



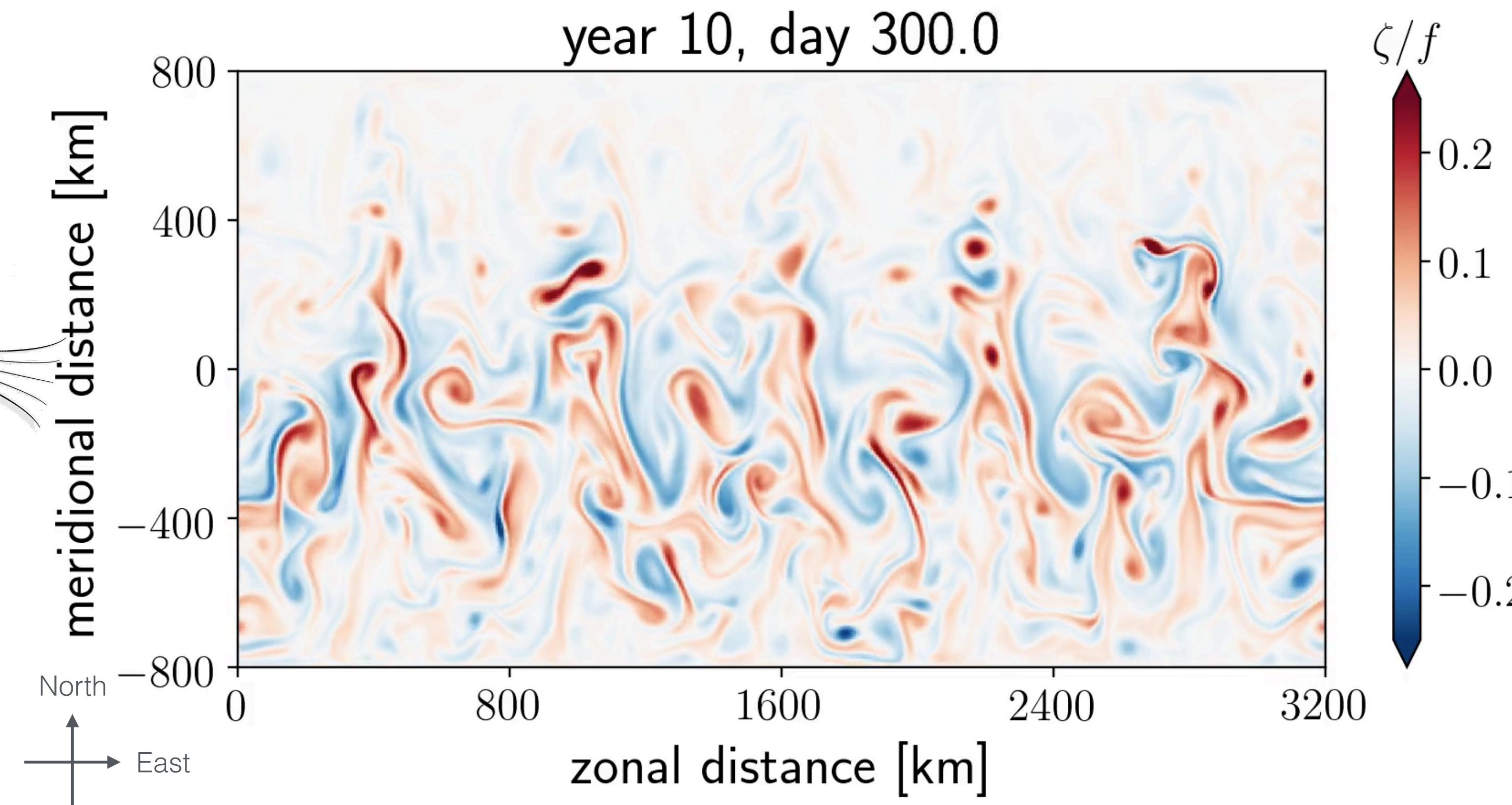
Australian National  
University

# Barotropic versus Baroclinic eddy saturation: implications to Southern Ocean dynamics

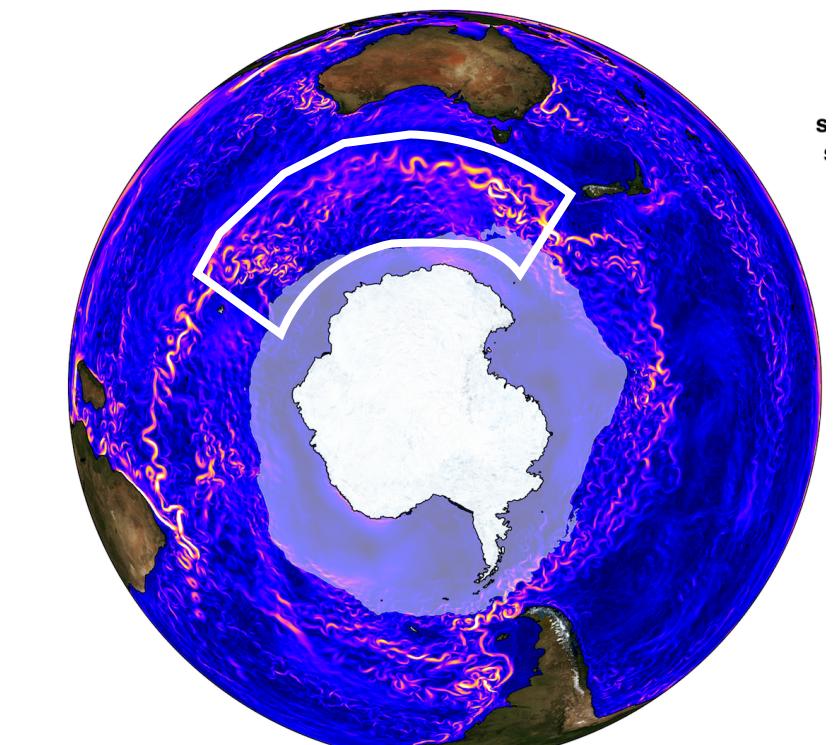


ARC Centre of Excellence  
for Climate Extremes

Navid Constantinou & Andy Hogg

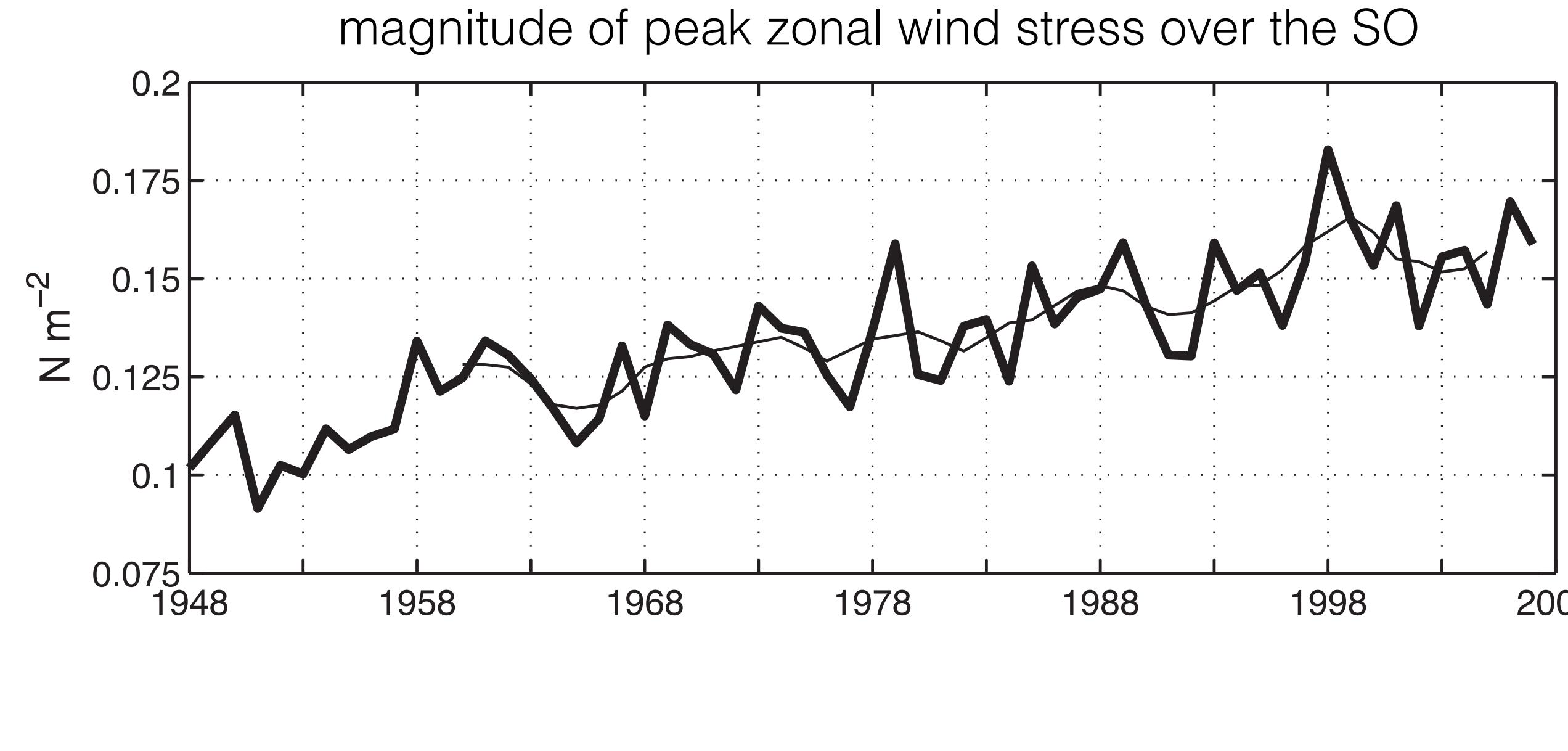


top-layer  
relative vorticity  
 $\zeta = \partial_x v - \partial_y u$



22<sup>nd</sup> AOFD Conference  
Portland ME, June 25th, 2019

# winds over Southern Ocean are getting stronger

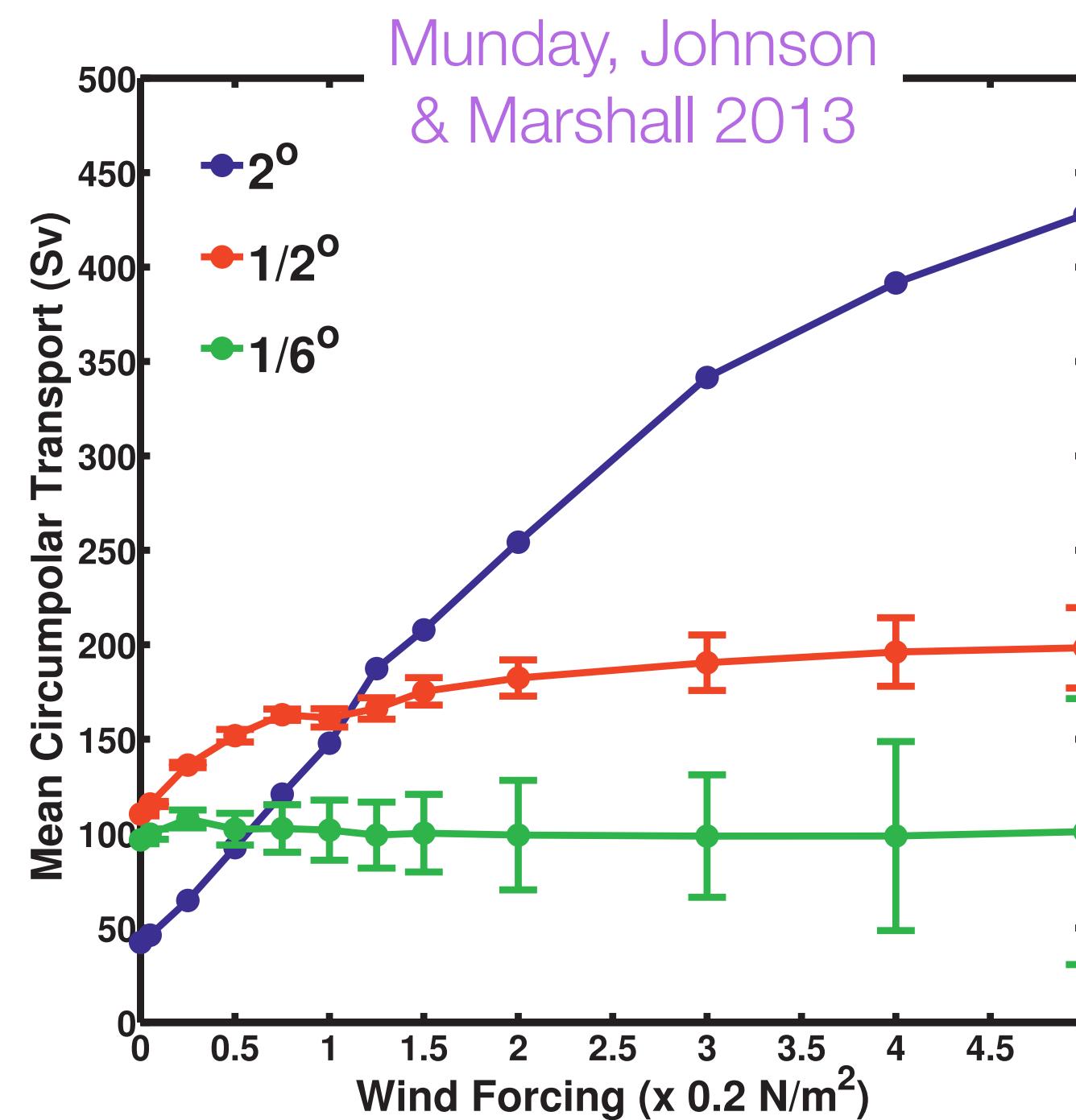


how will the Antarctic Circumpolar Current (ACC) respond?

does doubling the winds imply double ACC the transport?  
not always — “eddy saturation”

# what's eddy saturation?

The *insensitivity* of the time-mean ACC volume transport to wind stress increase.



higher resolution → eddy saturation “occurs”

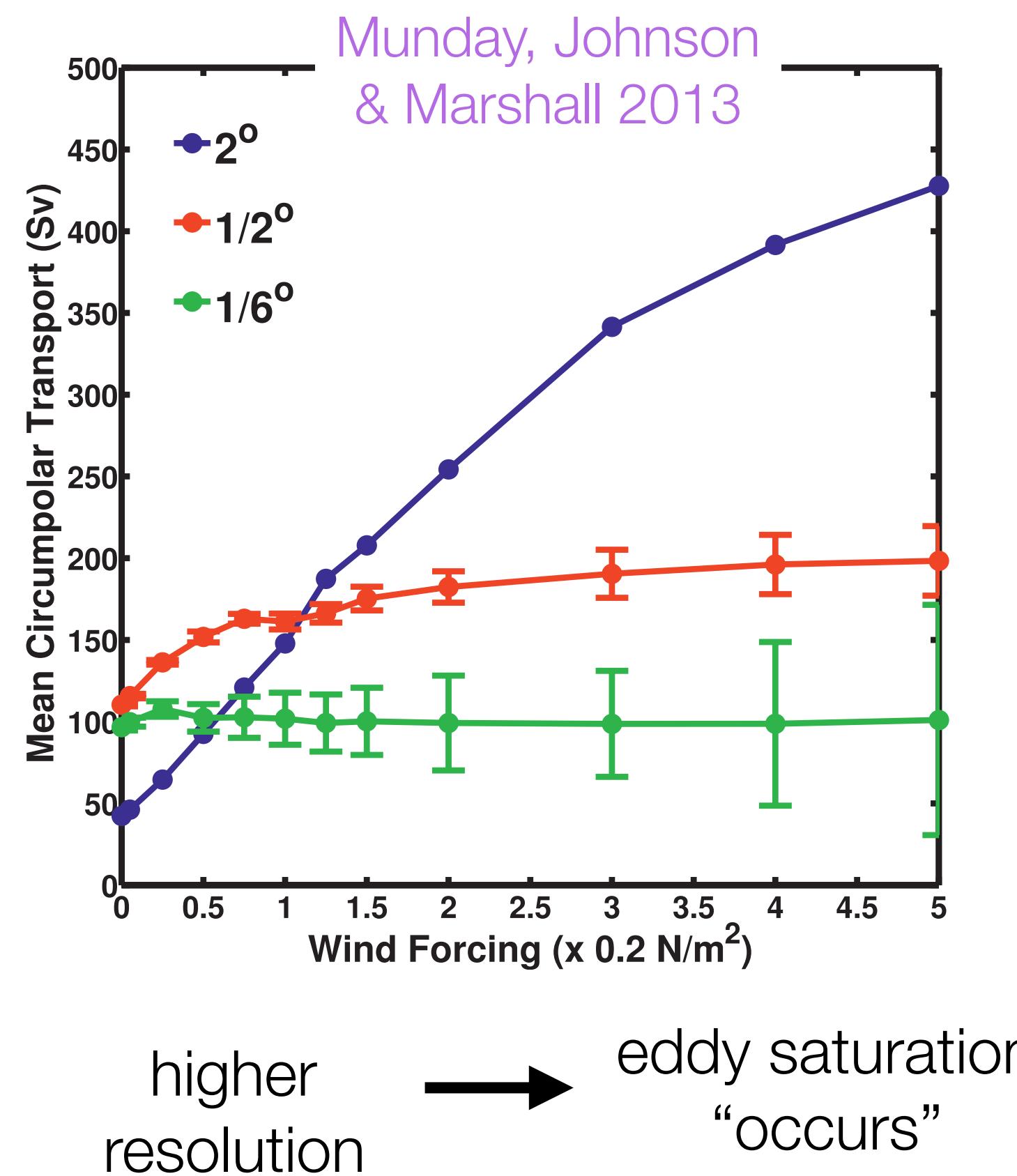
Eddy saturation is seen in eddy-resolving ocean models.  
(some hints also in obs.)

Eddy saturation was theoretically predicted by Straub (1993)  
but with an *entirely baroclinic* argument.

[Other examples: Hallberg & Gnanadesikan 2001, Tansley & Marshall 2001, Hallberg & Gnanadesikan 2006, Hogg et al. 2008, Nadeau & Straub 2009, 2012, Farneti et al. 2010, Meredith et al. 2012, Morisson & Hogg 2013, Abernathey & Cessi 2014, Farneti et al. 2015, Nadeau & Ferrari 2015, Marshall et al. 2017.]

# what's eddy saturation?

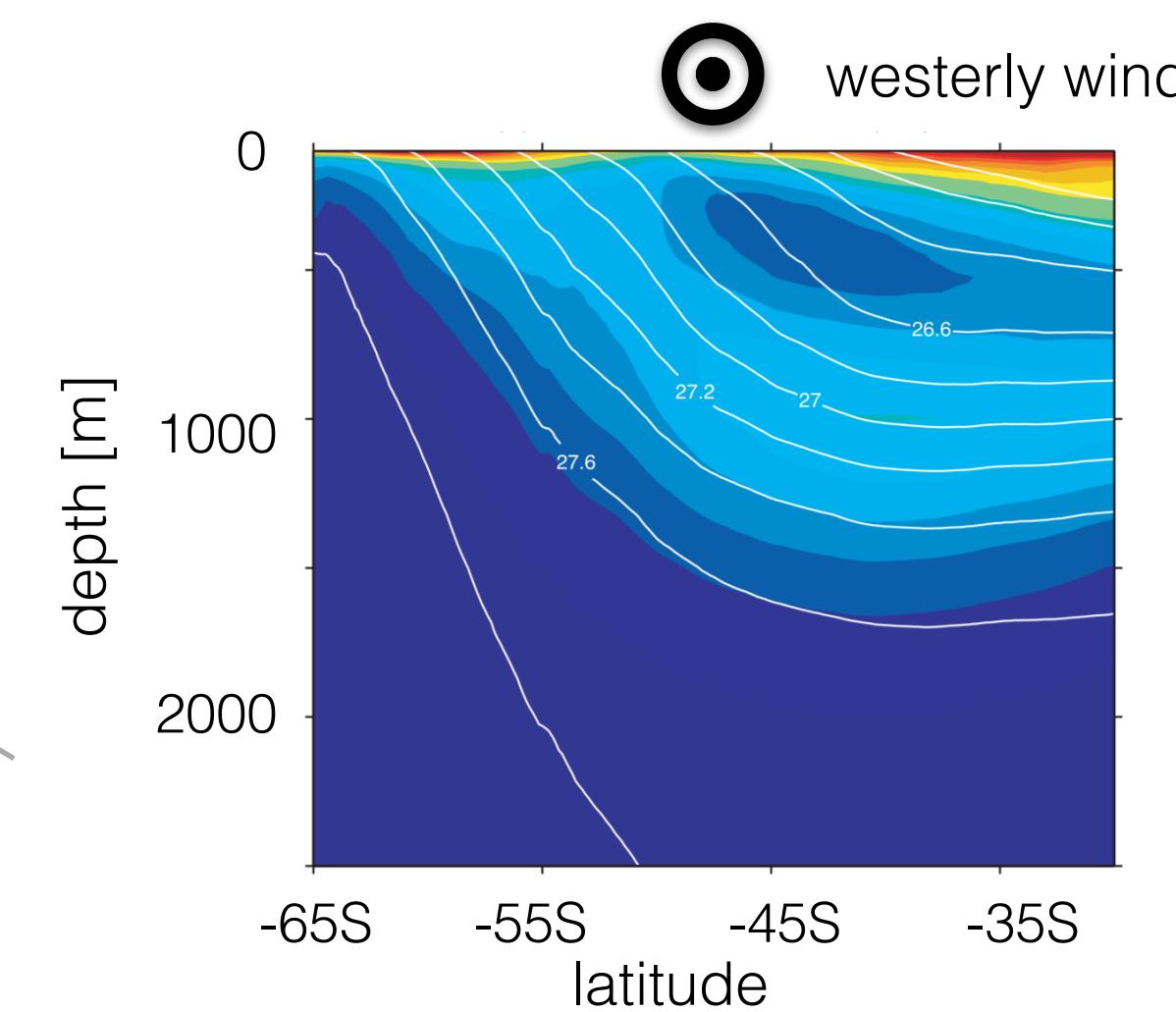
# The *insensitivity* of the time-mean ACC volume transport to wind stress increase.



Eddy saturation is seen in eddy-resolving ocean models.  
(some hints also in obs.)

Eddy saturation was theoretically predicted by Straub (1993) but with an *entirely baroclinic* argument.

wind increase  
slopes the isopycnals



baroclinic eddies  
restratify isopycnals

The diagram illustrates the effect of baroclinic eddies on isopycnal lines. It features several parallel, slightly curved grey lines representing isopycnals. A single black line, labeled "before" at its bottom end, slopes downwards from left to right. Another black line, labeled "after" at its top end, follows a similar path but is shifted to the right, indicating that the isopycnals have been displaced by the eddy's influence.

[Other examples: Hallberg & Gnanadesikan 2001, Tansley & Marshall 2001, Hallberg & Gnanadesikan 2006, Hogg et al. 2008, Nadeau & Straub 2009, 2012, Farneti et al. 2010, Meredith et al. 2012, Morisson & Hogg 2013, Abernathey & Cessi 2014, Farneti et al. 2015, Nadeau & Ferrari 2015, Marshall et al. 2017.]

# in the previous episode

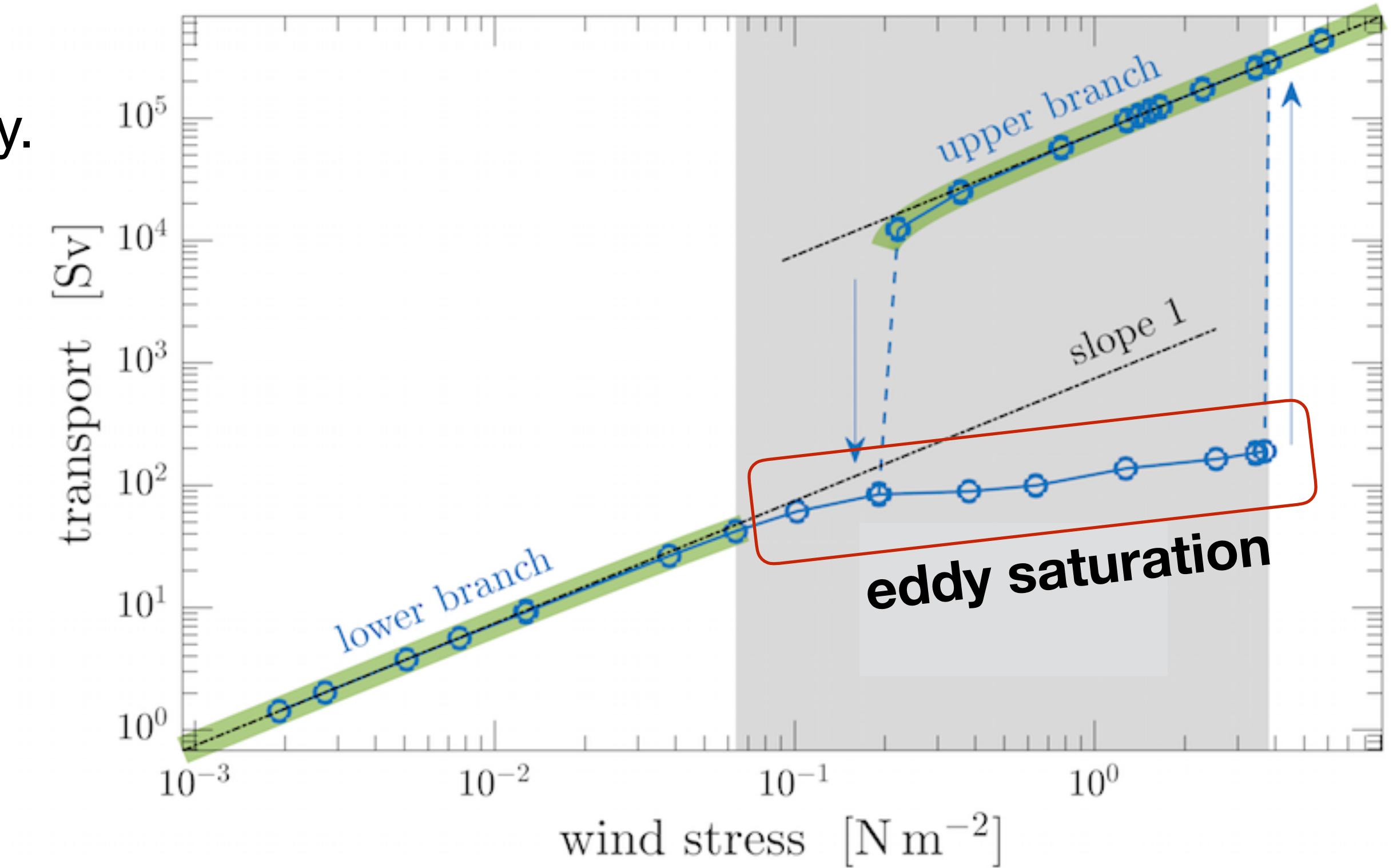
[back in 2017, in a Portland far far away]

Eddy saturation can occur *without* baroclinicity

in a homogeneous QG barotropic model with bathymetry.

Surprising!

All previous arguments *relied* on baroclinic instability  
for producing transient eddies.



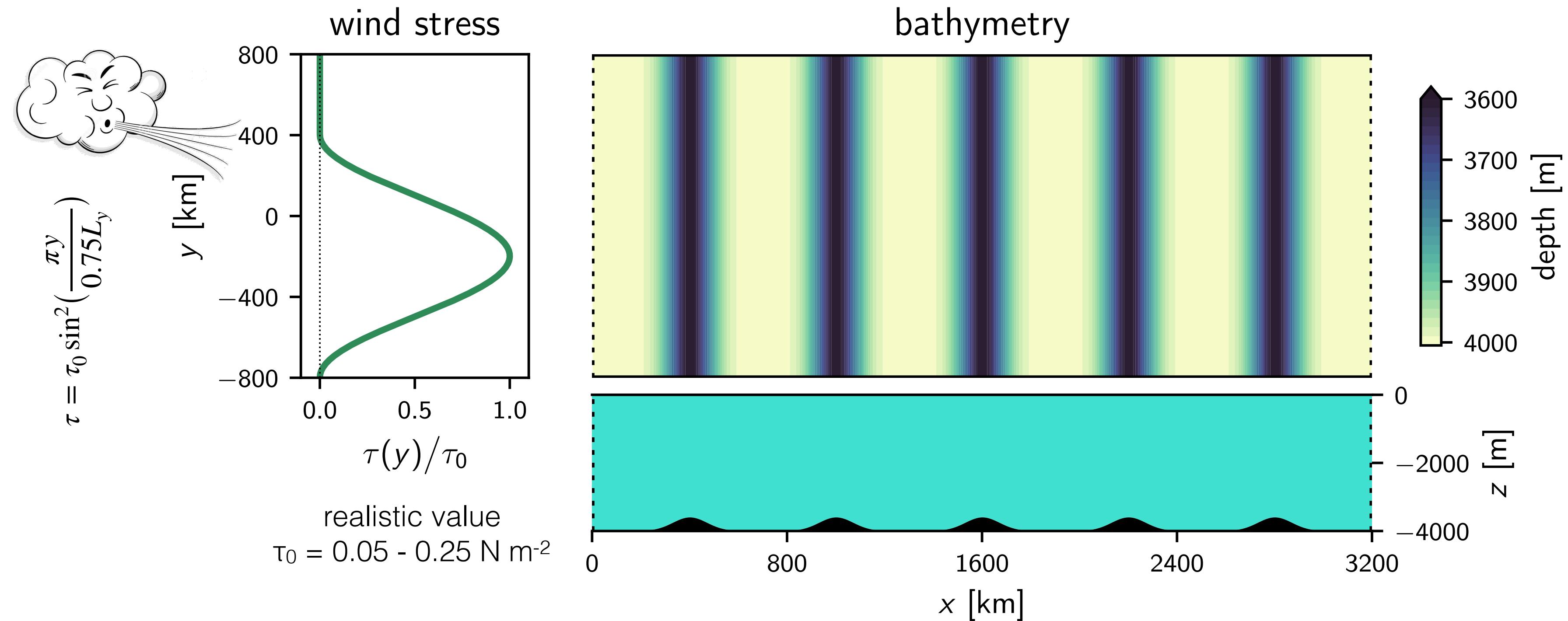
# what's the plan

Assess the relative role of  
**barotropic** versus **baroclinic** dynamics  
in establishing "eddy saturated" ocean states.

Use an isopycnal layered model  
with varying number of fluid layers.

# model setup

GFDL's MOM6  
primitive equations  
in isopycnal coordinates  
Boussinesq approximation

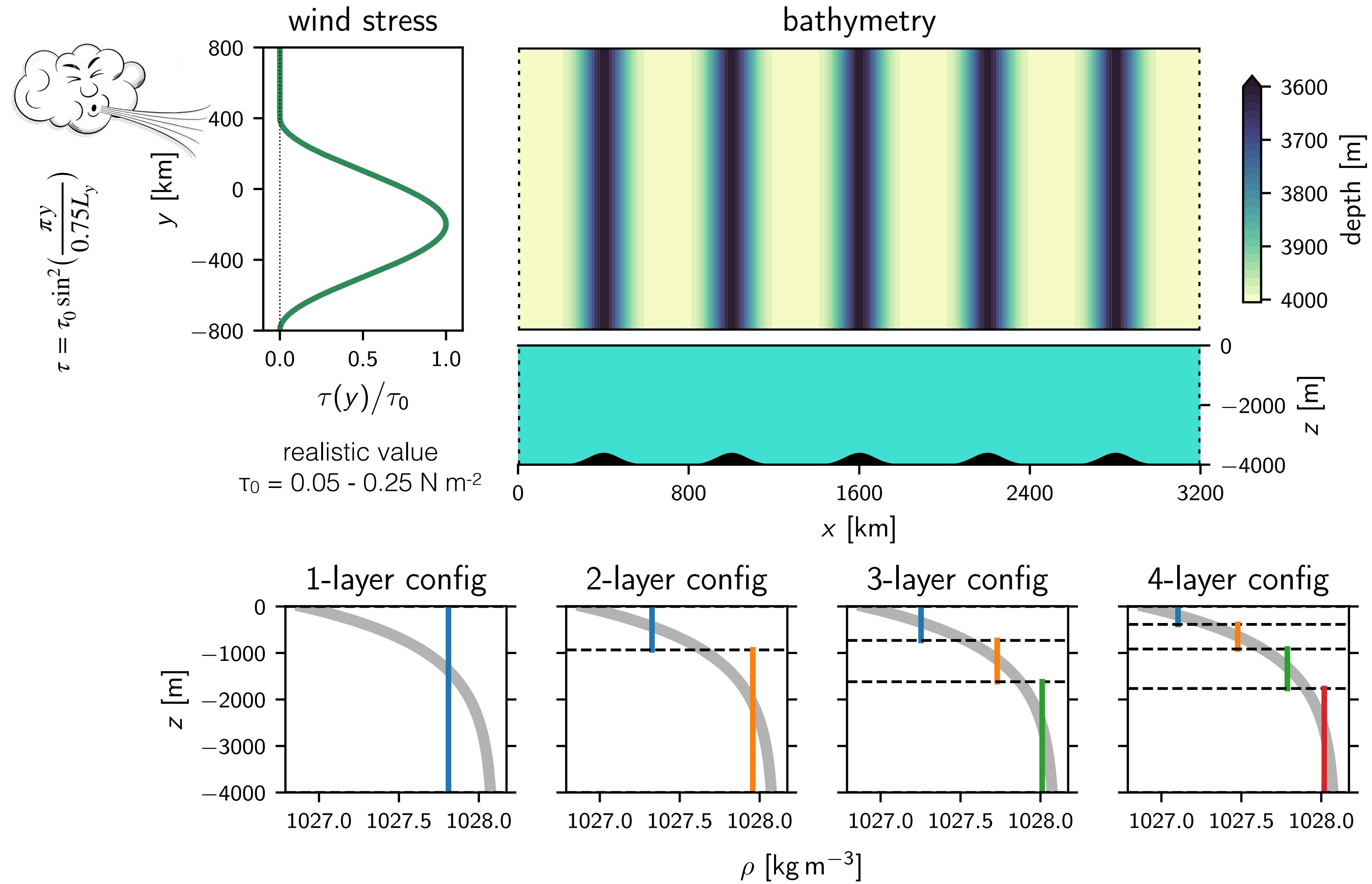


$\beta$ -plane  $f = f_0 + \beta y$   
1st deformation radius  $\approx 19 \text{ km}$   
zonally re-entrant  
free surface  
free-slip walls  
quadratic bottom drag  
grid spacing 4 km

bathymetry:  
Gaussian ridges  
400 m tall, half-width 165 km

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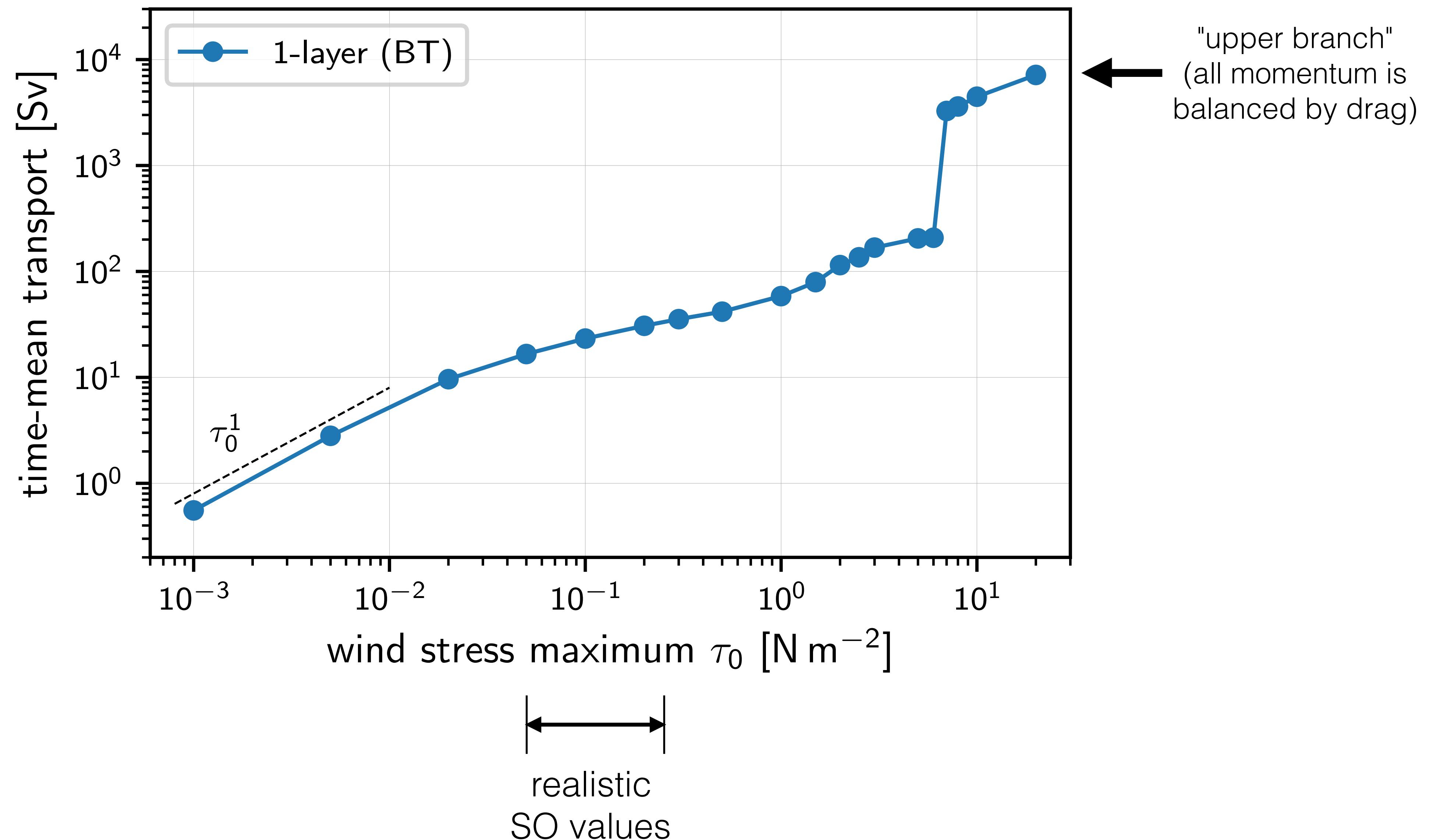
exponential density profile  

$$\rho = \rho_0 + \Delta\rho (1 - e^{z/d})$$
  
 $\Delta\rho = 1.2 \text{ kg m}^{-3}, d = 1 \text{ km}$

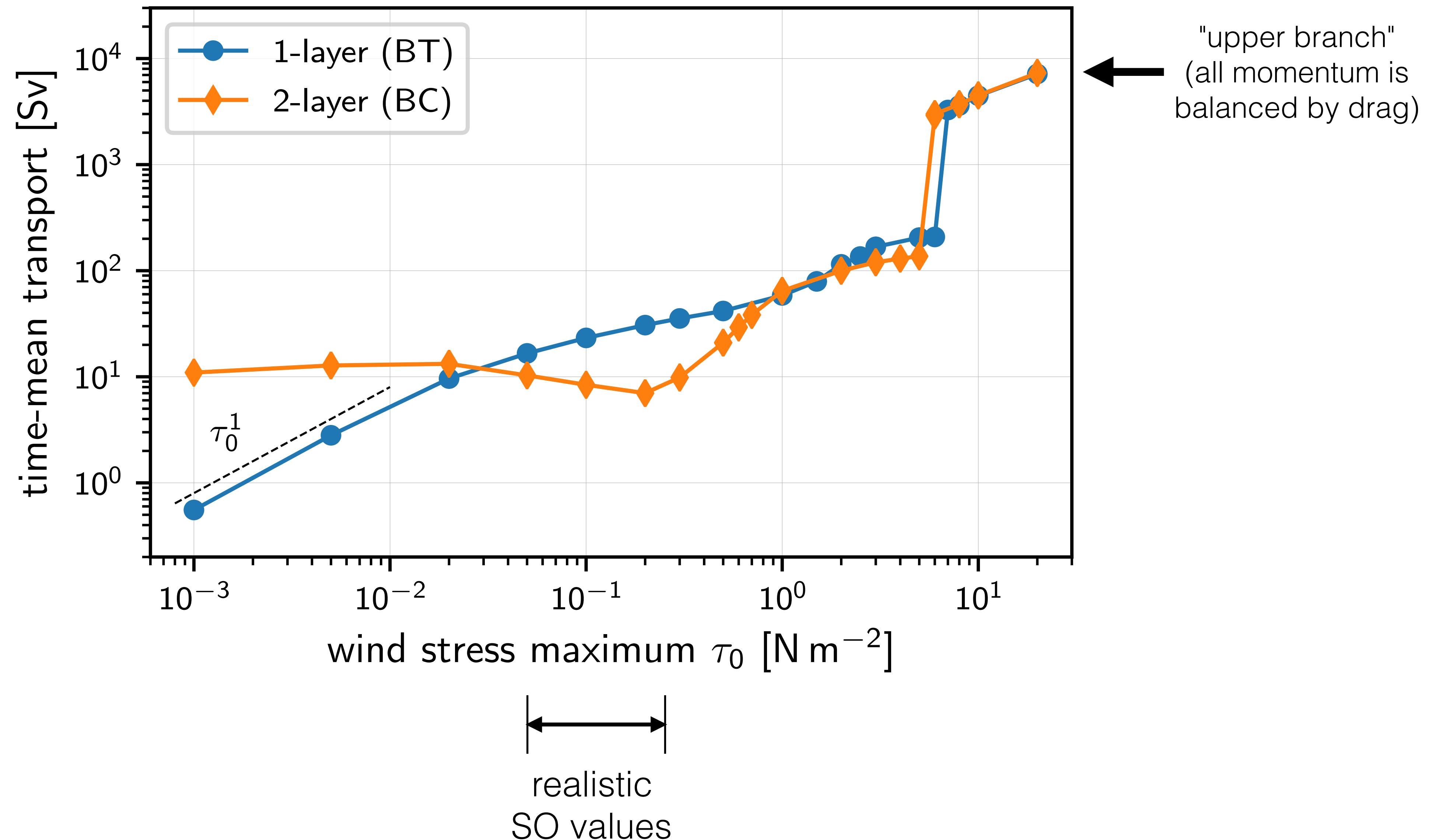
layered approximations

vary the wind stress amplitude  $\tau_0$   
and see how the time-mean zonal transport changes

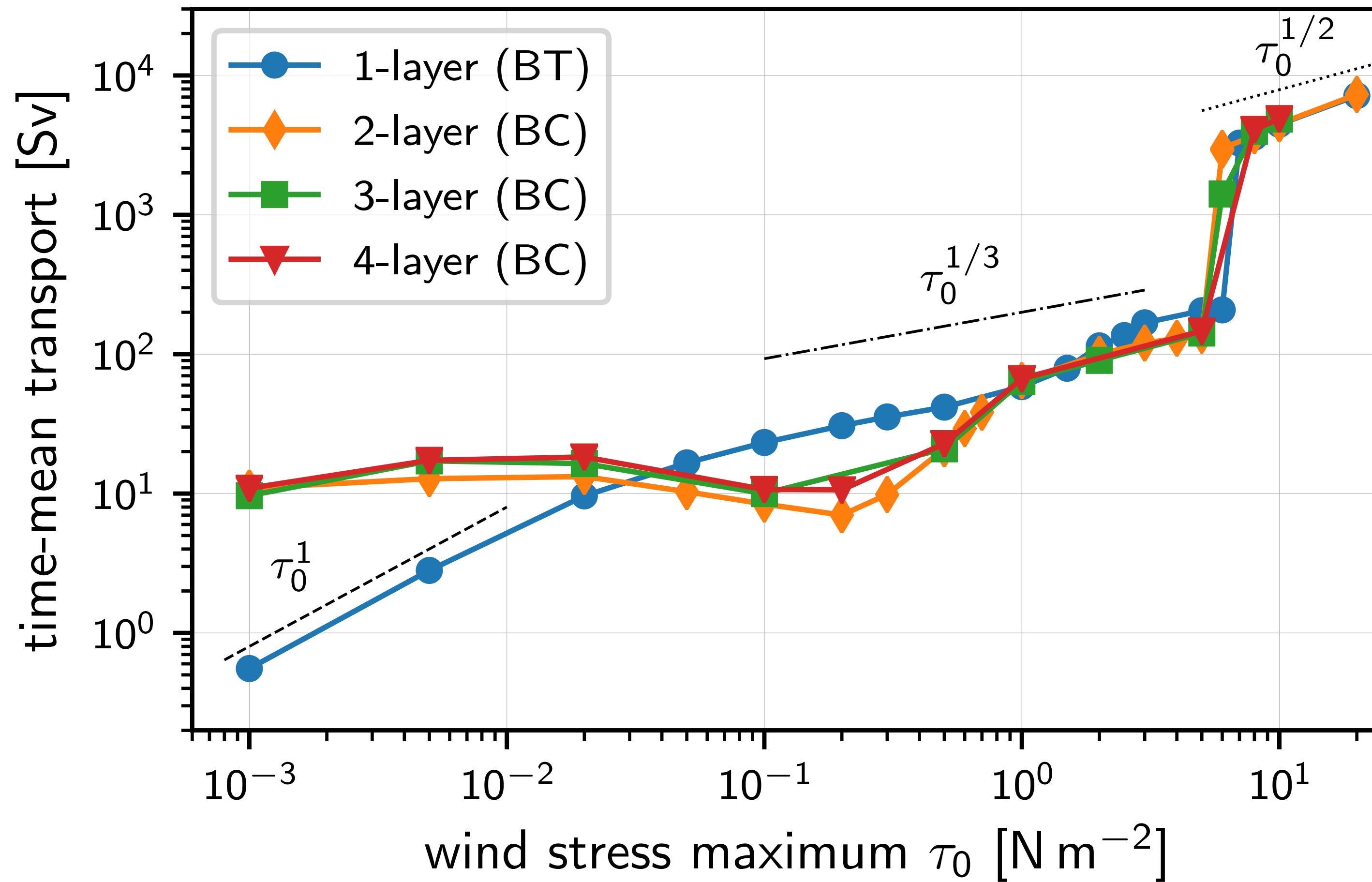
# mean zonal transport Vs wind stress



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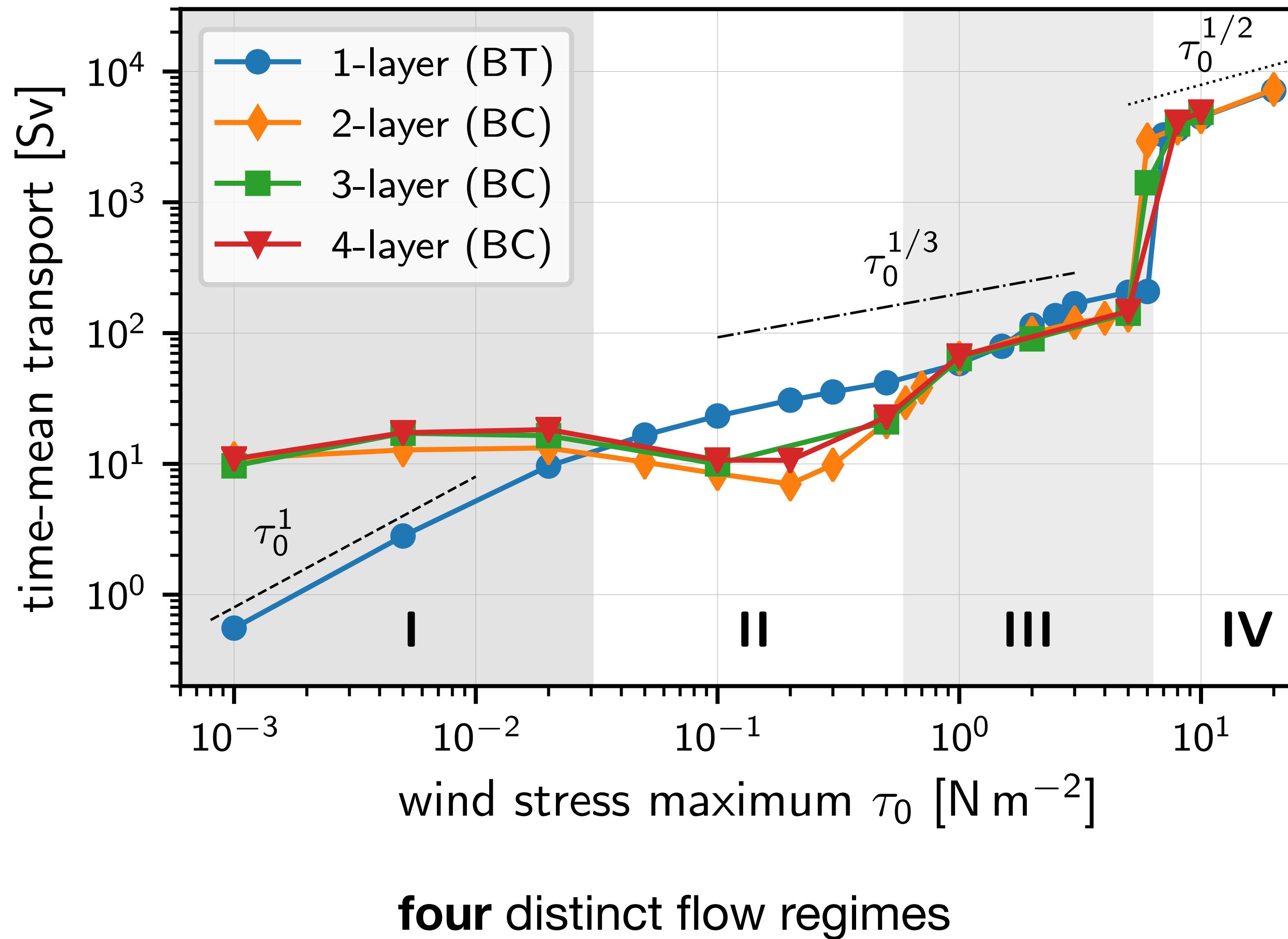


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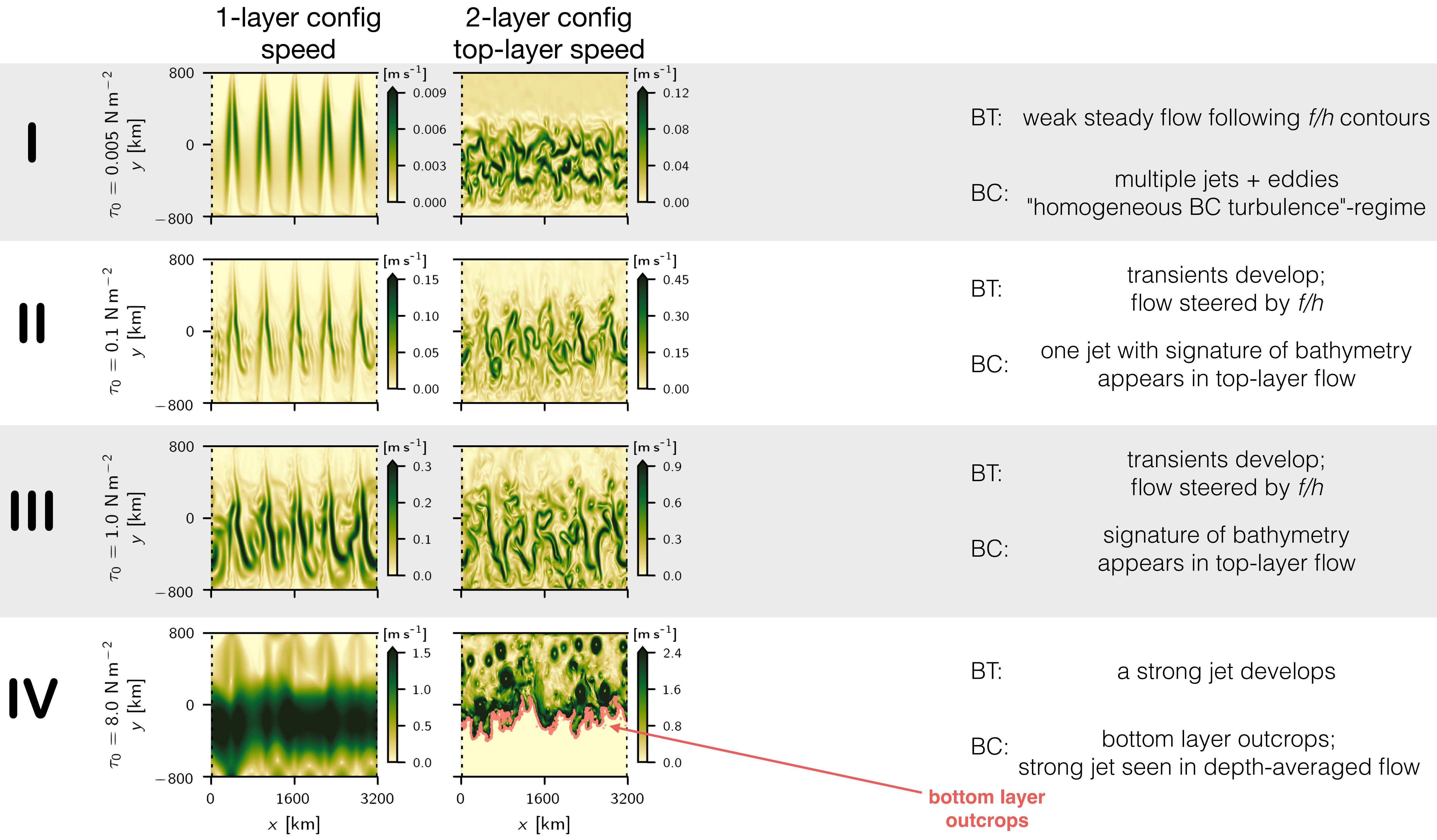


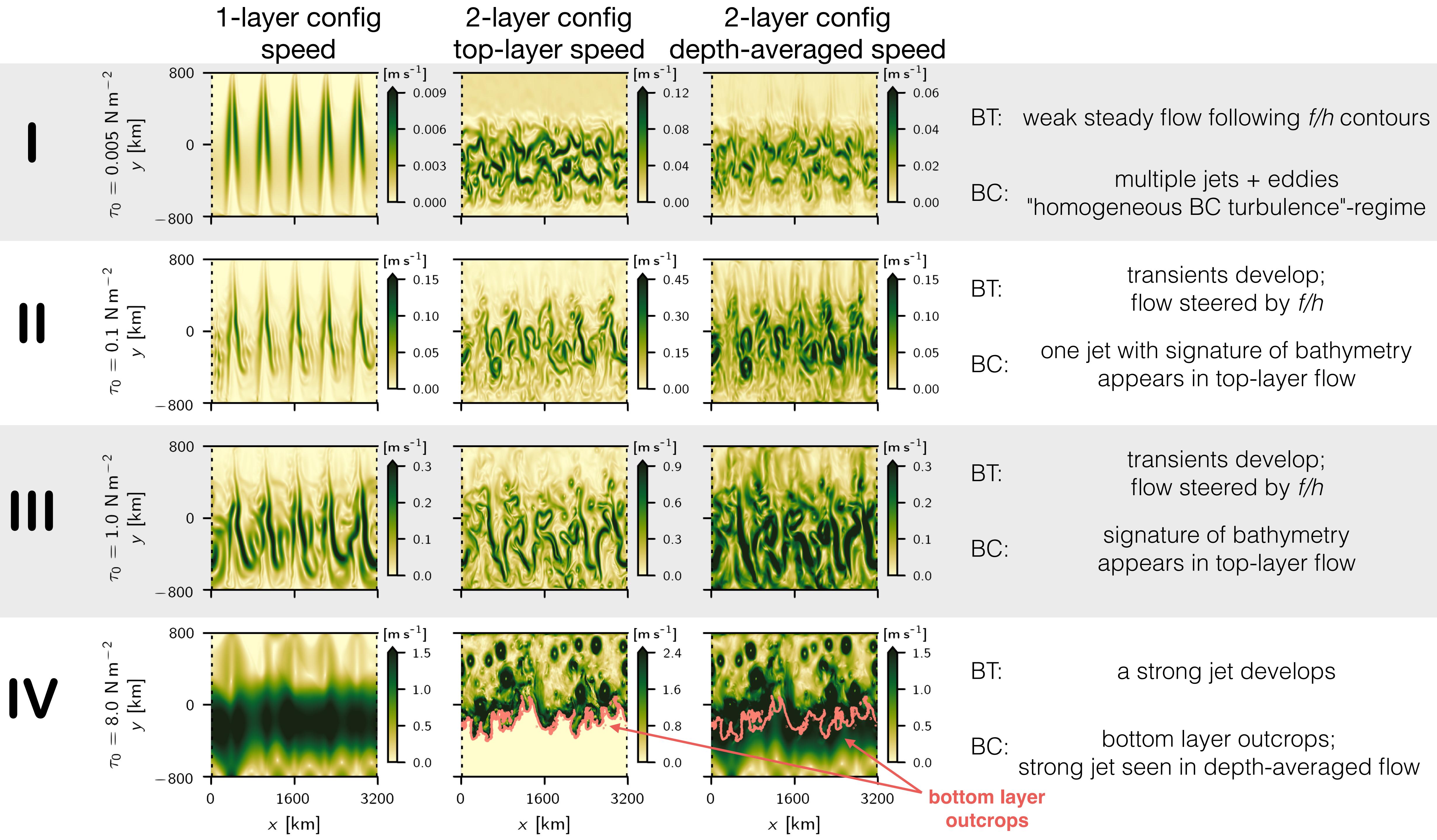
>3-layer configurations are the same as 2-layers  
(as far as the mean zonal transport is concerned)

# mean zonal transport Vs wind stress



how does the flow look like in the four flow regimes?





# depth-integrated zonal momentum balance

$\langle \rangle$  : layer average  
 $\overline{\langle \rangle}$  : time average

$$\langle \tau \rangle = \langle \overline{p_{\text{bot}} \partial_x h_{\text{bot}}} \rangle + \langle \rho_m c_D \overline{u_{\text{bot}} | \mathbf{u}_{\text{bot}} |} \rangle$$

$$\langle \overline{p_{\text{bot}} \partial_x h_{\text{bot}}} \rangle = \langle \overline{p_{\text{bot}}} \partial_x h_{\text{bot}} \rangle$$

only standing flow  
contributes to TFS

wind  
stress  
(WS)

topographic  
form stress  
(TFS)

bottom drag  
(BD)

# depth-integrated zonal momentum balance

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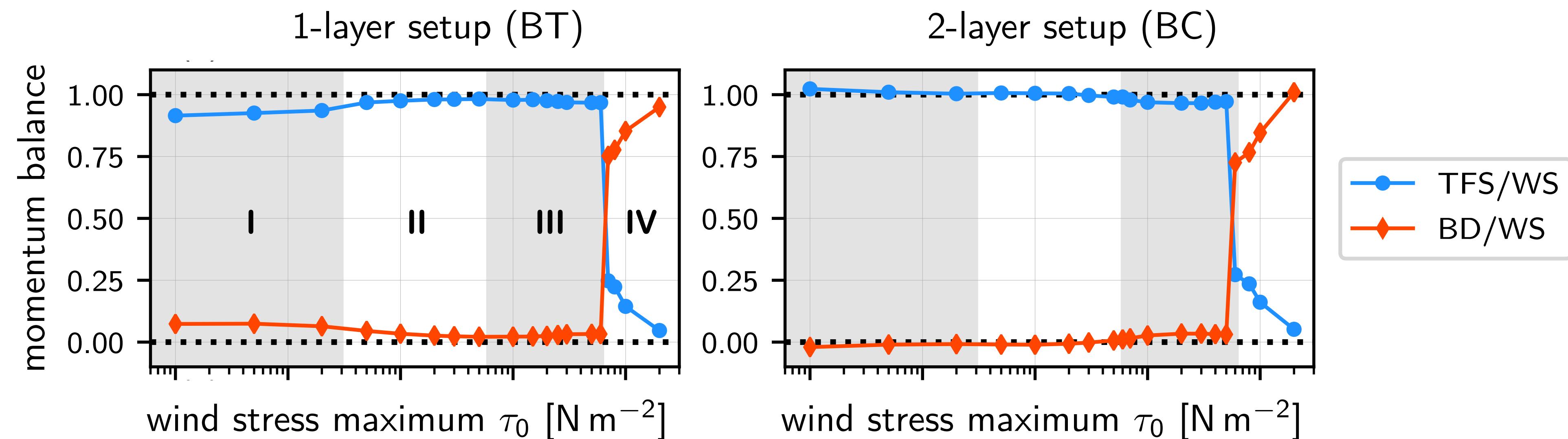
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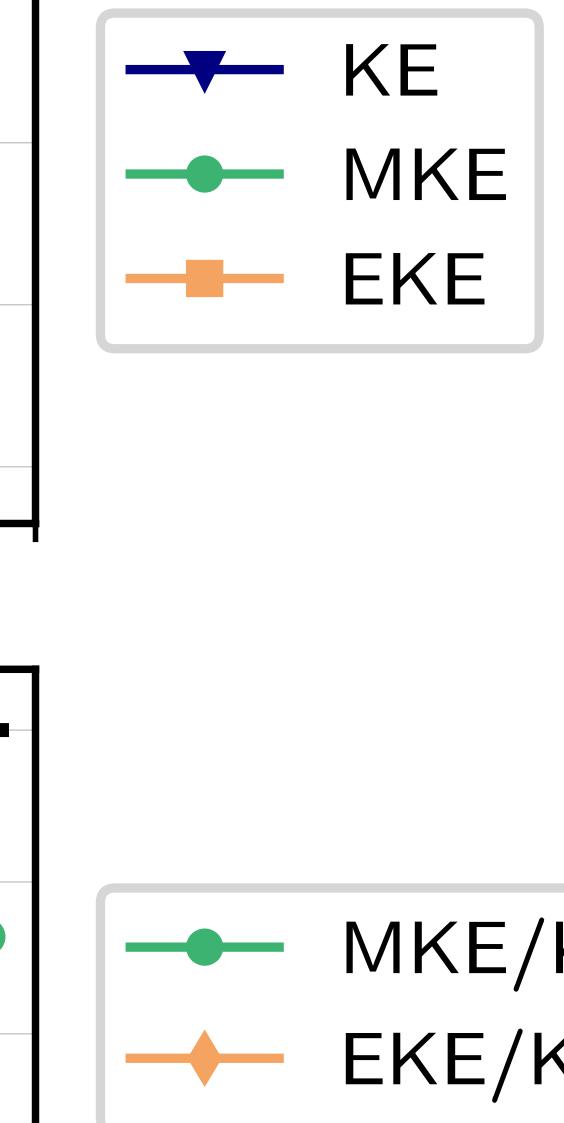
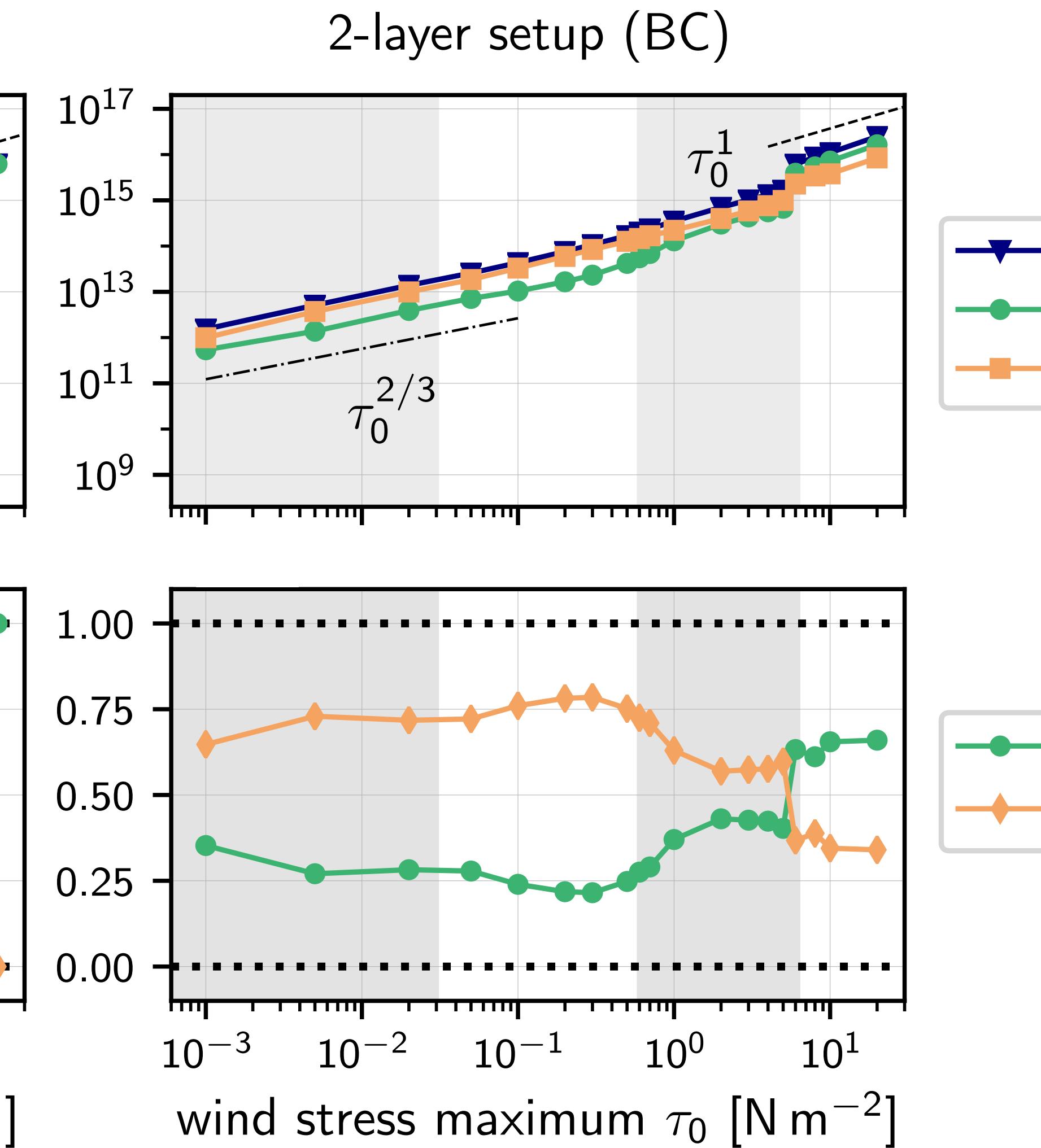
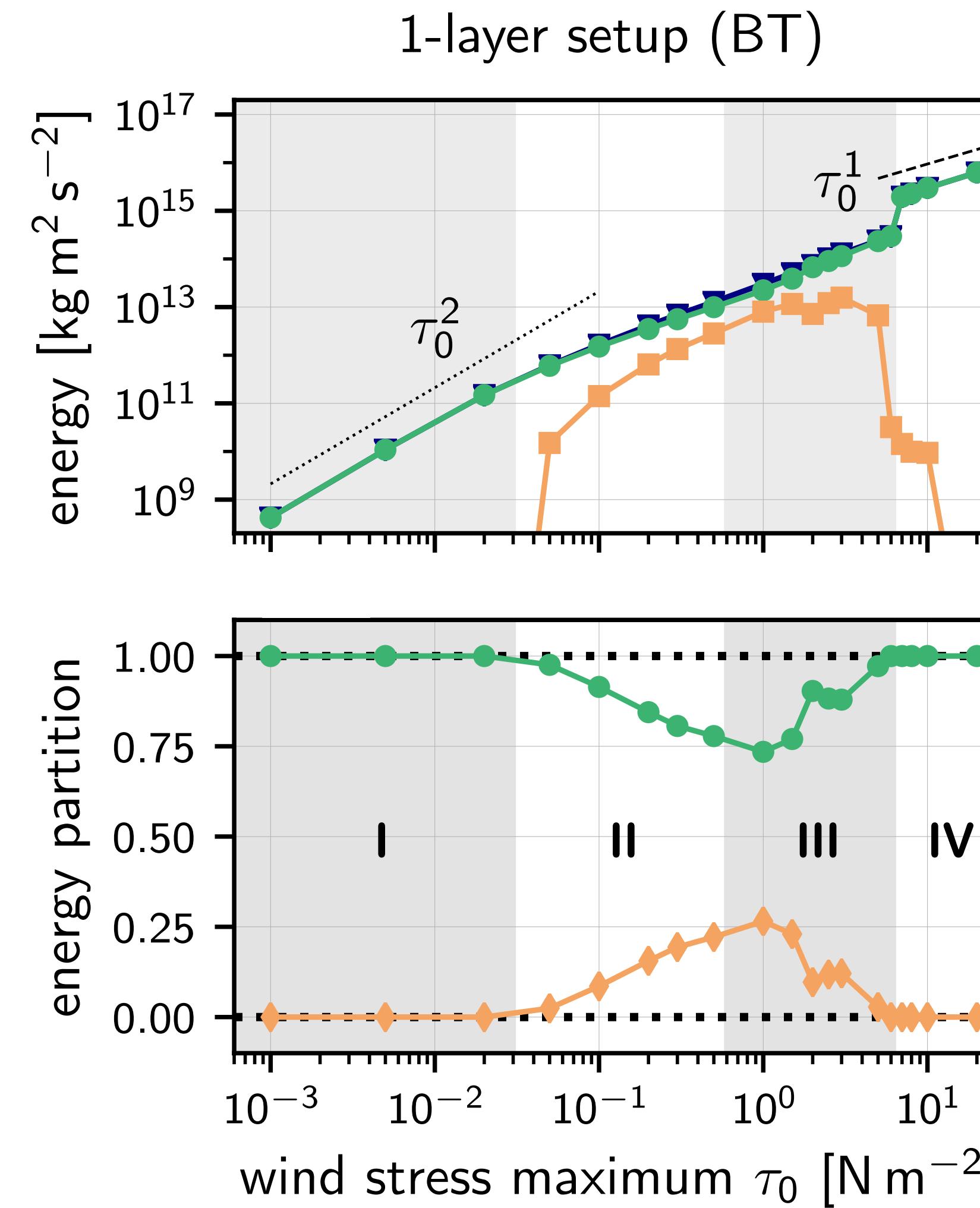
bottom drag  
(BD)



Almost all momentum is balanced by topographic form stress  
(except when flow transitions to "upper branch").

# standing–transient kinetic energy decomposition

BT config  
has transients  
only in **II & III**



standing flow  
dominates  
in BT config;  
transient flow  
dominates in BC

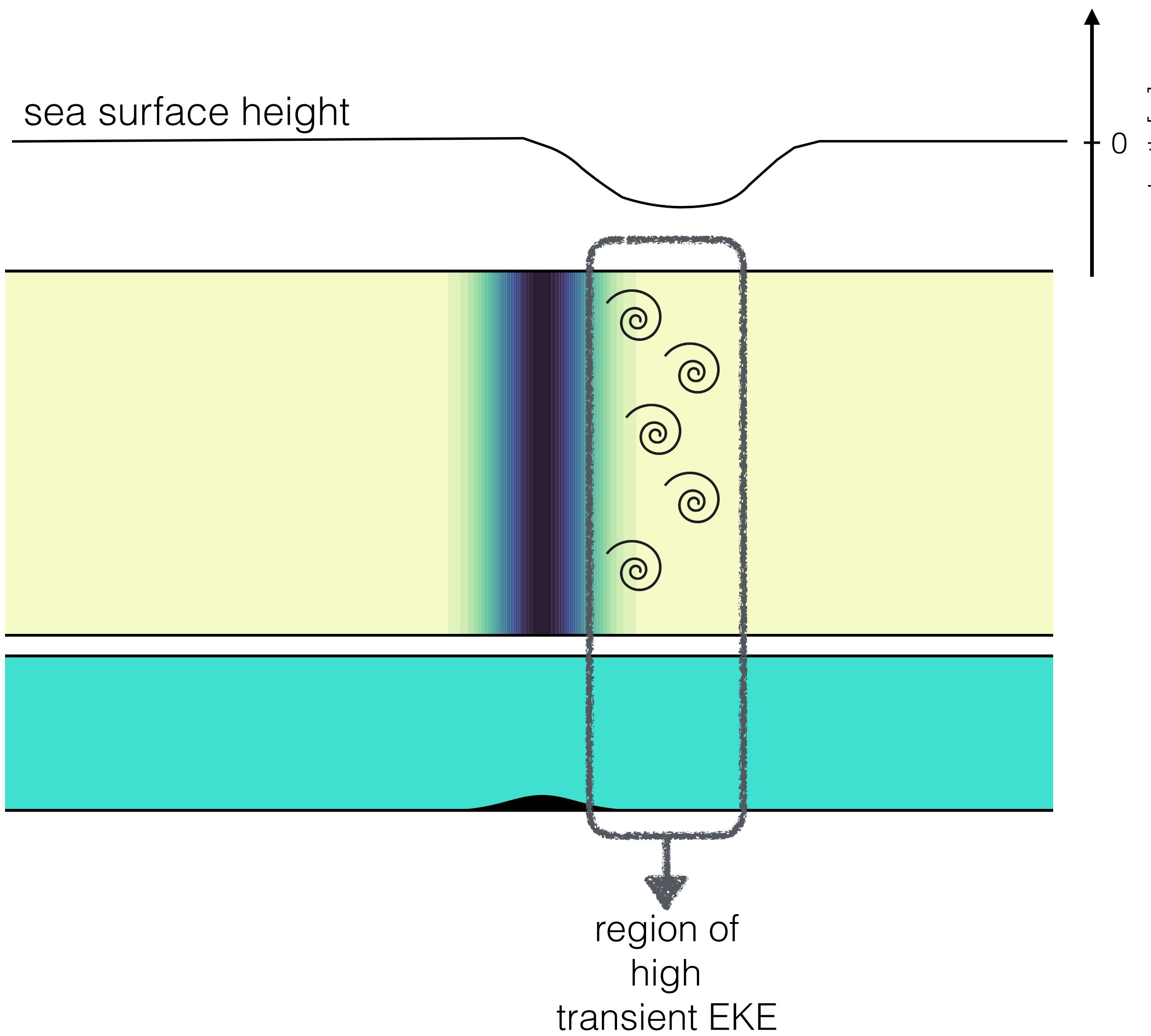
Despite the great differences in flow fields,  
both **BT** and **BC** configs show same mean zonal transport for regimes **III & IV**.

$$\langle \overline{p_{\text{bot}} \partial_x h_{\text{bot}}} \rangle = \langle \overline{p_{\text{bot}}} \partial_x h_{\text{bot}} \rangle$$

only standing flow contributes to  
topographic form stress

how transients affect  
topographic form stress?

# how transients lead to time-mean topographic form stress?



[Same process as described by Youngs et al. 2017]

# take home messages

when transient eddies exist (both in **barotropic** or **baroclinic** configs)  
the mean zonal transport becomes eddy saturated  
[transport is much less sensitive to wind stress increase]

**proposal:**

eddy saturation occurs due to  
transient eddies shaping the standing flow  
to produce topographic form stress that balances the wind stress  
(*regardless* of the process from which transient eddies originate)

our results show that the (oftentimes ignored) barotropic flow-component  
plays an important role in setting up the ACC transport

[in agreement with recent obs. evidence, e.g., Thompson & Naveira Garabato 2014,  
Peña-Molino et al. 2014, Donohue et al. 2016 (cDrake exp)]

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*thank you*

extra slides

# mean zonal transport Vs wind stress

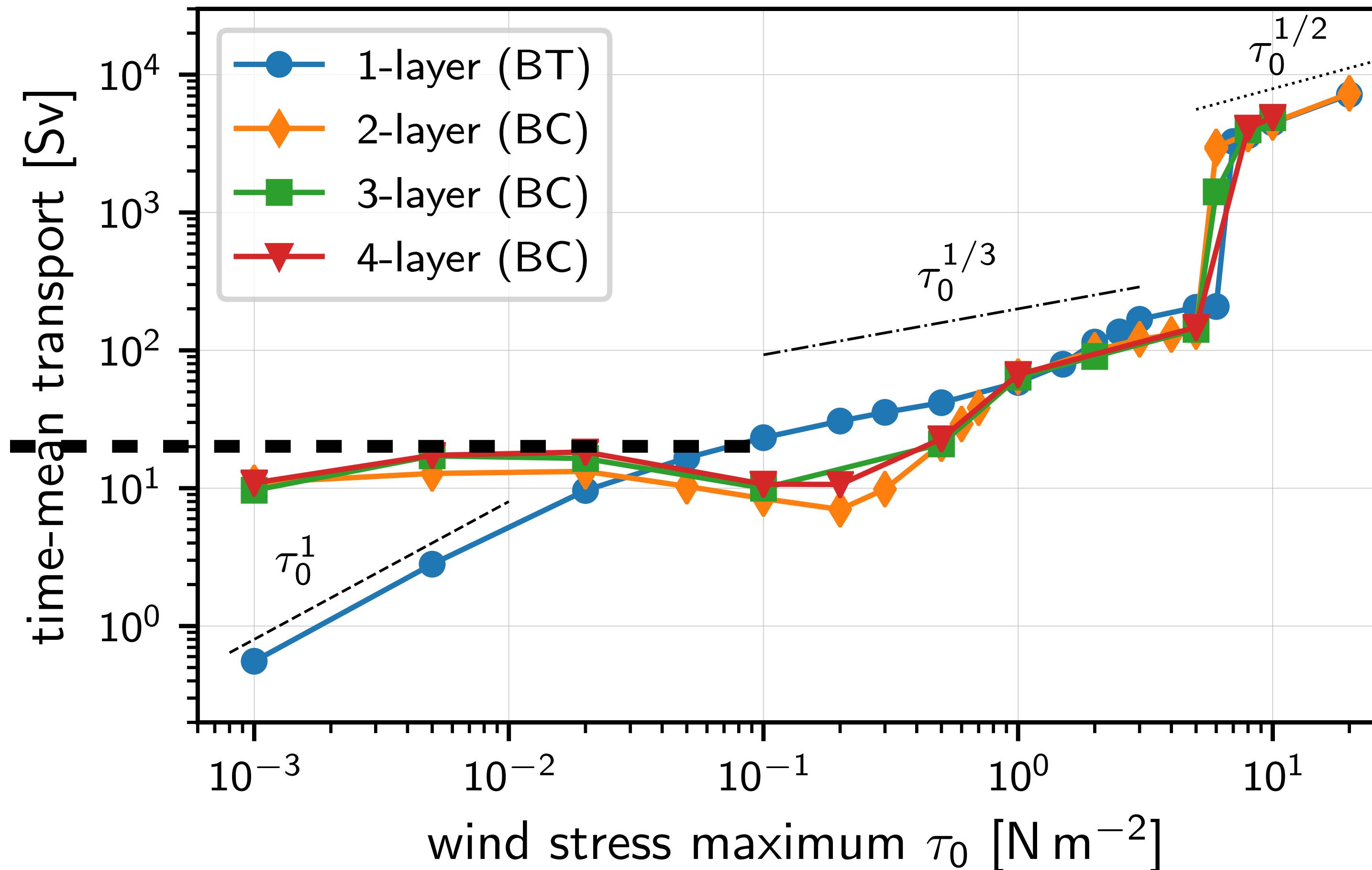
$$T = \lambda \frac{N}{|f|} \frac{H^2 L_y}{2\alpha_2} \approx 20 \text{ Sv}$$

Marshall et al. 2017

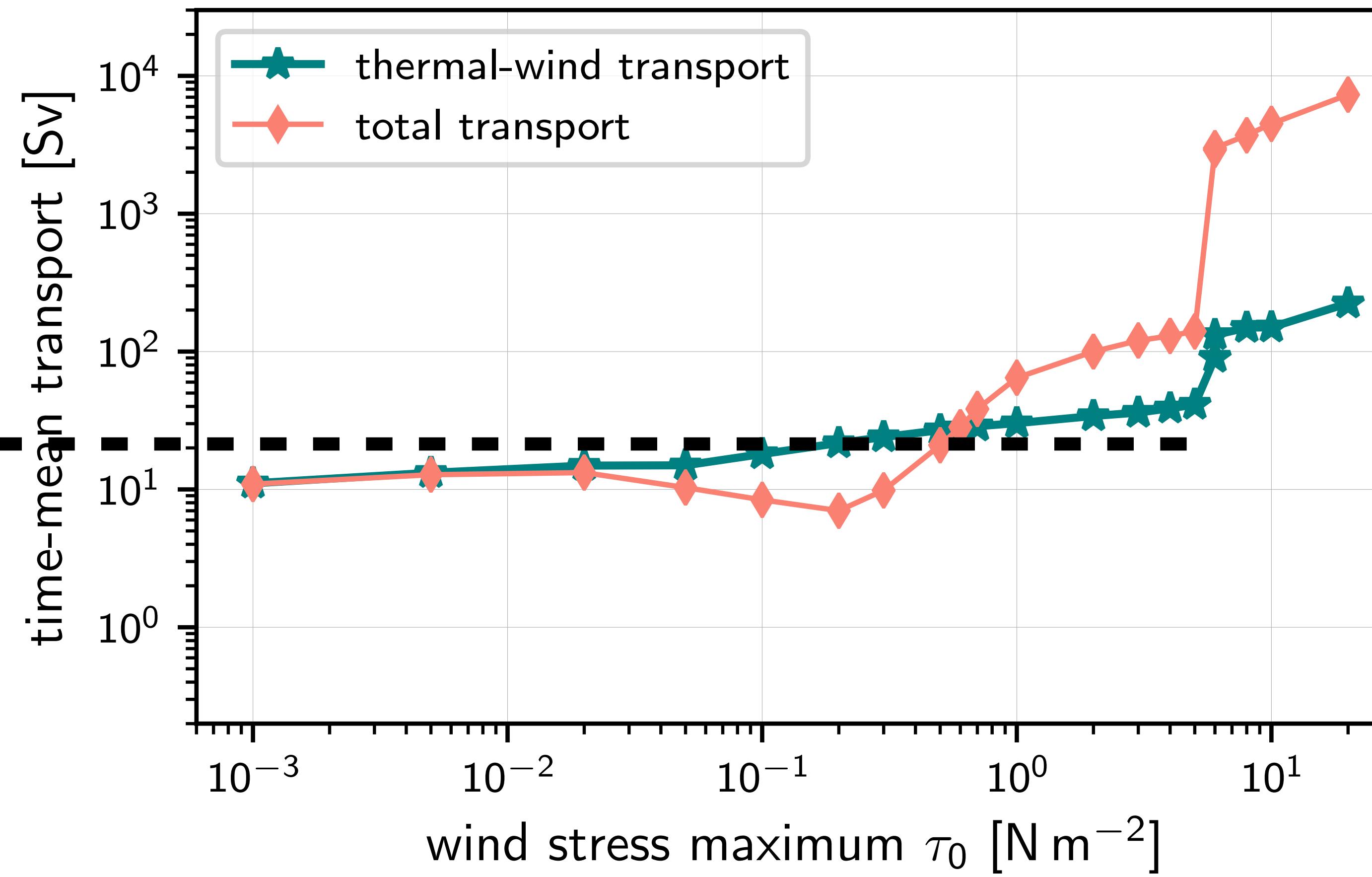
$$N = \frac{1}{H} \int_{-H}^0 \left( -\frac{g}{\rho_m} \frac{\partial \rho}{\partial z} \right)^{1/2} dz$$

$$\lambda = 1/(6 \text{ months})$$

$$\alpha_2 = 0.61$$



## 2-layer (BC)



$$T = \lambda \frac{N}{|f|} \frac{H^2 L_y}{2\alpha_2} \approx 20 \text{ Sv}$$

Marshall et al. 2017

$$N = \frac{1}{H} \int_{-H}^0 \left( -\frac{g}{\rho_m} \frac{\partial \rho}{\partial z} \right)^{1/2} dz$$

$$\lambda = 1/(6 \text{ months})$$

$$\alpha_2 = 0.61$$

$$\text{thermal wind transport} = \langle \overline{h_1(u_1 - u_2)} \rangle L_y$$