 1, 2, ..., B$, given by

$$\frac{\sum_{b=1}^{B} \left({\theta^*}_{(b)} - {\theta^*}_{(\cdot)}\right)^2}{(B-1)} \tag{S5.1}$$

   where ${\theta^*}_{(\cdot)} = \sum_{b=1}^{B} {\theta^*}_{(b)}/B$.

The Bias-Corrected method assumes that there is a montonic increasing function and the estimator $\hat{\lambda}_a$ has a monotonic increasing function $f()$ such that the transformed values $f(\hat{\lambda}_a)$ are normally distributed with mean $f(\lambda_a) - z_0$ and standard deviation one, where z_0 are the standard normal limits (Puth et al., 2015; Karlsson, 2009). Now, let $P^*\left(\hat{\theta}(\mathbf{x}^*) \leq \hat{\theta}(\mathbf{x})\right)$ denote the proportion of $\hat{\theta}(\mathbf{x}^*)^{'}$s in the bootstrap sample that have a value lower than the value of the parameter estimate $\hat{\theta}(\mathbf{x})$, and le z_0 be defined as

$$z_0 = \Phi^{-1}\left\{P^*\left(\hat{\theta}(\mathbf{x}^*) \leq \hat{\theta}(\mathbf{x})\right)\right\}, \tag{S5.2}$$

where Φ denotes the cumulative distribution function of the standard normal distribution. Also let $\tilde{\alpha}_1$ and $\tilde{\alpha}_2$ be defined as

$$\tilde{\alpha}_1 = \Phi(2z_0 + z_\alpha), \tag{S5.3}$$

and

$$\tilde{\alpha}_2 = \Phi(2z_0 + z_{1-\alpha}), \tag{S5.4}$$

respectively. A $100(1 - 2\alpha)$ percent confidence interval for $\theta(\mathbf{x})$ is then given by

$$\hat{\theta}_{(\tilde{\alpha}_1(B+1))}(\mathbf{x}^*) \leq \hat{\theta}(\mathbf{x}) \leq \hat{\theta}_{((\tilde{\alpha}_2-1)(B+1))}(\mathbf{x}^*). \tag{S5.5}$$

S6 IBTS data set for cod and saithe

Table S6.1: Age and length data for saithe and cod . Data collected in the first quarter (Q1) has no age 0 group but this is collected in quarter 3 (Q3) surveys.

Species		Years									
		2014		2015		2016		2017		2018	
		Q1	Q3	Q1	Q3	Q1	Q3	Q1	Q3	Q1	Q3
	Trawls	352	333	387	367	370	389	385	345	372	365
	Mean time of hauls (in minutes)	29.20	28.91	28.55	23.44	28.40	22.47	29.02	29.37	29.26	29.13
cod											
	Age range (in years)	1 - 9	0 - 10	1 - 9	0 - 8	1 - 10	0 - 10	1 - 11	0 - 11	1 - 12	0 - 11
	Length range (in cm)	8 - 113	NA	9 - 113	7 - 111	11 - 109	5 - 110	7 - 115	6 - 112	11 - 114	5 - 107
	Total otoliths	1903	2399	2895	2113	2046	1804	2501	2230	1600	1456
saithe											
	Age range (in years)	1 - 16	0 - 15	1 - 16	0 - 19	1 - 17	0 - 19	1 - 15	0 - 11	1 - 12	0 - 13
	Length range (in cm)	15 - 105	8 - 108	13 - 110	NA	16 - 107	12 - 115	15 - 108	6 - 112	11 - 114	7 - 109
	Total otoliths	584	1182	600	1526	581	1631	1083	2163	822	1085

Table S6.2: Summary of North Sea IBTS cod and saithe (in parentheses) data for third quarter in year 2017 and first quarter in year 2018.

Data	Description
Trawl hauls	Total of 372 trawl hauls in year 2018 Q1; 238 (83) with length and 230 (81) with age information. In 2017 Q3, a total of 345 trawl hauls were taken; 238 (129) with length and 237 (128) with age information.
Age	The age varied between 1 (1) to 12 (18) years in year 2018 Q1 and 0 (0) to 11 (17) in year 2017 Q3.
Length	Length information in cm varied between 11 (13) to 114 (106) cm in year 2018 Q1 and between 6 (10) to 112 (109) cm in year 2017 Q3.
Date	Date of catch in year 2018 Q1 varied between 15.01.2018 to 28.02.2018 and in year 2017 Q3 between 18.07.2017 to 31.08.2018
Duration of haul	Mean duration is 29.37 minutes, with 30 minutes as 83% coverage interval in year 2018 Q1; and in 2017 Q3 with mean duration of 29.26 minutes with 30 minutes as 88% coverage .
Total count for all ages	1600 (822) in year 2018 Q1 and 2330 (2163) 2017 Q3.

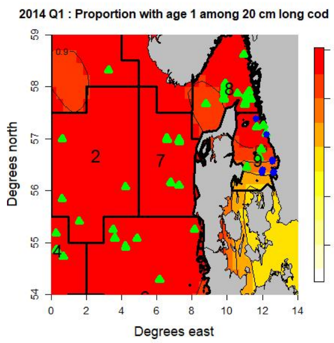
S7 Analysis of real data

S7.1 Proportion of age given length of cod

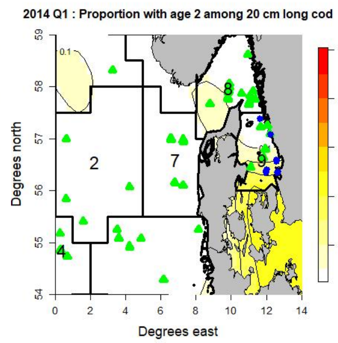
Figure S2 shows that age-length structure of cod varies over several years: the first quarter (Q1) in years 2014-2017. This indicates that the assumption of constant ALK over large areas proposed in DATRAS is invalid. The plots in Figure S3, which shows the proportion of age given different lengths of cod in 2018 Q1 further discredit this assumption as a fish of length 30 cm can be of age 2 (green triangle ▲) or age 3 (blue circle •) in the northern North Sea; see Figure S3 (a).

Table S6.3: Age and length data for saithe in year 2017 Q3 and cod in year 2018 Q1. Data collected in the first quarter (Q1) has no age 0 group but this is collected in quarter 3 (Q3) surveys.

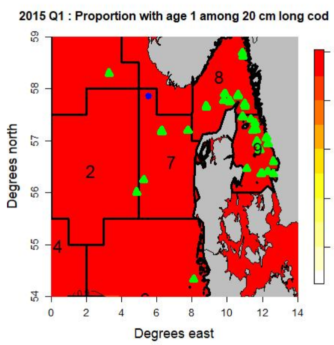
	saithe in year 2017 Q3						**cod in year 2018 Q1**					
Age	Numbers aged	$\mathbf{L_{min}}$	$\mathbf{L_{max}}$	$\mathbf{L_{mean}}$	Sd($\mathbf{L}$)	CV($\mathbf{L}$)	Numbers aged	$\mathbf{L_{min}}$	$\mathbf{L_{max}}$	$\mathbf{L_{mean}}$	Sd($\mathbf{L}$)	CV($\mathbf{L}$)
0	21	10	14	12.143	1.195	0.098						
1	26	23	32	27.654	2.297	0.083	149	11	30	18.407	3.693	0.201
2	65	27	47	38.077	3.337	0.088	814	17	53	33.180	6.290	0.190
3	531	34	56	42.041	3.785	0.090	222	30	81	50.654	10.185	0.202
4	767	35	73	48.261	4.521	0.094	189	43	92	64.479	8.399	0.130
5	334	46	78	56.876	6.105	0.107	102	54	96	76.627	9.594	0.125
6	159	50	91	66.025	7.137	0.108	84	54	100	80.871	9.456	0.117
7	127	57	93	73.976	7.163	0.097	28	58	110	84.086	11.308	0.134
8	69	63	94	77.725	7.010	0.090	4	80	94	85.500	6.455	0.075
9	18	64	97	85.333	7.499	0.088	5	66	96	83.400	11.305	0.061
10	22	84	107	92.364	5.803	0.063	1	87	87	-	-	-
11	5	79	102	92.800	9.311	0.100	1	106	106	-	-	-
12	7	91	109	99.429	6.554	0.066						
13	5	94	104	98.800	4.550	0.046						
14	1	108	108	108	-	-						
15	1	105	105	108	-	-						
16	4	93	106	100.250	5.439	0.054						
17	1	109	109	109	-	-						



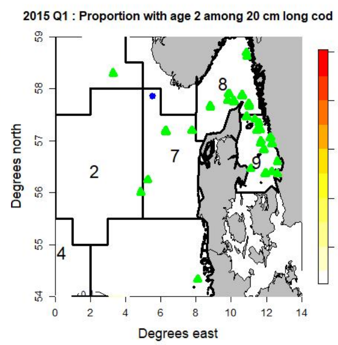
(a)



(b)



(c)



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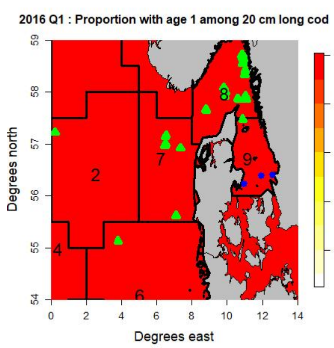

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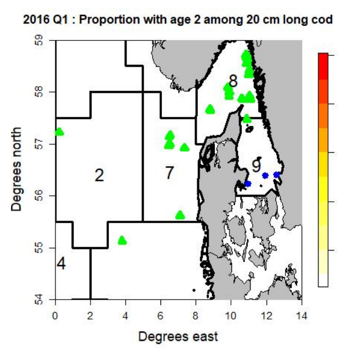

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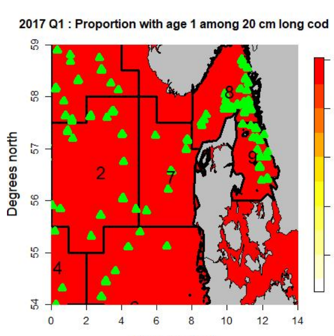
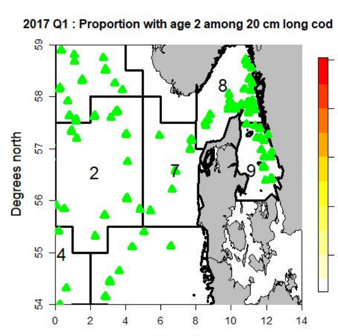
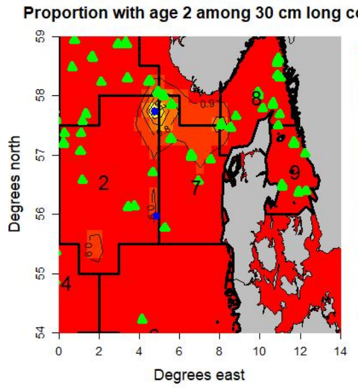


(g)

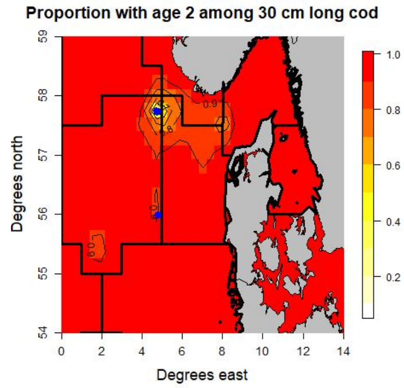


(h)

Figure S2: Estimated proportion of age 1 and 2 year-old cod of length 20 cm in the North Sea in the first quarter (Q1) in years 2014-2017. The green triangles (▲) are observations of 1-year olds and the blue circles (●) are observations of 2-year olds in the length interval 19 cm to 21 cm.

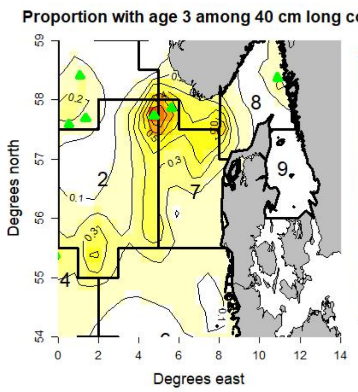


(a)



(b)

Estimated proportion of age 2 and 3 year-old cod of length 30 cm in the North Sea, where ▲ are observations of 2-year olds and ● are 3-year olds in the length interval 29 cm to 31 cm in 2018 Q1.



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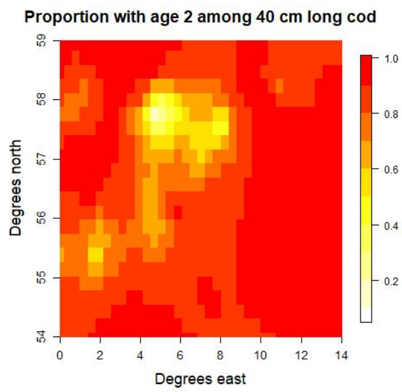
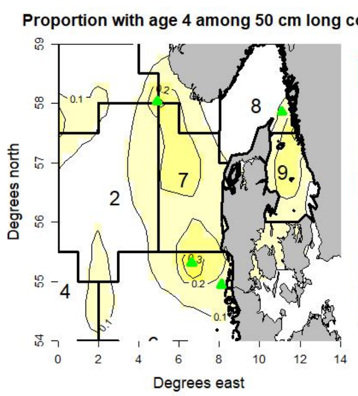
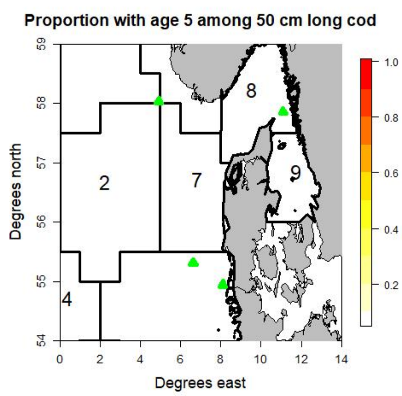


(d)

Estimated proportion of age 3 and 4 year-old cod of length 40 cm in North Sea, where ▲ are 3-year olds in the length interval 39 cm to 41 cm in 2018 Q1.



(e)



(f)

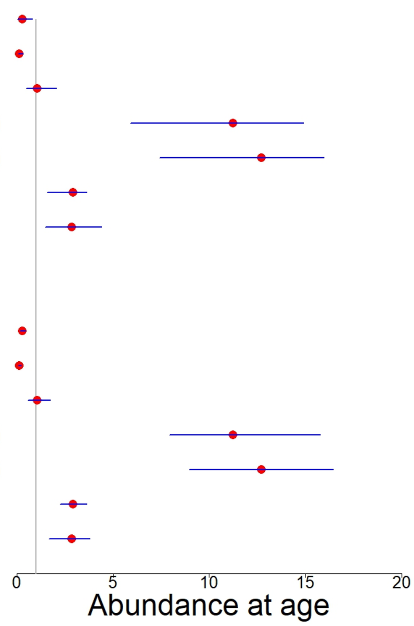
Estimated proportion of age 4 and 5 year-old cod of length 50 cm in Skagerak, where ▲ are 4-year olds in the length interval 49 cm to 51 cm in 2018 Q1.

Figure S3: Proportion of age given lengths 20 cm, 40 cm or 50 cm of cod in 2018 Q1 in the North Sea.

S7.2 Estimates from DATRAS and Stratified bootstrap procedures

The bootstrap procedure proposed by DATRAS lacks the potential to account for the spatial variation in the data. The DATRAS bootstrap procedure ignores the fine-scale stratification in the sampling process, leading to an overestimation of the uncertainty; and ignores the age-length data collected at the haul level, resulting in an underestimation of the uncertainty. The results (FigureS4) shows an overestimation of the uncertainty for all age groups, suggesting that it is relevant to account for the fine-scale stratification when resampling the data.

Age	Species	Mean	Median	SE	RSE%	Width CI-95	Estimate (CI_{95})
Datras							
0	saithe	0.431	0.368	0.3072	108.9	0.784	0.28 (0.01-0.80)
1	saithe	0.125	0.120	0.0668	53.8	0.261	0.12 (0.04-0.30)
2	saithe	1.126	1.049	0.4036	38.7	1.565	1.04 (0.47-2.03)
3	saithe	12.548	12.555	2.8061	25.0	8.997	11.24 (5.91-14.90)
4	saithe	14.196	14.227	2.7229	21.4	8.551	12.70 (7.42-15.97)
5	saithe	3.268	3.286	0.5770	19.8	2.054	2.91 (1.57-3.62)
6+	saithe	3.030	2.934	0.7421	26.1	2.941	2.84 (1.45-4.40)
Stratified							
0	saithe	0.276	0.280	0.0880	31.2	0.297	0.28 (0.14-0.43)
1	saithe	0.123	0.124	0.0527	42.5	0.173	0.12 (0.04-0.21)
2	saithe	1.005	0.997	0.2635	25.3	1.140	1.04 (0.57-1.71)
3	saithe	10.899	10.813	2.0905	18.6	7.845	11.24 (7.94-15.78)
4	saithe	12.424	12.425	1.8745	14.8	7.491	12.70 (8.95-16.45)
5	saithe	2.927	2.905	0.3528	12.1	1.384	2.91 (2.23-3.61)
6+	saithe	2.895	2.894	0.5621	19.8	2.138	2.84 (1.66-3.80)



(a) Datras and Stratified bootstrap Procedures

Figure S4: Comparison of estimated confidence intervals (CI_{95}) from DATRAS and stratified bootstrap procedures. The bias-corrected bootstrap method is used to give estimates for saithe in year 2017 Q3. Estimated indices of abundance (Estimate), and its standard error (SE), bootstrap mean (Mean), Median estimates, percentage relative standard error (RSE %) and width of confidence intervals are also given.

S7.3 Estimates from different sampling procedures

Table S7.1: Comparison of estimated uncertainty from proposed sampling procedures with estimated uncertainty from original data

age	mCPUE	SE.resampled	SE	RSE.resampled	RSE
1 cm					
1	0.86	0.122	0.119	14.179	13.895
2	6.50	1.002	0.902	15.426	13.897
3	1.57	0.180	0.140	11.518	8.934
4	1.58	0.294	0.304	18.611	19.223
5	0.74	0.122	0.113	16.560	15.269
6+	1.07	0.275	0.289	25.623	26.968
2 cm					
1	0.86	0.126	0.119	14.697	13.895
2	6.50	1.048	0.902	16.149	13.897
3	1.57	0.161	0.140	10.239	8.934
4	1.58	0.299	0.304	18.769	19.223
5	0.74	0.141	0.113	19.257	15.269
6+	1.07	0.263	0.289	24.643	26.968
3 cm					
1	0.86	0.133	0.119	15.478	13.895
2	6.50	1.059	0.902	16.311	13.897
3	1.57	0.192	0.140	12.279	8.934
4	1.58	0.298	0.304	18.714	19.223
5	0.74	0.132	0.113	17.767	15.269
6+	1.07	0.311	0.289	29.178	26.968
4 cm					
1	0.86	0.132	0.119	15.384	13.895
2	6.50	0.938	0.902	14.476	13.897
3	1.57	0.187	0.140	11.844	8.934
4	1.58	0.349	0.304	21.842	19.223
5	0.74	0.159	0.113	21.702	15.269
6+	1.07	0.280	0.289	26.335	26.968
5 cm					
1	0.86	0.129	0.119	15.126	13.895
2	6.50	0.995	0.902	15.338	13.897
3	1.57	0.163	0.140	10.381	8.934
4	1.58	0.320	0.304	20.095	19.223
5	0.74	0.208	0.113	27.857	15.269
6+	1.07	0.289	0.289	27.193	26.968

Table S7.2: Estimated abundance ($\hat{\lambda}_a$) for cod from the original data in year 2018 Q1 compared with estimated abundance ($\hat{\lambda}_a^*$) from the reduced data for different sampling procedures of length groups (l). The median estimated indices, estimated standard error of $\hat{\lambda}_a^*$ (SE($\hat{\lambda}_a^*$)), the percentage relative standard error (RSE%) and mean square error (MSE) are also given.

	l	$\hat{\lambda}_a$	$\hat{\lambda}_a^*$	(median) $\hat{\lambda}_a^*$	SE($\hat{\lambda}_a^*$)	RSE%	MSE	CI-95 ($\hat{\lambda}_a^*$)
age 1								
	1 cm	0.863	0.863	0.863	0.00910	0.000	0.0000	(0.86, 0.86)
	2 cm	0.863	0.865	0.867	0.00939	1.085	0.00009	(0.84, 0.88)
	3 cm	0.863	0.856	0.861	0.02803	3.274	0.00083	(0.80, 0.90)
	4 cm	0.863	0.857	0.859	0.02791	3.257	0.00082	(0.81, 0.91)
	5 cm	0.863	0.845	0.847	0.03694	4.370	0.00044	(0.81, 0.92)
	6 cm	0.863	0.860	0.861	0.03514	4.088	0.00125	(0.79, 0.93)
	7 cm	0.863	0.854	0.853	0.03803	4.454	0.00153	(0.80, 0.93)
age 2								
	1 cm	6.496	6.496	6.491	0.00552	0.085	0.00003	(6.49, 6.50)
	2 cm	6.496	6.486	6.486	0.02073	0.320	0.00053	(6.46, 6.53)
	3 cm	6.496	6.504	6.506	0.05414	0.832	0.00299	(6.38, 6.60)
	4 cm	6.496	6.498	6.500	0.05351	0.823	0.00287	(6.38, 6.60)
	5 cm	6.496	6.514	6.517	0.07322	1.124	0.00567	(6.32, 6.65)
	6 cm	6.496	6.503	6.507	0.07862	1.209	0.00623	(6.30, 6.65)
	7 cm	6.496	6.486	6.491	0.09414	1.452	0.00897	(6.31, 6.64)
age 3								
	1 cm	1.571	1.572	1.571	0.04499	2.861	0.00203	(1.49, 1.66)
	2 cm	1.571	1.578	1.572	0.07268	4.605	0.00533	(1.45, 1.74)
	3 cm	1.571	1.557	1.554	0.09893	6.353	0.00999	(1.41, 1.77)
	4 cm	1.571	1.640	1.632	0.10687	6.517	0.00161	(1.38, 1.86)
	5 cm	1.571	1.634	1.632	0.12411	7.593	0.01940	(1.31, 1.87)
	6 cm	1.571	1.649	1.643	0.13337	8.086	0.02390	(1.31, 1.93)
	7 cm	1.571	1.748	1.740	0.14741	8.432	0.05300	(1.28, 2.06)
age 4								
	1 cm	1.584	1.581	1.581	0.06670	4.219	0.00446	(1.45, 1.71)
	2 cm	1.584	1.597	1.596	0.11810	7.397	0.01410	(1.35, 1.83)
	3 cm	1.584	1.613	1.619	0.14715	9.123	0.02250	(1.25, 1.89)
	4 cm	1.584	1.563	1.568	0.14581	9.326	0.02170	(1.30, 1.84)
	5 cm	1.584	1.586	1.581	0.15534	9.794	0.02410	(1.30, 1.90)
	6 cm	1.584	1.596	1.595	0.16125	10.104	0.02620	(1.26, 1.93)
	7 cm	1.584	1.502	1.500	0.16988	11.311	0.03550	(1.33, 1.83)
age 5								
	1 cm	0.742	0.746	0.751	0.06817	9.1440	0.00466	(0.61, 0.87)
	2 cm	0.742	0.738	0.729	0.10457	14.170	0.01100	(0.58, 0.96)
	3 cm	0.742	0.765	0.756	0.11506	15.040	0.01380	(0.53, 1.00)
	4 cm	0.742	0.764	0.757	0.11686	15.299	0.01410	(0.54, 1.00)
	5 cm	0.742	0.801	0.787	0.12230	15.270	0.01840	(0.55, 1.07)
	6 cm	0.742	0.779	0.765	0.11546	14.817	0.01470	(0.58, 1.02)
	7 cm	0.742	0.828	0.814	0.12779	15.435	0.02360	(0.54, 1.11)
age 6+								
	1 cm	1.074	1.073	1.065	0.06707	6.251	0.00450	(0.95, 1.20)
	2 cm	1.074	1.067	1.060	0.10236	9.595	0.01050	(0.90, 1.28)
	3 cm	1.074	1.036	1.028	0.11648	11.247	0.01510	(0.90, 1.26)
	4 cm	1.074	1.009	1.003	0.11837	11.735	0.01830	(0.90, 1.25)
	5 cm	1.074	0.950	0.944	0.11578	12.184	0.02880	(0.96, 1.19)
	6 cm	1.074	0.944	0.930	0.11745	12.446	0.03090	(0.95, 1.20)
	7 cm	1.074	0.913	0.905	0.11462	12.553	0.03910	(1.00, 1.14)

Table S7.3: Estimated abundance ($\hat{\lambda}_a$) for saithe from the original data in year 2017 Q3 compared with estimated abundance ($\hat{\lambda}^*_a$) from the reduced data for different sampling procedures of length groups (l).

	l	$\hat{\lambda}_a$	$\hat{\lambda}^*_a$	(median) $\hat{\lambda}^*_a$	SE($\hat{\lambda}^*_a$)	RSE%	MSE	CI-95 ($\hat{\lambda}^*_a$)
age 0								
	1 cm	0.282	0.282	0.282	0.00000	0.00	0.00000	(0.28, 0.28)
	2 cm	0.282	0.282	0.282	0.00000	0.00	0.00000	(0.28, 0.28)
	3 cm	0.282	0.289	0.295	0.00626	2.17	0.00008	(0.28, 0.29)
	4 cm	0.282	0.290	0.295	0.00592	2.04	0.00010	(0.28, 0.29)
	5 cm	0.282	0.282	0.282	0.00000	0.00	0.00000	(0.28, 0.28)
	6 cm	0.282	0.297	0.295	0.01022	3.44	0.00030	(0.28, 0.31)
	7 cm	0.282	0.290	0.295	0.00594	2.05	0.00010	(0.28, 0.29)
age 1								
	1 cm	0.123	0.123	0.123	0.00000	0.00	0.00000	(0.12, 0.12)
	2 cm	0.123	0.123	0.123	0.00000	0.00	0.00000	(0.12, 0.12)
	3 cm	0.123	0.117	0.111	0.00626	5.36	0.00008	(0.11, 0.12)
	4 cm	0.123	0.118	0.115	0.00673	5.71	0.00008	(0.11, 0.13)
	5 cm	0.123	0.125	0.123	0.00139	1.12	0.000003	(0.12, 0.13)
	6 cm	0.123	0.112	0.114	0.01059	9.46	0.00024	(0.11, 0.13)
	7 cm	0.123	0.116	0.114	0.00628	5.43	0.00009	(0.11, 0.13)
age 2								
	1 cm	0.929	0.930	0.923	0.16851	18.13	0.02840	(0.64, 1.28)
	2 cm	0.929	0.916	0.861	0.28468	31.06	0.08120	(0.55, 1.53)
	3 cm	0.929	0.966	0.902	0.33158	34.32	0.11000	(0.53, 1.71)
	4 cm	0.929	0.955	0.900	0.31885	33.38	0.10200	(0.49, 1.66)
	5 cm	0.929	0.992	0.942	0.31609	31.85	0.10400	(0.48, 1.75)
	6 cm	0.929	0.966	0.893	0.36374	37.66	0.13400	(0.47, 1.83)
	7 cm	0.929	0.989	0.933	0.34996	35.40	0.12600	(0.45, 1.80)
age 3								
	1 cm	11.238	11.270	11.249	0.53506	4.75	0.28700	(10.19, 12.30)
	2 cm	11.238	11.179	11.187	0.92312	8.26	0.85600	(9.57, 13.11)
	3 cm	11.238	11.109	11.082	1.07691	9.69	1.18000	(9.30, 13.27)
	4 cm	11.238	11.000	11.009	1.08989	9.91	1.24000	(9.21, 13.15)
	5 cm	11.238	10.891	10.871	1.11346	10.22	1.36000	(9.41, 13.03)
	6 cm	11.238	10.920	10.905	1.06856	9.79	1.24000	(9.46, 13.04)
	7 cm	11.238	10.840	10.839	1.08304	9.99	1.33000	(9.53, 13.05)
age 4								
	1 cm	12.789	12.757	12.754	0.52780	4.14	0.28000	(11.79, 13.73)
	2 cm	12.789	12.816	12.827	0.93741	7.31	0.87900	(10.76, 14.60)
	3 cm	12.789	12.863	12.856	1.06438	8.27	1.14000	(10.68, 14.93)
	4 cm	12.789	12.950	12.954	1.09842	8.48	1.23000	(10.56, 15.14)
	5 cm	12.789	13.096	13.087	1.12912	8.62	1.37000	(10.51, 15.31)
	6 cm	12.789	13.061	13.051	1.08819	8.33	1.26000	(10.42, 15.11)
	7 cm	12.789	13.176	13.187	1.09385	8.30	1.35000	(10.33, 15.18)
age 5								
	1 cm	2.971	2.971	2.966	0.13399	4.51	0.01800	(2.72, 3.24)
	2 cm	2.971	3.048	3.037	0.27486	9.02	0.08150	(2.52, 3.62)
	3 cm	2.971	3.000	2.974	0.31856	10.62	0.10200	(2.42, 3.65)
	4 cm	2.971	3.038	3.005	0.34723	11.43	0.12500	(2.40, 3.77)
	5 cm	2.971	2.971	2.968	0.33433	11.25	0.11200	(2.35, 3.64)
	6 cm	2.971	2.980	2.964	0.38418	12.89	0.14800	(2.28, 3.77)
	7 cm	2.971	2.940	2.922	0.39677	13.49	0.15800	(2.32, 3.76)
age 6+								
	1 cm	2.819	2.818	2.820	0.05409	1.92	0.00293	(2.71, 2.92)
	2 cm	2.819	2.787	2.784	0.08700	3.12	0.00860	(2.68, 2.96)
	3 cm	2.819	2.808	2.808	0.11451	4.08	0.01320	(2.60, 3.04)
	4 cm	2.819	2.800	2.795	0.12424	4.44	0.01580	(2.61, 3.06)
	5 cm	2.819	2.793	2.791	0.13520	4.84	0.01890	(2.58, 3.07)
	6 cm	2.819	2.814	2.823	0.14353	5.10	0.02060	(2.54, 3.10)
	7 cm	2.819	2.800	2.794	0.16239	5.80	0.02670	(2.55, 3.14)