



Australian National
University

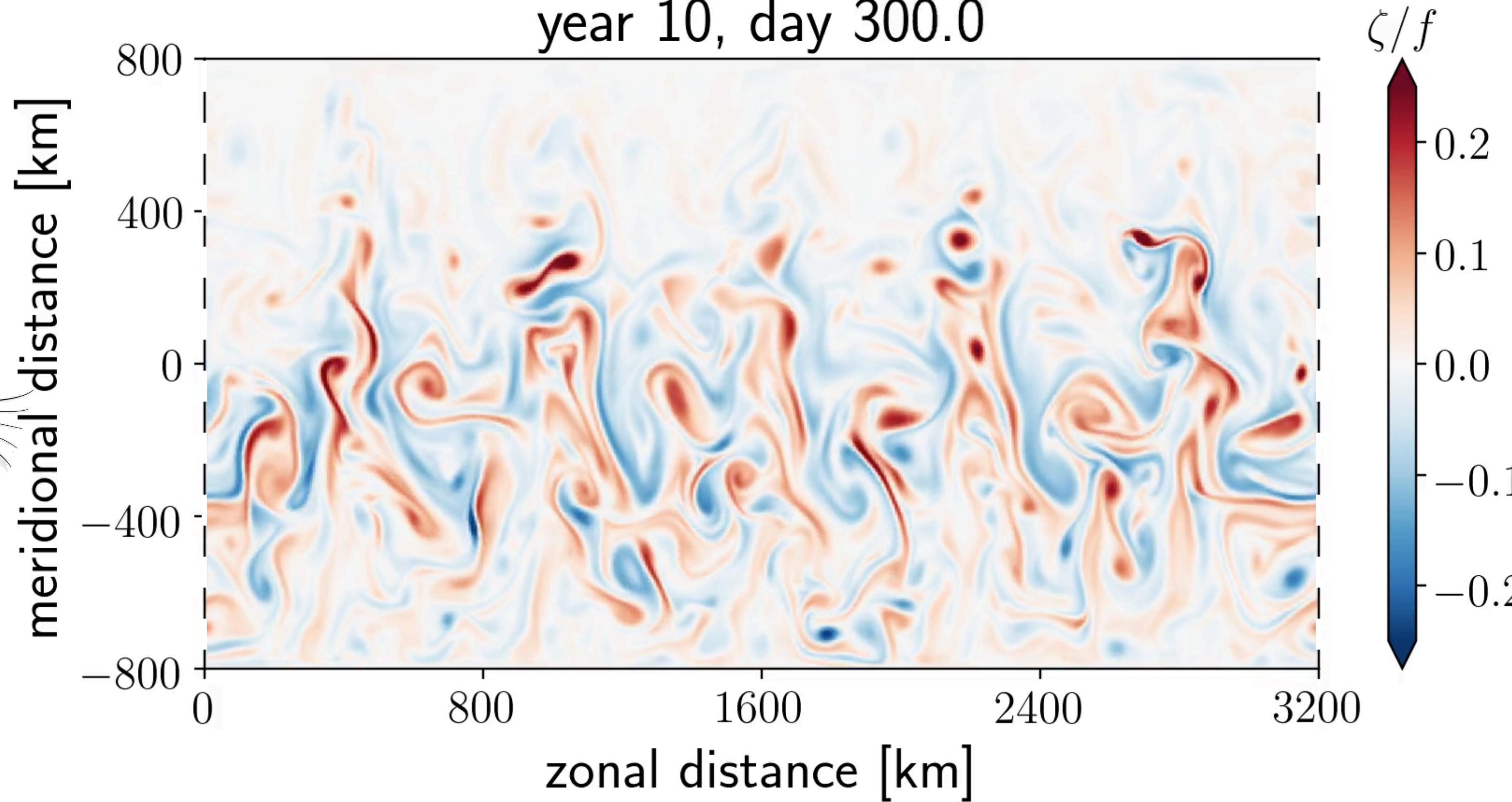
Barotropic versus Baroclinic eddy saturation: implications to Southern Ocean dynamics



ARC Centre of Excellence
for Climate Extremes

Navid Constantinou

year 10, day 300.0

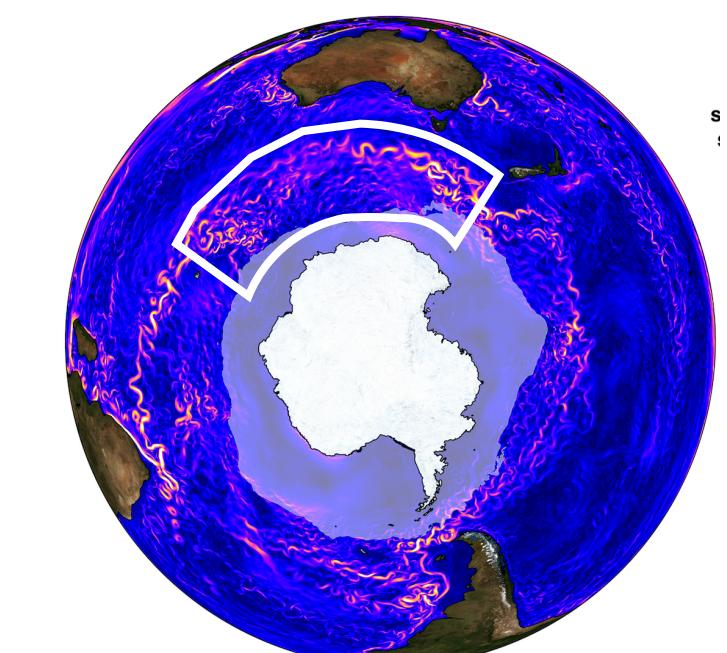


top-layer
relative vorticity
 $\zeta = \partial_x v - \partial_y u$

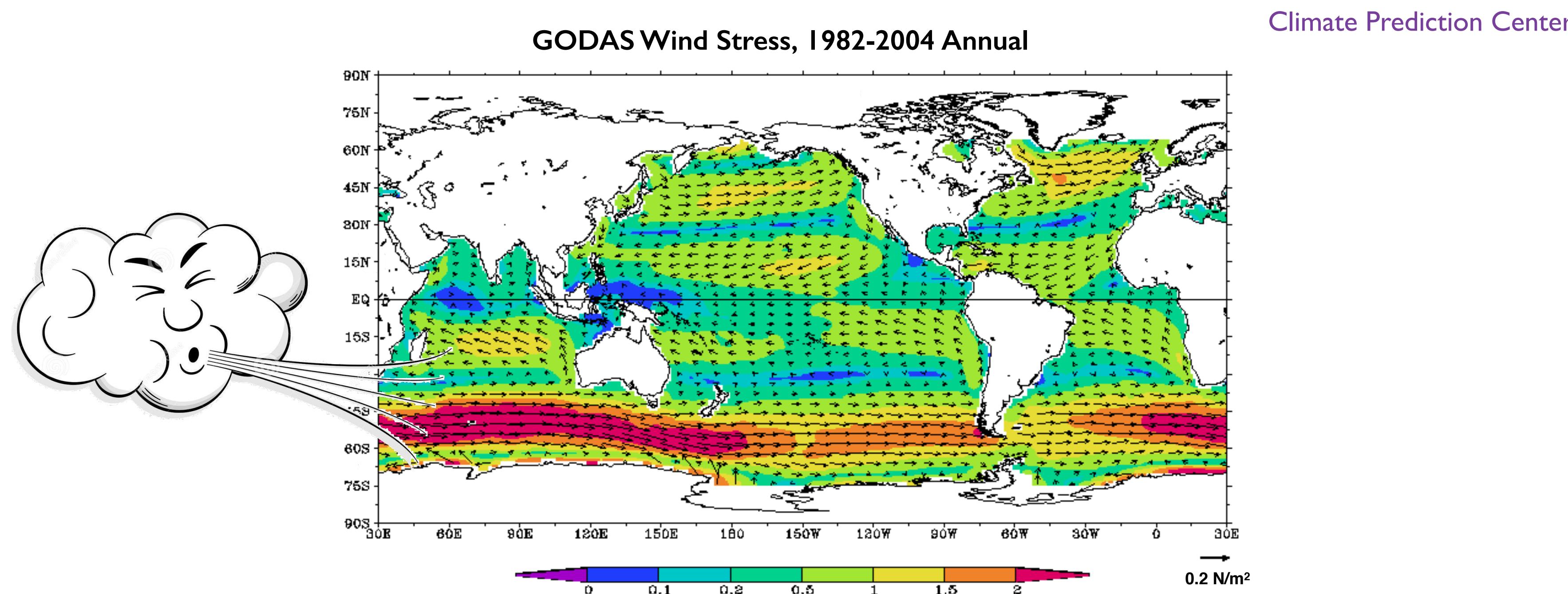


GFD Summer Program

Walsh Cottage — July 9th, 2019



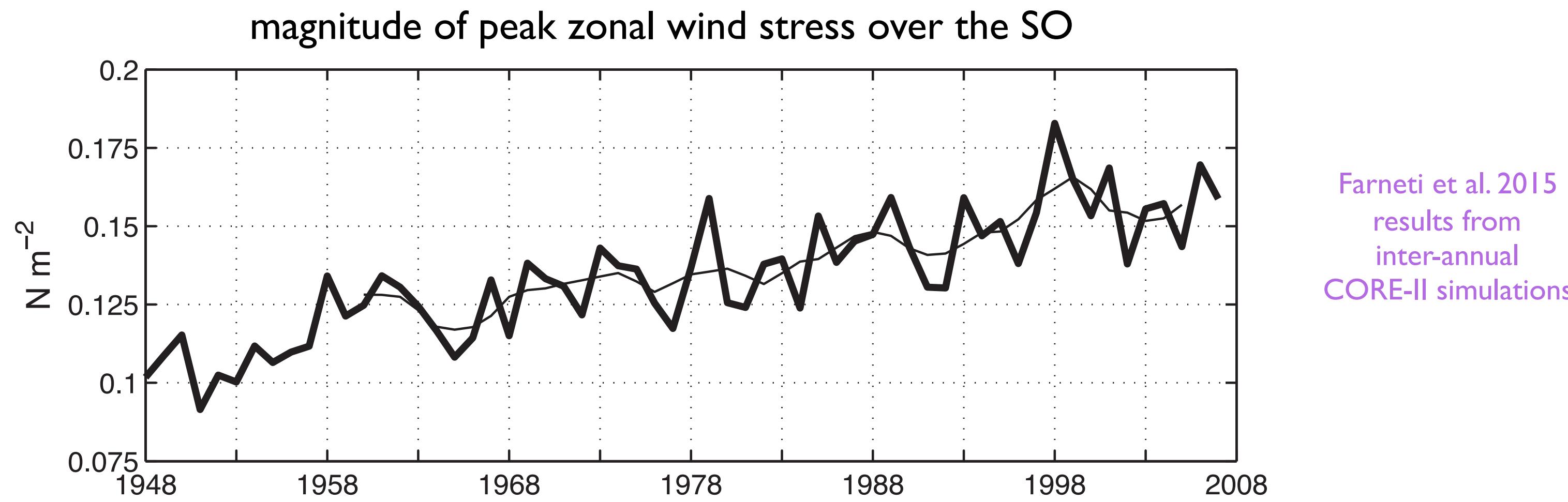
what drives the Antarctic Circumpolar Current?



strong westerly winds blow over the Southern Ocean transferring momentum through wind stress at the surface

how is this momentum balanced?

winds over the Southern Ocean are getting stronger



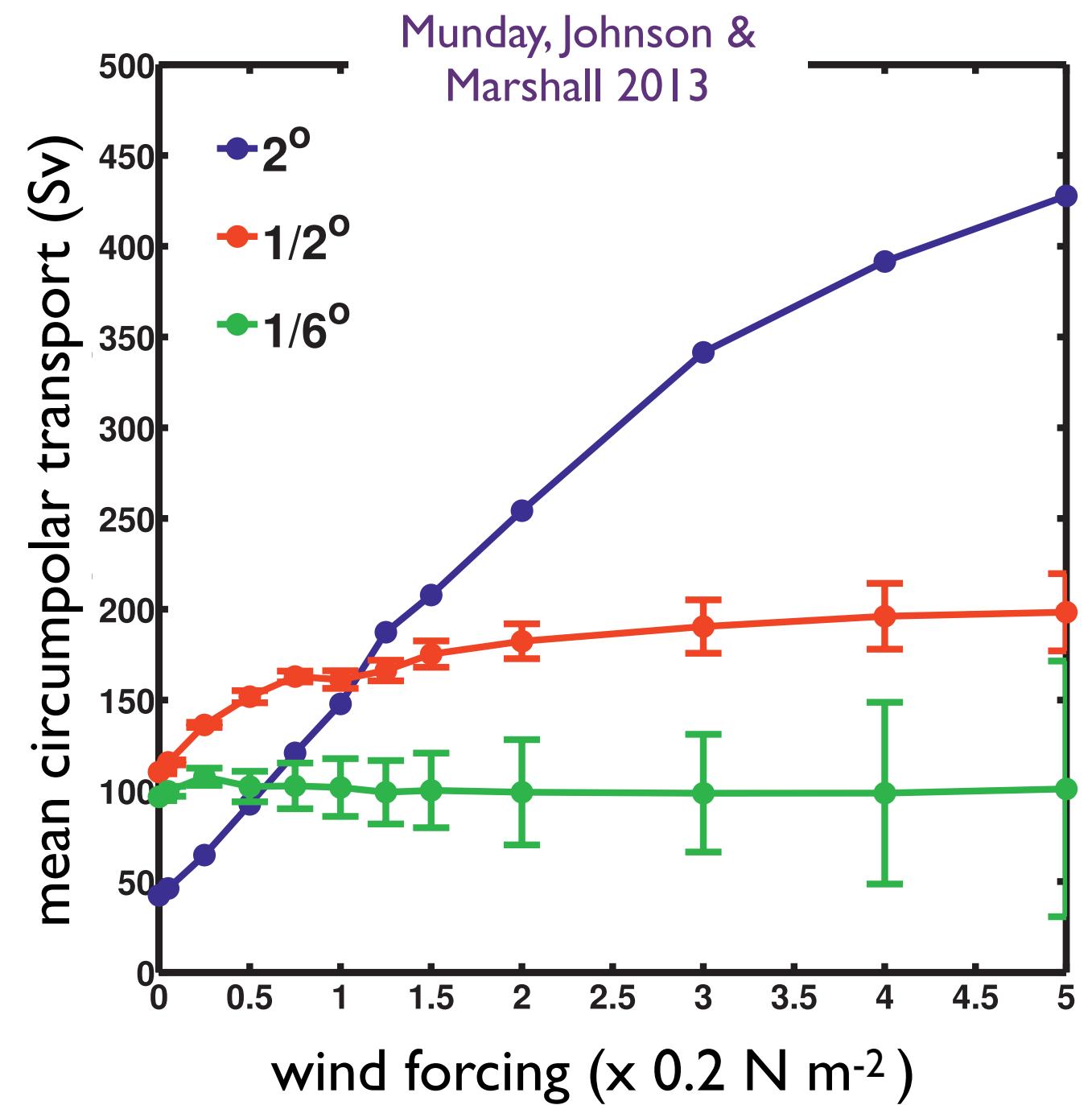
how will the Antarctic Circumpolar Current (ACC) respond?

does doubling the winds imply double ACC the transport?

not always — “eddy saturation”

but first, what is "eddy saturation"?

The *insensitivity* of the total ACC volume transport to wind stress increase.



Eddy saturation was theoretically predicted by Straub (1993) with an entirely baroclinic argument.

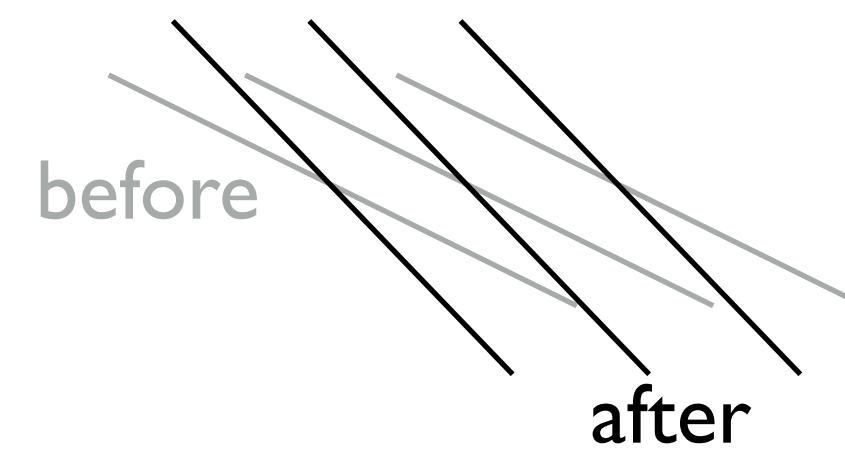
Eddy saturation is seen in eddy-resolving ocean models.
(some hints also in obs.)

higher resolution → eddy saturation “occurs”

[Other examples: Hallberg & Gnanadesikan 2001, Tansley & Marshall 2001, Hallberg & Gnanadesikan 2006, Hogg et al. 2008, Nadeau & Straub 2009, 2012, Farneti et al. 2010, Meredith et al. 2012, Morisson & Hogg 2013, Abernathey & Cessi 2014, Farneti et al. 2015, Nadeau & Ferrari 2015, Marshall et al. 2017.]

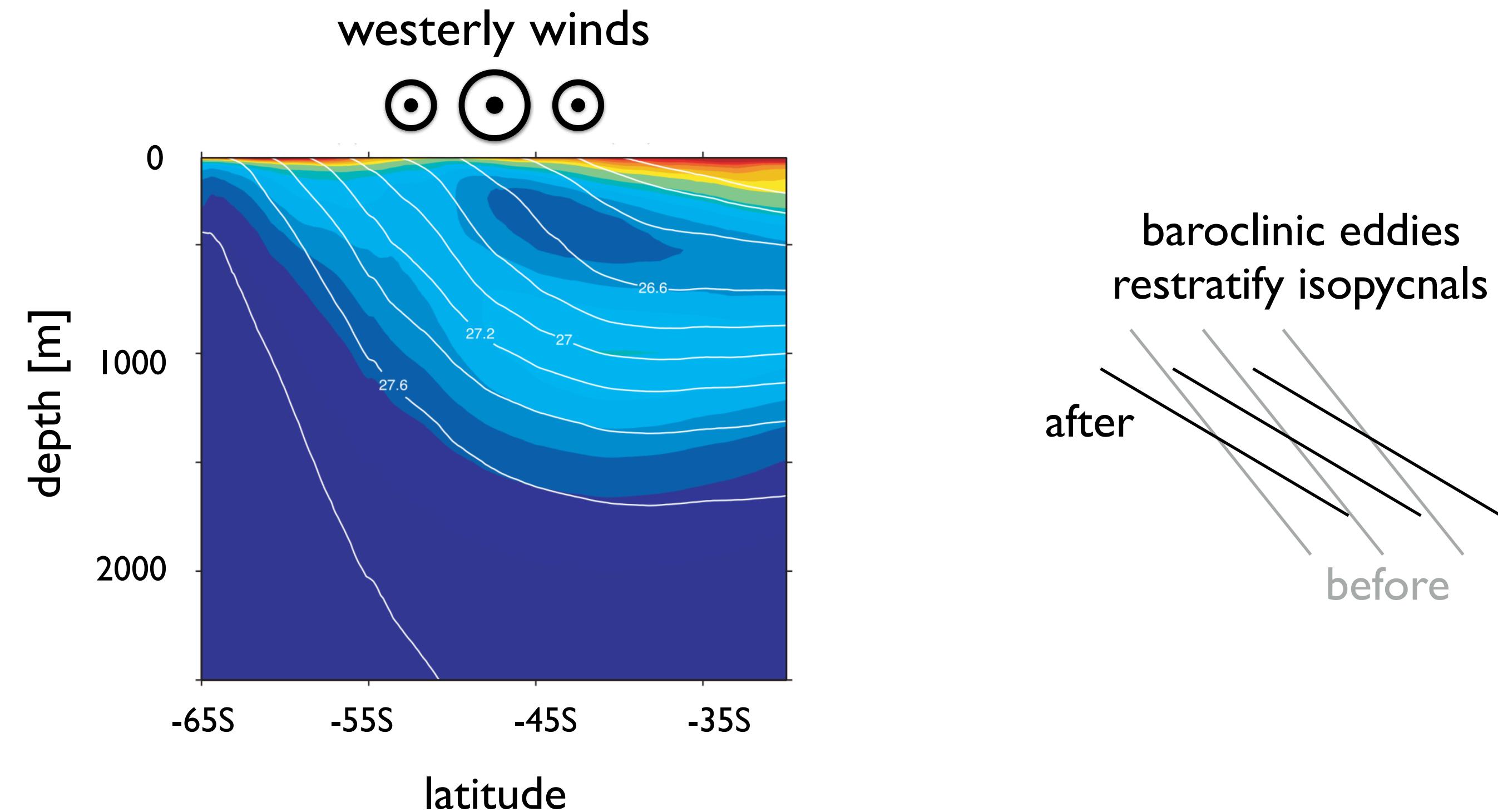
how baroclinic eddies lead to eddy saturation?

wind increase
slopes the isopycnals



The diagram illustrates the effect of wind on isopycnals. It shows two sets of grey lines representing density contours. The top set, labeled 'before', is relatively horizontal. The bottom set, labeled 'after', is tilted downwards from left to right, indicating that the wind has caused the isopycnals to slope.

before after



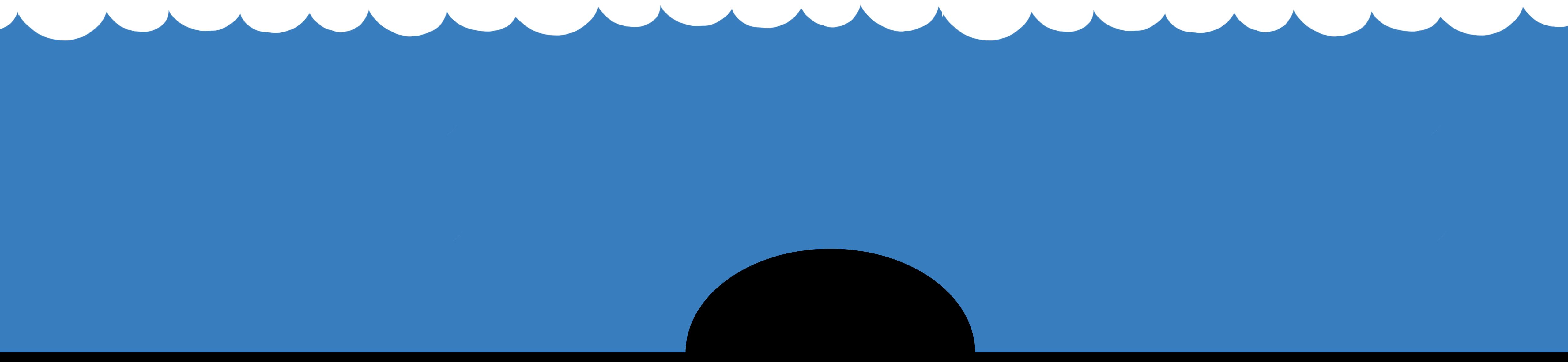
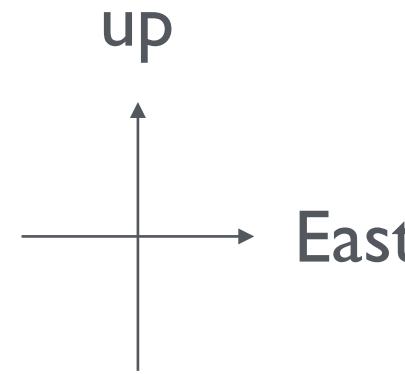
role of bathymetry?

role of bathymetry I

Momentum balance in the Southern Ocean is
"applied at the bottom [...] where ridges lie."

Munk & Palmen (1951)

topographic form stress



role of bathymetry I

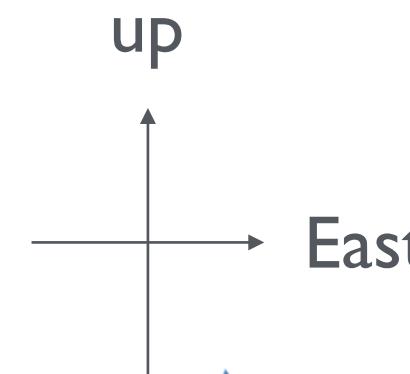
Momentum balance in the Southern Ocean is
"applied at the bottom [...] where ridges lie."

Munk & Palmen (1951)

topographic form stress

wind

τ



U

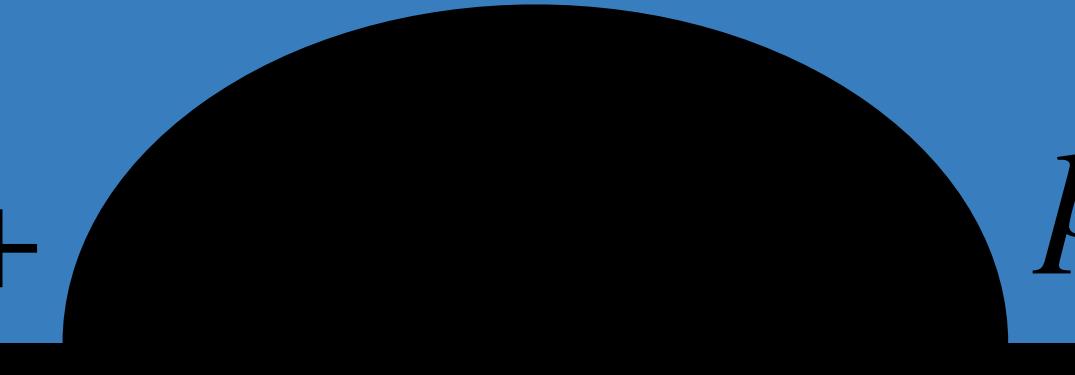


$$F_p = \Delta p/L$$



p_+

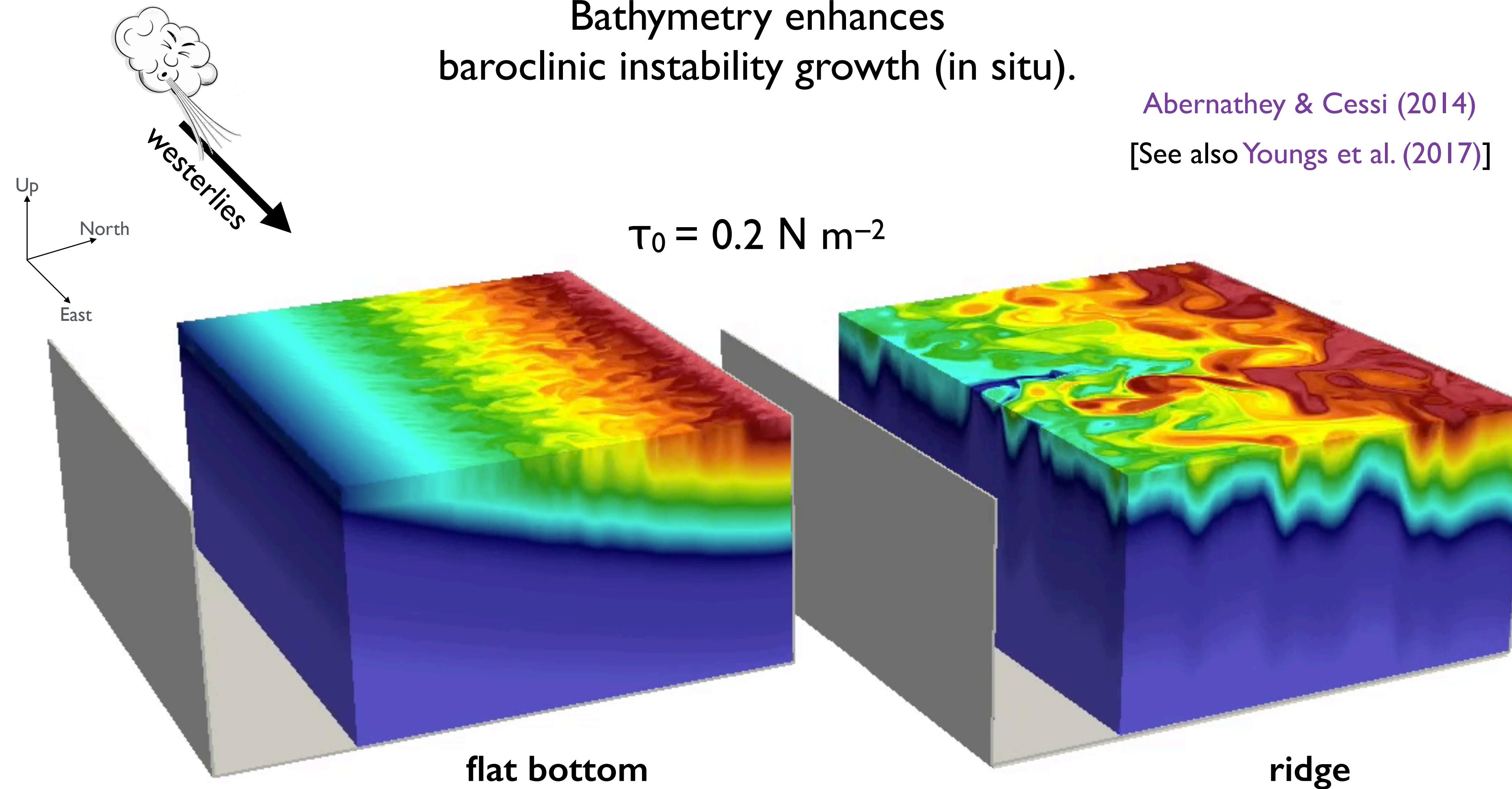
p_-



role of bathymetry II

Bathymetry enhances
baroclinic instability growth (in situ).

Abernathy & Cessi (2014)
[See also Youngs et al. (2017)]



<http://vimeo.com/55486114>

the "thermal-wind" zonal transport

baroclinic interpretation
of eddy saturation



thermal-wind component
dominates ACC trasport

[thermal-wind transport refers to
transport inferred from hydrography
assuming zero flow at the bottom]

cDrake experiment measured
time-mean bottom flows $\mathcal{O}(10\text{cm s}^{-1})$

Donohue et al. 2016

bottom-flow contribution to ACC transport ~25%

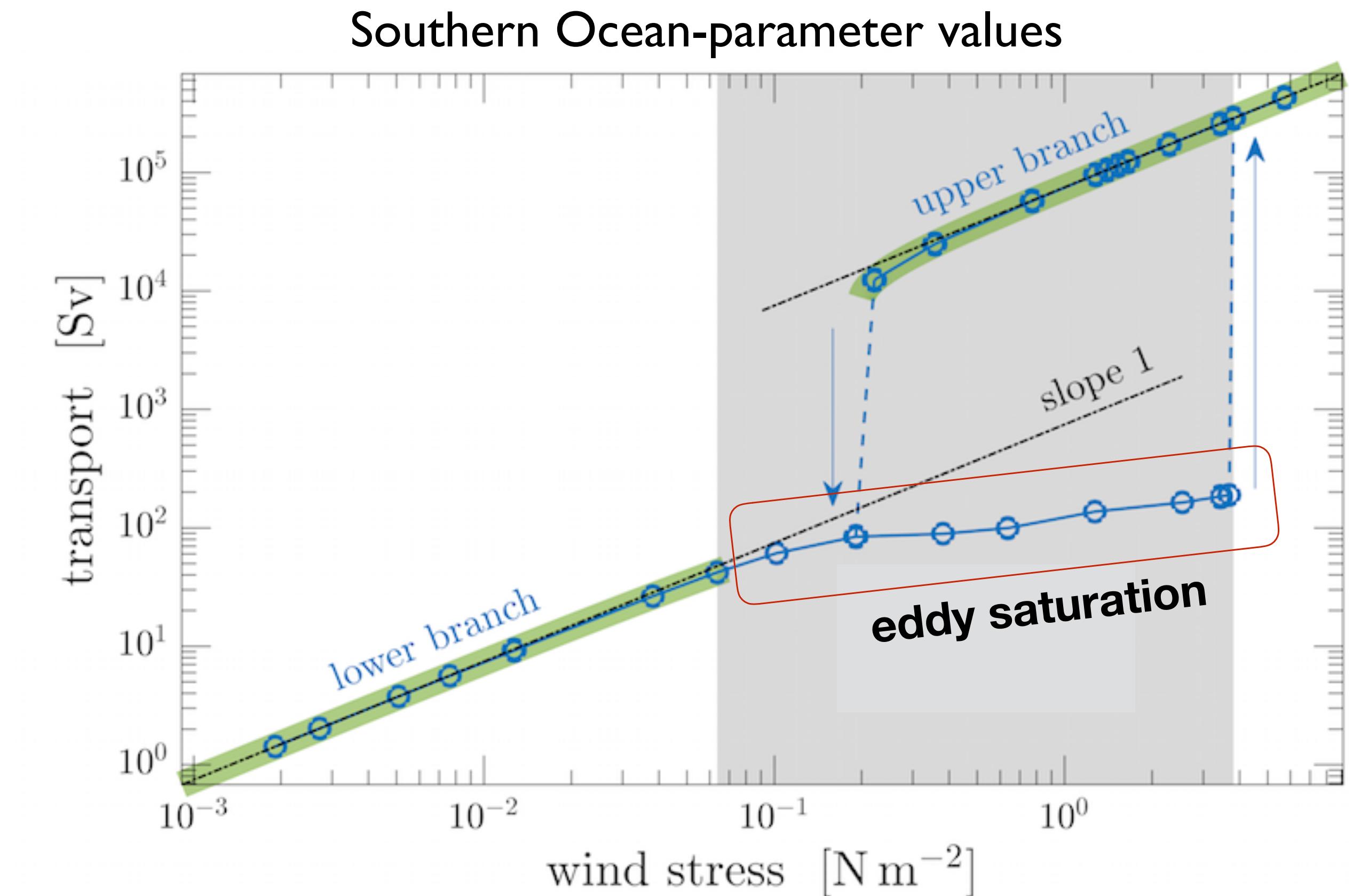


a surprise

Eddy saturation can occur
without baroclinicity
in a homogeneous QG barotropic
model with bathymetry.

Surprising!

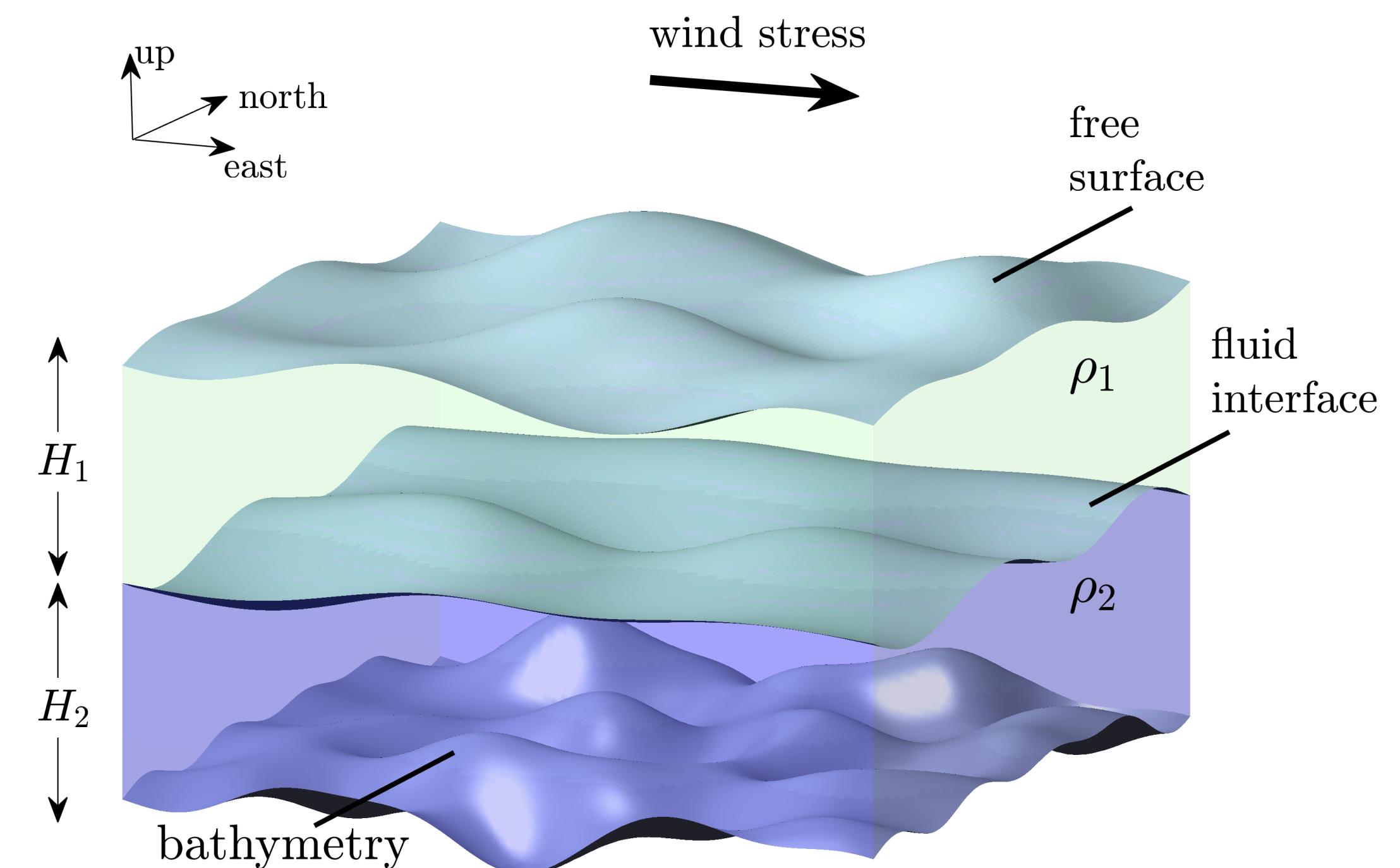
All previous arguments
relied on baroclinic instability
for producing transient eddies.



what's the plan for today

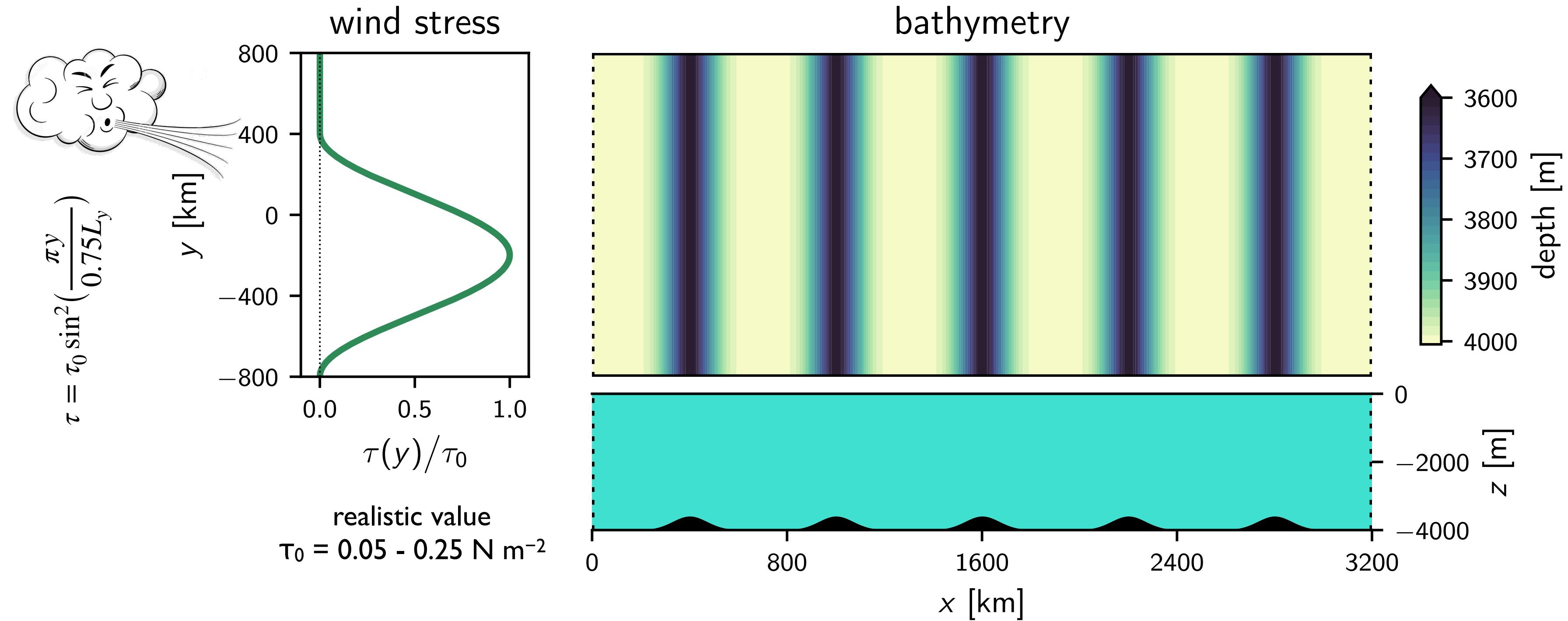
Assess the relative role of
barotropic versus **baroclinic** dynamics
in establishing "eddy saturated" ocean states.

Use an isopycnal layered model
with varying number of fluid layers.



model setup

GFDL's MOM6
primitive equations
in isopycnal coordinates
Boussinesq approximation



β -plane $f = f_0 + \beta y$
zonally re-entrant
1st deformation radius $\approx 19 \text{ km}$
(2nd deformation radius $\approx 10 \text{ km}$)
free surface
free-slip walls
quadratic bottom drag
grid spacing 4 km

bathymetry:
Gaussian ridges
400 m tall, half-width 165 km

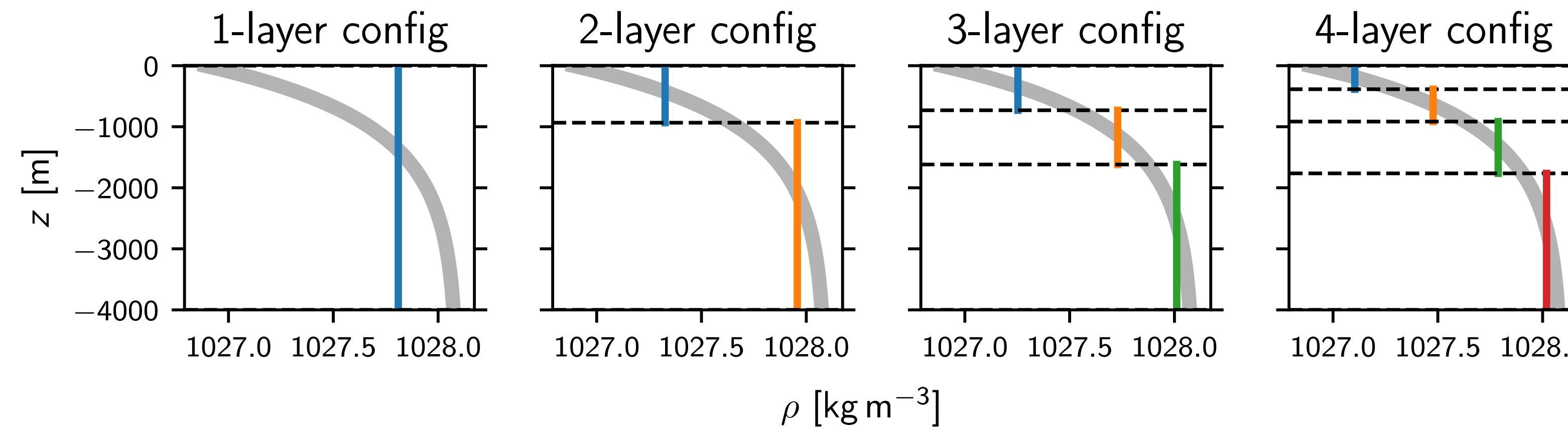
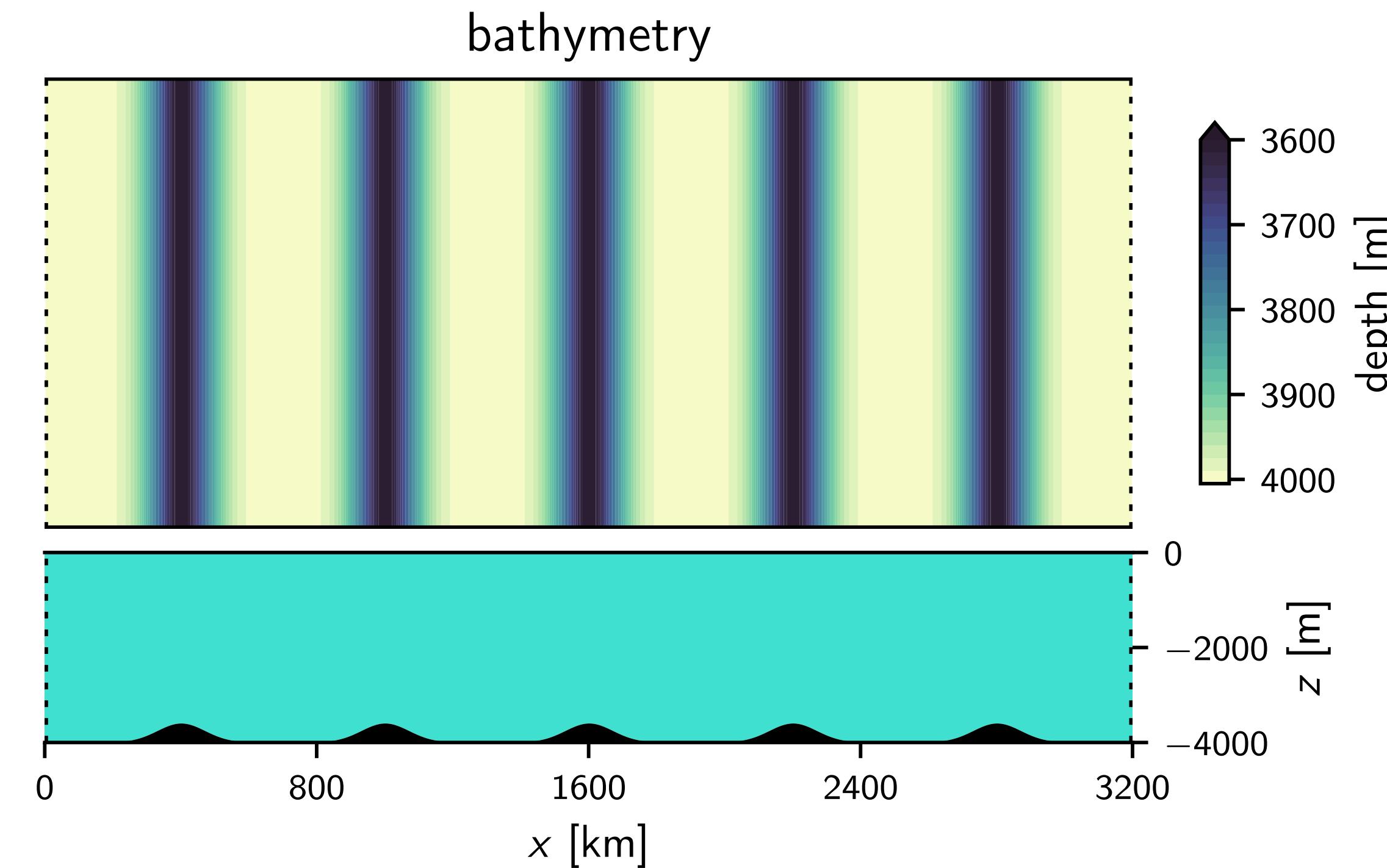
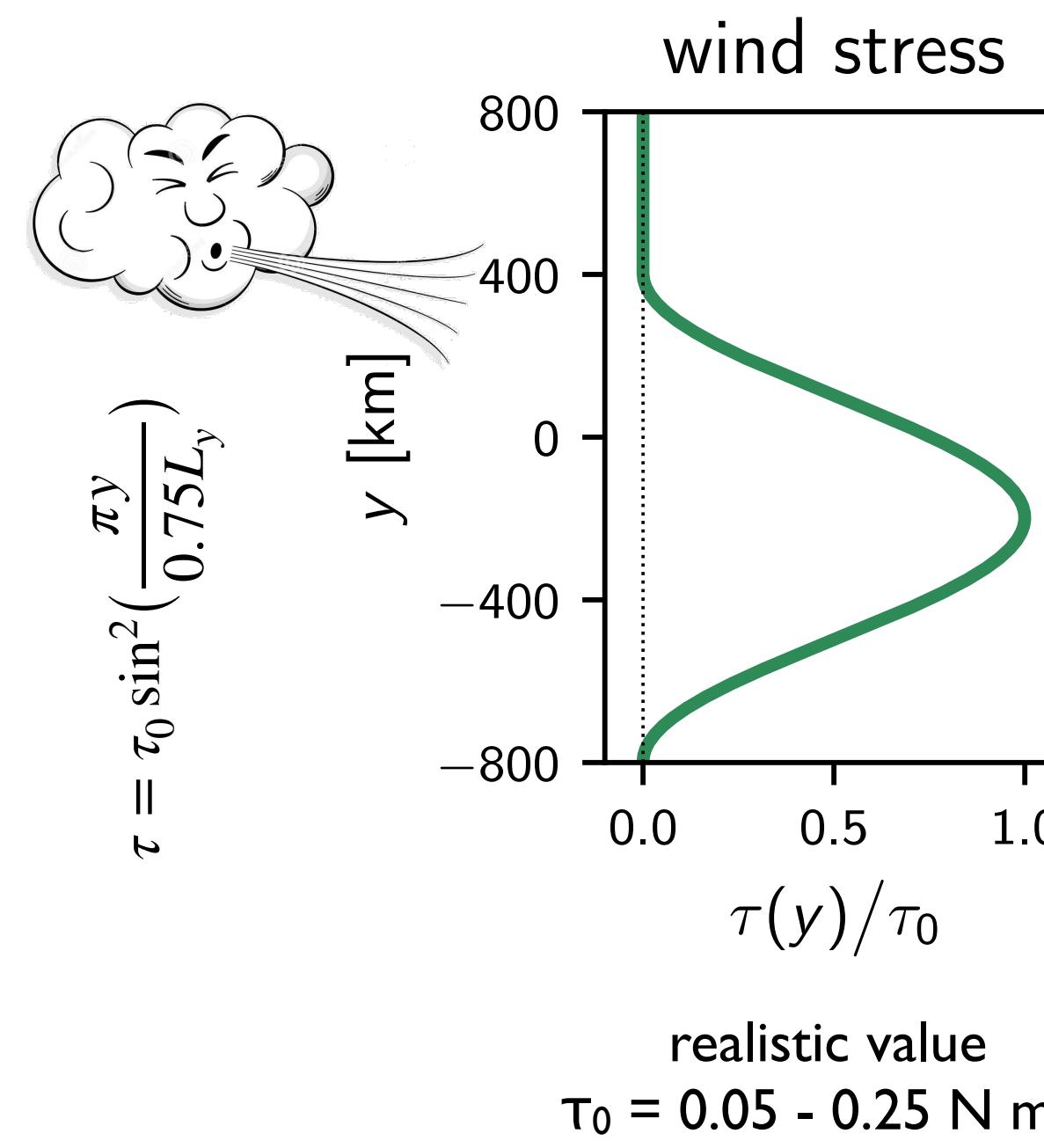
no buoyancy forcing

no diapycnal motions

f/h contours are not fully blocked

model setup

GFDL's MOM6
primitive equations
in isopycnal coordinates
Boussinesq approximation



β -plane $f = f_0 + \beta y$
zonally re-entrant
1st deformation radius $\approx 19 \text{ km}$
(2nd deformation radius $\approx 10 \text{ km}$)
free surface
free-slip walls
quadratic bottom drag
grid spacing 4 km

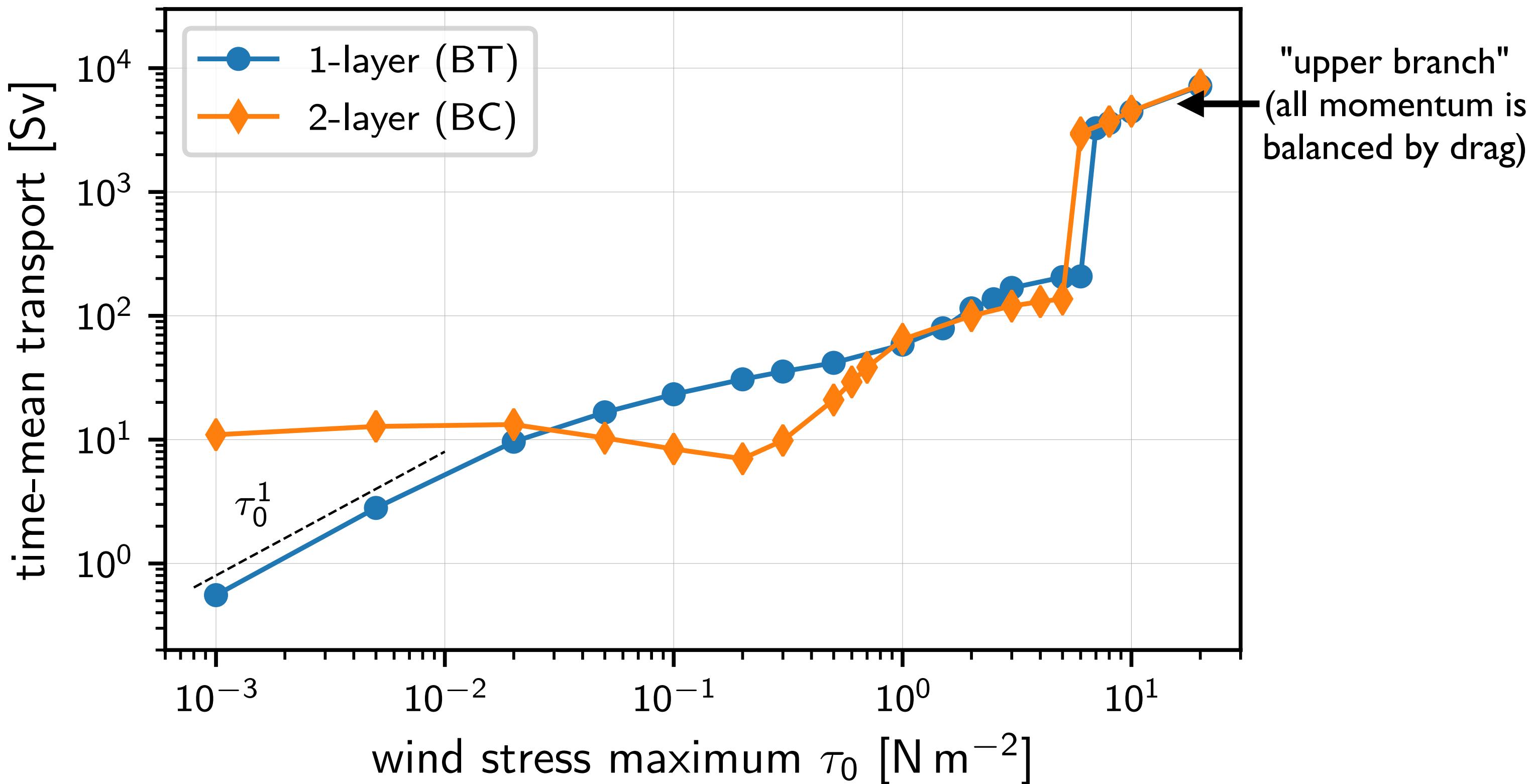
bathymetry:
Gaussian ridges
400 m tall, half-width 165 km

exponential density profile
 $\rho = \rho_0 + \Delta\rho(1 - e^{z/d})$
 $\Delta\rho = 1.2 \text{ kg m}^{-3}, d = 1 \text{ km}$

layered approximations

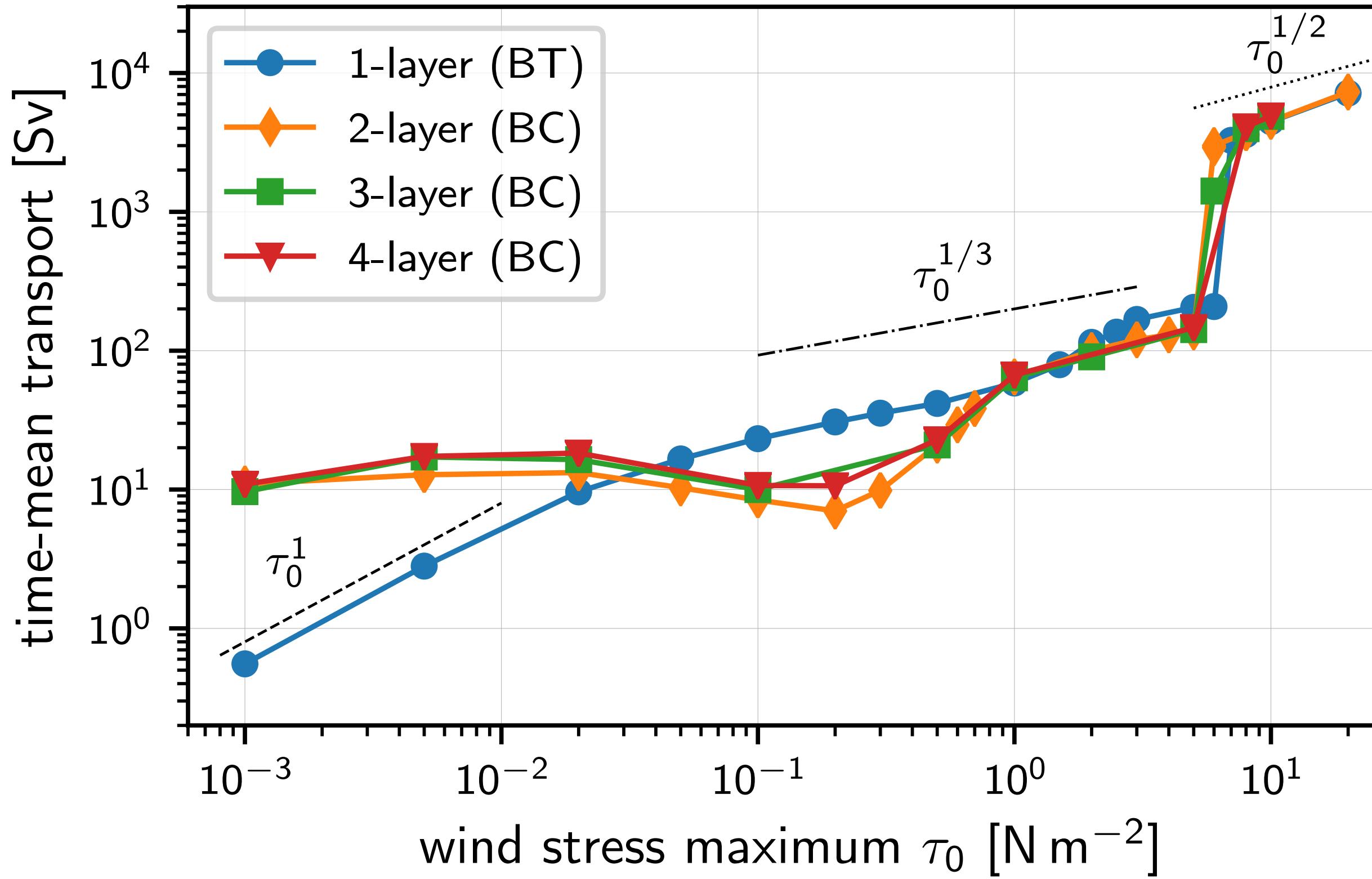
vary the wind stress amplitude τ_0
and see how the time-mean zonal transport changes

mean zonal transport versus wind stress



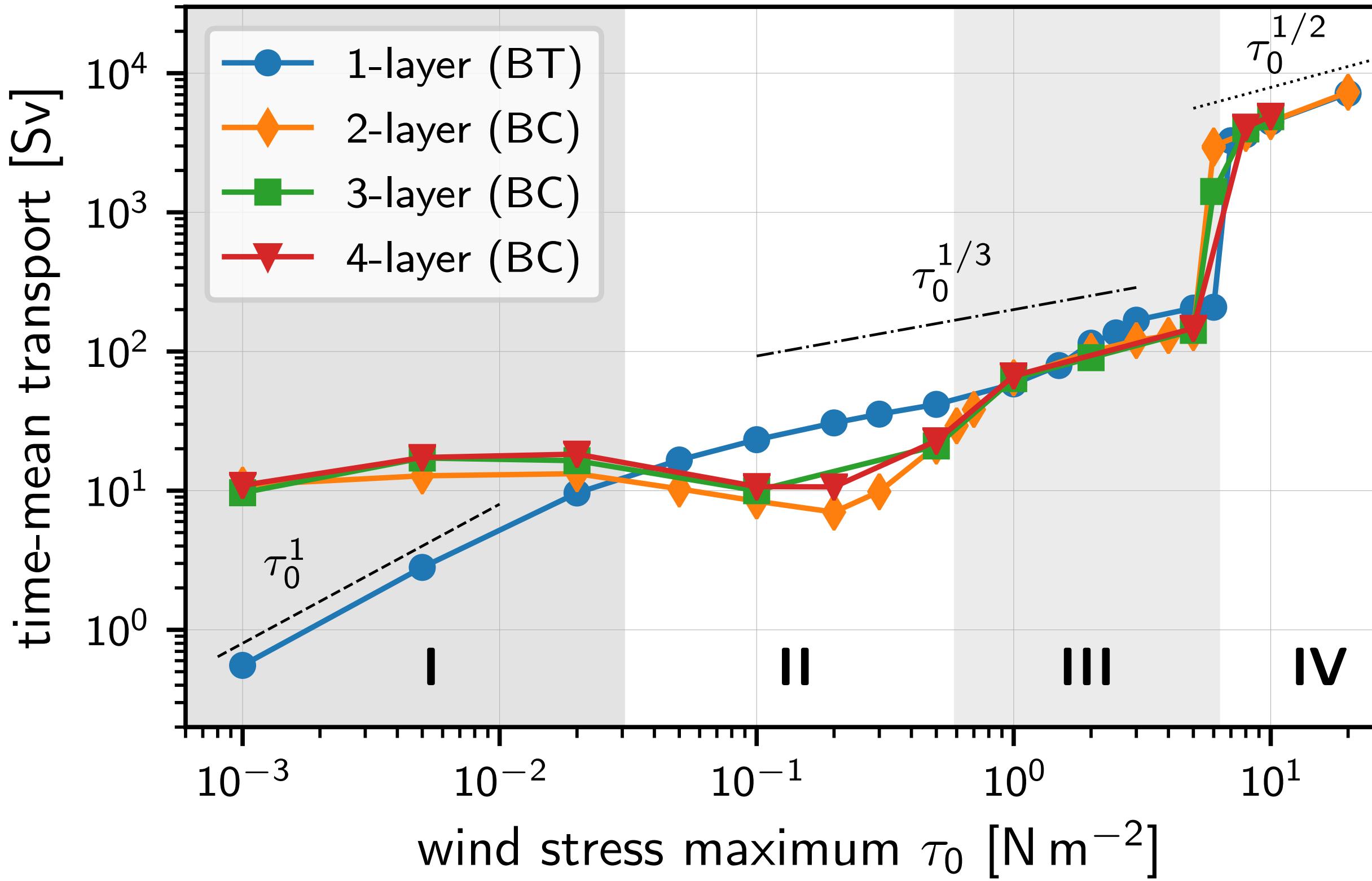
realistic
SO values

mean zonal transport versus wind stress



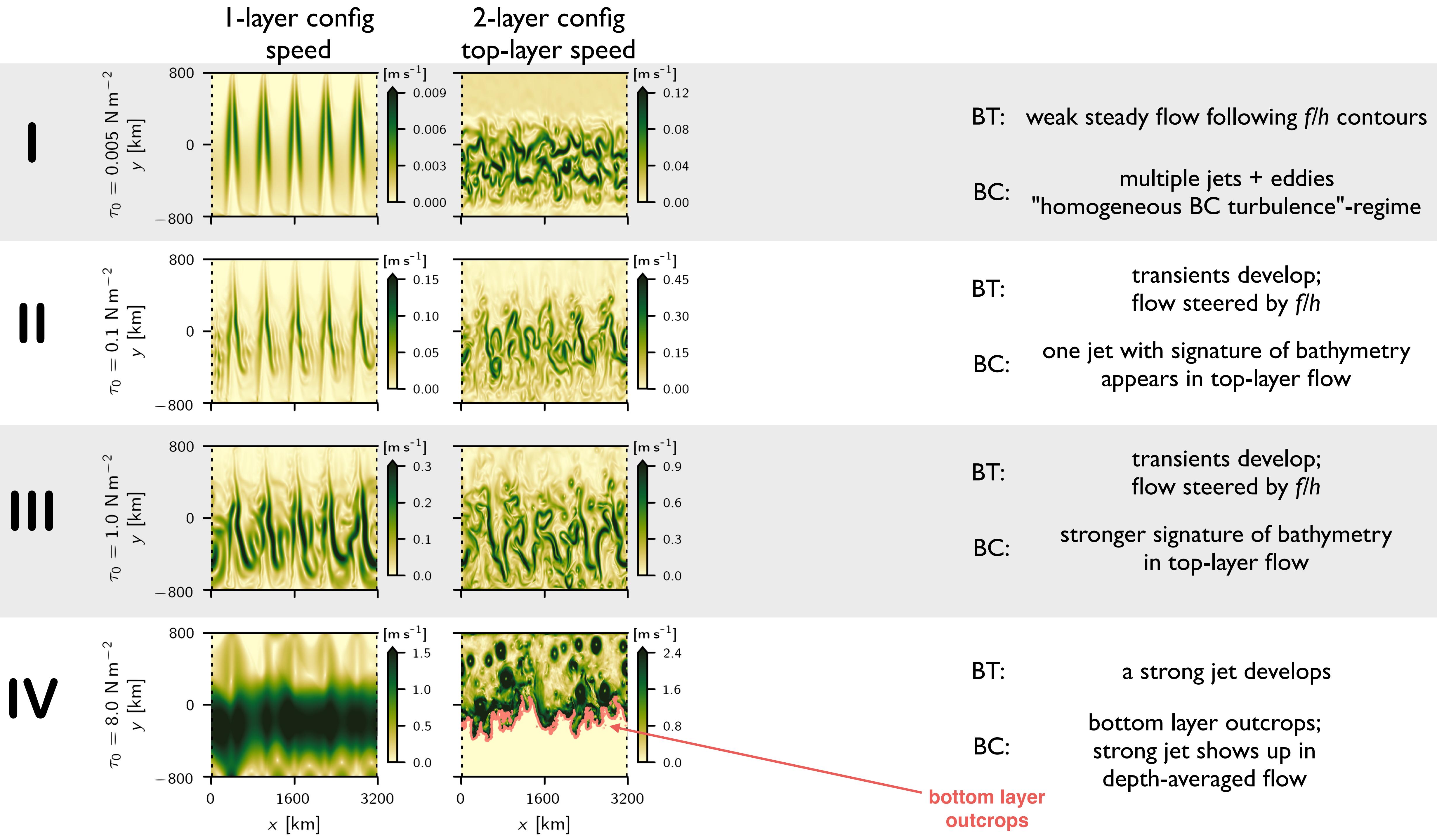
≥ 3 -layer configurations are the same as 2-layers
(as far as the mean zonal transport is concerned)

mean zonal transport versus wind stress

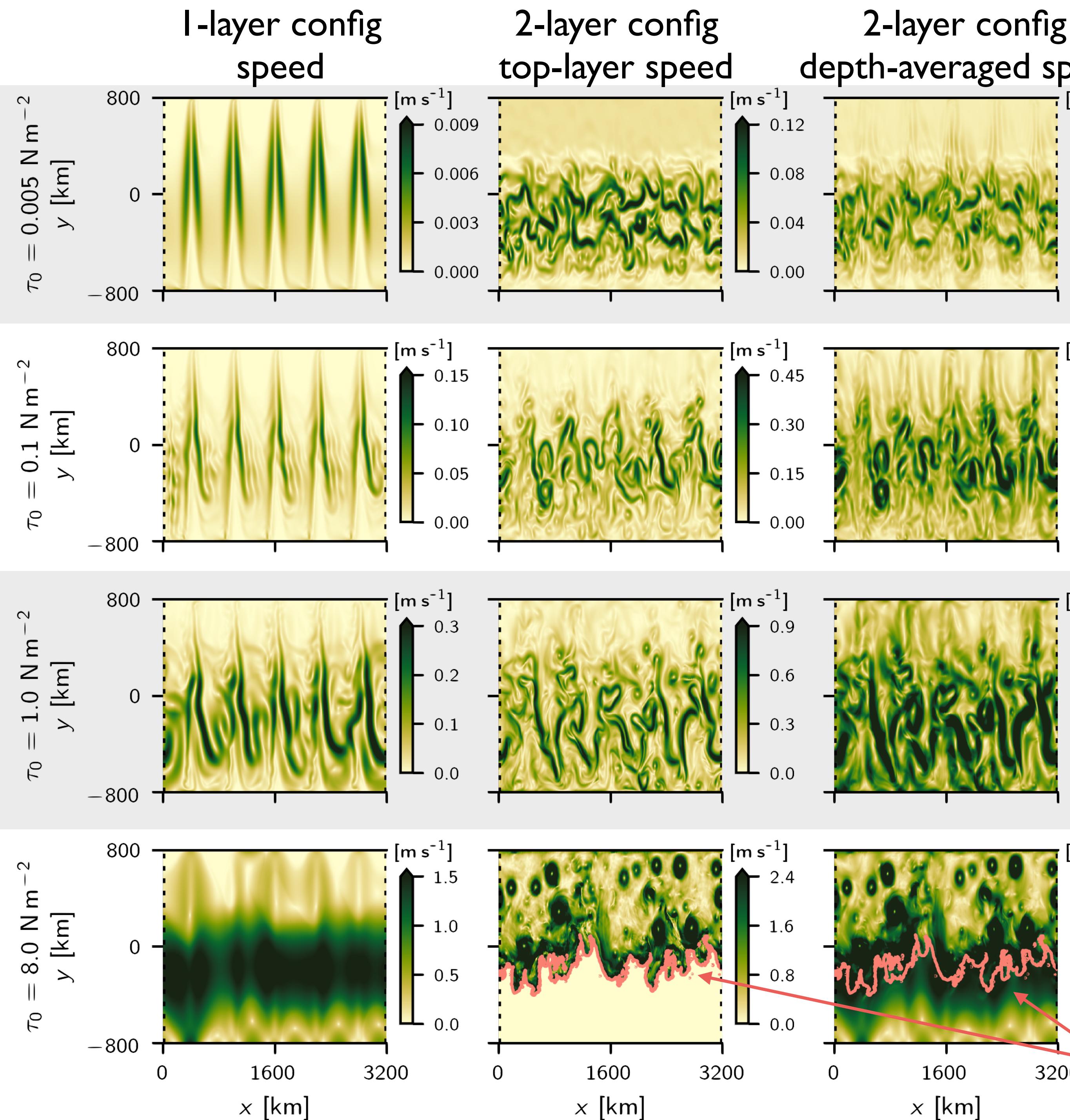


four distinct flow regimes

how does the flow look like
in the four flow regimes?



I
II
III
IV



- BT: weak steady flow following f/h contours
- BC: multiple jets + eddies
"homogeneous BC turbulence"-regime
- BT: transients develop;
flow steered by f/h
- BC: one jet with signature of bathymetry
appears in top-layer flow
- BT: transients develop;
flow steered by f/h
- BC: stronger signature of bathymetry
in top-layer flow
- BT: a strong jet develops
- BC: bottom layer outcrops;
strong jet shows up in
depth-averaged flow
- bottom layer
outcrops**

depth-integrated zonal momentum balance

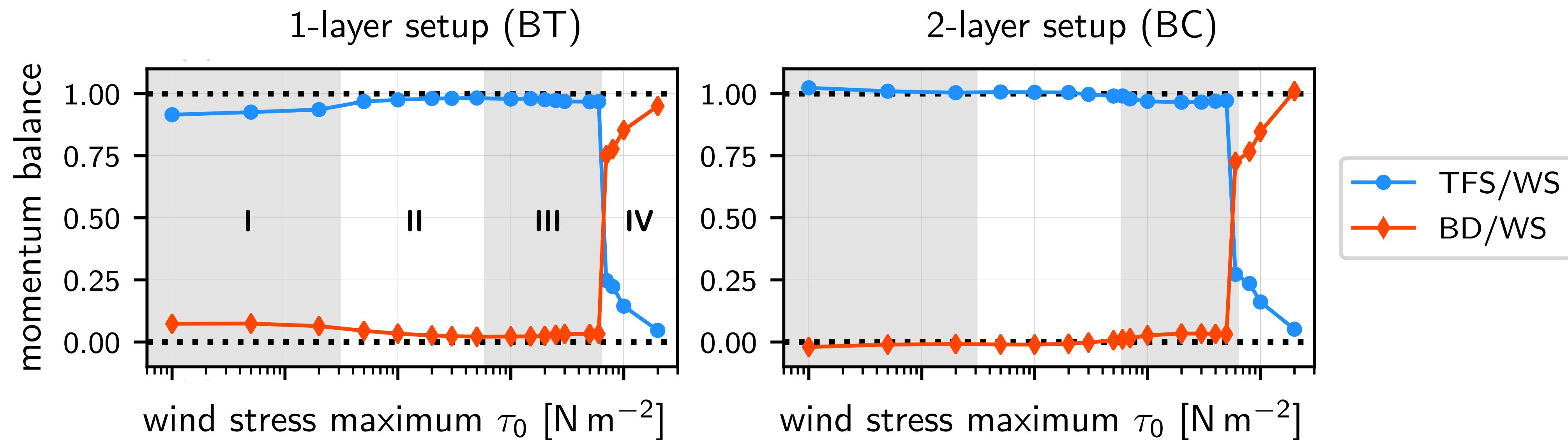
$\langle \rangle$: layer average
 $\overline{}$: time average

$$\langle \tau \rangle = \langle \overline{p_{\text{bot}} \partial_x h_{\text{bot}}} \rangle + \langle \rho_m c_D \overline{u_{\text{bot}} | \mathbf{u}_{\text{bot}} |} \rangle \quad \langle \overline{p_{\text{bot}} \partial_x h_{\text{bot}}} \rangle = \langle \overline{p_{\text{bot}}} \partial_x h_{\text{bot}} \rangle$$

only time-mean flow
contributes to TFS

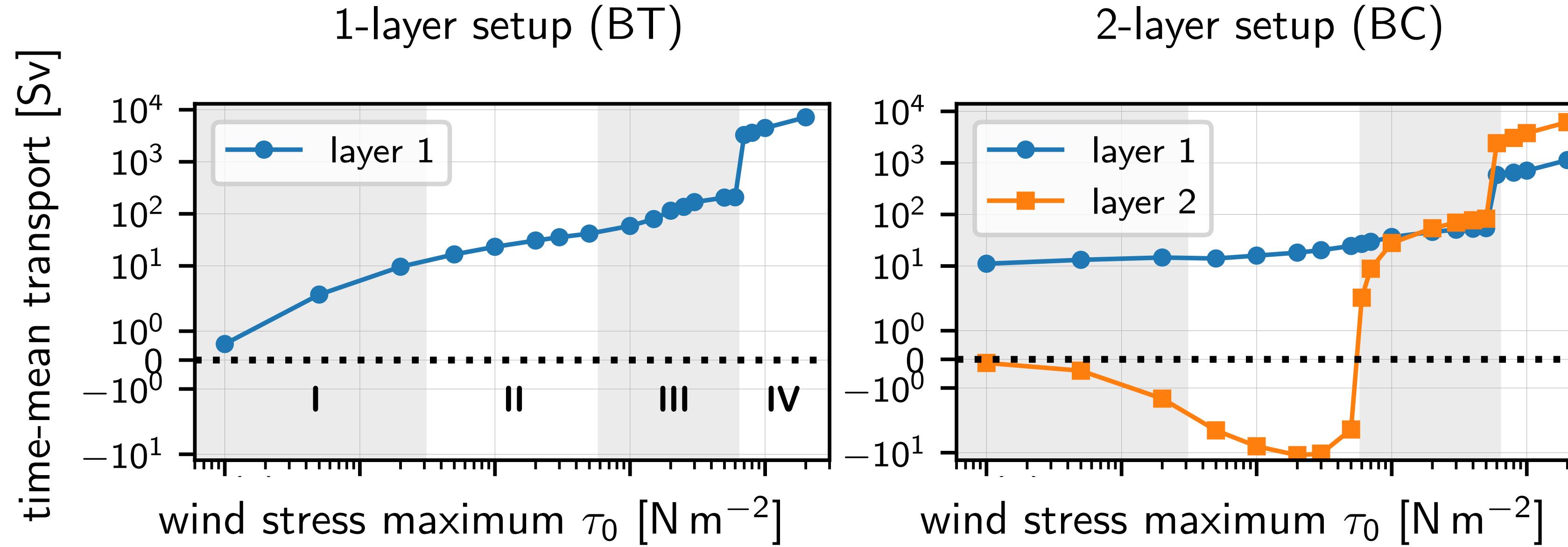
wind stress
(WS)
topographic
form stress
(TFS)

bottom drag
(BD)



Almost *all* momentum is balanced by topographic form stress
(except when flow transitions to "upper branch").

layer-wise transport decomposition



[Westward
bottom-layer flows
also in 3-layer and
4-layer configs.]

Similar bottom-layer westward flows were found by
Treguier & McWilliams (1990) and Stevens & Ivchenko (1997).

Obs. evidence in certain regions of the SO (Cunningham & Barker 1996).

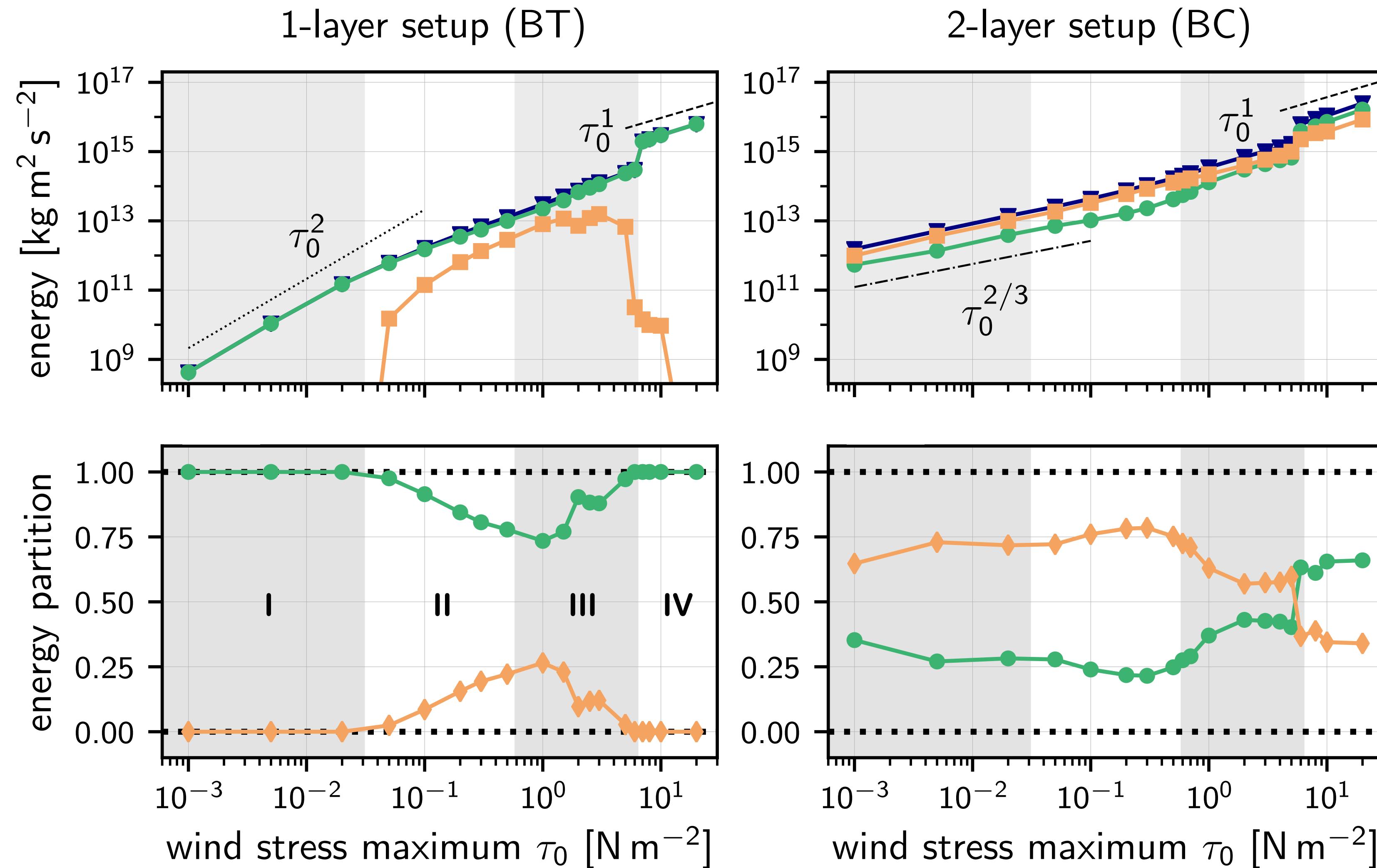
Westward flows are not robust.

Flip to eastward, e.g., for:

- $\beta=0$ [Neptune effect? (Holloway 1987)]
- single-ridge bathymetry

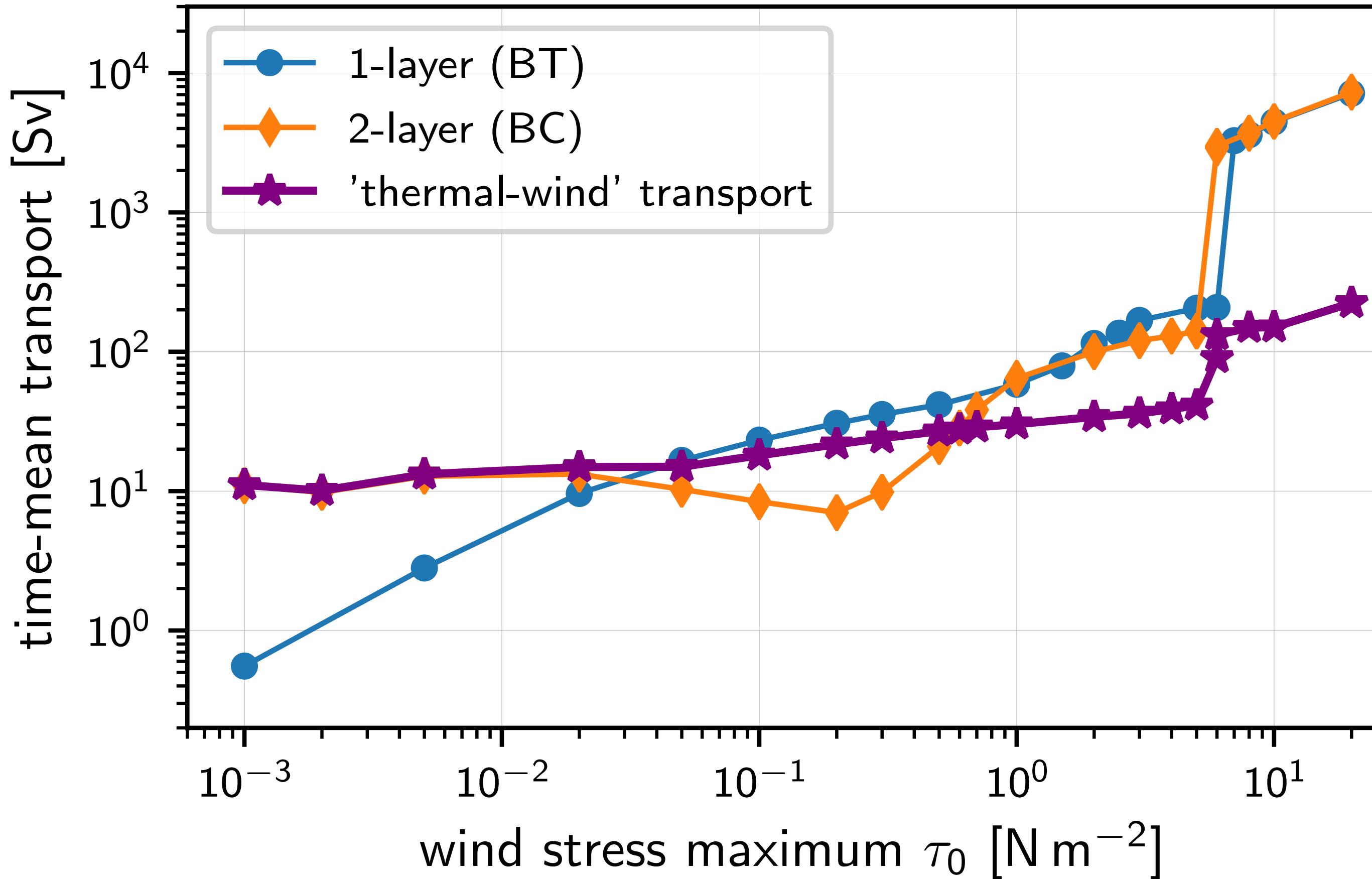
standing-transient kinetic energy decomposition

BT config
has transients
only in **II & III**



Despite the great differences in flow fields,
both **BT** and **BC** configs show same mean zonal transport for regimes **III & IV**.

"thermal-wind"-transport = $\langle \overline{h_1(u_1 - u_2)} \rangle L_y$



"thermal-wind"-transport = $\langle \overline{h_1(u_1 - u_2)} \rangle L_y$

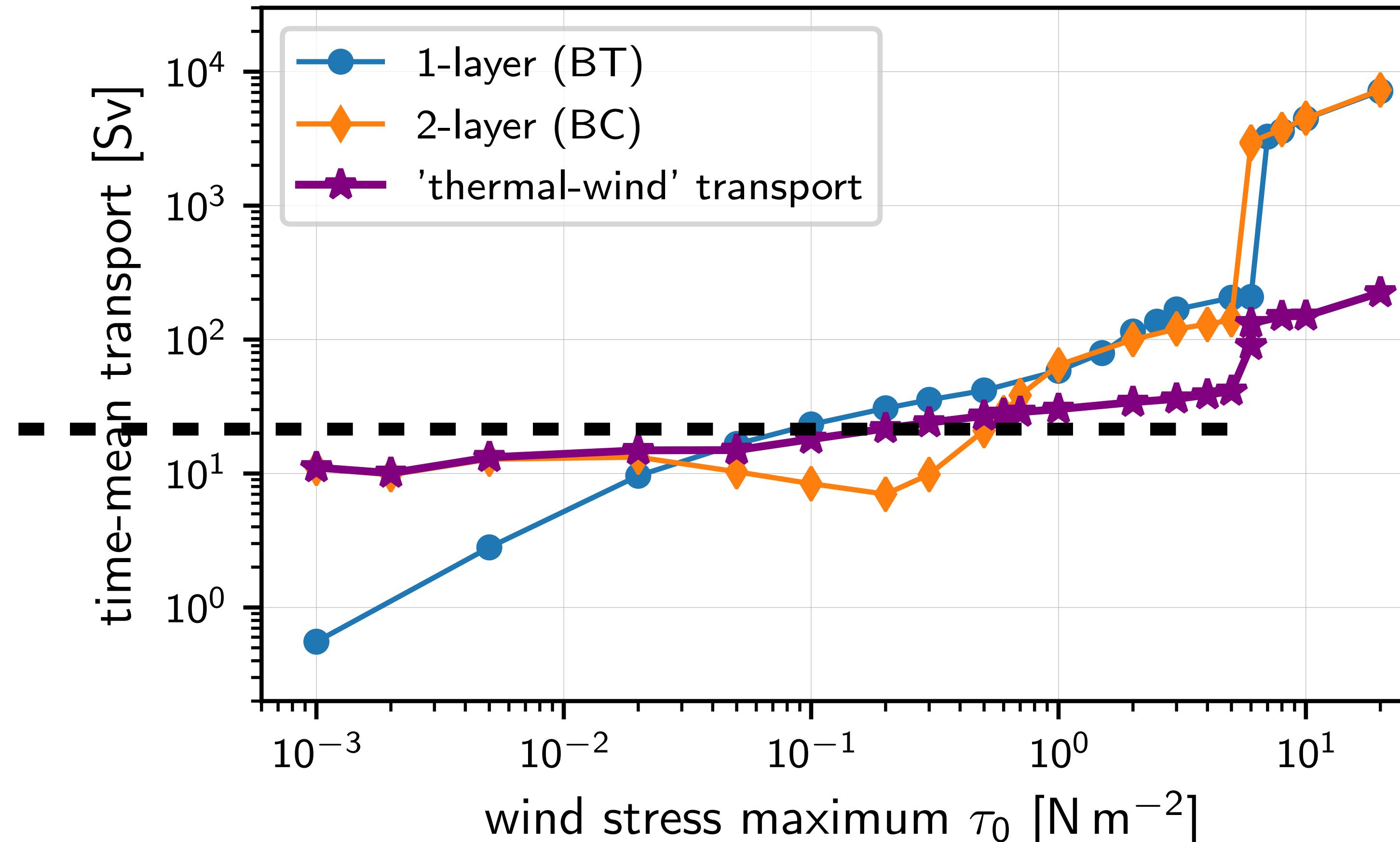
prediction by
Marshall et al. 2017

$$T_{\text{thermal wind}} = \lambda \frac{N}{|f|} \frac{H^2 L_y}{2\alpha_2} \approx 20 \text{ Sv}$$

$$N = \frac{1}{H} \int_{-H}^0 \left(-\frac{g}{\rho_m} \frac{\partial \rho}{\partial z} \right)^{1/2} dz$$

$$\lambda = 1 / (6 \text{ months})$$

$$\alpha_2 = 0.61$$



Coincidence? Probably....

A test would be to vary N and see how the Marshall's prediction performs....

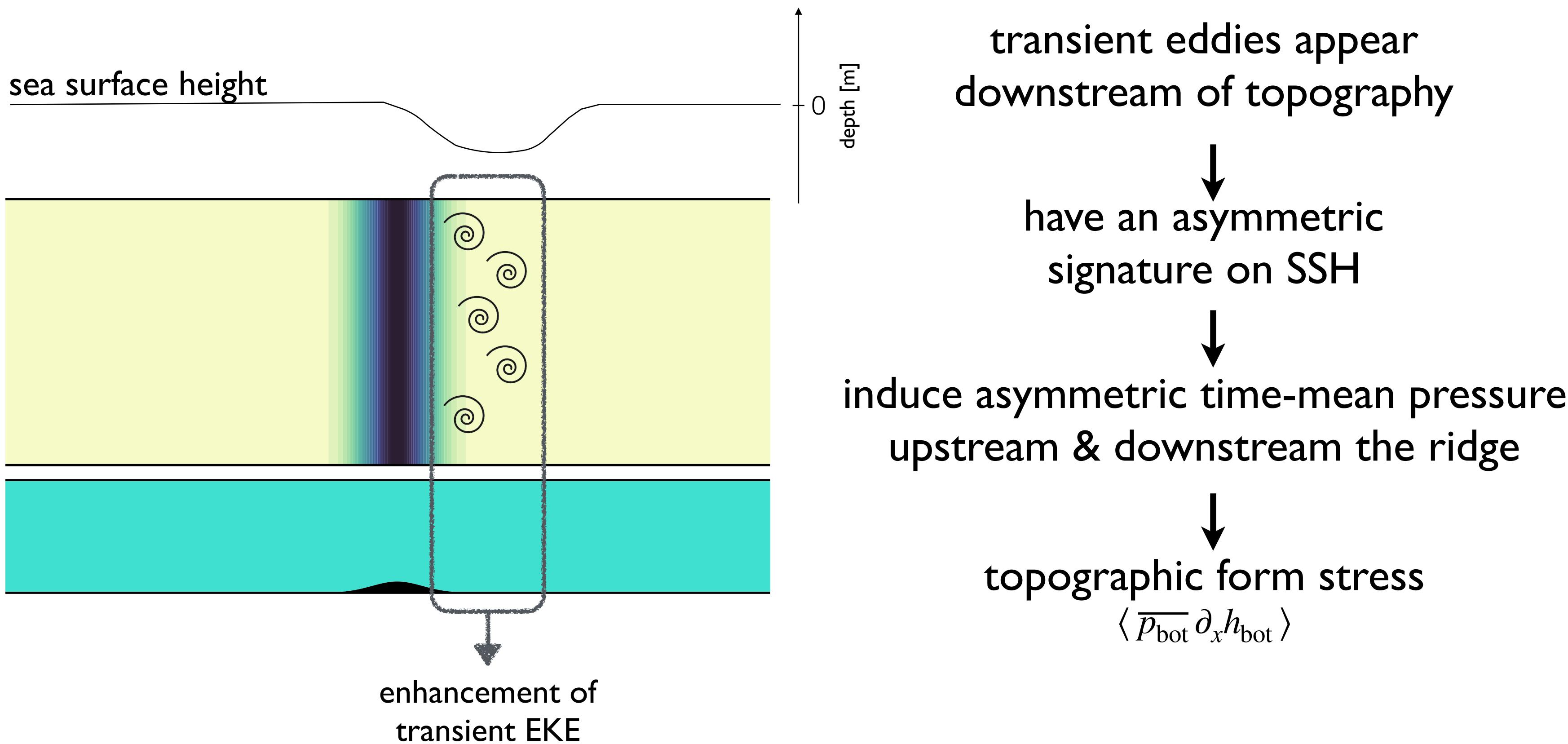
LP Nadeau finds $T_{\text{thermal wind}} \propto N^{3/2}$ (AOFD '19).

$$\langle \overline{p_{\text{bot}} \partial_x h_{\text{bot}}} \rangle = \langle \overline{p_{\text{bot}}} \partial_x h_{\text{bot}} \rangle$$

only standing flow contributes to
mean topographic form stress

how transients affect
topographic form stress?

how transients lead to time-mean topographic form stress?



[As also described by Youngs et al. 2017.]

take home messages

when transient eddies exist (both in **barotropic** or **baroclinic** configs)
the mean zonal transport becomes eddy saturated
[transport is much less sensitive to wind stress increase]

proposal: eddy saturation occurs due to
transient eddies shaping the standing flow
to produce topographic form stress that balances the wind stress
(*regardless* of the process from which transient eddies originate)

our results show that the (oftentimes ignored) barotropic flow-component
plays an important role in setting up the ACC transport
[in agreement with recent obs. evidence, e.g., Thompson & Naveira Garabato 2014,
Peña-Molino et al. 2014, Donohue et al. 2016 (cDrake exp)]

thank you

Constantinou and Hogg (2019). Eddy saturation of the Southern Ocean:
a baroclinic versus barotropic perspective. (in review, arXiv:1906.08442)