



Australian National  
University

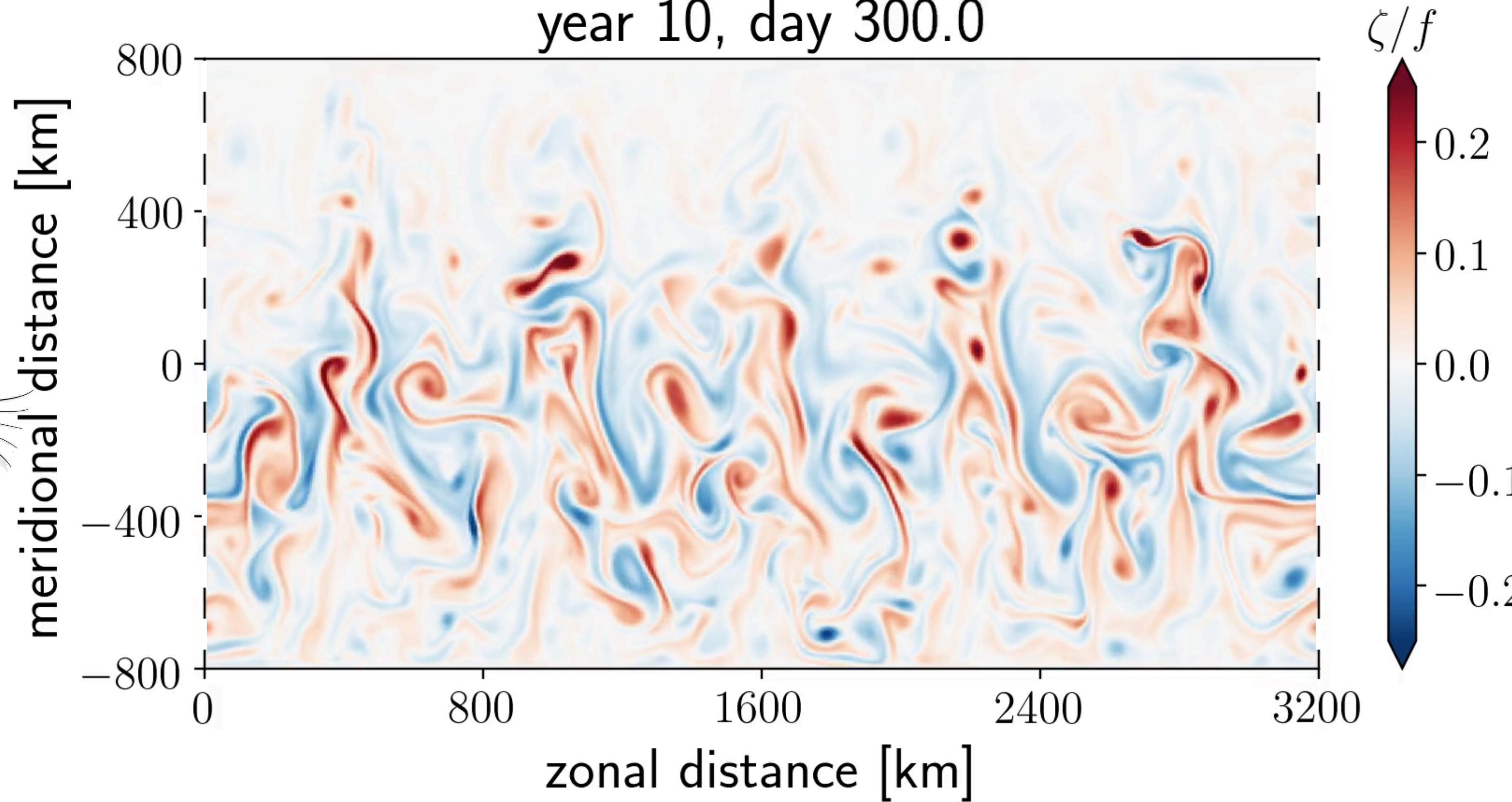
# Barotropic versus Baroclinic eddy saturation: implications to Southern Ocean dynamics



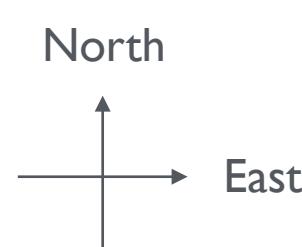
ARC Centre of Excellence  
for Climate Extremes

Navid Constantinou

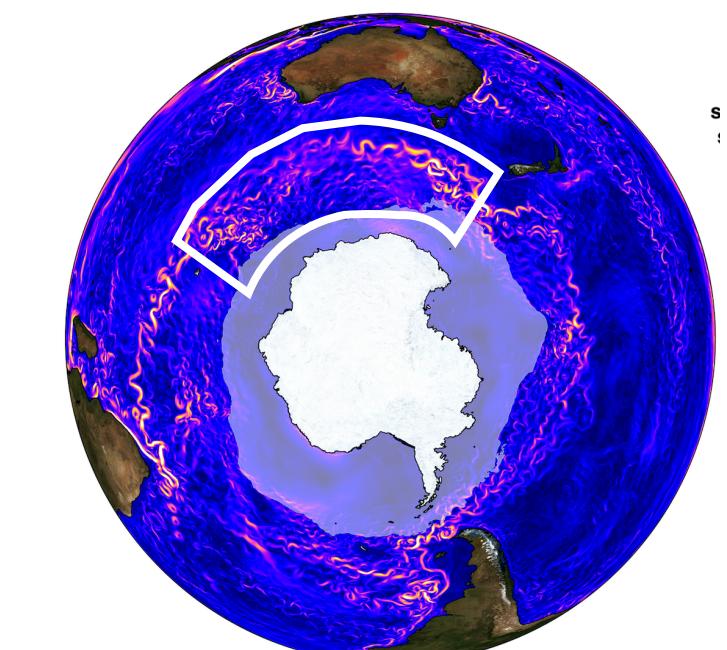
year 10, day 300.0



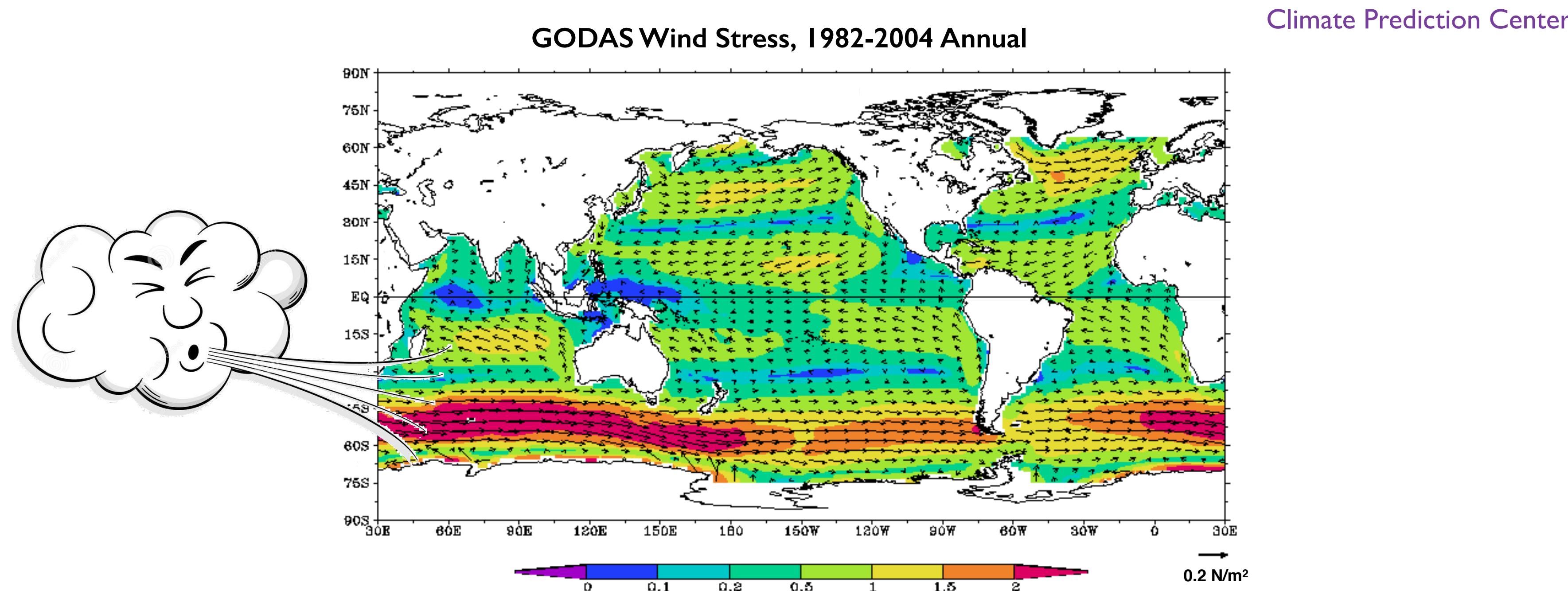
top-layer  
relative vorticity  
 $\zeta = \partial_x v - \partial_y u$



GFD Summer Program  
Walsh Cottage — July 9th, 2019



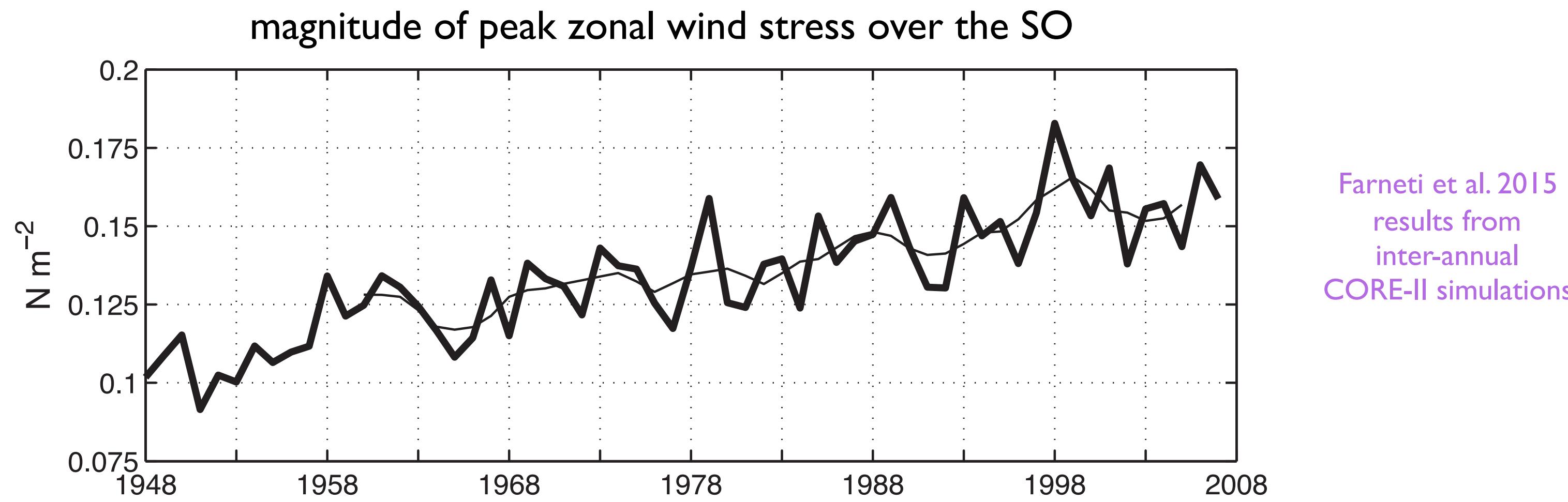
# what drives the Antarctic Circumpolar Current?



strong westerly winds blow over the Southern Ocean transferring momentum through wind stress at the surface

how is this momentum balanced?

# winds over the Southern Ocean are getting stronger



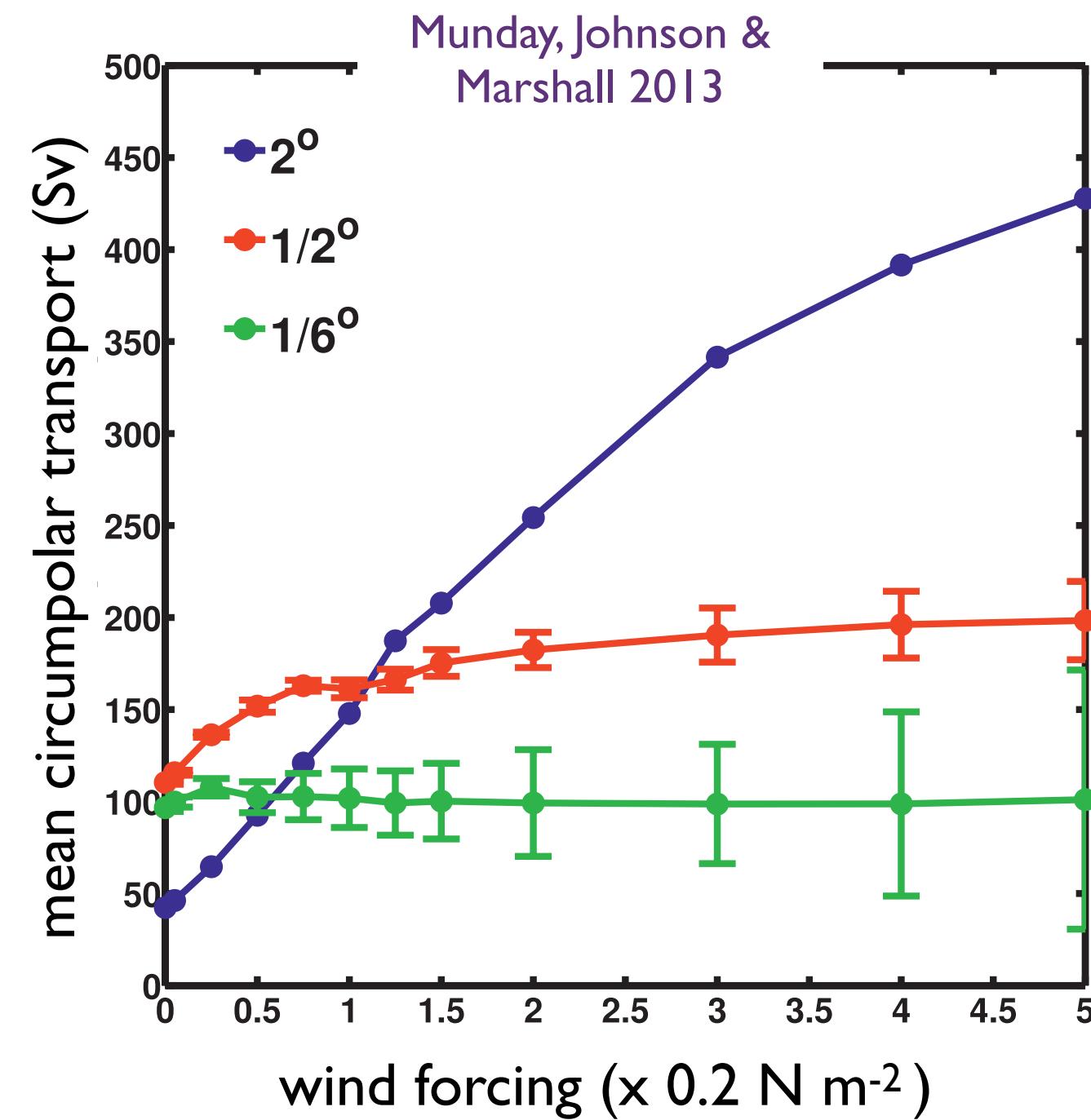
how will the Antarctic Circumpolar Current (ACC) respond?

does doubling the winds imply double ACC the transport?

not always — “eddy saturation”

# but first, what is "eddy saturation"?

The *insensitivity* of the total ACC volume transport to wind stress increase.



Eddy saturation was theoretically predicted by Straub (1993) with an entirely baroclinic argument.

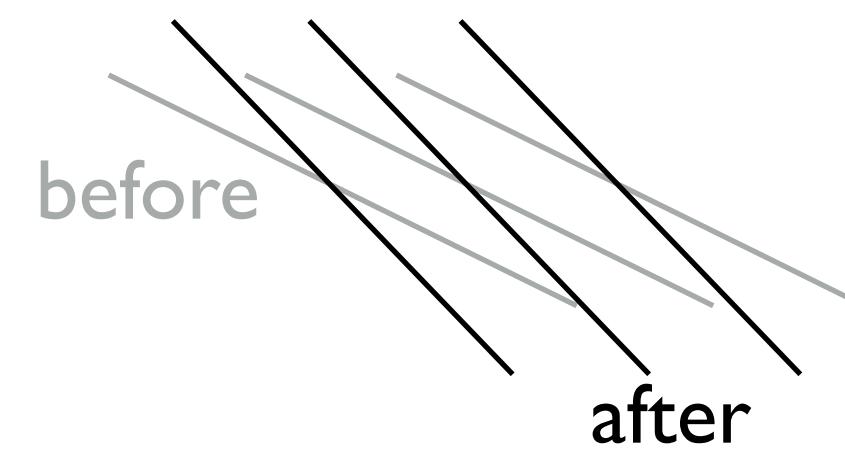
Eddy saturation is seen in eddy-resolving ocean models.  
(some hints also in obs.)

higher resolution → eddy saturation “occurs”

[Other examples: Hallberg & Gnanadesikan 2001, Tansley & Marshall 2001, Hallberg & Gnanadesikan 2006, Hogg et al. 2008, Nadeau & Straub 2009, 2012, Farneti et al. 2010, Meredith et al. 2012, Morisson & Hogg 2013, Abernathey & Cessi 2014, Farneti et al. 2015, Nadeau & Ferrari 2015, Marshall et al. 2017.]

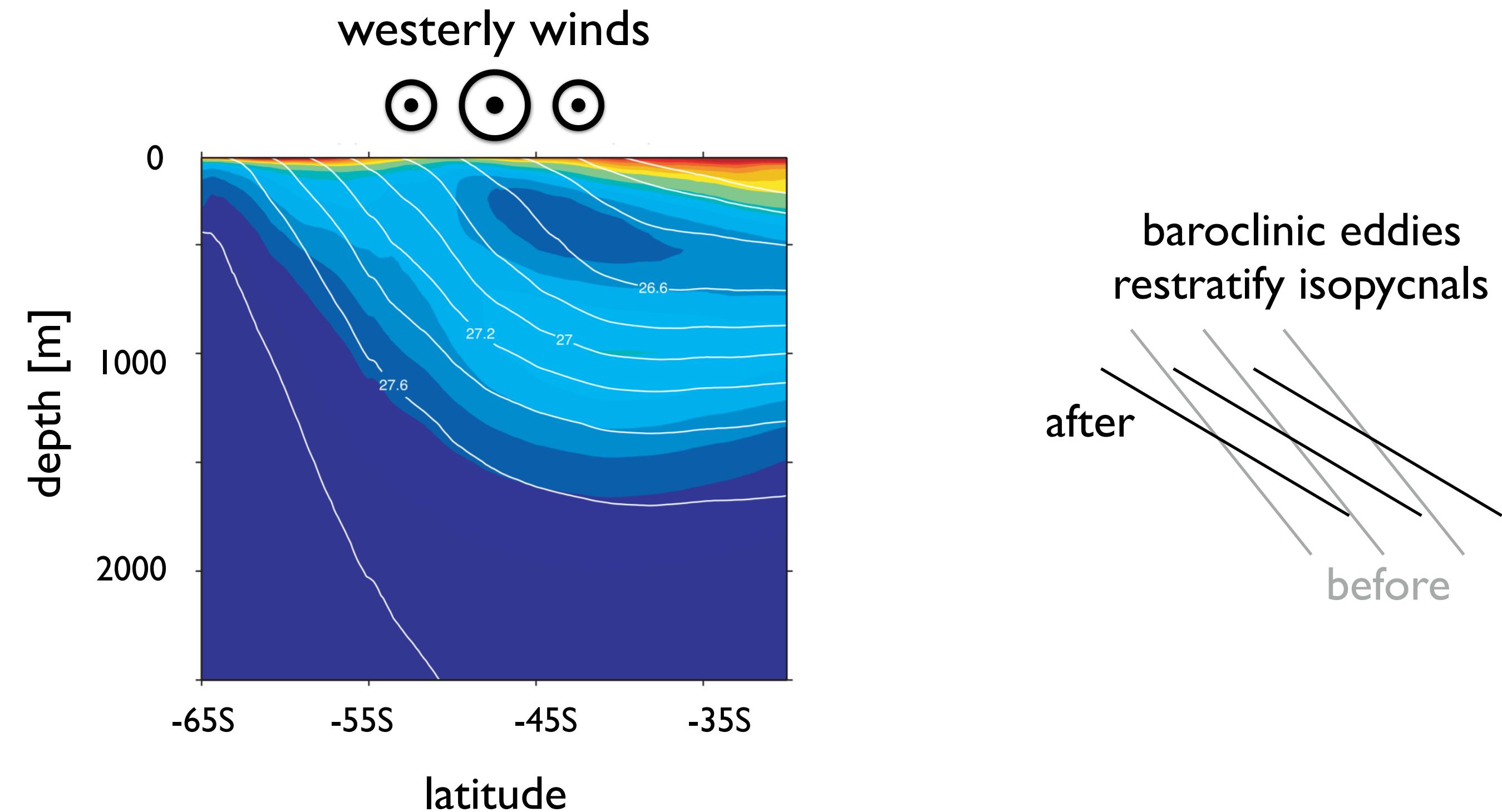
# how baroclinic eddies lead to eddy saturation?

wind increase  
slopes the isopycnals



The diagram illustrates the effect of wind on isopycnals. It shows two sets of grey lines representing density contours. The top set, labeled 'before', is relatively horizontal. The bottom set, labeled 'after', is tilted downwards from left to right, indicating that the wind has caused the isopycnals to slope.

before                          after



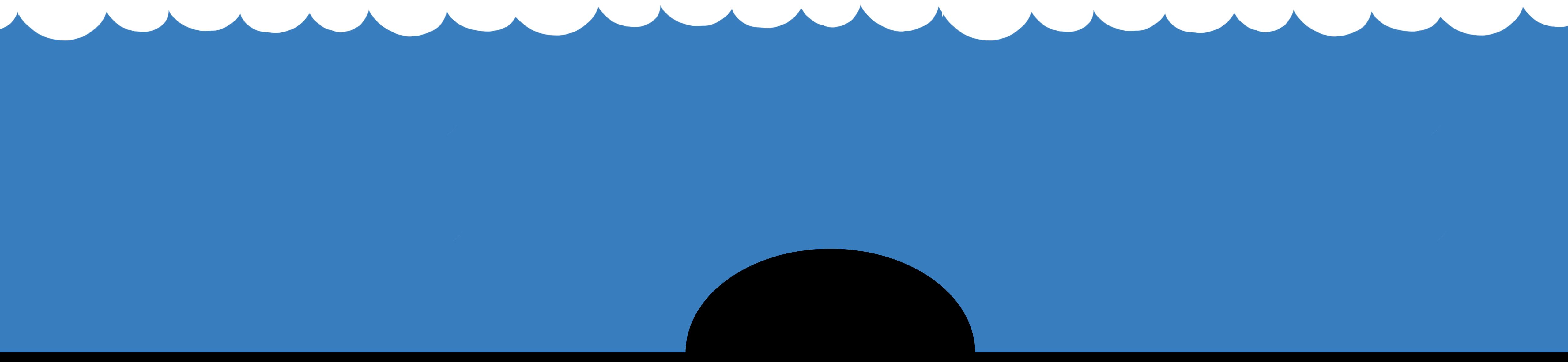
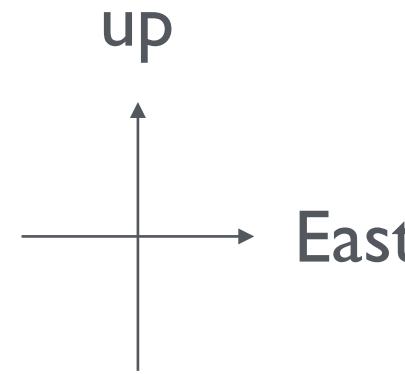
## role of bathymetry?

# role of bathymetry I

Momentum balance in the Southern Ocean is  
"applied at the bottom [...] where ridges lie."

Munk & Palmen (1951)

## topographic form stress



# role of bathymetry I

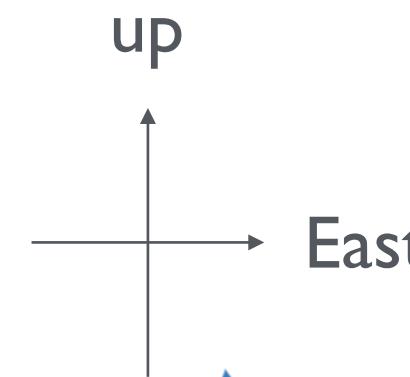
Momentum balance in the Southern Ocean is  
"applied at the bottom [...] where ridges lie."

Munk & Palmen (1951)

topographic form stress

wind

$\tau$



$U$

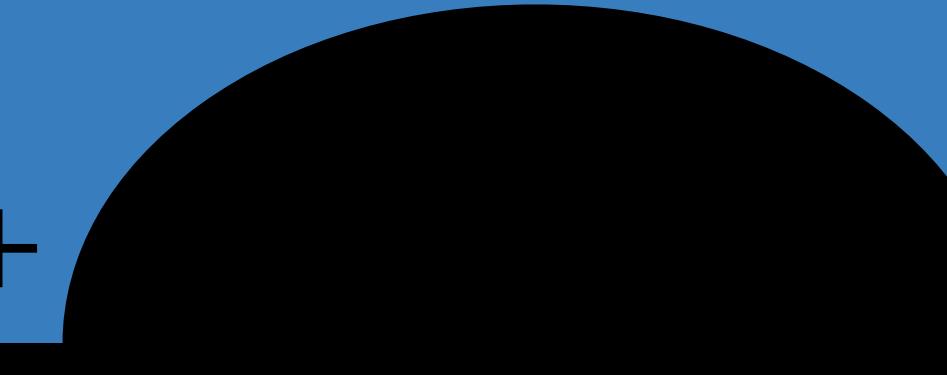


$$F_p = \Delta p/L$$



$p_+$

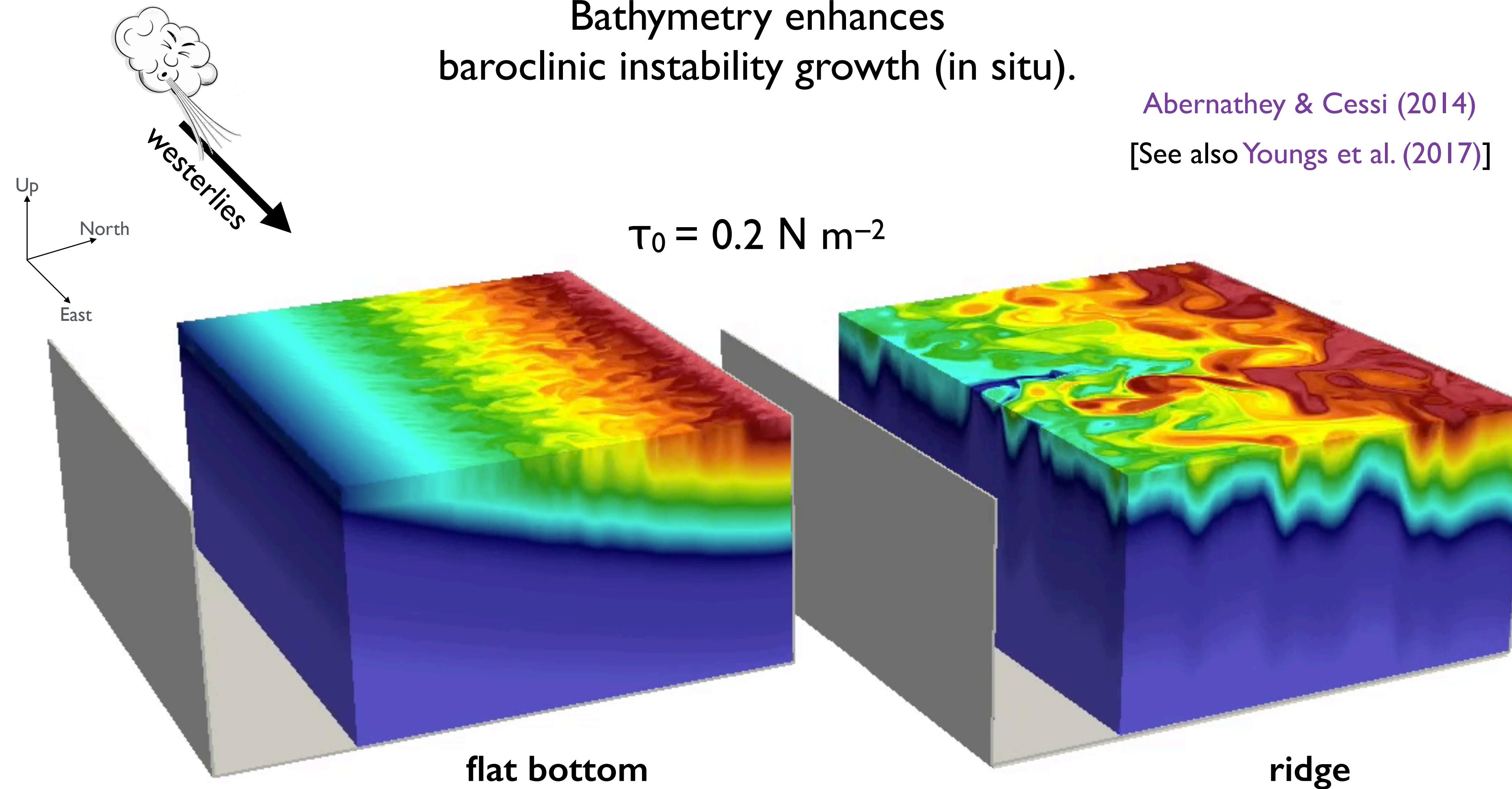
$p_-$



# role of bathymetry II

Bathymetry enhances  
baroclinic instability growth (in situ).

Abernathy & Cessi (2014)  
[See also Youngs et al. (2017)]



<http://vimeo.com/55486114>

equilibration ~100 yr  
isosurfaces of potential temperature  
colors from 0 °C to 8 °C

# the "thermal-wind" zonal transport

baroclinic interpretation  
of eddy saturation



thermal-wind component  
dominates ACC trasport

[thermal-wind transport refers to  
transport inferred from hydrography  
assuming zero flow at the bottom]

cDrake experiment measured  
time-mean bottom flows  $\mathcal{O}(10\text{cm s}^{-1})$

Donohue et al. 2016

bottom-flow contribution to ACC transport ~25%

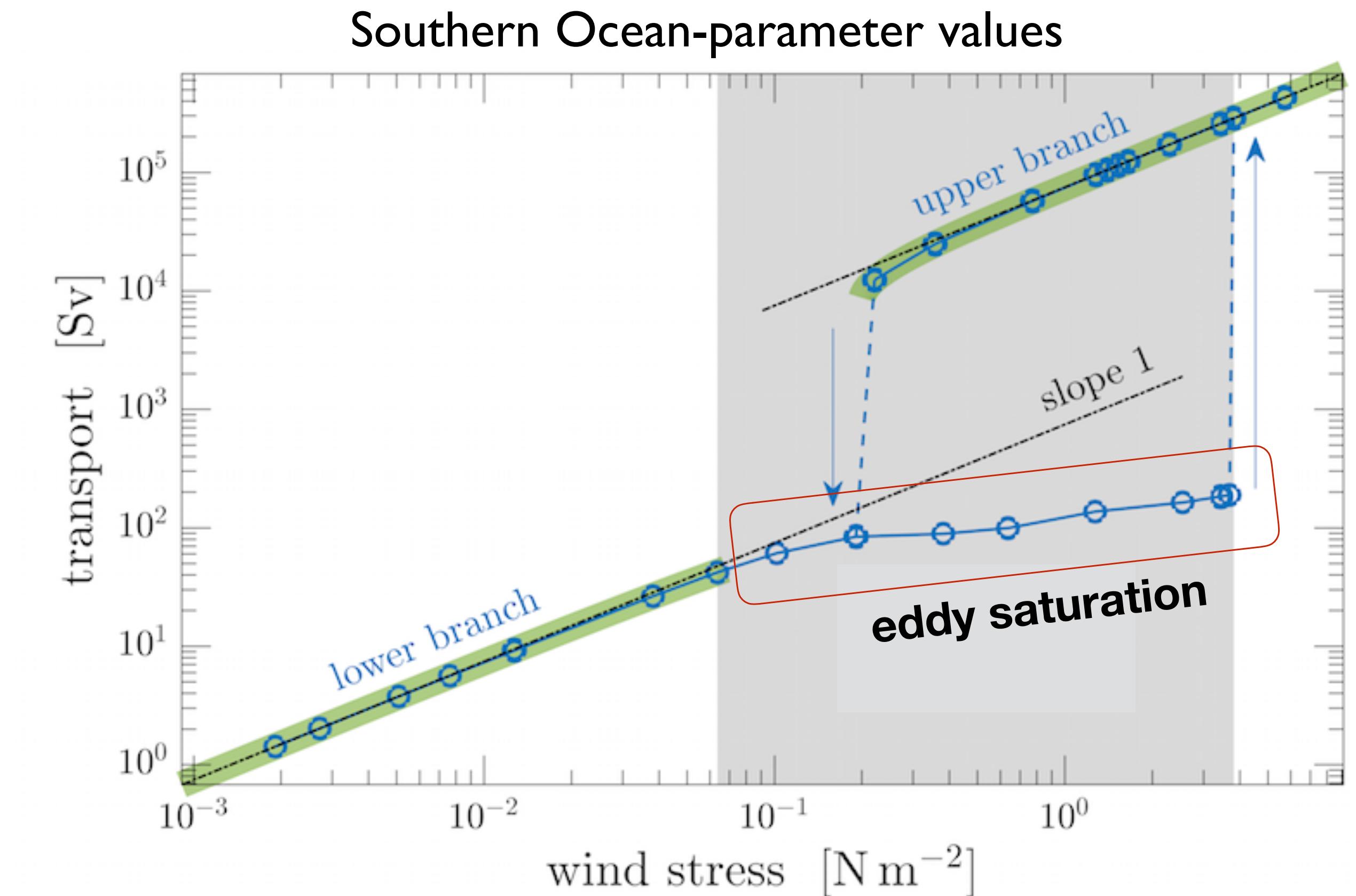


# a surprise

Eddy saturation can occur  
*without baroclinicity*  
in a homogeneous QG barotropic  
model with bathymetry.

Surprising!

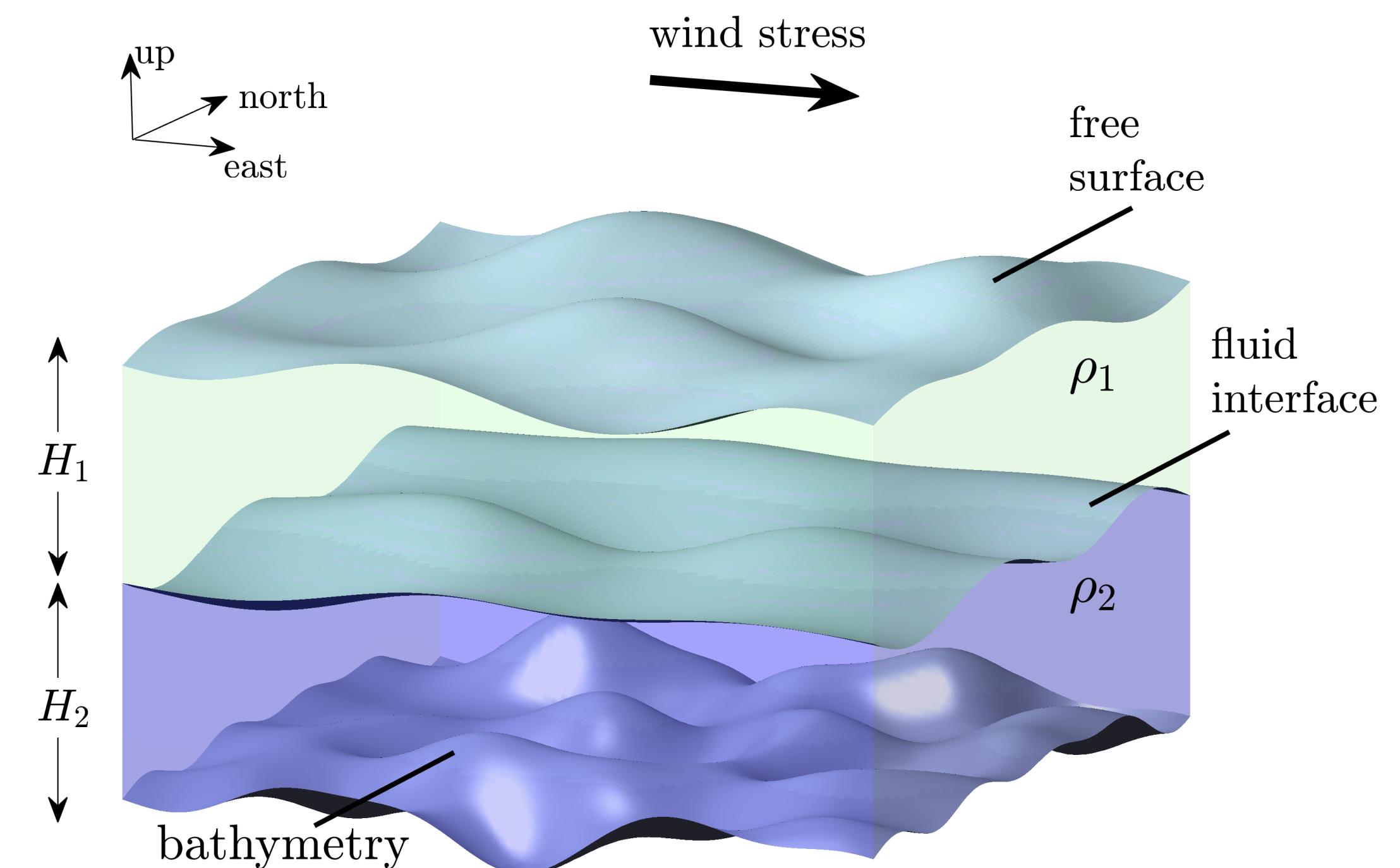
All previous arguments  
*relied on baroclinic instability*  
for producing transient eddies.



# what's the plan for today

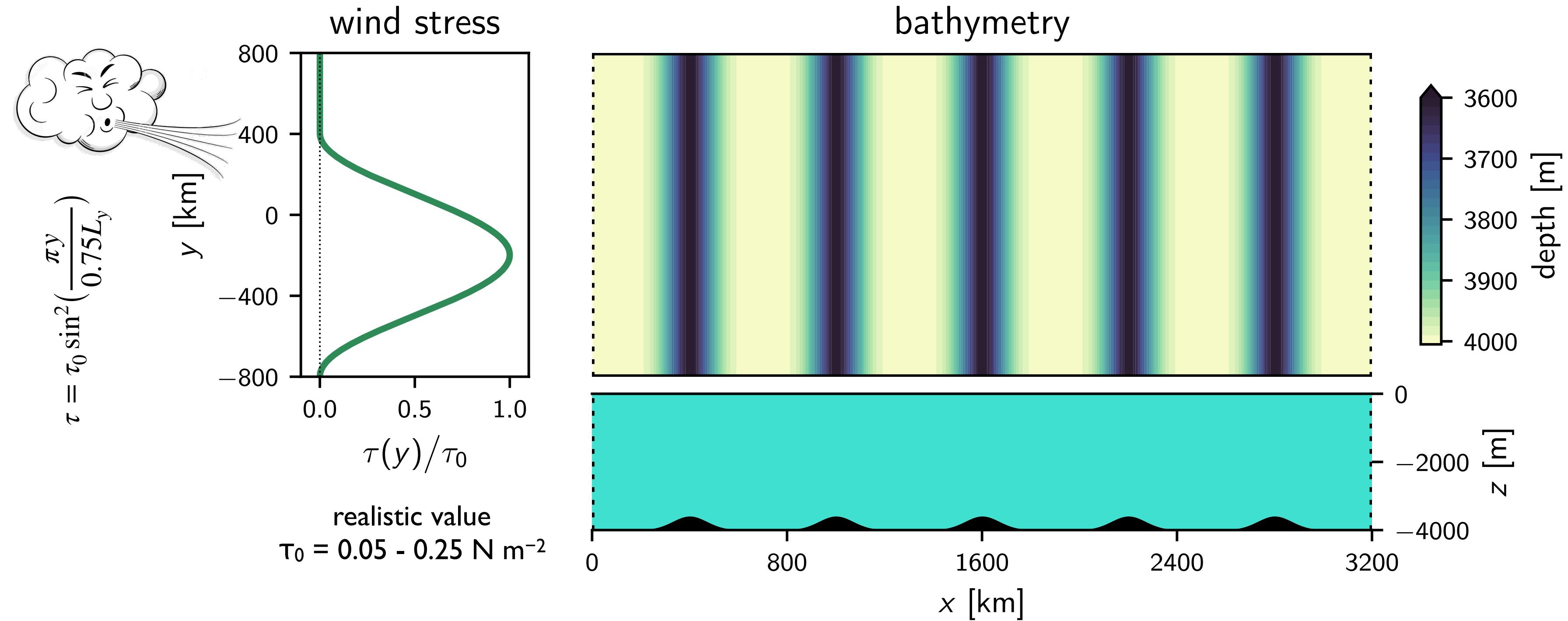
Assess the relative role of  
**barotropic** versus **baroclinic** dynamics  
in establishing "eddy saturated" ocean states.

Use an isopycnal layered model  
with varying number of fluid layers.



# model setup

GFDL's MOM6  
primitive equations  
in isopycnal coordinates  
Boussinesq approximation



$\beta$ -plane  $f = f_0 + \beta y$   
zonally re-entrant  
1st deformation radius  $\approx 19 \text{ km}$   
(2nd deformation radius  $\approx 10 \text{ km}$ )  
free surface  
free-slip walls  
quadratic bottom drag  
grid spacing 4 km

bathymetry:  
Gaussian ridges  
400 m tall, half-width 165 km

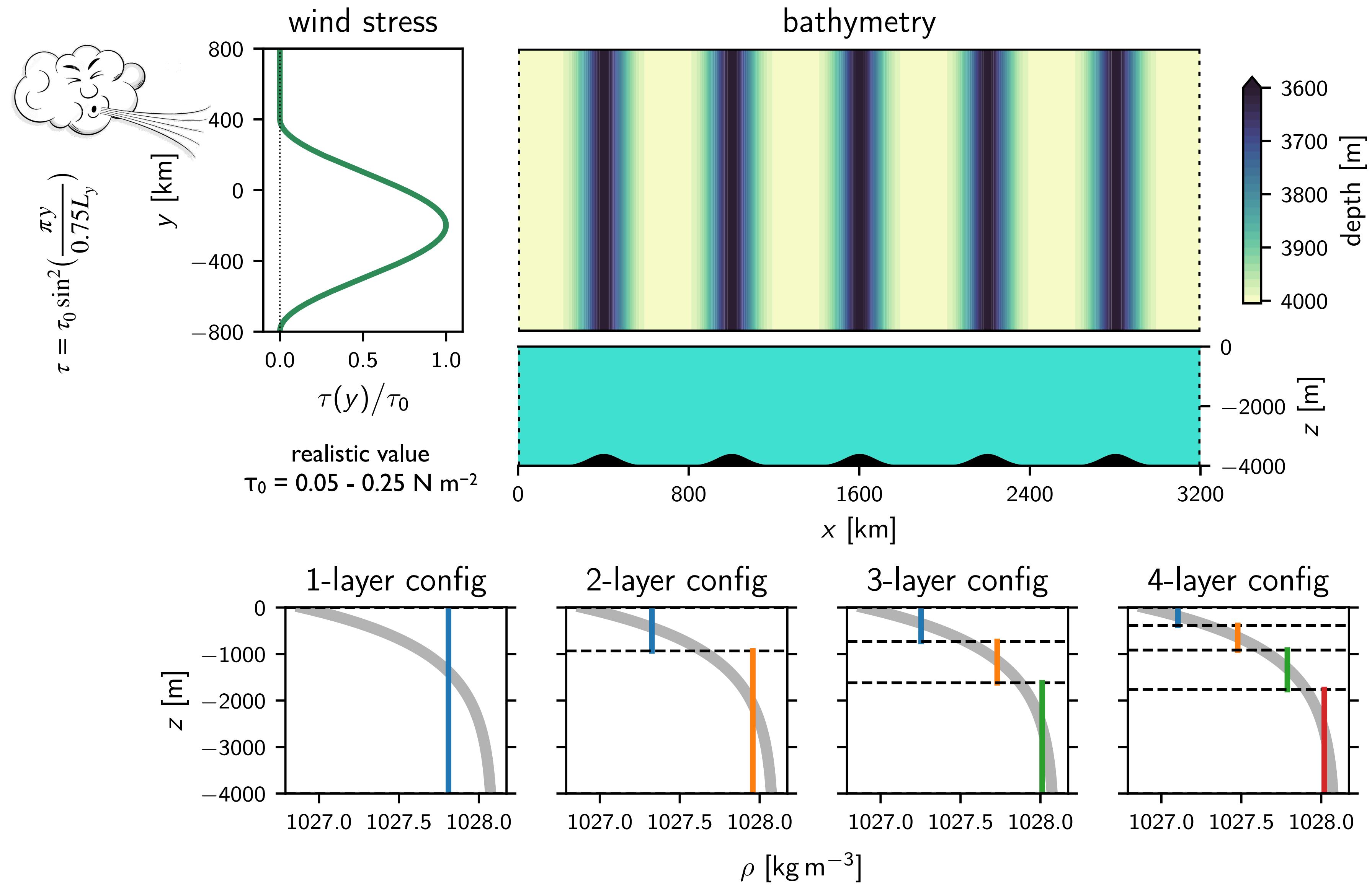
no buoyancy forcing

no diapycnal motions

$f/h$  contours are not fully blocked

# model setup

GFDL's MOM6  
 primitive equations  
 in isopycnal coordinates  
 Boussinesq approximation



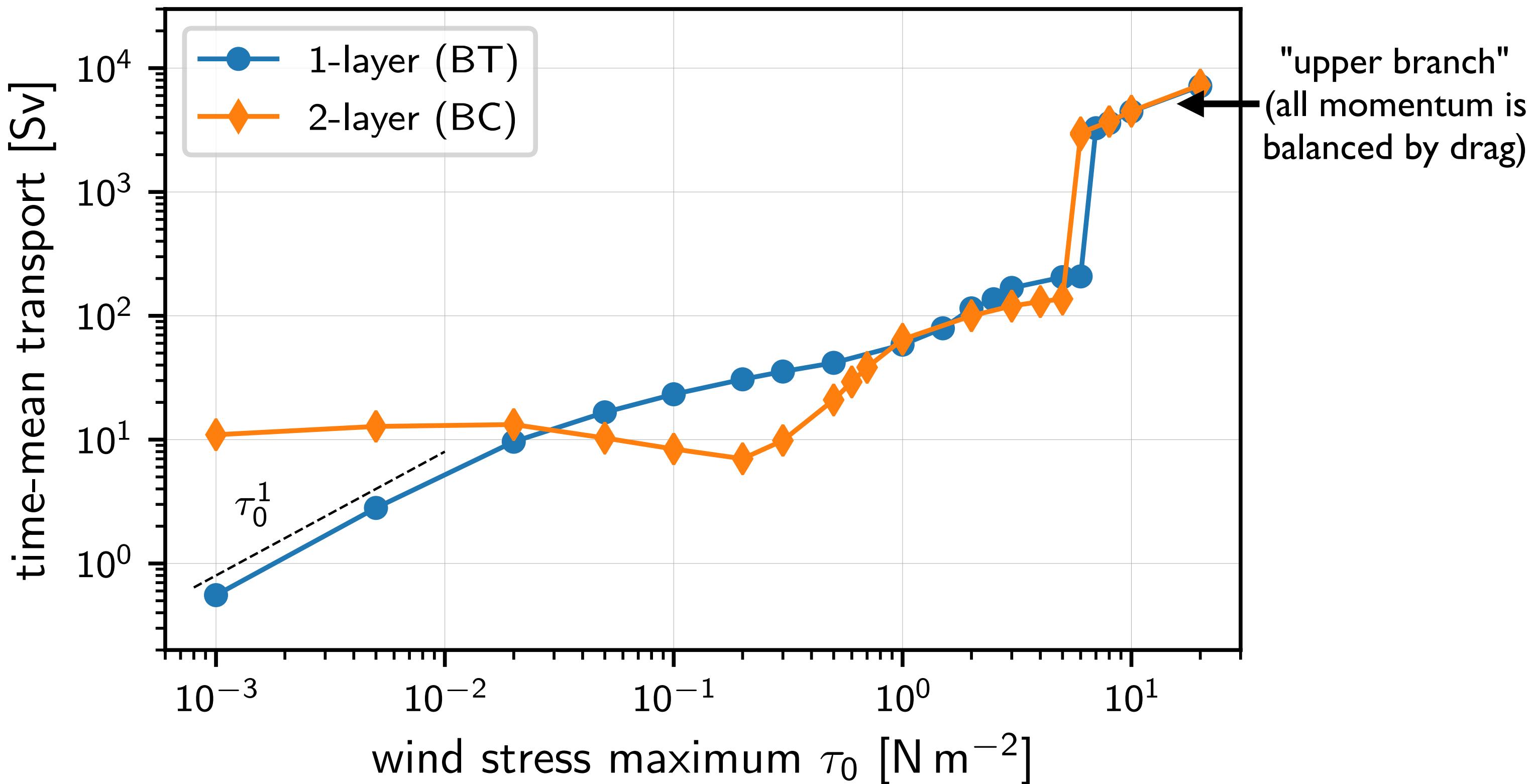
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 quadratic bottom drag  
 grid spacing 4 km

bathymetry:  
 Gaussian ridges  
 400 m tall, half-width 165 km

exponential density profile  
 $\rho = \rho_0 + \Delta\rho (1 - e^{z/d})$   
 $\Delta\rho = 1.2 \text{ kg m}^{-3}, d = 1 \text{ km}$

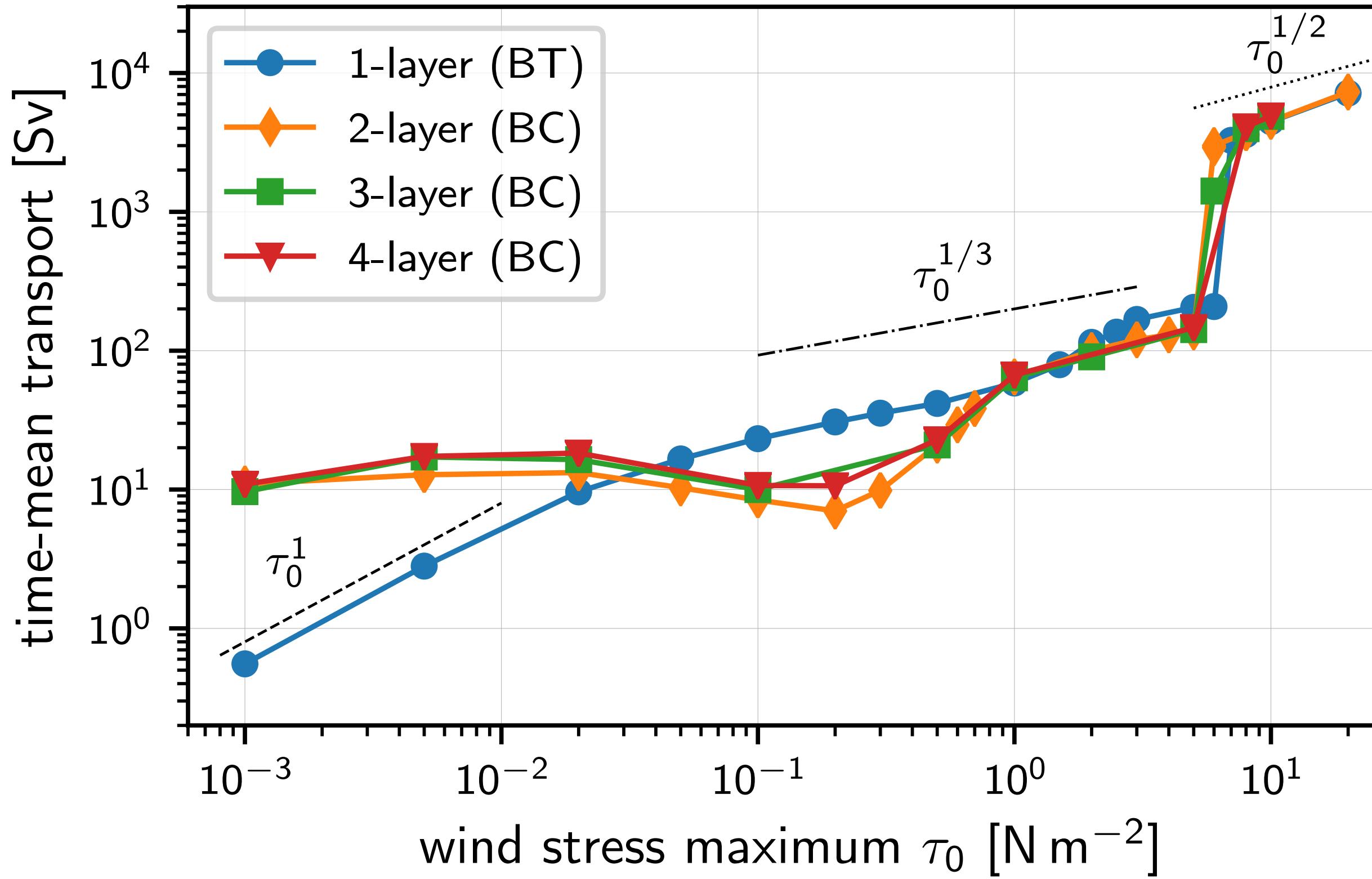
vary the wind stress amplitude  $\tau_0$   
and see how the time-mean zonal transport changes

# mean zonal transport versus wind stress



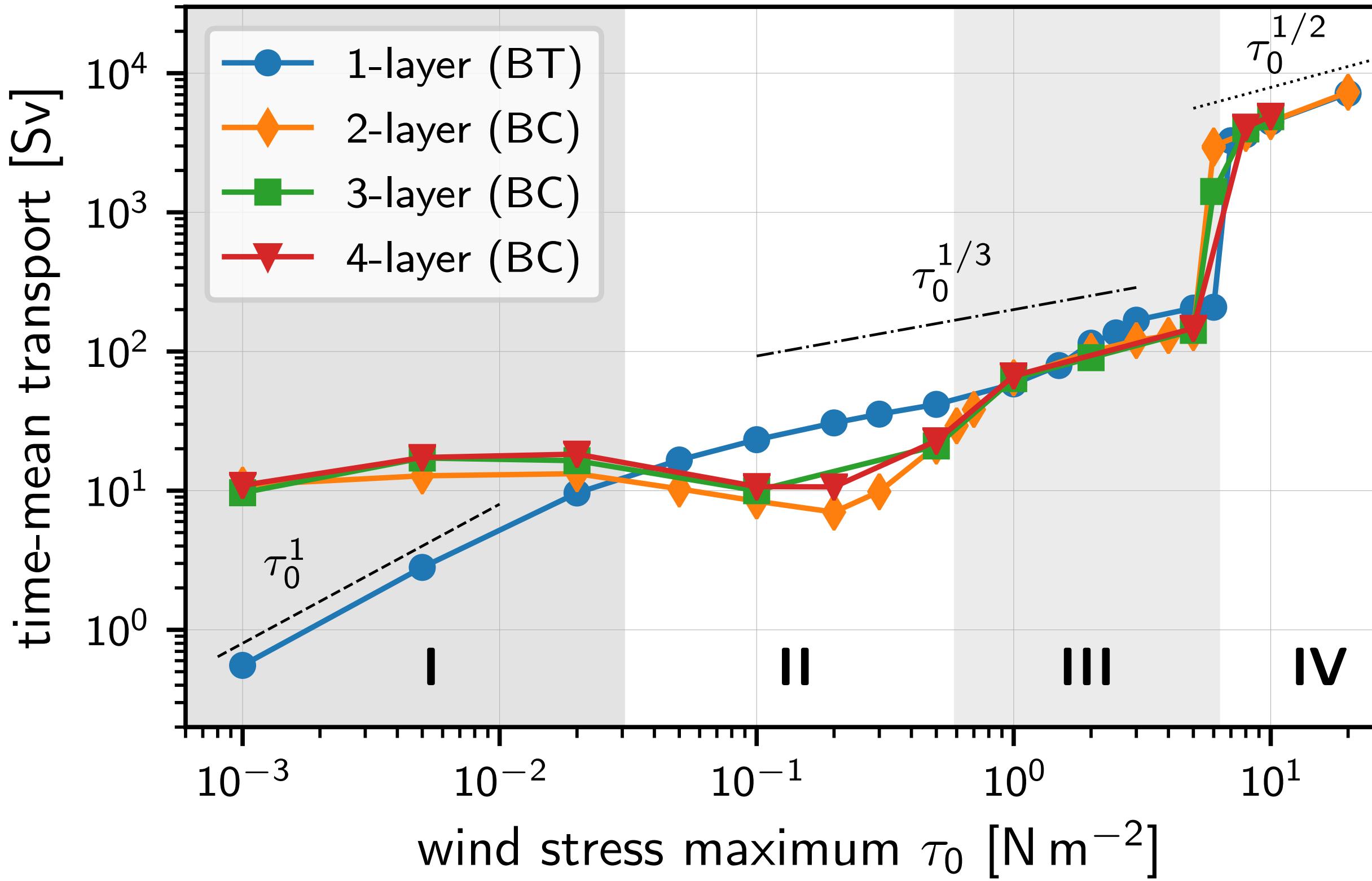
realistic  
SO values

# mean zonal transport versus wind stress



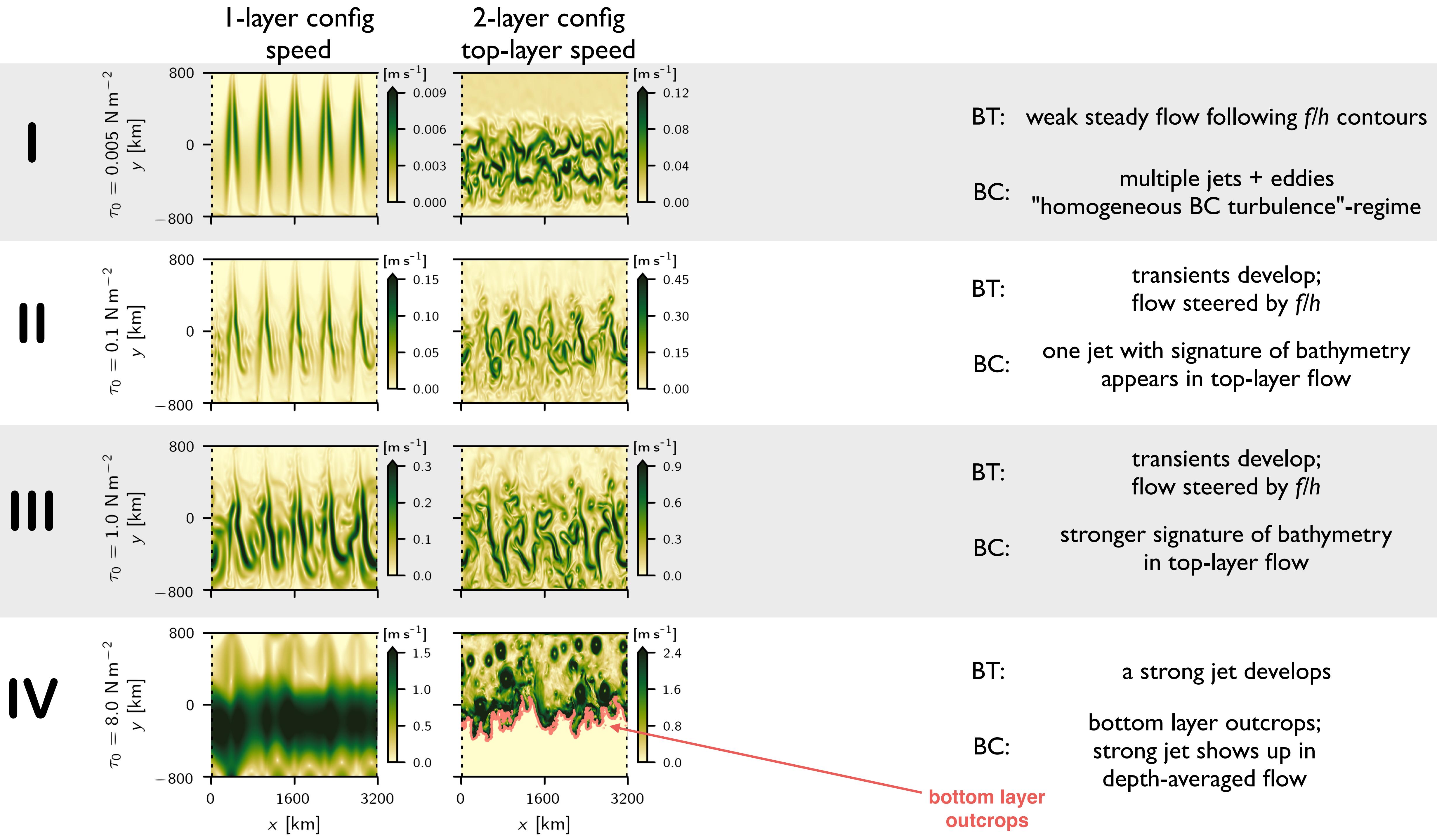
$\geq 3$ -layer configurations are the same as 2-layers  
(as far as the mean zonal transport is concerned)

# mean zonal transport versus wind stress

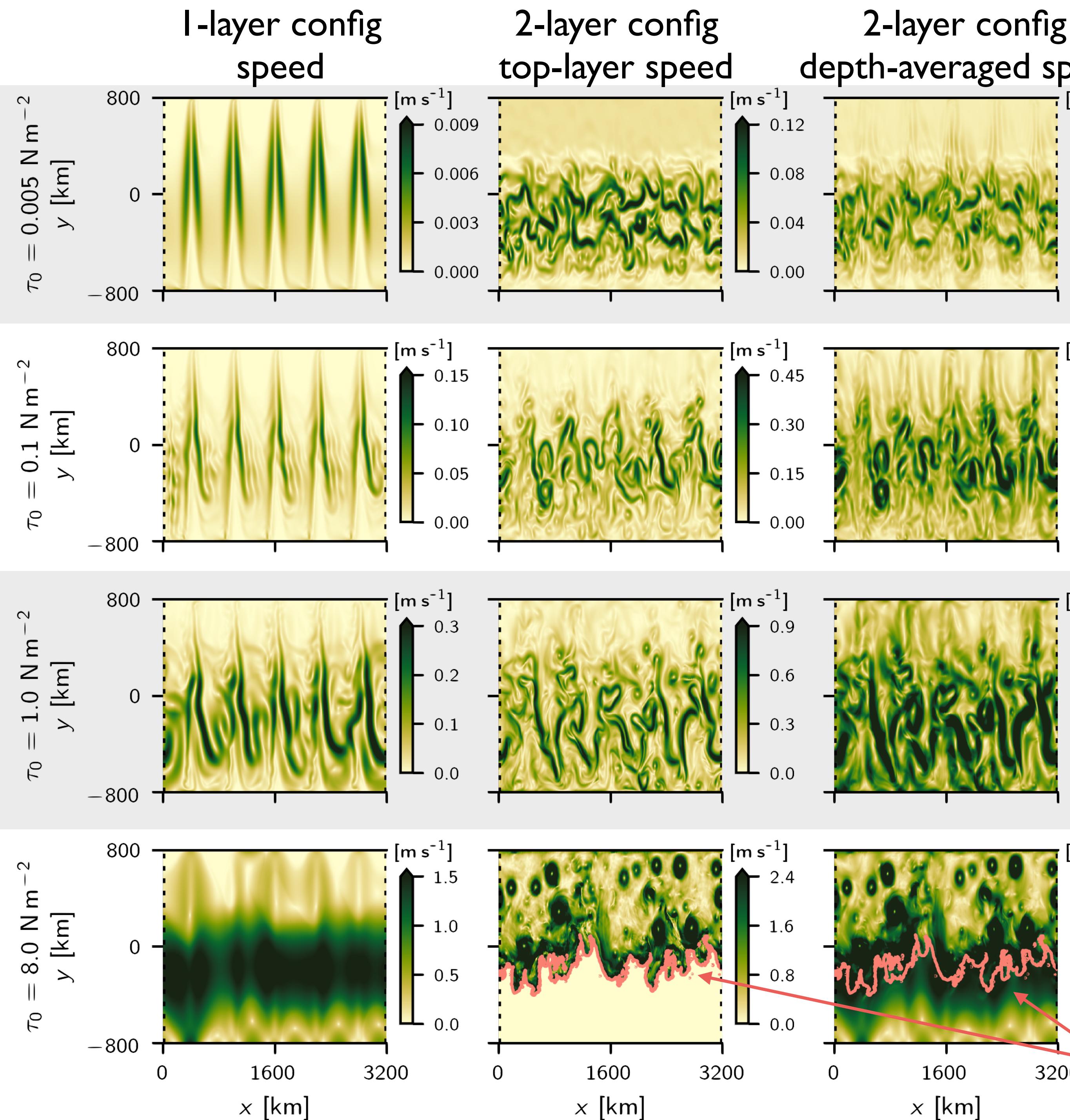


**four** distinct flow regimes

how does the flow look like  
in the four flow regimes?



I  
II  
III  
IV



BT: weak steady flow following  $f/h$  contours  
BC: multiple jets + eddies  
"homogeneous BC turbulence"-regime

BT:  
BC: transients develop;  
flow steered by  $f/h$

BT:  
BC: one jet with signature of bathymetry  
appears in top-layer flow

BT:  
BC: transients develop;  
flow steered by  $f/h$

BT:  
BC: stronger signature of bathymetry  
in top-layer flow

BT:  
BC: a strong jet develops  
bottom layer outcrops;  
strong jet shows up in  
depth-averaged flow

**bottom layer outcrops**

# depth-integrated zonal momentum balance

$\langle \rangle$ : layer average  
 $\overline{\quad}$ : time average

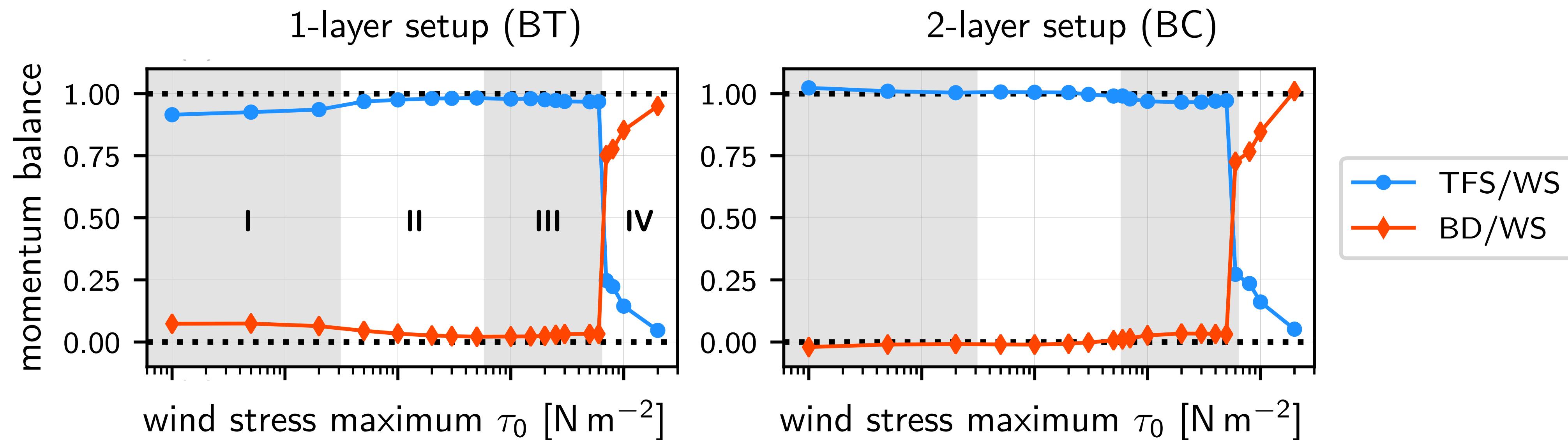
$$\langle \tau \rangle = \langle \overline{p_{\text{bot}} \partial_x h_{\text{bot}}} \rangle + \langle \rho_m c_D \overline{u_{\text{bot}} | \mathbf{u}_{\text{bot}} |} \rangle \quad \langle \overline{p_{\text{bot}} \partial_x h_{\text{bot}}} \rangle = \langle \overline{p_{\text{bot}}} \partial_x h_{\text{bot}} \rangle$$

only time-mean flow  
contributes to TFS

wind stress  
(WS)

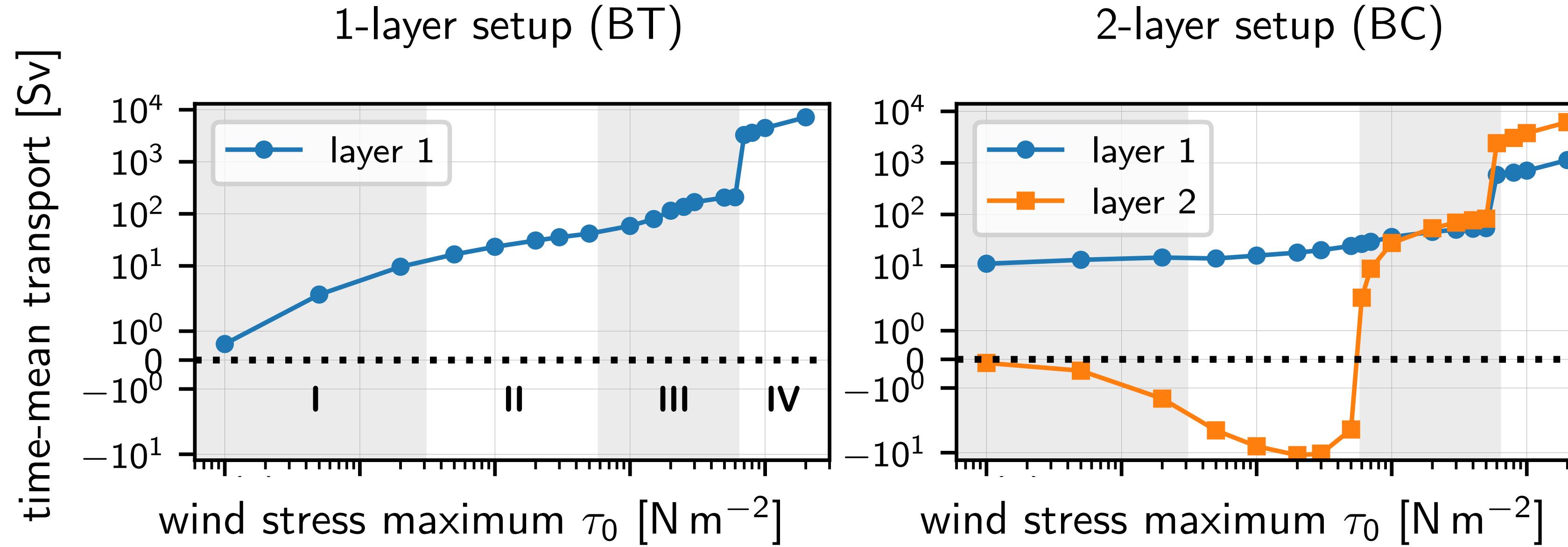
topographic  
form stress  
(TFS)

bottom drag  
(BD)



Almost *all* momentum is balanced by topographic form stress  
(except when flow transitions to "upper branch").

# layer-wise transport decomposition



[Westward  
bottom-layer flows  
also in 3-layer and  
4-layer configs.]

Similar bottom-layer westward flows were found by  
Treguier & McWilliams (1990) and Stevens & Ivchenko (1997).

Obs. evidence in certain regions of the SO (Cunningham & Barker 1996).

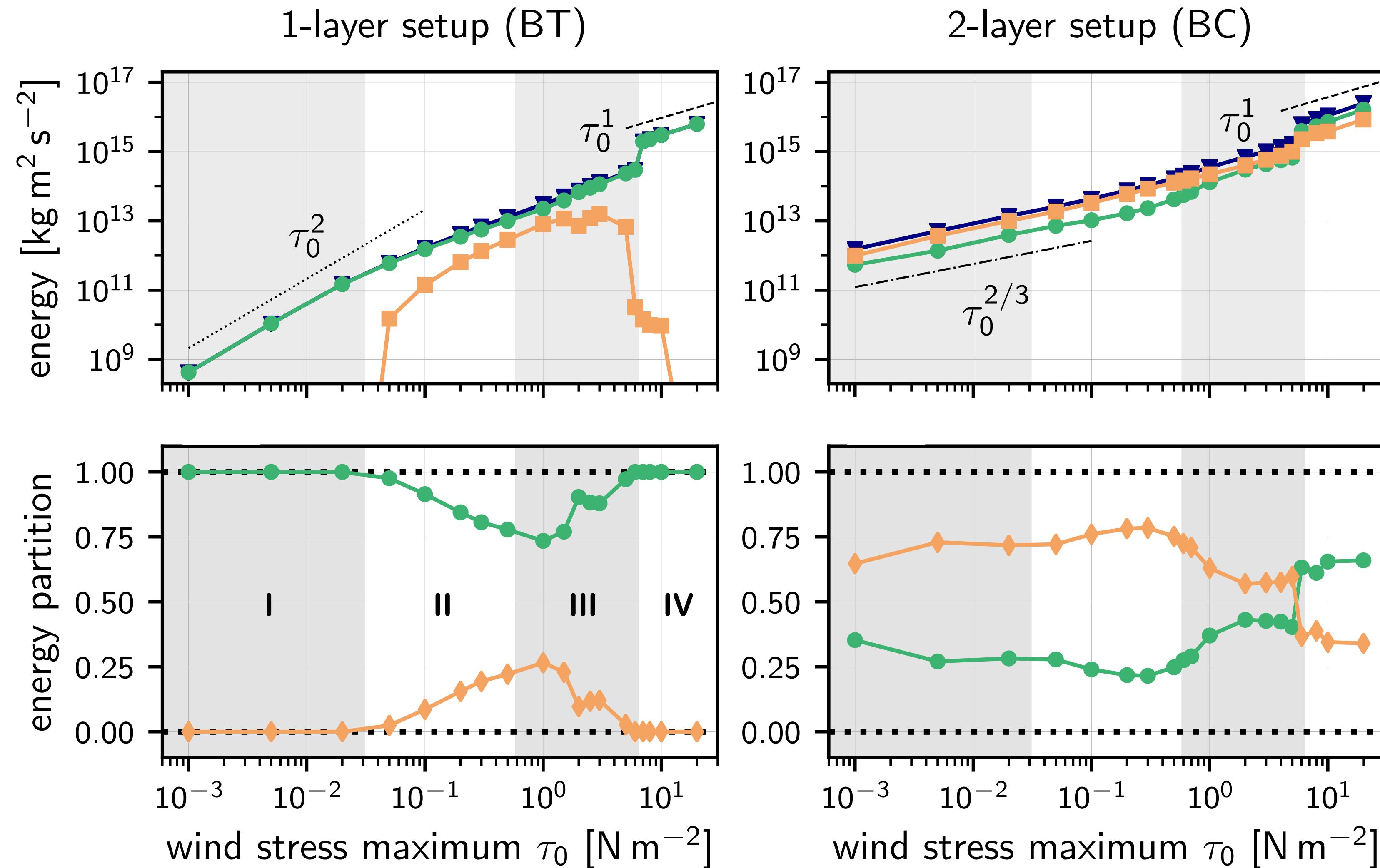
Westward flows are not robust.

Flip to eastward, e.g., for:

- $\beta=0$  [Neptune effect? (Holloway 1987)]
- single-ridge bathymetry

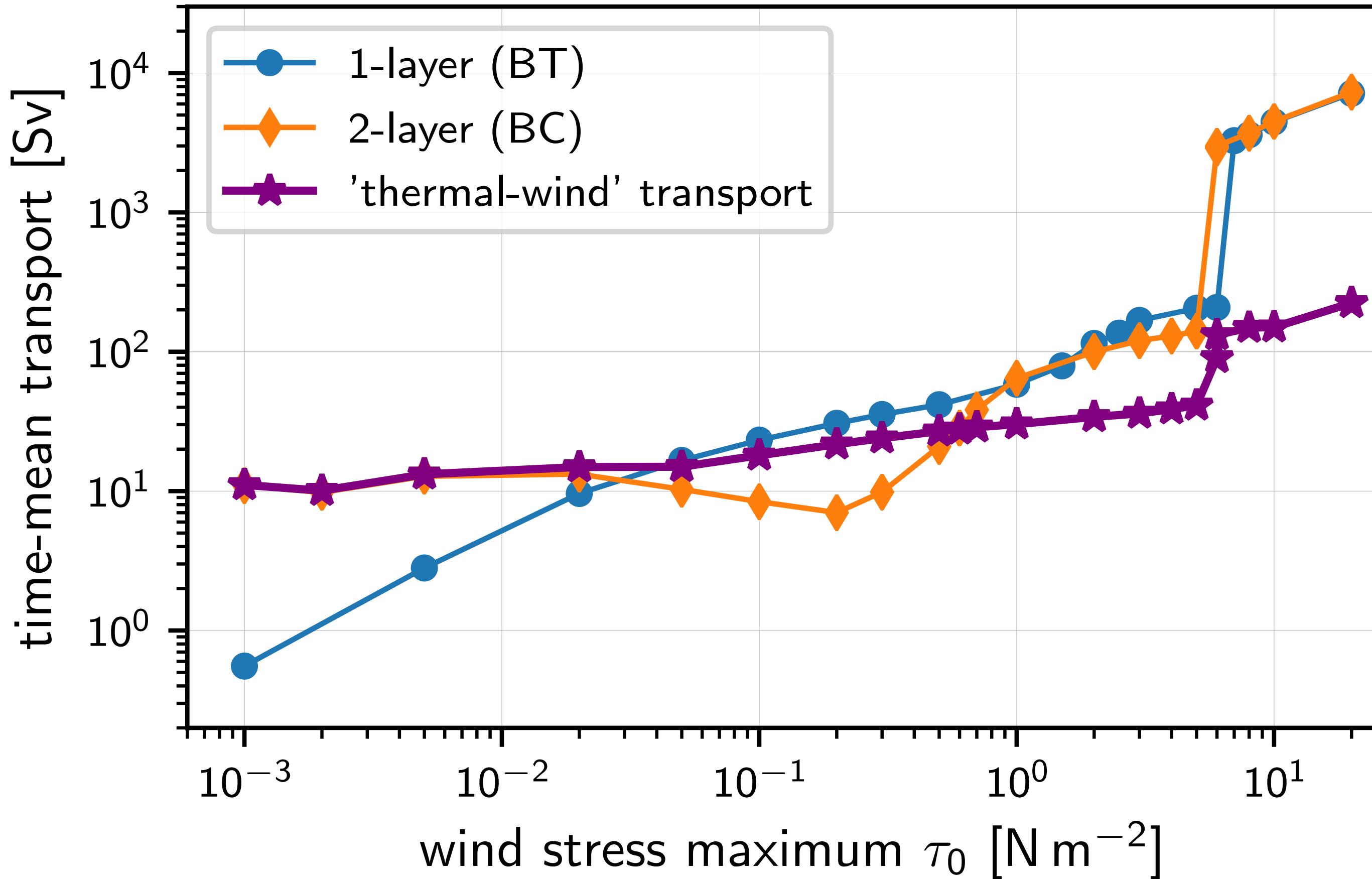
# standing-transient kinetic energy decomposition

BT config  
has transients  
only in **II & III**



Despite the great differences in flow fields,  
both **BT** and **BC** configs show same mean zonal transport for regimes **III & IV**.

"thermal-wind"-transport =  $\langle \overline{h_1(u_1 - u_2)} \rangle L_y$



"thermal-wind"-transport =  $\langle \overline{h_1(u_1 - u_2)} \rangle L_y$

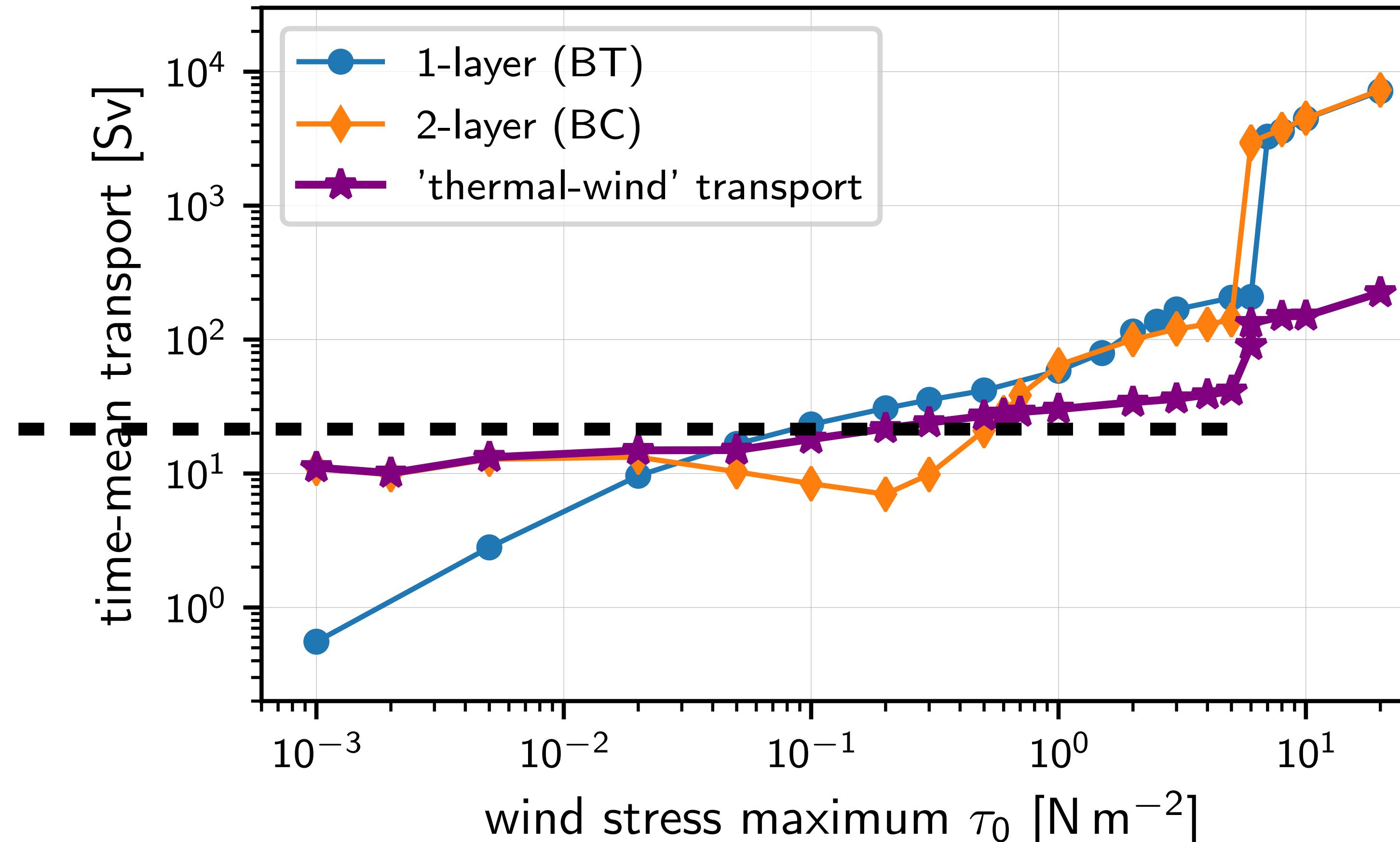
prediction by  
Marshall et al. 2017

$$T_{\text{thermal wind}} = \lambda \frac{N}{|f|} \frac{H^2 L_y}{2\alpha_2} \approx 20 \text{ Sv}$$

$$N = \frac{1}{H} \int_{-H}^0 \left( -\frac{g}{\rho_m} \frac{\partial \rho}{\partial z} \right)^{1/2} dz$$

$$\lambda = 1 / (6 \text{ months})$$

$$\alpha_2 = 0.61$$



Coincidence? Probably....

A test would be to vary  $N$  and see how the Marshall's prediction performs....

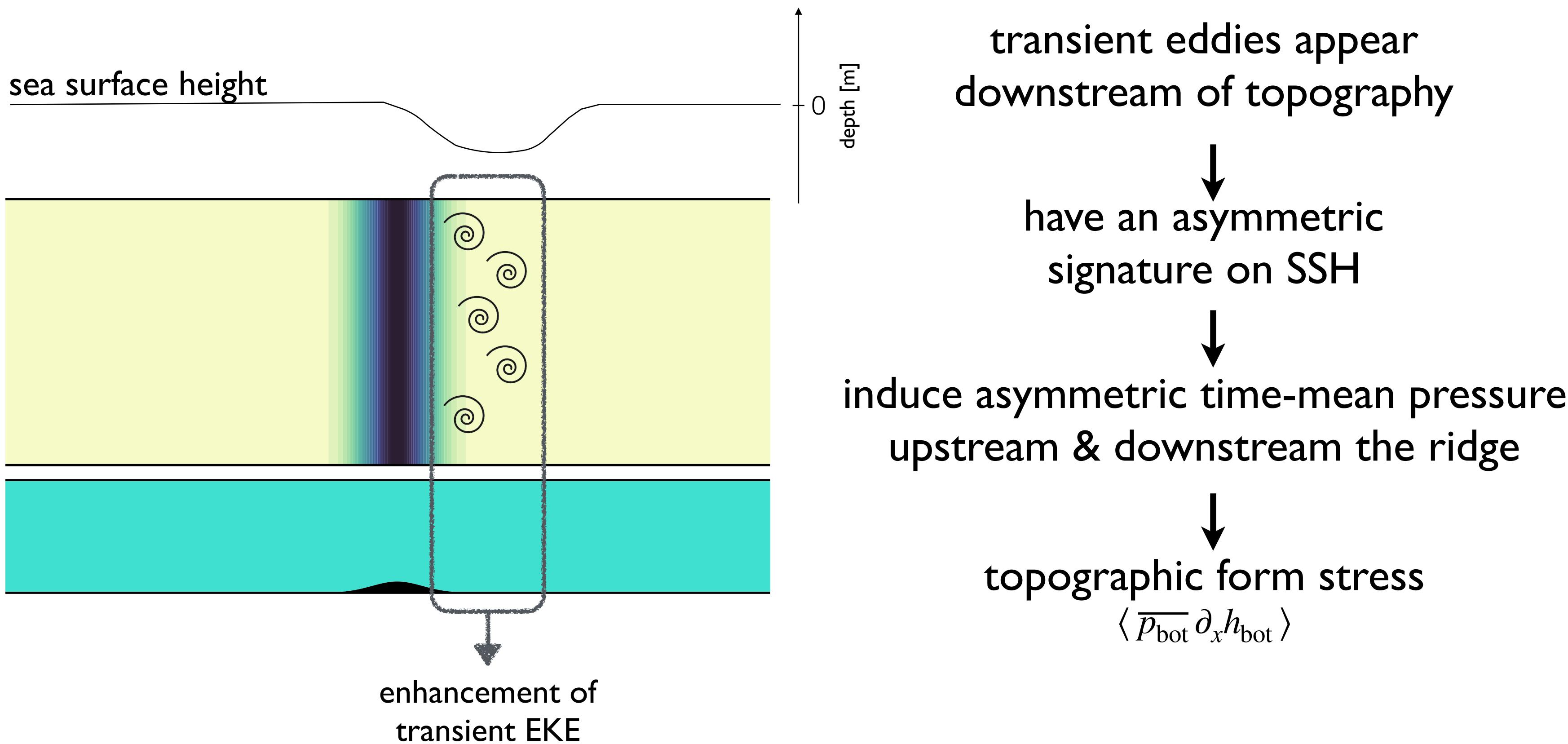
LP Nadeau finds  $T_{\text{thermal wind}} \propto N^{3/2}$  (AOFD '19).

$$\langle \overline{p_{\text{bot}} \partial_x h_{\text{bot}}} \rangle = \langle \overline{p_{\text{bot}}} \partial_x h_{\text{bot}} \rangle$$

only standing flow contributes to  
mean topographic form stress

how transients affect  
topographic form stress?

# how transients lead to time-mean topographic form stress?



[As also described by Youngs et al. 2017.]

# take home messages

when transient eddies exist (both in **barotropic** or **baroclinic** configs)  
the mean zonal transport becomes eddy saturated  
[transport is much less sensitive to wind stress increase]

**proposal:** eddy saturation occurs due to  
transient eddies shaping the standing flow  
to produce topographic form stress that balances the wind stress  
(*regardless* of the process from which transient eddies originate)

our results show that the (oftentimes ignored) bottom flow-component  
plays an important role in setting up the ACC transport  
[in agreement with recent obs. evidence, e.g., Thompson & Naveira Garabato 2014,  
Peña-Molino et al. 2014, Donohue et al. 2016 (cDrake exp)]

*thank you*

Constantinou and Hogg (2019). Eddy saturation of the Southern Ocean:  
a baroclinic versus barotropic perspective. (in review, arXiv:1906.08442)