### STRAIGHT LINES Exercise 7.1

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## 1 Problem

Q3. AD and BC are equal perpendiculars to a line segment. Show that CD bisects AB.

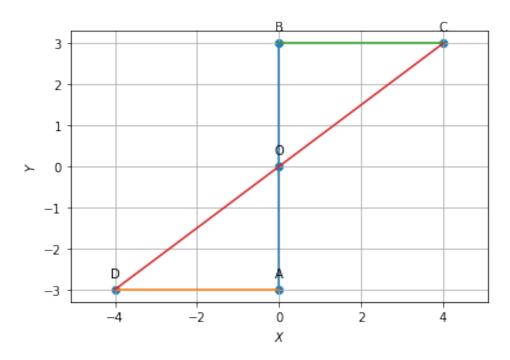


Figure 1:

#### 2 Construction

The input parameters for this construction are

Symbol	Values	Description
A	$\left  \begin{array}{c} 0 \\ -3 \end{array} \right $	point A
В	$\begin{pmatrix} 0 \\ 3 \end{pmatrix}$	point B
C	$\begin{pmatrix} 4 \\ 3 \end{pmatrix}$	point C
D	$\begin{pmatrix} -4 \\ -3 \end{pmatrix}$	point D
О	$\begin{pmatrix} 0 \\ 0 \end{pmatrix}$	point O

Table 2:

#### 3 **Solution**

Given:

$$AD = BC (1)$$

$$\angle CBO = \angle DAO$$
 (2)

To prove:

$$\angle ODA = \angle OCB$$
 (3)

### **Proof**

The directional vectors are:

$$m_1 = O - D \tag{4}$$

$$\mathbf{m_2} = \mathbf{D} - \mathbf{A} \tag{5}$$

The Normal vectors are:

$$\mathbf{n_1} = \mathbf{O} - \mathbf{C} \tag{6}$$

$$\mathbf{n_2} = \mathbf{C} - \mathbf{B} \tag{7}$$

(8)

$$\theta_1 = \cos^{-1}\left(\frac{m_1^T m_2}{\|m_1\| \|m_2\|}\right) \tag{9}$$

$$\theta_{1} = \cos^{-1} \left( \frac{m_{1}^{T} m_{2}}{\|m_{1}\| \|m_{2}\|} \right)$$

$$\theta_{2} = \cos^{-1} \left( \frac{n_{1}^{T} n_{2}}{\|n_{1}\| \|n_{2}\|} \right)$$
(9)
$$(10)$$

If  $\theta_1 = \theta_2$ 

$$\triangle OBC \cong \triangle OAD \tag{11}$$

$$OA = OB (12)$$