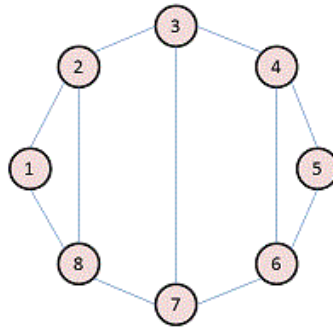


Communities

Question 1:

For the following graph:



Write the adjacency matrix A , the degree matrix D , and the Laplacian matrix L . For each, find the sum of all entries and the number of nonzero entries.

① Ans

Adjacency matrix:

	1	2	3	4	5	6	7	8
1	0	1	0	0	0	0	0	1
2	1	0	1	0	0	0	0	1
3	0	1	0	1	0	0	1	0
4	0	0	1	0	1	1	0	0
5	0	0	0	1	1	0	0	0
6	0	0	0	1	1	0	1	0
7	0	0	1	0	0	1	0	1
8	1	1	0	0	0	0	1	0

No. of non zero entries = 22

Sum of all entries = 22

Degree matrix:- \rightarrow No. of non-zero entries = 8
Sum of all entries = 8

	1	2	3	4	5	6	7	8
1	2	0	0	0	0	0	0	0
2	0	3	0	0	0	0	0	0
3	0	0	3	0	0	0	0	0
4	0	0	0	3	0	0	0	0
5	0	0	0	0	2	0	0	0
6	0	0	0	0	0	3	0	0
7	0	0	0	0	0	0	3	0
8	0	0	0	0	0	0	0	3

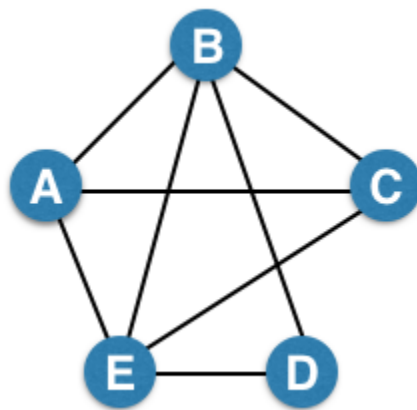
Laplacian Matrix ($L = D - A$)

	1	2	3	4	5	6	7	8
1	3	-1	0	0	0	0	0	-1
2	-1	3	-1	0	0	0	-1	0
3	0	-1	3	-1	0	0	-1	0
4	0	0	-1	3	-1	-1	-1	0
5	0	0	0	-1	3	-1	-1	0
6	0	0	0	-1	-1	3	-1	0
7	0	0	-1	0	0	-1	3	-1
8	-1	-1	0	0	0	0	-1	3

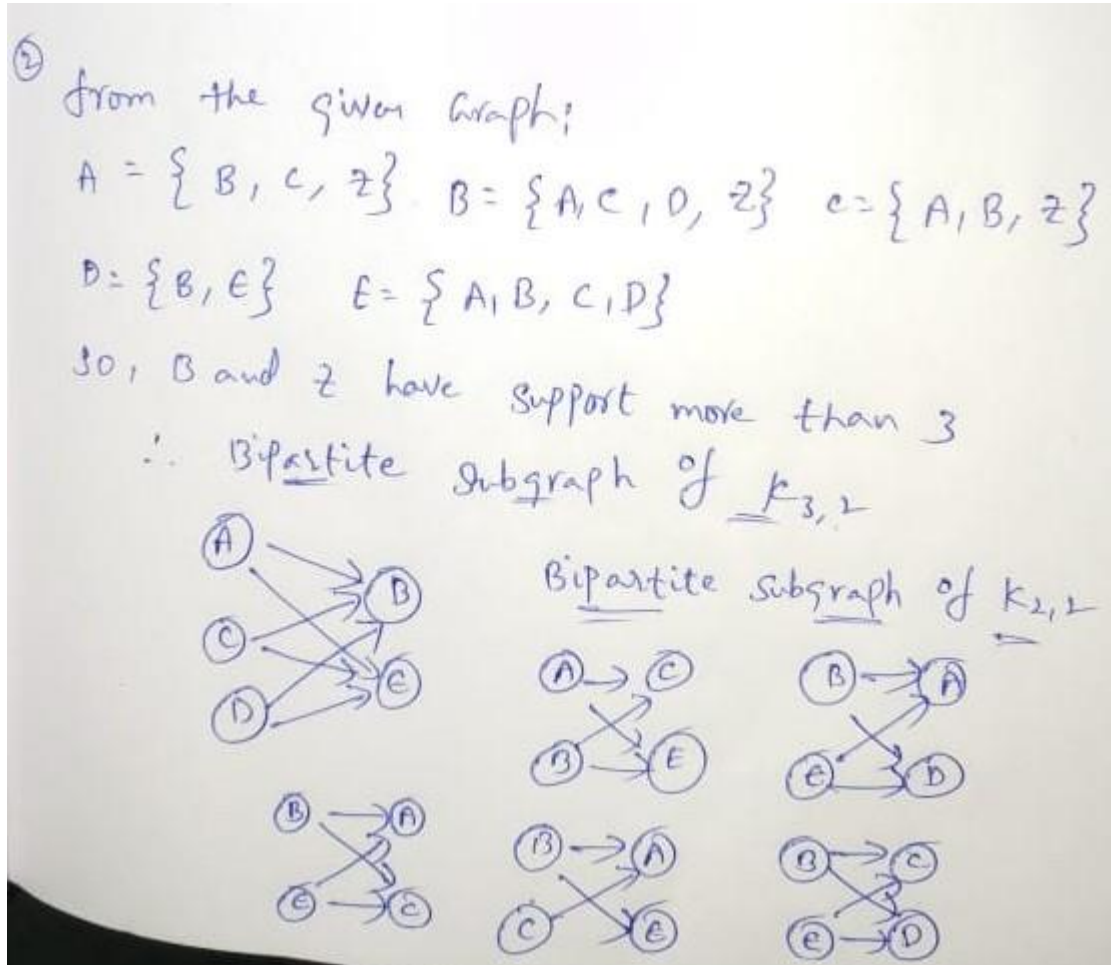
→ No. of non-zero entries = 30
 → Sum of all entries = 0

Question 2:

Consider the following undirected graph (i.e., edges may be considered bidirectional):

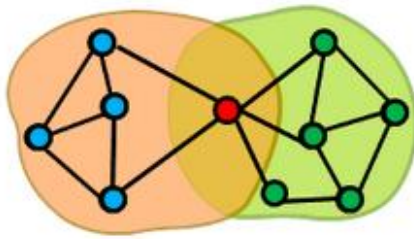


Run the "trawling" algorithm for finding dense communities on this graph and find all complete bipartite subgraphs of types $K_{3,2}$ and $K_{2,2}$. Note: In the case of $K_{2,2}$, we consider $\{\{W, X\}, \{Y, Z\}\}$ and $\{\{Y, Z\}, \{W, X\}\}$ to be identical.

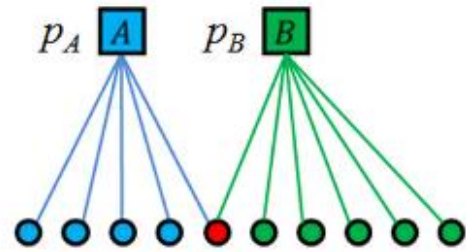


Question 3:

We fit AGM to the network on the left, and found the parameters on the right:



Network



Learned AGM parameters

Find the optimal values for p_A and p_B .

Ques

a) $p_a = \frac{\text{No. of edges in the network}}{\text{Total possible no. of edges}}$
 $= \frac{7}{SC_2} = \frac{7}{10} = 0.7$

b) $p_b = \frac{\text{No. of edges in the network}}{\text{Total possible no. of edges}}$
 $= \frac{9}{SC_2} = \frac{9}{15} = 0.6$