The 17th Japanese Olympiad in Informatics (JOI 2017/2018)

Spring Training Camp/Qualifying Trial

March 19–25, 2018 (Komaba/Yoyogi, Tokyo)

Contest Day 1 – Construction of Highway

# **Construction of Highway**

There are *N* cities in JOI Kingdom, which are indexed by the numbers from 1 to *N*. City 1 is the capital city. Each city has a value called **liveliness** and the initial value of liveliness of city i ( $1 \le i \le N$ ) is  $C_i$ .

Road in JOI Kingdom connects two different cities bidirectionally. Initially, there is no road in JOI Kingdom. You have planned N-1 constructions of roads. The j-th construction  $(1 \le j \le N-1)$  is planned to be done in the following way.

- Two cities,  $A_j$  and  $B_j$ , are appointed, when one can go from city 1 to city  $A_j$  and cannot go from city 1 to city  $B_j$  by using only roads constructed at that time.
- You construct a road connecting city  $A_j$  and city  $B_j$ . The cost of this construction is the number of pairs of cities (s,t) satisfying the following conditions:

City s and City t lie on the shortest path between city 1 and city  $A_j$ , and when one goes from city 1 to city  $A_j$  he arrives city s before city t, and the value of liveliness of city t is strictly larger than that of city t.

Here, cities lying on the path between city 1 and city  $A_j$  include city 1 and city  $A_j$ . Notice that the shortest path between city 1 and city  $A_j$  is unique.

• The values of liveliness of all cities lying on the path between city 1 and city  $A_j$  change to the value of liveliness of city  $B_j$ .

You want to know the cost of each construction.

#### **Task**

Given the data of cities and constructions of roads, write a program which calculates the cost of each construction.

## Input

Read the following data from the standard input.

- The first line of input contains a integer N. This means there are N cities in JOI Kingdom.
- The second line of input contains N space separated integers  $C_1, C_2, \dots C_N$ . This means the initial value of liveliness of city i ( $1 \le i \le N$ ) is  $C_i$ .
- The j-th line  $(1 \le j \le N 1)$  of following N 1 lines contains two space separated integers  $A_j$ ,  $B_j$ . This means city  $A_j$  and city  $B_j$  are appointed for the j-th construction of road.



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# **Output**

Write N-1 lines to the standard output. The j-th line  $(1 \le j \le N-1)$  of output contains the cost of the j-th construction of road.

#### **Constraints**

All input data satisfy the following conditions.

- $1 \le N \le 100\,000$ .
- $1 \le C_i \le 1\,000\,000\,000\,(1 \le i \le N)$ .
- $1 \le A_j \le N \ (1 \le j \le N 1)$ .
- $1 \le B_j \le N \ (1 \le j \le N 1)$ .
- By using roads constructed before the *j*-th construction, one can go from city 1 to city  $A_j$  and cannot go from city 1 to city  $B_j$   $(1 \le j \le N 1)$ .

#### **Subtask**

There are 3 subtasks. The score and additional constraints of each subtask are as follows:

#### Subtask 1 [7 points]

•  $N \le 500$ .

#### Subtask 2 [9 points]

•  $N \le 4000$ .

## Subtask 3 [84 points]

There are no additional constraints.



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## **Sample Input and Output**

Sample Input 1	Sample Output 1
5	0
1 2 3 4 5	0
1 2	0
2 3	2
2 4	
3 5	

In Sample Input 1, constructions are done as follows:

- In the first construction, there are no pairs (*s*, *t*) satisfying the conditions, so the cost is 0. A road connecting city 1 and city 2 is constructed and the value of liveliness of city 1 changes to 2.
- In the second construction, there are no pairs (s, t) satisfying the conditions too, so the cost is 0. A road connecting city 2 and city 3 is constructed and the values of liveliness of city 1 and city 2 change to 3.
- In the third construction, there are no pairs (s, t) satisfying the conditions too, so the cost is 0. A road connecting city 2 and city 4 is constructed and the values of liveliness of city 1 and city 2 change to 4.
- In the fourth construction, two pairs (s,t) = (1,3), (2,3) satisfy the conditions, so the cost is 2. A road connecting city 3 and city 5 is constructed and the values of liveliness of city 1, city 2 and city 3 change to 5.

Sample Input 2	Sample Output 2
10	0
1 7 3 4 8 6 2 9 10 5	0
1 2	0
1 3	1
2 4	1
3 5	0
2 6	1
3 7	2
4 8	3
5 9	
6 10	