Assignment 4

Information Retrieval

CS 834

Fall 2017

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Problem 8.3

1.1 Problem Statement

For one query in the CACM collection (provided at the book website), generate a ranking using Galago, and then calculate average precision, NDCG at 5 and 10, precision at 10, and the reciprocal rank by hand.

1.2 Solution

This problem uses CACM corpus provided in the test collection of the book. The queries ran against the CACM collection have been used from the processed queries section of the CACM test collection.

1.2.1 Query:interested in articles on robotics motion planning particularly the geometric and combinatorial aspects we are not interested in the dynamics of arm motion

The below xml file shows the query which was used in galago.

```
F:\Fall2017\InformationRetreival\Assignment3\Galgo\galagosearch-1.04-bin\galagosearch-1.04\bin>galago.bat batch-search --index=F:\Fall2017\InformationRetreival\Assignment4\index.

idx --count=10 F:\Fall2017\InformationRetreival\Assignment4\onequery.xml > F:\Fall2017\

InformationRetreival\Assignment4\cacm_onequery.list
```

The below list file is result of batch search for the query from galago with number of results for each query set to 10.

```
6 Q0 CACM-0695 1 -164.66490173 galago
6 Q0 CACM-2826 2 -166.82664490 galago
6 Q0 CACM-2828 3 -167.13014221 galago
6 Q0 CACM-1664 4 -167.29315186 galago
```

```
6 Q0 CACM-1543 5 -167.67100525 galago
```

6 Q0 CACM-2078 6 -168.12095642 galago

6 Q0 CACM-2176 7 -168.47441101 galago

6 Q0 CACM-1113 8 -169.13491821 galago

6 Q0 CACM-0605 9 -169.25828552 galago

6 Q0 CACM-1517 10 -169.68901062 galago

6 10

F:\Fall2017\InformationRetreival\Assignment3\Galgo\galagosearch-1.04-bin\galagosearch-1.04\bin> galago.bat eval F:\Fall2017\InformationRetreival\Assignment4\cacm_onequery.list F:\Fall2017\InformationRetreival\Assignment4\cacm.rel >F:\Fall2017\InformationRetreiva\Assignment4\onequeryoutput.txt

The below text file is the result of eval command by using the relevance judgments file provided in cacm test collections.

num_rel 6 3

num_rel_ret 6 3

 num_ret

map 6 0.4111

ndcg 6 0.5833

ndcg15 6 0.5833

R-prec 6 0.3333

bpref 6 0.0000

recip_rank 6 0.3333

P5 6 0.4000

P10	6 0.3000
P15	6 0.2000
P20	6 0.1500
P30	6 0.1000
P100	6 0.0300
P200	6 0.0150
P500	6 0.0060
P1000	6 0.0030
num_ret	all 10
num_rel	all 3
num_rel_ret	all 3
map	all 0.4111
ndcg	all 0.5833
ndcg15	all 0.5833
R-prec	all 0.3333
bpref	all 0.0000
recip_rank	all 0.3333
P5	all 0.4000
P10	all 0.3000
P15	all 0.2000
P20	all 0.1500

P30 all 0.1000

P100 all 0.0300

P200 all 0.0150

P500 all 0.0060

P1000 all 0.0030

The calculation of precision for the ranking was done with the help of relevance judgements provided with the test collection. It contains list of all the documents relevant to a collection. Below is the list of relevant documents for query 6.

- 6 QO CACM-1543 1
- 6 Q0 CACM-2078 1
- 6 Q0 CACM-2828 1

Precision at 10

Precision(1) = 0/1 = 0

Precision(2) = 0/2 = 0

Precision(3) = 1/3 = 0.33

Precision(4) = 1/4 = 0.25

 $Precision(5) = 2/5 = 0.4 \,$

Precision(6) = 3/6 = 0.5

Precision(7) = 3/7 = 0.429

Precision(8) = 3/8 = 0.375

$$Precision(9) = 3/9 = 0.33$$

$$Precision(10) = 3/10 = 0.3$$

where Precision(6) denotes precision at search result 6.

The Precision(10) for this query is 0.3.

Mean Average Precision

$$MAP = 1/3(1/3 + 2/5 + 3/6)$$

$$MAP = 0.41$$

Reciprocal Rank

The first relevant document is at position 3.

$$RR = 1/3$$

$$RR = 0.333$$

Normalized Discounted Cummulative Gain at 5

Relevance Score: 0, 0, 1, 0, 1

$$CG_5 = 0 + 0 + 1 + 0 + 1$$

$$CG_5 = 2$$

$$DCG = \sum_{i=1}^{5} rel_i / log_2(i+1)$$

$$DCG = 0 + 0 + 0.5 + 0 + 0.387 = 0.887$$

Table 1.1: Discounted Cummulative Gain

i
$$rel_i log_2(i+1) rel_i/log_2(i+1)$$

$$1 \quad 0 \qquad 1 \qquad \qquad 0$$

$$4 \quad 0 \qquad 2.322 \qquad 0$$

$$5 \quad 1 \quad 2.585 \quad 0.387$$

Table 1.2: Ideal Discounted Cummulative Gain

i
$$rel_i log_2(i+1) rel_i/log_2(i+1)$$

$$1 \quad 1 \qquad \qquad 1$$

$$4 \quad 0 \quad 2.322 \quad 0$$

$$5 \quad 0 \qquad 2.585 \qquad 0$$

Ideal Discounted Cummulative Gain has the document and relevance score as below:

Relevance Score: 1, 1, 0, 0, 0

$$CG_5 = 1 + 1 + 0 + 0 + 0$$

$$CG_5 = 2$$

$$IDCG = \sum_{i=1}^{5} rel_i / log_2(i+1)$$

$$IDCG = 1 + 0.631 + 0 + 0 + 0 = 1.631$$

Table 1.3: Discounted Cummulative Gain

i
$$rel_i log_2(i+1) rel_i/log_2(i+1)$$

- $1 \quad 0 \quad 1 \quad 0$
- $2 \quad 0 \quad 1.585 \quad 0$
- $3 \quad 1 \quad 2 \quad 0.5$
- 4 0 2.322 0
- 5 1 2.585 0.387
- 6 1 2.807 0.356
- 7 0 3 1
- 8 0 3.17 0
- 9 0 3.22 0
- 10 0 3.459 0

Normalized Discounted Cummulative Gain (NDCG)= DCG / IDCG

$$NDCG = 0.887/1.631 = 0.544$$

Normalized Discounted Cummulative Gain at 10

Relevance Score: 0, 0, 1, 0, 1, 1, 0, 0, 0, 0

$$CG_{10} = 0 + 0 + 1 + 0 + 1 + 1 + 0 + 0 + 0 + 0$$

$$CG_{10} = 3$$

$$DCG = \sum_{i=1}^{10} rel_i / log_2(i+1)$$

$$DCG = 0 + 0 + 0.5 + 0 + 0.387 + 0.356 + 0 + 0 + 0 + 0 = 1.243$$

Table 1.4: Ideal Discounted Cummulative Gain

i
$$rel_i log_2(i+1) rel_i/log_2(i+1)$$

1 1 1 1

2 1 1.585 0.61

 $3 \quad 1 \quad 2 \quad 0.5$

 $4 \quad 0 \quad 2.322 \quad 0$

 $5 \quad 0 \quad 2.585 \quad 0$

 $6 \quad 0 \quad 2.807 \quad 0$

7 0 3 0

8 0 3.17 0

 $9 \quad 0 \quad 3.22 \quad 0$

10 0 3.459 0

Ideal Discounted Cummulative Gain has the document and relevance score as below:

Relevance Score: 1, 1, 1, 0, 0, 0, 0, 0, 0, 0

 $CG_{10} = 3$

$$IDCG = \sum_{i=1}^{10} rel_i / log_2(i+1)$$

$$IDCG = 1 + 0.61 + 1 + 0.5 + 0 + 0 + 0 + 0 + 0 + 0 = 2.11$$

Normalized Discounted Cummulative Gain (NDCG)= DCG / IDCG

$$NDCG = 1.243/2.11 = 0.589$$

Problem 8.4

2.1 Problem Statement

For two queries in the CACM collection, generate two uninterpolated recall precision graphs, a table of interpolated precision values at standard recall levels, and the average interpolated recall-precision graph.

2.2 Solution

This problem uses CACM corpus provided in the test collection of the book. The queries ran against the CACM collection have been used from the processed queries section of the CACM test collection.

Table 2.1: Precision and Recall Table for Query 6

Index 1 2 3 7 8 9 10 6 Relevant no yes yes yes no no no no no no Recall 0 0 0.330.330.671 1 1 1 1 0.429Precision 0 0 0.330.250.40.50.3750.330.3

2.2.1 Query: Interested in articles on robotics motion planning particularly the geometric and combinatorial aspects we are not interested in the dynamics of arm motion

The below list file is result of batch search for the query from galago with number of results for each query set to 10.

- 6 Q0 CACM-0695 1 -164.66490173 galago
- 6 Q0 CACM-2826 2 -166.82664490 galago
- 6 Q0 CACM-2828 3 -167.13014221 galago
- 6 Q0 CACM-1664 4 -167.29315186 galago
- 6 Q0 CACM-1543 5 -167.67100525 galago
- 6 Q0 CACM-2078 6 -168.12095642 galago
- 6 Q0 CACM-2176 7 -168.47441101 galago
- 6 Q0 CACM-1113 8 -169.13491821 galago
- 6 Q0 CACM-0605 9 -169.25828552 galago
- 6 Q0 CACM-1517 10 -169.68901062 galago

Table 2.2: Precision and Recall Table for Query: Parallel algorithms

1 2 3 6 7 8 9 Index 5 10 Relevant no no yes no no yes no yes yes yes Recall 0.20 0 0.20.20.40.40.6 0.81 Precision 0 0 0.330.250.20.330.2860.3750.440.5

2.2.2 Query: Parallel algorithms

The below list file is result of batch search for the query from galago with number of results for each query set to 10.

- 19 Q0 CACM-2433 1 -10.82248116 galago
- 19 Q0 CACM-1811 2 -10.83561993 galago
- 19 Q0 CACM-2973 3 -10.86207390 galago
- 19 Q0 CACM-2289 4 -10.93358135 galago
- 19 Q0 CACM-0950 5 -10.96933460 galago
- 19 Q0 CACM-2266 6 -11.00977135 galago
- 19 Q0 CACM-2785 7 -11.07456684 galago
- 19 Q0 CACM-3075 8 -11.07782173 galago
- 19 Q0 CACM-3156 9 -11.13305855 galago
- 19 Q0 CACM-2664 10 -11.15161610 galago

Both the queries show their highest precision of 0.5 at recall of 1. This results in a interpolated recall-precision graph to be a straight horizontal line at precision 0.5.

Recall vs Precision Graph

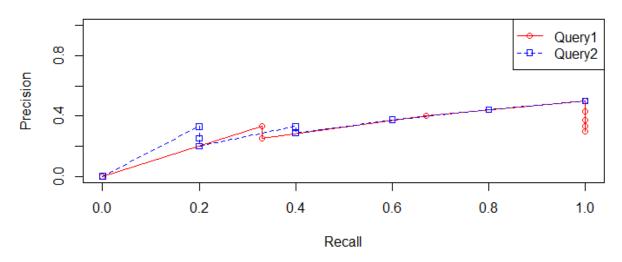


Figure 2.1: Recall vs Precision Graph

Table 2.3: Precision values at standard recall levels calculated using interpolation

Recall	0.0	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9	1	
Ranking 1	0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5	
Ranking 2	0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5	
Average Ranking	0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5	0.5	

Interpolated Recall vs Precision Graph

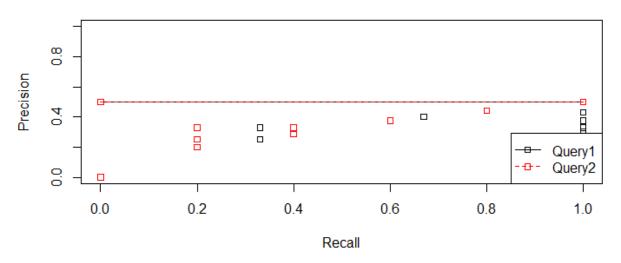


Figure 2.2: Interpolated Recall vs Precision Graph

Average Recall-Precision graph using standard recall levels

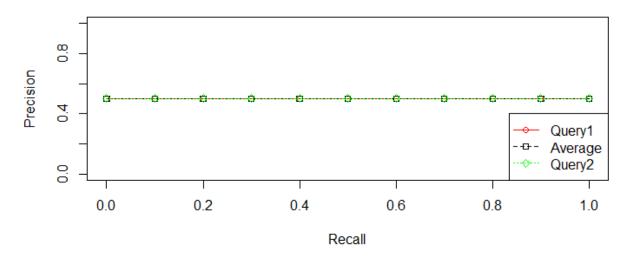


Figure 2.3: Average recall-precision graph using standard recall levels

Problem 8.5

3.1 Problem

Generate the mean average precision, recall-precision graph, average NDCG at 5 and 10, and precision at 10 for the entire CACM query set.

3.2 Solution

The results have been calculated by galago batch-search for rank result of 10. Galago provides NDCG 5 and 15 but not 10. So, by making a request for 10 results per query the NDCG15 is same as NDCG10 beacause all the calculations are based on 10 results for each query.

The values for MAP is lesser than Precision at 10 for the CACM query set. Th query sets having most of their relevant results at top indexes (between 1 and 5) have higher or equal NCDG5 and NCDG10, but for queries with most of their relevant documents lower in

the rank (between 6 and 10) have higher NCDG10 than NCDG5.

MAP for CACM Query Set

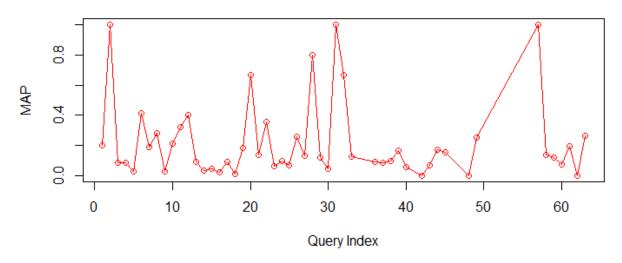


Figure 3.1: MAP values for CACM Query Set

NCDG5 for CACM Query Set

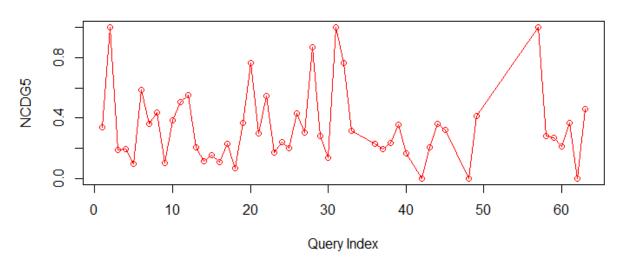


Figure 3.2: NCDG5 values for CACM Query Set

NCDG10 for CACM Query Set

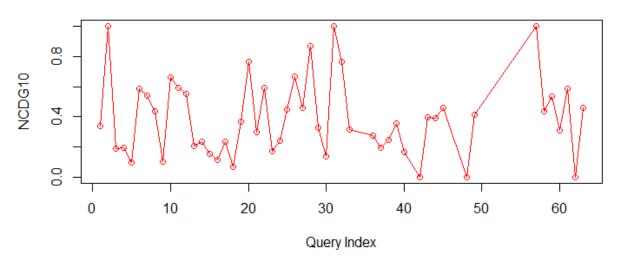


Figure 3.3: NCDG10 values for CACM Query Set

P10 for CACM Query Set

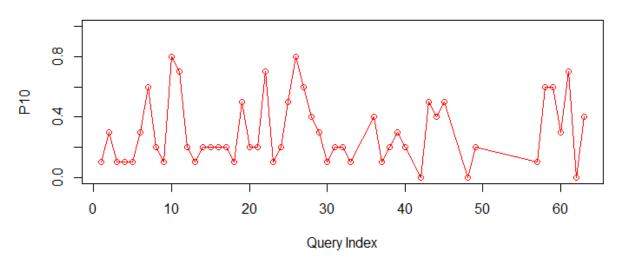


Figure 3.4: Precision at 10 values for CACM Query Set

Recall for CACM Query Set

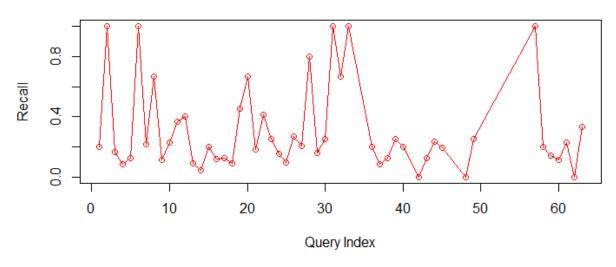


Figure 3.5: Recall values for CACM Query Set

Recall vs Precision for CACM Query Set

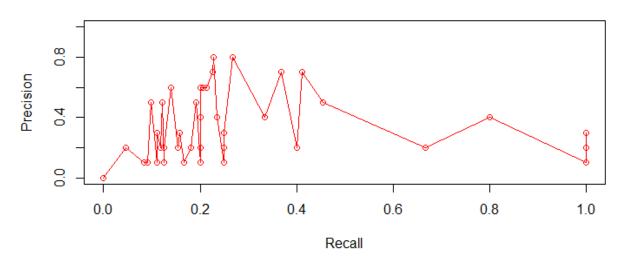


Figure 3.6: Recall vs Precision for CACM Query Set

Problem 8.7

4.1 Problem

Another measure that has been used in a number of evaluations is R-precision. This is defined as the precision at R documents, where R is the number of relevant documents for a query. It is used in situations where there is a large variation in the number of relevant documents per query. Calculate the average R-precision for the CACM query set and compare it to the other measures.

4.2 Solution

R-precision is defined as precision at R documents, where R is the number of relevant documents for a query. In context to the CACM query set, the relevance judgements file suggests that all the queries have varied number of relevant documents. It ranges from 0 to 51. So,

Table 4.1: CACM Query Set measured against different measures

map	0.2840
ndcg	0.4419
ndcg15	0.4734
R-prec	0.3192
bpref	0.0000
recip_rank	0.7296
P5	0.3922
P10	0.2980
P15	0.2614
P20	0.2373
P30	0.1843

for calculating R-precision number of relevant documents per query is set to 51 and evaluated in the galago. The results for the different measures inclusive of R-precision at relevant document 51 are above in the table:

Problem 8.9

5.1 Problem

For one query in the CACM collection, generate a ranking and calculate BPREF. Show that the two formulations of BPREF give the same value.

5.2 Solution

The solution is based on relevance results for query, interested in articles on robotics motion planning particularly the geometric and combinatorial aspects we are not interested in the dynamics of arm motion. The Table 5.1 shows the relevance results for the query. The relevance results show the search results had 3 relevant documents and 7 non- relevant documents.

6 Q0 CACM-0695 1 -164.66490173 galago

- 6 Q0 CACM-2826 2 -166.82664490 galago
- 6 Q0 CACM-2828 3 -167.13014221 galago
- 6 Q0 CACM-1664 4 -167.29315186 galago
- 6 Q0 CACM-1543 5 -167.67100525 galago
- 6 Q0 CACM-2078 6 -168.12095642 galago
- 6 Q0 CACM-2176 7 -168.47441101 galago
- 6 Q0 CACM-1113 8 -169.13491821 galago
- 6 Q0 CACM-0605 9 -169.25828552 galago
- 6 Q0 CACM-1517 10 -169.68901062 galago

5.2.1 Calculating BPREF

$$BPREF = 1/R \sum_{d_r} (1 - (N_{d_r}/min(R, N)))$$

where R is the number of relevant documents that are considered

N is the number of non-relevant documents that are considered

 d_r is the number of relevant documents

For a query result with 3 relevant documents R is 3 implying that first 3 non-relevant documents are considered. The relevance table for the query is manipulated for BPREF as,

$$BPREF = 1/R \sum_{d_r} (1 - (N_{d_r}/min(R, N)))$$

$$BPREF = 1/3[(1 - 2/3) + (1 - 3/3) + (1 - 3/3)]$$

Table 5.1: Relevance table showing R relevant and non-relevant documents

Index Relevance
No
No
No
Yes
No
Yes
Yes
Yes
Yes

$$BPREF = 1/3[(1/3) + 0 + 0] = 3/8 = 0.11$$

5.2.2 Calculating BPREF based on preference

BPREF = P/(P+Q)

where P is the number of relevant documents

Q is the number of non-relevant documents

For query: Code optimization for space efficiency

P = 3

Q = 3

BPREF = 3/(3+3)

BPREF = 0.5

The value of BPREF is 0.11 and 0.3 by computing respectively with relevant documents

formula and the clickthrough preference formula. The values computed are not equal because the bpref for clickthough formula does not take into account the ranking of relevant results and the value for BPREF with relevant documents formula dips due to the fist relevant result showing after two non-relevant result and the rest two relevant result appear after all the non-relevant documents taken in consideration. Thus, the last we relevant documents do not add any value to the BPREF.

Problem 9.8

6.1 Problem

Cluster the following set of two-dimensional instances into three clusters using each of the five agglomerative clustering methods: (4, 2), (3, 2), (2, 2), (1, 2), (1, 1), (1, 1), (2, 3), (3, 2), (3, 4), (4, 3) Discuss the differences in the clusters across methods. Which methods produce the same clusters? How do these clusters compare to how you would manually cluster the points?

6.2 Solution

The code for agglomerate clustering methods generates 3 clusters for the data set.

6.2.1 Discussion of the Methods

Single Linkage: It uses the minimum distance between between elements of two clusters to merge them as one cluster. For two clusters A and B, it finds the minimum euclidean distance between the points of each cluster and compares them against the minimum threshold distance of all the other clusters to merge them in one cluster. The disadvantage of this approach is that it does not consider how far spread each cluster is and focusing only on the minimum distance between the clusters to merge them.

Complete Linkage: It uses the maximum distance between elements of two clusters to merge them as one cluster. For two clusters A and B, it finds the maximum euclidean distance between the points of each cluster and compares them against the minimum distance of all the other clusters to merge them in one cluster. This approach creates a more comapact and less spread cluster than single linkage clustering technique.

Average Clustering: It uses average distance of all the elements between two clusters to merge them as one cluster. For two clusters A and B, it finds the average distance by calculating the euclidean distance between all the points in each cluster and dividing them by the number of elements in each cluster. The average distance calculated is compared against average distance of other clusters to merge the minimum average distance clusters in to one cluster. The type of cluster formed by average linkage depend heavily on the structure of clusters, since it is based on the average distance between all the elements in the two clusters.

Average Group Clustering: It uses centroid distance between teo clusters to merge them as one cluster. For two clusters A and B, it finds the centroid of the two clusters and merges them together by comparing against the centroid distances of other clusters. It forms similar clusters to the average linkage clusters.

Ward's Method: It uses sum of variance between two clusters to merge them as one cluster. It forms minimum spread clusters around the centroid of the cluster.

```
return minDistance
15
16
  def agglomerativeSingleLinkageCluster(clusterValue, clusterPoints):
18
      distanceMatrix = []
19
      finalClusters = []
20
21
      for i in range(0,len(clusterPoints)):
22
           finalClusters.append([i])
23
24
      for c in range (len (cluster Points), cluster Value, -1):
25
           bestClusterA = []
26
           bestClusterB = []
27
           bestCost = math.inf
28
           for i in range(0,len(clusterPoints)):
               temp = []
30
               for j in range(0,len(clusterPoints)):
                   temp.append(0)
               distanceMatrix.append(temp)
           for i in range(0,len(clusterPoints)):
               for j in range((i+1),len(clusterPoints)):
36
                   distance = singleLinkage(clusterPoints[i], clusterPoints[j])
37
                   distanceMatrix[i][j] = (distance)
38
                   if bestCost > distance:
39
                        bestCost = distance
40
```

```
if bestClusterA and bestClusterB:
41
                           bestClusterA.pop()
                           bestClusterB.pop()
                       bestClusterA.append(clusterPoints[i])
44
                       bestClusterB.append(clusterPoints[j])
45
          clusterPoints.remove(bestClusterB[0])
46
          index = clusterPoints.index(bestClusterA[0])
47
          for x in range(0,len(bestClusterB[0])):
48
               clusterPoints [index].append(bestClusterB[0][x])
49
      return (clusterPoints)
50
  def completeLinkage(clusterPointA, clusterPointB):
      maxDistance = 0
53
      for i in range(0, len(clusterPointA)):
54
          for j in range(0,len(clusterPointB)):
               distance = math.sqrt(math.pow((clusterPointA[i][0]-clusterPointB[j
56
     [[0]],2) + math.pow((clusterPointA[i][1]-clusterPointB[j][1]),2))
               if maxDistance < distance:
57
                   maxDistance = distance
      return maxDistance
  def agglomerativeCompleteLinkageCluster(clusterValue, input):
62
      distanceMatrix = []
63
      finalClusters = []
64
65
```

```
clusterPoints = input
66
      for i in range(0,len(clusterPoints)):
           finalClusters.append([i])
69
      for c in range (len (cluster Points), cluster Value, -1):
70
           bestClusterA = []
71
           bestClusterB = []
72
           bestCost = 0
73
           for i in range(0,len(clusterPoints)):
74
               temp = []
75
               for j in range(0,len(clusterPoints)):
                   temp.append(0)
77
               distanceMatrix.append(temp)
79
           for i in range(0,len(clusterPoints)):
80
               for j in range((i+1),len(clusterPoints)):
81
                   distance = completeLinkage(clusterPoints[i], clusterPoints[j])
                   distanceMatrix[i][j] = (distance)
                   if bestCost < distance:</pre>
                        bestCost = distance
                        if bestClusterA and bestClusterB:
                            bestClusterA.pop()
87
                            bestClusterB.pop()
88
                        bestClusterA.append(clusterPoints[i])
89
                        bestClusterB.append(clusterPoints[j])
90
           clusterPoints.remove(bestClusterB[0])
91
```

```
index = clusterPoints.index(bestClusterA[0])
92
            for x in range(0,len(bestClusterB[0])):
                 clusterPoints[index].append(bestClusterB[0][x])
       return (clusterPoints)
96
   \begin{array}{lll} \textbf{def} & average Linkage (\ cluster Point A\ , & cluster Point B\ ): \end{array}
       averageDistance = 0
98
       for i in range(0, len(clusterPointA)):
99
            for j in range(0,len(clusterPointB)):
100
                 averageDistance = averageDistance + math.sqrt(math.pow((
101
       clusterPointA[i][0] - clusterPointB[j][0]),2) + math.pow((clusterPointA[i
       [1] - cluster Point B [j][1], [2]
       averageDistance = averageDistance/(len(clusterPointA) +len(clusterPointB))
102
       return averageDistance
103
104
105
   def agglomerativeAverageLinkageCluster(clusterValue, clusterPoints):
107
       distanceMatrix = []
108
        finalClusters = []
109
110
       for i in range(0,len(clusterPoints)):
111
            finalClusters.append([i])
113
        for c in range (len (cluster Points), cluster Value, -1):
114
            bestClusterA = []
115
```

```
bestClusterB = []
116
           bestCost = math.inf
           for i in range(0,len(clusterPoints)):
               temp = []
119
               for j in range(0,len(clusterPoints)):
120
                    temp.append(0)
               distanceMatrix.append(temp)
           for i in range(0,len(clusterPoints)):
124
               for j in range ((i+1), len (cluster Points)):
                    distance = averageLinkage(clusterPoints[i], clusterPoints[j])
                    distanceMatrix[i][j] = (distance)
127
                    if bestCost > distance:
128
                        bestCost = distance
129
                        if bestClusterA and bestClusterB:
130
                            bestClusterA.pop()
131
                            bestClusterB.pop()
                        bestClusterA.append(clusterPoints[i])
133
                        bestClusterB.append(clusterPoints[j])
           clusterPoints.remove(bestClusterB[0])
           index = clusterPoints.index(bestClusterA[0])
136
           for x in range(0,len(bestClusterB[0])):
137
               clusterPoints [index].append(bestClusterB[0][x])
138
       return (clusterPoints)
139
140
def averageGroupLinkage(clusterPointA, clusterPointB):
```

```
centroidX_A = 0
142
        centroidY_A = 0
143
        centroidX_B = 0
144
        centroidY_B = 0
145
        centroidA = []
146
        centroidB = []
147
        for i in range(0, len(clusterPointA)):
148
            centroidX_A = centroidX_A + clusterPointA[i][0]
149
            centroidY_A = centroidY_A + clusterPointA[i][1]
        centroid A. append (centroid X_A/(len(cluster Point A)))
151
        centroidA.append(centroidY_A/(len(clusterPointA)))
152
        for j in range (0, len (clusterPointB)):
153
            centroidX_B = centroidX_B + clusterPointB[j][0]
154
            centroidY_B = centroidY_B + clusterPointB[j][1]
155
        centroidB.append(centroidX_B/(len(clusterPointB)))
156
        centroidB.append(centroidY_B/(len(clusterPointB)))
157
                              \operatorname{math.sqrt}(\operatorname{math.pow}((\operatorname{centroidA}[0] - \operatorname{centroidB}[0]), 2) +
        clusterDistance =
158
       math.pow((centroidA[1]-centroidB[1]),2))
        return clusterDistance
159
160
161
   def agglomerativeAverageGroupLinkageCluster(clusterValue, clusterPoints):
162
163
        distanceMatrix = []
164
        finalClusters = []
165
166
```

```
for i in range(0,len(clusterPoints)):
167
            finalClusters.append([i])
169
       for c in range (len (cluster Points), cluster Value, -1):
170
            bestClusterA = []
171
            bestClusterB = []
172
            bestCost = math.inf
173
            for i in range(0,len(clusterPoints)):
174
                temp = []
                for j in range (0, len (cluster Points)):
176
                    temp.append(0)
177
                distanceMatrix.append(temp)
178
179
            for i in range(0,len(clusterPoints)):
180
                for j in range((i+1),len(clusterPoints)):
181
                    distance = averageGroupLinkage(clusterPoints[i], clusterPoints
182
       [j])
                    distanceMatrix[i][j] = (distance)
183
                    if bestCost > distance:
                         bestCost = distance
185
                         if bestClusterA and bestClusterB:
186
                             bestClusterA.pop()
187
                             bestClusterB.pop()
188
                         bestClusterA.append(clusterPoints[i])
189
                         bestClusterB.append(clusterPoints[j])
190
            clusterPoints.remove(bestClusterB[0])
191
```

```
index = clusterPoints.index(bestClusterA[0])
192
             for x in range(0,len(bestClusterB[0])):
                 clusterPoints [index].append(bestClusterB[0][x])
194
        return (clusterPoints)
195
196
   def wardMethod(clusterPointA, clusterPointB):
197
        centroidX_A = 0
198
        centroidY_A = 0
199
        centroidX_B = 0
200
        centroidY_B = 0
201
        centroidA = []
202
        centroidB = []
203
        for i in range (0, len (clusterPointA)):
204
             centroidX_A = centroidX_A + clusterPointA[i][0]
205
             centroidY_A = centroidY_A + clusterPointA[i][1]
206
        centroid A. append (centroid X_A / (len (cluster Point A)))
207
        centroid A. append (centroid Y_A / (len (cluster Point A)))
208
        for j in range(0,len(clusterPointB)):
209
             centroidX_B = centroidX_B + clusterPointB[j][0]
210
             centroidY_B = centroidY_B + clusterPointB[j][1]
211
        centroidB.append(centroidX_B/(len(clusterPointB)))
        centroidB.append(centroidY_B/(len(clusterPointB)))
213
                               \operatorname{math.sqrt}(\operatorname{math.pow}((\operatorname{centroidA}[0] - \operatorname{centroidB}[0]), 2) +
        clusterDistance =
214
       \operatorname{math.pow}((\operatorname{centroidA}[1] - \operatorname{centroidB}[1]), 2))
        variance = len(clusterPointA)* len(clusterPointB)* clusterDistance/ len(
215
       clusterPointA)+ len(clusterPointB)
```

```
return variance
216
   def agglomerativeWardMethod(clusterValue, clusterPoints):
220
       distanceMatrix = []
221
       finalClusters = []
222
223
       for i in range(0,len(clusterPoints)):
224
           finalClusters.append([i])
225
226
       for c in range (len (cluster Points), cluster Value, -1):
227
           bestClusterA = []
228
           bestClusterB = []
229
           bestCost = math.inf
230
           for i in range(0,len(clusterPoints)):
231
                temp = []
                for j in range(0,len(clusterPoints)):
                    temp.append(0)
                distanceMatrix.append(temp)
235
236
           for i in range(0,len(clusterPoints)):
237
                for j in range((i+1),len(clusterPoints)):
238
                    distance = wardMethod(clusterPoints[i], clusterPoints[j])
239
                    distanceMatrix[i][j] = (distance)
240
                    if bestCost > distance:
241
```

```
bestCost = distance
242
                        if bestClusterA and bestClusterB:
                            bestClusterA.pop()
                            bestClusterB.pop()
245
                        bestClusterA.append(clusterPoints[i])
246
                        bestClusterB.append(clusterPoints[j])
247
           clusterPoints.remove(bestClusterB[0])
248
           index = clusterPoints.index(bestClusterA[0])
249
           for x in range (0, len (bestClusterB[0])):
250
                clusterPoints [index]. append (bestClusterB[0][x])
251
       return (clusterPoints)
252
253
  def main():
254
       clusters = 3
255
       256
      1]], [[2, 3]], [[3, 2]], [[3, 4]], [[4,3]]]
       file = open("ClusteringOutput.txt", "w")
257
       clusterPointsSingle = agglomerativeSingleLinkageCluster(clusters,input)
       file.write("Single Linkage" + "\n")
259
       for i in range (0, len (cluster Points Single)):
260
           file.write("Cluster " + str(i+1) + ": " + str(clusterPointsSingle[i]) +
261
       "\n")
        \text{inputComplete } = \! [[[-4 \,, \ -2]] \,, \ [[-3 \,, \ -2]] \,, \ [[-2 \,, \ -2]] \,, \ [[-1 \,, \ -2]] \,, \ [[1 \,, \ -1]] \,, \\
262
       [[1, 1]], [[2, 3]], [[3, 2]], [[3, 4]], [[4,3]]]
       clusterPointsComplete = agglomerativeCompleteLinkageCluster(clusters,
263
      inputComplete)
```

```
file . write ("\nComplete Linkage\n")
264
                           for i in range(0, len(clusterPointsComplete)):
265
                                           file . write ("Cluster" + str(i+1) + ": "+str(clusterPointsComplete[i])
266
                           + "\n")
                           inputAverage = [[[-4, -2]], [[-3, -2]], [[-2, -2]], [[-1, -2]], [[1, -1]],
267
                            [[1, 1]], [[2, 3]], [[3, 2]], [[3, 4]], [[4,3]]]
                           clusterPointsAverage = agglomerativeAverageLinkageCluster(clusters,
268
                        inputAverage)
                            file . write ("\nAverage Linkage\n")
269
                           for i in range (0, len (clusterPointsAverage)):
270
                                            file . write ("Cluster" + str(i+1) + ": " + str(clusterPointsAverage[i])+
271
                            "\n")
                           inputAverageGroup \, = \, \left[ \left[ \left[ \, -4 \, , \, -2 \right] \right], \, \left[ \left[ \, -3 \, , \, -2 \right] \right], \, \left[ \left[ \, -2 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, 1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, -2 \right] \right], \, \left[ \left[ \, -1 \, , \, 
272
                         [-1], [[1, 1]], [[2, 3]], [[3, 2]], [[3, 4]], [[4, 3]]
                           clusterPointsAverageGroup = agglomerativeAverageGroupLinkageCluster(
273
                         clusters ,inputAverageGroup)
                           file.write("\nAverage Group Linkage\n")
274
                           for i in range(0, len(clusterPointsAverageGroup)):
275
                                           file . write ("Cluster" + str(i+1) + ": "+str(clusterPointsAverageGroup
276
                         [i])+ "\n")
                          inputWard = [[[-4, -2]], [[-3, -2]], [[-2, -2]], [[-1, -2]], [[1, -1]],
277
                         [[1, 1]], [[2, 3]], [[3, 2]], [[3, 4]], [[4,3]]]
                           clusterPointsWard = agglomerativeWardMethod(clusters,inputWard)
278
                            file . write ("\nWard's Algorithm Linkage\n")
279
                           for i in range(0, len(clusterPointsWard)):
280
```

Single Linkage

Cluster 1: [[-4, -2], [-3, -2], [-2, -2], [-1, -2]]

Cluster 2: [[1, -1], [1, 1]]

Cluster 3: [[2, 3], [3, 2], [3, 4], [4, 3]]

Complete Linkage

Cluster 1: [[-4, -2], [4, 3], [3, 4], [-3, -2], [3, 2], [-2, -2], [2, 3], [-1, -2]]

Cluster 2: [[1, -1]]

Cluster 3: [[1, 1]]

Average Linkage

Cluster 1: [[-4, -2], [-3, -2], [-2, -2], [-1, -2]]

Cluster 2: [[1, -1], [1, 1]]

Cluster 3: [[2, 3], [3, 2], [3, 4], [4, 3]]

Average Group Linkage

Cluster 1: [[-4, -2], [-3, -2], [-2, -2], [-1, -2]]

Cluster 2: [[1, -1], [1, 1]]

Cluster 3: [[2, 3], [3, 2], [3, 4], [4, 3]]

Ward's Algorithm Linkage

Cluster 1: [[-4, -2], [-3, -2], [-2, -2], [-1, -2]]

Cluster 2: [[1, -1], [1, 1]]

Cluster 3: [[2, 3], [3, 2], [3, 4], [4, 3]]

6.2.2 Clustering Results vs Mannual Clustering

All the agglomerate clustering techniques except for complete linkage technique produced the same result for the provided dataset. The results of the clusters formed by all the clustering methods has been shown above.

Mannual Clustering of the data points on euclidean distance results in the same clusters generated by agglomerative clustering.

Cluster 1: (-4,-2), (-3,-2), (-2,-2), (-1,-2)

Cluster 2: (1,-1), (1,1)

Cluster 3: (2,3), (3,2), (3,4), (4,3)

Cluster 1 is easy to create due to it being far away from other data points. Cluster 2 and 3 have a close margin where the distance between point (1,1) and (-1,1) is equal to 2 and the distance between point (1,1) and (2,3) is $\sqrt{5}$. Therefore the points (1,1) and (-1,1) have been clustered together as Cluster 2.

If the data points are clustered on the basis of the quadrants they lie in:

Cluster 1: 1st Quadrant— > (-4,-2), (-3,-2), (-2,-2), (-1,-2)

Cluster 2: 3rd Quadrant ->(1,-1)

Cluster 3: 4th Quadrant -> (1,1), (2,3), (3,2), (3,4), (4,3)

Chapter 7

9.9

7.1 Problem

Use K-means and spherical K-means to cluster the data points in Exercise 9.8. How do the clusterings differ?

7.2 Solution

```
created on Nov 24, 2017

author: nauman

comport numpy as np
from sklearn.cluster import KMeans
```

```
8 from spherecluster import SphericalKMeans
 def kMeans(num):
11
     file = open("Kmeans.txt", "a+")
12
     13
     [2, 3], [3, 2], [3, 4], [4,3]
     kmeans = KMeans(n_clusters=num, random_state=0).fit(input)
14
     file.write("K means output for cluster size: "+ str(num) + "\n")
     file.write("Clusters index of points" + "\n")
16
     file.write(str(kmeans.labels_) + "\n")
17
     file . write ("Center of Clusters \n")
18
     file.write(str(kmeans.cluster\_centers\_) + "\n")
19
     file.close()
20
21
  def sphericalKMeans(num):
22
     num = 4
23
     file = open("Kmeans.txt", "a+")
24
     [2, 3], [3, 2], [3, 4], [4,3]]
     kmeans = SphericalKMeans(n_clusters=num).fit(input)
     file.write("Spherical K means output for cluster size : "+ str(num) + "\n"
27
    )
     file.write("Clusters index of points" + "\n")
28
     file . write (str(kmeans.labels_+) + "\n")
29
     file . write ("Center of Clusters \n")
30
```

```
file.write(str(kmeans.cluster_centers_) + "\n")
31
      file.close()
35 kMeans (4)
36 sphericalKMeans (4)
  K means output for cluster size : 3
  Clusters index of points
  [2 2 2 2 0 0 1 1 1 1]
  Center of Clusters
  [[ 1.0000000e+00
                      5.55111512e-17]
   [ 3.00000000e+00 3.00000000e+00]
   [ -2.50000000e+00 -2.00000000e+00]]
  Spherical K means output for cluster size : 4
  Clusters index of points
  [3 3 3 1 2 0 0 0 0 0]
  Center of Clusters
  [[ 0.70710678  0.70710678]
   [-0.4472136 -0.89442719]
   [ 0.70710678 -0.70710678]
   [-0.81836024 -0.57470559]]
  K means output for cluster size : 2
```

Clusters index of points

[0 0 0 0 0 1 1 1 1 1]

Center of Clusters

[[-1.8 -1.8]

[2.6 2.6]]

Spherical K means output for cluster size : 4

Clusters index of points

[3 3 3 0 2 1 1 1 1 1]

Center of Clusters

[[-0.4472136 -0.89442719]

[0.70710678 0.70710678]

[0.70710678 -0.70710678]

[-0.81836024 -0.57470559]]

K means output for cluster size : 4

Clusters index of points

[2 2 0 0 3 3 1 1 1 1]

Center of Clusters

[[-1.50000000e+00 -2.00000000e+00]

[3.00000000e+00 3.00000000e+00]

[-3.50000000e+00 -2.00000000e+00]

[1.00000000e+00 5.55111512e-17]]

Table 7.1: Index to Data Point relation

Index 0 1 2 3 4 5 6 7 8 9

Data Point (-4, -2) (-3, -2) (-2, -2) (-1, -2) (1, -1) (1, 1) (2, 3) (3, 2) (3, 4) (4, 3)

Spherical K means output for cluster size : 4

Clusters index of points

[3 3 3 1 2 0 0 0 0 0]

Center of Clusters

[[0.70710678 0.70710678]

[-0.4472136 -0.89442719]

[0.70710678 -0.70710678]

[-0.81836024 -0.57470559]]

The output of the code shows clusters on the basis of the index of data points and center of each cluster. Table 5.1 shows the index to data point relationship. The results for cluster size 2,3 and 4 are show for both the clustering techniques.

The clusters formed by K-means for cluster size 3 are same as the clusters formed by Single Linkage, Average Linkage and Average Group Linkage from the problem 9.8. The clusters formed by spherical K-means for cluster 3 is different from K-means due to the difference between finding similarity between points for clustering. K-means uses euclidean distance to find similarity while spherical K-mean uses cosine similarity to cluster items together. Spherical K-means clusters items on which fall in the ame quadrant approach discussed in the previous problem.

Chapter 8

Problem 9.11

8.1 Problem

The K nearest neighbors of a document could be represented by links to those documents.

Describe two ways this representation could be used in a search application.

8.2 Solution

The primary advantage of K nearest neighbor comapared to K means and agglomerative clustering techniques is that a document can be present in multiple clusters unlike the K means and agglomerative clustering technique where each documents is in a single cluster.

The K nearest neighbors of a documents can be used for tell-text search in search application. All the documents in the corpus can be clustered by K nearest neighbour. The

document can be in multiple clusters based on the features extracted from the cluster. For a corpus of documents containing sports news from USA, it can be classified into multiple clusters as football, baseball, basketball, athletics, Olympics, CONCAF Cup etc. A document that is in cluster soccer can simultaneously be clustered with Olympics and CONCAF Cup. Similarly the queries to the documents can also be clustered on the basis of its features. It presents all the documents that are in the cluster soccer for a query of feature soccer. The same set of documents can also be recalled if the query is about CONCAF Cup. It allows for relavant search results.

The K nearest neighbors can also be used for showing clustered search results. It can be helped to refine a very generic query to a more precise query to return relevant result. For example, a system that employs K nearest neighbor clustering on its queries. For a user input query apple, it will show all the possible clusters where the query term apple appears. For apple, it can be a fruit, it can be the company Apple, it can be products of Apple Company etc. A user on the basis of suggestions can select the particular suggestion to find search results that fall under the specified feature cluster.