# **Explanations for Multinomial Classifiers**

Tips and Tricks for Practitioners

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### **Abstract**

# 1 Introduction

This short discussion bookends popular and practical texts on machine learning explanations by Chaudhary, Gill, Hall et al by specifically addressing the common and somewhat vexing problem of explaining the behavior and predictions of multinomial classifiers [7], [6], [2].

# 2 Notation

To facilitate technical descriptions of explanatory techniques, notation for input and output spaces, datasets, and models is defined.

### 2.1 Spaces

- Input features come from the set  $\mathcal{X}$  contained in a P-dimensional input space,  $\mathcal{X} \subset \mathbb{R}^P$ .
- Known labels corresponding to instances of  $\mathcal{X}$  come from the set  $\mathcal{Y}$  contained in a C-dimensional input space,  $\mathcal{Y} \subset \mathbb{R}^C$ .
- Learned output responses come from the set  $\hat{\mathcal{Y}}$ . For classification models the set  $\hat{\mathcal{Y}}$  typically contains a column vector for each unique class in  $\mathcal{Y}$ . In this text, the space  $\hat{\mathcal{Y}}$  is said to be contained in a C'-dimensional output space,  $\hat{\mathcal{Y}} \subset \mathbb{R}^{C'}$ .

### 2.2 Datasets

- The input dataset X is composed of observed instances of the set  $\mathcal{X}$  with a corresponding dataset of labels Y, observed instances of the set  $\mathcal{Y}$ .
- Each i-th observation of  $\mathbf{X}$  is denoted as  $\mathbf{x}^{(i)} = [x_0^{(i)}, x_1^{(i)}, \dots, x_{P-1}^{(i)}]$ , with corresponding i-th labels in  $\mathbf{Y}, \mathbf{y}^{(i)} = [y_0^{(i)}, y_1^{(i)}, \dots, y_{C-1}^{(i)}]$ , and corresponding predictions in  $\hat{\mathbf{Y}}, \hat{\mathbf{y}}^{(i)} = [\hat{y}_0^{(i)}, \hat{y}_1^{(i)}, \dots, \hat{y}_{C-1}^{(i)}]$ .
- $\mathbf{X}$  and  $\mathbf{Y}$  consist of N tuples of observations:  $[(\mathbf{x}^{(0)}, \mathbf{y}^{(0)}), (\mathbf{x}^{(1)}, \mathbf{y}^{(1)}), \dots, (\mathbf{x}^{(N-1)}, \mathbf{y}^{(N-1)})].$
- ullet Each j-th input column vector of  ${\bf X}$  is denoted as  $X_j = [x_j^{(0)}, x_j^{(1)}, \dots, x_j^{(N-1)}]^T.$

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#### 2.3 Models

- A type of machine learning model g, selected from a hypothesis set H, is trained to represent
  an unknown signal-generating function f observed as X with labels Y using a training
  algorithm A:
- g generates learned output responses on the input dataset  $g(\mathbf{X}) = \hat{\mathbf{Y}}$ , and on the general input space  $g(\mathcal{X}) = \hat{\mathcal{Y}}$ .
- The model to be explained is denoted as g.

# 3 Global Analysis

#### 3.1 Data

Subsequent sections will use simulated data that empirically demonstrates the desired relationships between input feature importance and interactions in the input space  $\mathbf{X}$ , the label space  $f(\mathbf{X}) = \mathbf{Y}$ , a GBM model to be explained  $g_{\text{GBM}}$ , and a decision tree surrogate  $h_{\text{tree}}$ . Data with a known signal-generating function depending on four input features with interactions and with eight noise features is simulated such that:

$$f = \text{num}_1 * \text{num}_4 + |\text{num}_8| * \text{num}_9^2 + e \tag{1}$$

 $g_{\mathrm{GBM}}$  is trained:  $\mathbf{X}, \mathbf{f}(\mathbf{X}) \xrightarrow{\mathcal{A}} g_{\mathrm{GBM}}$  such that  $g_{\mathrm{GBM}} \approx f$ . Then  $h_{\mathrm{tree}}$  is extracted by  $\mathbf{X}, g_{\mathrm{GBM}}(\mathbf{X}) \xrightarrow{\mathcal{A}} h_{\mathrm{tree}}$ , such that  $h_{\mathrm{tree}}(\mathbf{X}) \approx g_{\mathrm{GBM}}(\mathbf{X}) \approx f(\mathbf{X})$ .

# 3.2 Decision Tree Surrogate

Given a learned function g, a set of learned output responses  $g(\mathbf{X}) = \hat{\mathbf{Y}}$ , and a tree splitting and pruning approach  $\mathcal{A}$ , a global – or over all  $\mathbf{X}$  – surrogate decision tree  $h_{\text{tree}}$  can be extracted such that  $h_{\text{tree}}(\mathbf{X}) \approx g(\mathbf{X})$ :

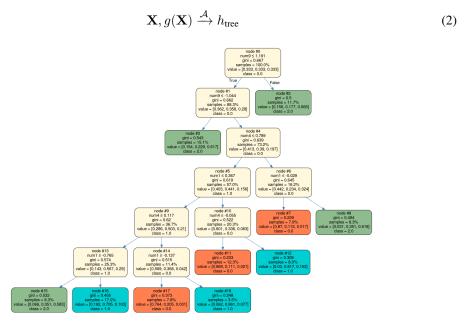


Figure 1:

Prescribed methods for training  $h_{\text{tree}}$  do exist [3] [1]. In practice, straightforward cross-validation and pruning approaches are often sufficient. Moreover, comparing cross-validated training error to traditional training error can give an indication of the stability of the single decision tree  $h_{\text{tree}}$ .

Elegantly handles high cardinality targets.

### 3.3 Decision Boundary Plots

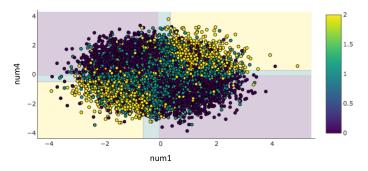


Figure 2:

What to do if very high cardinality in response, Y:

- 2- or 3-D plot against most important variables
- 2- or 3-D plot against sparse, interpretable extracted features: NMF, Sparse PCA

# 3.4 Shapley Global Feature Importance

Shapley explanations, including tree shap and even certain implementations of LIME, are a class of additive, consistent local feature contribution measures with long-standing theoretical support [10]. Shapley explanations are the only possible locally accurate and consistent feature contribution values, meaning that Shapley explanation values for input features always sum to  $g(\mathbf{x})$  and that Shapley explanation values can never decrease for some  $x_j$  when g is changed such that  $x_j$  truly makes a stronger contribution to  $g(\mathbf{x})$  [10].

$$g(\mathbf{x}) = \phi_0 + \sum_{j=0}^{j=\mathcal{P}-1} \phi_j \mathbf{z}_j$$
 (3)

$$\phi_j = \sum_{S \subseteq \mathcal{P} \setminus \{j\}} \frac{|S|!(\mathcal{P} - |S| - 1)!}{\mathcal{P}!} [g_x(S \cup \{j\}) - g_x(S)] \tag{4}$$

Shapley values can be estimated in different ways. Tree shap is a specific implementation of Shapley explanations. It does not rely on surrogate models. Both tree shap and a related technique known as *treeinterpreter* rely instead on traversing internal tree structures to estimate the impact of each  $x_j$  for some  $q(\mathbf{x})$  of interest [9], [12].

Simulated data is used to illustrate the utility of tree shap. Shapley explanations are estimated on  $g_{\rm GBM}({\bf X})$  for a simulated test set  ${\bf X}$  with known signal-generating function f. Results are presented in Figure 3. Firstly, the Shapley explanations are shown globally across all class outcomes in a stacked bar chart broken down by absolute global Shapley values per class outcome. This is a good way to see a overall picture of Shapley explanations for multinomial classifiers. Secondly, the Shapley explanations are broken down per class outcome in subsequent charts. All feature contributions for  $\operatorname{num}_1, \operatorname{num}_4, \operatorname{num}_8$  and  $\operatorname{num}_9$  are seen as most important across all class outcomes both in the global stacked bar chart and per class outcome, which is expected based on Equation 1. However, they are not seen in the same order. For example, class 0 and class 2 share the same ordering of  $\operatorname{num}_1, \operatorname{num}_4, \operatorname{num}_8$  and  $\operatorname{num}_9$  but class 1 does not ( $\operatorname{num}_1$  and  $\operatorname{num}_9$  are swapped). This information can be used to investigate why the Shapley explanataions differ between different class outcomes at a global level.

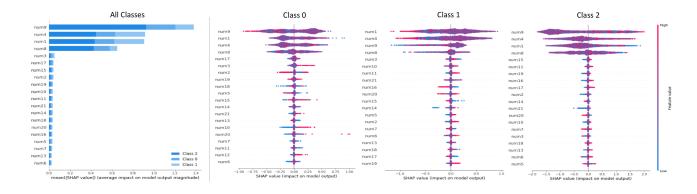


Figure 3: Shapley summary plot for known signal-generating function  $f = \text{num}_1 * \text{num}_4 + |\text{num}_8| * \text{num}_9^2 + e$ , and for learned GBM response function  $g_{\text{GBM}}$  per response outcome.

### 3.4.1 Recommendations

- Tree shap is ideal for estimating high-fidelity, consistent, and complete explanations of
  decision tree and decision tree ensemble models, perhaps even in regulated applications
  to generate regulator-mandated reason codes (also known as turn-down codes or adverse
  action codes).
- Because tree shap explanations are offsets from a global intercept, each  $\phi_j$  can be interpreted as the difference in  $g(\mathbf{x})$  and the average of  $g(\mathbf{X})$  associated with some input feature  $x_j$  [11].
- What to do if very high cardinality in response, Y:
  - Examine top-K most frequent classes
  - Examine top-K most accurate and inaccurate classes
  - Examine classes with highest variance in sum(absolute(shap))

#### 3.5 Partial Dependence and ICE

Partial dependence (PD) plots are a widely-used method for describing the average predictions of a complex model g across some partition of data  $\mathbf{X}$  for some interesting input feature  $X_j$  [4]. Individual conditional expectation (ICE) plots are a newer method that describes the local behavior of g for a single instance  $\mathbf{x} \in \mathcal{X}$ . Partial dependence and ICE can be combined in the same plot to identify interactions modeled by g and to create a holistic portrait of the predictions of a complex model for some  $X_j$  [5].

Following Friedman et al. a single feature  $X_j \in \mathbf{X}$  and its complement set  $\mathbf{X}_{(-j)} \in \mathbf{X}$  (where  $X_j \cup \mathbf{X}_{(-j)} = \mathbf{X}$ ) is considered. PD $(X_j,g)$  for a given feature  $X_j$  is estimated as the average output for a particular class outcome, C', of the learned function  $g(\mathbf{X})$  when all the components of  $X_j$  are set to a constant  $x \in \mathcal{X}$  and  $\mathbf{X}_{(-j)}$  is left unchanged. ICE $(x_j, \mathbf{x}, g)$  for a given instance  $\mathbf{x}$  and feature  $x_j$  is estimated as the output for a particular class outcome, C', for  $g(\mathbf{x})$  when  $x_j$  is set to a constant  $x \in \mathcal{X}$  and all other features  $\mathbf{x} \in \mathbf{X}_{(-j)}$  are left untouched. Partial dependence and ICE curves are usually plotted over some set of constants  $x \in \mathcal{X}$ .

As in Section 3.2, simulated data is used to highlight desirable characteristics of partial dependence and ICE plots. In Figure 4 partial dependence and ICE at the minimum, maximum, and each decile of  $g_{\rm GBM}({\bf X})$  are plotted per response outcome. The known quadratic behavior of num<sub>9</sub> is plainly visible, except for low/high value predictions across certain deciles per response outcome. When partial dependence and ICE curves diverge, this often points to an interaction that is being averaged out of the partial dependence. Given the form of Equation 1, there is a known interaction between num<sub>9</sub> and num<sub>8</sub>. Combining the information from partial dependence and ICE plots with  $h_{tree}$  can help elucidate more detailed information about modeled interactions in g.

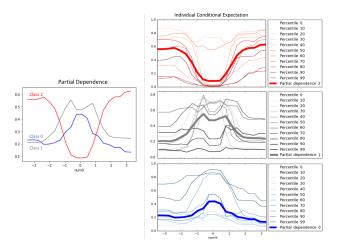


Figure 4: Partial dependence and ICE curves per response outcome for previously defined known signal-generating function f, learned GBM response function  $g_{\text{GBM}}$ , and important input feature num<sub>9</sub>.

### 3.5.1 Recommendations

- Combining  $h_{\text{tree}}$  with partial dependence and ICE curves per class outcome is a convenient method for detecting, confirming, and understanding important interactions in g.
- What to do if very high cardinality in response, Y:
  - Examine top-K most frequent classes
  - Examine top-K most accurate and inaccurate classes
  - Examine classes with highest variance in partial dependence
  - Examine classes with largest differences between partial dependence and ICE

# 4 Supplementary Materials

UCI credit card dataset [8].

https://github.com/navdeep-G/interpretable-ml/tree/master/notebooks/credit/multinomial

# 5 Conclusion

# **6** NIPS Style examples

**Paragraphs** There is also a \paragraph command available, which sets the heading in bold, flush left, and inline with the text, with the heading followed by 1 em of space.

# 6.1 Citations, figures, tables, references

These instructions apply to everyone.

# 6.2 Citations within the text

The natbib package will be loaded for you by default. Citations may be author/year or numeric, as long as you maintain internal consistency. As to the format of the references themselves, any style is acceptable as long as it is used consistently.

The documentation for natbib may be found at

```
http://mirrors.ctan.org/macros/latex/contrib/natbib/natnotes.pdf
```

Of note is the command \citet, which produces citations appropriate for use in inline text. For example,

```
\citet{hasselmo} investigated\dots
```

produces

```
Hasselmo, et al. (1995) investigated...
```

If you wish to load the natbib package with options, you may add the following before loading the nips\_2018 package:

```
\PassOptionsToPackage{options}{natbib}
```

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```
\usepackage[nonatbib] {nips_2018}
```

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The file nips\_2018.tex may be used as a "shell" for writing your paper. All you have to do is replace the author, title, abstract, and text of the paper with your own.

The formatting instructions contained in these style files are summarized in Sections ??, ??, and 6.1 below.

#### **6.3** Footnotes

Footnotes should be used sparingly. If you do require a footnote, indicate footnotes with a number<sup>3</sup> in the text. Place the footnotes at the bottom of the page on which they appear. Precede the footnote with a horizontal rule of 2 inches (12 picas).

Note that footnotes are properly typeset after punctuation marks.<sup>4</sup>

### 6.4 Figures

### 6.5 Tables

Place one line space before the table title, one line space after the table title, and one line space after the table. The table title must be lower case (except for first word and proper nouns); tables are numbered consecutively.

Note that publication-quality tables *do not contain vertical rules*. We strongly suggest the use of the booktabs package, which allows for typesetting high-quality, professional tables:

<sup>&</sup>lt;sup>3</sup>Sample of the first footnote.

<sup>&</sup>lt;sup>4</sup>As in this example.

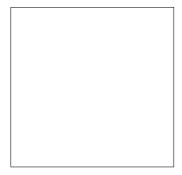


Figure 5: Sample figure caption.

Table 1: Sample table title

	Part	
Name	Description	Size $(\mu m)$
Dendrite Axon Soma	Input terminal Output terminal Cell body	$\begin{array}{c} \sim \! 100 \\ \sim \! 10 \\ \text{up to } 10^6 \end{array}$

https://www.ctan.org/pkg/booktabs

This package was used to typeset Table 1.

The \bbold package almost always uses bitmap fonts. You should use the equivalent AMS Fonts:

\usepackage{amsfonts}

followed by, e.g.,  $\mathbb{R}$ ,  $\mathbb{R}$ ,  $\mathbb{R}$ ,  $\mathbb{R}$ , or  $\mathbb{R}$ ,  $\mathbb{R}$  or  $\mathbb{R}$ . You can also use the following workaround for reals, natural and complex:

Note that amsforts is automatically loaded by the amssymb package.

# Acknowledgments

Use unnumbered third level headings for the acknowledgments. All acknowledgments go at the end of the paper. Do not include acknowledgments in the anonymized submission, only in the final paper.

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