

170727

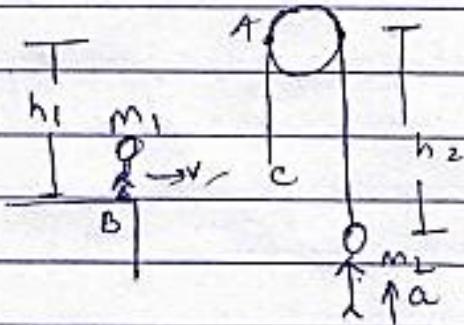
170471

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Q.



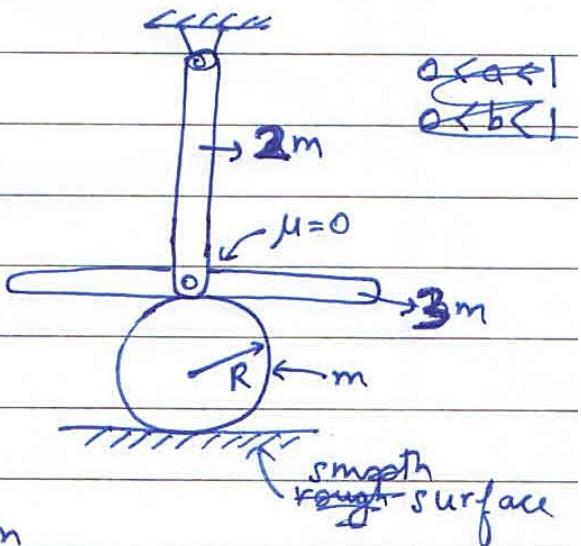
There are two monkeys and a rope-pulley system. One of the monkey jumps on and holds the rope with velocity  $v$ . At the same moment, the other monkey starts climbing up. Both the monkeys are climbing with same acceleration and one of them Radially is having small oscillations about  $A$ .

Find tension. Consider the distance between B and C to be very less. Assume ideal pulley and rope.

{ Find total instantaneous tension in string after the monkey jumps }

Q) A rod is hinged to the ceiling, and is hinged further at the centre of another rod.

Both have equal lengths.



A disc of radius  $R$  and mass  $m$  is under the horizontal rod (not connected), and on a smooth surface.

There is pure rolling everywhere.

The disc is displaced slightly. Find the time period of oscillations.

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SUMIT KUMAR SUMAN 170731

PARIMAL MUKUL 170460

ANKIT KUMAR 170123

RAGHAV AGRAWAL 170519

## Group

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37 Nikhil S. Pannar	- 160451
47 Ashigyan Verma	- 160013
57 Pragya Patel	- 170477

## Question

A rod of length  $l$ , mass  $m$  is tied at its end by two strings of length ( $L$ ). as shown in fig 1. Now the figure system is given a small -angular displacement  $\theta$  about the  $z$ -axis as shown fig.2.  
Find the frequency of small oscillations. ( $\omega_0$ ).

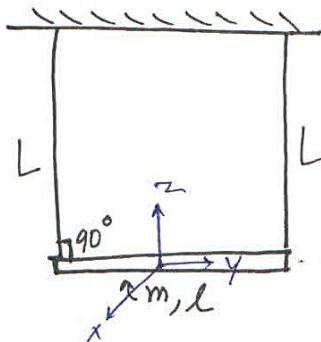


FIGURE 1

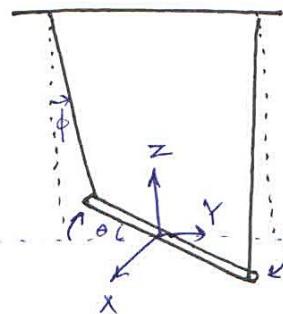


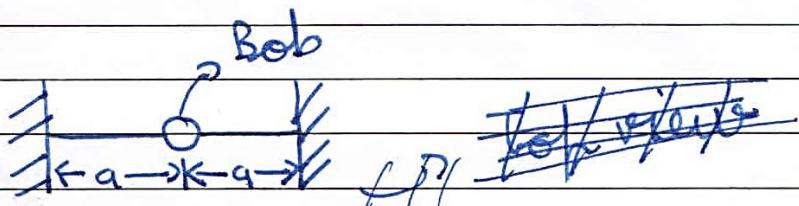
FIGURE 2

# ESO 209-DYNAMICS

Page \_\_\_\_\_

## QUIZ

- ① 170252 DINESH
- ② 170051 Aditya Sarkar
- ③ 170061 Aditya Tiwari
- ④ 170113 ANIMESH NAREDA
- ⑤ 170115 ANIRUDH ~~SHARMA~~



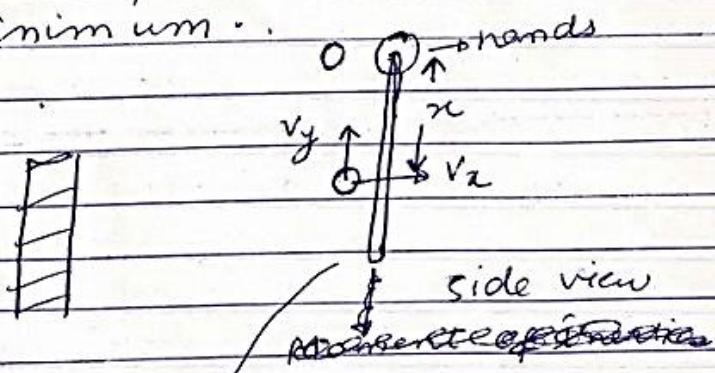
- ⑥ A small particle of mass  $M_{Bob}$  is attached to 2 highly tensioned wires as shown. Determine the natural frequency  $\omega_0$  of the system for a small oscillation (vertical). The tension in both wire is given  $T$  and is constant.

D. In a cricket match,  
A bowler delivers a ball which follows  
The batsman plays a straight drive.

Problem is to find the sweet spot of the bat so that the impulsive force on the hands of batsman is minimum.

Assumptions: The motion of bat before and after the shot is assumed to be negligible. Surface of bat is assumed to be flat.  
(Bat is a non-uniform object of mass).

Given : i)  $v_x$  and  $v_y$  of the Ball before collision.  
ii) Moment of Inertia of the bat is given.  
iii) Coefficient of restitution  $e$  is given.  
iv) Linear mass density  $\mu(x)$  of bat is given.  
To find : The distance from the hands of the point of contact of ball and the bat so that the reaction force (impulsive) at the hands is minimum.



(ii) Linear Mass Density  
of bat =  $\mu x$

(iii)  $e$  (coefficient of restitution is given).

Given :- i)  $v_x, v_y$  of ball.

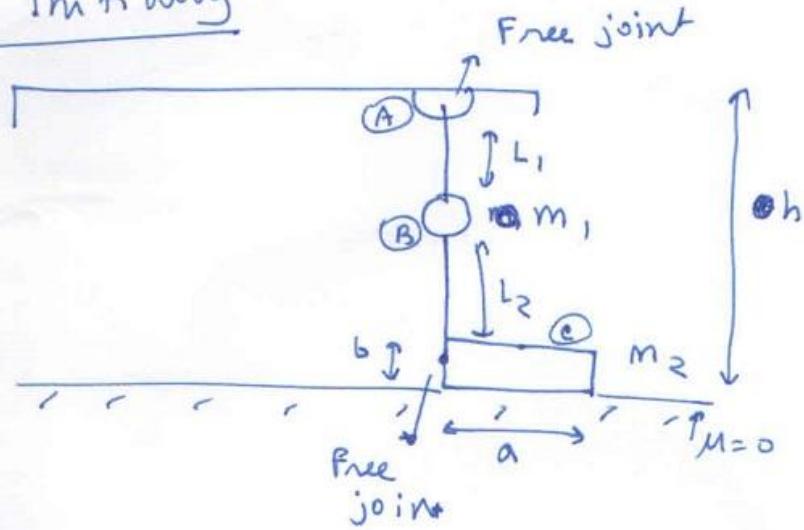
ii) Mass density (per unit length) =  $\mu x$   
( $x$  is distance from hand)

(iii)  $e$  is given.

NITISH	KUMAR	170999
LICHA	TALO	160366
MAHIPAL	BERA	170369
SHEKHAR	SAINI	170661
SHUBHAM	RAJ	170688

This is Nitish Kumar, ESO 209 student. Sir i would like to make slight change in the question submitted by our group. Instead of giving linear mass density of the bat, it's moment of inertia about the point from where it's held is given as  $I_0$ . Also the position of centre of mass with respect to held point is given. The length of bat is  $L$  (given).

Initially:



170052-Aditya

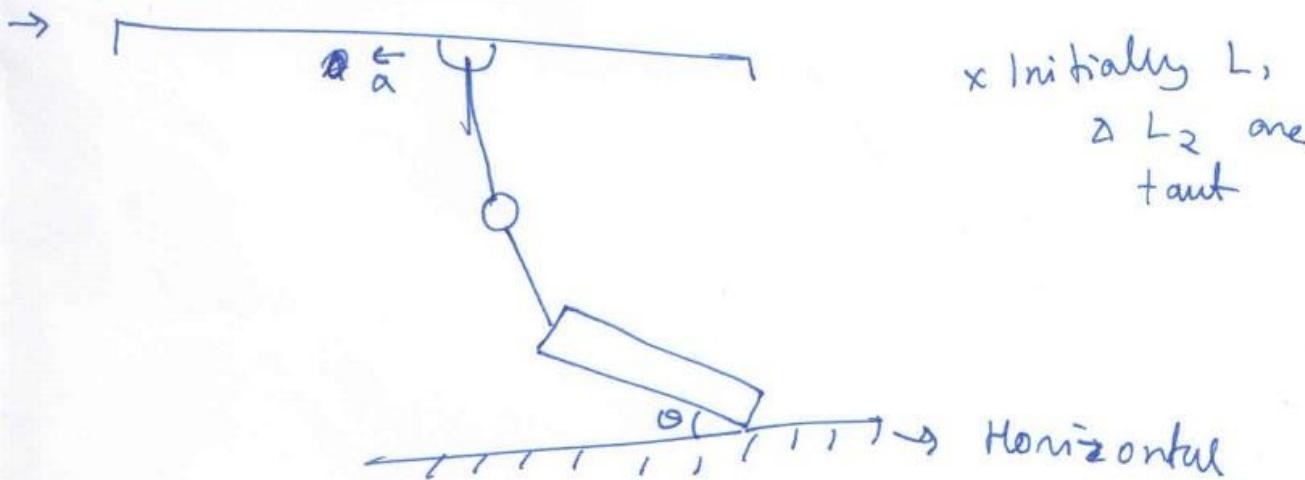
170013-Abhay

170296 → Hemant

170097-Amarendra

170389-Arjun

(A) is accelerated to left with acceleration  $\alpha$



x Initially  $L_1$   
Δ  $L_2$  one  
+ and

Find  $\theta$  in steady state

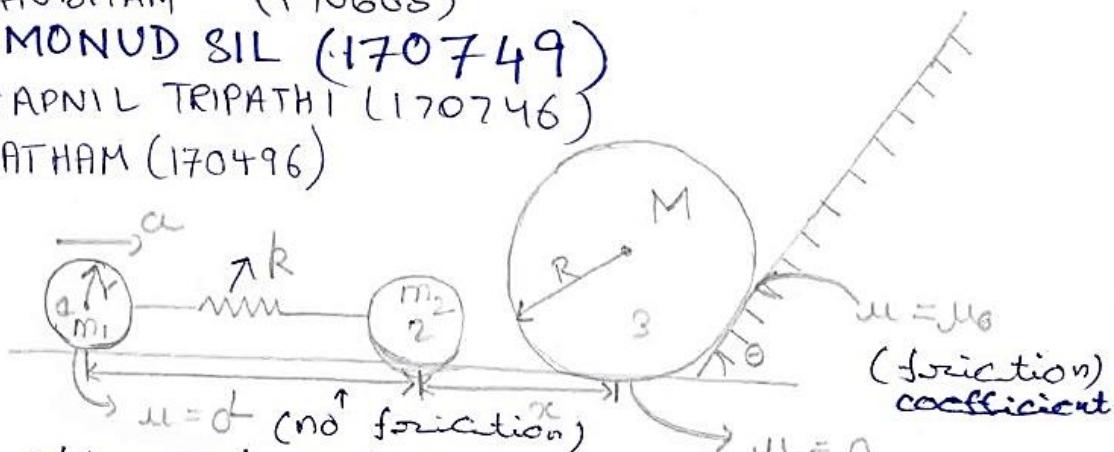
① TRIPTESH BISWAS (170757)

② SHUBHAM (170685)

③ TAMONUD SIL (170749)

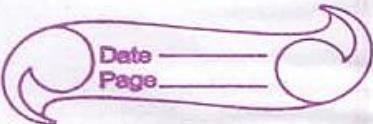
④ SWAPNIL TRIPATHI (170746)

⑤ PRATHAM (170496)

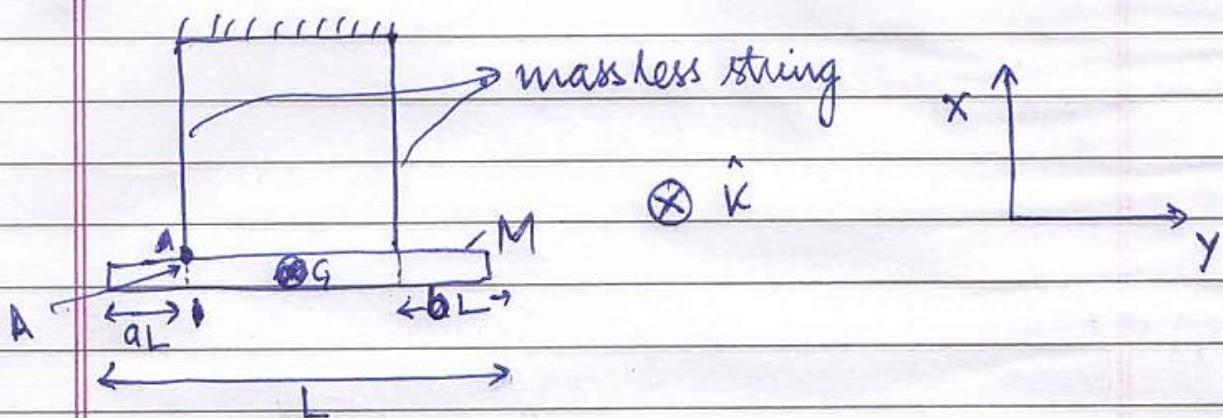


- Two sphere of radius  $r$  mass  $m_1$  and  $m_2$ .
  - One large sphere of radius  $R$  mass  $M$ .
  - friction coefficient between the spheres  $\mu = 0$
  - the mass  $m_1$  is given an acceleration  $a$  towards right, ~~simultaneously~~  
the mass  $m_2$  approaches mass  $M$  and makes a contact.
- a) Find the range of  $\theta$  that the mass  $M$  climbs up the inclined plane without leaving contact (i.e. the sphere may bounce off).
- b) If the mass  $M$  climbs up find the distance travelled by it on the inclined plane.

- 1) 170805 VISHESH KAUSHIK  
 2) 170333 KARAN VAISH  
 3) 170362 LAVPREET SINGH  
 4) 170235 DEEPANSHU KATARE  
 5) 170081 AMAN GAUTAM



Q



Impulse is given inward at point A that is equal to  $J \hat{k}$ .

Will the system perform SHM, if yes then find the angular frequency of small oscillation.

Assume  $J$  to be small

And angular displacement is ' $\alpha$ '  
(AMPLITUDE)

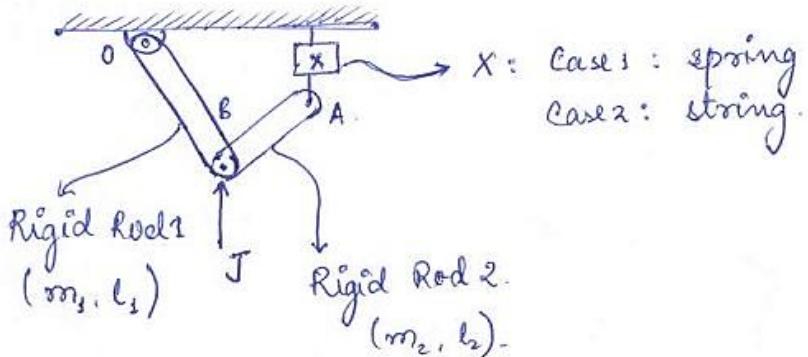
3rd Nov 2019

QUIZ

ESO 209

YASH RATSINGH - 170819  
SUYASH SINGH - 170743  
SHASHANK BUCHASIA - 170654  
PRIYANSHU SAXENA - 170513  
SATHVIK BHAGAVAN - 170638

QUESTION :

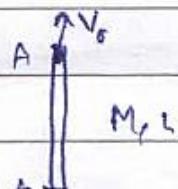
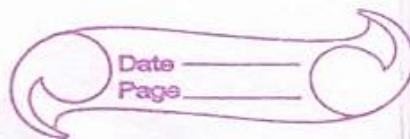


X : Case 1 : spring  
Case 2 : string.

The above system contains 2 rigid rods, one of them hinged at O with the wall/ceiling) and the other hinged at the end of the first rod at B. The element X attached to the ceiling at one end and to the second rod at the other end. A vertical impulse ( $J$ ) is applied at point "B".

- Supposing "X" to be a spring of spring constant ( $k$ ) Calculate the velocity of point A.
- Supposing "X" to be a string, calculate the velocity of point A.
- Analyse the Answers for the two cases.

RISHU KATIYAR (170575)  
 VIJIT MALIK (170791)  
 SHASHANK KUMAR (170653)  
 AAIYUSH KAPURWAN (170002)  
 HEMRAS MEENA (170299)

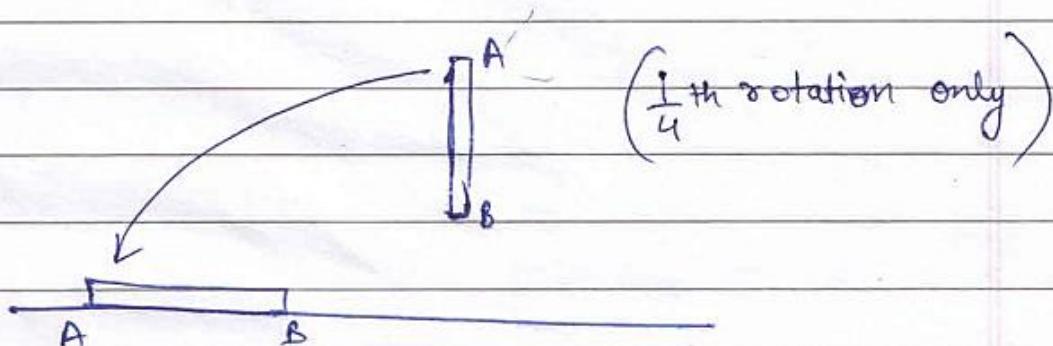


Fig(a)

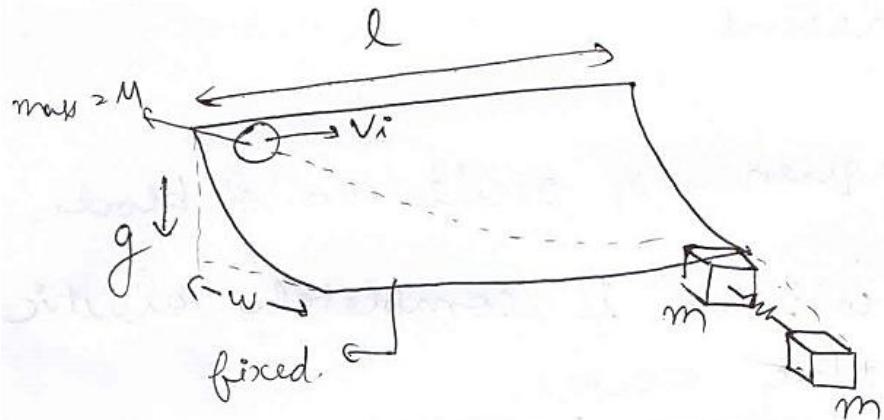
ground

Initially, a rod of length  $l$ , mass  $M$  is thrown vertically from the ground with an initial velocity  $v_0$ . When it reaches its max<sup>m</sup> height, a bead of mass,  $m$ , with a velocity (horizontal)  $v$  strikes at the top of the rod and gets embedded.

- What is the velocity (in terms of  $v_0$ ) of the bead so that the (rod + bead) system strikes the ground horizontally without any complete rotation. (Refer Fig (b))
- Calculate the time taken, for the same (in part A)

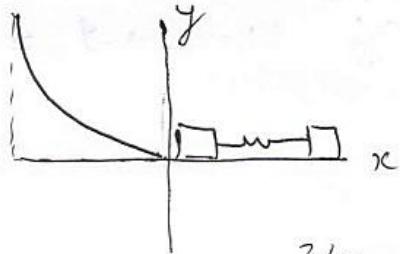


Fig(b)



Roll no.	Name ..
170019	ABHINAV
160812	NIVEK
170323	JAYANT
14074 / 14807074	AMAN
160016	ABHINA

Profile view:



$$\text{Eq}' \text{ of curve} \Rightarrow y = (-x)^{3/2}$$

The blocks are perfectly aligned with the wedge.

The ball starts from the position shown with only a horizontal component of the velocity initially.

The velocity is such that the ball always hits the block closer to the wedge.

Dimensions of wedge are as marked in figure.

(i) Friction absent.

(a) Find  $v_i$ .

(b) Find frequency of oscillation of blocks.

(ii) Friction present

(a) Find  $v_i$ :

(b) Find frequency of oscillation of blocks.

The collision is completely elastic  
in both the cases.

Also, spring constant  $\neq k$ .

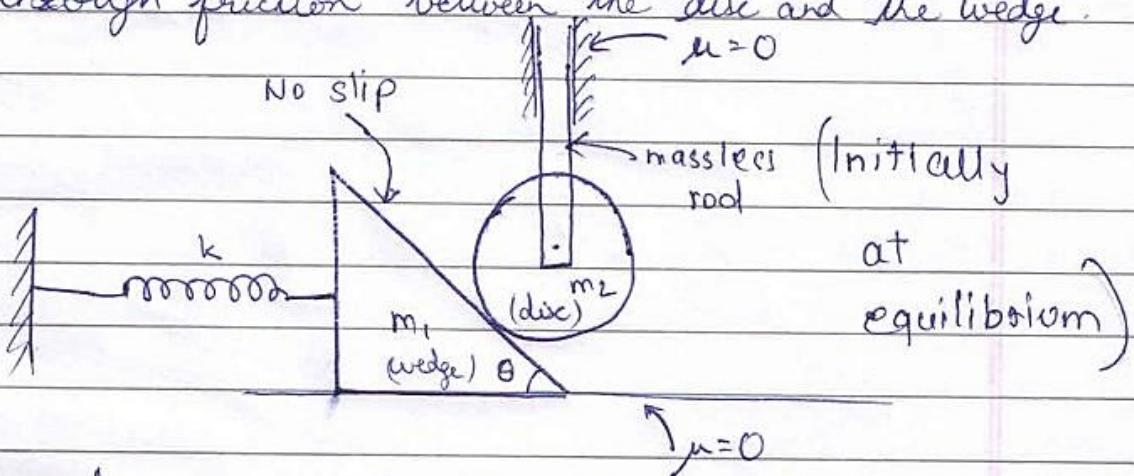
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## Surprise Quiz

Sameer Kumar Singh	170618
Himanshu Pandey	170301
Abhishek Mugal	170028
Kratik Jain	170345
Rohit Saini	170595

- Q. See the setup given below. A spring of spring constant  $k$  is fixed to the ground and connected to a wedge of mass  $m_1$ . A disc of mass  $m_2$  is placed such that ~~there is no slip condition~~ between the wedge and the disc. The disc is constrained to move only in the vertical direction. Initially the setup is at rest and in equilibrium. Assume no friction ~~b/w~~ the ground and the wedge and enough friction between the disc and the wedge.



Find frequency for small oscillations.

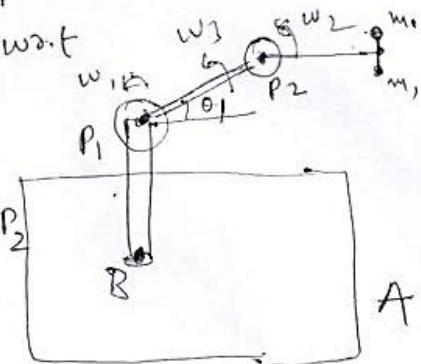
Q1. pulley  $P_1$  rotates anticlockwise =  $\omega_1$

$$P_2 \text{ " " } = \omega_1 \text{ w.r.t } P_1$$

$$m_1 \text{ & } m_2 \text{ " " } \omega_2 \text{ w.r.t } P_2$$

The system moves with

velocity on plane A.



Find velocity of  $m_1$  &  $m_2$ ?

Roll No : 170201

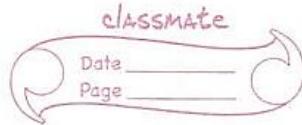
170295

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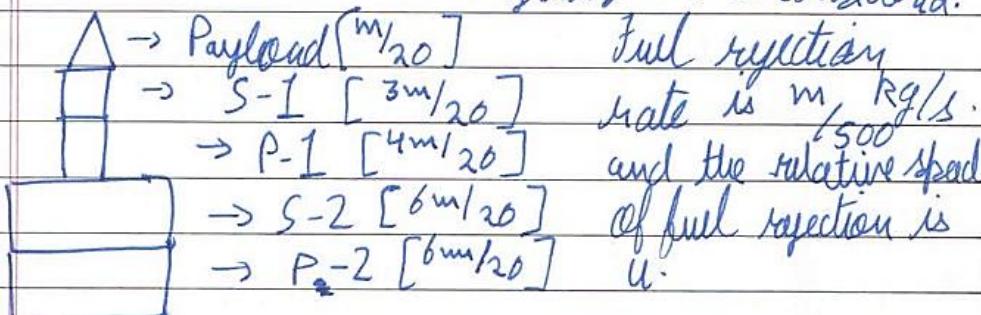
Name	Roll
ANISH SAXENA	170118
INSHU NAMDEV	170308
BHAVES SAXENA	170210
SUDHANSHU MISHRA	170726
PRADEEP SHUKLA	170497



Problem: A rocket, consisting of 5 different stages including the payload, S-1, S-2, P-1 and P-2. P-1 and P-2 are propellant masses while S-1 and S-2 are structural masses.

The rocket reaches the outer space only with the payload stage and the rest of the mass is rejected in space on the way in the stages as follows:

→ Gravity is to be considered.



The sequence of separation is:  
 P-2 followed by S-2 then  
 P-1 then S-1.

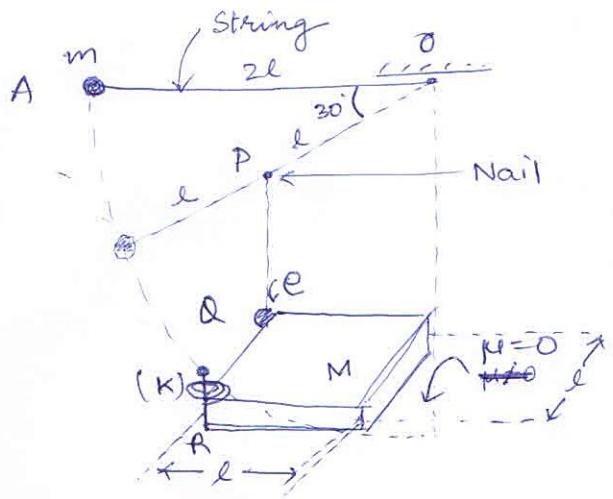
→ ~~that~~ Stage is separated as soon as fuel is emptied.

sked

Q1. Find the final velocity of the payload given initial speed is  $v_0$  vertically upwards.

Q2. Subsequent structural masses (S-1 and S-2) are ejected after time to separation of P-1 and P-2 respectively. complete P.T.O

Q2. Plot the vel speed dependence as a function  
of time.  $V(t=0) = V_0$ .

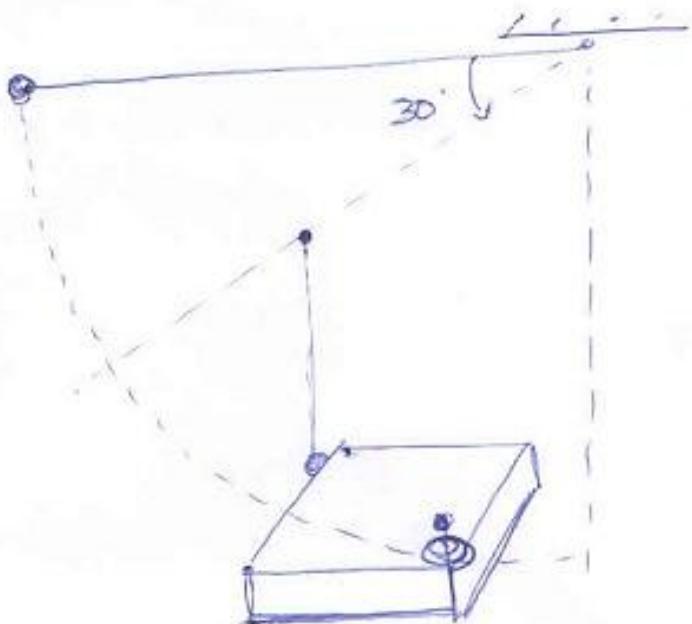


A ball of mass  $m$ , released from point A. The ball is attached to an inextensible string of length  $2l$  from point O. A nail is attached at point P, which obstructs the motion of the string.

The ball collides with the box of mass 'M' at point Q. The box is hinged at point R and a spring is attached at R of torsional constant ( $k$ ). The coefficient of restitution is 'e'.

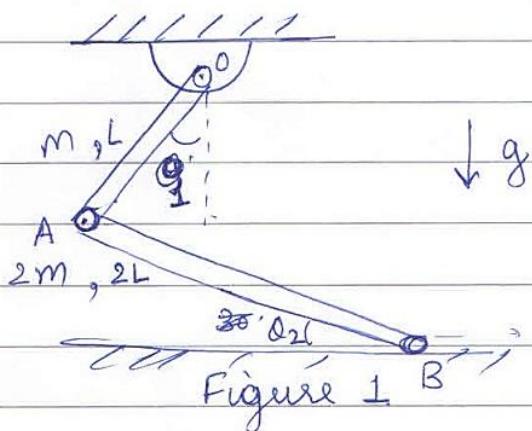
Find the time taken for the block to stop reach max<sup>m</sup> angular displ.  
 (b) Maximum angular displacement of the box

ROLL NOS - 170307, 170257, 170506, 170325, 170317



Hvani Srivastava	-	170178
Maitreyee Srivastava	-	170371
Pratigya Tomar	-	190499
Priyakree Kachari	-	170509
Manoj Kumar	-	14372

(Ques)



In the given figure an impulse of  $2N$  at  $2N$ s at point  $B$  is given initially.

$$\theta_1 = 60^\circ, \theta_2 = 30^\circ, L = 1m, m = 1kg$$

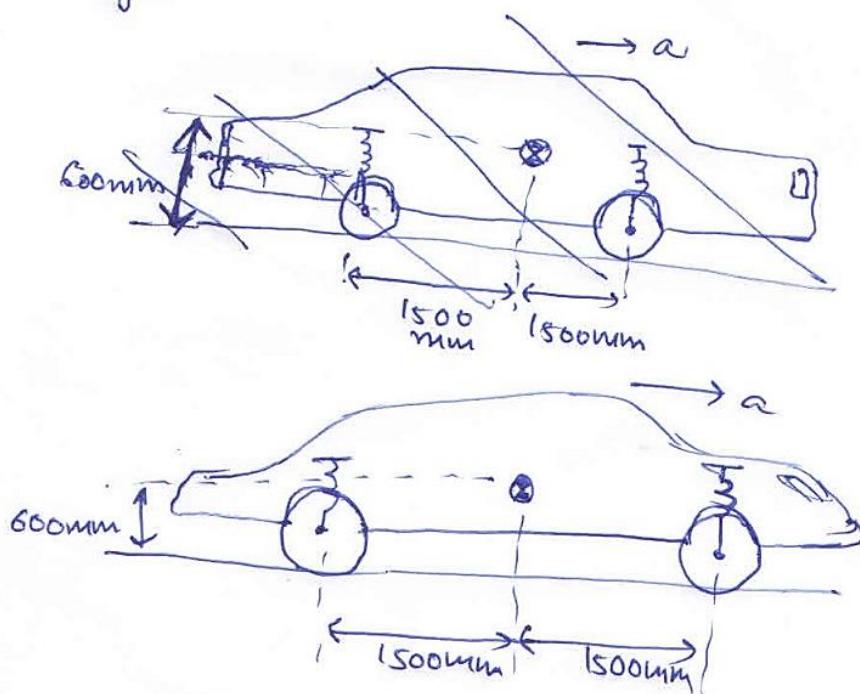
~~rod~~ B Point B slides frictionlessly on the ground.

At the instant when  $\theta_1 = 0^\circ$ , find  $W_{OA}$ . (~~rod~~ OA).

Joints are frictionless.

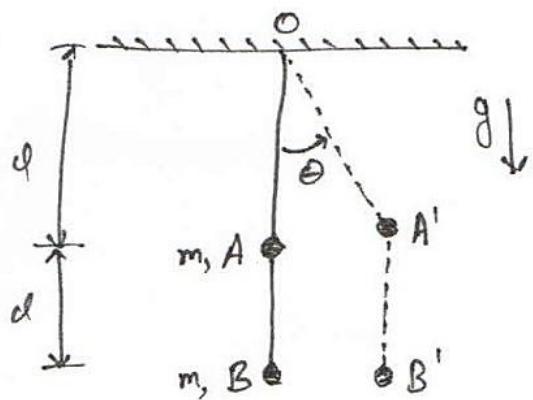
TEAM: ① PULKIT PANDEY - 170516  
 ② AKASH KUMAR - 170069  
 ③ NAVEEN BALAJI - 170420  
 ④ VIPIN - 170800  
 ⑤ ADITHYA SINGH - 170056

Q. A 1ton rear wheel drive accelerates forward at  $\alpha = g/3$ .  
 If the spring constant of both rear and front wheels are  $40\text{KN/m}$   
 estimate the resulting momentary nose-up pitch angle  $\theta$ .  
 Neglect unsprung mass of tires and wheels. Consider vehicle rigid.



Roll No → (150753), (14287), (170193), (160063), (14088)  
(Swarnit), (Manmohan), (Ashaan), (Akash), (AMIT)

Q



what will be frequency of double-pendulum when  $\theta = 30^\circ$

& mass A is released from A'?

- mass A & B is attached with masses string
- $OA = AB = l$
- mass of A = mass of B = m

Roll no.

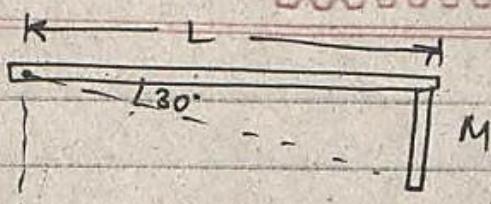
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PAGE NO.  
DATE

$t = 0$



$\leftarrow d_1 \rightarrow$

$$e = e_0$$

$m_1$

radius =  $r$   
solid Sphere

$h_1$

$\leftarrow d_2 \rightarrow$

$$e = 0$$



No losses occur

$$\frac{1}{4} = \alpha \quad M = 0.1$$

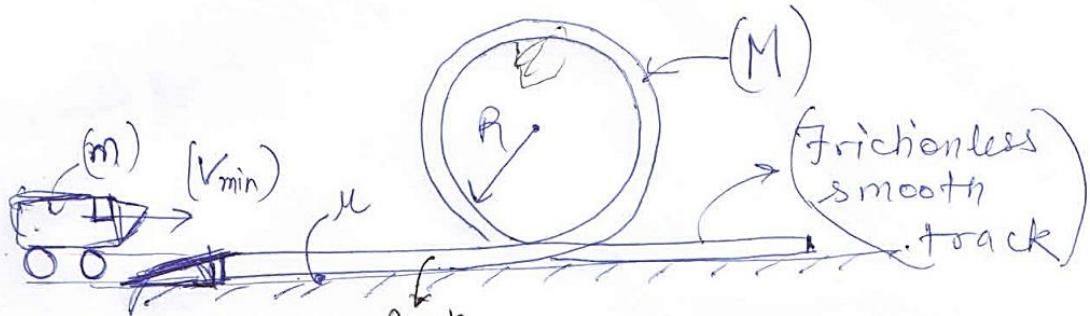
A rod L-Shaped is released from rest ( $\text{mass} = M$ )

it strikes with a ball of mass  $m_1$ , coefficient of restitution  $e_0$ . The ball moves down the wedge as shown in fig. No friction, No slipping occurs or no losses occur. After that it

strikes to mass  $m_2$  with  $e = 0$ . They both starts to free fall (Projectile motion).

If rod is released at  $t = 0$ , find to when

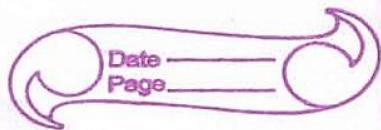
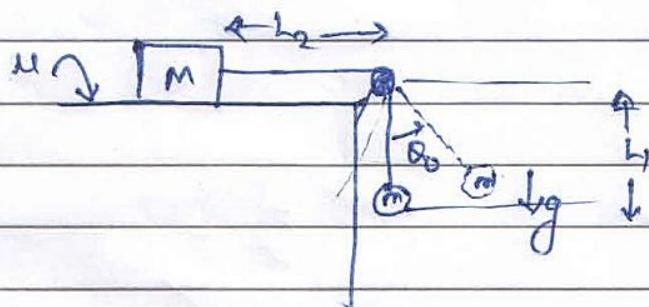
bullet should be fired ( $V_{\text{bullet}} = 200 \text{ m/s}$ ) Horizontally such that it strikes the combined mass system of  $m_1$  and  $m_2$ .



- Q) In a hot-wheels loop toy.
- Given a car of mass  $m$ . A ramp with a circular loop of radius  $R$  with mass  $M$ . The car is given an initial velocity  $V$ . The track is smooth. Coeff. of friction b/w the ramp and the ground is  $\mu$ . ( $\mu$  is sufficiently less). ~~for completion of loop.)~~ (which means  $m$  will also move)
- Find the minimum velocity for which the car completes the loop.

### Group members

Abhilash Choudhary	- 170016
Arpit Gupta	- 170145
Dayush Saini	- 170009
MANVENDRA SINGH	- 170381
RAM JASH JANGID	- 170552

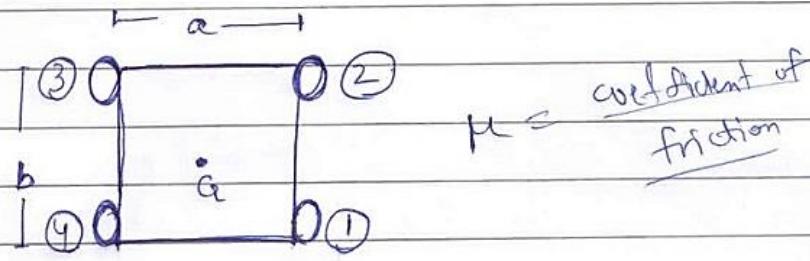
Soln

A block of mass  $M$  lies on a surface with coefficient of friction  $\mu$ , an another mass  $m$  hangs from the pulley (massless) connected to  $M$  with a string. At  $\theta_0$  an instant,  $m$  is given angular displacement  $\theta_0$ , and it starts undergoing oscillation.

With  $M, \mu, L, L_2$  given, find the maximum angular displacement  $\theta_0$  that can be provided so that ~~that~~  $L_2$  doesn't change.

Soln  $\Rightarrow$

Q



Toy cart with 4 wheels

wheel radius  $R$  Mass of cart excluding wheels =  $M$   
Mass of each wheel =  $m$

wheel ① and ② rotate more

(a) wheel ① and ② move forward with  $\omega$

wheel ③ and ④ move backward with  $\omega$

~~with~~ how much time ~~angular velocity~~ will it take  
for body to rotate  $360^\circ$  and about what point

(b) wheel ① and ② move forward with  $2\omega$

wheel ③ and ④ move backward with  $\omega$

~~with~~ how much time ~~angular velocity~~ will it take  
body to rotate  $360^\circ$  and about what point

~~Roller~~ ~~or~~ ~~apply~~ ~~no~~ ~~rolling~~

Roll Number

17071

170554

170596

170304

170340

MANJEET YADAV (170378)

NITIK JAIN (170448)

PRATEEK YADAV (170495)

RATNESH ARJAL 170559

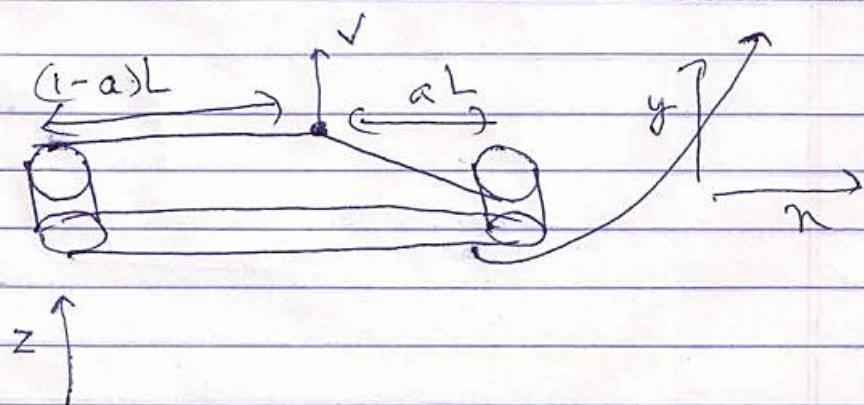
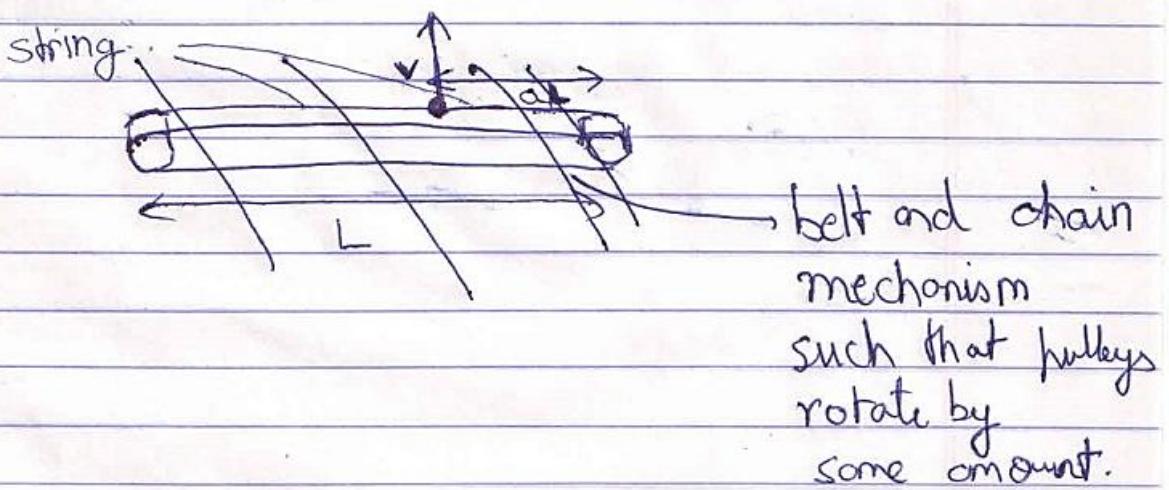
BALDIP 170203

(Q) A stone tied to 2 strings is shown as shown. The strings unfold on 2 pulley without slipping as shown.

It is given that the tension is constant in the both strings (assume that it possible). Find the end coordinates of stone given the initial velocity is vertical and  $v$ .

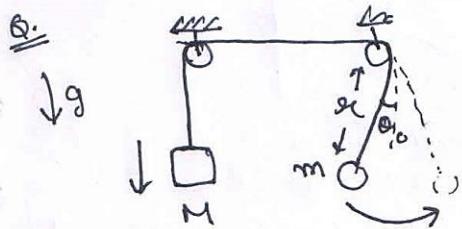
The stone has mass  $m$ .

→ Assume the pulleys to be very small as compared to the other distances in the problem.



1) ABHIEET	170015
2) MATARIA PENCE	170382
3) RATNANGSHU DAS	170558
4) AYUSH GUPTA	170191
5) GARVIT GOPAL	160261

---



$M$  is oscillating up and down

$m$  is swinging, with initial release angle  $\theta_0$

Find the equation of motion of  $m$ .

170 463

Parth Athole

170 761

Tushar Goswami

170 141

Apurva Nandan

170 147

Arikant Jain

170 354

Kumar Shivam

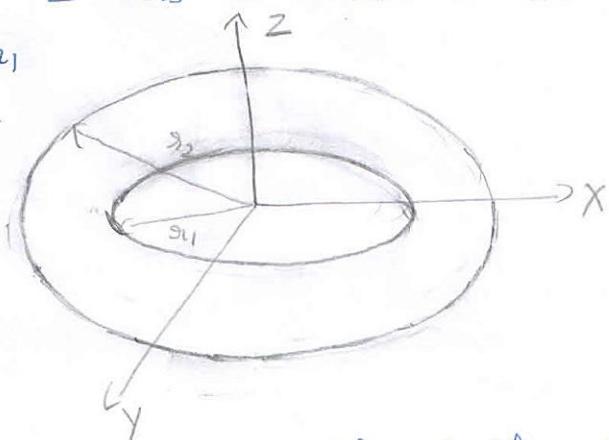
Q. Find the Moment of Inertia of a Torus (Donut)  
about the z axis as shown below:

Inner Radius =  $r_1$

Outer Radius =  $r_2$

Mass =  $m$

Density =  $\rho$



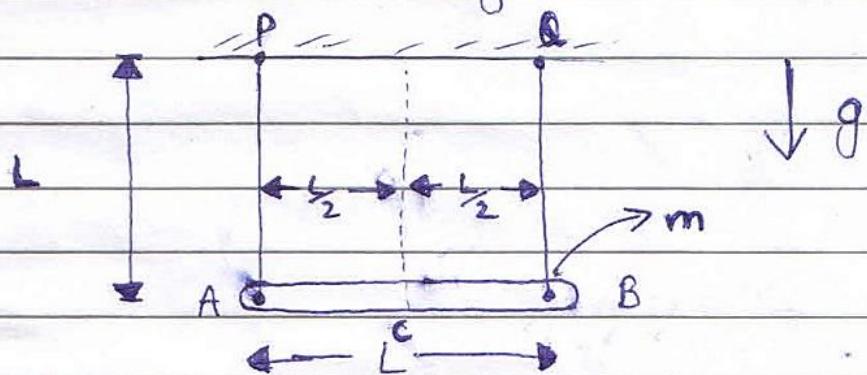
(z-axis passes through the center & perpendicular to the diameter)

Ans:  $I = \begin{bmatrix} \frac{m}{8} (5R^2 + 4\rho^2) & 0 & 0 \\ 0 & \frac{m}{8} (5R^2 + 4\rho^2) & 0 \\ 0 & 0 & \frac{m}{4} (3R^2 + 4\rho^2) \end{bmatrix}$

where  $R = r_2 - r_1$

Q) The rod AB of mass  $m$  and length  $L$  hangs at rest as shown, suspended by inextensible massless string PA and QB. String QB is cut. At the instant immediately afterwards :

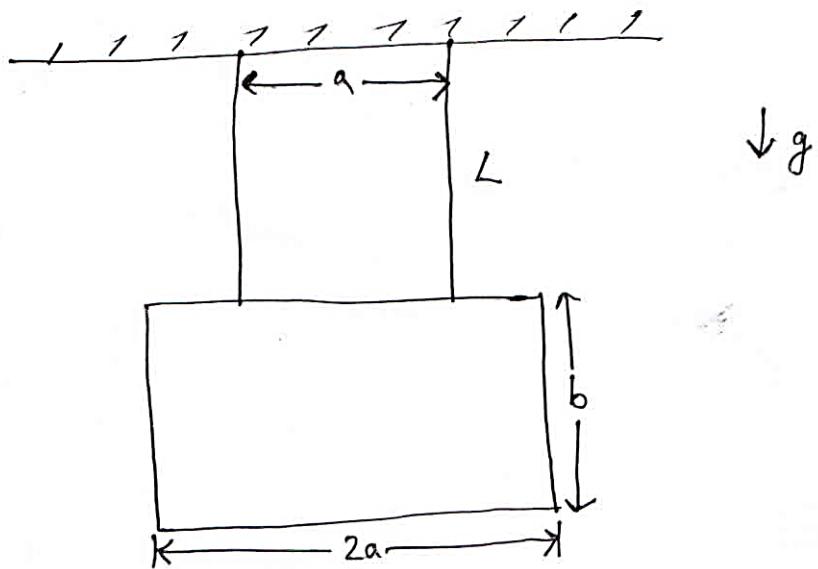
- i) Find the Tension in string PA.



{ Extra

Roll no:- 170303, 170768, 170162, 150555, 150569

Q.



A thin uniform rectangular metal sheet of mass  $m$ , and length  $2a$  and width  $b$  is hung by two strings of length  $L$  symmetrically as shown in the figure. For small oscillations find the frequency of metal sheet about the equilibrium.

170294 - HARSHIT RAI

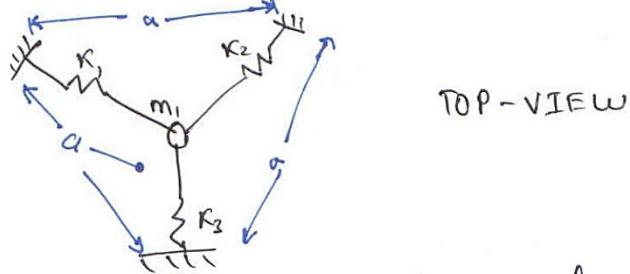
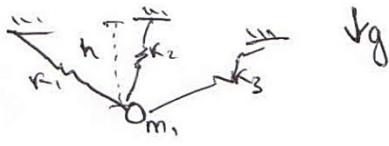
170414 - NAMAN JAIN

170207 - BHARAT SWAMI

170205 - BAROT DIVYANSHU  
BHARAT BHAI

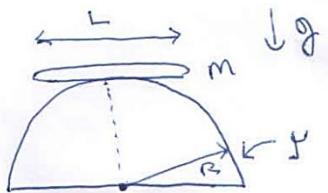
170807 - VIVEK GUPTA.

Ques: → A ball of mass 'm' is attached to 3 springs with spring constants  $k_1$ ,  $k_2$  &  $k_3$ . At  $t=0$ , the system is at equilibrium. Now ~~the~~ a mass 'm<sub>2</sub>' falls from a height 'h' above m<sub>1</sub> & strikes m<sub>1</sub> & sticks to it. a, Find the time period of oscillation of system of masses. (h = equilibrium height of m<sub>1</sub>)



b, also determine the ratio of h & the amplitude of the oscillations of the combined mass.

→ Make suitable assumptions, if needed



Given a fixed hemispherical inverted bowl with coefficient of friction  $\mu$

R.no.- 170019 (Abhirav)

160812 (Vivek)

170323 (JAYANT)

14074/4807074 (AMAN)

160016 (ABHINAV)

A thin rod of mass  $m$  & length  $L$  is placed on the bowl such that top most pt of bowl coincides with center of rod.

Find frequency of small oscillations of rod?

Extra

Group members :- Shivam Shekhar (170672)

Shashi Ranjan (170657)

Kush Bagla (170357)

Vijay Lather (170358)

Soumik Ghosh (170712)

~~Two beads of masses  $m$  &  $M (>>m)$  slide on a frictionless rod as shown in fig. Initially  $m$  is at rest and  $M$  moves with velocity  $V$  towards it. The distance between  $m$  and wall is  $L$ . All collisions are perfectly elastic. Find how close can the heavier  $M$  get to the wall.~~

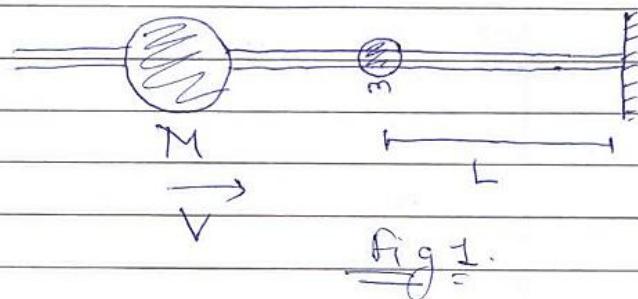


Fig 1.

Ques

Two beads of masses  $m$  &  $M (>>m)$  slide on a rigid rod as shown in fig. 1. Initially  $m$  is at rest and  $M$  moves with  $V$  velocity towards  $m$ . The distance between  $m$  and wall is  $L$ . All collisions are perfectly elastic. find how close can the heavier  $M$  get to the wall.