

# Home work-4 on Logic in AI

naven aaron karasu

Q1 consider the knowledge base KB

$$a \leftarrow b \wedge c$$

$$b \leftarrow d$$

$$b \leftarrow e$$

$$c$$

$$d \leftarrow h$$

$$e$$

$$f \leftarrow g \wedge b$$

$$g \leftarrow c \wedge k$$

$$i \leftarrow a \wedge b$$

a) show how the bottom up proof procedure work for this example  
Give all logical sequences of KB

A:- The bottom up proof procedure works as follows

$$\{b\}$$

$$\{c\}$$

$$\{c, e\}$$

$$\{c, e, b\}$$

$$\{c, e, b, a\}$$

$$\{c, e, b, a, i\}$$

The algorithm terminates with  $c = \{c, e, b, a, i\}$

b)  $P$  is not a logical sequence of KB. Give a model of KB in which  $P$  is false

A:-  $P$  is not a logical consequences of KB because when we try to derive above knowledge base bottom up proof. Then it derives a set  $\{c, e, b, a, i\}$  which is all are true. So, the remaining variables  $\{d, f, g, h, k\}$  is not going to be derived.



so that's why  $P$  is not a logical consequences

c)  $a$  is a logical consequences of  $KB$ . Give a top down derivation for the ask  $a$ ?

A:- consider the starting variable in this top-down model is ' $a$ ' so, the model will derive the following steps

$yes \leftarrow a$

$yes \leftarrow b \wedge c$

$yes \leftarrow e \wedge c$

$yes \leftarrow c$

$yes \leftarrow$

In this way these sequence of choice will lead to proof of solution

Q2:- consider the following clauses

$False \leftarrow a \wedge b$

$a \leftarrow d$

$b \leftarrow d$

$False \leftarrow c$

$a \leftarrow g$

$b \leftarrow e$

$c \leftarrow h$

$a \leftarrow h$

Suppose the assumables are  $\{d, e, f, g, h, i\}$  what are minimal conflicts

A:- from the given clause and integrity constraints these are the minimal conflicts that can be derived

$\{d, g\} \rightarrow$  when (A)  $d = true$  &  $g = true$  (B)  $d \wedge g = true$  conflict

$\{d, h\} \rightarrow$  when (A)  $d = true$  &  $h = true$  (B)  $d \wedge h = true$  conflict

$\{e, d\} \rightarrow$  when (A)  $e = true$  &  $d = true$  (B)  $e \wedge d = true$  conflict

$\{e, h\} \rightarrow$  when (A)  $e = true$  &  $h = true$  (B)  $e \wedge h = true$  conflict

$\{e, g\} \rightarrow$  when (A)  $e = true$  &  $g = true$  (B)  $e \wedge g = true$  conflict

$\{d\} \rightarrow$  when (A)  $d = true$  &  $d = true$  (B)  $d \wedge d = true$  conflict

$\{h\} \rightarrow$  when (C)  $h = true$  &  $h = true$  conflict



These are the minimal conflict  $\{d, g\}$   $\{d, h\}$   $\{e, d\}$   $\{e, g\}$   
 $\{e, h\}$   $\{d\}$   $\{h\}$

Q3) When we want to derive atomic consequences then first we have to write all the ground instances. There are

$\delta(a)$

$\delta(e)$

$P(e)$

$\downarrow(b)$

$S(a, b)$

$S(d, b)$

$S(e, d)$

$P(a) \leftarrow \downarrow(a) \wedge \delta(a)$

$P(b) \leftarrow \downarrow(b) \wedge \delta(b)$

$P(c) \leftarrow \downarrow(c) \wedge \delta(c)$

$P(d) \leftarrow \downarrow(d) \wedge \delta(d)$

$P(e) \leftarrow \downarrow(e) \wedge \delta(e)$

$\downarrow(b) \leftarrow S(b, a) \wedge \downarrow(a)$

$\downarrow(b) \leftarrow S(b, h) \wedge \downarrow(h)$

$\downarrow(b) \leftarrow S(b, c) \wedge \downarrow(c)$

$\downarrow(b) \leftarrow S(b, d) \wedge \downarrow(d)$

$\downarrow(b) \leftarrow S(b, e) \wedge \downarrow(e)$

$\downarrow(a) \leftarrow S(a, a) \wedge \downarrow(a)$

$\downarrow(a) \leftarrow S(a, b) \wedge \downarrow(b)$

$\downarrow(a) \leftarrow S(a, c) \wedge \downarrow(c)$

$\downarrow(a) \leftarrow S(a, d) \wedge \downarrow(d)$

$\downarrow(a) \leftarrow S(a, e) \wedge \downarrow(e)$

$\downarrow(c) \leftarrow S(c, a) \wedge \downarrow(a)$



$$Q(e) \leftarrow S(c,b) \wedge Q(b)$$

$$Q(c) \leftarrow S(c,c) \wedge Q(c)$$

$$Q(c) \leftarrow S(c,d) \wedge Q(d)$$

$$Q(c) \leftarrow S(c,e) \wedge Q(e)$$

$$Q(e) \leftarrow S(e,a) \wedge Q(a)$$

$$Q(e) \leftarrow S(e,b) \wedge Q(b)$$

$$Q(e) \leftarrow S(e,c) \wedge Q(c)$$

$$Q(e) \leftarrow S(e,d) \wedge Q(d)$$

$$Q(e) \leftarrow S(e,e) \wedge Q(e)$$

These are above all the ground instances from all these ~~different~~ ground instances by using the bottom up procedure. We will find the ground atomic consequences. So by using bottom up procedure these below are the ground atomic consequences

$$\rightarrow \{ \}$$

$$\rightarrow \{ \delta(a) \}$$

$$\rightarrow \{ \delta(a), \delta(e) \}$$

$$\rightarrow \{ \delta(a), \delta(e), \delta(c) \}$$

$$\rightarrow \{ \delta(a), \delta(e), P(c), Q(b) \}$$

$$\rightarrow \{ \delta(a), \delta(e), P(c), Q(b) \}$$

$$\rightarrow \{ \delta(a), \delta(e), P(c), Q(b), S(a,b) \}$$

$$\rightarrow \{ \delta(a), \delta(e), P(c), Q(b), S(a,b), S(d,b) \}$$

$$\rightarrow \{ \delta(a), \delta(e), P(c), Q(b), S(a,b), S(d,b), S(e,d) \}$$

$$\rightarrow \{ \delta(a), \delta(e), P(c), Q(b), S(a,b), S(d,b), S(e,d), Q(a) \}$$

$$\rightarrow \{ \delta(a), \delta(e), P(c), Q(b), S(a,b), S(d,b), S(e,d), Q(a), Q(d) \}$$

$$\rightarrow \{ \delta(a), \delta(e), P(c), Q(b), S(a,b), S(d,b), S(e,d), Q(a), Q(d), Q(e) \}$$



So the final of ground atomic consequences that derived from the bottom up procedure is  $\{x(a), x(e), P(c), \neg(b), S(a,b), S(d,b), S(e,d), \neg(a), \neg(d), \neg(c)\}$

Q4:- provide an SLD derivation of the Query has

a)  $\text{access}[\text{todd}, \text{library}]$

$\leftarrow \text{has\_access}[\text{todd}, \text{library}]$

$\swarrow \text{has\_access}(x, \text{library}) \leftarrow \text{has\_access}(y, \text{library}) \wedge \text{parent}(y, x)$

$\leftarrow \text{has\_access}(y, \text{library}) \wedge \text{parent}(y, \text{todd})$

$\swarrow \text{parent}(\text{karen}, \text{todd})$

$\leftarrow \text{has\_access}(\text{karen}, \text{library}) \wedge \text{parent}(\text{karen}, \text{todd})$

Here we done the two substitutions one is  $x$  with  $\text{todd}$  & second is  $y$  with  $\text{karen}$

So final unified set is  $\{\text{todd}/x, \text{karen}/y\}$



Q4

b) The query has-access(mary, library) has two SLD Deviations

Give both of them

First deviation:-

$\leftarrow \text{has\_access}(\text{mary}, \text{library})$

$\left| \text{has\_access}(x, \text{library}) \leftarrow \text{student}(x) \right|$

$\text{student}(\text{mary})$

Here we have done only one substitution that is  $x$  with  $\text{mary}$   
So final subset is  $\{\text{mary}/x\}$

Second Deviation:-

$\leftarrow \text{has\_access}(\text{mary}, \text{library})$

$\left| \text{has\_access}(x, \text{library}) \leftarrow \text{has\_access}(y, \text{library}) \wedge \right|$

$\text{parent}(y, x)$

$\leftarrow \text{has\_access}(y, \text{library}) \wedge \text{parent}(y, \text{mary})$

$\left| \text{parent}(\text{karen}, \text{mary}) \right|$

$\leftarrow \text{has\_access}(\text{karen}, \text{library}) \wedge \text{parent}(\text{karen}, \text{mary})$

Here we done two substitutions one is  $x$  with  $\text{mary}$  & The other is  $y$  with  $\text{karen}$

So final set is  $\{\text{mary}/x, \text{karen}/y\}$



Q4c) There is deviation for  $\text{has\_access}(\text{ariel}, \text{library})$  because there is a supporting constraint that helps is  $\text{parent}(\text{sarah}, \text{ariel})$   
 so the deviation looks like this

$\leftarrow \text{has\_access}(\text{ariel}, \text{library})$

$\left| \text{has\_access}(x, \text{library}) \leftarrow \text{has\_access}(y, \text{library}) \right.$   
 $\quad \wedge \text{parent}(y, x)$

$\leftarrow \text{has\_access}(y, \text{library}) \wedge \text{parent}(y, \text{ariel})$

$\left| \text{parent}(\text{sarah}, \text{ariel}) \right.$

$\leftarrow \text{has\_access}(\text{sarah}, \text{library}) \wedge \text{parent}(\text{sarah}, \text{ariel})$

so here we have two substitution one is  $x$  with  $\text{ariel}$  & other is  $y$  with  $\text{sarah}$

so, final subset is  $\{\text{ariel} / x, \text{sarah} / y\}$

Q4d) set of answers for the query  $\text{has\_access}(x, \text{office})$  is because of its clause

$\text{has\_access}(x, \text{office}) \leftarrow \text{has\_keys}(x)$

but for  $\text{has\_keys}(x)$  there is no derivation that's why the answer for query is empty



(Q41) e) if we add the given clauses to knowledge <sup>base</sup> after then the SLD derivation for this query  $\text{has\_access}(x, \text{office})$  That is

$\leftarrow \text{has\_access}(x, \text{office})$

$\downarrow \text{has\_access}(x, \text{office}) \leftarrow \text{has\_keys}(x)$

$\leftarrow \text{has\_keys}(x)$

$\downarrow \text{has\_keys}(x) \rightarrow \text{faculty}(x)$

$\leftarrow \text{faculty}(x)$

The answer set for  $x$  is  $\{\text{diane}, \text{ming}\}$

Answer to the given query is  $\{\text{diane}, \text{ming}\}$