# Naveen\_joon\_ML\_Lab9

## April 24, 2020

```
In [1]: import pandas as pd
        import numpy as np
        from sklearn.model_selection import train_test_split
        import matplotlib.pyplot as plt
        /matplotlib inline
```

PROBLEM 1: Here you must read an input file. Each line contains 785 numbers (comma delimited): the first values are between 0.0 and 1.0 correspond to the 784 pixel values (black and white images), and the last number denotes the class label: 0 corresponds to digit 0, 1 corresponds to digit 1, etc.

## 0.1 Solution 1:

Problem 2:Implement the backpropagation algorithm in a zero hidden layer neural network

## 0.2 Solution 2:

```
self.weights=[]
               self.bias=[]
               self.outputs=[]
               self.derivatives=[]
               self.activations=[]
def connect(self,layer1,layer2):
                """layer 2 of shape 1xn"""
               self.derivatives.append(np.random.uniform(0,0.1,size=(layer1.shape[1]+1,layer2)) \\
               self.weights.append(np.random.uniform(-1,1,size=(layer1.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]
               self.bias.append(np.random.uniform(-1,1,size=(layer1.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer2.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,layer3.shape[1]+1,
def softmax(self,z):
               e=np.exp(z)
               return e/np.sum(e,axis=1).reshape(-1,1)
def max_log_likelihood(self,y_pred,y):
                """cross entropy"""
               return y*np.log(y_pred)
def delta_mll(self,y,y_pred):
                """derivative of cross entropy"""
               return y_pred-y
def forward_pass(self,x,y,weights,bias):
               cost=0
               self.outputs=[]
               for i in range(len(weights)):
                              samples=len(x)
                              ones_array=np.ones(samples).reshape(samples,1)
                               self.outputs.append(x)
                              z=np.dot(np.append(ones_array,x,axis=1),weights[i]+bias[i])
                              x=self.softmax(z)
               self.outputs.append(x)
               self.y\_pred=x
               temp=-self.max_log_likelihood(self.y_pred,y)
               cost=np.mean(np.sum(temp,axis=1))
               return cost
def backward_pass(self,y,lr):
               for i in range(len(self.weights)-1,-1,-1):
                              ones_array=np.ones(len(n.outputs[i])).reshape(len(n.outputs[i]),1)
                              prev_term=self.delta_mll(y,self.y_pred)
                               self.derivatives[i] = np.dot(prev_term.T,np.append(ones_array,self.outputs[i])
                               self.weights[i]=self.weights[i]-lr*((self.derivatives[i].T)/len(y))
                               self.bias[i]=self.bias[i]-lr*((self.derivatives[i].T)/len(y))
```

```
def train(self,batches,lr=1e-3,epoch=10):
                """number of batches to split data in, Learning rate and epochs"""
                for epochs in range(epoch):
                    samples=len(self.x)
                    c=0
                    for i in range(batches):
                      x_batch=self.x[int((samples/batches)*i):int((samples/batches)*(i+1))]
                      y_batch=self.y.loc[int((samples/batches)*i):int((samples/batches)*(i+1))
                      c=self.forward_pass(x_batch,y_batch,self.weights,self.bias)
                      self.backward_pass(y_batch,lr)
                    print(epochs,c/batches)
            def predict(self,x):
                """input: x_test values"""
                x=x/255
                for i in range(len(self.weights)):
                    samples=len(x)
                    ones_array=np.ones(samples).reshape(samples,1)
                    z=np.dot(np.append(ones_array,x,axis=1),self.weights[i]+self.bias[i])
                    x=self.softmax(z)
                return np.argmax(x,axis=1)
In [5]: n=Perceptron(X_train,Labels)
        n.connect(X_train,Labels)
        n.train(batches=1000,lr=0.2,epoch=30)
0 0.0007346536093938932
1 0.001333487169224761
2 0.0013481239936291142
3 0.00140891863962916
4 0.0013453292726588928
5 0.0013381109501742542
6 0.0012614553011848957
7 0.001106183056327947
8 0.0009913863734484585
9 0.0008757571024339127
10 0.0007338984410219489
11 0.0006864509257048199
12 0.0005775119638534283
13 0.00048018933575138346
14 0.00037368116723659746
15 0.0002783396432771148
16 0.00021805448702410285
17 0.00018112696097078769
18 0.00014298112213567696
19 0.000120601465357245
```

```
20 0.00011512104828964503
21 0.00010645510225767944
22 9.898418290156401e-05
23 9.471556040883543e-05
24 8.981066362311253e-05
25 8.515503292730198e-05
26 8.086352397337016e-05
27 7.612173743806715e-05
28 7.182886799448558e-05
29 6.86133687423989e-05
In [6]: pred=n.predict(X_test)
        np.bincount(n.predict(X_test)),np.bincount(y_test)
Out[6]: (array([311, 333, 303, 327, 330, 280, 286, 325, 234, 271]),
         array([296, 327, 305, 326, 305, 283, 282, 336, 252, 288]))
In [7]: print(f"accuracy: {np.bincount(np.abs(y_test-pred))[0]*100/len(y_test)} %")
accuracy: 89.0 %
```

Problem 3: Extend your code from problem 2 to support a single layer neural network with N hidden units

## 0.3 Solution 3:

```
In [8]: class Layer():
            size: Number of nodes in the hidden layer
            activation: name of activation function for the layer
            def __init__(self,size,activation='sigmoid'):
                self.shape=(1,size)
                self.activation=activation
        class SingleLayerNeuralNetwork():
            def __init__(self,x,y):
                 ,,,,,,
                x is 2d array of input images
                y are one hot encoded labels
                 11 11 11
                self.x=x/255
                self.y=y
                self.weights=[]
                self.bias=[]
                self.outputs=[]
                self.derivatives=[]
```

```
self.activations=[]
def connect(self,layer1,layer2):
    """layer 2 of shape 1xn"""
    self.derivatives.append(np.random.uniform(0,0.1,size=(layer1.shape[1]+1,layer2
    self.weights.append(np.random.uniform(-1,1,size=(layer1.shape[1]+1,layer2.shape[1]+1)
    self.bias.append(np.random.uniform(-1,1,size=(layer1.shape[1]+1,layer2.shape[1]
    if isinstance(layer2,Layer):
        self.activations.append(layer2.activation)
def activation(self,name,z,derivative=False):
    if name=='sigmoid':
        if derivative==False:
            return 1/(1+np.exp(-z))
        else:
            return z*(1-z)
def softmax(self,z):
    e=np.exp(z)
    return e/np.sum(e,axis=1).reshape(-1,1)
def max_log_likelihood(self,y_pred,y):
    """cross entropy"""
    return y*np.log(y_pred)
def delta_mll(self,y,y_pred):
    """derivative of cross entropy"""
    return y_pred-y
def forward_pass(self,x,y,weights,bias):
    cost=0
    self.outputs=[]
    for i in range(len(weights)):
        samples=len(x)
        ones_array=np.ones(samples).reshape(samples,1)
        self.outputs.append(x)
        z=np.dot(np.append(ones_array,x,axis=1),weights[i]+bias[i])
        if i==len(weights)-1:
            x=self.softmax(z)
        else:
            x=self.activation(self.activations[i],z)
    self.outputs.append(x)
    self.y_pred=x
    temp=-self.max_log_likelihood(self.y_pred,y)
    cost=np.mean(np.sum(temp,axis=1))
    return cost
```

```
for i in range(len(self.weights)-1,-1,-1):
                     ones_array=np.ones(len(n.outputs[i])).reshape(len(n.outputs[i]),1)
                     if i==len(self.weights)-1:
                         prev_term=self.delta_mll(y,self.y_pred)
                         # derivatives follow specific order,last three terms added new,rest fr
                         self.derivatives[i]=np.dot(prev_term.T,np.append(ones_array,self.outpu
                     else:
                         prev_term=np.dot(prev_term,self.weights[i+1][1:].T)*self.activation(self.weights[i+1][1:].T)
                         \verb|self.derivatives[i]=| \verb|np.dot(prev_term.T, \verb|np.app| end(ones_array, \verb|self.outpu|)| \\
                     self.weights[i]=self.weights[i]-lr*((self.derivatives[i].T)/len(y))
                     self.bias[i]=self.bias[i]-lr*((self.derivatives[i].T)/len(y))
            def train(self,batches,lr=1e-3,epoch=10):
                 """number of batches to split data in, Learning rate and epochs"""
                for epochs in range(epoch):
                     samples=len(self.x)
                     c=0
                     for i in range(batches):
                       x_batch=self.x[int((samples/batches)*i):int((samples/batches)*(i+1))]
                       y_batch=self.y.loc[int((samples/batches)*i):int((samples/batches)*(i+1))
                       c=self.forward_pass(x_batch,y_batch,self.weights,self.bias)
                       self.backward_pass(y_batch,lr)
                     print(epochs,c/batches)
            def predict(self,x):
                 """input: x_test values"""
                x=x/255
                for i in range(len(self.weights)):
                     samples=len(x)
                     ones_array=np.ones(samples).reshape(samples,1)
                     z=np.dot(np.append(ones_array,x,axis=1),self.weights[i]+self.bias[i])
                     if i==len(self.weights)-1:
                         x=self.softmax(z)
                     else:
                         x=self.activation(self.activations[i],z)
                return np.argmax(x,axis=1)
In [9]: n=SingleLayerNeuralNetwork(X_train,Labels)
        11=Layer(100)
        n.connect(X_train,11)
        n.connect(l1,Labels)
        n.train(batches=1000,lr=0.1,epoch=50)
```

def backward\_pass(self,y,lr):

- 0 0.00026507369571026614
- 1 0.00025858462939753183
- 2 0.0003219614067774773
- 3 0.0003969718784473034
- 4 0.00040219823644652093
- 5 0.0003539709694831452
- 6 0.0002872648113062959
- 7 0.00022643033055996613
- 8 0.00017733474096884785
- 9 0.00013823525845028798
- 10 0.00010853908154940441
- 11 8.745823571803799e-05
- 12 7.289272699810053e-05
- 13 6.290169997826579e-05
- 14 5.5982952283681096e-05
- 15 5.0701449324372964e-05
- 16 4.612029222306469e-05
- 17 4.2153518585174634e-05
- 18 3.894917880239001e-05 19 3.640450110123102e-05
- 20 3.4349600142749704e-05
- 21 3.265893785975352e-05
- 22 3.1218027519601566e-05
- 23 2.9930836254492685e-05
- 24 2.8743384629089865e-05
- 25 2.7640925347847073e-05
- 26 2.6626127615626717e-05
- 27 2.5691004651994144e-05
- 28 2.481661925753757e-05
- 29 2.3986358964226792e-05
- 30 2.3192789990938606e-05
- 31 2.243617005877505e-05
- 32 2.17189028243342e-05
- 33 2.1041594716529147e-05
- 34 2.0402456071458396e-05
- 35 1.9798332478703507e-05
- 36 1.9225746165598018e-05
- 37 1.8681471640113977e-05
- 38 1.8162740072012184e-05
- 39 1.7667251520627377e-05
- 40 1.7193113843307993e-05
- 41 1.6738766155371304e-05
- 42 1.6302909147056948e-05
- 43 1.5884448022904003e-05
- 44 1.5482447477912558e-05
- 45 1.5096096376830381e-05
- 46 1.472467983609257e-05
- 47 1.4367556963838973e-05

Problem 4: Extend your code from problem 3 (use cross entropy error) and implement a 2-layer neural network, starting with a simple architecture containing N hidden units in each layer

#### **0.4** Solution 4:

In [12]: class Layer():

```
size: Number of nodes in the hidden layer
     activation: name of activation function for the layer
     def __init__(self,size,activation='sigmoid'):
          self.shape=(1,size)
          self.activation=activation
class DoubleLayerNeuralNetwork():
     def __init__(self,x,y):
          x is 2d array of input images
          y are one hot encoded labels
          11 11 11
          self.x=x/255
          self.y=y
          self.weights=[]
          self.bias=[]
          self.outputs=[]
          self.derivatives=[]
          self.activations=[]
     def connect(self,layer1,layer2):
          """layer 2 of shape 1xn"""
          self.derivatives.append(np.random.uniform(0,0.1,size=(layer1.shape[1]+1,layer
          self.weights.append(np.random.uniform(-1,1,size=(layer1.shape[1]+1,layer2.shape[1]+1)
          self.bias.append(np.random.uniform(-1,1,size=(layer1.shape[1]+1,layer2.shape[-1,1,size=(layer1.shape[1]+1,layer2.shape[-1,1,size=(layer1.shape[1]+1,layer2.shape[-1,1,size=(layer1.shape[1]+1,layer2.shape[-1,1,size=(layer1.shape[1]+1,layer2.shape[-1,1]+1])
          if isinstance(layer2, Layer):
```

```
self.activations.append(layer2.activation)
def activation(self,name,z,derivative=False):
    if name=='sigmoid':
        if derivative==False:
            return 1/(1+np.exp(-z))
        else:
            return z*(1-z)
def softmax(self,z):
    e=np.exp(z)
    return e/np.sum(e,axis=1).reshape(-1,1)
def max_log_likelihood(self,y_pred,y):
    """cross entropy"""
    return y*np.log(y_pred)
def delta_mll(self,y,y_pred):
    """derivative of cross entropy"""
    return y_pred-y
def forward_pass(self,x,y,weights,bias):
    self.outputs=[]
    for i in range(len(weights)):
        samples=len(x)
        ones_array=np.ones(samples).reshape(samples,1)
        self.outputs.append(x)
        z=np.dot(np.append(ones_array,x,axis=1),weights[i]+bias[i])
        if i==len(weights)-1:
            x=self.softmax(z)
        else:
            x=self.activation(self.activations[i],z)
    self.outputs.append(x)
    self.y_pred=x
    temp=-self.max_log_likelihood(self.y_pred,y)
    cost=np.mean(np.sum(temp,axis=1))
    return cost
def backward_pass(self,y,lr):
    for i in range(len(self.weights)-1,-1,-1):
        ones_array=np.ones(len(n.outputs[i])).reshape(len(n.outputs[i]),1)
        if i==len(self.weights)-1:
            prev_term=self.delta_mll(y,self.y_pred)
            self.derivatives[i] = np.dot(prev_term.T, np.append(ones_array, self.outp
```

```
prev_term=np.dot(prev_term,self.weights[i+1][1:].T)*self.activation(self.weights[i+1][1:].T)
                          self.derivatives[i] = np.dot(prev_term.T, np.append(ones_array, self.outp
                     self.weights[i]=self.weights[i]-lr*((self.derivatives[i].T)/len(y))
                     self.bias[i]=self.bias[i]-lr*((self.derivatives[i].T)/len(y))
             def train(self,batches,lr=1e-3,epoch=10):
                  """number of batches to split data in, Learning rate and epochs"""
                 for epochs in range(epoch):
                      samples=len(self.x)
                      c=0
                      for i in range(batches):
                       x_batch=self.x[int((samples/batches)*i):int((samples/batches)*(i+1))]
                       y_batch=self.y.loc[int((samples/batches)*i):int((samples/batches)*(i+1)
                        c=self.forward_pass(x_batch,y_batch,self.weights,self.bias)
                        self.backward_pass(y_batch,lr)
                      print(epochs,c/batches)
             def predict(self,x):
                 """input: x_test values"""
                 x = x/255
                 for i in range(len(self.weights)):
                      samples=len(x)
                      ones_array=np.ones(samples).reshape(samples,1)
                      z=np.dot(np.append(ones_array,x,axis=1),self.weights[i]+self.bias[i])
                      if i==len(self.weights)-1:
                         x=self.softmax(z)
                      else:
                         x=self.activation(self.activations[i],z)
                 return np.argmax(x,axis=1)
In [13]: n=DoubleLayerNeuralNetwork(X_train,Labels)
         11=Layer(100)
         12=Layer(100)
         n.connect(X_train,11)
         n.connect(11,12)
         n.connect(12,Labels)
         n.train(batches=1000,lr=0.1,epoch=20)
0 0.0006147752088982143
1 0.00022125939912860426
2 0.00011095514297885743
3 7.204884572833662e-05
4 5.308982882593679e-05
5 4.081481599292317e-05
6 3.72397198080972e-05
```

else:

```
7 3.457702926569818e-05
8 3.6016675373810834e-05
9 4.140543148333343e-05
10 4.646969123463548e-05
11 4.9277103508864534e-05
12 5.152655618035941e-05
13 5.163862117340579e-05
14 4.846590370833118e-05
15 4.41444585177594e-05
16 3.972547920999699e-05
17 3.530803170294093e-05
18 3.119814553556046e-05
19 2.776326929273412e-05
In [14]: pred=n.predict(X_test)
        np.bincount(n.predict(X_test)),np.bincount(y_test)
Out[14]: (array([306, 335, 294, 320, 327, 288, 283, 332, 238, 277]),
         array([296, 327, 305, 326, 305, 283, 282, 336, 252, 288]))
In [15]: print(f"accuracy: {np.bincount(np.abs(y_test-pred))[0]*100/len(y_test)} %")
```

Problem 5: Extend your code from problem 4 to implement different activations functions which will be passed as a parameter. In this problem all activations (except the final layer which should remain a softmax) must be changed to the passed activation function.

## 0.5 Solution 5:

```
In [16]: class Layer():
    """
    size: Number of nodes in the hidden layer
    activation: name of activation function for the layer
    """
    def __init__(self,size,activation='sigmoid'):
        self.shape=(1,size)
        self.activation=activation

class NeuralNetworkActivations():
    def __init__(self,x,y):
        """
        x is 2d array of input images
        y are one hot encoded labels
        """
        self.x=x/255
        self.y=y
```

```
self.weights=[]
    self.bias=[]
    self.outputs=[]
    self.derivatives=[]
    self.activations=[]
def connect(self,layer1,layer2):
    """layer 2 of shape 1xn"""
    self.derivatives.append(np.random.uniform(0,0.1,size=(layer1.shape[1]+1,layer
    self.weights.append(np.random.uniform(-1,1,size=(layer1.shape[1]+1,layer2.shape[1]+1)
    self.bias.append(np.random.uniform(-1,1,size=(layer1.shape[1]+1,layer2.shape[
    if isinstance(layer2,Layer):
        self.activations.append(layer2.activation)
def activation(self,name,z,derivative=False):
    if name=='sigmoid':
        if derivative==False:
            return 1/(1+np.exp(-z))
        else:
            return z*(1-z)
    elif name=='relu':
        if derivative==False:
            return np.maximum(0.0,z)
        else:
          z[z \le 0] = 0.0
          z[z>0] = 1.0
          return z
    elif name=='tanh':
      if derivative==False:
            return np.tanh(z)
      else:
            return 1.0 - (np.tanh(z)) ** 2
def softmax(self,z):
    e=np.exp(z)
    return e/np.sum(e,axis=1).reshape(-1,1)
def max_log_likelihood(self,y_pred,y):
    """cross entropy"""
    return y*np.log(y_pred)
def delta_mll(self,y,y_pred):
    """derivative of cross entropy"""
    return y_pred-y
def forward_pass(self,x,y,weights,bias):
    cost=0
```

```
self.outputs=[]
    for i in range(len(weights)):
        samples=len(x)
        ones_array=np.ones(samples).reshape(samples,1)
        self.outputs.append(x)
        z=np.dot(np.append(ones_array,x,axis=1),weights[i]+bias[i])
        if i==len(weights)-1:
            x=self.softmax(z)
        else:
            x=self.activation(self.activations[i],z)
    self.outputs.append(x)
    self.y_pred=x
    temp=-self.max_log_likelihood(self.y_pred,y)
    cost=np.mean(np.sum(temp,axis=1))
    return cost
def backward_pass(self,y,lr):
    for i in range(len(self.weights)-1,-1,-1):
        ones_array=np.ones(len(n.outputs[i])).reshape(len(n.outputs[i]),1)
        if i==len(self.weights)-1:
            prev_term=self.delta_mll(y,self.y_pred)
            self.derivatives[i]=np.dot(prev_term.T,np.append(ones_array,self.outp
        else:
            prev_term=np.dot(prev_term, self.weights[i+1][1:].T)*self.activation(self.weights[i+1][1:].T)
            \verb|self.derivatives[i]=| \verb|np.dot(prev_term.T, \verb|np.append(ones_array, \verb|self.outpred)|| \\
        self.weights[i]=self.weights[i]-lr*((self.derivatives[i].T)/len(y))
        self.bias[i]=self.bias[i]-lr*((self.derivatives[i].T)/len(y))
def train(self,batches,lr=1e-3,epoch=10):
    """number of batches to split data in, Learning rate and epochs"""
    for epochs in range(epoch):
        samples=len(self.x)
        c=0
        for i in range(batches):
          x_batch=self.x[int((samples/batches)*i):int((samples/batches)*(i+1))]
          y_batch=self.y.loc[int((samples/batches)*i):int((samples/batches)*(i+1)
          c=self.forward_pass(x_batch,y_batch,self.weights,self.bias)
          self.backward_pass(y_batch,lr)
        print(epochs,c/batches)
def predict(self,x):
    """input: x_test values"""
    for i in range(len(self.weights)):
        samples=len(x)
```

```
ones_array=np.ones(samples).reshape(samples,1)
                     z=np.dot(np.append(ones_array,x,axis=1),self.weights[i]+self.bias[i])
                     if i==len(self.weights)-1:
                         x=self.softmax(z)
                     else:
                         x=self.activation(self.activations[i],z)
                 return np.argmax(x,axis=1)
In [17]: n=NeuralNetworkActivations(X_train,Labels)
         11=Layer(100, 'sigmoid')
         12=Layer(50, 'tanh')
         n.connect(X train, 11)
         n.connect(11,12)
         n.connect(12,Labels)
         n.train(batches=1000,lr=0.1,epoch=20)
0 6.393954821616651e-05
1 0.0005118562710481734
2 0.00023085754588267473
3 0.00016826567329880513
4 0.0002573099462506769
5 0.0006350785332999381
6 4.7923176876536626e-05
7 3.840975191833874e-05
8 3.430696135163668e-05
9 1.0051623852615276e-05
10 0.0005127406062526722
11 4.717236913963525e-06
12 0.00034750915286958333
13 2.7764888942601524e-06
14 7.91851544017604e-06
15 5.149784307016578e-07
16 1.7189875833741053e-05
17 1.1657772127244548e-05
18 2.1612809181756667e-05
19 1.0198810562150977e-06
In [18]: pred=n.predict(X_test)
         np.bincount(n.predict(X_test)),np.bincount(y_test)
Out[18]: (array([305, 329, 296, 331, 308, 265, 286, 338, 246, 296]),
          array([296, 327, 305, 326, 305, 283, 282, 336, 252, 288]))
In [19]: print(f"accuracy: {np.bincount(np.abs(y_test-pred))[0]*100/len(y_test)} "")
accuracy: 92.9 %
```

Problem 6: Extend your code from problem 5 to implement momentum with your gradient descent. The momentum value will be passed as a parameter. Your function should perform "epoch" number of epochs and return the resulting weights.

#### 0.6 Solution 6:

```
In [20]:
             class Layer():
                 11 11 11
                 size: Number of nodes in the hidden layer
                 activation: name of activation function for the layer
                 def __init__(self,size,activation='sigmoid'):
                     self.shape=(1,size)
                     self.activation=activation
             class NeuralNetworkMomentum():
                 def __init__(self,x,y):
                     x is 2d array of input images
                     y are one hot encoded labels
                      11 11 11
                     self.x=x/255 # Divide by 255 to normalise the pixel values (0-255)
                     self.y=y
                     self.weights=[]
                     self.bias=[]
                     self.outputs=[]
                     self.derivatives=[]
                     self.activations=[]
                     self.delta_weights=[]
                     self.delta_bias=[]
                 def connect(self,layer1,layer2):
                      """layer 2 of shape 1xn"""
                     #Initialise weights, derivatives and activation lists
                     self.derivatives.append(np.random.uniform(0,0.1,size=(layer1.shape[1]+1,1
                     self.weights.append(np.random.uniform(-1,1,size=(layer1.shape[1]+1,layer2)
                     self.bias.append(np.random.uniform(-1,1,size=(layer1.shape[1]+1,layer2.shape[1]+1)
                     self.delta_weights.append(np.zeros((layer1.shape[1]+1,layer2.shape[1])))
                     self.delta_bias.append(np.zeros((layer1.shape[1]+1,layer2.shape[1])))
                     if isinstance(layer2,Layer):
                          self.activations.append(layer2.activation)
                 def activation(self,name,z,derivative=False):
                     #implementation of various activation functions and their derivatives
                     if name=='sigmoid':
                          if derivative==False:
                              return 1/(1+np.exp(-z))
```

```
else:
            return z*(1-z)
    elif name=='relu':
        if derivative==False:
            return np.maximum(0.0,z)
        else:
          z[z \le 0] = 0.0
          z[z>0] = 1.0
          return z
    elif name=='tanh':
      if derivative==False:
            return np.tanh(z)
      else:
            return 1.0 - (np.tanh(z)) ** 2
def softmax(self,z):
    e=np.exp(z)
    return e/np.sum(e,axis=1).reshape(-1,1)
def max_log_likelihood(self,y_pred,y):
    """cross entropy"""
    return y*np.log(y_pred)
def delta_mll(self,y,y_pred):
    """derivative of cross entropy"""
    #return y*(y_pred-1)
    return y_pred-y
def forward_pass(self,x,y,weights,bias):
    cost=0
    self.outputs=[]
    for i in range(len(weights)):
        samples=len(x)
        ones_array=np.ones(samples).reshape(samples,1)
        self.outputs.append(x) #append without adding ones array
        z=np.dot(np.append(ones_array,x,axis=1),weights[i]+bias[i])
        if i==len(weights)-1:
            x=self.softmax(z)
        else:
            x=self.activation(self.activations[i],z)
    self.outputs.append(x)
    self.y_pred=x
    temp=-self.max_log_likelihood(self.y_pred,y)
    cost=np.mean(np.sum(temp,axis=1))
    return cost
```

```
for i in range(len(self.weights)-1,-1,-1):
                         ones_array=np.ones(len(n.outputs[i])).reshape(len(n.outputs[i]),1)
                         if i==len(self.weights)-1:
                             prev_term=self.delta_mll(y,self.y_pred)
                             # derivatives follow specific order, last three terms added new, re
                             self.derivatives[i]=np.dot(prev_term.T,np.append(ones_array,self.
                         else:
                             prev_term=np.dot(prev_term, self.weights[i+1][1:].T)*self.activation
                             self.derivatives[i]=np.dot(prev_term.T,np.append(ones_array,self.
                         if momentum:
                             self.delta_weights[i]=beta*self.delta_weights[i]-lr*((self.deriva
                             self.delta_bias[i]=beta*self.delta_bias[i]-lr*((self.derivatives[
                             self.weights[i]=self.weights[i]+self.delta_weights[i]
                             self.bias[i]=self.bias[i]+self.delta_bias[i]
                         else:
                             self.weights[i]=self.weights[i]-lr*((self.derivatives[i].T)/len(y
                             self.bias[i]=self.bias[i]-lr*((self.derivatives[i].T)/len(y))
                 def train(self,batches,lr=1e-3,epoch=10,beta=0.5):
                     """number of batches to split data in, Learning rate and epochs"""
                     for epochs in range(epoch):
                         samples=len(self.x)
                         c=0
                         for i in range(batches):
                           x_batch=self.x[int((samples/batches)*i):int((samples/batches)*(i+1)
                           y_batch=self.y.loc[int((samples/batches)*i):int((samples/batches)*(
                           c=self.forward_pass(x_batch,y_batch,self.weights,self.bias)
                           self.backward_pass(y_batch,lr,momentum=True,beta=0.5)
                         print(epochs,c/batches)
                 def predict(self,x):
                     """input: x_test values"""
                     x = x/255
                     for i in range(len(self.weights)):
                         samples=len(x)
                         ones_array=np.ones(samples).reshape(samples,1)
                         z=np.dot(np.append(ones_array,x,axis=1),self.weights[i]+self.bias[i])
                         if i==len(self.weights)-1:
                             x=self.softmax(z)
                         else:
                             x=self.activation(self.activations[i],z)
                     return np.argmax(x,axis=1)
In [21]: n=NeuralNetworkMomentum(X_train,Labels)
         11=Layer(100, 'sigmoid')
         12=Layer(50, 'tanh')
```

def backward\_pass(self,y,lr,momentum=False,beta=0.5):

```
n.connect(X_train,11)
         n.connect(11,12)
         n.connect(12,Labels)
         n.train(batches=500,lr=0.1,epoch=20,beta=0.5)
0 0.0007368871858396068
1 4.896638893996719e-05
2 0.00014723111518745942
3 9.195402384843673e-05
4 8.46722106169578e-05
5 0.0004254245940298797
6 0.0004518025915654164
7 0.0005144148604648345
8 0.00034785497903570513
9 6.636344183019607e-05
10 0.00017596769111351266
11 1.2285565898844749e-05
12 9.561366468641029e-06
13 3.946537442020382e-05
14 3.768419621026274e-06
15 1.4724958080051827e-06
16 9.895523345277317e-07
17 1.1006430491781112e-06
18 1.0262939221277626e-06
19 9.465183321892398e-07
In [22]: pred=n.predict(X_test)
         np.bincount(n.predict(X_test)),np.bincount(y_test)
Out[22]: (array([304, 326, 293, 323, 296, 271, 295, 335, 259, 298]),
          array([296, 327, 305, 326, 305, 283, 282, 336, 252, 288]))
In [23]: print(f"accuracy: {np.bincount(np.abs(y_test-pred))[0]*100/len(y_test)} %")
accuracy: 92.6 %
In []:
```