Supplemental information for `neonSoilFlux`: An R Package for Continuous Sensor-Based Estimation of Soil CO_2 Fluxes

1 Assessment of data gaps

For a given half-hourly time period, the `neonSoilFlux` packages assigns a QA flag for a measurement if more one values across all measurement depths uses gap-filled data (Section 4.2.1 of the main text). Panel a of Figure S1 reports the proportion of gap-filled data for all input environmental measurements at each site during the period when field measurements were made. Soil fluxes are computed from 4 different types of input measurements (T_S, SWC, P, and CO_2), any of which could have a QA flag in a half-hourly interval. Panel b of Figure S1 displays at each site the distribution of the number of different gap-filled measurements used to compute a half-hourly flux. The largest cause of measurements needing to be gap-filled was missing or flagged soil moisture data. Calculating fluxes for WOOD, WREF, and SJER required using the largest proportion of gap-filled measurements, due to flagged or missing SWC and CO_2 data.

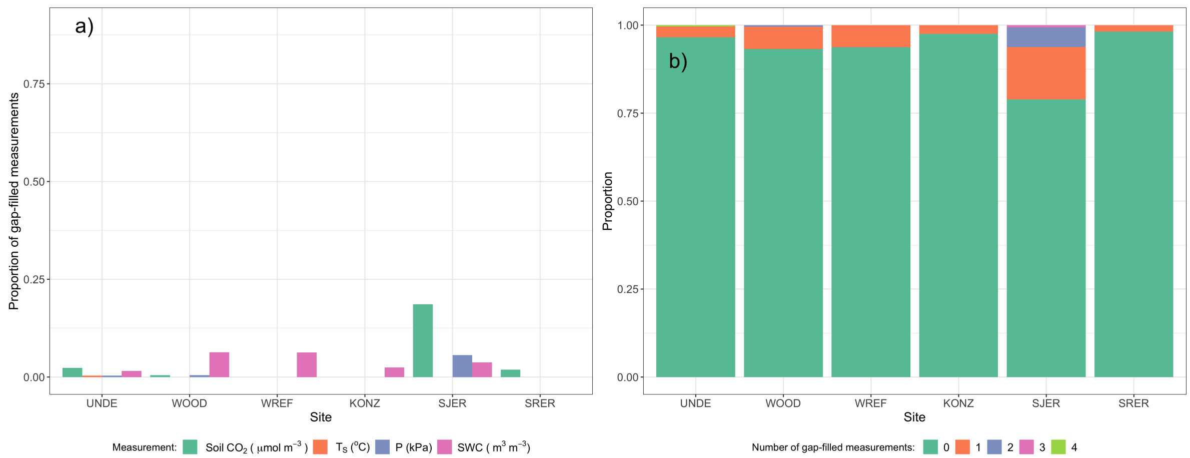

Figure S1: Panel a) Proportion of input gap-filled environmental measurements used to generate F_S from the `neonSoilFlux` package, by study site. Panel b) distribution of the usage of gap-filled measurements at each site.

2 Assessing the signal to noise ratio (SNR) and evaluating estimated uncertainties

Following collection of field measurements and calculation of the soil fluxes from `neonSoilFlux` package, we compared measured F_S based on closed-dynamic chamber measurements with the LI-COR instruments to a given soil flux calculation from `neonSoilFlux` for each site and flux computation method. Beyond the model statistics defined in the main text, we computed the signal to noise ratio (SNR), defined as the ratio of a modeled soil flux (F_{ijk}) from `neonSoilFlux` to its quadrature uncertainty (σ_{ijk}).

We observed that the range of values (*e.g.* $F_{ijk} \pm \sigma_{ijk}$ was much larger than the measured field flux. We evaluated $|F_S - F_{ijk}| < (1-\epsilon)\sigma_{ijk}$, where F_S is a measured field soil flux from the LI-COR 6800 (as the LI-COR 870/8250 was used at only three sites in 2024 but the 6800 was used at all sites in both years). The parameter ϵ was an uncertainty reduction factor to evaluate how much the quadrature uncertainty could be reduced while maintaining precision between modeled F_{ijk} and measured F_S.

The computed signal to noise ratio (SNR) and the proportion of measured field fluxes within the modeled uncertainty for a given flux computation method F_{ijk} suggest that there was substantial variability in the agreement between the gradient method and field-measured observations (Figure S2). Here, values of SNR greater than unity (vertical dashed lines in Figure S2) indicate lower reported uncertainty, as propagated by quadrature due to a relatively higher precision of measured input variables (CO_2, T_S, SWC, or P).

The sensitivity to an uncertainty reduction factor (ϵ, bottom panels in Figure S2) demonstrates how concordance between measured and modeled fluxes would be affected if environmental measurement uncertainty σ_{ijk} were to decrease. As ϵ increases from left to right in each figure, the possible range of values for each predicted flux value decreases and the proportion of measured fluxes that fall within that range also decreases.

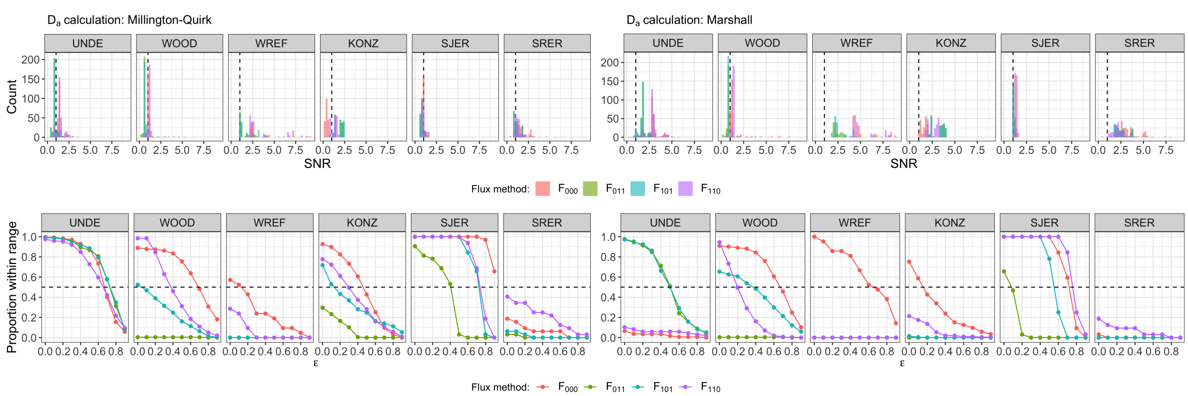

Figure S2: Top panels: distribution of SNR values across each of the different sites for modeled effluxes from the `neonSoilFlux` package, depending on the diffusivity calculation used (Millington-Quirk or Marshall, Section 3.2.2 of the main text). Dashed lines indicate a signal to noise ratio of 1. Bottom panels: Proportion of measured F_S within the modeled range of a flux computation method F_{ijk} given an uncertainty reduction factor ϵ, or $|F_S - F_{ijk}| < (1-\epsilon)\sigma_{ijk}$.