Homework3

Q1. PCA and 1- Nearest Neighbor classification error on test and train data.

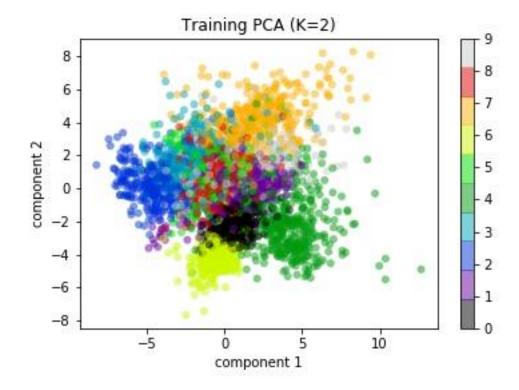
Test Error: Train Error:

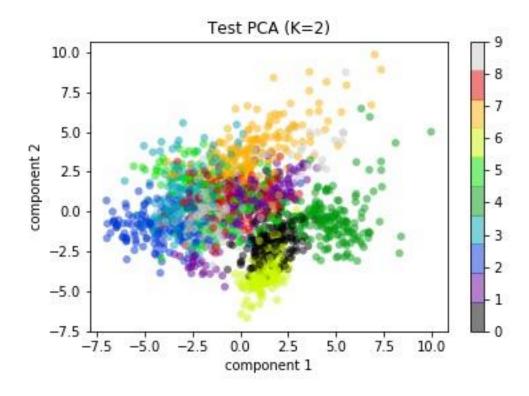
| Class | K = 2 | K = 3 | K = 8 | K = 20 | Class | K = 2 | K = 3 | K = 8 | K = 20 |
|-------|----------|----------|----------|----------|-------|-------|-------|-------|--------|
| 0 | 0.47191 | 0.994382 | 1 | 0.994382 | 0 | 0 | 0 | 0 | 0 |
| 1 | 0.71978 | 0.956044 | 0.791209 | 0.807692 | 1 | 0 | 0 | 0 | 0 |
| 2 | 0.412429 | 0.926554 | 0.79096 | 0.830508 | 2 | 0 | 0 | 0 | 0 |
| 3 | 0.737705 | 0.830601 | 0.655738 | 0.617486 | 3 | 0 | 0 | 0 | 0 |
| 4 | 0.353591 | 0.475138 | 0.381215 | 0.486188 | 4 | 0 | 0 | 0 | 0 |
| 5 | 0.868132 | 0.840659 | 0.631868 | 0.532967 | 5 | 0 | 0 | 0 | 0 |
| 6 | 0.624309 | 0.646409 | 0.983425 | 0.983425 | 6 | 0 | 0 | 0 | 0 |
| 7 | 0.469274 | 0.592179 | 0.458101 | 0.418994 | 7 | 0 | 0 | 0 | 0 |
| 8 | 0.821839 | 0.712644 | 0.643678 | 0.781609 | 8 | 0 | 0 | 0 | 0 |
| 9 | 0.844444 | 0.983333 | 0.95 | 0.944444 | 9 | 0 | 0 | 0 | 0 |

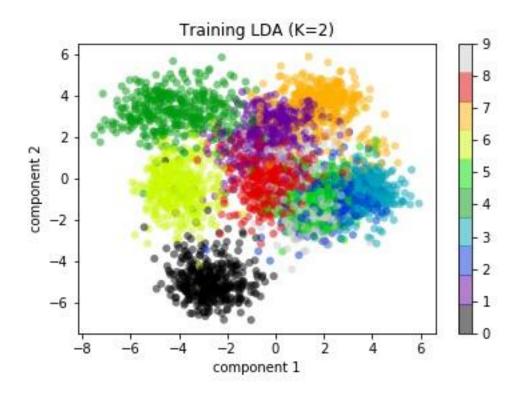
Q2. LDA and 1- Nearest Neighbor classification error on test and train data.

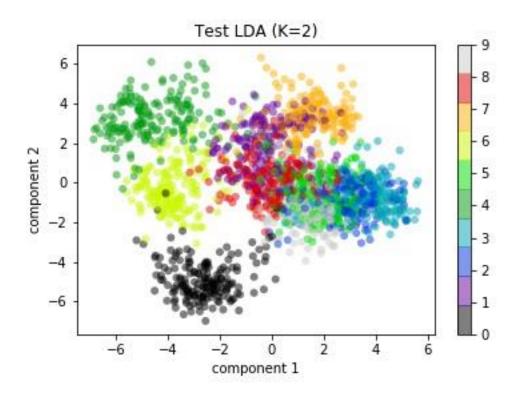
Test Error: Train Error:

| Class | K= 2 | K=3 | K=8 | K=20 | Class | K = 2 | K = 3 | K = 8 | K = 20 |
|-------|----------|----------|----------|----------|-------|-------|-------|-------|--------|
| 0 | 0.08427 | 0.02809 | 0.016854 | 0.011236 | 0 | 0 | 0 | 0 | 0 |
| 1 | 0.527473 | 0.21978 | 0.049451 | 0.038462 | 1 | 0 | 0 | 0 | 0 |
| 2 | 0.734463 | 0.146893 | 0.028249 | 0.028249 | 2 | 0 | 0 | 0 | 0 |
| 3 | 0.36612 | 0.234973 | 0.054645 | 0.054645 | 3 | 0 | 0 | 0 | 0 |
| 4 | 0.093923 | 0.038674 | 0.033149 | 0.016575 | 4 | 0 | 0 | 0 | 0 |
| 5 | 0.708791 | 0.478022 | 0.021978 | 0.021978 | 5 | 0 | 0 | 0 | 0 |
| 6 | 0.127072 | 0.121547 | 0.016575 | 0.016575 | 6 | 0 | 0 | 0 | 0 |
| 7 | 0.346369 | 0.145251 | 0.100559 | 0.072626 | 7 | 0 | 0 | 0 | 0 |
| 8 | 0.454023 | 0.333333 | 0.132184 | 0.126437 | 8 | 0 | 0 | 0 | 0 |
| 9 | 0.655556 | 0.538889 | 0.055556 | 0.044444 | 9 | 0 | 0 | 0 | 0 |









Q5. K-means

| k-means Clustering Error PCA reduced | k=2 dim | k=8 dim | k=64 dim | k=2 dim | k=8 dim | k=64 dim |
|--|------------|----------|----------|------------|----------|----------|
| | Training E | rror | | Test Error | | |
| Class=0 | 0.91573 | 0.629213 | 0.010638 | 0.179775 | 0.02809 | 0.005618 |
| Class=1 | 0.681319 | 0.93956 | 0.660668 | 0.582418 | 0.549451 | 0.153846 |
| Class=2 | 0.785311 | 0.903955 | 0.331579 | 0.412429 | 0.587571 | 1 |
| Class=3 | 0.956284 | 0.89071 | 0.203085 | 0.759563 | 0.393443 | 1 |
| Class=4 | 0.839779 | 0.801105 | 0.105943 | 0.486188 | 0.98895 | 0.044199 |
| Class=5 | 1 | 0.901099 | 1 | 0.631868 | 0.307692 | 0.483516 |
| Class=6 | 1 | 0.861878 | 0.119363 | 0.19337 | 0.077348 | 0.044199 |
| Class=7 | 0.614525 | 0.905028 | 0.232558 | 0.256983 | 0.039106 | 0.044693 |
| Class=8 | 1 | 0.896552 | 0.210526 | 1 | 1 | 0.247126 |
| Class=9 | 0.783333 | 0.794444 | 0.353403 | 1 | 0.616667 | 0.227778 |

| k-means Clustering Error | k=2 dim | k=8 dim | k=64 dim | k=2 dim | k=8 dim | k=64 dim |
|-----------------------------|-------------|----------|----------|------------|----------|----------|
| LDA reduced | | | | | | |
| | Training Er | ror | | Test Error | | |
| Class=0 | 0.904494 | 0.668539 | 0.010638 | 0.106742 | 1 | 0.005618 |
| Class=1 | 0.78022 | 0.60989 | 0.660668 | 0.565934 | 0.346154 | 0.153846 |
| Class=2 | 0.80791 | 0.824859 | 0.331579 | 0.700565 | 0.259887 | 1 |
| Class=3 | 0.715847 | 1 | 0.203085 | 0.273224 | 0.038251 | 1 |
| Class=4 | 0.944751 | 0.889503 | 0.105943 | 0.513812 | 0.679558 | 0.044199 |
| Class=5 | 1 | 0.785714 | 1 | 0.708791 | 0.021978 | 0.483516 |
| Class=6 | 1 | 0.917127 | 0.119363 | 0.060773 | 0.016575 | 0.044199 |
| Class=7 | 0.793296 | 1 | 0.232558 | 0.675978 | 0.357542 | 0.044693 |
| Class=8 | 1 | 1 | 0.210526 | 0.804598 | 0.16092 | 0.247126 |
| Class=9 | 0.633333 | 0.927778 | 0.353403 | 0.461111 | 0.327778 | 0.227778 |

Q6. GMM

| GMM Clustering Error PCA reduced | k=2 dim | k=8 dim | k=64 dim | k=2 dim | k=8 dim | k=64 dim |
|--|--------------|----------|----------|------------|----------|----------|
| | Training Err | or | | Test Error | | |
| Class=0 | 1 | 0.007979 | 1 | 1 | 1 | 1 |
| Class=1 | 1 | 0.015424 | 1 | 1 | 1 | 1 |
| Class=2 | 0.010526 | 1 | 0.442105 | 0.19209 | 0.248588 | 0.610169 |
| Class=3 | 1 | 1 | 1 | 1 | 1 | 1 |
| Class=4 | 0.162791 | 1 | 0.741602 | 1 | 1 | 1 |
| Class=5 | 1 | 1 | 0.109043 | 0.153846 | 1 | 1 |
| Class=6 | 0.015915 | 1 | 0.02122 | 0 | 0.005525 | 0.005525 |
| Class=7 | 0.124031 | 0.178295 | 1 | 0.435754 | 0.128492 | 0.888268 |
| Class=8 | 1 | 1 | 1 | 1 | 1 | 1 |
| Class=9 | 1 | 1 | 1 | 1 | 1 | 1 |

| GMM | k=2 dim | k=8 dim | k=64 dim | k=2 dim | k=8 dim | k=64 dim |
|------------------|-------------|----------|----------|------------|----------|----------|
| Clustering Error | | | | | | |
| LDA reduced | | | | | | |
| | Training Er | ror | | Test Error | | |
| Class=0 | 1 | 1 | 1 | 1 | 1 | 1 |
| Class=1 | 1 | 0.005141 | 1 | 1 | 1 | 1 |
| Class=2 | 1 | 1 | 0.442105 | 1 | 0.00565 | 0.610169 |
| Class=3 | 0 | 1 | 1 | 0.010929 | 1 | 1 |
| Class=4 | 1 | 0.010336 | 0.741602 | 1 | 0.005525 | 1 |
| Class=5 | 1 | 1 | 0.109043 | 1 | 0 | 1 |
| Class=6 | 0.015915 | 1 | 0.02122 | 1 | 0.027624 | 0.005525 |
| Class=7 | 0.067183 | 0.002584 | 1 | 0.039106 | 1 | 0.888268 |
| Class=8 | 1 | 1 | 1 | 1 | 1 | 1 |
| Class=9 | 1 | 1 | 1 | 1 | 1 | 1 |

Q7. Agglomerative

| Agglomerative Clustering Error PCA reduced | k=2 dim | k=8 dim | k=64 dim | k=2 dim | k=8 dim | k=64 dim |
|--|-------------|----------|----------|------------|----------|----------|
| | Training Er | ror | | Test Error | | |
| Class=0 | 0.212766 | 0.005319 | 0.005319 | 0.702247 | 0.005618 | 0 |
| Class=1 | 0.832905 | 0.174807 | 0.735219 | 0.637363 | 0.016484 | 0.175824 |
| Class=2 | 0.360526 | 0.055263 | 0.297368 | 0.305085 | 1 | 0.706215 |
| Class=3 | 1 | 0.316195 | 0.210797 | 0.650273 | 1 | 1 |
| Class=4 | 0.54522 | 1 | 0.385013 | 0.093923 | 0.447514 | 0.077348 |
| Class=5 | 1 | 0.611702 | 0.079787 | 0.510989 | 0.10989 | 0.824176 |
| Class=6 | 0.076923 | 1 | 0.106101 | 0.138122 | 0.049724 | 0.005525 |
| Class=7 | 0.108527 | 0.178295 | 0.865633 | 0.916201 | 0.396648 | 0.156425 |
| Class=8 | 0.428947 | 0.215789 | 0.05 | 1 | 0.701149 | 0.982759 |
| Class=9 | 1 | 0.117801 | 0.748691 | 0.944444 | 0.238889 | 1 |

| Agglomerative Clustering Error LDA reduced | k=2 dim | k=8 dim | k=64 dim | k=2 dim | k=8 dim | k=64 dim |
|--|-------------|----------|----------|------------|----------|----------|
| | Training Er | ror | | Test Error | • | • |
| Class=0 | 0.093085 | 0.005319 | 0.005319 | 0.078652 | 0.011236 | 0 |
| Class=1 | 0.390746 | 0.041131 | 0.735219 | 1 | 0.631868 | 0.175824 |
| Class=2 | 1 | 0.028947 | 0.297368 | 0.734463 | 0.079096 | 0.706215 |
| Class=3 | 0.25964 | 0.028278 | 0.210797 | 0.644809 | 0.081967 | 1 |
| Class=4 | 0.514212 | 0.082687 | 0.385013 | 0.138122 | 0.033149 | 0.077348 |
| Class=5 | 0.827128 | 0.034574 | 0.079787 | 1 | 0.791209 | 0.824176 |
| Class=6 | 0.249337 | 0.01061 | 0.106101 | 0.171271 | 0.773481 | 0.005525 |
| Class=7 | 0.571059 | 0.79845 | 0.865633 | 0.251397 | 0.027933 | 0.156425 |
| Class=8 | 1 | 0.692105 | 0.05 | 0.356322 | 1 | 0.982759 |
| Class=9 | 0.575916 | 1 | 0.748691 | 0.361111 | 0.027778 | 1 |