```
def FASTMAP(Sn):
2
      "Project data on a line between
3
      two distant points"
4
                 = random.choose(Sn)
                                                      1 | def CrossTree(Sn):
5
                 = furthest(z, Sn)
      east
                                                      2
                                                            "Tree of clusters and results
                 = furthest(east, Sn)
6
      west
                                                      3
                                                             from their differences"
      Sn.poles = (west,east)
                                                      4
8
                 = dist(west,east)
                                                      5
                                                            \#Calculate(X,Y) of solutions
9
      for one in Sn.members:
                                                            Sn = FASTMAP(Sn)
10
       one.X, one.Y = project (west, east, c, one)
                                                      7
                                                            #Accumulate Clusters
      {f return} Sn #data members updated with (X,Y)
11
                                                      8
                                                            Cm = [C for C in WHERE4(Sn,min,max)]
12
                                                      9
                                                            #Replace data with discretized values
13
   def project(west, east, c, x):
                                                      10
                                                            Cm = Discretize(Cm)
14
      "Project x onto line east to west"
                                                     11
                                                            #Score clusters
15
      a = dist(x, west)
                                                            BetterC, WorseC = score(Cm)
                                                     12
     b = dist(x, east)
16
                                                      13
17
     X = (a*a + c*c - b*b)/(2*c), # cosine rule
                                                     14
                                                            #Build CART Decision Tree
     Y = (a*a - X)**0.5 # dist to line b/w poles
18
                                                     15
                                                            Dtree = cart(Cm)
19
     return X, Y
                                                     16
20
                                                     17
                                                            #Prune same and more leaves
21
   def furthest(x,Sn): # furthest from x?
                                                     18
                                                            for leaf in Dtree:
22
     out, max = x, 0
                                                     19
                                                              if size(leaf.clusters) > 1:
23
      for y in Sn:
                                                     20
                                                                Dtree.prune(leaf)
24
       d = dist(x, y)
                                                     2.1
                                                            for subtree in Dtree:
25
        if d > max: out, max = y, d
                                                              if size(subtree.uniq_clusters) < 2:</pre>
26
      return out
                                                     23
                                                                Dtree.prune(subtree)
                                                     24
                                                     25
                                                            for Branch in Dtree:
                                                     26
         Figure 1: Splitting data with FASTMAP
                                                     27
                                                              #Find a better branch for current branch
                                                     28
                                                              BBranch = Dtree.nearest_best(Branch.C,
                                                     29
                                                     30
                                                     31
                                                              if BBranch:
                                                                #Contrast Set(CS) represents diff b/w
                                                     33
                                                                #limits of Better and Worse Cluster
                                                     34
                                                                CS = Dtree.differ(WBranch.C,
   def WHERE4(Sn,min,max):
1 l
                                                     35
                                                                                   BBranch.C)
2
      "Recursive cluster quadrants of data"
                                                     36
3
      if Sn.length > min:
                                                     37
                                                                #Generate new population from model
4
        \textbf{if} \ \texttt{Sn.length} \ < \ \textbf{max:}
                                                     38
                                                                #using Contrast set
5
         yield Sn
                                                     39
                                                                ContrastSn = model(Size=Branch.C.size←
6
        else:
                                                                    *10.
7
          Xcap, Ycap = mean(Sn.Xs, Sn.Ys)
                                                     40
                                                                                    ContrastSet)
8
          for one in Sn:
                                                     41
9
            Sll += one if one.X < Xcap
                                                     42
10
                           and one.Y < Ycap</pre>
                                                                q1,q2,q3,q4 += ContrastSn.qs
                                                     43
11
            Slh += one if one.X < Xcap
12
                           and one.Y > Ycap
                                                     44
                                                              else:
                                                                #Balance distribution
13
            Shl += one if one.X > Xcap
14
                                                     46
                                                                q1, q2, q3, q4 += Limits(Branch.C).qs
                           and one.Y < Ycap
                                                     47
15
            Shh += one if one.X > Xcap
                                                     48
                                                            #25\, median, 75\, Maximum
16
                           and one.Y > Ycap
                                                     49
                                                            return q1,q2,q3,q4
17
          for S in (Sll,Slh,Shl,Shh):
18
            WHERE4(S,min,max)
19
      else:
```

Figure 3: Generating Deltas between clusters using

CrossTree

Figure 2: Recursing Spectrally in quadrants using WHERE4 Algorithm

20

yield Sn

```
1 |
    def score(Cm):
2
      "Divides set of clusters into better
3
       and worse based on objectives"
4
       better, worse, similar = 0,0,0
                                                                                CT vs NSGA XOMO
5
       for this in Cm:
         for other in Cm:
6
                                                                       nsga_xomofl
7
            for obj in Cm.objectives:
                                                                      nsga_xomogr
8
              pop1,pop2 = this.pop[obj],
                                                                        - nsga xomoos
9
                            other.pop[obj]
10
              #similar check
                                                                       – nsga_xomoo2
              if a12(pop1,pop2) and
11
                                                                        - nsga_xomoal
                                                             Time (in mins)
12
                 bootstrap(pop1,pop2):
                                                                          ct_xomofl
13
                 similar += 1
                                                                          ct xomogr
14
              #different being better or worse
15
              elif median(pop1) > median(pop2):
                                                                          ct_xomoos
16
                better += 1
                                                                          ct_xomoo2
17
              else:
18
                 worse += 1
19
            if better > 0 and worse == 0:
20
              scores[this] += 1
       #top square root of len are better
21
                                                                     100
                                                                                         300
                                                                                                   400
22
       Cm, cut = sorted(scores), scores.len**0.5
                                                                                     Population Size
       return Cm[:cut], Cm[cut:]
```

Figure 4: Generating Deltas between clusters using CrossTree

Figure 6: Times for CT and NSGA II on XOMO Model.

500

```
def discretize(Cm):
      "Discretizes data into bin and replaces
3
       its values with respective bin ids"
4
       #find best cut with least entropy
5
       #to predict clusters
       for C in Cm:
6
7
         pairs[d].append(C.id, C.dvalue)
8
       for d in decisions:
9
         bins[d] = divide(pairs[d])
10
11
       def divide(this):
12
         lhs, rhs
                   = Counts(),
13
                      Counts(sym(x) for x in this)
14
         for j,x in enumerate(this):
15
           maybe= lhs.n/n0*lhs.ent()
                  + rhs.n/n0*rhs.ent()
16
17
           if maybe < least:</pre>
18
             cut,least = j,maybe
19
           rhs - sym(x)
20
           lhs + sym(x)
21
         if cut:
22
           return bins+=divide(this[:cut])
23
                       +=divide(this[cut:])
24
         else: return bins
25
26
       for C, d in Cm, Cm. decisions:
27
         C.values[d] = bins.id(C,d)
28
29
       return Cm
```

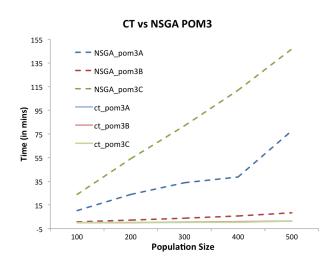


Figure 7: Times for CT and NSGA II on POM Model.

Figure 5: Generating Deltas between clusters using CrossTree

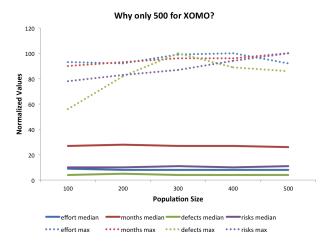


Figure 8: Median and Max of NSGA on XOMO when population size increases from 100 to 500.

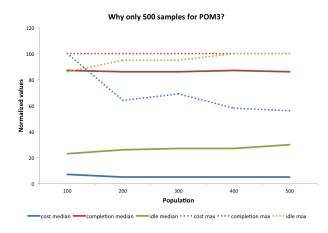


Figure 9: Median and Max of NSGA on POM when population size increases from 100 to 500.

Model: POM Objective	Market Ma	median	IOR		
,	Base Line	32	28		
cost		35			
	CT0		25		
1	NSGA II	3	0	•	_
completion	Base Line	85	2		•
	CT0	75	0	•	
	NSGA II	86	1		•
idle	Base Line	22	36	—	
	CT0	17	29	—	
	NSGA II	31	45		
Model: POM					
Objective	method	median	IQR		
cost	Base Line	32	27	—	
	CT0	19	14	-•-	
	NSGA II	6	0	•	
completion	Base Line	84	2	-	•
	CT0	55	0	•	
	NSGA II	86	2	=	•
idle	Base Line	29	37		
	CT0	17	27		
	NSGA II	32	47		
Model: POM	3C				
Objective	method	median	IQR		
cost	Base Line	40	25	—	
	CT0	31	20		
	NSGA II	10	0	•	
completion	Base Line	90	0		•
	CT0	63	1	. •	
	NSGA II	90	1		. •
idle	Base Line	34	33		
	CT0	21	25	-	
	NSGA II	36	41		
	110071	50	71	-	

Figure 10: Model: POM3

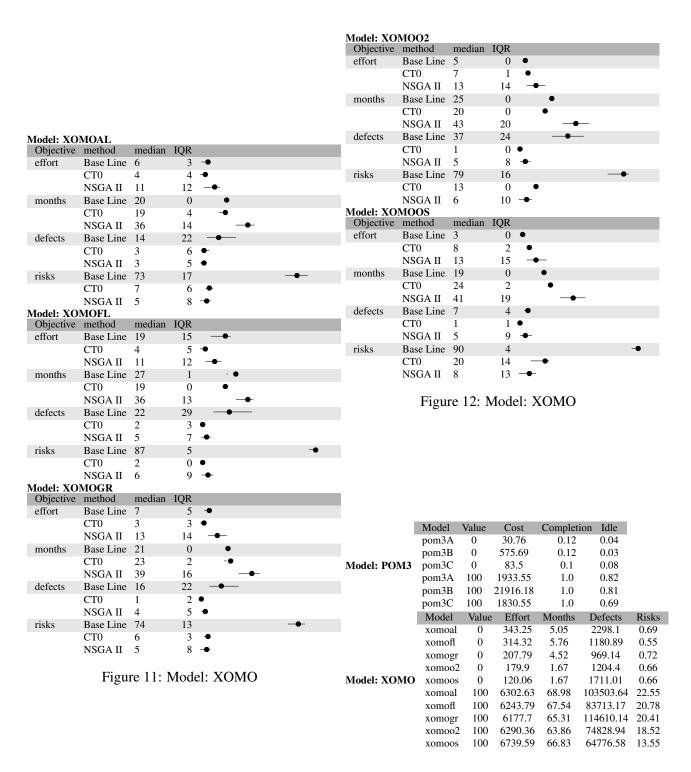


Figure 13: XOMO and POM3 0100 values

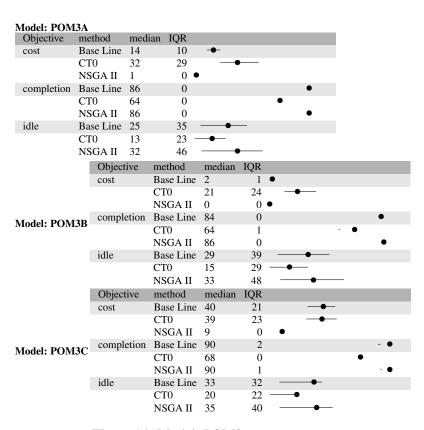


Figure 14: Model: POM3