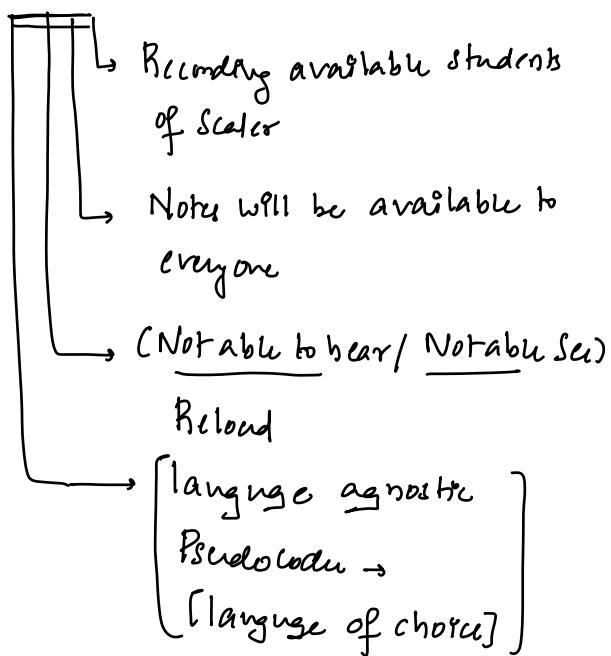


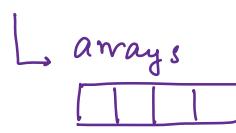
N. Satya Sai Sir Rama krishna → 2 3/4 years

Today's Content

- Trees Intro
- Naming Convention
- Tree Traversal
- Basic Tree Problems
- LCA
- $\frac{1}{2}$ Adv



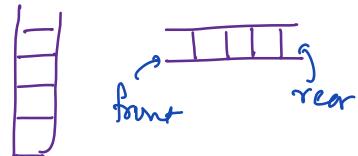
Linear:



linked list

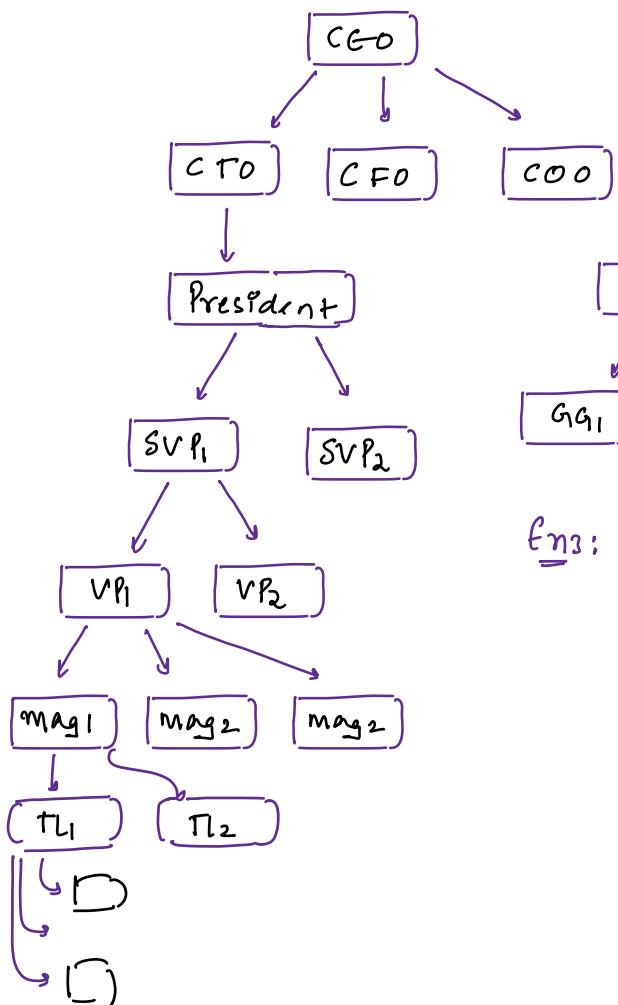


stacks & queues

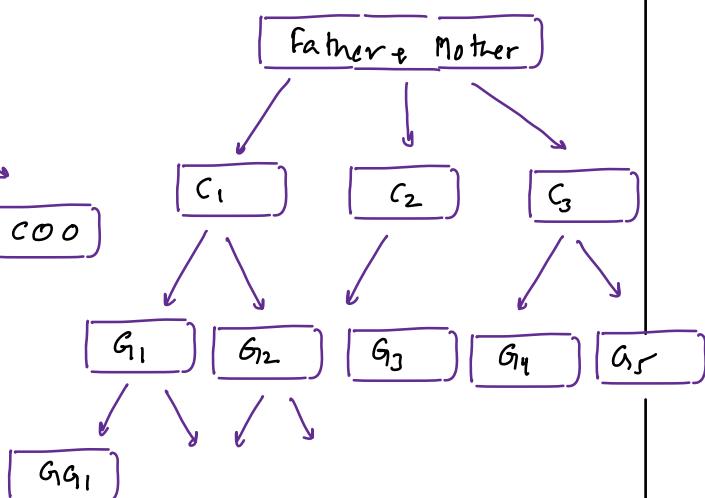


Hierarchical Data

Eg1: Company organisation

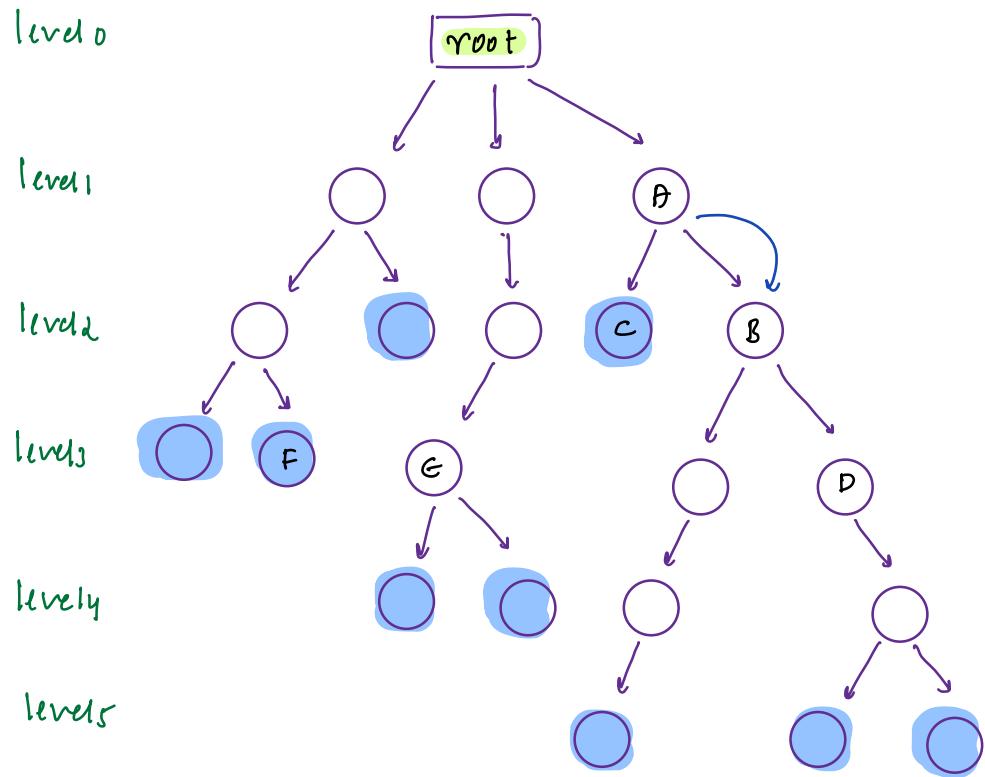


Eg2: Family tree



Eg3:





Naming

$A \rightarrow B$: A is parent of B , B is child of A

$A \rightarrow D$: A is ancestor of D , D is descendent of A

$B \rightarrow C$: siblings

F, E, D : nodes at same level

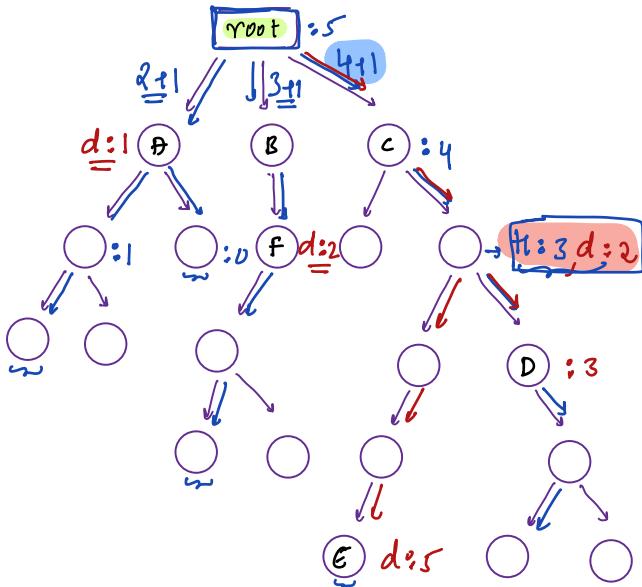
root : node without parent

leaf : node without child

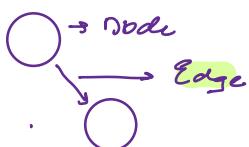
True : other than root, every node only single parent

height(Node):

$\left[\begin{array}{l} \text{length of longest path} \\ \text{from node, to any of} \\ \text{its descendant leaf} \\ \text{nodes} \end{array} \right]$



Note: Path is calculated
Based on no. of edges



$$h(A) : 2$$

$$h(B) : 3$$

$$h(C) : 4$$

$$h(D) : 2$$

$$h(E)$$

$$h(F)$$

obs1:

$$h(\text{node}) = 1 + \max(\text{height of child node})$$

obs2:

$$h(\text{leaf Node}) = 0$$

depth(Node):

length of path from
root to the node

$$d(A) : 1$$

$$d(F) : 2$$

$$d(E) : 5$$

$$d(D) :$$

root

$$\underline{\text{obs:}} \quad \text{depth}(\text{node}) = d$$

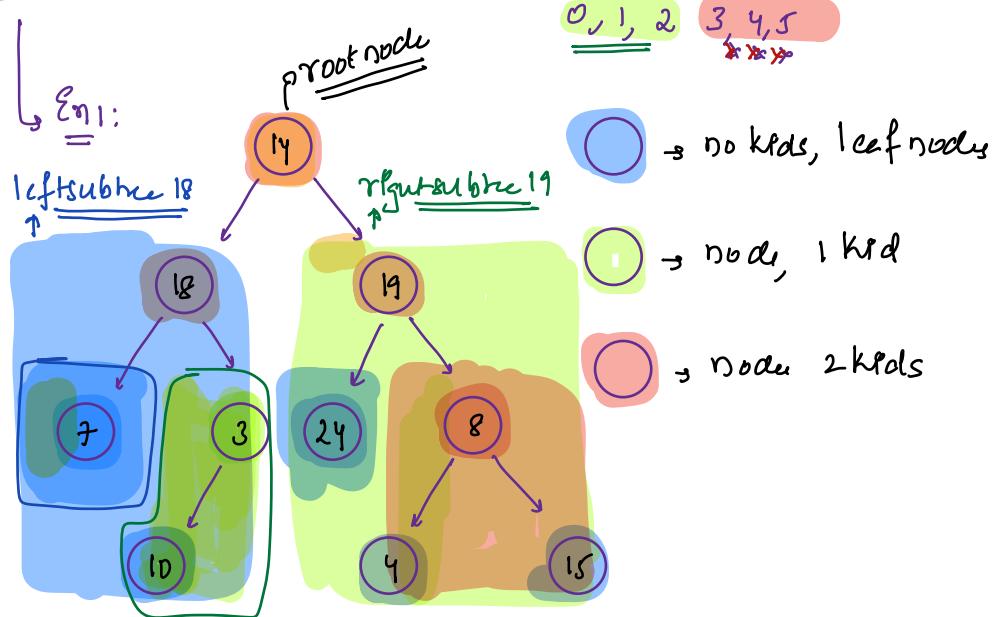
$$\text{depth}(\text{child node}) = d+1$$

$$\underline{\text{obs2:}} \quad \text{depth}(\text{root}) = 0$$

$$\underline{\text{obs:}} \quad \text{height}(\text{node}) = \text{depth}(\text{node})$$

$$\text{depth} = d+1$$

Binary Tree : Every node can at max have 2 children



Class node {

 int d; // data

 node left; //
 node right; //

[object reference of node class, can hold
address of node object]

 node(int n){

 d = n

 left = null

 right = null

 Node root = new Node(50)

 → data Node = 50

If we have root
node we can go
to all nodes

#ad1		
left #ad2	data 50	right #ad3
#ad4		

#ad2		
left #ad5	data 80	right null
#ad6		

#ad3		
left #ad6	data 40	right #ad7
#ad8		

#ad4		
left null	data 60	right null

#ad6		
left null	data 90	right null

#ad5		
left null	data 70	right null

Tree Traversals:

↳ (given root node)

→ Tree Traversals = { iterate in complete tree }

1) Preorder

2) Inorder

3) Postorder

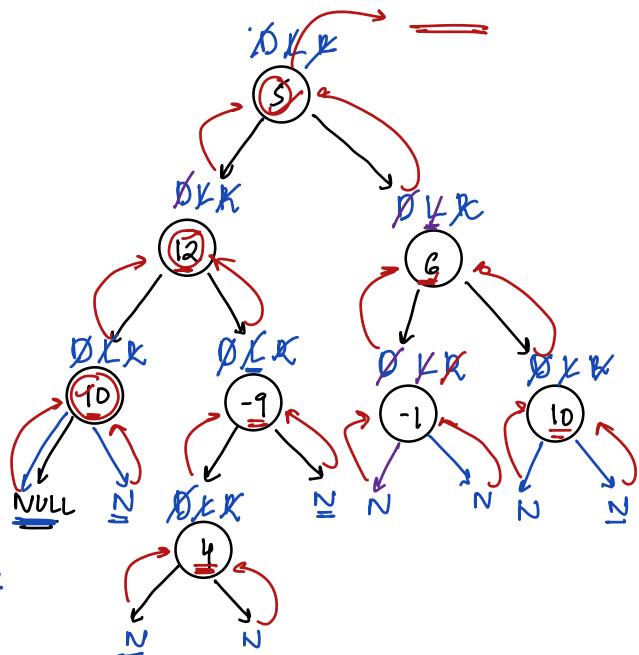
Tree Traversals :

→ Preorder : D L R

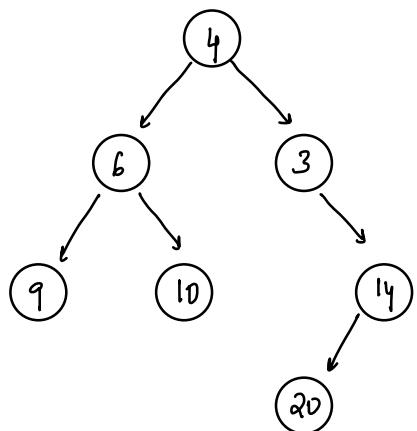
Step1 : Print root data

Step2 : Go to left subtree
↳ print entire leftsubtree
In preorder

Step3 : Go to rightsubtree
↳ print entire rightsubtree
In preorder



Output: 5 12 10 -9 ↳ 6 -1 10



Preorder: 4 6 9 10 3 14 20

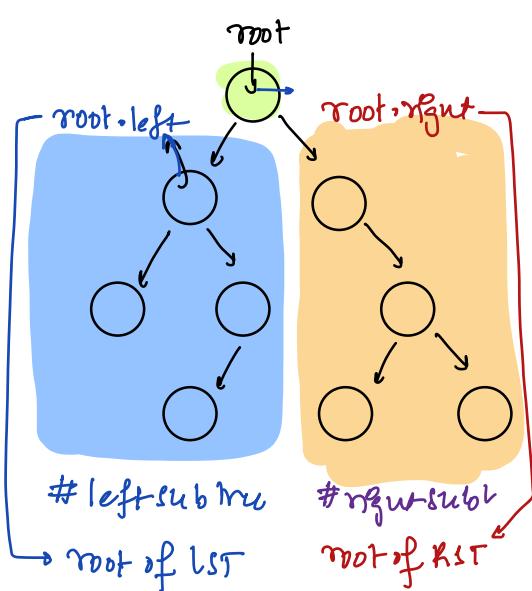
preorder:

Pseudo Code:

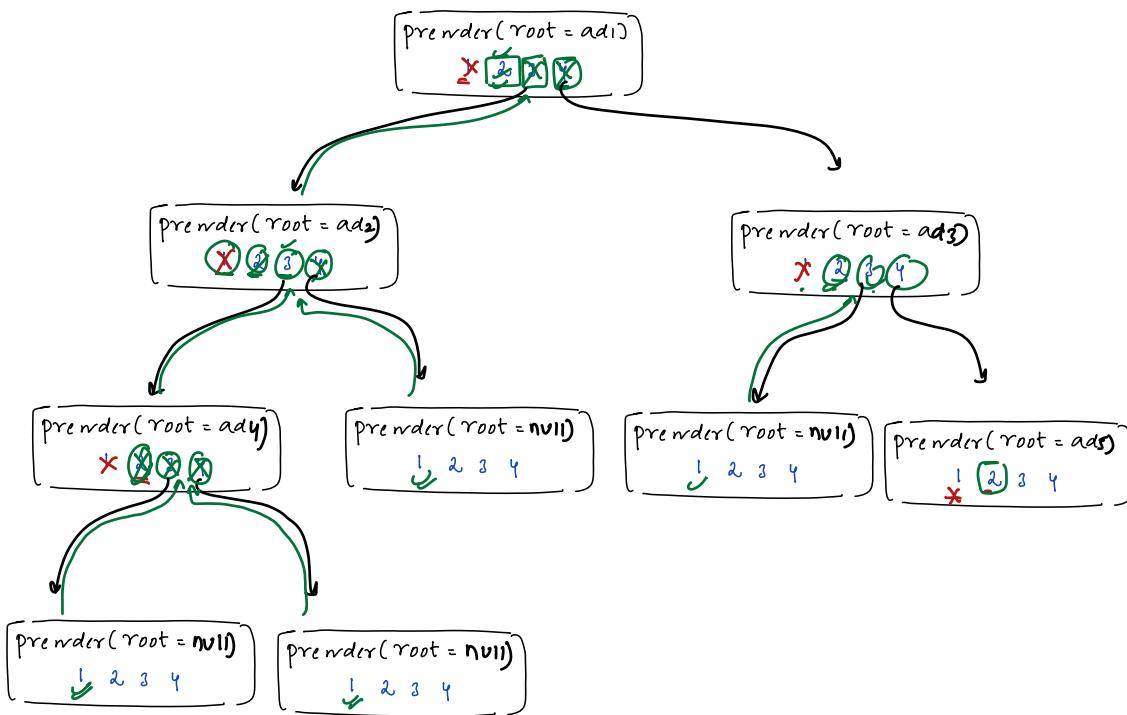
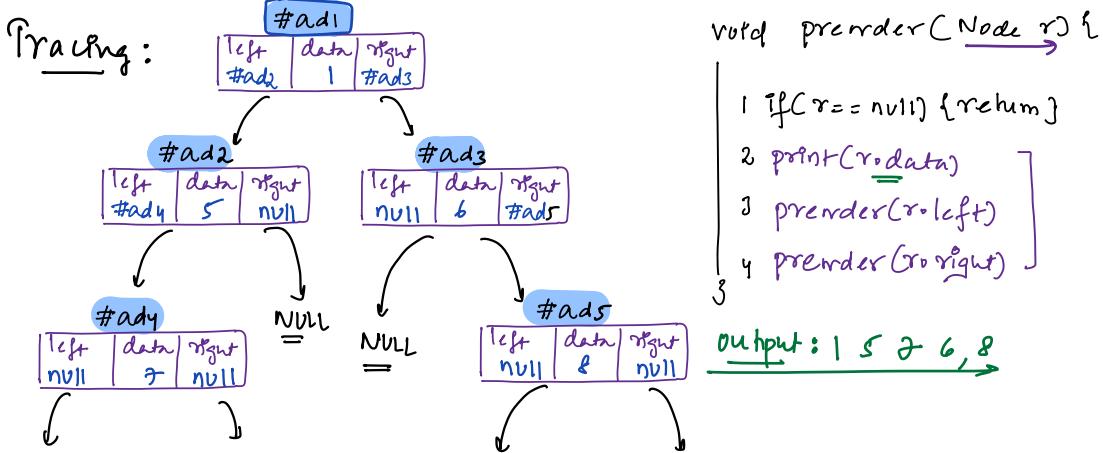
Given root node, print entire in pre-order

```
void preOrder(Node r) {  
    ↗ root node
```

```
    1 if(r==null) {return}  
    2 print(r.data)  
    3 preOrder(r.left) // print preOrder of LST  
    4 preOrder(r.right) // print preOrder of RST  
    ↘
```



Pseudo Code:



// Note: When a function is completely enclosed,
it will return blank.

Tree Problems:

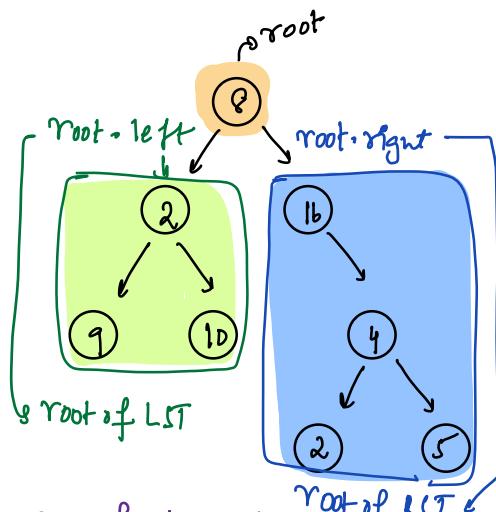
a) $\text{Size}(\text{Node root})$ ✓

b) $\text{Sum}(\text{Node root})$ ✓

Ass: Given root node, return size of Tree

$$\text{Size}(\text{root}) = \underbrace{\text{Size of LST}}_{\text{LST}} + \text{Size of RST} + 1$$

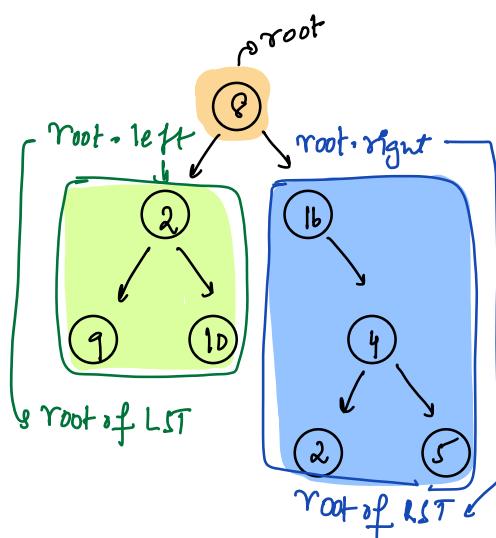
```
int Size (Node root)
{
    if (root == null) { return 0 }
    int l = Size (root.left)
    int r = Size (root.right)
    return l+r+1
}
```



Ass: Given root node, it will return sum of all nodes

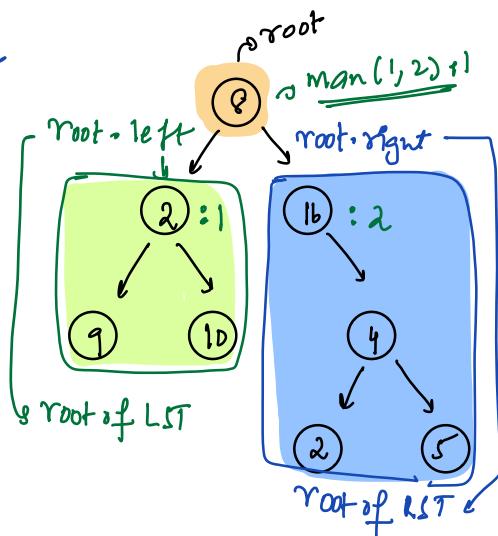
$$\text{Sum}(\text{root}) = \text{sum of node LST} + \text{sum of node RST} + \text{root.data}$$

```
int sum (Node root)
{
    if (root == null) { return 0 }
    int ls = sum (root.left)
    int rs = sum (root.right)
    return ls+rs+root.data
}
```

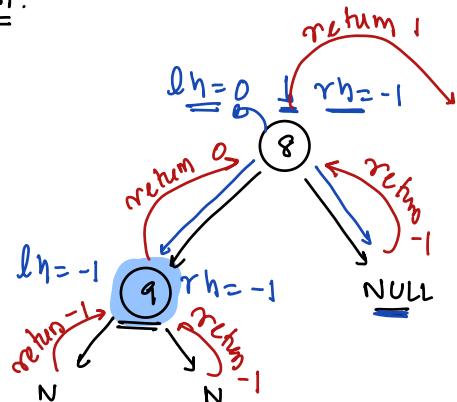


// Given root node, get height of node

```
int height(Node root){  
    if(root == null) { return -1 }  
    int lh = height(root.left)  
    int rh = height(root.right)  
    return max(lh, rh)+1
```

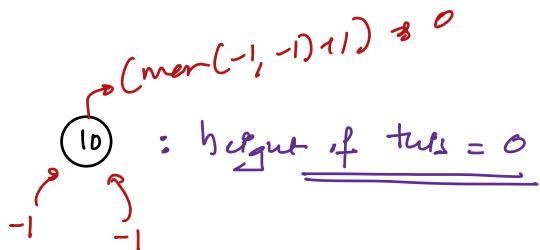


Ex:



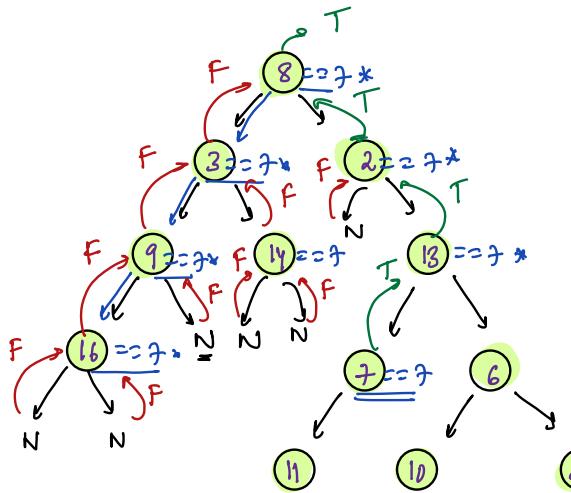
Issue: height of lead node = 0
but we are returning 1

Ex:



// Given BT & root node, all value are distinct, search for a

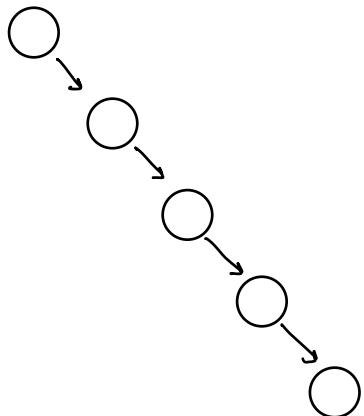
node with value = k., k=7 k=25



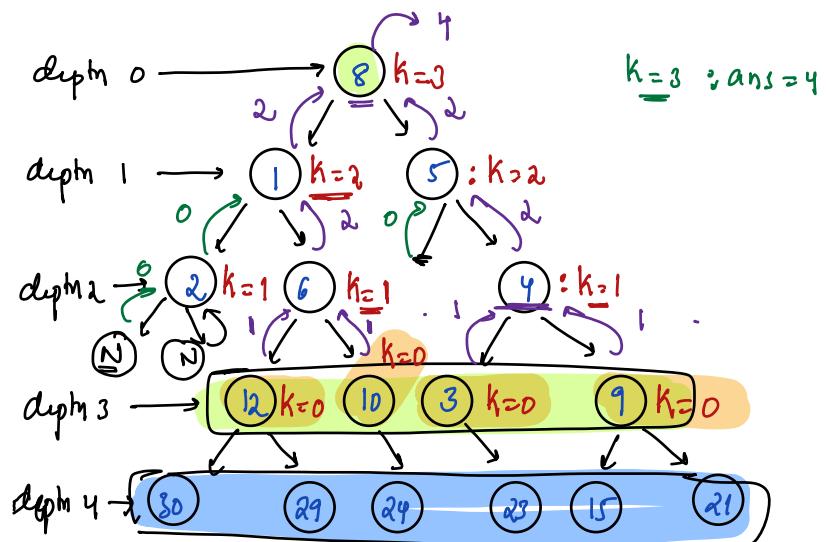
```
bool search(Node r, int k){  
    if(r==null){ return false }  
    if(r.data == k){ return true }  
    if( search(r.left, k) || search(r.right, k) )  
        return true  
    return false  
}
```

// If N node in tree, max height = (N-1)

N=5: h=4



// Given root node & k, calculate no. of nodes at depth k.



```
int countdepth(Node root, int k){
```

```
    if (root == null) { return 0; }
```

```
    if (k == 0) { return 1; }
```

```
    int l = countdepth(root.left, k-1);
```

```
    int r = countdepth(root.right, k-1);
```

```
    return l+r;
```

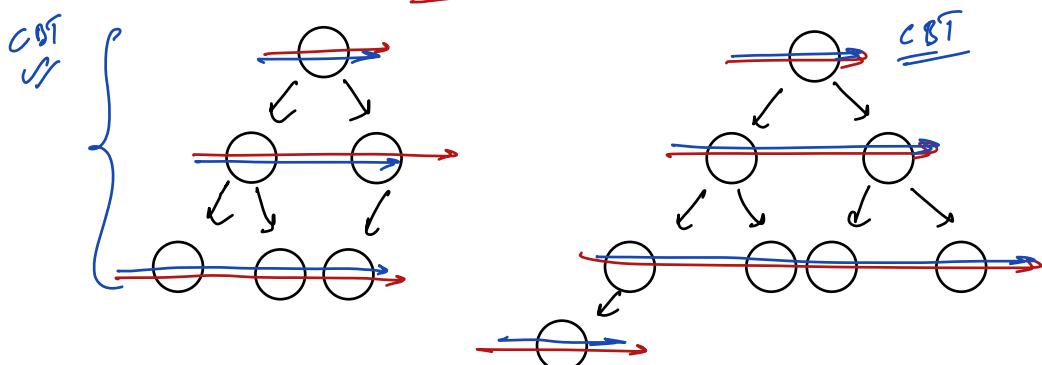
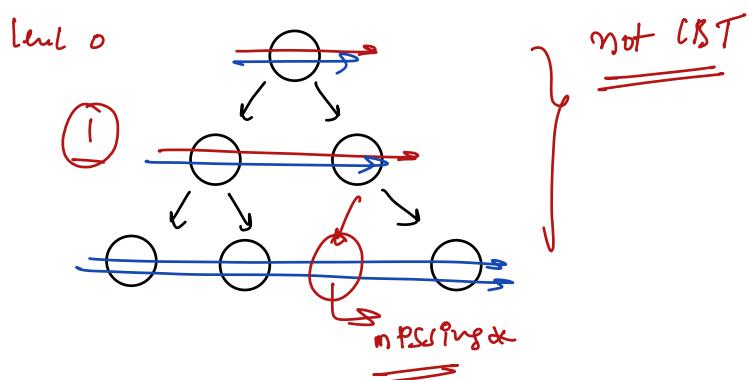
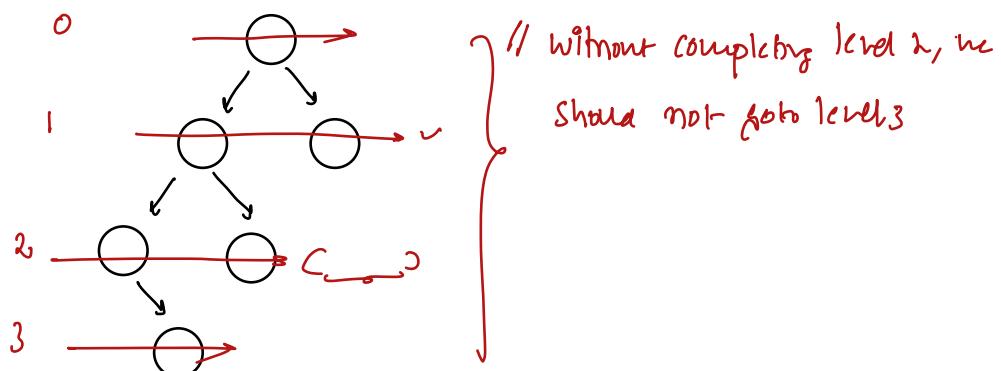
}

if (root == null) { return 0; } *node at depth k from root node*

CBT: Complete Binary Tree

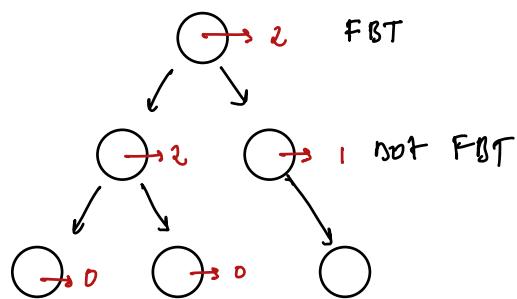
↳ BT as CBT

- a) Nodes should be filled level by level, until all nodes at current level are filled, don't go to next level, last level need not be complete
- b) Create nodes left → right in each level



→ FBT: (full Binary Tree)

↳ Every node has 0 or 2 child nodes



→

